UC Berkeley

UC Berkeley Previously Published Works

Title

Urban Spatial Order: Street Network Orientation, Configuration, and Entropy

Permalink

<https://escholarship.org/uc/item/5nx408q3>

Journal

Applied Network Science, 4(1)

ISSN

2364-8228

Author

Boeing, Geoff

Publication Date

2019-08-23

DOI

10.1007/s41109-019-0189-1

Peer reviewed

RESEARCH

Open Access

Urban spatial order: street network orientation, configuration, and entropy

Geoff Boeing

Correspondence: boeing@usc.edu
Department of Urban Planning and
Spatial Analysis, Sol Price School of
Public Policy, University of Southern
California, 201B Lewis Hall, Los
Angeles, California 90089-0626, USA

Abstract

Street networks may be planned according to clear organizing principles or they may evolve organically through accretion, but their configurations and orientations help define a city's spatial logic and order. Measures of entropy reveal a city's streets' order and disorder. Past studies have explored individual cases of orientation and entropy, but little is known about broader patterns and trends worldwide. This study examines street network orientation, configuration, and entropy in 100 cities around the world using OpenStreetMap data and OSMnx. It measures the entropy of street bearings in weighted and unweighted network models, along with each city's typical street segment length, average circuitry, average node degree, and the network's proportions of four-way intersections and dead-ends. It also develops a new indicator of orientation-order that quantifies how a city's street network follows the geometric ordering logic of a single grid. A cluster analysis is performed to explore similarities and differences among these study sites in multiple dimensions. Significant statistical relationships exist between city orientation-order and other indicators of spatial order, including street circuitry and measures of connectedness. On average, US/Canadian study sites are far more grid-like than those elsewhere, exhibiting less entropy and circuitry. These indicators, taken in concert, help reveal the extent and nuance of the grid. These methods demonstrate automatic, scalable, reproducible tools to empirically measure and visualize city spatial order, illustrating complex urban transportation system patterns and configurations around the world.

Introduction

Spatial networks such as streets, paths, and transit lines organize the human dynamics of complex urban systems. They shape travel behavior, location decisions, and the texture of the urban fabric (Jacobs 1995; Levinson and El-Geneidy 2009; Parthasarathi et al. 2015). Accordingly, researchers have recently devoted much attention to street network patterns, performance, complexity, and configuration (Barthelemy et al. 2013; Batty 2005a; Boeing 2018a; Buhl et al. 2006; Chan et al. 2011; Ducruet and Beauguitte 2014; Jiang et al. 2014; Jiang and Claramunt 2004; Marshall 2004; Masucci et al. 2013; Nilsson and Gil 2019; Tsio-tas and Polyzos 2018; Wang 2015). In these spatial networks, entropy has deep theoretical connections with complexity (Batty 2005b; Batty et al. 2014). One research stream has explored the nature of entropy and order in urban street networks, seeking to quantify patterns of spatial order and disorder in urban circulation systems (Gudmundsson and Mohajeri 2013; Li et al. 2018; Mohajeri et al. 2013a, 2013b; Mohajeri and Gudmundsson 2012, 2014; Yeh and Li 2001).

Theories of urban order span sociological frameworks of physical-social disorder (e.g., “broken windows” theory), to public health goals of opening-up and sanitizing pathogenic urban spaces, to city planners’ pursuit of functional differentiation and regulation (Boyer 1983; Hatuka and Forsyth 2005; Mele 2017; O’Brien et al. 2019; Park and Burgess 1925; Xu 2008). This study considers the spatial logic and geometric ordering that arise through street network orientation. A city’s development eras, design paradigms, underlying terrain, culture, and local economic conditions influence the pattern, topology, and grain of its street networks (Jackson 1985; Kostof 1991). These networks in turn structure the human interactions and transportation processes that run along them, forming an important pillar of city planners’ quest for spatial order (Rose-Redwood and Bigon 2018). In particular, network orientation and geometry have played an out-sized role in urban planning since its earliest days (Smith 2007).

Measuring these network patterns can help researchers, planners, and community members understand local histories of urban design, transportation planning, and morphology; evaluate existing transportation system patterns and configurations; and explore new infrastructure proposals and alternatives. It also furthers the science of cities by providing a better understanding of urban patterns and how they correspond to evolutionary mechanisms, planning, and design. However, due to traditional data gathering challenges, this research literature has necessarily relied on small samples, limited geographies, and abstract indicators. Past studies have typically explored circuitry and entropy in individual or paired case studies—less is known about broader cross-sectional trends worldwide. How do street network configurations organize and order urban space in cities around the world?

This paper addresses this gap by empirically modeling and measuring order and configuration in 100 city street networks around the world, comprising over 4.8 million nodes and 3.3 million edges. It measures street network orientation entropy, circuitry, connectedness, and grain. It also develops a straightforward new indicator, the orientation-order ϕ , to quantify the extent to which a street network follows the spatial ordering logic of a single grid. It finds significant statistical relationships between city orientation and other indicators of spatial order (including street circuitry and connectedness). The most common orientation worldwide, even among cities lacking a strong grid, tends toward north-south-east-west. It also finds that American cities tend to be far more grid-like and less circuitous than cities elsewhere. Considered jointly, this collection of indicators helps reveal the extent and nuance of the grid around the world.

Background

Street network planning

The orthogonal grid, the most common planned street pattern, is often traced back to Hippodamus of Miletus (Mazza 2009; Paden 2001)—whom Aristotle labeled the father of city planning for his orthogonal design of Piraeus in ancient Greece—but archaeologists have found vestiges in earlier settlements around the world (Burns 1976; Stanislawski 1946). Mohenjo-Daro in the Indus Valley, dating to 2500 BCE, featured a north-south-east-west orthogonal grid (McIntosh 2007). Ancient Chinese urban design organized capital cities

around gridded patterns codified in the *Kao Gong Ji*, a scientific text from c. 500 BCE (Elman and Kern 2009). Teotihuacan featured an offset grid, dating to 100 BCE, that aligned with the Valley of Mexico's zenith sunrise (Peterson and Chiu 1987; Sparavigna 2017). The Roman Empire used standardized street grids to efficiently lay out new towns and colonies during rapid imperial expansion (Kaiser 2011). Many medieval towns were even planned around approximate, if distorted, grids possibly to maximize sun exposure on east-west streets during winter market days (Lilley 2001). In 1573, King Phillip II of Spain issued the Law of the Indies, systematizing how colonists sited new settlements and designed rectilinear gridded street networks around central plazas (Low 2009; Rodriguez 2005). In the US, many east coast cities planned their expansions around street grids, including Philadelphia in 1682, Savannah in 1733, Washington in 1791, and New York in 1811 (Jackson 1985; Sennett 1990). The subsequent US Homestead Act sweepingly organized the American interior according to the spatial logic of the gridiron (Boeing 2018b).

