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Collision-Free Asynchronous Multi-Channel Access in Ad Hoc Networks

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Abstract—In this paper, we present a collision-free asynchronous multi-channel access protocol for Ad Hoc wireless networks using a single transceiver. Our protocol, dubbed AM-MAC for Asynchronous Multi-channel Medium Access Control, targets low-cost, low-power deployments where nodes are equipped with a single transceiver. Other distinguishing features of AM-MAC include its simplicity and the fact that it does not require temporal synchronization among nodes. This is accomplished through an asynchronous split phase together with an observation phase as well as an unique handshake. Nodes observe the control channel for a period of time before asynchronously switching to the negotiated channel. Protocol correctness and collision-freedom in a multi-channel environment are verified. We also provide an analytical throughput assessment for our multichannel approach. Simulation results show that AM-MAC improves performance significantly when compared to IEEE 802.11. Our simulations also show that AM-MAC exhibits comparable performance to MMAC, a well-known multi-channel medium access control protocol, without the need for temporal synchronization.

I. INTRODUCTION

Bandwidth demand in wireless networks continues to rise as existing and emerging applications including multimedia streaming, emergency response and disaster rescue operations, smart environments, etc. become increasingly popular. As new physical layer technology (e.g., single-chip radios featuring advanced coding and modulation techniques) is able to sustain higher data rates, the fundamental limits challenging development and deployment of high data-rate, QoS-sensitive applications have been shifting from the Physical layer (PHY) to the medium access control (MAC) layer. Consequently, it is imperative to design efficient MAC techniques that will “expose” the underlying PHY’s data rates to the applications, yet keeping cost low. Low cost is especially critical in dense deployments in “extreme”, remote environments where nodes need to be disposable. Energy efficiency is another critical design requirement in such environment.

Since Gupta and Kumar[5] established the scalability limitations of wireless ad-hoc networks (MANETs) in terms of their capacity to carry point-to-point traffic, numerous research efforts have focused on proposing techniques to improve this fundamental limitation. A notable example is the work by Glossglauser and Tse[4] that shows that with mobility, constant throughput is achievable as the number of nodes increases. More recently, multi-packet reception and trans-

mission techniques have been proven to reverse the Gupta-Kumar scaling laws and effectively allow MANET capacity to increase as the number of nodes increases[3]. However, such techniques require multiple and more sophisticated radios, increasing cost and energy consumption considerably.

An alternative that is quite attractive given its cost-performance benefits is to make use of low-cost, low-power, widely available multi-channel radios. Indeed, while IEEE 802.11’s Distributed Coordinate Function (DCF) has been originally designed for one common channel, the IEEE 802.11 PHY offers multiple channels transmission capability. More recently, a number of multi-channel MAC protocols have been proposed as a way to increase performance and network utilization. However, transmission over multiple channels raise a number of challenges including hidden terminals over multiple channels and node synchronization. In fact, as described in Section II, which overviews related work in multi-channel MAC, many proposed multi-channel MAC protocols rely heavily on temporal synchronization

In this paper, we introduce the Asynchronous Multi-Channel Medium Access Control protocol, or AM-MAC for short, an asynchronous collision-free multi-channel medium-access control protocol. AM-MAC’s main features include its efficient utilization of the medium and energy efficiency without the need for time synchronization. Additionally, AM-MAC’s simplicity and ease of implementation makes it well suited for low-cost, limited-capability devices.

The rest of the paper is organized as follows. Section II reviews related work. Section III describes our protocol in detail. Section IV presents our simulation results while Section V presents our analytical throughput results. Finally, Section VI concludes the paper.

II. BACKGROUND AND RELATED WORK

Multi-channel MAC approaches can be classified into the following categories: dedicated control channel, split phase, common hopping, and parallel rendezvous. We will briefly describe each approach; for more details, we refer the reader to [8]

In the dedicated control channel approach, a channel is reserved exclusively for exchanging control information. Usually, a node is equipped with 2 radios, in which one is

solely used for control information exchange. For example, the DCA protocol [15] maintains a dedicated radio for control messages and the other for data transmission. Since each node has two transceivers, it can always monitor the control channel. The multi-channel hidden terminal problem simply does not exist in this case. However, an obvious drawback is the low spectrum utilization since one radio is reserved exclusively for control data exchange. Other drawbacks of the dedicated control channel approach include higher cost and energy consumption associated with equipping and operating nodes with two radios.

