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September 1967

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Lawrence Radiation Laboratory  
Berkeley, California

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MEASUREMENT OF POLARIZATION IN  $\pi^-p$   
ELASTIC SCATTERING FROM 229 to 390 Mev\*

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September, 1967

ABSTRACT

The polarization parameter in elastic  $\pi^-p$  scattering has been measured, at the Berkeley 184" synchrocyclotron, with the use of a polarized proton target. At 318, 337 and 390 Mev incident pion kinetic energy, the angular range from  $70^\circ$  to  $180^\circ$  in the center of mass system was covered. At 229 Mev polarization measurements were made in the angular range  $150^\circ$  to  $180^\circ$ . Phase shift analyses using these and other published data were made at the two lowest energies.

## I. Introduction

The phenomenological analysis of low-to-medium energy pion-nucleon scattering has usually taken the form of phase-shift analyses.<sup>1</sup> This type of analysis has had the difficulty that, except at the lowest energies, it is not always possible to determine whether a unique solution exists.

A possible route out of this difficulty is to start with a well-established solution at a low energy and to continue this solution upwards at small increments in energy. At each energy one would make the requirement of any solution found that it not only fit the data well, but also that it join continuously to the (presumably unique) solutions found at lower energies. We do not exclude that other criteria such as those established by unitarity and causality considerations (i.e., dispersion relations) be also imposed. In this manner one may hope eventually to establish a phase-shift solution that is unique at all energies for which sufficient data exist.

The object of this experiment was to increase the amount of data available in order to try to pin down a unique solution at energies near ~300 Mev. At the same time we attempted to resolve certain inconsistencies among previously existing experiments<sup>2,3</sup> and analyses<sup>4,5</sup>.

In the experiment reported here the polarization parameter,  $P(\theta)$ , in elastic  $\pi^-p$  scattering was measured at incident pion kinetic energies of 318, 337 and 390 Mev, in the range from  $70^\circ$  to  $180^\circ$  in center-of-mass scattering angles. At 229 Mev, the angular range from  $150^\circ$  to  $180^\circ$  c.m.s. was covered. The technique used was single scattering from a polarized proton target. Scintillation counter hodoscopes were used to detect

both final-state particles, with sufficient angular resolution to identify elastic scattering events from free protons. The measured asymmetry of the counting rate in any channel, upon reversal of the direction of target polarization (which is normal to the plane of scattering), can be directly related to the polarization parameter,  $P(\theta)$ , once the degree of polarization of the target is known.

Section II of this paper outlines the experimental procedure. Section III contains the results of this experiment. In section IV we present the results of a phase-shift analysis based on this and other results at 229 and 310 Mev.

## II. Experimental Procedure

### A. Beam and Target

The negative pion beams were produced at the internal target of the Berkeley 184" synchrocyclotron and guided out through the cyclotron shielding wall into a second shielded area known as the meson cave. The magnet system was designed so that it could be tuned to several different energies without having to move either the target or the concrete shielding. Momentum resolution was  $\pm 5\%$ . Data were taken at beam kinetic energies centered at 229, 318, 337, and 390 Mev, as determined by range measurements, to within 2%.

The polarized target has been described elsewhere<sup>6</sup> and the principles of operation will not be repeated here.

Four crystals of  $(.99 \text{ La}, .01 \text{ Nd}^{142})_2 \text{ Mg}_3 (\text{NO}_3)_{12} \cdot 24 \text{ H}_2\text{O}$ , weighing a total of approximately 22 grams and filling a 1" diameter X 1" long cylinder, were used as the target. The hydrogen

in the water of hydration provided the protons capable of being polarized by the method of dynamic nuclear orientation.

#### B. Method

The polarization parameter  $P$  in  $\pi N$  scattering was originally defined in terms of the recoiling nucleon from an unpolarized target. If the scattering is taken to be in the horizontal plane, then for a given center-of-mass angle  $\theta$ ,

$$P(\theta) = \frac{\text{number of nucleons with spin "up" minus number with spin "down"}}{\text{total number of nucleons recoiling at angle } \theta}$$

(This "up" direction is more precisely defined below as the direction  $\hat{n}$ .) Many such experiments have been performed, but they all have had to face the difficulty of determining the recoil polarization through making the nucleon scatter a second time.

With the assumption that parity is conserved in the interaction or that it is invariant under time reversal, however, the same parameter can be determined with only one scattering if that scattering is from a polarized target. Only the differential cross section  $I(\theta)$  and target polarization  $\vec{P}_T$  need be measured. The relation between  $P$ ,  $I$ , and  $\vec{P}_T$  is

$$I(\theta) = I_0(\theta)(1 + P(\theta)\hat{n}\cdot\vec{P}_T)$$

where  $I_0$  is the differential cross section measured with an unpolarized target, and  $\hat{n} = \hat{k}_i \times \hat{k}_f$  is the unit normal to the plan determined by the pion's initial and final momenta  $\vec{k}_i$  and  $\vec{k}_f$ . In practice it is easier to avoid systematic errors by measuring the two rates  $I_+$  and  $I_-$ ,

corresponding to scattering with target polarized in the direction of the normal to the plane of scattering and opposite to that normal, respectively. Then what is computed is the asymmetry

$$\epsilon(\theta) = \frac{I_+ - I_-}{I_+ + I_-}$$

Finally (ignoring background),

$$P(\theta) = \frac{\epsilon(\theta)}{P_T}$$

In the experiment reported here,  $P(\theta)$  was determined by this second method. The target geometry was such that  $\hat{n}$  and  $\vec{P}_T$  were horizontal in the laboratory.

### C. Counters and Electronics

All events were recorded as coincidences between two counter hodoscopes which detected the scattered pion and recoil proton as indicated in Fig. 1. To extend the available angular range without doubling the number of counters, the polarized target magnet was operated with opposite polarities at different times. In this way pions scattered at certain angle which would miss the array with one



setting of the magnet will be deflected into the array with the opposite polarity. We hasten to point out that these polarity reversals are not required to reverse the direction of proton polarization. Target polarization reversal is accomplished, at either magnet polarity, by a change of 0.3% in the frequency of the microwave radiation used in the dynamic polarization process.