In the context of urban form, the concept of "spatial order" is fuzzy. Street networks that deviate from griddedness inherently possess different spatial logics and ordering principles (Karimi 1997; Southworth and Ben-Joseph 1995, 2004). Cities planned without a grid—as well as unplanned cities that grew through accretion—may lack clearly defined orientation order, but can still be well-structured in terms of complex human dynamics and land use (Hanson 1989). Specific visual/geometric order should not be confused for functional/social order (Roy 2005; Salingaros 1998; Smith 2007). Different design logics support different transportation technologies and appeal to different cultures and eras (Jackson 1985).

The grid has been used to express political power, promote military rule, improve cadastral legibility, foster egalitarianism, and encourage land speculation and development (Ellickson 2013; Groth 1981; Low 2009; Martin 2000; Mazza 2009; Rose-Redwood 2011; Sennett 1990). Many cities spatially juxtapose planned and unplanned districts or non-binarily intermingle top-down design with bottom-up self-organized complexity. Old cores may comprise organic patterns adjacent to later gridirons, in turn adjacent to later winding suburbs. Even previously highly-ordered urban cores can grow in entropy as later generations carve shortcuts through blocks, reorganize space through infill or consolidation, and adapt to shifting points of interest—all of which occurred in medieval Rome and Barcelona, for instance (Kostof 1991).

Street network modeling

Street networks are typically modeled as graphs where nodes represent intersections and dead-ends, and edges represent the street segments that link them (Barthelemy and Flammini 2008; Cardillo et al. 2006; Lin and Ban 2013; Marshall et al. 2018; Porta et al. 2006). These edges are spatially embedded and have both a length and a compass bearing (Barthelemy 2011). The present study models urban street networks as undirected nonplanar multigraphs with possible self-loops. While directed graphs most-faithfully represent constraints on flows (such as vehicular traffic on a one-way street), undirected graphs better model urban form by corresponding 1:1 with street segments (i.e., the linear sides of city blocks). While many street networks are approximately planar (having relatively few overpasses or underpasses), nonplanar graphs provide more accurate models by accommodating

those bridges and tunnels that do often exist (Boeing 2018c; Eppstein and Goodrich 2008).

The data to study these networks typically come from shapefiles of digitized streets. In the US, the Census Bureau provides TIGER/Line shapefiles of roads nationwide. In other countries, individual municipal, state, or federal agencies may provide similar data, however, digitization standards and data availability vary. Accordingly, cross-sectional research of street network orientation and entropy has tended to be limited to individual geographical regions or examine small samples. However, today, OpenStreetMap presents a new alternative data source. OpenStreetMap is a collaborative worldwide mapping project that includes streets, buildings, amenities, and other spatial features. Although its data quality varies somewhat between countries, in general its streets data are high quality, especially in cities (Barrington-Leigh and Millard-Ball 2017; Barron et al. 2014; Zielstra et al. 2013). This data source offers the opportunity to conduct cross-sectional research into street network form and configuration around the world.

Recently, scholars have studied street network order and disorder through circuitry and orientation entropy. The former measures street curvature and how this relates to other urban patterns and processes (Boeing 2019; Giacomini and Levinson 2015; Levinson and El-Geneidy 2009). The latter quantifies and visualizes the entropy of street orientations to assess how ordered they are (Courtat et al. 2011; Gudmundsson and Mohajeri 2013; Mohajeri et al. 2013a, 2013b; Mohajeri and Gudmundsson 2012, 2014), as entropy quantifies the fundamentally related concepts of disorder, uncertainty, and dispersion. Louf and Barthelemy (2014) explore city block geometries around the world as a function of block size and form factor, clustering them to identify differences between US and European cities. However, less is known about cross-sectional trends in the spatial orientation and ordering of street networks worldwide. This study builds on this prior research into circuitry, order, and entropy by drawing on OpenStreetMap data to examine cities around the world and explore their patterns and relationships.

Methods

Data

To better understand urban spatial order and city street network entropy, we analyze 100 large cities across North America, South America, Europe, Africa, Asia, and Oceania. Our sampling strategy emulates Louf and Barthelemy's (2014) to select cities through a balance of high population, regional significance, and some stratification to ensure geographical diversity within regions. Accordingly, this sample comprises a broad cross-section of different histories, cultures, development eras, and design paradigms. Of course, no single consistent definition of "city" or its spatial jurisdiction exists worldwide as these vary between countries for historical and political reasons. We aim for consistency by trying to use each study site's closest approximation of a "municipality" for the city limits. The lone exception is Manhattan, where we focus on one borough's famous grid instead of the amalgam of boroughs that compose New York City.

Once these study sites are defined, we use the OSMnx software to download the street network within each city boundary and then calculate several indicators. OSMnx is a free, open-source, Python-based toolkit to automatically download

spatial data (including municipal boundaries and streets) from OpenStreetMap and construct graph-theoretic objects for network analysis (Boeing 2017).

Analysis

For each city, we calculate the street network's edges' individual compass bearings with OSMnx using two different methods. The first method simplifies the topology of each graph such that nodes exist only at intersections and dead-ends; edges thus represent street segments (possibly curving, as full spatial geometry is retained) between them (ibid.). In this method, the bearing of edge e_{uv} equals the compass heading from u to v and its reciprocal (e.g., if the bearing from u to v is 90° then we additionally add a bearing of 270° since the one-dimensional street centerline points in both directions). This captures the orientation of street segments but ignores the nuances of mid-block curvature. To address this, the second method does not simplify the topology: edges represent OpenStreetMap's raw straight-line street segments, either between intersections or in chunks approximating curving streets. This method weights each edge's bearing by length to adjust for extremely short edges in these curve-approximations. In both methods, self-looping edges have undefined bearings, which are ignored.

Once we have calculated all of the bearings (and their reciprocals) for all the edges in a city, we divide them into 36 equal-sized bins (i.e., each bin represents 10°). To avoid extreme bin-edge effects around common values like 0° and 90° , we shift each bin by -5° so that these values sit at the centers of their bins rather than at their edges. This allows similar common bearings such as 359.9° and 0.1° to fall in the same bin as each other. Once the bearings are binned, we calculate the Shannon entropy, H , of the city's orientations' distribution (Shannon 1948). For each city's graph, we first calculate the entropy of the unweighted/simplified street orientations, H_o , as:

$$H_o = -\sum_{i=1}^n P(o_i) \log_e P(o_i) \quad (1)$$

where n represents the total number of bins, i indexes the bins, and $P(o_i)$ represents the proportion of orientations that fall in the i^{th} bin. We similarly calculate the entropy of the weighted/unsimplified street orientations, H_w , as:

$$H_w = -\sum_{i=1}^n P(w_i) \log_e P(w_i) \quad (2)$$

where n represents the total number of bins, i indexes the bins, and $P(w_i)$ represents the proportion of weighted orientations that fall in the i^{th} bin. While H_w is biased by the city's shape (due to length-weighting), H_o is not.

