

Dirac nodal line in hourglass semimetal Nb_3SiTe_6

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ABSTRACT: Glide-mirror symmetry in nonsymmorphic crystals can foster the emergence of novel hourglass nodal loop states. Here, we present spectroscopic signatures from angle-resolved photoemission of a predicted topological hourglass semimetal phase in Nb_3SiTe_6 . Linear band crossings are observed at the zone boundary of Nb_3SiTe_6 , which could be the origin of the nontrivial Berry phase and are consistent with a predicted glide quantum spin Hall effect; such linear band crossings connect to form a nodal loop. Furthermore, the saddle-like Fermi surface of Nb_3SiTe_6 observed in our results helps unveil linear band crossings that could be missed. *In situ* alkali-metal doping of Nb_3SiTe_6 also facilitated the observation of other band crossings and parabolic bands at the zone center correlated with accidental nodal loop states. Overall, our results complete the system's band structure, help explain prior Hall measurements, and suggest the existence of a nodal loop at the zone center of Nb_3SiTe_6 .

KEYWORDS: Hourglass fermions, Dirac nodal loop, nonsymmorphic crystals, glide-mirror symmetry, photoemission, first-principles band structures

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4 Topology in condensed-matter systems has emerged as a fundamental avenue for realizing
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7 exotic symmetry-protected Dirac fermions and emergent phases with unconventional but
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10 technologically relevant electronic properties, including topological insulators, topological
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13 crystalline insulators, and topological superconductors^{1,2,3,4,5,6}. From initial theoretical
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16 discussions regarding the intimate connection between massless Dirac surface states and their
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19 topological protection due to time-reversal symmetry, particle-hole symmetry, etc.⁷, the
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22 theoretical and experimental focuses have now blossomed into considerations of unusual—
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25 albeit versatile—fermion states that arise due to certain crystal point group symmetries^{5,6}, even
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28 those that are protected by a nonsymmorphic space group^{8,9}. Indeed, in the presence of certain
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31 crystalline symmetries, the Dirac fermion states may cross to form a Dirac point or generate a
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34 manifold Dirac nodal point, a Dirac nodal curve, or a Dirac nodal loop in k -space^{6,10,11,12}, and
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37 electrons' behaviors near a manifold Dirac point have been classified, for example, as Weyl
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40 fermion^{6,10}, hourglass fermion¹¹, and wallpaper fermion¹². However, though numerous
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43 compounds have been predicted to host topological nodal lines or nodal loops¹³, recent
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46 experimental works via angle-resolved photoemission spectroscopy (ARPES) of these
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49 topological quasiparticle band dispersions have mainly focused on just a few isostructural
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52 families, such as transition metal monpnictides^{14,15,16}, ZrSiS and others in the PbFCl-type
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55 family^{17,18,19,20,21,22}, and PbTaSe₂¹³, rendering the physical picture of most topological nodal
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58 line semimetals largely incomplete.

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4 Particularly, hourglass fermions are among the newest types of nodal fermions expected
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7 to emerge in topological nodal line semimetals possessing glide-mirror symmetry^{11,23}. In such
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10 materials, the partner switching of eigenstates between certain time-reversal invariant momenta
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13 (TRIM), as required by mirror and glide-mirror symmetries, causes so-called “hourglass-like”
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16 band dispersions to arise with a fourfold-degenerate nodal point, which connects with other
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19 nodal points to form a closed and topologically protected Dirac loop in k -space²³. Prior
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22 experimental results have confirmed the existence of hourglass fermions in KHgSb²⁴, but their
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25 presence has also been predicted in the orthorhombic family of $X_3\text{SiTe}_6$ ($X = \text{Ta}, \text{Nb}$) crystals²³,
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28 ²⁵, wherein the hourglass bands are robust under the spin-orbit interaction²³. Nevertheless,
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31 while prior ARPES studies have focused on probing one-dimensional massless Dirac fermions
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34 in the related $\text{NbSi}_{0.45}\text{Te}_2$ compound²⁶ as well as nodal lines and their relation to hourglass
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37 fermions in Ta_3SiTe_6 ²⁷, a comprehensive survey of the electronic band structure of Nb_3SiTe_6 —
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40 one that considers hourglass bands that disperse with respect to the momentum k_z along the
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43 direction normal to the crystal’s surface—is still lacking.
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46 In this work, by combining density functional theory (DFT) calculations together with
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49 high-resolution ARPES, we have carefully performed a systematic study of the electronic band
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52 structure of the hourglass semimetal candidate Nb_3SiTe_6 . By conducting mappings with respect
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55 to the momentum k_z parallel to the crystal’s surface normal, we have observed a downward
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58 dispersing band near the Fermi level that is the lower part of hourglass fermion bands, as
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4 inferred from our DFT calculations. The observed band shapes strongly support Nb_3SiTe_6 as
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7 an hourglass semimetal candidate. Moreover, our careful k_z band mappings indicate that the
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10 nodal line associated with these hourglass dispersions is periodic every two Brillouin zones
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13 (BZs), as verified by our DFT calculations of the spectral function. Also, a saddle-like Fermi
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16 surface has been mapped, which supports prior evidence from transport^{28,29,30,31} for the
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19 dominance of hole carriers in the system's electronic properties. Lastly, *in situ* K doping of
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22 Nb_3SiTe_6 during ARPES facilitated the examination of other band crossings and parabolic
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25 bands at the zone center that are associated with nodal loop dispersions. Our results not only
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28 provide compelling indications of hourglass fermions in Nb_3SiTe_6 but also suggest that these
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31 hourglass fermions must figure prominently in the physics of Nb_3SiTe_6 by virtue of their
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34 proximity to the system's Fermi level, rendering Nb_3SiTe_6 an intriguing candidate for
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37 topological device applications.

