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JOURNAL OF PHYSICAL OCEANOGRAPHY

## **Observations of shoaling density current regime changes in internal wave interactions**

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## ABSTRACT

We present in-situ and remote observations of a Mississippi plume front in the Louisiana bight. The plume propagated freely across the bight, rather than as a coastal current. The observed cross-front circulation pattern is typical of density currents, as are the small width ( $\approx 100m$ ) of the plume front, and the presence of surface frontal convergence. A comparison of observations with stratified density current theory is conducted. Additionally, subcritical to supercritical transitions of frontal propagation speed relative to Internal-Gravity wave (IGW) speed are demonstrated to occur. That is in part due to IGW speed reductions due to decreasing bottom depths as the front approaches the shore. Theoretical steady state density current propagation speed is in good agreement with the observations in the critical and supercritical regimes but not in the inherently unsteady subcritical regime. The latter may be due to interaction of IGW with the front, an effect previously demonstrated only in laboratory and numerical experiments. In the critical regime, finite-amplitude IGWs form and remain locked to the front. A critical to supercritical transition eventually occurs as the ambient conditions change in frontal propagation, after which IGWs are not supported at the front. The subcritical (critical) to critical (supercritical) transition is related to Froude number ahead (under) the front, consistently with theory. Finally, we find that the front-locked IGW (critical) regime is itself dependent on significant nonlinear speed enhancement of the IGW by their growth to finite amplitude at the front.

### 1. Introduction

Salinity and temperature fronts are a common occurrence in coastal regions where rivers and other waterways outflow. The corresponding high horizontal density gradients result in a baroclinic horizontal pressure gradient force (HPGF), which can strongly influence the dynamics and circulation in the shelf and beyond. Several circulation patterns of the buoyant outflow typically emerge. The first is a geostrophic along-shore density current that is typically prograde, i.e., in the direction of a Kelvin wave. The second pattern is a cyclostrophiclly-balanced buoyant bulge with anticyclonic circulation around the outflow (Horner-Devine et al. 2015). The bulge does not tend to propagate, but may repeatedly grow and breakup (Yankovsky and Chapman 1997; Horner-Devine 2009). A third circulation pattern is transient density currents, with fronts of width from meters to kilometers in scale. Here we refer to free (rather than traveling along-coast) density currents, i.e., a nonlinear flow pattern, where the HPGF is balanced mainly by advection. Free density currents may form when the outflow flux variability is high enough, such as in strongly tidal conditions (Horner-Devine et al. 2009); or where salinity anomalies are high enough to force direct propagation even from slow, balanced, initial conditions (Sarkar et al. 2016; Warner et al. 2018; Pham and Sarkar 2018).

Density current theory is well developed and supported by decades of extensive laboratory measurements and numerical modeling (Simpson 1997; Ungarish 2009; Griffiths 1986). For times short enough compared with an inertial day (Gill 1982), the Coriolis force may be neglected. The circulation is then predominantly in the cross-frontal

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direction, towards the denser side at the surface, with a return flow at depth (in case of a buoyant surface anomaly rather than a deep dense anomaly). Another salient feature is then a "head-wave", of elevated mixing, which forms under the surface front. Benjamin (1968) derived an analytical solution for the propagation speed of a homogeneous density current moving relative to a homogeneous ambient, depending on the density difference, layer thickness, and head loss. Benjamin's theory was extended allow for entrainment in a semi-empirical manner by Britter and Simpson (1978), who also largely confirmed the framework in careful lab experiments.

Since Benjamin's work, theoretical density current models accounting for stratified conditions (Ungarish 2006, 2009, 2012) were developed. Stratification generally changes the propagation speeds of DCs, and additionally a stratified ambient supports internal gravity waves (IGW). These can be excited at the front; be trapped by it, while possibly growing in amplitude and finally emitted (Nash and Moum 2005; White and Helfrich 2008; Kilcher and Nash 2010; White and Helfrich 2012); Frontal emission of IGWs can drain large fractions of density current energy (Pan and Jay 2009; White and Helfrich 2012); Finally, interactions between the IGW and density current may also slow down the latter periodically (Maxworthy et al. 2002; Goldman et al. 2014).

Several comparisons of density current observations with theory were previously conducted (Luketina and Imberger 1987; Marmorino and Trump 2000; O'Donnell 2010). These observations were within weakly stratified ambients, and compared favorably with classical (unstratified layers) density current theory. Here we present measurements taken around a propagating Mississippi plume front in stratified conditions within the Louisiana Bight, and present a comparison with stratified density current theory.

The Mississippi outflow plume differs from most of the plume front areas studied observationally in recent years (Garvine and Monk 1974; Luketina and Imberger 1987; O'Donnell et al. 1998; Orton and Jay 2005; Horner-Devine et al. 2009; O'Donnell 2010; Kilcher and Nash 2010) on account of the combination of strong stratification, weak tides, and large discharge rate (largest annual mean discharge rate in the United States) (Walker et al. 2005). The main contribution to the study of the smaller frontal scales on the bight was made by Wright and Coleman (1971), who concentrated mainly on the mixing and initial expansion at exits of the Mississippi channel. Since then, most studies of the dynamics of the Mississippi plume on the bight have concentrated on the larger scales of the plume, and the effects of wind on formation of the coastal current and outflow bulge (e.g., Rouse 1998; Walker et al. 2005; Schiller et al. 2011; Androulidakis et al. 2015). In contrast, we focus on characterization of the frontal circulation of a free density current

in the far-field away from the outflow, and (to a lesser extent) the larger scale ambient circulation it is embedded within.

Our measurements were conducted in early May 2017 during the SPLASH campaign (http://carthe.org/splash/). The front was observed during two consecutive days of airplane sea surface temperature (SST) measurements and satellite imagery, and was sampled in situ repeatedly using a number of platforms and instruments during a 8-hour period. The rest of the paper is structured as follows: in section 2 we present the measurements taken, auxiliary data sets, and data processing methods. The frontal propagation and surface velocity field are first described in section 3a, based mainly on drifter observations and remote sensing. In section 3b, the density structure across the front is analyzed, based mainly on a novel towed instrument array. In section 3c sections of full-depth velocity measurements are used to separately characterize the small-scale frontal circulation pattern, and a larger ambient circulation. In section 4a we conduct comparisons of the frontal propagation speed with stratified density current theory. The presence of IGW and their possible interaction with the front are examined in section 4b. A summary and discussion are given in section 5.

### 2. Data and Methods

During May 1st-2nd, 2017, in-situ and remote observations were taken of a propagating salinity front in the Louisiana bight. Two small, fast boats were used for in situ measurements and deployments of drifters, the UCLA Kodiak and RSMAS Argus. The front was located using aerial SST observations (section 2d) during the preceding nighttime (Fig. 1a). An animation (SA1) of trajectories of the vessels and drifters is accessible in the supplementary material.

Between 11:00 and 12:00, the Argus deployed 25 CARTHE drifters (section 2a) in an approximate radiator pattern, at  $\approx 500$  m intervals. Following that, the Argus took CTD casts on both sides of the front (section 2c). Since the front propagated shoreward at relatively high speed (section 3a), the general sampling strategy employed by the Kodiak was to cross the front in a given direction, drive for about 7 minutes, turn back, return to the front, and repeat in the opposite direction. This completed one cycle, or two sections. A total of 15 sections were taken by the Kodiak between 11:30 and 15:30, about 500 meters away from the front to each side. The front was easily identified visually by a line (henceforth, frontal foam-line) of buoyant material and foam, co-located with a peak in horizontal gradient of sea surface salinity. During the sections the Kodiak took continuous measurements along its path. These included a towed instrument array continuously sampling the temperature and salinity down

to 9 meters depth while driving (section 2c); and a boatmounted ADCP (section 2b).

Due to the advection of dynamic and tracer fields by the front, it is convenient to present data in a co-frontal coordinate system, (x, y), where y is cross front and pointing towards the saline side, and x points along-front 90° to the right of y. The fluid velocity components in the x and y directions are denoted by u and v, respectively. The x dependency of variables is generally suppressed, since little systematic change or variations are observed along-front over the duration of our observations.

The orientation of the frontal coordinates is taken as constant in time and space, which is found to be a very good approximation (section 3). Therefore, knowledge of the location of a single point on the front at any given time is sufficient, together with the orientation angle, to determine the frontal line. The location of such a point is identified in one of two ways. For Kodiak-based sections, maximal sea surface salinity gradient is a natural identifier of frontal crossings due to the narrowness and amplitude of the signal. Comparison with a few records of times of foam-line crossings in the ship log confirm this identification method. A linear interpolation in time between two adjacent Kodiak frontal crossing positions approximately identifies the instantaneous position of a point on the front. For CARTHE drifter measurements, the needed frontal point is taken as the position of drifter 5 (i.e., the third deployed, see animation SA1), since it was deployed near the front and represents its velocity well (section 3a.