The pion hodoscope and the normal proton hodoscope each had 12 counters overlapped as shown in Fig. 1 to give 23 electronically distinguishable bins in the " $\theta$ " direction. The array used to detect protons when the magnet polarity was reversed used 11 such bins. In addition each array had 5 non-overlapping " $\phi$ " counters (not shown) running the full length of the arrays behind the  $\theta$  counters. Anti-coincidence counters to left, right and above the beam were placed between the pole tips upstream from the crystal.

A coincidence between at least one counter in each of the four arrays (pion " $\theta$ ", pion " $\phi$ ", proton " $\theta$ ", proton " $\phi$ ") activated the "data-break" input channel to an on-line PDP-5 computer. The identities of all counters which had registered in coincidence were then stored directly in the computer memory later to be read out onto magnetic tape. The PDP-5 also performed a partial reduction of the data and displayed summaries of selected portions of it on an oscilloscope.

#### D. Data Analysis

Analysis of the IBM compatible data tapes produced by the PDP-5 was mainly performed using an IBM 7094 computer off-line. Events for which one and only one bin had registered in each array were further

classified according to these bin numbers into a matrix having, typically,  $23 \times 5 \times 23 \times 5 = 13225$  elements. This analysis was carried out separately for each beam energy and magnet polarity.

Elastic scatters from hydrogen in the target have well defined kinematics and form a narrow band through the matrix. Background events are more or less uniformly smeared over the whole matrix. A program which displayed graphically selected slices of the array was used to determine the hydrogen peak regions. The definition of these regions was then inserted into the final analysis program.

A dummy target, similar to the crystals with respect to quantity of the various atomic masses but containing no hydrogen, was used to measure the background due to scattering from heavy elements. Correction was also made for the presence of helium liquid in the vicinity of the target. The background from these sources was usually a small fraction of the counts in the channels corresponding to elastic scattering from hydrogen, in the worst cases amounting to 30% of the total in those channels.

The final computational program took the selected regions in the crystal and dummy target data and calculated the polarization parameter,  $P(\theta)$ , according to the following formulas:

$$P(\theta) = \frac{\epsilon}{1 - \bar{p} \epsilon}$$

where

$$\epsilon = \frac{\sum_i N_i Q_i}{\left( \sum_i N_i - R \sum_j B_j \right) Q^2}$$

$i$  =  $i^{\text{th}}$  data taking run

$N_i$  = number of counts (in hydrogen region, at scattering angle  $\theta$ ) during  $i^{\text{th}}$  polarized target run

$j$  =  $j^{\text{th}}$  dummy target run

$B_j$  = number of counts, in same region, during  $j^{\text{th}}$  dummy run

$P_i$  = average target polarization during  $i^{\text{th}}$  run

$m_i$  = number of monitor counts during  $i^{\text{th}}$  run

$$\bar{p} = \frac{\sum_i m_i P_i}{\sum_i m_i} \quad \text{should be close to zero if data is evenly distributed between positive and negative target polarization.}$$

$$Q_i = P_i - \bar{p}$$

$$Q^2 = \frac{\sum_i m_i Q_i^2}{\sum_i m_i}$$

$$R = \frac{\sum_i \sum_{\text{NH}} N_i}{\sum_j \sum_{\text{NH}} B_j} \quad (\text{background is normalized to total counts in the non-hydrogen region})$$

NH refers to non-hydrogen regions of matrix.

Target polarization was reversed every two to three hours to keep possible long-term drifts from affecting data taken with one sign of target polarization differently than with the other.

The scattering angle was calculated using a computer program which found the trajectories of particles through the measured magnetic field. Conjugate proton and pion counters calculated in this fashion agreed perfectly with the hydrogen peak regions found in the data matrix. Within our resolution of about  $1^\circ$  laboratory angle, no evidence for error in scattering angle was formed.

E. Target Polarization Measurement

Target polarization was measured by a nuclear magnetic resonance technique, as described in references 6 and 7. This signal was monitored continuously during the run. Every half hour a slow (several minute) sweep through the NMR signal was made, during which the value of the rf level and its first derivative were digitized at small intervals. These data plus calibration signals (thermal equilibrium) which were taken approximately once every 24 hours were analyzed by computer program to give a corrected area under the resonance, which is thought to be proportional to the true polarization. The ratio of these areas, plus knowledge of the temperature and magnetic field at the crystal during calibration, yielded the absolute target polarization.

The polarization measured in this manner averaged 35% during this run. This rather low value may have been due to such factors as insufficient microwave power. On the other hand we cannot rule out the possibility of a systematic error in the polarization measurement. This possibility is supported both by internal evidence (certain difficulties encountered in the polarization-measuring electronics) and by external consistency with other data, mentioned below.

We assign a systematic error of  $\pm 10\%$  to the calibration of the polarization measurement. This is to be interpreted as an uncertainty in the scale, to be applied uniformly to all the data reported in this article, in addition to the errors (largely statistical) reported here for the individual points.

### III. Results

The results of this experiment are reported in Tables I, II, III and IV. They are presented graphically in Figures 2, 3, 4 and 5.

At 318 Mev, near where a conflict exists between measurements of Rugge and Vik<sup>2</sup> and those of Vasilevski et al.<sup>3</sup> at 310 Mev, our results tend to lie in between the two, but perhaps a bit closer to the former.

### IV. Phase Shift Analysis

#### A. Input Data

Using the present polarization measurements along with other published data as input, we have made a phase-shift search at 229 and at 310 Mev.

The input data used, besides our own, were:

For 229 Mev:  $\pi^+$ p polarization at 246 Mev<sup>8</sup>;  $\pi^+$ p total and differential cross-section at 240 Mev<sup>9</sup>;  $\pi^-$ p total and differential cross-sections at 226 Mev<sup>10</sup>; and  $\pi^-$ p charge exchange differential cross-section at 230 Mev<sup>11</sup>.

For 310 Mev:  $\pi^+$ p total and differential cross-sections at 310 Mev<sup>12</sup>;  $\pi^-$ p differential cross-section at 310 Mev<sup>2</sup>;  $\pi^-$ p charge exchange differential cross-section at 313 Mev<sup>13</sup>;  $\pi^+$ p polarization

at 310 Mev<sup>14</sup>; and one point of  $\pi^-p$  charge exchange polarization at 310 Mev<sup>15</sup>.

A normalization parameter was introduced for each bloc of data to account for systematic uncertainties in the scale of each measurement. This parameter was allowed to vary in order to achieve the best fit. It was generally found that solutions found when the normalization parameters were held fixed at unity were not significantly different from those found when they were allowed to vary, but that they had considerably higher  $\chi^2$ .