Split phase approaches avoid the need for multiple radios by having a dedicated common control channel and having nodes alternate between channel negotiation phases on the common channel and data transfer phases on the negotiated channels. This approach, however, requires tight time synchronization among all nodes in order to agree on when to switch between the control and data phases. Additionally, the control channel is under utilized as it is dedicated to control information exchange exclusively. Another drawback is that if a node missed the negotiation period or did not succeed contending during this period, it would have to wait until the next negotiation phase to contend again. A notable example of the split phase approach is the MMAC protocol [10]. Wiflex [6] is another multi-channel MAC that uses split phase, but does not require nodes to be synchronized. However, it does not guarantee collision-free transmission

Protocols that follow the common hopping approach have all idle nodes follow a common hopping sequence. A pair of nodes will stop hopping as soon as they agree on a hopping sequence to communicate; they will go back to hopping at the end of their exchange. CHMA[13] is an example of the common hopping approach. It eliminates the need for carrier sensing and code assignment by allowing the source-destination pair to agree and remain in the same hopping frequency in order to communicate. The main drawbacks are frequent channel switching and tight synchronization requirement.

Finally, following the parallel rendezvous approach, each node publishes its own channel hopping schedule. Senders learn their receiver's current hopping sequence via a seed broadcast mechanism. Senders, then, must adopt the published sequence if they want to increase the time spend on the channel with the receiver. The advantage is that there is no single channel bottleneck. This approach also does require tight synchronization. Examples include [8], [1]

From the previous discussion on the state-of-the-art of multi-channel MAC protocols, we note that most existing approaches require tight temporal synchronization among nodes and when that requirement is relaxed, collision-freedom cannot be guaranteed. AM-MAC provides an elegant and simple solution to achieving collision freedom without the need for temporal synchronization. The following section describes AM-MAC in detail.

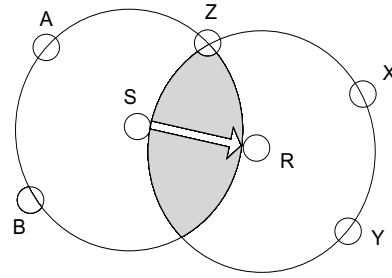


Fig. 1: Sender S and receiver R both send the ATS simultaneously. The shaded region shows the anticipated noise

III. AM-MAC PROTOCOL

We start by listing our design assumptions.

- Each node is equipped with a single transceiver such that it can either transmit or receive, but not both simultaneously
- A node's transceiver has N orthogonal channels of equal bandwidth; channel orthogonality means that simultaneous transmissions do not interfere with one another.

A. AM-MAC Handshake

For collision freedom (see Section 2), nodes must observe the control channel for a specified period of time. Then nodes interested in transmitting data engage in the handshake exchange described below.

We borrow the basic CSMA handshake mechanism and carrier sensing for channel negotiation. However, the regular RTS/CTS handshake is not sufficient to provide collision-free transmission. For example, consider the scenario in Figure 2. R sends a CTS to S after having received a request RTS from S 's; however X , hidden from S , begins to send a RTS to Y at the same time. X has no knowledge of R 's channel selection. Thus a collision in the data channel may occur.

In order to guarantee collision-freedom without the need for nodes to synchronize, we introduce the ATS (for Announce To Send) control frame. ATS is used to inform the sender's and receiver's neighbors of the ongoing transmission or data channel selection and, at the same time, serves as a jamming signal to prevent possible interference and to prevent hidden terminal problems.