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40 As shown in Fig. 1(a), the orthorhombic unit cell for Nb_3SiTe_6 consists of two
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43 van-der-Waals-bonded layers, each of which contains a Nb-Si atomic sheet sandwiched in
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46 between two puckered-hexagonal atomic layers of Te. The stacking between the unit cell's
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49 component layers is of the AB-type. That is, the four Te layers are in an AABB stacking pattern
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52 along the (001) direction of the unit cell, suggestive of the system's glide mirror symmetry.
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55 The bulk lattice is assembled by vertically stacking many unit cells on top of one another with
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58 van der Waals bonding between layers. For reference, Fig. 1(b) displays the orthorhombic bulk
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4 BZ along with its (001)-projected surface BZ with key high-symmetry points indicated.
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7 Topographic images of *in situ* cleaved Nb₃SiTe₆ single crystals, as obtained from scanning
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10 tunneling microscopy (STM), confirmed both the atomic structure and high crystallinity of the
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13 probed surfaces [Fig. 1(c)]. First-principles calculations of the bulk band structure for Nb₃SiTe₆
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16 [see Fig. 1(d)] yield two hourglass-like band dispersions near $E = 0$ eV and $E = -0.4$ eV
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19 [marked as α and γ , respectively, in Fig. 1(d)], which correspond to two pairs of hourglass
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22 fermions. Near the zone center, another set of bands with a nodal loop dispersion is evident
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25 along ΓY in the theoretical band structure [identified as β in Fig. 1(d)], whose lower half
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28 converges at the zone center to form a saddle-like surface in energy-momentum space [labelled
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31 as s in Fig. 1(d)]; the gap opening in these hourglass bands is due to glide-mirror symmetry
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34 breaking. The Fermi surface of Nb₃SiTe₆ itself is generally saddle-shaped with a local
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37 minimum along ΓY and a local maximum along ΓX [Fig. 1(e)], and the hourglass fermion band
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40 crossings along $X S$ [identified as α and γ in Fig. 1(d)] connect to form a Dirac nodal loop in
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43 k -space in the $XSRU$ plane, centered about the zone boundary point S [see Fig. 1(f)].
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46 Representative ARPES results for the valence band structure of Nb₃SiTe₆ are summarized
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49 in Fig. 2. In Fig. 2(a), the Fermi surface contour map, taken over multiple BZs, displays a
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52 dumbbell-shaped contour centered about the zone center and with its long axis oriented along
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55 $\overline{\Gamma Y}$, while another open contour centered about the \overline{X} point arches along the zone boundary;
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58 the latter contour should be associated with a topological nodal line, as in Ta₃SiTe₆²⁷. Clearly,
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4 though the intensities of Fermi surface contours decrease markedly outside of the first BZ (FBZ)
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7 and are likely modulated by complex matrix element effects and photon-energy-dependent
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10 (k_z -dependent) cross sections³², such contours are nevertheless sharp and display a clear
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13 periodic pattern in k space over multiple BZs, indicative of the high single crystallinity of the
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16 measured Nb_3SiTe_6 sample [Fig. 2(a)], as confirmed by our X-ray diffraction results (see
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19 Supporting Information). Particularly, the dumbbell-shaped contour in the FBZ continuously
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22 connects with that of the next BZ along $\overline{\Gamma Y}$.
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25 Select momentum cuts through these dumbbell-shaped Fermi surface contours [Fig. 2(a)]
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28 at strategically chosen k_x and k_y , where k_x and k_y are momentum components parallel to $\overline{\Gamma X}$
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31 and $\overline{\Gamma Y}$, respectively, provide further support for both the periodicity and anisotropy of the
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34 system's electronic band structure, while illustrating rich photoemission matrix element effects
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37 in the measured band dispersions [Figs. 2(b)–2(e) and 3(a)]. Indeed, though ARPES intensities
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40 of states near the Fermi level in the FBZ are too intense for resolving band features
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43 [cuts 1 and 3, e.g., $k_x = k_y = 0 \text{ \AA}^{-1}$, in Figs. 2(b) and 2(d)], k -space cuts taken away from the
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46 sample's normal in other Brillouin zones [cuts 2 and 4, e.g., $k_x = 0.96 \text{ \AA}^{-1}$ and $k_y = -0.52 \text{ \AA}^{-1}$,
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49 in Figs. 2(c) and 2(e)] are highly illuminating: For cut 2 parallel to $\overline{\Gamma Y}$ [Fig. 2(c)], two
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52 parabolic bands opening upwards—a small one with its minimum at $E = \sim -0.02 \text{ eV}$ and another
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55 spanning the energy range $E = 0$ to -0.2 eV —are repeatedly observable at the zone centers of
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58 multiple Brillouin zones [see Fig. 2(c) from $k_y = -0.78$ to -1.82 \AA^{-1}]; however, for cut 4 parallel
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4 to $\overline{\Gamma X}$ [Fig. 2(e)], a large, holelike band centered about the zone center and with its apex at
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7 $E = \sim -0.02$ eV is instead discernible. These two results thus reveal a saddle-like surface in
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10 energy-momentum space, with its saddle point at the zone center at $E = \sim -0.02$ eV, as well as
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13 the dominance of holelike carriers to the crystal's electronic properties, consistent with the
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16 theoretical band structure [refer to bands marked by blue arrows in Fig. 1(d)] and prior
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19 observations from transport and the system's thermoelectric properties^{28,29,30,31}. Nevertheless,
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22 the predicted energy position of the saddle point is deeper in energy (at $E = \sim -0.1$ eV) than that
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25 observed in these measurements (at $E = \sim -0.02$ eV), likely attributable to slight doping of the
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28 Nb_3SiTe_6 crystal during its synthesis.

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34 Furthermore, the observation of this saddle-like surface is inherently tied to potential
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37 signatures of hourglass dispersions gapped by spin-orbit coupling (SOC) near the zone center
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40 of Nb_3SiTe_6 ²³, per our theoretical and experimental band structure comparisons [Figs. 1(d) and
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43 3(a)–3(c)]. Like Fig. 2(c) but now overlaid with theoretical band structures, Fig. 3(a) displays
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46 the band mapping for cut 2 indicated in the Fermi surface map of Fig. 2(a) (with $k_x = 0.96 \text{ \AA}^{-1}$),
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49 which is the cleanest cut parallel to $\overline{\Gamma Y}$ for observing and confirming the periodicity of one
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52 of the saddle-shaped surface's bands over multiple BZs [blue arrow in Fig. 3(a)]. Figures 3(b)
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55 and 3(c) summarize two-dimensional (2D) curvature results for ARPES spectra measured
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58 along $\overline{\Gamma Y}$ in the FBZ before and after *in situ* alkali doping, each superimposed with the
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associated DFT calculations of pure Nb_3SiTe_6 ³³. The results before and after alkali metal

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4 doping are quite clear [compare Figs. 3(b) and 3(c)]: Aside from effectively shifting all bands
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7 to deeper binding energies, alkali metal doping of the Nb_3SiTe_6 surface facilitates further
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10 identification of band features likely related to nodal loop bands [green arrow in each of
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13 Figs. 3(a) and 3(c)], namely, one giving rise to a band crossing at the \bar{Y} point [red arrow in
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16 Fig. 3(c)] and also the upward opening parabolic band of the saddle-like surface [blue arrow in
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19 each of Fig. 3(a) and 3(c)]. The photoemission intensity of the former is largely suppressed in
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22 the pristine case [Fig. 3(b)] but is visible in the alkali-doped system [red arrow in Fig. 3(c)],
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25 likely due to complex photoelectron diffraction effects and cross section variations of the
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28 probed bands. Overall, though the complete band dispersions of the hourglass fermions gapped
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31 by SOC are inaccessible through photoemission based upon our theoretical and experimental
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34 analysis, there is nevertheless evidence for nodal loop band dispersions located very close to
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37 the Fermi level [Figs. 3(a)–3(c)]²³, which have yet to be considered in the physics of hourglass
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40 semimetals and related systems^{24,26,27}.