Also included were the non-spin-flip forward scattering amplitudes derived from dispersion relations.<sup>16</sup>

Partial wave amplitudes up to and including  $L = 3$  (F- waves) were varied in the search for minimum  $\chi^2$ , starting from values chosen randomly within certain regions described below.

Because of limited computer time and memory, it was considered impractical to generate the random starts from points selected uniformly throughout the total range of the variables (phase shift  $\delta$  between  $-180^\circ$  and  $+180^\circ$ ; inelasticity parameter  $\eta$  between 0 and 1; for each partial wave). To reduce the region searched to manageable proportions we made use of the facts that: 1) the solutions should link up reasonably continuously with solutions found at nearby energies; 2) at these low energies, the elasticity is expected to be near unity; and 3) F- wave amplitudes are expected to be small. Whereas the starting points for the searches were selected within the restricted regions defined below, the solutions found proceeding from these starts were not so restricted.

The selected regions in each case centered about the solution found at a nearby energy by BBSV<sup>4</sup>.

B. 229 Mev

At 229 Mev, the region for random starts was defined as follows: For S and P-waves,  $\eta$  between 0.9 and 1.0,  $\delta$  within  $45^\circ$  of the BBSV solution. For D-waves,  $\eta$  between 0.9 and 1.0,  $\delta$  within  $30^\circ$  of the BBSV solution. For F-waves  $\eta = 1.0$ ,  $\delta = 0^\circ$ . Searches were made starting from 40 points chosen randomly within these limits.

The BBSV solution or minor modifications of this solution were found 16 times, with the confidence level of the best fit being 14%. Another solution of confidence level 8% was found once followed by solutions with confidence levels of 1% or less. Solution B can be excluded by using the Wigner condition<sup>17</sup> to link the 229 Mev phase shifts to the 310 Mev phase shifts given below. This condition states that  $\frac{d\delta}{dk} \geq -R$  where R is the radius of interaction. Setting R equal to one pion Compton wave length, we find that the  $S_{31}$  phase shift either goes through an improbable resonance ( $\delta = 90^\circ$ ) between 229 and 310 Mev or decreased 5 times more rapidly than the Wigner condition allows.

These two solutions are shown in Table V.

C. 310 Mev

At this energy an intensive search was made over a wide region of allowed starting points. 120 starts were made from a region which for S, P, and D waves allowed all values of  $\eta$ , from 0.0 to 1.0, and  $\delta$  within  $90^\circ$  (i.e., a semi-circle) of the BBSV value. F-waves were started from

$\eta = 1.0$  and  $\delta = 0^\circ$ . No good solutions were found in any of these searches. 50 starts were made from a more restricted region, namely the same region defined above for the 229 Mev search, but with BBSV solutions appropriate to 310 Mev. Some acceptable solutions were now found. We conclude that in the previous case the search region was so wide that there was very small probability of finding a solution with  $\chi^2$  comparable to that of the BBSV solution.

40 starts were made from the same region, but with F-waves allowed to vary with the limits  $\eta$  between 0.95 and 1.0,  $\delta$  between  $-10^\circ$  and  $+10^\circ$ .

181 starts were made from regions centered at  $0^\circ$  phase shift, within the following limits:  $S_{11}$  and  $P_{11}$ ,  $\pm 30^\circ$ ;  $S_{31}$  and  $P_{31}$ ,  $\pm 90^\circ$ ;  $P_{13}$  and  $D_{13}$ ,  $\pm 23^\circ$ ;  $P_{33}$  and  $D_{33}$ ,  $\pm 45^\circ$ ;  $D_{15}$  and  $F_{15}$ ,  $\pm 19^\circ$ ;  $D_{35}$  and  $F_{35}$ ,  $\pm 38^\circ$ ;  $F_{17}$ ,  $\pm 15^\circ$ ;  $F_{37}$ ,  $\pm 30^\circ$ . For S, P and D-waves,  $\eta$  between 0.9 and 1.0. For F-waves  $\eta$  between 0.95 and 1.0. These limits were selected so that any partial wave can by itself account for the known total cross-section. This procedure should be capable of finding every physically admissible solution.

The program was adjusted to find the minima with an accuracy of about one degree in the phase shifts  $\delta$  and .01 in the elasticity parameters  $\eta$ ; two minima as found by the computer were judged to be equivalent if they were identical to about this accuracy in every parameter. The BBSV solution was found<sup>18</sup> 14 times, with confidence level 37 percent. A similar, but not identical, solution was found



3 times; its confidence level was 6% and it had a rather different normalization factor for  $\pi^- p$  polarization than the first (BBSV) solution. Table VI shows the parameters for each of these solutions. Other solutions had confidence levels of 0.5% or less ( $\chi^2 \geq 100$ ).

Table VII gives values of some quantities that were calculated from the various solutions. These quantities were not fit to experimental data within the program. The elastic cross-sections are reasonable in every case, but the inelastic cross-sections are generally too large. However, since very small changes in the  $\eta$  parameters would give agreement with the experimental numbers<sup>19</sup>, it has seemed acceptable to leave the solutions as they are.

## V. Conclusions

The results of this experiment demonstrate that:

With respect to the conflict in the  $\pi^- p$  polarization data<sup>2,3</sup> at 310 Mev, our results lie between the two, but tend to be closer to those of Rugge and Vik.

We confirm the solution of BBSV<sup>4</sup> as giving a good fit to all the data, including the results of the present experiment, which were not used in their original search.

The results of our phase shift search at 310 Mev seem to indicate that solution A is probably unique. Extensive searching throughout the region permitted by unitarity failed to discover any other solution with comparable  $\chi^2$ . The slightly different solution B has marginally acceptable  $\chi^2$ .

Further experiments have been undertaken at this laboratory to measure polarization in both  $\pi^+ p$  and  $\pi^- p$  scattering in this energy range.

V. Acknowledgments

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Dr. P. Grannis composed the phase shift fitting programs used in this analysis.