Both sender and receiver need to broadcast the ATS simultaneously which acts like a busy-tone in order to broadcast channel selection information and prevent potential interfering neighbors. This strategy is similar to the work done in [12] using of a separate busy-tone channel. As for neighbors, they must adhere the to backoff rules stipulated by the control frame exchange. This is illustrated by the example in Figure 1 where both S and R transmit the ATS at the same time. Some neighbors of S , say A and B , can receive the ATS; the same applies to X and Y , neighbors of R . However, the mutual neighbor Z of S and R (in the shaded region) will only hear noise. Depending on the proximity of S and R transmission, this overlapping region may shrink or expand. On the sender side, ATS helps neighbors who have not heard the CTS to be

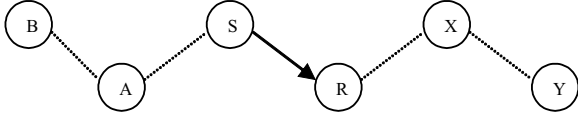


Fig. 2: Sender S and receiver R together with potential interferences from the neighbors

aware of the channel selection. Simply, the sender announce its intention twice, once through an RTS and once through an ATS. On the receiver side, the ATS acts like an extended CTS to announce the channel selection and jam any potential interfering nodes. In the following section, we will show that this unique handshake ensures collision-free data transmission with some additional conditions.

In summary, AM-MAC's control frames are:

- RTS (Request to Send): Used when a sender has data to send. We modified the RTS to contain some additional fields such as the available channel list, and data transfer time.
- CTS (Clear To Send): Used to acknowledge reception of the RTS. We introduce some additional fields, i.e., selected channel, and data transfer time.
- ATS (Announce To Send): Used to inform neighbors of the sender and receiver of the ongoing transmission and the data channel selection. It also acts as a jamming signal or a busy tone. Additional fields are: selected channel and data transfer time.

B. Collision free conditions for AM-MAC

Figure 2 illustrates possible cases of hidden terminal involving the source-destination pair S and R . Node A represents any neighbor of S that is hidden from R while node B represents any neighbor of A hidden from S but can cause collision at A and prevents A from following the conversation between S and R . Similarly, node X is a neighbor of R but is hidden from S and may cause collision at R . Node Y represents any neighbor of X that is hidden from R and can prevent X from following the conversation between S and R .

Let us also define the following notations:

- The maximum end-to-end propagation time in the channel is $\tau < \infty$.
- The transmission times of the RTS, CTS, and ATS are $\gamma, \gamma', \gamma''$, respectively; the transmission time of a data packet is δ ; the channel switching delay is ε , and $\gamma, \gamma', \gamma'' < \delta < \infty$

Theorem 1: AM-MAC provides correct data channel acquisition in the presence of hidden terminals, provided that $\gamma > \tau$ and $\gamma + 2\tau + \varepsilon < \gamma', \gamma'' < \infty$

Proof: Consider the illustration in Figure 2. For S to send data to R , S must first select a channel and receive a CTS from R confirming the use of the selected channel. Without loss of generality, assume that at time t_0 S sends an RTS to R . Because the channel has minimum propagation delay, any

neighbor of S must begin receiving the RTS at time $t_0^A > t_0$. If the RTS arrives at A with no errors, A must backoff for a period larger than $3\tau + \gamma' + \gamma''$ after receiving the RTS, or for a total time of $3\tau + \gamma + \gamma' + \gamma''$ after t_0^A . If the RTS arrives at A in error (e.g., because of possible interference from B), A must also back off for a period larger than $3\tau + \gamma' + \gamma''$ after receiving the RTS. It follows that the RTS sent by S at time t_0 forces any neighbor of S other than R to back off until time $t_1 > t_0 + \gamma + \gamma' + \gamma'' + 3\tau$.

If R receives the RTS from S in error, R will simply ignore or drop it. Assume that the RTS is received correctly at time t_2 . R must begin to reply with a CTS to S at time $t_2 \leq t_0 + \gamma + \tau$. Within one propagation delay, S receives the CTS from R at time $t_3 \leq t_2 + \gamma' + \tau = t_0 + \gamma + \gamma' + 2\tau$.

Because $t_1 > t_3$, any potential interfering neighbors of S must back off long enough for S to be able to receive CTS without collisions. S and R will begin their ATS broadcast at time $t_4 \leq t_3 + \gamma'' + \tau \leq t_0 + \gamma + \gamma' + \gamma'' + 3\tau$. Because $t_1 > t_4$, any potential interfering neighbors of S must back off long enough to allow the transmission of CTS or ATS. Otherwise, ATS transmission will jam any potential interfering neighbors and let them know of the channel selection.