The natural logarithm means the value of H is in dimensionless units called "nats," or the natural unit of information. The maximum entropy, $H_{\max}$, that any city could have equals the logarithm of the number of bins: 3.584 nats. This represents the maximum entropy distribution, a perfectly uniform distribution of street bearings across all bins. If all the bearings fell into a single bin, entropy would be minimized and equal 0. However, given the undirected graph, the minimal theoretical entropy a street network could have (e.g., if all of its streets ran only north-south, thus falling evenly into two bins) would be 0.693 nats. But given the nature of the real world, a more plausible minimum would instead be an idealized city grid with all streets in four equal proportions (e.g., north-south-

east-west). This perfect grid entropy, H_g , would equal 1.386 nats. Therefore, we can calculate a normalized measure of orientation-order, ϕ , to indicate where a city stands on a linear spectrum from completely disordered/uniform to perfectly ordered/grid-like as:

$$\phi = 1 - \left(\frac{H_o - H_g}{H_{\max} - H_g} \right)^2 \quad (3)$$

Thus, a ϕ value of 0 indicates low order (i.e., perfect disorder and maximum entropy with a uniform distribution of streets in every direction) and a ϕ value of 1 indicates high order (i.e., a single perfectly-ordered idealized four-way grid and minimal possible entropy). Note that the value is squared to linearize its already normalized scale between 0 and 1, allowing us to interpret it as the *extent* to which a city is ordered according to a single grid. All remaining indicators' formulae use the (unweighted) simplified graph for the most faithful model of the urban form, geographically and topologically. We calculate each city's median street segment length $\bar{l}$, average node degree k (i.e., how many edges are incident to the nodes on average), proportion of nodes that are dead-ends P_{de} , and proportion of nodes that are four-way intersections P_{4w} . Finally, we calculate each city street network's average circuitry, ζ , as:

$$\zeta = \frac{L_{\text{net}}}{L_{\text{gc}}} \quad (4)$$

where L_{net} represents the sum of all edge lengths in the graph and L_{gc} represents the sum of all great-circle distances between all pairs of adjacent nodes. Thus, ζ represents how much more circuitous a city's street network is than it would be if all its edges were straight-line paths between nodes (Boeing 2019; Qureshi et al. 2002).

We visualize these characteristics and examine their statistical relationships to explore the nature of spatial order/disorder in the street networks' orientations, hypothesizing that more-gridded cities (i.e., higher ϕ values) have higher connectedness (i.e., higher node degrees, more four-way intersections, fewer dead-ends) and less-winding street patterns. Finally, to systematically interpret city similarities and differences, we cluster the study sites in a four-dimensional feature space of the key indicators of interest (k , ϕ , $\bar{l}$, and ζ), representing a cross-section of street network character. We first standardize the features for appropriate scaling, then perform hierarchical agglomerative clustering using the Ward linkage method with a Euclidean metric.

Results

Table 1 presents the indicators' values for each of the cities studied. We find that H_o and H_w are very strongly correlated (Pearson product-moment correlation coefficient $r > 0.99$, $p < 0.001$) and thus provide essentially redundant statistical information about these networks. Therefore, the remainder of these findings focus on H_o unless otherwise explicitly stated. Three American cities (Chicago, Miami, and Minneapolis) have the lowest orientation entropies of all the cities studied, indicating that their street networks are the most ordered. In fact, all 16 cities with the lowest entropies are in the US and Canada. Outside of the US/Canada, Mogadishu, Kyoto, and Melbourne have the lowest orientation entropies. Surprisingly, the city with the highest entropy, Charlotte,

Table 1 Resulting indicators for the 100 study sites

Region	City	ϕ	H_o	H_w	$\bar{t}$	$\mathcal{S}$	$\bar{k}$	P_{de}	P_{dw}
Asia/Oceania	Bangkok	0.105	3.465	3.452	64.6	1.059	2.385	0.360	0.108
	Beijing	0.335	3.177	3.206	177.5	1.053	2.985	0.135	0.241
	Hanoi	0.010	3.573	3.572	64.4	1.065	2.610	0.246	0.102
	Hong Kong	0.012	3.571	3.563	61.0	1.137	2.932	0.114	0.174
	Jakarta	0.167	3.391	3.347	52.8	1.065	2.741	0.175	0.096
	Kabul	0.076	3.499	3.510	79.3	1.062	2.673	0.226	0.130
	Karachi	0.088	3.485	3.493	71.3	1.032	3.027	0.095	0.216
	Kathmandu	0.054	3.523	3.500	63.3	1.071	2.595	0.234	0.089
	Kyoto	0.357	3.148	3.229	49.6	1.090	2.887	0.134	0.157
	Manila	0.062	3.514	3.484	63.5	1.023	3.141	0.095	0.347
	Melbourne	0.340	3.172	3.203	51.9	1.037	3.160	0.060	0.332
	Mumbai	0.075	3.499	3.476	68.9	1.081	2.705	0.211	0.136
	New Delhi	0.062	3.515	3.491	62.5	1.083	2.696	0.197	0.119
	Osaka	0.243	3.298	3.306	51.0	1.025	3.155	0.069	0.292
	Phnom Penh	0.324	3.193	3.235	81.6	1.040	2.784	0.205	0.188
	Pyongyang	0.024	3.557	3.568	132.4	1.097	2.524	0.294	0.120
	Seoul	0.009	3.573	3.573	53.5	1.048	3.011	0.101	0.205
	Shanghai	0.121	3.447	3.433	233.0	1.040	3.017	0.156	0.317
	Singapore	0.005	3.578	3.570	64.7	1.077	2.994	0.110	0.215
	Sydney	0.092	3.480	3.431	93.1	1.073	2.674	0.206	0.087
Europe	Taipei	0.158	3.402	3.428	73.5	1.068	3.096	0.110	0.305
	Tokyo	0.050	3.528	3.529	49.6	1.046	2.950	0.119	0.186
	Ulaanbaatar	0.058	3.519	3.463	88.7	1.065	2.486	0.283	0.061
	Amsterdam	0.071	3.504	3.488	65.8	1.080	2.897	0.146	0.205
	Athens	0.041	3.538	3.532	55.5	1.019	3.245	0.056	0.363
	Barcelona	0.108	3.462	3.460	78.1	1.052	3.135	0.078	0.303
	Berlin	0.011	3.572	3.570	113.1	1.040	3.002	0.118	0.259
	Budapest	0.050	3.528	3.516	93.0	1.032	3.037	0.096	0.231
	Copenhagen	0.029	3.552	3.551	78.0	1.048	2.881	0.146	0.194
	Dublin	0.024	3.557	3.541	71.5	1.061	2.492	0.279	0.068
	Glasgow	0.047	3.531	3.513	72.3	1.079	2.620	0.238	0.109
	Helsinki	0.006	3.577	3.571	42.0	1.063	2.348	0.395	0.134
	Kiev	0.014	3.568	3.554	125.1	1.053	2.813	0.164	0.160
	Lisbon	0.023	3.558	3.546	60.8	1.068	2.923	0.108	0.154
	London	0.015	3.566	3.564	70.3	1.061	2.561	0.251	0.070
	Madrid	0.019	3.562	3.553	62.5	1.050	3.079	0.065	0.210
	Moscow	0.007	3.576	3.573	130.5	1.055	2.999	0.074	0.170
	Munich	0.078	3.496	3.482	96.0	1.046	2.958	0.099	0.200
	Oslo	0.008	3.574	3.564	78.0	1.095	2.711	0.197	0.113
	Paris	0.016	3.566	3.568	71.5	1.023	3.110	0.050	0.240
	Prague	0.049	3.529	3.513	84.5	1.065	2.807	0.177	0.171
	Reykjavik	0.056	3.522	3.529	63.2	1.071	2.540	0.283	0.117
	Rome	0.005	3.578	3.578	73.7	1.070	2.820	0.161	0.145
	Sarajevo	0.039	3.540	3.558	94.7	1.133	2.522	0.270	0.078