FOOTNOTES AND REFERENCES

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Table I. Experimental results for polarization in  $\pi^- p$  scattering at 229 MeV. A systematic error of 10% is to be added because of uncertainty in the target polarization.

| 229 MeV                          |             |                    |
|----------------------------------|-------------|--------------------|
| $\theta_{\pi}^*$ (degrees, c.m.) | $P(\theta)$ | $\Delta P(\theta)$ |
| 153.5                            | -.031       | .051               |
| 155.9                            | -.030       | .050               |
| 158.4                            | -.017       | .046               |
| 160.8                            | -.063       | .043               |
| 163.5                            | .054        | .039               |
| 166.0                            | .102        | .038               |
| 168.5                            | -.010       | .040               |
| 171.1                            | .020        | .036               |
| 173.8                            | .043        | .035               |
| 176.3                            | .085        | .037               |
| 178.6                            | .033        | .058               |
| 178.9                            | .005        | .043               |

Table II. Experimental results for polarization in  $\pi^- p$  scattering at 318 MeV. A systematic error of 10% is to be added because of uncertainty in the target polarization.

| 318 MeV                            |             |                    |
|------------------------------------|-------------|--------------------|
| $\theta_{\pi}^*$<br>(degrees c.m.) | $P(\theta)$ | $\Delta P(\theta)$ |
| 66.8                               | -.892       | .045               |
| 70.7                               | -.784       | .036               |
| 74.6                               | -.654       | .036               |
| 78.5                               | -.569       | .035               |
| 82.3                               | -.501       | .033               |
| 85.8                               | -.463       | .035               |
| 89.3                               | -.310       | .037               |
| 92.6                               | -.147       | .042               |
| 96.1                               | -.113       | .040               |
| 99.3                               | .070        | .044               |
| 102.4                              | .165        | .045               |
| 105.7                              | .292        | .045               |
| 108.9                              | .332        | .047               |
| 111.8                              | .524        | .049               |
| 114.7                              | .529        | .054               |
| 117.5                              | .523        | .049               |
| 120.5                              | .668        | .047               |
| 123.3                              | .530        | .048               |
| 126.0                              | .529        | .049               |
| 128.6                              | .489        | .048               |
| 131.3                              | .511        | .050               |
| 163.0                              | .280        | .112               |
| 165.3                              | .207        | .100               |
| 167.7                              | .164        | .095               |
| 170.2                              | .134        | .092               |
| 172.7                              | .120        | .078               |
| 175.2                              | .028        | .081               |
| 177.3                              | -.052       | .101               |
| 177.7                              | -.007       | .085               |
| 179.8                              | -.103       | .087               |

Table III. Experimental results for polarization in  $\pi^-p$  scattering at 337 Mev. A systematic error of 10% is to be added because of uncertainty in the target polarization.

| 337 MeV                         |             |                    |
|---------------------------------|-------------|--------------------|
| $\theta_{\pi}^*$ (degrees c.m.) | $P(\theta)$ | $\Delta P(\theta)$ |
| 73.5                            | -.709       | .038               |
| 77.4                            | -.606       | .039               |
| 81.2                            | -.619       | .040               |
| 85.0                            | -.544       | .037               |
| 88.5                            | -.363       | .039               |
| 91.9                            | -.244       | .047               |
| 95.2                            | -.190       | .052               |
| 98.6                            | -.077       | .055               |
| 101.8                           | .008        | .053               |
| 104.9                           | .162        | .057               |
| 108.1                           | .353        | .061               |
| 111.2                           | .399        | .052               |
| 114.1                           | .501        | .061               |
| 116.9                           | .507        | .060               |
| 119.8                           | .509        | .060               |
| 122.7                           | .559        | .055               |
| 125.4                           | .611        | .053               |
| 128.1                           | .367        | .064               |
| 130.7                           | .554        | .057               |
| 133.4                           | .540        | .063               |
| 161.6                           | .265        | .071               |
| 164.2                           | .259        | .060               |
| 166.5                           | .170        | .053               |
| 168.9                           | .080        | .049               |
| 171.4                           | .093        | .044               |
| 173.9                           | .053        | .042               |
| 176.1                           | .024        | .058               |
| 176.4                           | .072        | .041               |
| 178.6                           | -.031       | .042               |
| 178.9                           | .118        | .045               |

Table IV. Experimental results for polarization in  $\pi^- p$  scattering at 390 MeV. A systematic error of 10% is to be added because of uncertainty in the target polarization.

| 390 MeV                             |             |                    |
|-------------------------------------|-------------|--------------------|
| $\theta_{\pi}^*$<br>(degrees, c.m.) | $P(\theta)$ | $\Delta P(\theta)$ |
| 74.9                                | -.759       | .036               |
| 78.8                                | -.716       | .039               |
| 82.6                                | -.620       | .042               |
| 86.4                                | -.610       | .043               |
| 90.1                                | -.515       | .047               |
| 93.5                                | -.353       | .055               |
| 96.8                                | -.258       | .057               |
| 100.0                               | .103        | .070               |
| 103.3                               | .252        | .078               |
| 106.5                               | .469        | .066               |
| 109.5                               | .520        | .079               |
| 112.6                               | .643        | .079               |
| 115.6                               | .897        | .074               |
| 118.5                               | .742        | .074               |
| 121.2                               | 1.020       | .078               |
| 123.9                               | .821        | .071               |
| 126.7                               | .728        | .065               |
| 129.4                               | .796        | .071               |
| 132.0                               | .688        | .070               |
| 134.6                               | .692        | .065               |
| 137.1                               | .524        | .070               |
| 167.5                               | .119        | .043               |
| 169.8                               | .112        | .043               |
| 172.2                               | .054        | .042               |
| 173.0                               | .059        | .058               |
| 174.5                               | .113        | .041               |
| 175.5                               | .000        | .045               |
| 177.1                               | .049        | .036               |
| 178.0                               | -.056       | .038               |
| 179.5                               | .023        | .037               |



Table V. 229 MeV. 18 degrees of freedom.  $\delta$  in degrees. Phase shifts accurate to  $\pm 1^\circ$ .  $\eta$ 's accurate to .01.