All data are presented in Central Daylight time (CDT). Many measurements are presented as composites, or means, in 3 different periods: 11:00-12:30, 12:30-13:30, and 13:30-15:00. These will be denoted by periods 1, 2, and 3, respectively. A composite is computed by binning a variable within each individual section in 5 *m* cross-front intervals. The following subsections each present the specifications and methodologies for each of the main instruments used. Mean positions and seabed depths at the plume front boat crossings in each period are given in appendix A. For context, meteorological conditions are reported in the supplementary material.

### a. Surface drifters

CARTHE drifters (Novelli et al. 2017) follow the average currents over the top  $50 - 60 \ cm$  of the ocean. The drifters are designed to minimize Stokes drift, as well as windage effects. A Spot Trace GPS unit is installed on each drifter to track its trajectory, so water velocities and other properties may be calculated. The positions are reported at approximate 5 minute intervals, with  $\approx 5 \ m$  accuracy (figure 1 in Novelli et al. 2017).

Twenty-five drifters were deployed in a  $5 \times 5$  grid, with 500 *m* spacing in the zonal and meridional directions. Drifter numbers in the text relate to deployment positions

as follows: 1 is the southwest-most drifter, 2-5 deployed sequentially to its north, 6 the next one east of 5, 7-10 sequentially south of 6, etc.

#### b. Boat-mounted ADCP

The Kodiak was equipped with a Nortek Signature 1000 ADCP. Four of the ADCP's five beams were used, with the maximal possible acquisition rate, 16 Hz. A hydrofoil was fitted around the instrument to reduce turbulence and bubble formation in front of the transducers. The ADCP was mounted from the side of the boat, such that the transducers were at a mean depth of about 30 cm underwater. A bin size of 25 cm was used, and the blanking distance was  $10 \, cm$ . Maximal range  $(30 \, m)$  was deeper than the sea floor in the observations. The seafloor depth is detected offline as well by the vertical maximum in 4-beam-mean echoamplitude, and then running-median with 10 sample width is applied to the bottom depth. The bottom 15% of depth bins are removed to avoid data contaminated by sidelobeinterference (RD Instruments 1996). The top ADCP bin is at 0.5 m depth.

Heading corrections were applied, following a calibration, from the boat dual GPS antenna. The ADCP (GPS) data were nominally low passed filtered using a second order Chebyshev type 2 filter, with a cutoff period of 4 (8) seconds, and 20 dB stopband attenuation relative to passband. Depth-independent signals, indicative of sudden boat movements, were additionally filtered by the following procedure. A depth averaged velocity was calculated, and a low-pass-filtered version of it calculated by applying a Loess filter of span 200 *m*. Then the unfiltered depth-average flow was removed (subtracted) from the total signal, and the low-pass-filtered series added to it instead. After filtering, composites for periods 1-3 were computed (section 2). Finally, the depth-average flow filtering was repeated on the composited data.

### c. Towed Instrument Array (TIA)

A towed instrument array (TIA) was designed (manuscript in preparation, Solodoch et al 2019) to allow deployment from a small boat. Each of the array's loggers measure temperature (T) and/or salinity (S) and/or depth (pressure in fact, P). They are connected to a metal wire at regular intervals. The wire is towed behind the boat, and a hydrofoil supplying negative lift is connected to the bottom of the wire. The momentarily depth of a logger is determined by its pressure reading, with a typical error of 0.01 m. Depth of loggers not equipped with pressure sensors is determined by linear interpolation of depth loggers above and below them, or by extrapolation if there are no pressure loggers in one direction. Modeling and observations (Solodoch et al 2019, manuscript in preparation) show that the change of line angle with depth is smooth enough to make the depth error associated with linear interpolation (extrapolation with 1 *m*-far neighbor) of depth for the configuration used in the present observations quite small, 0.035 (0.05) m.

During the May 2nd observations the TIA line was stacked with 10 loggers, at intervals of 1 m. Five of the loggers were RBR model TDR-2050, which have P (0.01 m) and T (0.002° C) sensors, and the other five were JFE model Infinity-A7CT, which have T (0.01° C) and S (0.01 psu) sensors. Numbers in parentheses denote instrumental measurement accuracy. The S sensors are in fact conductivity sensors of course, and the salinity accuracy given here takes into account the inaccuracies in temperature and conductivity together, and their influence on salinity inaccuracy for the measured range of values. These two types of loggers (TS and TP) were layed out on the line in an interleaving manner, with a TS logger on top, a TP logger second, a TS logger following it in the third position, etc.

The Kodiak is additionally fitted with an intake system, which continuously provides near-surface water to a SBE45 MicroTSG Thermosalinograph, measuring near sea-surface salinity (SSS) and SST to accuracy of  $0.005 \, psu$  and  $0.002^{\circ} \, C$ , respectively. The surface sampler is treated as another TIA data point, at a depth of  $0.3 \, m$ , which is an estimate of the pump intake depth. Composites of TIA data are created as described in section 2, after linear interpolation vertically between loggers.

Vertical CTD sections taken on both sides of the front, with vertical resolution as fine as 0.1 m, confirm that no persistent patterns are missed by TIA measurements due to its lower vertical resolution. That includes (section 3b) the approximate linear stratification within the shallow plume layer, as well as the relatively well-mixed or homogeneous shallow layer outside the plume.

### d. Remote Sensing

Aerial and satellite based imagery are used to determine the large scale motion of river plume across the bight. The plume front is recognized in the imagery by a strong SST gradient, or by color intensity gradients in the RGB and ERGB images. The latter contrast is presumably due to elevated sediment or dissolved material concentration.

Aerial SST images were taken from a Parthanavia P86 airplane equipped with an infrared imaging system during the SPLASH campaign. Multiple flight tracks, obtained while flying in a raster pattern, were combined to create composite SST maps covering areas of about 50km x 50km with 5m resolution. Each raster pattern was acquired during 4-6 hours of flight, and therefore the time displayed in plane-derived SST figures in this paper corresponds to one specific point chosen for a reference point of interest in each image. Further information regarding the airplane instrument package and data processing, as used in the previous LASER campaign, is given in Rascle et al. (2017); D'Asaro et al. (2018).

Satellite Red-Green Blue (RGB) images and enhanced RGB images (ERGB), based on VIIRS and MODIS satellite data, were provided courtesy of the University of South Florida Optical Oceanography Lab (https://optics.marine.usf.edu). These included MODIS Terra 11:55, VIIRS 13:06, MODIS Aqua 13:25, and VI-IRS 14:48 overpasses.

#### 3. Results

#### a. Plume propagation and surface circulation

During the nighttime before May 2, 2017 a SST front was identified in the Louisiana bight using the airborne infrared imaging system (Fig. 1b). A coarser resolution, MODIS-Aqua SST image from earlier that night is shown as well. The two consistent SST patterns suggest the cold anomaly in the center and east of the bight is due to the Mississippi river discharge plume, as later confirmed in situ by its low salinity. The Mississippi outflow is often colder than the ambient water it drains into (Walker et al. 2005).

The May 2nd daytime plane and satellite imagery, taken between 11:55 to 18:00 (as detailed in section 2d), show westward propagation of the front occurred between each pair of overpasses during this time. Imagery from 13:06 and 18:00 is shown in Fig. 1. The difference between the frontal locations in temporally-consecutive imagery may be used to estimate the frontal velocity component in the cross-front direction,  $0.7 \pm 0.05 \ m/s$  between 11:55-14:48. In its motion, the front aligned with and coherently approached the western bight shoreline. The front appears quite straight over its > 20 km length on this north-western side, as quantified below.

The drifters were deployed either on the plume side of the front up to 4 km away from it, or no more than 100 mfrom it on the saline side. Their motions are representative of surface circulation (section 2a). All drifters converged towards the front in time. That may be seen from the drifters trajectories overlayed on the remote imagery (Fig. 1), or from the animation in the supplementary material. A few drifters seen in the figure as trailing the front were in fact retrieved from the front foam line slightly earlier than the imagery time. Drifters that were not retrieved continued the shoreward propagation (not shown), and got caught in a coastal current after reaching a distance of around 2 km from the coastline. These eventually beached sometime during the nighttime.