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43 Besides candidate gapped hourglass bands close to the zone center, two other species of
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46 hourglass subbands with linear, Dirac-like dispersions near the BZ boundaries also appear in
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49 our ARPES data—one set very close to the Fermi level, the other buried at deeper binding
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52 energies from $E = -0.4$ to -0.6 eV [Figs. 1(d), 2(e), and 4(a)–4(c)]. A schematic diagram
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55 showing the relationships of these linear dispersions (along ΓX) to their partner hourglass band
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58 crossings (on the XS k -path) is displayed in Fig. 4(a). Evidently, like the presumed nodal loop
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 4 bands of the saddle-like surface, the ARPES intensities of these linear bands exhibit marked
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 7 photoemission matrix element effects, as captured by their modulations across the BZ in the
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 10 constant energy contour maps [Fig. 2(b)] and left-right intensity asymmetry in the band
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 13 mappings [Figs. 2(d), 2(e), and 4(c)]. All linear dispersions here are spin-polarized
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 16 [schematically indicated by thin aqua and blue arrows in Fig. 4(b)], as shown in the related
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 19 hourglass fermion system K₂HgSb^{11,24} and further unveiled in our theoretical calculations of
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 22 each linear band's spin texture (with spin projection taken along the k_y -direction or parallel to
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 25 $\overline{\Gamma Y}$) [Fig. 4(d)]. (See also Section 5 in the Supporting Information.) Specifically, for each
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 28 Dirac-like point, the two partner bands possess opposite spin polarizations relative to one
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 31 another, which all taken together contribute no net current flow over the BZ¹¹. Consequently,
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 34 such hourglass systems have been dubbed glide-symmetric analogs of the quantum spin Hall
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 37 (QSH) state—or more aptly, so-called double QSH systems per the two species of linear band
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 40 crossings [Figs. 4(b) and 4(c)]^{11,24,34}. Thus far, experimental signatures of a double QSH state
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 43 have only appeared in transport measurements of K₂HgSb³⁴ but clearly, in the case of Nb₃SiTe₆,
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 46 our theoretical calculations of spin textures around the \overline{X} point now also suggest that Nb₃SiTe₆
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 49 is a candidate double QSH system [Fig. 4(d)].

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 52 However, in Nb₃SiTe₆, the two sets of linear bands also exhibit distinct, divergent
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 55 behaviors in their spin polarizations [Fig. 4(d)] (see Section 5 in the Supporting Information):
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 58 For bands at deeper binding energies [aqua arrows in Figs. 4(b) and 4(c)], the linear dispersions
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4 exhibit strong spin polarization, while for those nearest the Fermi level [blue arrows in Figs. 4(b)
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7 and 4(c)], there exists two subbands with an energy splitting of ~ 20 meV and very closely
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10 spaced spin-polarized bands near the Fermi level, though all linear subbands here are more
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13 clearly spin-polarized at deeper binding energies (starting from $E \sim -0.075$ eV). Therefore, due
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16 to the expected small energy splitting between subbands and the marked superpositions of spin
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19 polarizations near the Fermi level around the \bar{X} points, a spin-resolved transport measurement
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22 might be unable to identify a clear double QSH state in Nb_3SiTe_6 . Nevertheless, this
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25 observation certainly does not discount the importance of these linear band crossings to the
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28 system's nontrivial band topology²³. Indeed, in a recent transport study of Nb_3SiTe_6 , a
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31 nontrivial Berry phase has been found via Shubnikov-de Haas oscillation measurements³⁰,
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34 which can be readily attributed to the linear subbands of the hourglass fermions and their
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37 unusual spin textures about the \bar{X} points. Spin-resolved ARPES measurements would be
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40 helpful for probing the spin textures of these linear subbands in the future.

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43 Lastly, because the band structure of Nb_3SiTe_6 should exhibit dispersion along the
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46 k_z -direction or the surface normal direction, as evidenced by the predicted hourglass bands
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49 along the XS k -path [Fig. 1(f)], band mappings under varying incident photon energy were
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52 undertaken to directly probe hourglass fermions' band dispersions in Nb_3SiTe_6 . As revealed in
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55 the Fermi surface mapping in the k_x - k_z plane [Fig. 4(e)], where k_x and k_z are momentum
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58 components parallel to the $\bar{\Gamma X}$ and [001] directions, respectively, the linear subbands nearest
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4 the Fermi level at the \bar{X} point [Figs. 4(a)–4(d)] give rise to a continuous line along XS, though
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7 the photoemission intensity itself varies but peaks every 2 BZs [Fig. 4(e)]. These periodic
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10 intensity variations are attributable to the weak van der Waals bonding between neighboring
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13 Nb_3SiTe_6 layers, consistent with prior findings from ARPES mappings of the related hourglass
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16 semimetal Ta_3SiTe_6 ²⁷. Moreover, this periodicity is readily captured in our theoretical spectral
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19 function of Nb_3SiTe_6 along XS calculated over multiple BZs, once DFT results are unfolded
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22 according to the BZ of $1T\text{NbTe}_2$ [Fig. 5(a)]. Such experimental and theoretical results suggest
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25 that the spectral weights of hourglass bands near the Fermi level [nodal point indicated by a
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28 red arrow in Fig. 5(a)] should vary periodically every 2 BZs [Figs. 4(e) and 5(a)].
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31 Furthermore, since the energy splitting between hourglass bands near the Fermi level is
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34 often very small [~ 20 – 50 meV, per Figs. 1(d) and 5(a)], 2D curvature data processing³³ of
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37 k_z -dependent band mappings around the \bar{X} point was employed to search for hourglass bands
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40 with characteristic dispersions along the XS k -path [Figs. 5(b)–5(g)]. As shown in
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43 Figs. 5(b) and 5(c), 2D curvature band mappings along XS exhibit a downward dispersing band
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46 with an apex at the S point, which corresponds quite well with an hourglass band found in the
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49 theoretical data [Fig. 5(a)]; the experimental results confirm that only half of the hourglass-like
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52 structure is accessible by photoemission [Figs. 5(a)–5(c)]. Even so, although the hourglass
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55 nodal point near $E = \sim 0$ eV is not discernible in the measured mappings [compare
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58 Fig. 5(a) to Figs. 5(b) and 5(c)], the observed downward band is certainly direct evidence for
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4 hourglass physics [Figs. 5(a)–5(c)] and importantly a Dirac nodal curve in Nb_3SiTe_6 , as
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6 confirmed by 2D curvature mappings around the \bar{X} point taken along $\bar{\Gamma\bar{X}}$ at judiciously
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8 chosen k_z [Figs. 5(d)–5(g)]. Undoubtedly, the apex of the Dirac-like band crossing structure
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10 near the Fermi level varies as a function of k_z , shifting by about $\sim+20$ meV (~-20 meV) to lower
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12 (higher) binding energies as k_z is continuously tuned from the X to S (S to X) points
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14 [Figs. 5(b)–5(g)]. While Ta_3SiTe_6 and the related system $\text{NbSi}_{0.45}\text{Te}_2$ have been measured very
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16 recently by ARPES^{26,27}, this Dirac nodal curve along XS and more generally all dispersions
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18 along XS of X_3SiTe_6 ($X = \text{Ta}, \text{Nb}$) have not been reported yet^{26,27}. However, the strongest and
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20 most direct evidence for hourglass physics in Nb_3SiTe_6 is provided by studying bands along
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22 XS, as in Figs. 4(e)–5(g).