As for the receiver side, any neighbor of R must begin receiving CTS at time $t_2^X > t_2$. If CTS from R arrives at X with no errors, X then must back off for a period of time greater than $3\tau + \gamma''$ after t_2^X . If R 's CTS arrives at X in error, X must also back off for a period greater than $3\tau + \gamma''$ after t_2^X . It follows that CTS sent by R at time t_2 forces X and any neighbor of R other than S to back off until $t_5 > t_2 + 3\tau + \gamma' + \gamma''$.

Because $t_5 > t_4$, it follows that any other potential interfering neighbors of R must back off long enough for the transmission CTS or ATS. They should hear at least either a CTS packet or a ATS packet. This is important because ATS and CTS carry the data channel selection information. Thus, any neighbor in the vicinity of S and R must have heard either CTS or ATS. On the receiver side, the transmission of CTS and ATS acts as a long CTS to jam any potential interferers in order to reserve the channel. ■

Having complete knowledge of channel selection is crucial to provide a collision free protocol. Nodes which just finished data transmission will often have no knowledge of the channel status. Thus, nodes must observe for the maximum data transmission time before initiating any request for transmission.

Let T_0 be the observation period before a node initiates a request in the common channel and T_{MAX} be the maximum data access allowed.

Theorem 2: Assuming a single collision domain network. If $T_0 \geq T_{MAX}$,

Then AM-MAC is collision free.

Proof: Consider a node A just coming back from the data channel, and a node B switching to the data channel simultaneously. Obviously, A and B are not aware of each others' activities. If node A has observed the common channel for T_0 period, node A will have complete knowledge of the channel selected by B since B 's data access is upper bounded

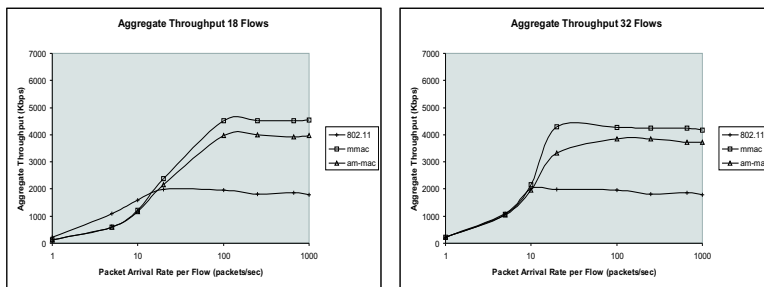


Fig. 3: Aggregate Throughput vs Packet Arrival Rate, in Fully Connected Mesh.

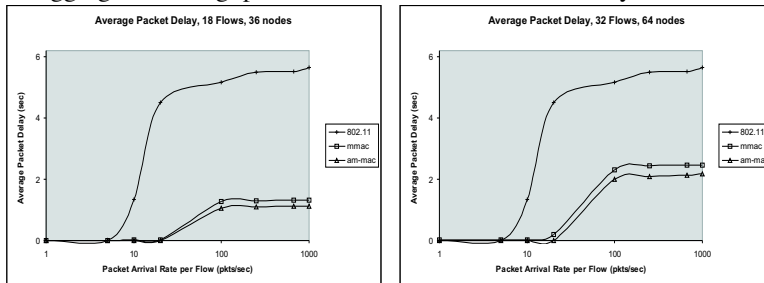


Fig. 4: Average Packet Delay vs Packet Arrival Rate, in Fully Connected Mesh.

by T_0 . If there is a collision, two things can happen. Either node A did not observe for a sufficient time T_0 or node B held onto the data channel for a time of $T_B > T_0$. This contradicts our assumptions that $T_0 \geq T_{MAX}$. ■

C. AM-MAC Operation

Having described all the basic mechanisms that form the core of AM-MAC, its complete operation is presented here. Suppose A has data destined for B and A gets access to the common channel, the procedures used by A and B is described as follows:

- 1) A transmits RTS to B , assuming A had already listened in the common channel for the required observation time.
- 2) B replies by sending a CTS to A . B starts a timer for the CTS so that upon its expiration, it will send the RTS.
- 3) On receiving the CTS, A updates its channel list and prepares to send RTS packet.
- 4) A and B begin broadcast RTS packet at the same time and switch to the negotiated channel.
- 5) A then begins sending data to B .
- 6) After data has been transmitted, A and B will go back to observing the channel for a full waiting period T_0 before transmitting or responding to a request.