The positions, in the frontal reference frame (section 2), of the CARTHE drifters right after their deployment (12:03), and again just before commencement of retrieval (16:24) are shown in Fig. 2a. The figure suggests high horizontal convergence and/or strain values were sustained up to a distance of at least  $\approx 4 \ km$  from the front. Thirteen

21

20.5

[°C]

21.5

22





FIG. 1. Satellite and plane imagery. (a,c) SST [ $^{\circ}C$ ] (in color) imagery from the UCLA plane. Acquisition times are indicated in each title, but each panel is a mosaic of images taken over several continuous flights hours. The indicated time in panel a (c), 04:00 (18:00), corresponds to the location of the green square (diamond) marker. The green square in (a) also represents the deployment position of CARTHE drifters on May 2nd. In panel (a), SST contours from an earlier (2:30 am of same day) MODIS-Aqua overpass are superimposed. In (c), the 12:00-18:15 trajectories of drifters deployed near the front are shown in solid black lines. Bathymetric depth is marked by dashed line in (c), between 10 and 100 m, at 10 m intervals, as well as the 150 and 200 m isobaths. The coastline is shown in a thick black line. The main outflow to the Louisiana bight occurs at the Southwest Pass, the elongated landmass just north of the 28.9 latitude tick mark on the east boundary of each panel. (b) Enhanced RGB image processed from VIIRS satellite May 2nd 13:06 overpass data. ERGB color intensity (not related to colorbar) is generally expected to grow with surface sediment concentration.

drifters which were initially closer to the front (marked with filled symbols) converged to a (frontal) line. Indeed, these drifters were shortly after picked up from the frontal foam-line (between 16:30 and 18:00). Based on animation SA1, the relative deformation and near convergence to a frontal line of these 13 drifters has mostly concluded before 16:24.

19

19.5

20

To estimate the frontal angle on the horizontal plane, the linear least-square fit to the positions of these 13 CARTHE drifters is computed (blue line in Fig. 2a). Additionally plotted in Fig. 2a are the frontal crossings of both vessels, in the moving frontal coordinate frame (section 2). The root-mean-square deviation from the line considering both CARTHE drifters and boat-crossings is 120 *m*, and the median absolute deviation is 70 *m*, over the sampled frontal length  $\approx 6 \text{ km}$ . The line fit suggests a frontal orientation angle of 28.7° anti-clockwise to east. Similar fits done on drifter positions 1 or 2 hours earlier are quite similar and return angles different by up to 5°, although fewer drifters were on the front at these earlier hours.

Plane SST imagery (in higher magnification then displayed here) also shows that the undulations in the front are mostly smaller than 100 m in the area of deployment of the drifters. The imagery shows that the frontal orientation along its 20 km long north-west face (detected using a maximal gradient method) is very similar to that found

from the in situ measurements here. For example, in the VIIRS 14:48 overpass, the orientation is  $\approx 29^{\circ}$ . These observations support the assumption of along-frontal homogeneity. Henceforth, the frontal angle value we use in calculations is the one quoted above.

The distribution of surface velocity within the plume can be investigated through the drifter motions. The crossfront velocity component of several drifters are plotted against time in Fig. 2b. Between 11:55-14:48 the crossfrontal velocity of drifter 5, which was seeded on the frontal line, is  $0.72 \pm 0.03 \ m/s$ . That is similar to the velocity estimated (above) from the remote imagery over the same time window. An along-front velocity of similar or slightly smaller magnitude than the across-front component occurs as well (not shown), consistent with the clockwise turning of the drifter trajectories (Fig. 1c).

As seen in Fig. 2b, drifters experience "sudden" (15-20 minutes long) cross-frontal deceleration events, in which their cross-frontal velocity reduces by  $0.1 - 0.2 m/s^1$ . Examination of the spatial trajectories (animation SA1, supplemental material) of individual drifters shows these decelerations occur as the drifter is converging to and aligning with the plume front. Indeed, during a deceleration event, the velocity of a drifter approaches that of

<sup>&</sup>lt;sup>1</sup>1. Results for drifters not shown in figure 2b are similar. 2. Similar decelerations do not occur in drifter along-front velocities



FIG. 2. (a) Position of CARTHE drifters relative to the moving front after deployment (black squares) at 12:03, and just before retrieval began, at 16:24 (red diamonds). Drifters which eventually reached the front are color-filled. Note that what appears like a slightly thicker red diamond at coordinates origin is in fact 4 very close solid diamonds and a solid square. Approximate frontal line (see text) shown in blue. All frontal crossings of both boats are marked in circles color-coded for frontal crossing time. The positions of all crossings were propagated to 16:24 (see text) with the velocity of the closest drifter. (b) Cross-front velocity of individual CARTHE drifters (drifter number given in legend). Drifter 5, which was seeded on the frontal foam line, is shown in a thick black line.

drifter 5, and later remains close to it. Thus a convergence field is established within the plume and towards the front with overtaking velocity (Britter and Simpson 1978)  $0.1 - 0.2 \ m/s$  from the plume interior towards the plume front.

We observe (Fig. 2b) that the velocity in the crossfrontal direction within the plume decreases significantly towards the beginning of the in-situ observation. That is consistent with the presence of the front in the same location it was observed from plane imagery during the night (Fig. 1), as well as with frontal speed estimated prior to 11:00 from early frontal crossings (not shown). In the rest of the manuscript we focus on the frontal circulation relative to the ambient circulation ahead of the plume rather than on the ambient circulation (and absolute plume velocity), its acceleration, and its forcing mechanism. The latter subjects need be addressed in a future study.

### b. Frontal thermohaline structure

Figure 3 shows composites (see section 2) of SST and SSS along the cross-front axis, using measurements from the Kodiak's surface sampler and GPS. The SSS composites change by about 6 *psu* across the front, over a distance of about 100 m. The mean width is 70 (110) m for the center 60% (80%) of the salinity variation. Other fronts with density gradients as strong or stronger were observed during SPLASH and are not unusual in this area, due to the strong influx of fresh water from the Mississippi river. Away ( $\geq 100 m$ ) from the front, SSS is approximately uniform in space and changes mostly in time. The horizontal difference of SSS across the front decays during the course of the day from 8 to  $\sim 4 psu$ . In terms of effect on density, the salinity variations are dominant, causing a density change of approximately 5  $kg/m^3$  across the front, while temperature variations cause a smaller density change of order 0.1  $kg/m^3$  across the front.

SST increases with time faster on the fresh side, which is colder (warmer) early (late) in the day, compared with the salty side. That is consistent with the plane SST data (section 3a). The effect is likely due to a reduction in vertical mixing at the base of the plume (aka barrier layer) due to higher stratification, relative to the ambient. For a related discussion of barrier layer effects in fresh water plumes, see Mahadevan et al. (2016).

In Fig. 4 we present TIA composites for periods 1-3 (section 2c). The cross-front density structure is seen to be reminiscent of a density current, especially during periods 1-2. On the plume side, a buoyant surface layer terminates abruptly at a depth of  $\approx 2$  m; Its density is clearly distinguished from that of the fluid across the narrow ( $\approx 100$  m) front; At the front, isopycnals dip in a structure visually similar to a density current head-wave (Simpson 1997), in which typically enhanced mixing and entrainment occur. The isopycanl dipping is in our case associated with internal waves occurring at the front as well, at least during period 2 (section 4).

Unlike many previous observations and modeling studies, the plume occurs in a strongly stratified environment. The fluid is stably stratified, and similarly so on both sides of the front beneath  $\approx 3 m$  depth. The buoyant plume is itself also stratified, and limited to the top  $\approx 2 m$ . The mean vertical density (salinity) difference is about  $4 kg/m^3 (5.5 psu)$  at the observed depth range on the saline side, a similar magnitude to to the horizontal difference across the front at the surface.

Temperature is negligible relative to salinity in determining the density variations at depth as well. The maximal vertical temperature differences grow from 0.7 in early sections to  $1.7^{\circ}$  C later in the day. Hence the increase in density due to temperature drop with depth is no more than  $\approx 0.5 kg/m^3$ .

A gradual freshening of the layer immediately beneath the original plume occurs over time, possibly due to verti-



FIG. 3. Composites of (a) sea-surface salinity and (b) sea-surface temperature (SST), vs cross-frontal distance binned at 5 *m* intervals. Each color represents a composite over a different period. Periods 1-3 correspond to 11:00-12:30, 12:30-13:30, and 13:30-15:00, respectively.

cal mixing. A more dramatic evolution occurred in period 3 as the entire observed water column freshens up. Due to the strong vertical shear of velocity (section 3c), material at depth originates further west relative to material at the surface. The freshening at depth may thus be the result of a previous freshening of the western ambient, e.g., by a bottom-attached coastal current (Yankovsky and Chapman 1997).