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34 Altogether, our comprehensive photoemission and theoretical study of bulk Nb_3SiTe_6
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36 single crystal provides direct evidence for the existence of hourglass fermions as well as
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38 unconventional spin textures in Nb_3SiTe_6 . Specifically, the observation of a saddle-shaped
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40 surface in the measured band mappings and Fermi surface supports the existence of nodal loop
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42 dispersions near the zone center, in corroboration with prior transport works²⁸. Additionally,
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44 the identification of two species of Dirac-like, linear band crossings at the \bar{X} point, together
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46 with their theoretical spin-resolved band structures, support a scenario for an exotic double
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48 QSH state in Nb_3SiTe_6 , previously only discovered in the hourglass semimetal KHgSb ³⁴.
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58 Furthermore, our photon-energy-dependent or k_z -dependent mappings along XS—never
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4 undertaken in any ARPES work on the orthorhombic family of $X_3\text{SiTe}_6$ ($X = \text{Ta}, \text{Nb}$) single
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7 crystals^{26,27}—have unveiled an hourglass band that is a Dirac nodal curve, based upon our DFT
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10 results and experimental data. Though only half of an hourglass-like structure is accessible
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13 through photoemission, the k_z -dependent band maps nonetheless suggest that hourglass
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16 fermions must contribute to the electronic properties of Nb_3SiTe_6 due to the proximity of their
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19 band structures near the Fermi level. All in all, our work not only provides future impetus in
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22 the identification of even more unusual topological materials but also identifies Nb_3SiTe_6 as a
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25 candidate system harboring unconventional spin textures accessible to spintronic applications.
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28 **ASSOCIATED CONTENT**

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31 Supporting Information: Additional information about the sample preparation, the
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34 experimental setup, the DFT calculation details, XRD measurement, XPS measurement, and
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37 spin-resolved DFT calculations.
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40 **AUTHOR INFORMATION**

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52 **Author Contributions**

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4 RYL, MKL, PC, and JAH performed ARPES measurements at the ALS or NSRRC, where JD
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6
7 and CMC provided technical help during beamline operations. AH and HTJ performed
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10 theoretical calculations. RS synthesized the single crystal. SCW performed XRD
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13 measurements. CCS and TMC performed STM measurements. RYL and TCC analyzed the
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16 data, interpreted the results, and wrote the first draft. All coauthors contributed to discussions
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19 and improvements that led to the final version of the manuscript.
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REFERENCES

- (1) Fu, L.; Kane, C. L.; Mele, E. J. Topological Insulators in Three Dimensions. *Phys. Rev. Lett.* **2007**, *98* (10), 106803.
- (2) *Topological Matter*; Bercioux, D., Cayssol, J., Vergniory, M. G., Reyes Calvo, M., Eds.; Springer Series in Solid-State Sciences; Springer International Publishing: Cham, 2018; Vol. 190.
- (3) Fu, L. Topological Crystalline Insulators. *Phys. Rev. Lett.* **2011**, *106*, 106802.
- (4) Shiozaki, K.; Sato, M. Topology of Crystalline Insulators and Superconductors. *Phys. Rev. B* **2014**, *90*, 165114.
- (5) Liu, Z. K.; Zhou, B.; Zhang, Y.; Wang, Z. J.; Weng, H. M.; Prabhakaran, D.; Mo, S. K.; Shen, Z. X.; Fang, Z.; Dai, X.; Hussain, Z.; Chen, Y. L. Discovery of a Three-Dimensional Topological Dirac Semimetal, Na₃Bi. *Science* **2014**, *343* (6173), 864–867.
- (6) Lin, C.-L.; Arafune, R.; Liu, R.-Y.; Yoshimura, M.; Feng, B.; Kawahara, K.; Ni, Z.; Minamitani, E.; Watanabe, S.; Shi, Y.; Kawai, M.; Chiang, T.-C.; Matsuda, I.; Takagi, N. Visualizing Type-II Weyl Points in Tungsten Ditelluride by Quasiparticle Interference. *ACS Nano* **2017**, *11*, 11459–11465.
- (7) Schnyder, A. P.; Ryu, S.; Furusaki, A.; Ludwig, A. W. W. Classification of Topological

- 1
2
3
4 Insulators and Superconductors in Three Spatial Dimensions. *Phys. Rev. B - Condens.*
5
6
7 *Matter Mater. Phys.* **2008**, 78, 195125.
8
9
- (8) Shiozaki, K.; Sato, M.; Gomi, K. Topology of Nonsymmorphic Crystalline Insulators
10
11 and Superconductors. *Phys. Rev. B* **2016**, 93, 195413.
12
13
14
- (9) Alexandradinata, A.; Wang, Z.; Bernevig, B. A. Topological Insulators from Group
15
16 Cohomology. *Phys. Rev. X* **2016**, 6 (2), 021008.
17
18
19
- (10) Feng, B.; Chan, Y. H.; Feng, Y.; Liu, R. Y.; Chou, M. Y.; Kuroda, K.; Yaji, K.;
20
21 Harasawa, A.; Moras, P.; Barinov, A.; Malaeb, W.; Bareille, C.; Kondo, T.; Shin, S.;
22
23 Komori, F.; Chiang, T. C.; Shi, Y.; Matsuda, I. Spin Texture in Type-II Weyl Semimetal
24
25 WTe_2 . *Phys. Rev. B* **2016**, 94, 195134.
26
27
28
- (11) Wang, Z.; Alexandradinata, A.; Cava, R. J.; Bernevig, B. A. Hourglass Fermions. *Nature*
29
30
31 **2016**, 532, 189–194.
32
33
34
- (12) Wieder, B. J.; Bradlyn, B.; Wang, Z.; Cano, J.; Kim, Y.; Kim, H. S. D.; Rappe, A. M.;
35
36 Kane, C. L.; Andrei Bernevig, B. Wallpaper Fermions and the Nonsymmorphic Dirac
37
38 Insulator. *Science* **2018**, 361 (6399), 246–251.
39
40
41
- (13) Bian, G.; Chang, T.-R.; Sankar, R.; Xu, S.-Y.; Zheng, H.; Neupert, T.; Chiu, C.-K.;
42
43 Huang, S.-M.; Chang, G.; Belopolski, I.; Sanchez, D. S.; Neupane, M.; Alidoust, N.;
44
45 Liu, C.; Wang, B.; Lee, C.-C.; Jeng, H.-T.; Zhang, C.; Yuan, Z.; Jia, S.; Bansil, A.; Chou,
46
47 F.; Lin, H.; Hasan, & M. Z. Topological Nodal-Line Fermions in Spin-Orbit Metal
48
49
50
51
52
53
54
55
56
57
58
59
60

- PbTaSe₂. *Nat. Commun.* **2016**, *7*, 10556.
- (14) Lv, B. Q.; Weng, H. M.; Fu, B. B.; Wang, X. P.; Miao, H.; Ma, J.; Richard, P.; Huang, X. C.; Zhao, L. X.; Chen, G. F.; Fang, Z.; Dai, X.; Qian, T.; Ding, H. Experimental Discovery of Weyl Semimetal TaAs. *Phys. Rev. X* **2015**, *5*, 031013.
- (15) Souma, S.; Wang, Z.; Kotaka, H.; Sato, T.; Nakayama, K.; Tanaka, Y.; Kimizuka, H.; Takahashi, T.; Yamauchi, K.; Oguchi, T.; Segawa, K.; Ando, Y. Direct Observation of Nonequivalent Fermi-Arc States of Opposite Surfaces in the Noncentrosymmetric Weyl Semimetal NbP. *Phys. Rev. B* **2016**, *93*, 161112.
- (16) Xu, S. Y.; Belopolski, I.; Alidoust, N.; Neupane, M.; Bian, G.; Zhang, C.; Sankar, R.; Chang, G.; Yuan, Z.; Lee, C. C.; Huang, S. M.; Zheng, H.; Ma, J.; Sanchez, D. S.; Wang, B. K.; Bansil, A.; Chou, F.; Shibayev, P. P.; Lin, H.; Jia, S.; Hasan, M. Z. Discovery of a Weyl Fermion Semimetal and Topological Fermi Arcs. *Science* **2015**, *349* (6248), 613–617.
- (17) Fu, B. B.; Yi, J.; Zhang, T. T.; Caputo, M.; Ma, J. Z.; Gao, X.; Lv, B. Q.; Kong, L. Y.; Huang, Y. B.; Richard, P.; Shi, M.; Strocov, V. N.; Fang, C.; Weng, H. M.; Shi, Y. G.; Qian, T.; Ding, H. Dirac Nodal Surfaces and Nodal Lines in ZrSiS. *Sci. Adv.* **2019**, *5* (5), eaau6459.
- (18) Takane, D.; Wang, Z.; Souma, S.; Nakayama, K.; Trang, C. X.; Sato, T.; Takahashi, T.; Ando, Y. Dirac-Node Arc in the Topological Line-Node Semimetal HfSiS. *Phys. Rev. B*