As for any neighbors of A or B , they will observe the control channel and update their channel usage list accordingly.

IV. PERFORMANCE EVALUATION

We evaluate AM-MAC's performance through extensive simulations using the ns-2[14] network simulator with CMU's wireless extension[11]. We evaluate AM-MAC against IEEE 802.11 and MMAC. As performance metrics, we used aggregate throughput and average packet delay.

Throughput is calculated as the number of successful packets received multiplied by the packet length and divided by the total simulation time. Packet delay is calculated as the difference between the time a packet arrives at the queue and the time a packet gets transmitted successfully.

For our simulations, we used two network scenarios, namely a fully connected mesh and multi-hop topologies. In the fully connected mesh scenario, every node is within range of one another and is able to reach any destination in one hop. In the multi-hop scenarios, a packet may travel several hops before it reaches the destination.

A. Simulation Setup

Our simulation setup is based on MMAC's setup model because we consider our protocol a variant of MMAC protocol. The difference is that each node follows its own observation phase instead having a single control phase for all nodes. In our simulations, the bit rate for each channel is 3Mbps and the transmission range is set to 250m. Each source generates and transmits constant-bit rate traffic. We use 3 or 4 available channels depending on the scenarios, packet size of 512 bytes, drop-tail queues with maximum queue length of 50 packets, omnidirectional antenna, and TwoRayGround propagation model.

In the fully connected mesh scenario, every node is within each other's range (in ns2 we disable routing so that any node is reachable within one hop). We simulate two scenarios, one with 36 nodes and 18 concurrent flows and another with 64 nodes and 32 concurrent flows, in a 400x400m area. Nodes move according to the random waypoint model with speeds varying between 0 and 10m/s and with no pause. In each scenario, approximately half of the nodes are sources and half are destinations. All nodes begin transmission at the same

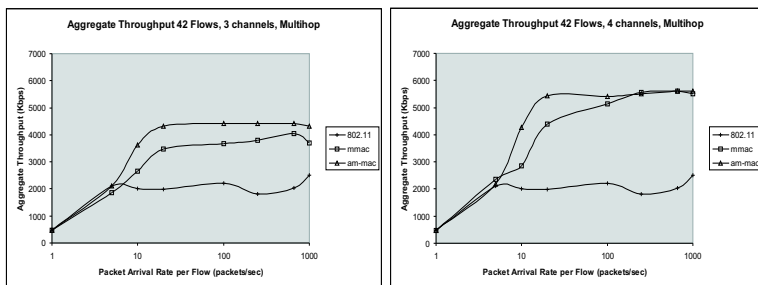


Fig. 5: Aggregate Throughput vs Packet Arrival Rate, Multi-hop.

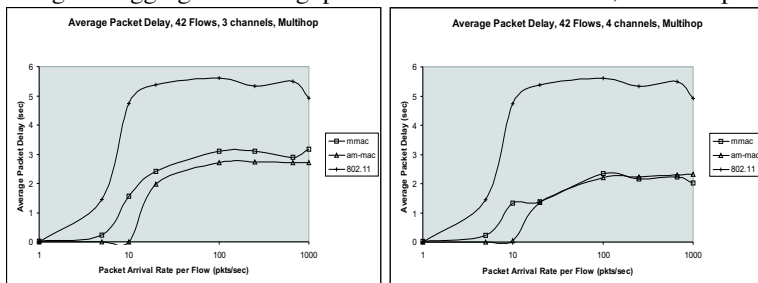


Fig. 6: Average Packet Delay vs Packet Arrival Rate, Multi-hop.

time.