### c. Frontal velocity structure

Horizontal velocity data was obtained from both the boat-mounted ADCP (section 2). A second downward-looking ADCP was attached to a drifting buoy and deployed on the frontal foam-line at 13:30; comparison was conducted with the boat-mounted ADCP measurements in the vicinity ( $\pm 50 m$ ) of the front. The instruments show excellent agreement in pattern and amplitude of the velocity profile considering that they were not co-located. Therefore velocity data is presented based on the boat-mounted ADCP measurements alone.

The surface velocity from drifters (section 3a) showed velocity approximately homogeneous up to 4 km away from the front on the plume side. Therefore we decompose the depth-dependent flow field u as the sum of a reference velocity U = (U, V) independent of horizontal position, and a relative velocity  $\underline{u'} = (u', v')$ , i.e.,  $\underline{u}(y, z, t) =$ U(z,t) + u'(y,z,t). The reference velocity field is defined at each depth as the average of the measured velocity on the saline side between a distance of 100-500 m from the front. As discussed before, we assume along-frontal homogeneity. The usefulness of the decomposition is clearly seen in Fig. 5: (1) the magnitude of the reference velocity U is significantly larger than the u' magnitude in most areas. (2) The relative velocity displays a clear frontal structure in its cross-front component v', i.e., variation over a short distance across the front, as further discussed below. Therefore the introduced decomposition may be understood effectively as a decomposition to a frontal-scale circulation component  $\underline{u'}$  and a larger-scale circulation component  $\underline{U}$ .

The  $\underline{U}$  magnitude and direction near the surface are similar to the velocity of the deployed drifters (section 3a). The reference cross-frontal velocity is towards (away from) the saline side in the upper (lower)  $\approx 10$  m. A significant O(0.5m/s) along-front reference velocity component exists. Given the observed density field, a direct evaluation of the Thermal Wind equation (Gill 1982),

$$\frac{\partial u}{\partial z} = \frac{g}{f\rho} \frac{\partial \rho}{\partial y},\tag{1}$$

predicts at the plume depths (0-2 m) an along-front jet with vertical shear  $\frac{\partial u}{\partial z} \approx 7 \text{ s}^{-1}$ . Beneath the plume the result is  $\approx 0.35 \text{ s}^{-1}$ , where we disregarded the head-wave and estimated  $\frac{\partial \rho}{\partial y} \approx \frac{\Delta \rho}{\Delta y}$ , with  $\Delta \rho$  based on density differences > 100 *m* away from the front on either side, and  $\Delta y$  corresponding to the frontal thermohaline width ( $\approx 100 \text{ m}$ ). In contrast, the measured along-front reference velocity shear values are much lower,  $\sim 0.1 \text{ s}^{-1}$  in the entire water column, and of the opposite sign to that required by thermal wind<sup>2</sup>. Thus, the circulation pattern is far from geostrophic balance.

Composites of the relative cross-frontal velocity v'(y,z) are shown in Fig. 5 up to a distance of 300 *m* from the front<sup>3</sup>. The relative velocity is towards the saline side at the surface, and towards the fresh side at depth. The 2-layer structure qualitatively resembles the canonical density current structure (Benjamin 1968; Simpson 1997; Ungarish 2009). A head-wave like feature also appears. That is typical of gravity current fronts (section 1), although here internal waves contribute to it as well (section 4). The mid-depth flow is more noisy, or displays more scales of variability, but since density measurements beneath 10 *m* 

<sup>&</sup>lt;sup>2</sup>The shear of u' composites in the upper five meters is, like the U shear, of the opposite sign to that required by thermal wind.

<sup>&</sup>lt;sup>3</sup>Individual sections reaching distances up to 500 m from to the front do not show significant deviations from the composites shown here.



FIG. 4. TIA density data vs depth and (5-meter binned) cross-front distance. Composites for sections from periods 1-3 (11:00-12:30, 12:30-13:30, and 13:30-15:00, respectively) are shown in panels a-c, respectively. Contour interval =  $0.5 kg/m^2$ .

depth are unavailable, we do not comment on it further. Along-front velocity u' (not shown) is generally less coherent than v', and several times smaller in magnitude than U.

Since buoyant material accumulates at the surface, and since horizontal thermohaline gradients are maximal there, the frontal propagation velocity relative to the ambient (reference) flow,  $v_{f,obs}$ , is defined as the cross-frontal component of the relative velocity (v') in the upper bin. Another, semi-independent calculation of  $v_{f,obs}$  is provided by the difference between cross-frontal velocity of drifters on the front, and the cross-frontal component of the ADCP-derived reference velocity (V). The two methods give very similar results: in periods 1,2, and 3, respectively, the drifter-based (ADCP-based) relative frontal velocities are  $v_{f,obs} = 0.08$  (0.13), 0.24 (0.22), and 0.25 (0.23) m/s. More details are given in appendix B. Thus the relative frontal velocity grows in time, i.e., the density current initially accelerates.

Cross-front convergence was observed in the motions of the CARTHE drifters (section 3a). A quantitative measure of convergence is now obtained. As individual drifters converged to the front, their velocities dropped by up to 0.2 m/s within  $\approx 20$  minutes. Thus the convergence distance is  $\sim 0.5 \times 0.15 [m/s] \times 20 [minutes] \approx 100 m$ , and the convergence value is  $\approx 0.15 [m/s]/100 [m] \approx 40 f$ . The magnitude is confirmed in a calculation of the strain tensor from relative motions of drifter groups (Molinari and Kirwan Jr 1975), which we shall not expand upon here. The cross-front convergence is characteristic of density currents. The convergence magnitude ( $\delta$ ) is very high relative to mesoscale ( $\geq 10 \ km$  scales,  $\delta \sim o(f)$ ) ocean motions. Similar magnitudes ( $\delta \sim O(10f)$ ) were previously measured in fronts of similar or slightly larger scales (Rascle et al. 2017; D'Asaro et al. 2018) where intense submesoscale circulations (McWilliams 2016) occur. Similar

and larger values (> 100 f) were measured for even narrower or strongly tidal buoyant plumes (O'Donnell et al. 1998; Orton and Jay 2005).

### 4. Comparison with stratified density current theory

The frontal-scale circulation pattern and density field diagnosed in previous sections, are qualitatively consistent with density current structure. The main points of similarity are (a) a sharp ( $\approx 100 \ m$  wide) front separating waters of very different densities near the surface (Fig. 4); The frontal width is much lower than the Rossby radius of deformation  $R_d = \frac{N \cdot H_e}{f}$ , which we estimate at 5-20 km. Here N is the Brunt-Vaisala frequency, and  $H_e$ is the "equivalent depth" (Gill 1982). The value assigned to the latter is varied between the plume thickness to the full fluid depth in the  $R_d$  estimate. (b) Propagation of the buoyant layer into the dense "ambient", with a return flow at depth (Fig. 5b-d); (c) a head-wave exists at the front (Fig. 4); (d) an occurrence of convergence towards the front at the buoyant layer (sections 3a and c); (e) Consistently, the frontal circulation is very far from geostrophic balance (section 3c).

In light of the qualitative consistency of the frontal circulation with density current features, in this section we make a quantitative comparison of the diagnosed frontal propagation speed (section 3c) to the theoretical prediction based on stratified density current theory. In subsection a, steady statified density current theory is used, whereas in subsection b, interactions of the density current with internal gravity waves are considered.

#### a. Steady flow theory

The speed of propagation of a steady one-dimensional density current (Ungarish 2009) of thickness h, within an



FIG. 5. Composites of velocity derived from repeated sampling sections by boat mounted ADCP, for periods 1-3 (11:00-12:30, 12:30-13:30, and 13:30-15:00, respectively). Panels a and b show "reference velocity" (average velocity on the saline side, see text) vs depth, in terms of speed and direction (panel a), or cross-front and along-front velocity components (panel b). Panels c-f shows relative velocity components (defined relative to the reference velocity) vs depth and cross-front distance. Cross-front relative velocity composites for periods 1,2, and 3, are shown in panels c-e, respectively. A single along-front relative velocity composite for periods 1-3 is displayed in panel e. Positive *u* values indicate velocities towards the saline side.

ambient fluid of total depth *H* is approximately proportional to  $c_i = \sqrt{\frac{\Delta P}{\rho}}$ , where  $\Delta P$  is the hydrostatic pressure difference between both sides of its front. For the case of a homogeneous density current propagating within a homogeneous (unstratified) ambient, the exact relation was derived by Benjamin (1968), taking into account energy dissipation (but not entrainment):

$$v_f = F_B(h/H) \cdot \sqrt{\frac{\Delta P}{\rho_0}},\tag{2}$$

$$F_B(a) = \left[\frac{(2-a)(1-a)}{1+a}\right]^{0.5}.$$
 (3)

The non-dimensional function  $F_B$  derived by Benjamin (1968) is a decreasing function of h/H, with O(1) values. For a thin plume  $(h/H \ll 1)$ , and if the density current and ambient are each unstratified,  $F_B$  is approximately the ratio of the frontal propagation speed to the interfacial wave speed. However, it should not be confused with the ambient Froude number defined in the next subsection. The quantity  $\rho_0$  is a reference (say, column average) density value.