| Solution |          | A     | B     |
|----------|----------|-------|-------|
| $\chi^2$ |          | 25    | 27    |
| $S_{11}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | 10.2  | 6.2   |
| $P_{11}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | 4.4   | 2.3   |
| $P_{13}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | -3.9  | 3.3   |
| $D_{13}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | 5.1   | -5.6  |
| $D_{15}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | -.6   | 5.5   |
| $F_{15}$ | $\eta$   | .99   | .97   |
|          | $\delta$ | 3.1   | -1.4  |
| $F_{17}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | -1.4  | .4    |
| $S_{31}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | -16.6 | 74.7  |
| $P_{31}$ | $\eta$   | .98   | 1.00  |
|          | $\delta$ | -4.9  | -34.9 |
| $P_{33}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | -64.9 | -29.5 |
| $D_{33}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | -2.2  | -2.3  |
| $D_{35}$ | $\eta$   | 1.00  | 1.00  |
|          | $\delta$ | -.6   | 2.5   |
| $F_{35}$ | $\eta$   | .97   | 1.00  |
|          | $\delta$ | -1.7  | 2.3   |
| $F_{37}$ | $\eta$   | 1.00  | .97   |
|          | $\delta$ | 3.4   | -2.8  |

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Normalizing factors for input data

|   |                   |                   |
|---|-------------------|-------------------|
| $\frac{d\sigma}{d\Omega}(\pi^+ p)$        | .99<br>$\pm .01$  | 1.00<br>$\pm .01$ |
| $\frac{d\sigma}{d\Omega}(\pi^- p)$        | 1.00<br>$\pm .01$ | 1.00<br>$\pm .01$ |
| $\frac{d\sigma}{d\Omega}(\text{ch. ex.})$ | .99<br>$\pm .02$  | .99<br>$\pm .02$  |
| $P(\pi^+ p)$                              | .96<br>$\pm .01$  | .89<br>$\pm .08$  |
| $P(\pi^- p)$                              | .84<br>$\pm .06$  | .84<br>$\pm .05$  |

Table VI. 310 MeV. 66 degrees of freedom.  $\delta$  in degrees. Phase shifts accurate to  $\pm 1^\circ$ .  $\eta$ 's accurate to .01.

| Solution        |          | A     | B     |
|-----------------|----------|-------|-------|
| $\chi^2$        |          | 72.8  | 84.4  |
| S <sub>11</sub> | $\eta$   | 1.000 | 1.000 |
|                 | $\delta$ | 10.6  | 4.6   |
| P <sub>11</sub> | $\eta$   | .97   | .90   |
|                 | $\delta$ | 21.6  | 20.2  |
| P <sub>13</sub> | $\eta$   | .96   | .978  |
|                 | $\delta$ | -4.6  | -7.7  |
| D <sub>13</sub> | $\eta$   | 1.000 | 1.000 |
|                 | $\delta$ | 5.81  | 8.2   |
| D <sub>15</sub> | $\eta$   | 1.000 | .982  |
|                 | $\delta$ | .55   | -.102 |
| F <sub>15</sub> | $\eta$   | 1.000 | 1.000 |
|                 | $\delta$ | 1.52  | 2.26  |
| F <sub>17</sub> | $\eta$   | 1.000 | 1.000 |
|                 | $\delta$ | -.37  | .21   |
| S <sub>31</sub> | $\eta$   | .97   | .964  |
|                 | $\delta$ | -21.1 | -32.4 |
| P <sub>31</sub> | $\eta$   | .994  | 1.000 |
|                 | $\delta$ | -10.8 | -14.1 |
| P <sub>33</sub> | $\eta$   | 1.000 | 1.000 |
|                 | $\delta$ | -41.3 | -30.4 |
| D <sub>33</sub> | $\eta$   | .957  | .91   |
|                 | $\delta$ | -2.1  | -9.7  |
| D <sub>35</sub> | $\eta$   | 1.000 | 1.000 |
|                 | $\delta$ | 1.19  | 11.0  |
| F <sub>35</sub> | $\eta$   | .980  | .984  |
|                 | $\delta$ | -.84  | -.52  |
| F <sub>37</sub> | $\eta$   | 1.000 | 1.000 |
|                 | $\delta$ | 2.16  | -1.07 |

-----  
 Normalizing factors for input data.

|   |                |                |
|---|----------------|----------------|
| $\frac{d\sigma}{d\Omega}(\pi^+ p)$        | .91 $\pm$ .02  | .89 $\pm$ .01  |
| $\frac{d\sigma}{d\Omega}(\pi^- p)$        | 1.03 $\pm$ .02 | 1.00 $\pm$ .02 |
| $\frac{d\sigma}{d\Omega}(\text{ch. ex.})$ | 1.11 $\pm$ .04 | 1.07 $\pm$ .03 |
| P( $\pi^+ p$ )                            | .99 $\pm$ .03  | 1.00 $\pm$ .03 |
| P( $\pi^- p$ )                            | .89 $\pm$ .03  | .75 $\pm$ .03  |
| P(ch.ex.)                                 | 1.03 $\pm$ .03 | 1.05 $\pm$ .03 |

TABLE VII. Values Calculated from Phase Shift Solutions

229 MeV

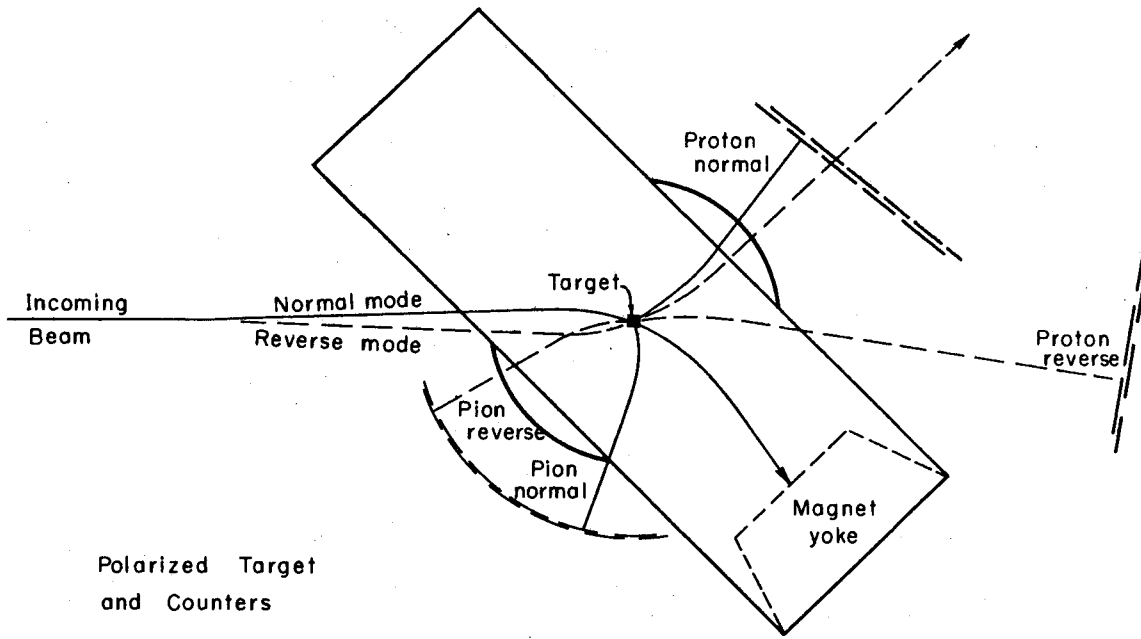
|                                 | Solution<br>A        | Solution<br>B        | Experiment <sub>19</sub>       |
|---------------------------------|----------------------|----------------------|--------------------------------|
| $\pi^+$ inelastic cross section | $4.82 \pm 1.50$ mb   | $4.79 \pm 1.15$ mb   | small                          |
| $\pi^+$ elastic cross section   | $125.63 \pm 2.10$ mb | $126.82 \pm 2.12$ mb | $\sigma_T = 130.00 \pm 7.2$ mb |
| $\pi^-$ inelastic cross section | $2.57 \pm .65$ mb    | $3.79 \pm .69$ mb    | $>0.3 \pm 0.3$ mb              |
| $\pi^-$ elastic cross section   | $16.05 \pm .32$ mb   | $16.00 \pm .51$ mb   | $20.8 \pm 0.4$ mb              |
| charge exchange cross section   | $29.36 \pm .65$ mb   | $29.60 \pm .68$ mb   | $30.4 \pm 1.3$ mb              |