In the multi-hop network scenario, 121 nodes are placed randomly in a 1000x1000m area. Sources and destinations are randomly selected such that a node may be the source for multiple destinations and a node maybe a destination for multiple sources. At any given point in time, 42 concurrent flows are active. Nodes move according to the random waypoint model with speeds varying between 0 and 10m/s with no pause time. For these simulations, we use 3 and 4 available channels.

B. Simulation Results

Figure 3 shows the aggregate throughput in the fully connected mesh scenarios. When the network load is low, all protocols have somewhat similar performance. When the network approaches saturation, AM-MAC performs significantly better than 802.11 and yields comparable performance to MMAC. Figure 3 shows similar performance behavior for a 64-node mesh with 32 concurrent flows. The significant gain in performance over IEEE 802.11 is mainly due to multi-channel transmission. multiple channels. In the fully-connected mesh environments, AM-MAC performs slightly lower than MMAC. This is because when a pair of nodes is negotiating for a channel, all nodes in the networks must delay their requests for data transmissions anyway. As a result, perfect synchronization seems to give MMAC a slight advantage in this environment.

Figure 4 shows the average packet delay in the fully connected mesh environment. When the number of contending nodes is moderate, AM-MAC has significantly better average packet delay than 802.11 and has similar performance to MMAC. The same result applies when we increase the number of contending nodes, flows, and packet arrival rate. We observe that increasing the number of contending nodes does adversely affect the average delay performance in all protocols. In any

case, AM-MAC achieves superior performance over IEEE 802.11 in terms of delay because of the additional channels.

Figure 5 shows simulation results for the multi-hop scenario. With 3 available channels, we vary the constant-bit rate traffic from low to very high. For low traffic loads, all protocols have similar performance. However, under moderate to high traffic load conditions, AM-MAC performs better than 802.11 and slightly better than MMAC in terms of aggregate throughput. We repeat the same experiment with 4 available channels, and notice a similar performance trend.

Average packet delay for all protocols in the multi-hop environment is shown in Figure 6. We again observe that AM-MAC obtains significantly better average packet delay than 802.11 and comparable performance to MMAC.

V. APPROXIMATE THROUGHPUT ANALYSIS

In this section, we present the approximate throughput analysis for our protocol using Markov chain. Our goal is to calculate the average throughput obtained by using multiple channels. To make the analysis tractable, we made the following assumptions about the networks

- A finite population of N nodes
- Arrival of RTS at each node is Poisson distributed with λ
- Traffic loads are identical among all nodes
- Network is fully connected, each node has the same number of neighbors
- Destination for each packet is chosen from a random uniform distribution
- Packet lengths are independent and geometrically distributed with probability q
- The arrival of RTS packets and the completion of data occurs as a single event

Let k be the number of channels currently in use, then, we have a total of $2k$ nodes in current transmissions and $(N - 2k)$ idle nodes. In this model the value of k is bounded by 0 and $\lfloor \frac{N}{2} \rfloor$

The arrival of RTS packet at any given state k is given by

$$\lambda_k = \lambda(N - 2k) \quad (1)$$

We are interested in the probability of success of RTS at any given state, k , in our Markov process. This probability is simply equal to the probability that no other RTS arrives during the vulnerability period and the intended destination node is currently listening on the common channel. For networks using carrier sensing with propagation delay τ . We obtain the following:

$$P_{S_k} = e^{-(\lambda_k)\tau} \left(\frac{(N-1) - 2k}{(N-1)} \right) \quad (2)$$

The probability that this RTS packet will result in a transition to the next state is

$$P_{T_k} = \lambda_k \cdot P_{S_k} \quad (3)$$

Then, transition probability for our markov model can be expressed as follow:

$$P_{ij} = \begin{cases} 0, & \text{if } j > i + 1; \\ (1 - q)^i P_{T_i}, & \text{if } j = i + 1; \\ q^{i-j+1} (1 - q)^{j-1} P_{T_i} \\ + q^{i-j} (1 - q)^j (1 - P_{T_i}), & \text{if } 0 < j \leq i; \end{cases} \quad (4)$$

The first condition makes sure that no more than one agreement can be made at any given time in the common channel. The second condition allows the Markov transition to move to the next state. It is the probability that none of the current data packet transmissions is yet finished, and there is a new data packet agreement. The third condition captures the probability that the state k may remain in the same state or go back to other previous states.