Table 1 Resulting indicators for the 100 study sites (*Continued*)

Region	City	ϕ	H_o	H_w	$\bar{i}$	$\mathcal{S}$	$\bar{k}$	P_{de}	P_{dw}
Latin America	Stockholm	0.006	3.577	3.568	82.0	1.091	2.681	0.222	0.141
	Venice	0.017	3.564	3.553	23.2	1.090	2.474	0.300	0.073
	Vienna	0.050	3.528	3.515	90.4	1.043	2.985	0.122	0.244
	Warsaw	0.036	3.544	3.532	90.9	1.043	2.717	0.204	0.160
	Bogota	0.040	3.539	3.529	58.4	1.044	2.977	0.122	0.234
	Buenos Aires	0.151	3.411	3.423	104.8	1.011	3.548	0.027	0.576
	Caracas	0.029	3.551	3.564	95.3	1.148	2.710	0.217	0.145
	Havana	0.029	3.551	3.552	86.9	1.040	3.130	0.118	0.357
	Lima	0.278	3.254	3.228	76.7	1.017	3.161	0.040	0.331
	Mexico City	0.154	3.408	3.406	69.9	1.043	2.977	0.146	0.264
	Port au Prince	0.028	3.552	3.554	55.0	1.088	2.495	0.295	0.087
Middle East/Africa	Rio de Janeiro	0.014	3.568	3.566	74.0	1.055	2.804	0.172	0.147
	Sao Paulo	0.002	3.581	3.580	76.0	1.050	2.936	0.120	0.176
	Baghdad	0.083	3.490	3.498	68.3	1.033	3.043	0.050	0.144
	Beirut	0.206	3.344	3.308	63.9	1.026	3.061	0.072	0.218
	Cairo	0.041	3.538	3.526	66.6	1.067	2.996	0.085	0.171
	Cape Town	0.025	3.556	3.553	75.2	1.102	2.793	0.183	0.162
	Casablanca	0.094	3.477	3.461	48.0	1.048	3.026	0.080	0.178
	Damascus	0.043	3.536	3.525	65.8	1.085	2.801	0.146	0.107
	Dubai	0.031	3.550	3.529	79.7	1.087	2.925	0.074	0.073
	Istanbul	0.007	3.576	3.574	50.1	1.059	2.998	0.093	0.174
	Jerusalem	0.014	3.568	3.562	44.0	1.092	2.735	0.180	0.109
US/Canada	Johannesburg	0.019	3.562	3.556	88.6	1.098	2.865	0.158	0.182
	Lagos	0.039	3.540	3.521	87.2	1.048	2.619	0.223	0.070
	Mogadishu	0.375	3.123	3.292	39.4	1.019	3.346	0.055	0.472
	Nairobi	0.014	3.568	3.556	91.8	1.083	2.506	0.279	0.075
	Tehran	0.137	3.427	3.405	52.0	1.045	2.652	0.240	0.134
	Atlanta	0.315	3.204	3.197	112.5	1.074	2.806	0.164	0.153
	Baltimore	0.223	3.324	3.367	100.0	1.036	3.182	0.085	0.360
	Boston	0.026	3.554	3.552	77.0	1.039	2.945	0.135	0.211
	Charlotte	0.002	3.582	3.581	117.2	1.067	2.546	0.288	0.139
	Chicago	0.899	2.083	2.103	105.3	1.016	3.343	0.074	0.507
	Cleveland	0.486	2.961	2.899	103.7	1.029	2.979	0.091	0.198
	Dallas	0.305	3.218	3.182	106.1	1.042	3.120	0.091	0.317
	Denver	0.678	2.634	2.571	102.7	1.031	3.249	0.071	0.416
	Detroit	0.582	2.807	2.718	101.2	1.012	3.352	0.053	0.482
	Honolulu	0.034	3.545	3.550	101.8	1.073	2.681	0.252	0.185
	Houston	0.425	3.052	3.006	96.2	1.045	3.027	0.127	0.307
	Las Vegas	0.542	2.874	2.775	86.1	1.079	2.676	0.230	0.166
	Los Angeles	0.348	3.161	3.145	109.9	1.048	2.911	0.171	0.273
	Manhattan	0.669	2.650	2.571	82.2	1.017	3.508	0.027	0.572
	Miami	0.811	2.341	2.291	96.7	1.023	3.236	0.069	0.407
	Minneapolis	0.749	2.486	2.464	115.4	1.023	3.393	0.053	0.521
	Montreal	0.204	3.346	3.332	87.4	1.057	3.239	0.051	0.344

Table 1 Resulting indicators for the 100 study sites (*Continued*)

Region	City	ϕ	H_o	H_w	$\bar{l}$	ζ	$\bar{k}$	P_{de}	P_{4w}
	New Orleans	0.123	3.444	3.457	99.6	1.035	3.378	0.077	0.526
	Orlando	0.481	2.969	2.929	100.1	1.064	2.914	0.120	0.237
	Philadelphia	0.312	3.209	3.267	83.9	1.030	3.315	0.047	0.398
	Phoenix	0.586	2.801	2.563	97.1	1.073	2.795	0.186	0.171
	Pittsburgh	0.018	3.564	3.565	94.0	1.054	2.854	0.173	0.231
	Portland	0.679	2.632	2.680	82.1	1.041	3.032	0.146	0.327
	San Francisco	0.278	3.253	3.226	94.4	1.033	3.304	0.087	0.454
	Seattle	0.723	2.542	2.474	97.2	1.028	3.107	0.136	0.369
	St Louis	0.276	3.256	3.225	107.0	1.023	3.165	0.098	0.374
	Toronto	0.474	2.980	2.885	103.1	1.090	2.994	0.109	0.217
	Vancouver	0.749	2.488	2.413	103.7	1.022	3.308	0.073	0.455
	Washington	0.377	3.121	3.113	99.5	1.038	3.252	0.065	0.370

ϕ is the orientation-order indicator, H_o represents street orientation entropy, H_w represents weighted street orientation entropy, $\bar{l}$ represents median street segment length (meters), ζ represents average circuitry, $\bar{k}$ represents average node degree, P_{de} represents the proportion of nodes that are dead-ends, and P_{4w} represents the proportion of nodes that are four-way intersections

is also in the US. São Paulo and Rome immediately follow it as the next highest cities. Chicago, the most ordered city, has a ϕ of 0.90, while Charlotte, the most disordered, has a ϕ of 0.002. Recall that a ϕ of 0 indicates a uniform distribution of streets in every direction and a ϕ of 1 indicates a single perfectly-ordered grid. Charlotte's and São Paulo's street orientations are nearly perfectly disordered.