Equation 2 is written here in terms of  $\Delta P$  rather than in terms of a density anomaly, although the latter form is the common formulation in the unstratified case. The present form generalizes well to stratified conditions, where equations 2-3 still serve as an approximation to  $v_f$ , in good agreement with laboratory and numerical experiments (Ungarish and Huppert 2002; White and Helfrich 2008; Goldman et al. 2014). The approximation also compared well with rigorous theory developed for the limiting cases of an unstratified density current propagating within a stratified ambient (Ungarish 2006), and of a stratified density current propagating within an unstratified ambient (Ungarish 2012).

Density currents in qualitatively similar stratification conditions to the present were observed by Warner et al. (2018) in the equatorial Pacific - strong stratification within the plume, mixed conditions at the same depths outside of the plume, and intermediate stratification beneath. Their computations of theoretical density current speed is thus a good basis for comparison with the stratified theory used here. We note that Warner et al. (2018) diagnose rather than compute  $F_B$  in their observations. The second factor in equation 2 is replaced in their calculations by  $\sqrt{g'h}$ , where the density difference in the reduced gravity g' is averaged over the buoyant layer depth. That is numerically very similar in these stratification conditions to our  $\sqrt{\frac{\Delta P}{\rho}}$  prescription, with  $\Delta P$  evaluated at the base of the plume. Warner et al. (2018) diagnose  $F_B \approx 0.7$ , from the ratio of observed propagation speed to  $\sqrt{g'h}$ . We note that this  $F_B$  value is the only one which can correspond to vanishing dissipation in the front (Benjamin 1968), and that a similar  $F_B$  value was also suggested to hold in density current observations in the same area by Johnson (1996). Thus we suggest that previous measurements (Johnson 1996; Warner et al. 2018) are plausibly consistent with the presented formulation, which follows from stratified density current theory.

The theoretical frontal speed  $v_f$  (evaluated from equation 2, see appendix C), and the observed frontal velocity,  $v_{f,obs}$  (section 3c and appendix B) are compared in Fig. 7. We find that  $v_{f,obs}$  was initially substantially lower than  $v_f$ , but grew in magnitude during period 1, attaining values within 25% of (mean deviation 10% from)  $v_f$  during each of periods 2-3. We shall see in subsection b that reasonable agreement with steady theory may be expected apriori only in periods 2-3, since at these times internal waves cannot overrun the front.

A decrease in  $v_f$  over time is predicted, and attributed (see appendix C) mainly to thermohaline changes (section 3b) and the associated decrease in the frontal pressure head. From late period 3 on, the decrease in  $v_{f,obs}$ is more rapid than the decrease in  $v_f$ . However, some extrapolation (e.g., for reference velocity) is used in deriving frontal velocities after 3 pm (appendices B-C), and hence their respective errors are uncertain at that time.

The steady-state theory used in this subsection is formally invalid when IGW occur, and specifically when they overrun the front. During early period 1 the front appeared to have been almost stationary, i.e, a speed decrease as one looks back in time to  $\approx 0.1$  (a third of  $v_f$ ) towards 11 am. A possible reason for this early-time discrepancy is suggested to be interaction with IGW, as discussed and analyzed in subsection b.

### b. Density current - IGW interactions

In stratified conditions ambient IGW become possible, and stratified density current theory also deals with the interactions between the density current and the IGW in the ambient. IGWs are observed in TIA sections by the plunging of isopycnals in the vicinity of the front (Fig. 6). Isopycnals from the base of the plume to at least as deep as 9 *m*, plunge an extra 1 - 2 m at the front. In this section we demonstrate and analyze several regime changes in interactions of IGW with the density current front.

(i) Supercritical transitions A key parameter in current-wave interaction is the ambient Froude number  $F_a$  (not to be confused with  $F_B$ ), here the ratio of the frontal propagation speed  $v_f$  to the fastest long-IGW speed in the ambient ahead of the density current,  $c_a$ . The  $F_a$  values define the sub-critical ( $F_a < 1$ ), critical ( $F_a = 1$ ), and super-critical ( $F_a > 1$ ) regimes. We also define the fastest IGW

speed in the ambient under the plume  $c_u$ , and the Froude number in the same region,  $F_u$ .

Laboratory experiments and numerical simulations of density currents in ambient stratification (Maxworthy et al. 2002; White and Helfrich 2008) show that for  $F_a < 1$ , IGW can form at the front and overrun it, propagating to the ambient ahead of it. The waves crossing the frontal area compromise the validity of steady state model, such as that used in the previous subsection, in case of a sub-critical regime. In contrast, IGWs may grow to finite amplitudes and remain locked to the front if the regime is critical or somewhat supercritical (Maxworthy et al. 2002; White and Helfrich 2008), i.e.,  $F_a \gtrsim 1$  (a more distinguished criterion is addressed below). Finally, in the strongly supercritical regime (at still larger  $F_a > 1$  values), no significant waves lock to the front, or propagate ahead of it, although they may appear at or propagate towards its rear.

In observations of the Columbia river plume, Nash and Moum (2005) have demonstrated a super-critical to critical  $F_a$  transition. At the initial stages of the Columbia plume life, the  $F_a$  regime was slightly supercritical, and large amplitude IGW formed at the front. Nash and Moum (2005) suggest that the frontal convergence field converts density current kinetic energy to potential energy, which is subsequently trapped at the front as a front-locked IGW due to the supercritical condition. As the plume decelerates in its expansion and dissipation, a subcritical transition occurs, and IGW start radiating ahead of the front.

In the present observations, we find (Fig. 6) that the opposite  $F_a$  transition occurs, relative to the process observed by Nash and Moum (2005). In TIA sections during period 1, small-amplitude isopycnal disturbances are found on both sides of the front, suggesting that the regime is subcritical, i.e., IGW occur that are faster than the front. However, in later TIA sections (late period 1 onwards), prominent IGW are found only at the front itself, and their amplitude is increased relative to the earlier sections. That suggests that the  $F_a$  has transitioned to a critical or supercritical value between periods 1 and 2. An additional (qualitative) condition for formation of large-amplitude front-locked IGW in the simulations of White and Helfrich (2008), that the fluid be non-linearly stratified, is also met in our observations as the ambient stratification decreases significantly with depth, e.g., a factor of  $\approx 2$  between 3 to 6 meters depth (Fig. 6).

To examine the critical transition in more detail, we compute the speed of long IGW on the ambient side at each period. We take both ambient stratification and ambient velocity shear into account and obtain the IGW speeds by solving numerically the Taylor-Goldstein equation (TGE), as detailed in appendix D.

The fastest downstream IGW speeds per period,  $c_a$ , are displayed in Fig. 7, along with  $v_f$  and  $v_{f,obs}$ . The TGE IGW speed is seen to be higher (lower) than the instantaneous frontal speed  $v_{f,obs}$  before (after) 12 pm. This sup-



FIG. 6. TIA sections data: density vs depth and (5-meter binned) cross-front distance. Each panel shows a single section with progressively later crossing time. The time given in the title for each section relates to the time of day ([0-24] hours) in which the front was crossed. Contour interval = 0.5 kg m<sup>-3</sup>. Annotations: plume thickness h, frontal velocity  $v_f$ , and "overtaking" velocity  $v_m$ . The velocities as drawn are defined in the frontal coordinate system, i.e., relative to the velocity of the front. Details are given in the text.

ports the interpretation (above) that a critical to supercritical transition occurred during the later part of period 2. Note that the sub- or super- critical character of the density current is insensitive to the error estimates (crosses), which are of the order of  $0.03 ms^{-1}$ . Furthermore, a  $c_a$  estimate is produced for the beginning of period 1 (11:00) as well (appendix C). Its value suggests that  $F_a$  was subcritical at early period 1 with regards to the theoretical (rather than instantaneous) frontal velocity  $v_f$  as well.