Setting up the systems of equations, we have:

$$\begin{aligned} \pi_0 P_{01} &= \pi_1 P_{10} + \pi_2 P_{20} + \pi_3 P_{30} + \dots + \pi_k P_{k0} \\ \pi_1 P_{10} + \pi_1 P_{12} &= \pi_0 P_{01} + \pi_2 P_{21} + \pi_3 P_{31} + \dots + \pi_k P_{k1} \\ \dots \\ \pi_i \left(\sum_{j=0}^k \& \& j \neq i P_{ij} \right) &= \pi_{i-1} P_{(i-1)i} + \sum_{j=i+1}^k \pi_j P_{ji} \end{aligned}$$

This becomes a system of n equations and n unknowns, and can be easily solved, knowing $\sum_{i=0}^k \pi_i = 1$

The average data utilization is the average number of channels sending data

$$E[k] = \sum_{i=0}^k i \cdot \pi_i \quad (5)$$

Since we assume that the traffic is uniformly distributed across all stations, the average capacity per node is simply

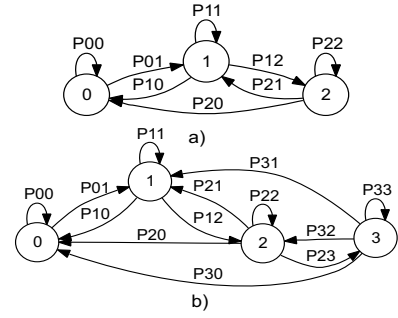


Fig. 7: The Markov chain state for a)3 channels b)4 channels

$E[k]/N$. And the average utilization per channel is $E[k]/k$. Note, we may need to take into account of the channel capacity for the throughput calculations.

As for a fixed packet length, we use the well-known birth and death Markov process to simplify our Markov model above. Basically, completion of data transmission is sequential, not simultaneous. At any given instant, only one data packet may depart. We assume the data service time has the inter-arrival times of Poisson arrivals, or exponentially distributed.

The rate of arrival of successful RTS packets that results in the transition forward to a new state is simply P_{T_k} , see (3).

The rate of departure for data packets at a given state (1/average service time)

$$\mu_k = k \cdot 1/\delta$$

Let us define the ratio of arrival and departure to be $r_k = P_{T_{k-1}}/\mu_k$ and $R_k = r_k r_{k-1} \dots r_1$ and $R_0 = 1$. Then π_0 can easily be found from:

$$1 = \left(\sum_{j=0}^k R_j \right) \pi_0$$

Then, the stationary probability [7] is given by

$$\pi_i = \frac{R_i}{\sum_{j=0}^k R_j} \quad (6)$$

Having found the probability of being in a particular state of the Markov process, we can proceed to find $E[k]$ and throughput of the system. The analytical results for AM-MAC are shown in Figure 8.

VI. CONCLUSION

In this paper we presented AM-MAC a novel solution to multi-channel medium access for single-transceiver nodes. AM-MAC employs a simple, yet efficient approach to collision-free data transmission over multiple channels without the need of temporal synchronization among nodes. Our simulation results show that AM-MAC significantly improves performance when compared against IEEE 802.11, and comparable performance to MMAC [10], which requires synchronization.

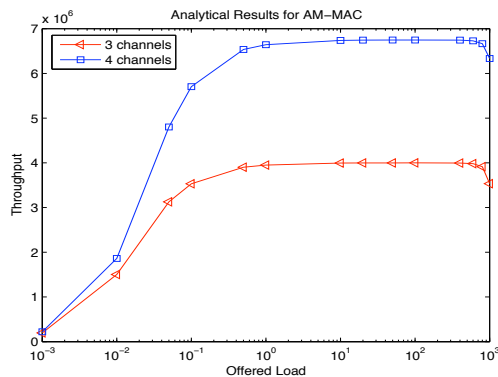


Fig. 8: Analytical Results

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