Venice, Mogadishu, Helsinki, Jerusalem, and Casablanca have the shortest median street segment lengths (indicating fine-grained networks) while Kiev, Moscow, Pyongyang, Beijing, and Shanghai have the longest (indicating coarse-grained networks). Due to their straight gridded streets, Buenos Aires, Detroit, and Chicago have the least circuitous networks (only 1.1%–1.6% more circuitous than straight-line distances), while Caracas, Hong Kong, and Sarajevo have the most circuitous networks (13.3%–14.8% more circuitous than straight-line distances) due largely to topography. Helsinki and Bangkok have the lowest average node degrees, each with fewer than 2.4 streets per node. Buenos Aires and Manhattan have the greatest average node degrees, both over 3.5 streets per node. Buenos Aires and Manhattan similarly have the largest proportions of four-way intersections and the smallest proportions of dead-end nodes.

Figure 1 and Table 2 aggregate these results by world region (though note that the regional aggregation sample sizes are relatively small and thus the usual caveats apply). On average, the US/Canadian cities exhibit the lowest street orientation entropy, circuitry, and proportions of dead-ends as well as the highest median street segment lengths, average node degrees, and proportions of four-way intersections. They are also by far the most grid-like in terms of ϕ . On average, the European cities exhibit the highest street orientation entropy and proportion of dead-ends as well as the lowest average node degrees. They are the least grid-like in terms of ϕ .

To illustrate the geography of these order/entropy trends, Fig. 2 maps the 100 study sites by ϕ terciles. As expected, most of the sites in the US and Canada fall in the highest tercile (i.e., they have low entropy and highly-ordered, grid-like street orientations), but the notable exceptions of high-entropy Charlotte, Boston, and Pittsburgh fall in the lowest tercile. Most of the sites in Europe fall in the lowest tercile (i.e., they have high

entropy and disordered street orientations). Most of the sites across the Middle East and South Asia fall in the middle tercile.

To better visualize spatial order and entropy, we plot polar histograms of each city's street orientations. Each polar histogram contains 36 bins, matching the description in the methods section. Each histogram bar's direction represents the compass bearings of the streets (in that histogram bin) and its length represents the relative frequency of streets with those bearings. The two examples in Fig. 3 demonstrate this. On the left, Manhattan's 29° angled grid originates from the New York Commissioners' Plan of 1811, which laid out its iconic 800-ft $\times$ 200-ft blocks (Ballon 2012; Koeppel 2015). Broadway weaves diagonally across it, revealing the path dependence of the old Wick-quasgeck Trail's vestiges, by which Native Americans traversed the island long before the first Dutch colonists arrived (Holloway 2013). On the right, Boston features a grid in some neighborhoods like the Back Bay and South Boston, but they tend to not align with one another, resulting in the polar histogram's jumble of competing orientations. Furthermore, the grids are not ubiquitous and Boston's other streets wind in various directions, resulting from its age (old by American standards), terrain (relatively hilly), and historical annexation of various independent towns with their own pre-existing street networks.

Figures 4 and 5 visualize each city's street orientations as a polar histogram. Figure 4 presents them alphabetically to correspond with Table 1 while Fig. 5 presents them in descending order of ϕ values to better illustrate the connection between entropy, griddedness, and statistical dispersion. The plots exhibit perfect 180° rotational symmetry and, typically, approximate 90° rotational symmetry as well. About half of these cities (49%) have an at least approximate north-south-east-west orientation trend (i.e., 0°-90°-180°-270° are their most common four street bearing bins). Another 14% have the adjacent

Table 2 Mean values of indicators aggregated by world region

	ϕ	H_o	H_w	$\bar{t}$	ζ	$\bar{k}$	P_{de}	P_{4w}
Asia/Oceania	0.123	3.439	3.437	80.6	1.062	2.836	0.171	0.184
Europe	0.033	3.547	3.540	78.7	1.061	2.814	0.172	0.172
Latin America	0.081	3.490	3.489	77.5	1.055	2.971	0.140	0.257
Middle East/Africa	0.081	3.490	3.490	65.8	1.064	2.883	0.137	0.162
US/Canada	0.427	3.003	2.969	98.8	1.043	3.090	0.116	0.334

See Table 1 for column definitions

orientations (i.e., 10° - 100° - 190° - 280° or 80° - 170° - 260° - 350°) as their most common. Thus, even cities without a strong grid orientation often still demonstrate an overall tendency favoring north-south-east-west orientation (e.g., as seen in Berlin, Hanoi, Istanbul, and Jerusalem).

Straightforward orthogonal grids can be seen in the histograms of Chicago, Miami, and others. Detroit presents an interesting case, as it primarily comprises two separate orthogonal grids, one a slight rotation of the other. While Seattle's histogram looks fairly grid-like, it is not fully so: most of Seattle is indeed on a north-south-east-west grid, but its downtown rotates by both 32° and 49° (Speidel 1967). Accordingly, there are observations in all of its bins and its $H_o = 2.54$ and $\phi = 0.72$, whereas a perfect grid would have $H_o = 1.39$ and $\phi = 1$. Thus, it is about 72% of the way between perfect disorder and a single perfect grid. However, its rotated downtown comprises a relatively small number of streets such that the

rest of the city's much larger volume swamps the histogram's relative frequencies. The same effects are true of similar cities, such as Denver and Minneapolis, that have downtown grids at an offset from the rest of the city (Goodstein 1994). If an entire city is on a grid except for one relatively small district, the primary grid tends to overwhelm the fewer offset streets (cf. Detroit, with its two distinct and more evenly-sized separate grids).

Figures 4 and 5 put Chicago's low entropy and Charlotte's high entropy in perspective. Of these 100 cities, Chicago exhibits the closest approximation of a single perfect grid with the majority of its streets falling into just four bins centered on 0° , 90° , 180° , and 270° . Its $\phi = 0.90$, suggesting it is 90% of the way between perfect disorder and a single perfect grid, somewhat remarkable for such a large city. Most American cities' polar histograms similarly tend to cluster in at least a rough, approximate way. Charlotte, Rome, and São Paulo, meanwhile, have nearly uniform distributions of street orientations around the compass. Rather than one or two primary orthogonal grids organizing city circulation, their streets run more evenly in every direction.

As discussed earlier, orientation entropy and weighted orientation entropy are strongly correlated. Additionally, ϕ moderately and negatively correlates with average circuitry ($r(\phi, c) = -0.432, p < 0.001$) and the proportion of dead-ends ($r(\phi, P_{de}) = -0.376, p < 0.001$), and

moderately and positively correlates with the average node degree ($r(\phi, k) = 0.518, p < 0.001$) and proportion of four-way intersections ($r(\phi, P_{4w}) = 0.634, p < 0.001$). As hypothesized, cities with more grid-like street orientations tend to also have more streets per node, more four-way junctions, fewer winding street patterns, and fewer dead-ends. Besides these relationships, ϕ also has a weak but significant correlation with median street segment length ($r(\phi, \bar{l}) = 0.27, p < 0.01$), concurring with previous findings examining the UK alone (Gudmundsson and Mohajeri 2013). Average circuitry moderately strongly and negatively correlates with the average node degree ($r(\zeta, k) = -0.672, p < 0.001$) and the proportion of four-way intersections ($r(\zeta, P_{4w}) = -0.689, p < 0.001$). Cities with more winding street patterns tend to have fewer streets per node and fewer grid-like four-way junctions.