In simple stratification scenarios,  $c_a$  grows with H. For example,  $c_a = \frac{NH}{\pi}$  for a case of constant  $N \sim \sqrt{(\Delta\rho)_z/H}$ and with a rigid lid. If the vertical top to bottom density difference  $(\Delta\rho)_z$  is constant, then  $c_a \sim \sqrt{H}$ . This relation scales well for the TGE solutions as well (appendix D and figure C8). This suggests that transition from subcritical to critical  $F_a$  occurs due to  $c_a$  reduction (and  $F_a$  increase) over time as a result of density current shoaling.

Having established the critical transition during period 1, we turn to further conditions on the formation of frontlocked IGW, observed in period 2. White and Helfrich (2008) showed that a more accurate condition to their formation is (rather than  $F_a \approx 1$ )  $F_u \approx 1$  (e.g., their figures 13-14). The condition that the linear IGW speed under the plume be close to critical, may be roughly interpreted as allowing the co-propagation with or accumulation of IGW disturbances at the front. It appears that nonlinearity (and associated with it, enhanced propagation speed) may be necessary to allow disturbances with speed slightly lower than  $v_f$  (i.e.,  $F_u > 1$ ) to accumulate at the front. Therefore we compute both  $c_u$ , using the TGE again, and its first order nonlinear correction,  $c_{nl}$ . The nonlinear correction is related to the KdV equation (see appendix E).

The results for  $c_u$  and  $c_{nl}$  are shown in figure 7, and given in table D1 as well. During early and mid-period 1,  $u_a$ ,  $u_p$ , and  $u_{nl}$  are all similar <sup>4</sup>. However, during period 2  $c_{nl}$  is similar in magnitude to  $v_f$ , while linear wave speeds are  $\approx 50\%$  lower. Therefore, finite-amplitude front-locked

<sup>&</sup>lt;sup>4</sup>The  $c_u$  and  $c_{nl}$  calculation scatter is quite low (high) for periods 2-3 (1), as detailed in appendix E. Hence we avoid over-interpreting period 1  $c_u$  and  $c_{nl}$  values.



FIG. 7. The plot compares the measured  $(v_{f,obs}, \text{black})$  and steadystate theoretical  $(v_f, \text{blue})$  frontal velocities, and demonstrates that several regime transitions (approximately indicated by bottom arrows) occur in relation to IGW front speed criticality. IGW speed ahead of the plume  $c_a$  is shown in red circles at 11:00, and per period 1-3. Crosses denote  $c_a$  uncertainty estimates. The red curve is obtained by spline interpolation from the red circles, and by uniform forward extrapolation after 15:00. Solid (hollow) triangles denote nonlinear (linear) IGW speed in the ambient under the plume,  $c_{nl}$  ( $c_u$ ). Triangles symbols relate to the same times as circles, but are horizontally offset for visual clarity. Further details on calculations are given in section 4 and in appendices B-D. Error estimates for  $c_u$  and  $c_{nl}$  are given in table E1. The annotations "subcritical", "supercritical ahead", and "supercritical on both sides", refer to  $F_a < 1$ ,  $F_a > 1$  while  $F_u \leq 1$ , and both > 1, respectively.

IGW developed in "tight" critical conditions in terms of the nonlinear wave speed  $c_{nl}$ . Hence nonlinearity is a decisive factor in allowing the frontal locking of IGW in period 2, and hence perhaps in attaining their larger amplitudes as well.

Unlike in period 2, at period 3  $c_{nl}$  is considerably lower than  $v_f$  (despite that a nonlinear wave amplitude similar to that observed in period 2 was assumed in the period 3 calculation). That is also consistent with the disappearance of the prominent front-locked IGW in period 3 (figure 4c). Instead, isopycnals ahead of the plume monotonically plunge under it (compare with, e.g., White and Helfrich 2008, figures 11c and 12c). The front-locked IGW of period 2 is presumably left behind as  $F_u$  grows in period 3, or is dissipated, but in any case cannot be supported at the front. Thus another criticality regime transition occurs between periods 2 and 3, specifically,  $F_u$  passes from nearcriticality (period 2) to supercriticality (period 3).

The changes in  $c_{nl}$  (and therefore in  $F_u$ ) over time are consistent with the presence or absence of IGWs at the front, as described above. These  $c_{nl}$  differences are in turn determined by changes in depth, ambient stratification, and ambient velocity (appendices D-E). It does not appear straightforward to determine which of these factors have more weight in influencing the  $c_{nl}$  changes, but note that significant ambient stratification changes occur between periods 2 and 3 as the front approaches the shoreline (figures 4 and E1).

Calculated spatial IGW properties are also in rough agreement with the observed. The calculated period 2 plume-side<sup>5</sup> IGW isopycnal displacement  $\eta(z)$  (appendix E) peaks at depths of 3.5-4 m, is in rough agreement with the observed depth of peak isoypcnal plunging (figure 6). The horizontal scale (say, half a wavelength) of the observed IGWs (Fig. 6) is  $\approx 20 - 100 m$ . The specific wavelengths excited at the front were postulated by White and Helfrich (2008) to be related to the mechanism of resonant forcing over "topography", where the latter is represented by the density current shape. While the IGW speeds displayed in Fig. 7 correspond to wavelength  $\rightarrow \infty$ , the wave speed changes very little for disturbances long compared to the fluid depth. Indeed, repeating the TGE calculations for a wavelength of 50 m changes the  $c_a$  and  $c_u$  wave speeds by only a few cm/s. Hence there may be said to be a supercritical transition with respect to wavelengths comparable to the observed IGWs, consistently with the observations. The calculated KdV soliton widths W (for  $c_{nl}$ , appendix E) during period 2, 40 - 50 m, are also similar in magnitude to the observed IGW widths in period 2.

(ii) Density current deceleration by IGWs Experiments in stratified conditions show that density current interface becomes wavy in subcritical  $F_a$  conditions. In some cases, interaction with the internal wave field may cause deceleration of the gravity current in this regime. The effect was first demonstrated by Maxworthy et al. (2002), in their laboratory and numerical experiments. In their experiments the deceleration occurs when IGW troughs became aligned with the front after propagating past it. Alignment of IGW crests with the front accelerated the latter, but to a lesser degree than the acceleration by the troughs, causing a net mean deceleration. Goldman et al. (2014) also find similar relative deceleration in numerical experiments for a stratified density current in a stratified ambient. In numerical and laboratory experiments (Maxworthy et al. 2002; Ungarish and Huppert 2006; Goldman et al. 2014), the deceleration generally occurs under the conditions that (1) the front is subcritical wrt IGW propagation speeds; (2) the ambient vertical density difference is comparable in size to the total vertical density difference in the plume side of the front. The magnitude of the deceleration is often larger than 50%, and can also be large enough to effectively arrest the density current temporarily.

The summarized conditions for deceleration are examined in regards to our observations. (1) Fig. 7 suggests that around 11:20, a subcritical to supercritical transition

<sup>&</sup>lt;sup>5</sup>i.e., associated with  $c_u$  and  $c_{nl}$ .

has occurred relative to  $v_f$ . (2) the ambient vertical density difference is of similar magnitude (larger than 50%) relative to the total vertical difference on the plume side; Additionally, (3) The reduction in speed in period 1 relative to that predicted or observed in periods 2-3, is similar to the magnitude of deceleration in experiments (referenced above) due to IGW-front interactions. The conclusion is that it is plausible that prior to  $\approx 11:30$  am, the density current speed was much reduced due to interaction with IGWs in a subcritical  $F_a$  condition. Once the IGW speed decreased (due to propagation of the front to shallower water, (i) above), a subcritical to supercritical transition occurred relative to  $v_f$ , which allowed  $v_{f,obs}$  to recover and gradually grow again to values close to  $v_f$ .

#### 5. Summary and discussion

Detailed observations of a propagating Mississippi outflow plume and its sharp front were taken in the Gulf of Mexico's Louisiana bight during early May 2017. While previous observations of the Mississippi plume focused mainly on bight scale surface circulation, we focus on frontal circulation and its interaction with internal gravity waves (IGW). In the observations, the plume moved across the center of the bight, rather than as a coastal current. Thus the large scale spatio-temporal circulation pattern on the bight was in contrast to the arch-typical patterns of semi-steady circulation following river outflows, the coastal current and the recirculating bulge.

The remote sensing and the in situ data show that the front extended over 20 km in length, while its width was O(100m), considerably smaller than the Rossby radius of deformation. It is found meaningful to decompose the flow field near the front into two components: reference (larger scale), and relative (frontal) flow fields. The relative velocity and density fields display several qualitative similarities with density currents, including a narrow front, flow away from the buoyant layer, a return flow beneath it, and a strong surface convergence towards the front on the buoyant side.