310 MeV

|                                 |                    |                    |                              |
|---------------------------------|--------------------|--------------------|------------------------------|
| $\pi^+$ inelastic cross section | $4.78 \pm .73$ mb  | $6.96 \pm .53$ mb  | small                        |
| $\pi^+$ elastic cross section   | $55.4 \pm .8$ mb   | $54.0 \pm .6$ mb   | $\sigma_T = 65.5 \pm 1.7$ mb |
| $\pi^-$ inelastic cross section | $3.57 \pm .47$ mb  | $5.77 \pm .35$ mb  | $1.47 \pm .10$ mb            |
| $\pi^-$ elastic cross section   | $10.47 \pm .26$ mb | $10.51 \pm .20$ mb | $11.4 \pm 0.8$ mb            |
| charge exchange section         | $15.13 \pm .27$ mb | $14.42 \pm .19$ mb | $17.8 \pm 1.0$ mb            |

FIGURE CAPTIONS

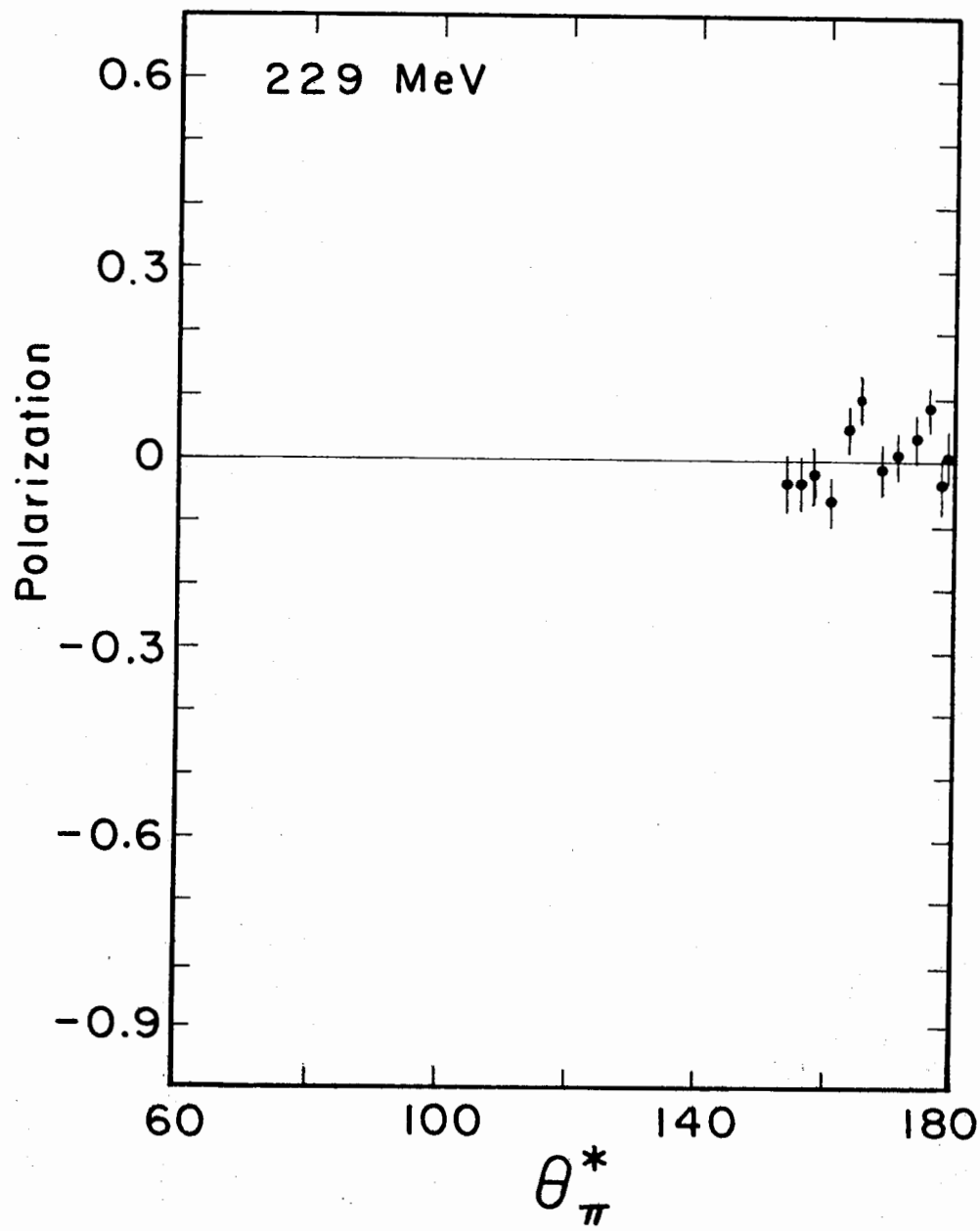
- Fig. 1. Polarized Target, Magnet and Scintillation Counter Arrays.
- Fig. 2. Experimental results for polarization in  $\pi^-p$  scattering at 229 Mev. A systematic error of 10% in the vertical scale is to be added because of uncertainty in the target polarization.
- Fig. 3. Experimental results for polarization in  $\pi^-p$  scattering at 318 Mev. A systematic error of 10% in the vertical scale is to be added because of uncertainty in the target polarization.
- Fig. 4. Experimental results for polarization in  $\pi^-p$  scattering at 337 Mev. A systematic error of 10% in the vertical scale is to be added because of uncertainty in the target polarization.
- Fig. 5. Experimental results for polarization in  $\pi^-p$  scattering at 390 Mev. A systematic error of 10% in the vertical scale is to be added because of uncertainty in the target polarization.