- 1
2
3
4 **2016**, *94*, 121108.
5
6
7 (19) Hosen, M. M.; Dimitri, K.; Aperis, A.; Maldonado, P.; Belopolski, I.; Dhakal, G.; Kabir,
8
9
10 F.; Sims, C.; Hasan, M. Z.; Kaczorowski, D.; Durakiewicz, T.; Oppeneer, P. M.;
11
12
13 Neupane, M. Observation of Gapless Dirac Surface States in ZrGeTe. *Phys. Rev. B* **2018**,
14
15
16 *97*, 121103.
17
18
19 (20) Hosen, M. M.; Dhakal, G.; Dimitri, K.; Maldonado, P.; Aperis, A.; Kabir, F.; Sims, C.;
20
21
22 Riseborough, P.; Oppeneer, P. M.; Kaczorowski, D.; Durakiewicz, T.; Neupane,
23
24
25 M. Discovery of Topological Nodal-Line Fermionic Phase in a Magnetic Material
26
27
28 GdSbTe. *Sci. Rep.* **2018**, *8* (1), 13283.
29
30
31 (21) Wang, Y.; Qian, Y.; Yang, M.; Chen, H.; Li, C.; Tan, Z.; Cai, Y.; Zhao, W.; Gao, S.;
32
33
34 Feng, Y.; Kumar, S.; Schwier, E. F.; Zhao, L.; Weng, H.; Shi, Y.; Wang, G.; Song, Y.;
35
36
37 Huang, Y.; Shimada, K.; Xu, Z.; Zhou, X. J.; Liu, G. Spectroscopic Evidence for the
38
39
40 Realization of a Genuine Topological Nodal-Line Semimetal in LaSbTe. *Phys. Rev. B*
41
42
43 **2021**, *103*, 125131.
44
45
46 (22) Yen, Y.; Chiu, C. L.; Lin, P. H.; Sankar, R.; Chuang, T. M.; Guo, G. Y. Dirac Nodal Line
47
48
49 and Rashba Spin-Split Surface States in Nonsymmorphic ZrGeTe. *New J. Phys.* **2021**,
50
51
52 *23* (10), 103019.
53
54
55 (23) Li, S.; Liu, Y.; Wang, S.-S.; Yu, Z.-M.; Guan, S.; Sheng, X.-L.; Yao, Y.; Yang, S.
56
57
58 A. Nonsymmorphic-Symmetry-Protected Hourglass Dirac Loop, Nodal Line, and Dirac
59
60

- 1
2
3
4 Point in Bulk and Monolayer Ta_3SiTe_6 ($X = Ta, Nb$). *Phys. Rev. B* **2018**, *97*, 045131.
5
6
7 (24) Ma, J.; Yi, C.; Lv, B.; Wang, Z.; Nie, S.; Wang, L.; Kong, L.; Huang, Y.; Richard, P.;
8
9
10 Zhang, P.; Yaji, K.; Kuroda, K.; Shin, S.; Weng, H.; Bernevig, B. A.; Shi, Y.; Qian, T.;
11
12
13 Ding, H. Experimental Evidence of Hourglass Fermion in the Candidate
14
15
16 Nonsymmorphic Topological Insulator $KHgSb$. *Sci. Adv.* **2017**, *3*, e1602415.
17
18
19 (25) Li, J.; Badding, M. E.; DiSalvo, F. J. Synthesis and Structure of Nb_3SiTe_6 , a New
20
21
22 Layered Ternary Niobium Telluride Compound. *J. Alloys Compd.* **1992**, *184*, 257–263.
23
24
25 (26) Yang, T. Y.; Wan, Q.; Yan, D. Y.; Zhu, Z.; Wang, Z. W.; Peng, C.; Huang, Y. B.; Yu,
26
27
28 R.; Hu, J.; Mao, Z. Q.; Li, S.; Yang, S. A.; Zheng, H.; Jia, J.-F.; Shi, Y. G.; Xu,
29
30
31 N. Directional Massless Dirac Fermions in a Layered van Der Waals Material with One-
32
33
34 Dimensional Long-Range Order. *Nat. Mater.* **2020**, *19*, 27–33.
35
36
37 (27) Sato, T.; Wang, Z.; Nakayama, K.; Souma, S.; Takane, D.; Nakata, Y.; Iwasawa, H.;
38
39
40 Cacho, C.; Kim, T.; Takahashi, T.; Ando, Y. Observation of Band Crossings Protected
41
42
43 by Nonsymmorphic Symmetry in the Layered Ternary Telluride Ta_3SiTe_6 . *Phys. Rev. B*
44
45
46 **2018**, *98*, 121111.
47
48
49 (28) Naveed, M.; Fei, F.; Bu, H.; Bo, X.; Shah, S. A.; Chen, B.; Zhang, Y.; Liu, Q.; Wei, B.;
50
51
52 Zhang, S.; Guo, J.; Xi, C.; Rahman, A.; Zhang, Z.; Zhang, M.; Wan, X.; Song,
53
54
55 F. Magneto-Transport and Shubnikov-de Haas Oscillations in the Layered Ternary
56
57
58 Telluride Topological Semimetal Candidate Ta_3SiTe_6 . *Appl. Phys. Lett.* **2020**, *116* (9),
59
60

- 1
2
3
4 92402.
5
6
7 (29) Hu, J.; Liu, X.; Yue, C. L.; Liu, J. Y.; Zhu, H. W.; He, J. B.; Wei, J.; Mao, Z. Q.; Yu
8
9 Antipina, L.; Popov, Z. I.; Sorokin, P. B.; Liu, T. J.; Adams, P. W.; A Radmanesh, S.
10
11
12 M.; Spinu, L.; Ji, H. Enhanced Electron Coherence in Atomically Thin Nb₃SiTe₆. *Nat.*
13
14
15
16 *Phys.* **2015**, *11*, 471–476.
17
18
19 (30) An, L.; Zhang, H.; Hu, J.; Zhu, X.; Gao, W.; Zhang, J.; Xi, C.; Ning, W.; Mao, Z.; Tian,
20
21
22 M. Magnetoresistance and Shubnikov-de Haas Oscillations in Layered Nb₃SiTe₆ Thin
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43
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59
60
- (31) Pang, Y.; Rezaei, E.; Chen, D.; Li, S.; Jian, Y.; Wang, Q.; Wang, Z.; Duan, J.; Zebarjadi, M.; Yao, Y. Thermoelectric Properties of Layered Ternary Telluride Nb₃SiTe₆. *Phys. Rev. Mater.* **2020**, *4*, 094205.
- (32) Moser, S. An Experimentalist's Guide to the Matrix Element in Angle Resolved Photoemission. *J. Electron Spectros. Relat. Phenomena* **2017**, *214*, 29–52.
- (33) Zhang, P.; Richard, P.; Qian, T.; Xu, Y.-M.; Dai, X.; Ding, H. A Precise Method for Visualizing Dispersive Features in Image Plots. *Rev. Sci. Instrum.* **2011**, *82*, 043712.
- (34) Liang, S.; Kushwaha, S.; Gao, T.; Hirschberger, M.; Li, J.; Wang, Z.; Stolze, K.; Skinner, B.; Bernevig, B. A.; Cava, R. J.; Ong, N. P. A Gap-Protected Zero-Hall Effect State in the Quantum Limit of the Non-Symmorphic Metal KHgSb. *Nat. Mater.* **2019**, *18*, 443–447.