The frontal circulation is compared with stratified density current theory (section 4a). Previous comparisons (Luketina and Imberger 1987; Marmorino and Trump 2000; O'Donnell 2010) have used classical homogeneous density current theory, for weakly or partially stratified conditions. The observed frontal propagation speed is shown to differ by  $\approx 10\%$  on average from the stratified theory prediction during mid to late in-situ observations (periods 2-3, defined in section 2). Earlier however, the front was significantly slower, in apparent contradiction to the (steady-state) theory.

The frontal speed anomaly relative to the steady state theory during period 1 is to be expected if conditions were in fact not steady. Indeed, repeated density sections across the front show IGW anomalies on both frontal sides during early to mid period 1. The velocity of ambient IGWs is estimated from the Taylor–Goldstein equation (TGE), and confirm that the  $F_a < 1$  (subcritical Froude number relative to IGWs ahead of the plume) during that time, i.e., IGWs (which may be generated at the front, e.g., Nash and Moum 2005; White and Helfrich 2008) are faster than the front, and overrun it.

Previous laboratory experiments and numerical simulations (Maxworthy et al. 2002; White and Helfrich 2008; Goldman et al. 2014) have demonstrated that a stratified density current in a subcritical regime may be slowed down significantly by interactions with the generated IGWs. Conditions at which such deceleration by IGW interactions occurred in experiments are reviewed, and appear consistent with conditions in our observations. It is therefore plausible that the slow anomaly during period 1 occurred due to interactions with IGWs in a subcritical  $F_a$  regime, a phenomenon previously demonstrated in numerical and lab experiments only.

The TGE calculations suggest that IGW speed at the front decreased during the observations due to the propagation of the front to shallower water. The IGW speed decrease facilitated a subcritical to critical transition by late period 1. The transition is in contrast to previous observations (Nash and Moum 2005; Kilcher and Nash 2010). In Nash and Moum (2005), large amplitude IGW grew and remained locked to the front in the (initial) supercritical regime, and radiated ahead of the front as it slowed down and transitioned to a subcritical regime.

In our observations, finite amplitude front-locked IGW appeared as  $F_a$  grew to supercritical values in period 2. Based on numerical simulations and theory, White and Helfrich (2008, 2012) show that the regime in which frontlocked IGWs appear is better described in terms of criticality of  $F_u$ , the Froude number relative to linear IGW speed under the plume (rather than ahead of it,  $F_a$ ). In our observations  $F_u \approx 2$  during period 2, where the linear IGW speed is again evaluated from the TGE. Indeed, in the calculations of White and Helfrich (2008) as well, in some cases front-locked waves appeared even for  $F_u > 1$ (Their figures 13-14). Therefore we additionally calculate the first nonlinear (KdV) correction to the internal wave speed,  $c_{nl}$ . It is found that the mean  $c_{nl}$  value during period 2 is within a few percents of the observed frontal speed. That is, during the presence of finite amplitude front-locked IGWs, a "tight" criticality occurs in terms of the nonlinear wave speed. It is thus suggested that the finite-amplitude IGW criticality is enforced by the nonlinear speed enhancement, and a positive feedback may be at work.

Finally, a transition to strict  $F_u$  supercriticality occurs between periods 2 and 3, after which front-locked waves do not appear, as the front can overrun any ambient IGW. The IGW speed calculations suggest this occurs again (as in the period 1 transition) due to ambient IGW slowdown. However in the period 3 case, it is not as clear that shoaling is (directly) a significant cause of the IGW slowdown. Rather, significant ambient stratification changes, as well as ambient shear changes, may be the main causes.

In this paper we concentrated on the dynamics of the frontal circulation, identified as a density current, and its possible interactions with internal gravity waves. We note that the reference surface velocity contributes a larger fraction of the plume velocity than the relative (frontal) velocity, including in the cross-front direction. Hence the large scale (reference) velocity component holds an important role in the cross-bight plume propagation, which contrasts with the more common observations of coastally-trapped density currents. Further investigation of the associated large scale cross-bight propagation pattern and its dynamical causes are thus desirable as well.

We note that a complicating factor in the presented theoretical analysis is that the front is embedded in vertically sheared ambient flow, more intense than the density current circulation. The theory and previous simulation results compared with in section 4 take ambient stratification into account, but not ambient shear. A possible alleviating factor is that the plume is limited to the top two meters of the water column, and the ambient (reference) velocity varies by a small fraction ( $\leq 10\%$ ) over the same depth.

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The presented datasets collected as part of SPLASH are available for download from the Gulf of Mexico Research Initiative Information and Data Cooperative (GRI-IDC) website: https://data.gulfresearchinitiative.org/

### APPENDIX A

## Mean frontal position per period

The average mean position of the frontal plume in-situ observations are given in table A1 per each period (section 2). The positions are based on the mean Kodiac positions (which took repeated sections across the front) for each period. They are thus representative of the position in the cross-front coordinate (sections 2 and 3a), whereas the

TABLE A1. Mean frontal position and seabed depth in each averaging period (section 2)

Time	Longitude	Latitude	Seabed depth
11:00-12:30	-89.9954°	$29.0074^{\circ}$	23.8 m
12:30-13:30	-90.0349°	$29.0177^{\circ}$	20.7 m
13:30-15:00	$-90.0736^{\circ}$	29.0369°	16.6 m

front by definition is elongated in the along-front direction. The seabed depths given correspond to the locations given, and are approximately representative of the entire front since the front aligned with the isobaths (section 3a).

## APPENDIX B

#### **Observed frontal velocity**

The observed relative frontal velocity  $v_{f,obs}$  is estimated in each period using two different methods. Both methods rely on the same reference velocity, i.e., the ADCP reference velocity V, and define the relative frontal velocity as an absolute velocity minus this reference velocity. We use the top bin of V (hereafter  $V_s$ ) in each period, since the reference cross-front velocity varies little in the top  $\approx$  meter (Fig. 5a). The first method uses for the absolute frontal velocity the ADCP-derived absolute velocity within the top bin averaged between 50 m from the front on the fresh side to 25 m from the front on the saline side (the results are not sensitive to changes by a factor of two in these distance values). The second method uses the velocity of drifter 5 (which which was on the front at all times and is representative of velocity of other drifters on the front, section 3a) to define the absolute frontal velocity. The two methods give very similar results, as detailed in table B1.

In addition to  $V_s$  so defined at each mid-period (11:45, 13:00, 14:15), we define  $V_s = 0.1$  m/s at 11:00. That is in rough agreement with extrapolation of drifter 5 velocity (figure 2b) backward in time, as well as with (not shown) additional data based on Kodiac frontal crossings around 10:45. See also discussion at end of section 3a.

To derive an "instantaneous"  $v_{f,obs}$  (used in section 4) rather than a period-averaged one, we again use the ("instantaneous", this time) velocity of drifter 5 relative to the top bin ADCP measured reference velocity  $V_s$ . The three  $V_s$  values are are spline-interpolated to the drifter time-base. After 15:00, ADCP observations were not made, and hence the reference velocity at that time (up to 17:00) is defined as equal to its value at 15:00. The result is smoothed with a 1st order Savitzky-Golay filter with a 0.5-hour window size.

TABLE B2. Relative frontal velocity  $v_{f,obs}$  estimates. Each row relates to a different averaging period (1,2, and 3. See section 2). The "drifter-based" estimates reply on absolute velocity of drifter 5. The ADCP-based estimates rely on absolute velocity from the ship-mounted ADCP, either from its top bin, or from linearly-extrapolating its measurements (0.5 m upwards) to the surface based on the two top bins. All three methods reply on the ADCP-based reference velocity, which appears to vary little vertically in its top bins

Time	Drifter – based	ADCP-based	ADCP-based
		(top bin)	(interpolated)
11:00-12:30	0.08 m/s	0.13 m/s	0.16 m/s
12:30-13:30	0.24 m/s	0.22 m/s	0.275 m/s
13:30-15:00	0.25 m/s	0.23 m/s	0.3 m/s

#### APPENDIX C

#### Theoretical frontal velocity

To evaluate  $v_f$  from equation 2, we calculate  $\Delta P$  and h by values 300 m away from the front on either side, in each TIA section. The results (Fig. 7) are not sensitive to the specific distance chosen. The plume thickness h was defined based on the depth of the deepest isopycnal that surfaces on the ambient side (see fig. 4), about 2 (2.65) m during periods 1-2 (3). The cross-front pressure difference  $\Delta P$  is calculated at depth h. It is analogous to the prescription of  $\Delta P$  at the base of dense (as opposed to buoyant) density currents in stratified ambients (Ungarish and Huppert 2002; Ungarish 2006, 2012).