Polarized Target  
and Counters

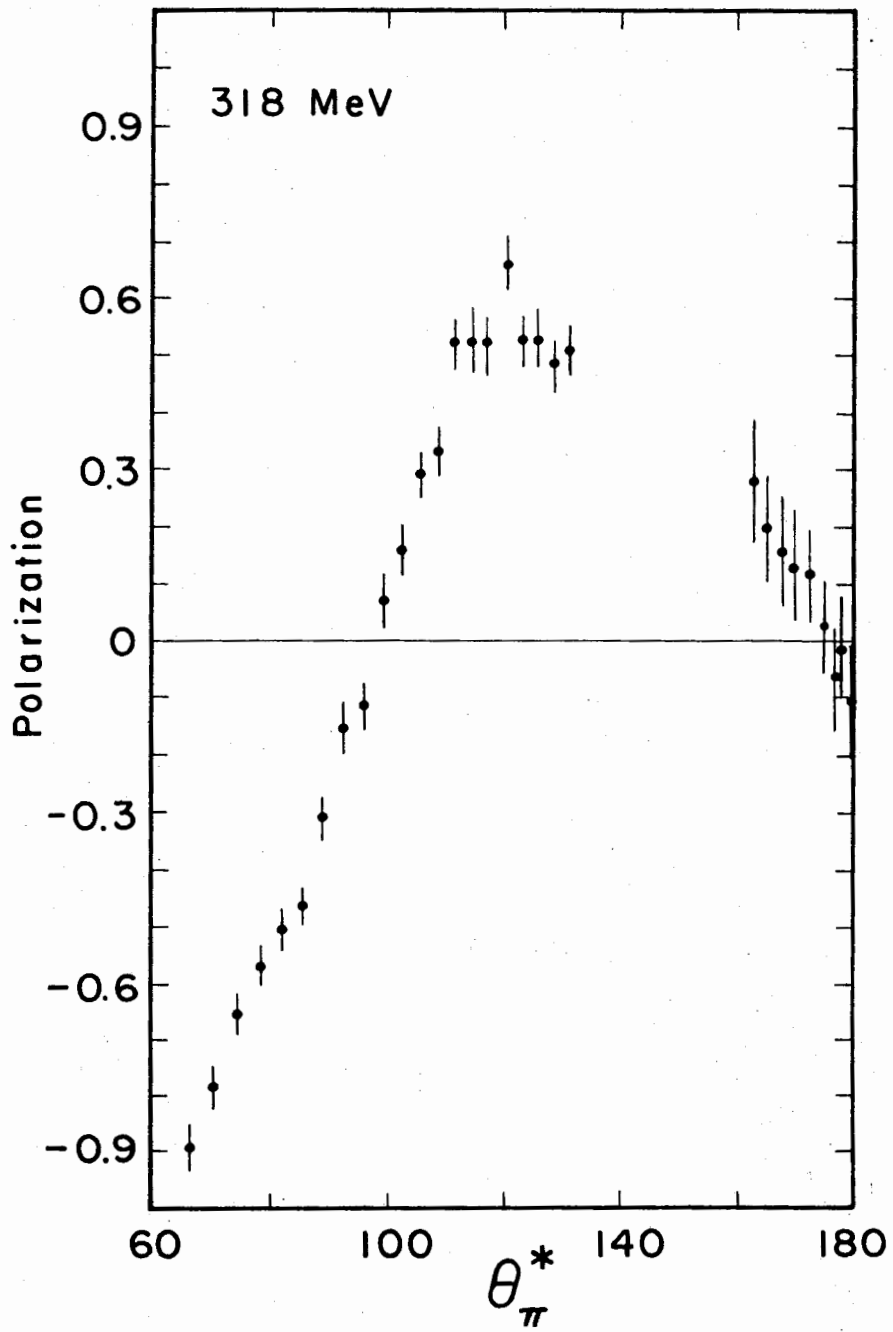
MUB-10360

Fig. 1



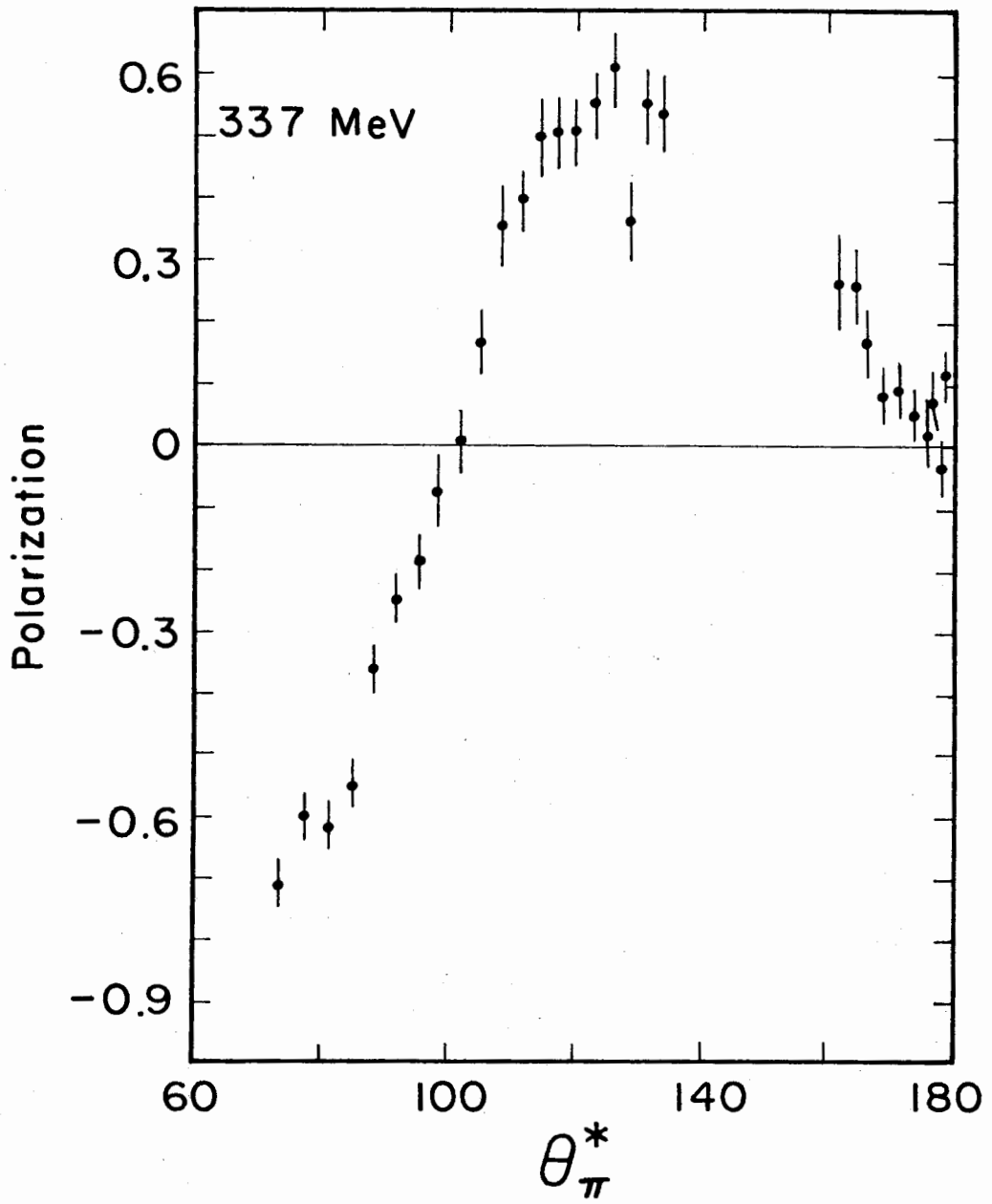
MUB-12293

Fig. 2