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4 **FIGURE CAPTIONS**
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7 **Figure 1. Atomic lattice structure and characterizing hourglass bands in Nb₃SiTe₆.**
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10 (a) Atomic structure of Nb₃SiTe₆. (b) Bulk BZ and (001)-projected surface BZ (gray rectangle).
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13 (c) Topographic image of an *in situ* cleaved Nb₃SiTe₆ surface ($V_s = -100$ mV, $I_t = 1500$ pA,
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16 10×10 nm², $T = 4.2$ K). The inset is the corresponding Fast Fourier Transform (FFT) of the
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19 topographic image. In the inset, the red rectangle marks the [001]-projected SBZ, while yellow
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22 circles indicate Bragg peaks from Te atoms in the topmost layer. (d) DFT band structure of
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25 Nb₃SiTe₆. Here, the label α and red arrows identify hourglass band dispersions along the XS
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28 k -path near the Fermi level, while hourglass bands gapped by SOC along YTZ close to the
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31 Fermi level are marked by the label β and a green arrow; the label γ and yellow arrows indicate
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34 hourglass bands at deeper binding energies, and the label s and blue arrows flag bands which
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37 form a saddle-shaped surface centered about the Γ point in energy-momentum space.
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40 (e) Panoramic view of the constant energy contours of Nb₃SiTe₆ in the first BZ (FBZ).
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43 (f) Schematic diagrams for the nodal loop in the XSRU plane (left, red oval) and band
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46 structures of the hourglass dispersion 1 (HD1) and hourglass dispersion 2 (HD2) along SX Γ
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49 (right) that give rise to the nodal loop. The nodal loop is formed by the band crossing points
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52 (red and yellow points in the right panel).
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4 **Figure 2. Fermi surface and band mappings of Nb₃SiTe₆.** (a) Fermi surface map of Nb₃SiTe₆.

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7 Here, the result is obtained by integrating the ARPES intensity within ± 10 meV of the Fermi
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9 level. Solid black lines correspond to BZ boundaries, where the lengths of $\overline{\Gamma X}$ and $\overline{\Gamma Y}$ are
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11 0.48 \AA^{-1} and 0.26 \AA^{-1} , respectively; the first BZ is at the top left corner (labelled FBZ), while
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13 strategically chosen momentum cuts used for obtaining ARPES band mappings are indicated
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15 by colored arrows. (b), (c) Measured band maps along cuts 1 and 2 in the Fermi surface map
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17 of (a), respectively [red and orange arrows in (a)]; both momentum cuts are parallel to $\overline{\Gamma Y}$.
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19 (d),(e) Experimental ARPES spectra along cuts 3 and 4 in the Fermi surface map of (a),
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21 respectively [green and blue arrows in (a)]; both momentum cuts are parallel to $\overline{\Gamma X}$, and the
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23 fat blue and aqua arrows in (e) identify two sets of Dirac-like, linear band crossings. In all
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25 mappings here, the incident photon energy is 60 eV.
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Figure 3. Candidate nodal loop bands before and after alkali-metal doping along $\overline{\Gamma Y}$.

(a) Band structure along cut 2 in Fig. 2(a) obtained using 60-eV photons; the mapping is overlaid with DFT results (red solid lines), and a nodal loop band structure (green arrow and label β) and the saddle-shaped surface (blue arrow and label s) are identified. (b),(c) 2D curvature results for band mappings along $\overline{\Gamma Y}$ before and after K doping, respectively, each taken using an incident photon energy of 100 eV and superimposed with DFT band structures (red solid lines). In (c), a band whose intensity is enhanced after K doping is identified (red arrow), and bands corresponding to the saddle-shape surface (blue arrow and label s) and the hourglass bands gapped by SOC (green arrow and label β) are indicated.

Figure 4. Constant energy contour maps and potential double QSH state in Nb₃SiTe₆.

(a) BZ and the schematic band structures (blue and aqua lines) of hourglass fermions and their partner linear subbands along the SX Γ k -path. (b),(c) Constant energy contour maps in the FBZ and band mapping along $\overline{\Gamma X}$, respectively, all taken using 70-eV photons. The integrated energy range in each map is 25 meV; in (b) and (c), aqua and blue arrows indicate two sets of linear bands near each of the \overline{X} points, while in (b), the red solid arrow indicates a momentum cut corresponding to the ARPES spectra in (c). (d) Spin-resolved DFT band structures for the two linear band crossings at the \overline{X} point with spin-polarization projection taken along the k_y -direction or $\overline{\Gamma Y}$. (e) Fermi surface mapping in the k_x - k_z plane obtained by integrating the ARPES intensity within ± 25 meV of the Fermi level, where k_x and k_z are momentum components parallel to the $\overline{\Gamma X}$ and [001] directions, respectively; BZ boundaries are labelled along the left axis and/or identified by black lines.

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4 **Figure 5. k_z -dependent band mappings of hourglass fermion dispersions.** (a) DFT band
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6 structure results along the XS k -path; the nodal point of the hourglass fermion in the middle of
7 XS is marked by a red arrow, and the dashed red rectangles identify both the BZ boundaries
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9 and possible regions of interest for k_z -dependent mappings of hourglass bands near the Fermi
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11 level. (b) 2D curvature map corresponding to the k_z -dependent spectra taken at the \bar{X} point;
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13 here, k_z is varied from around 4.0 to 4.5 \AA^{-1} . (c) Similar to (b) but for k_z taken from around 4.5
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15 to 5.0 \AA^{-1} . (d)–(g) 2D curvature band mappings along $\bar{\Gamma\bar{X}}$ measured near \bar{X} for $k_z = 4.0, 4.23,$
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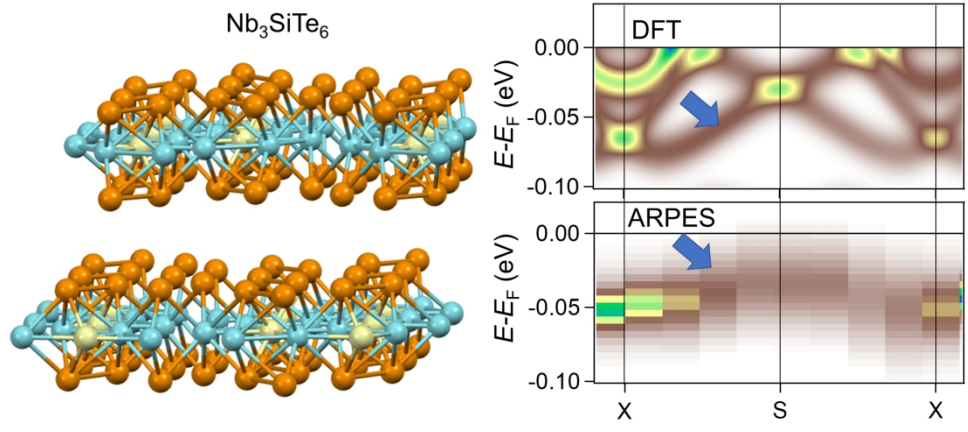