A smoothed  $v_f$  is obtained by the application of a 1st order Savitzky-Golay filter with a 1-hour window size. The smoothed version is then extrapolated in time by assuming that the stratification profile did not differ after the last TIA section, and using bathymetric depth *H* of the front at each hour from drifter positions. To gauge the influence of reduction in  $\Delta P$  over time in the frontal velocity, the calculation is repeated as described above, except that  $\Delta P$  is kept at the value measured in the first section. The result is compared with the full calculation in Fig. C.

## APPENDIX D

# Internal wave speed calculation in ambient ahead of plume

The discretized Taylor-Goldstein equation (TGE) is solved using the generalized eigenvalue solver described in Jagannathan et al. (2017), with boundary conditions of no-normal flow at the top and bottom. For each observational period (section 2), the phase speeds of the fastest downstream IGW is determined, equal to the maximal real TGE eigenvalue. For the mid-period time of each period



FIG. C8. Theoretical Benjamin (1968) frontal speed  $v_f$  (blue solid line) is compared with the theoretical speed where the pressure head  $\Delta P$ is kept at its initial value (blue dashed line). Estimated maximal wave speeds base on the Taylor-Goldstein equation (TGE, red solid line) is compared with a scaling estimate  $c(t) = c_0 \sqrt{H(t)}/H_0$ , where  $c_0$  and  $H_0$ are the full TGE estimate and depth at 13:25, and H(t) is the depth at each time. Blue circles denote  $v_f$  values calculated from density structure obtained in individual frontal-crossings. The blue curve is obtained by interpolation of the blue circles data points (some quantities used in the calculation are extrapolation after 3 pm). Other symbols are as defined in Fig. 7.

1-3, the background vertical profiles of cross-frontal velocity and stratification considered are as shown in Figs. 5 and 4, respectively.

Uncertainty ( $\pm 0.03 \text{ m/s}$ ) was quantified first by varying the depth and strength of the peak stratification in the top 10 m, by 10% about the measured values and recomputing the IGW speeds. Second, since stratification measurements under 10 m depth were not available the reported phase speeds were calculated assuming stratification is constant beneath 9 m depth. However, we find that the deep stratification has very small impact on the maximal phase speed: changing the stratification under 10 m by  $\pm 50\%$  changes the peak phase speed by up to 0.02 m/s in the variations we attempted.

A solution for 11:00 was calculated as well. Since the plume was almost stationary at that time (appendix B), the density stratification was taken as identical to period 1 (11:00-12:30) as density changed little in period 1. The same uncertainty quantification as reported above was applied. Similarly, the reference speed was taken as identical to period 1 in vertical pattern but with amplitude multiplied by a = 0.2, consistently with the estimate of surface velocity at 11:00 (appendix B). Changes of the factor a from a = 0 to a = 0.4, changed the IGW speed within the uncertainty values reported in table E1 ( $\approx 0.1$  m/s), not affecting the interpretation in section 3b. Scaling IGW speed relative to seabed depth (next paragraph) also gives similar results at period 1.

The  $c_a$  results per period are given in table E1. The values and their cubic-spline interpolation in time are shown in Fig. 7). The smoothed curve is also extrapolated for display purposes uniformly forward in time from 15:00 to 17:00. To gauge the influence of depth change on the IGW speeds, we plot the TGE speed together with the quantity  $c(t) \equiv c_0 \sqrt{H(t)/H_0}$  in Fig. C1. Here  $c_0$  and  $H_0$  are the full TGE IGW speed estimate and depth at 13:00, and H(t) is the depth at each time. In simple cases of a set top to bottom density difference, uniform stratification, and no ambient velocity shear, the scaling is exact.

### APPENDIX E

## Internal waves of finite amplitude in ambient under the plume

To investigate the formation of front-locked finiteamplitude IGW in period 2 we calculate the ambient IGW wave speed under the plume. We denote by  $c_u$  the fastest such IGW at a given period. The theory and simulations of White and Helfrich (2008) suggest that to a good approximation, a calculation of  $c_u$  can be performed under the assumption that the plume bottom serves as a rigid lid to IGW propagating under it (see also Ungarish 2006). We solve the TGE (appendix C) using the period-averaged ambient density and velocity field under the plume, for each period.

We additionally calculate the first nonlinear correction to the TGE linear wave speed, still taking ambient shear and stratification into effect, using the methodology described by Maslowe and Redekopp (1980). Perturbation analysis shows that any TGE mode may occur as a horizontally-compact disturbance (a soliton), governed by a Korteweg–de Vries (KdV) equation. The soliton width,  $\Delta$ , and its speed of propagation  $c_{nl}$  are then determined by simple integrals (which we perform numerically) of the particular TGE eigenfunction.

The nonlinear speed correction  $c' = c_{nl} - c_u$  is linear in the amplitude of the soliton (Ostrovsky and Stepanyants 1989), i.e., the vertical isopycnal displacement ( $\eta(z)$ ) of greatest magnitude within the disturbance,  $\eta_0$ . The functional form of the KdV soliton (Ostrovsky and Stepanyants 1989) is  $\eta = \eta_0 sech^2 \left(\frac{y-ct}{\Delta}\right)$ . The width parameter  $\Delta$  is therefore approximately the half-width at half-height. For simplicity we define  $W = 4\Delta$ , which is approximately the width of the soliton at  $\eta = 0.1\eta_0$ , and to observational accuracy may be taken as the full width of the finiteamplitude disturbance that can be distinguished visually from other (smaller) undulations. We estimate  $\eta_0 \approx 2$  m, and  $W \approx 100$  m on average during period 2 (figure 6).

The asymptotic analysis used in deriving the KdV equation assumes the parameters  $\varepsilon = \eta_0/(H/\pi)$  and  $\delta = (H/\pi)^2/L^2$  to be "small" ( $\ll$  1), where *L* is a typical IGW horizontal scale, and *H* is the total water depth (Lee and



FIG. E9. Ambient density ( $\rho$ ) and cross-front velocity (V) under the plume are shown in solid and dashed lines, respectively. Profiles are shown for periods 1-3. These are the nominal (see text for description of variations) profiles used in the  $c_u$  and  $c_{nl}$  calculations. Similar profiles for the  $c_a$  calculations (ahead of the plume, appendix D) are given in figure 5 for V explicitly or can be deduced for  $\rho$  from figure 4).

Beardsley 1974). In our case we estimate  $\varepsilon = 0.3$  and  $\delta = 0.1$ , where we assumed  $L = \Delta$ , as computed in our period 2 solutions. Although  $\varepsilon$  is not strictly  $\ll 1$ , KdV is often reasonably accurate outside of its formal validity limits (Ostrovsky and Stepanyants 1989). Although higher order approximations exist (Ostrovsky and Stepanyants 1989; Helfrich and Melville 2006), we consider that multiple complicating factors do not justify going beyond the first nonlinear correction of  $c_u$ . Specifically, the ambient density, velocity, and depth are not constant in time (although changing slowly relative to the hypothetical soliton time scales, e.g.,  $\Delta/c$ ). Additionally, the stratification is unknown under 9 m. The latter caveat is dealt with, as in appendix D, by testing various downwards continuations of the observed stratification, continuously increasing or decreasing in magnitude by up to 50%. The results during periods 2-3 are highly insensitive to these variations (table E1). The nominal (i.e., stratification unchanged in bottom water column) density profile and the velocity profiles per period are shown in figure E1.

The results of the TGE and KDV calculations per period are given in table E1 in the form  $a \pm da$ , where a is the mean value of the particular IGW wave speed at the given period. The value is averaged over the outcomes of different deep stratification profiles as described above, between the 0% and  $\pm 50\%$  cases (trial and error suggests

TABLE E3. Internal gravity wave speeds (relative to reference velocity, appendices D-E) in ambient ahead of the plume  $(c_a)$ , and under the plume  $(c_u, c_{nl})$ . The first two are obtained via the Taylor-Goldstein equation (TGE, appendices D-E).  $c_{nl}$  is the first nonlinear correction to  $c_u$  (appendix E). Men values for each variable are given at 11:00 and for each period 1-3

Time	$c_a[m/s]$	$c_u[m/s]$	$c_{nl}[m/s]$
11:00	$0.49\pm0.05$	$0.45\pm0.1$	$0.45\pm0.1$
11:00-12:30	$0.19 \pm 0.03$	$0.10\pm0.04$	$0.12\pm0.05$
12:30-13:30	$0.11 \pm 0.03$	$0.13\pm0.003$	$0.26\pm0.01$
13:30-15:00	$0.09 \pm 0.03$	$0.1\pm0.002$	$0.13\pm0.003$

intermediate cases give velocities falling between these). Error  $(\pm)$  values given are the maximal deviation between the two extreme stratification cases and the average.

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