Figure 6 presents the dendrogram obtained from the cluster analysis, allowing us to systematically explore cities that are more- or less-similar to each other. The dendrogram's structure suggests three high-level superclusters of cities, but for further analysis, we cut its tree at an intermediate level (eight clusters) for better external validity and more nuanced insight into those larger structures. To visualize these clusters another way, we map their four-dimensional feature space to two dimensions using t-SNE, a manifold learning approach for nonlinear dimensionality reduction that is well-suited for embedding higher-dimensional

data in a plane for visualization (van der Maaten and Hinton 2008). Figure 7 scatterplots the cities in these two dimensions: the t-SNE projection preserves their cluster structure relatively well despite inherent information loss, but, given the global density-equalizing nature of the algorithm, the relative distances within

and between clusters are not preserved in the embedding and should not be interpreted otherwise.

Most of the North American cities lie near each other in three adjacent clusters (red, orange, and blue), which contain grid-like—and almost exclusively North American—cities. The orange cluster represents relatively dense, gridded cities like Chicago, Portland, Vancouver, and Manhattan. The blue cluster contains less-perfectly gridded US cities, typified by San Francisco and Washington (plus, interestingly, Buenos Aires). The red cluster represents sprawling but relatively low-entropy cities like Los Angeles, Phoenix, and Las Vegas. Sprawling, high-entropy Charlotte is in a separate cluster (alongside Honolulu) dominated by cities that developed at least in part under the auspices of twentieth century communism, including Moscow, Kiev, Warsaw, Prague, Berlin, Kabul, Pyongyang, and Ulaanbaatar. Beijing and Shanghai are alone in their own cluster, more dissimilar from the other study sites. The dark gray cluster comprises the three cities with the most circuitous networks: Caracas, Hong Kong, and Sarajevo. While the US cities tend to group together in the red, orange, and blue clusters, the other world regions' cities tend to distribute more evenly across the green, purple, and light gray clusters.

Discussion

The urban design historian Spiro Kostof once said: “We ‘read’ form correctly only to the extent that we are familiar with the precise cultural conditions that generated it... The more we know about cultures, about the structure of society in various periods of history in different parts of the world, the better we are able to read their built environment” (Kostof 1991, p. 10). This study does not identify whether or how a city is planned or not. Specific spatial logics cannot be conflated with planning itself, which takes diverse forms and embodies innumerable patterns and complex structures, as do informal settlements and organic urban fabrics. In many cities, centrally planned and

self-organized spatial patterns coexist, as the urban form evolves over time or as a city expands to accrete new heterogeneous urban forms through synoecism.

Yet these findings do, in concert, illustrate different urban spatial ordering principles and help explain some nuances of griddedness. For example, gridded Buenos Aires has a ϕ value suggesting it only follows a single grid to a 15% extent. However, its low circuituity and high average node degree values demonstrate how it actually comprises multiple competing grids—which can indeed be seen in Figs. 4 and 5—and it clusters accordingly in Figs. 6 and 7 with gridded American cities. Jointly considered, the ϕ indicator, average circuituity, average node degree, and median street segment length tell us about the extent of griddedness and its character (curvilinear, straight-line, monolithic, heterogeneous, coarse-grained, etc.). Charlotte further illustrates the importance of taking these indicators together. Although its ϕ and orientation entropy are more similar to European cities' than American cities', it is of course an oversimplification to claim that Charlotte is therefore the US city with the most “European” street network—in fact, its median street segment length is about 50% longer than that of the average European city, and among European cities, Charlotte clusters primarily with those of the Communist Bloc. Pittsburgh, on the other hand, sits alone in a small sub-cluster with Munich and Vienna.

We find that cities with higher ϕ values also tend to have higher node degrees, more four-way intersections, fewer dead-ends, and less-winding street patterns. That is, cities that are more consistently organized according to a grid tend to exhibit greater connectedness and less circuituity. Interestingly, the H_o and H_w orientation entropies are extremely similar and strongly correlated: the weighted curvatures (versus straight-line orientation) of individual street segments have little impact on citywide orientation entropy, but the average circuituity of the city network as a whole positively correlates with orientation entropy. This finding deserves further exploration.

These results also demonstrate substantial regional differences around the world. Across these study sites, US/Canadian cities have an average ϕ value nearly thirteen-times greater than that of European cities, alongside nearly double the average proportion of four-way intersections. Meanwhile, these European cities' streets on average are 42% more circuitous than those of the US/Canadian cities. These findings illustrate the differences between North American and European urban patterns. However, likely due to such regional heterogeneity, this study finds statistical relationships somewhat weaker (though still significant) than prior findings examining cities in the UK exclusively.

Accordingly, given the heterogeneity of these world regions, future research can estimate separate statistical models for individual regions or countries—or even the neighborhoods of a single city to draw these findings closer to the scale of planning/design practice. The methods and indicators developed here offer planners and designers a toolbox to quantify urban form patterns and compare their own cities to those elsewhere in the world. Our preliminary results suggest trends and patterns, but future work should introduce additional controls to clarify relationships and make these findings more actionable for researchers and practitioners. For instance, topography likely constrains griddedness and influences circuituity and orientation entropy: a study of urban elevation change and hilliness in conjunction with entropy and circuituity would help clarify these relationships. Additionally,

further research can unpack the relationship between development era, design paradigm, city size, transportation planning objectives, and street network entropy to explore how network growth and evolution affect spatial order. Finally, given the importance of taking multiple indicators in concert, future work can develop a grid-index to unify them and eventually include streetscape and width attributes as further enrichment to explore walkability and travel behavior.

Conclusion

Street networks organize and constrain a city's transportation dynamics according to a certain spatial logic—be it planned or unplanned, ordered or disordered. Past studies of this spatial order have been challenged by small samples, limited geographies, and abstract entropy indicators. This study accordingly looked at a larger sample of cities around the world, empirically examining street network configuration and entropy across 100 cities for the first time. It measured network orientation entropy, circuitry, connectedness, and grain. It also developed an orientation-order indicator ϕ , to quantify the extent to which a network is ordered according to a single grid.

This study found significant correlations between ϕ and other indicators of spatial order, including street circuitry and measures of connectedness. It empirically confirmed that the cities in the US and Canada are more grid-like (exhibiting far less entropy and circuitry) than was typical elsewhere. It is noteworthy that Chicago—the foremost theoretical model of twentieth century city growth and development in urban studies (Dear 2001; Park and Burgess 1925; Wirth 1928)—is an extreme outlier among world cities in terms of spatial orientation-order. In sum, these methods and indicators demonstrate scalable techniques to empirically measure and visualize the complexity of spatial order, illustrating patterns in urbanization and transportation around the world.

Acknowledgements

Not applicable.

Author's contributions

The author designed and conducted the study and wrote, revised, and approved the final manuscript.

Funding

Not applicable.