MUB-12295

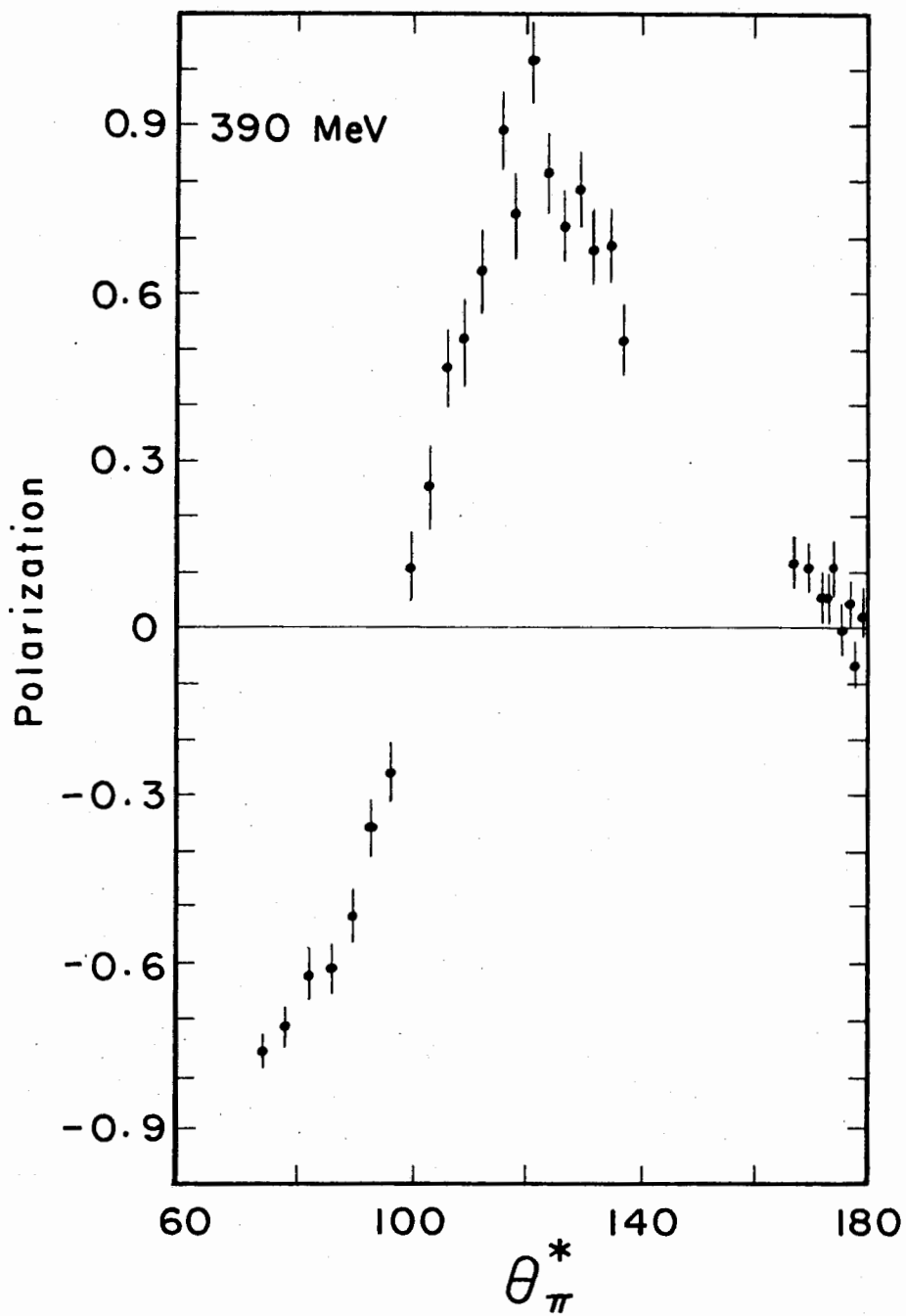
Fig. 3



MUB-12296

Fig. 4





MUB-12294

Fig. 5

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