Table of Contents Graphic
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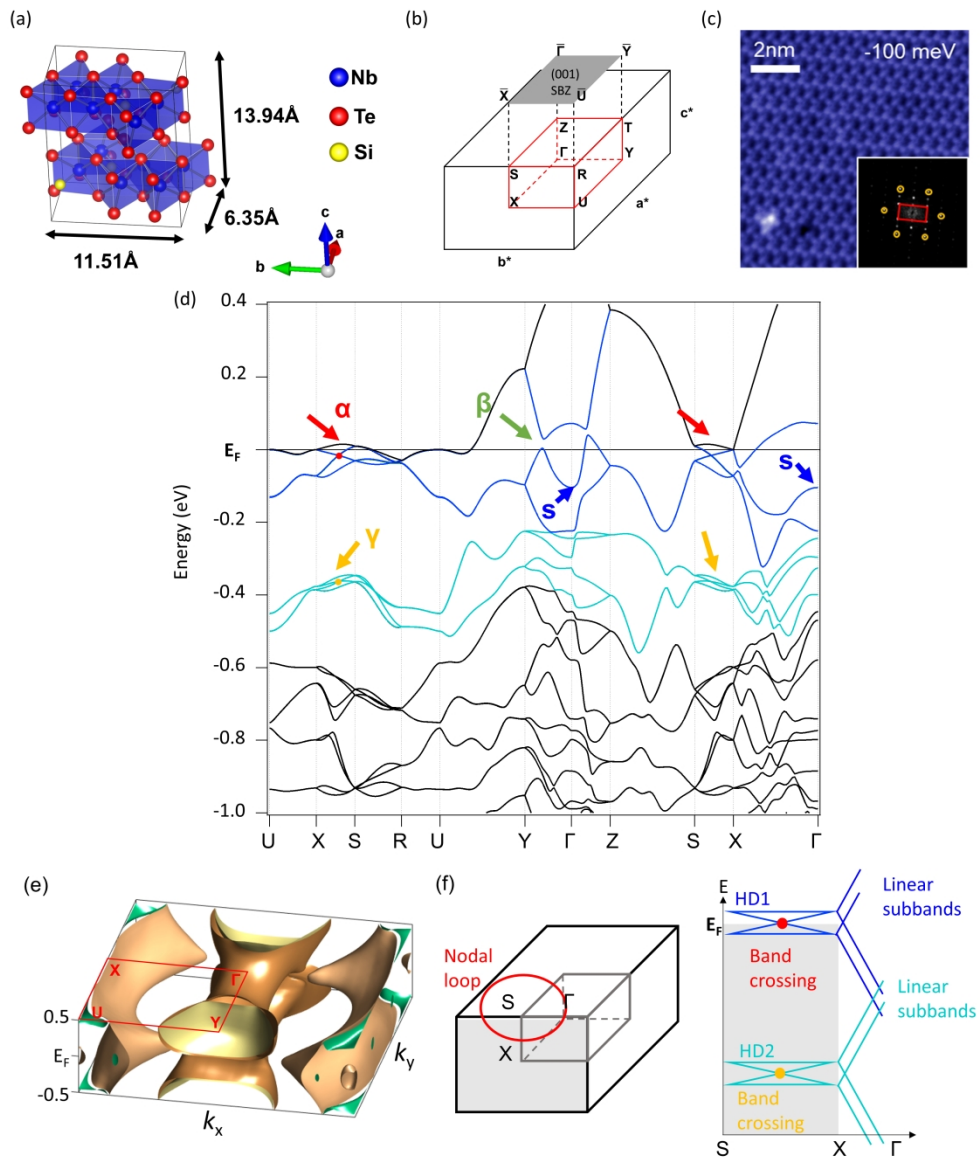


Figure 1.

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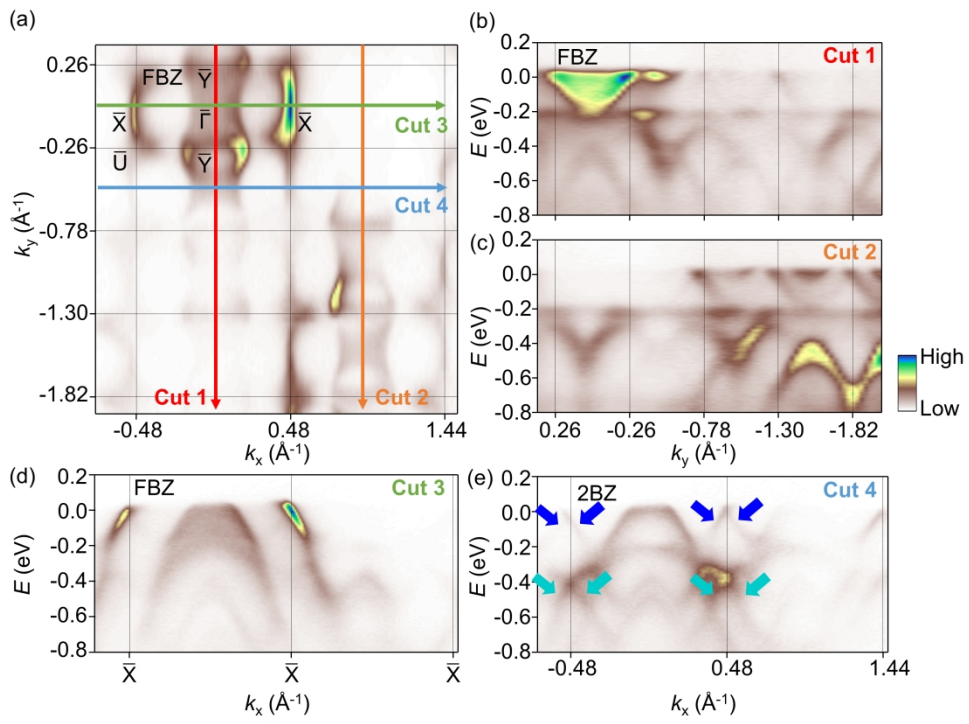


Figure 2.