Availability of data and materials

All data used in this study are publicly available from <https://www.openstreetmap.org/>.

Ethics approval and consent to participate

Not applicable.

Consent for publication

Not applicable.

Competing interests

The author declares that he has no competing interests.

Received: 6 March 2019 Accepted: 12 August 2019

Published online: 23 August 2019

References

- Ballon H (ed) (2012) The greatest grid: the master plan of Manhattan, 1811–2011. Columbia University Press, New York
- Barrington-Leigh C, Millard-Ball A (2017) The world's user-generated road map is more than 80% complete. *PLoS One* 12: e0180698. <https://doi.org/10.1371/journal.pone.0180698>

- Barron C, Neis P, Zipf A (2014) A comprehensive framework for intrinsic OpenStreetMap quality analysis. *Trans GIS* 18: 877–895. <https://doi.org/10.1111/tgis.12073>
- Barthelemy M (2011) Spatial networks. *Phys Rep* 499:1–101. <https://doi.org/10.1016/j.physrep.2010.11.002>
- Barthelemy M, Bordin P, Berestycki H, Gribaudo M (2013) Self-organization versus top-down planning in the evolution of a city. *Sci Rep* 3. <https://doi.org/10.1038/srep02153>
- Barthelemy M, Flammini A (2008) Modeling Urban Street Patterns. *Phys Rev Lett* 100. <https://doi.org/10.1103/PhysRevLett.100.138702>
- Batty M (2005a) Network geography: relations, interactions, scaling and spatial processes in GIS. In: Unwin DJ, Fisher P (eds) *Re-presenting GIS*. Wiley, Chichester, pp 149–170
- Batty M (2005b) Cities and complexity: understanding cities with cellular automata, agent-based models, and fractals. MIT Press, Cambridge
- Batty M, Morphet R, Masucci P, Stanilov K (2014) Entropy, complexity, and spatial information. *J Geogr Syst* 16:363–385. <https://doi.org/10.1007/s10109-014-0202-2>
- Boeing G (2017) OSMnx: new methods for acquiring, constructing, analyzing, and visualizing complex street networks. *Comput Environ Urban Syst* 65:126–139. <https://doi.org/10.1016/j.compenvurbysys.2017.05.004>
- Boeing G (2018a) Measuring the complexity of urban form and design. *Urban Des Int* 23:281–292. <https://doi.org/10.1057/s41289-018-0072-1>
- Boeing G (2018b) A multi-scale analysis of 27,000 urban street networks: every US City, town, urbanized area, and Zillow neighborhood. *Environ Plan B: Urban Anal City Sci*:1–19. <https://doi.org/10.1177/2399808318784595>
- Boeing G (2018c) Planarity and street network representation in urban form analysis. *Environ Plan B: Urban Anal City Sci*:1–13. <https://doi.org/10.1177/2399808318802941>
- Boeing G (2019) The morphology and circuitry of walkable and drivable street networks. In: D'Acci L (ed) *The mathematics of urban morphology*. Birkhäuser, Basel. https://doi.org/10.1007/978-3-030-12381-9_12
- Boyer CM (1983) *Dreaming the Rational City*. The MIT Press, Cambridge
- Buhl J, Gautrais J, Reeves N, Solé RV, Valverde S, Kuntz P, Theraulaz G (2006) Topological patterns in street networks of self-organized urban settlements. *Eur Phys J B* 49:513–522. <https://doi.org/10.1140/epjb/e2006-00085-1>
- Burns A (1976) Hippodamus and the Planned City. *Historia: Zeitschrift Alte Geschichte* 25:414–428
- Cardillo A, Scellato S, Latora V, Porta S (2006) Structural properties of planar graphs of urban street patterns. *Phys Rev E* 73. <https://doi.org/10.1103/PhysRevE.73.066107>
- Chan SHY, Donner RV, Lämmer S (2011) Urban road networks — spatial networks with universal geometric features? *Eur Phys J B* 84:563–577. <https://doi.org/10.1140/epjb/e2011-10889-3>
- Courtat T, Gloaguen C, Douady S (2011) Mathematics and morphogenesis of cities: a geometrical approach. *Phys Rev E* 83:1–12. <https://doi.org/10.1103/PhysRevE.83.036106>
- Dear M (2001) *From Chicago to L.A.: making sense of urban theory*. Sage publications, Thousand oaks
- Ducruet C, Beauguette L (2014) Spatial science and network science: review and outcomes of a complex relationship. *Netw Spat Econ* 14:297–316. <https://doi.org/10.1007/s11067-013-9222-6>
- Ellickson RC (2013) The law and economics of street layouts: how a grid pattern benefits a downtown. *Alabama Law Rev* 64:463–510
- Elman B, Kern M (eds) (2009) *Statecraft and classical learning: the rituals of Zhou in east Asian history*. Brill Academic Pub, Boston
- Eppstein D, Goodrich MT (2008) Studying (non-planar) road networks through an algorithmic Lens. In: *Proceedings of the 16th ACM SIGSPATIAL international conference on advances in geographic information systems, GIS '08*. Presented at the SIGSPATIAL '08, Irvine, California, p 16. <https://doi.org/10.1145/1463434.1463455>
- Giacomin DJ, Levinson DM (2015) Road network circuitry in metropolitan areas. *Environ Plan B: Plan Des* 42:1040–1053. <https://doi.org/10.1068/b130131p>
- Goodstein P (1994) *Denver streets: names, numbers, locations, Logic*. New Social Publications, Denver
- Groth P (1981) Streetgrids as frameworks for urban variety. *Harvard Archit Rev* 2:68–75
- Gudmundsson A, Mohajeri N (2013) Entropy and order in urban street networks. *Sci Rep* 3. <https://doi.org/10.1038/srep03324>
- Hanson J (1989) Order and structure in Urban Design. *Ekistics* 56:22–42
- Hatuka T, Forsyth L (2005) Urban design in the context of globalization and nationalism. *Urban Des Int* 10:69–86. <https://doi.org/10.1057/palgrave.udi.9000142>
- Holloway M (2013) *The measure of Manhattan: the tumultuous career and surprising legacy of John Randel, Jr., cartographer, surveyor, inventor*. W. W. Norton & Company, New York
- Jackson KT (1985) *Crabgrass frontier: the suburbanization of the United States*. Oxford University Press, New York
- Jacobs A (1995) *Great streets*. MIT Press, Cambridge
- Jiang B, Claramunt C (2004) Topological analysis of urban street networks. *Environ Plan B: Plan Des* 31:151–162. <https://doi.org/10.1068/b306>
- Jiang B, Duan Y, Lu F, Yang T, Zhao J (2014) Topological structure of urban street networks from the perspective of degree correlations. *Environ Plan B: Plan Des* 41:813–828. <https://doi.org/10.1068/b39110>
- Kaiser A (2011) *Roman urban street networks: streets and the Organization of Space in four cities*. Routledge, London
- Karimi K (1997) The spatial logic of organic cities in Iran and the United Kingdom. Presented at the space syntax first international symposium. England, London
- Koeppl G (2015) *City on a grid: how New York became New York*. Da Capo Press, Boston
- Kostof S (1991) *The City shaped: urban patterns and meanings through history*. Bulfinch Press, New York
- Levinson D, El-Geneidy A (2009) The minimum circuitry frontier and the journey to work. *Reg Sci Urban Econ* 39:732–738. <https://doi.org/10.1016/j.regsciurbeco.2009.07.003>
- Li W, Hu D, Liu Y (2018) An improved measuring method for the information entropy of network topology. *Trans GIS* 22: 1632–1648. <https://doi.org/10.1111/tgis.12487>
- Lilley KD (2001) Urban planning and the design of towns in the middle ages. *Plan Perspect* 16:1–24. <https://doi.org/10.1080/02665430010000751>
- Lin J, Ban Y (2013) Complex network topology of transportation systems. *Transp Rev* 33:658–685. <https://doi.org/10.1080/01441647.2013.848955>
- Louf R, Barthelemy M (2014) A typology of street patterns. *J R Soc Interface* 11:1–7. <https://doi.org/10.1098/rsif.2014.0924>
- Low SM (2009) Indigenous architecture and the Spanish American plaza in Mesoamerica and the Caribbean. *Am Anthropol* 97:748–762. <https://doi.org/10.1525/aa.1995.97.4.02a00160>
- Marshall S (2004) *Streets and patterns*. Spon Press, New York