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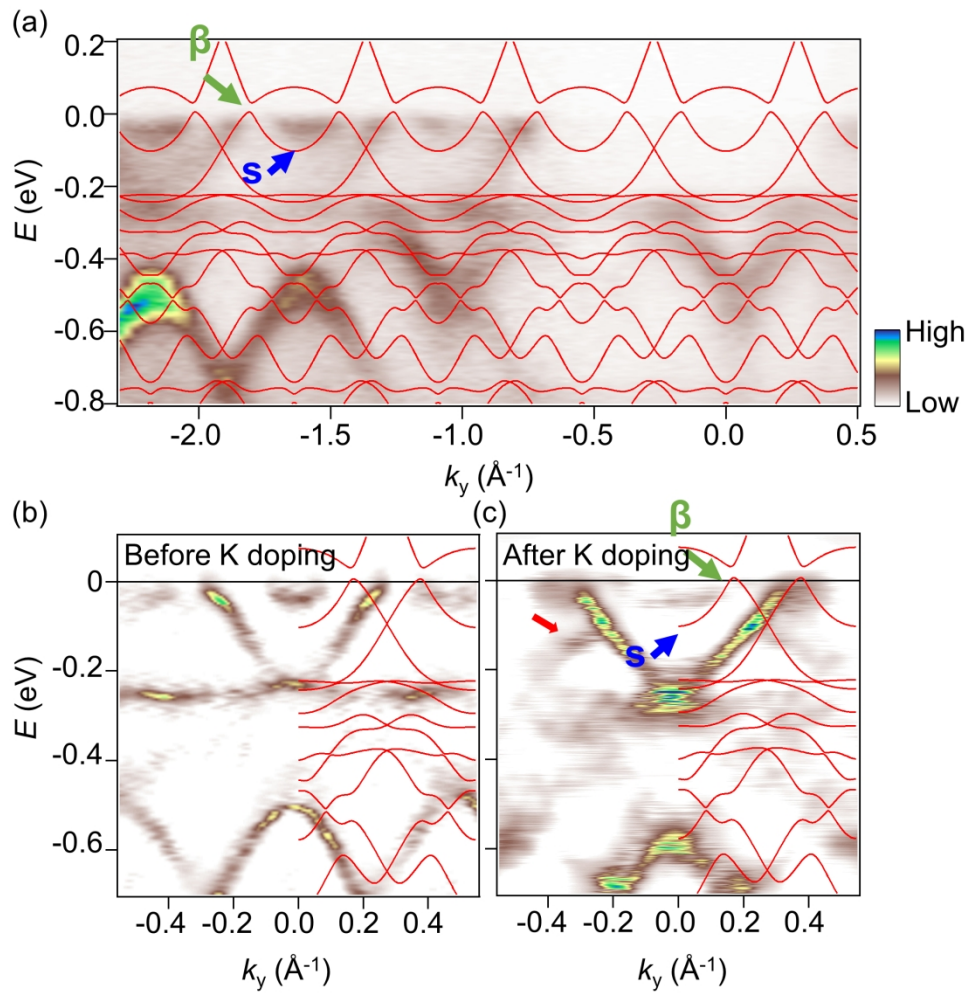


Figure 3.

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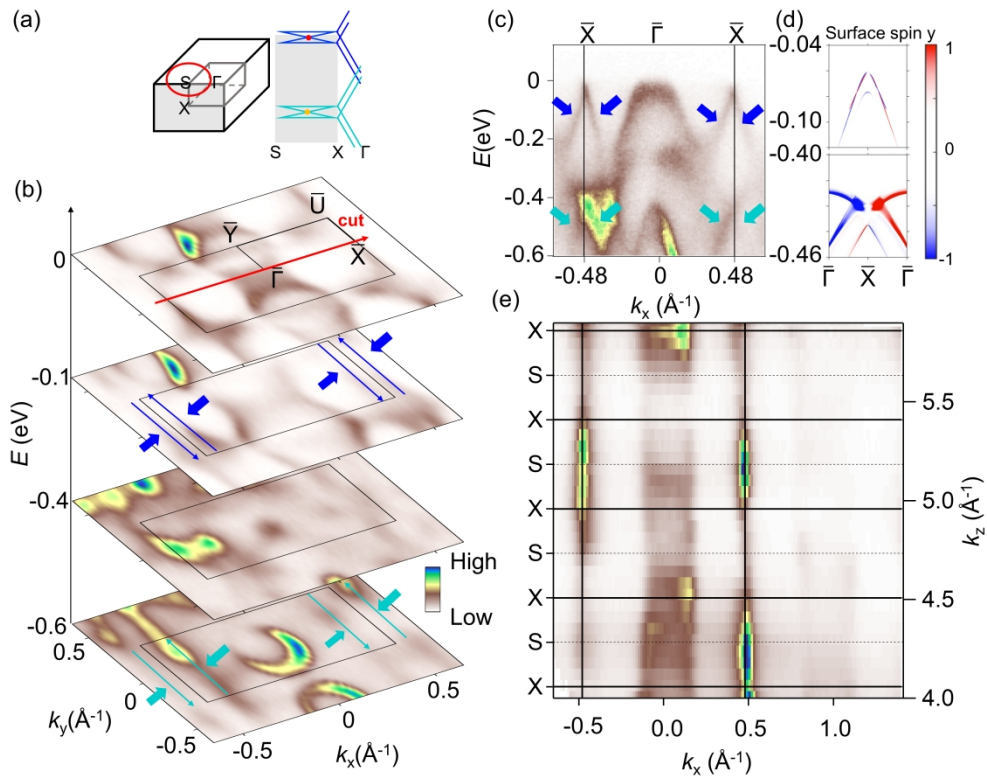


Figure 4.

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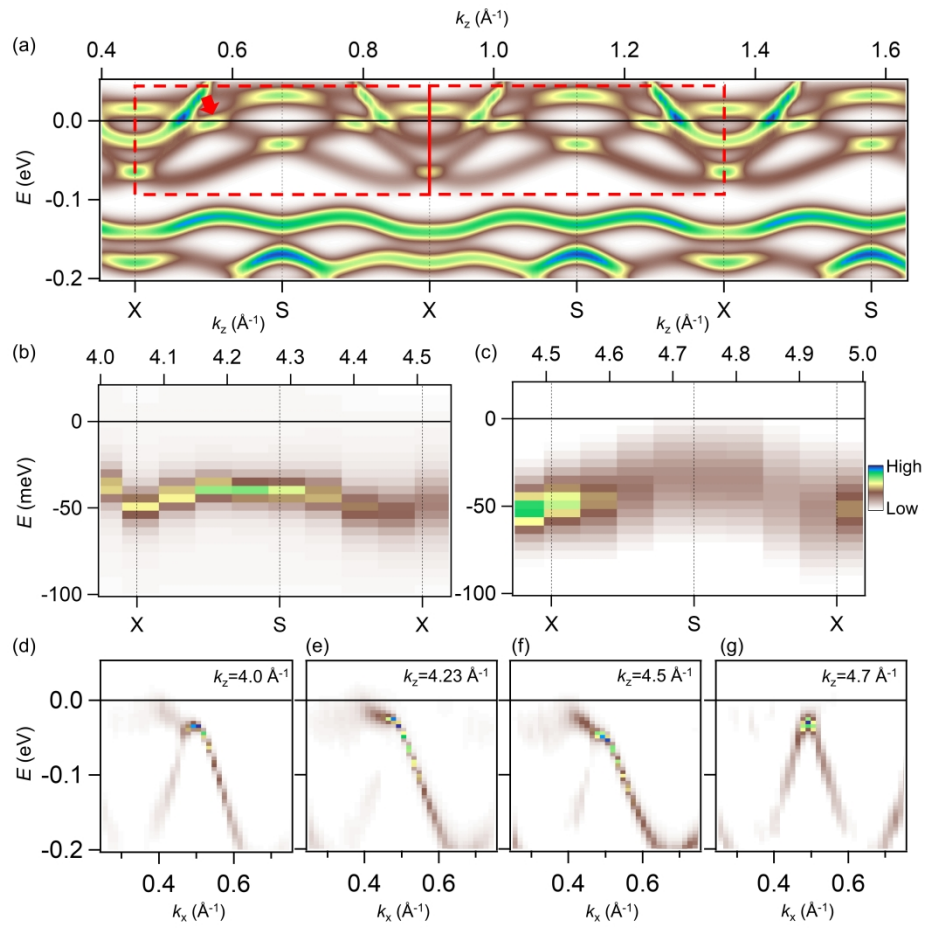


Figure 5.

363x345mm (300 x 300 DPI)