- Marshall S, Gil J, Kropf K, Tomko M, Figueiredo L (2018) Street network studies: from networks to models and their representations. *Netw Spat Econ*. <https://doi.org/10.1007/s11067-018-9427-9>
- Martin L (2000) The grid as generator. *Archit Res Q* 4:309–322. <https://doi.org/10.1017/S1359135500000403>
- Masucci AP, Stanilov K, Batty M (2013) Limited urban growth: London's street network dynamics since the 18th century. *PLoS One* 8:e69469. <https://doi.org/10.1371/journal.pone.0069469>
- Mazza L (2009) Plan and constitution - Aristotle's Hippodamus: towards an "ostensive" definition of spatial planning. *Town Plan Rev* 80:113–141. <https://doi.org/10.3828/tpr.80.2.2>
- McIntosh JR (2007) The ancient Indus Valley: new perspectives. ABC-CLIO, Santa Barbara
- Mele C (2017) Spatial order through the family: the regulation of urban space in Singapore. *Urban Geogr* 38:1084–1108. <https://doi.org/10.1080/02723638.2016.1187372>
- Mohajeri N, French J, Gudmundsson A (2013a) Entropy measures of street-network dispersion: analysis of coastal cities in Brazil and Britain. *Entropy* 15:3340–3360. <https://doi.org/10.3390/e15093340>
- Mohajeri N, French JR, Batty M (2013b) Evolution and entropy in the organization of urban street patterns. *Ann GIS* 19:1–16. <https://doi.org/10.1080/19475683.2012.758175>
- Mohajeri N, Gudmundsson A (2012) Entropies and scaling exponents of street and fracture networks. *Entropy* 14:800–833. <https://doi.org/10.3390/e14040800>
- Mohajeri N, Gudmundsson A (2014) The evolution and complexity of urban street networks: urban street networks. *Geogr Anal* 46:345–367. <https://doi.org/10.1111/gean.12061>
- Nilsson L, Gil J (2019) The signature of organic urban growth: degree distribution patterns of the City's street network structure. In: D'Acci L (ed) *The mathematics of urban morphology*. Springer, Cham, pp 93–121. https://doi.org/10.1007/978-3-030-12381-9_5
- O'Brien DT, Farrell C, Welsh BC (2019) Looking through broken windows: the impact of neighborhood disorder on aggression and fear of crime is an artifact of research design. *Ann Rev Criminol* 2:53–71. <https://doi.org/10.1146/annurev-criminol-011518-024638>
- Paden R (2001) The two professions of Hippodamus of Miletus. *Philos Geogr* 4:25–48. <https://doi.org/10.1080/10903770124644>
- Park RE, Burgess EW (eds) (1925) *The City*. University of Chicago Press, Chicago
- Parthasarathi P, Hochmair H, Levinson D (2015) Street network structure and household activity spaces. *Urban Stud* 52:1090–1112. <https://doi.org/10.1177/0042098014537956>
- Peterson CW, Chiu BC (1987) On the astronomical origin of the offset street grid at Teotihuacan. *J Hist Astron* 18:13–18. <https://doi.org/10.1177/002182868701801102>
- Porta S, Crucitti P, Latora V (2006) The network analysis of urban streets: a primal approach. *Environ Plan B: Plan Des* 33:705–725. <https://doi.org/10.1068/b32045>
- Qureshi M, Hwang H-L, Chin S-M (2002) Comparison of distance estimates for commodity flow survey: great circle distances versus network-based distances. *Transp Res Rec*:212–216. <https://doi.org/10.3141/1804-28>
- Rodriguez R (2005) The foundational process of cities in Spanish America: the law of indies as a planning tool for urbanization in early colonial towns in Venezuela. *Focus* 2:47–58. <https://doi.org/10.15368/focus.2005v2n1.8>
- Rose-Redwood R (2011) Mythologies of the grid in the Empire City, 1800–2011. *Geogr Rev* 101:396–413. <https://doi.org/10.1111/j.1931-0846.2011.00103.x>
- Rose-Redwood R, Bigon L (2018) *Gridded worlds: an urban anthology*. Springer, Cham
- Roy A (2005) Urban informality: toward an epistemology of planning. *J Am Plan Assoc* 71:147–158. <https://doi.org/10.1080/0194360508976689>
- Salingaros NA (1998) Theory of the urban web. *J Urban Des* 3:53–71. <https://doi.org/10.1080/13574809808724416>
- Sennett R (1990) American cities: the grid plan and the Protestant ethic. *Int Soc Sci J* 42:269–285. https://doi.org/10.1007/978-3-319-76490-0_11
- Shannon CE (1948) A mathematical theory of communication. *Bell Syst Tech J* 27(379–423):623–656. <https://doi.org/10.1145/584091.584093>
- Smith ME (2007) Form and meaning in the earliest cities: a new approach to ancient urban planning. *J Plan Hist* 6:3–47. <https://doi.org/10.1177/1538513206293713>
- Southworth M, Ben-Joseph E (1995) Street standards and the shaping of suburbia. *J Am Plan Assoc* 61:65–81. <https://doi.org/10.1080/01944369508975620>
- Southworth M, Ben-Joseph E (2004) Reconsidering the Cul-de-sac. *Access* 24:28–33. <https://doi.org/10.1179/chi.2008.28.1.135>
- Sparavigna AC (2017) The zenith passage of the sun and the architectures of the tropical zone. *Mech Mater Sci Eng* 10:239–250. <https://doi.org/10.2412/mmse.20.89.933>
- Speidel WC (1967) *Sons of the profits*. Nettle Creek Publishing, Seattle
- Stanislowski D (1946) The origin and spread of the grid-pattern town. *Geogr Rev* 36:105–120. <https://doi.org/10.2307/211076>
- Tsiotas D, Polyzos S (2018) The complexity in the study of spatial networks: an epistemological approach. *Netw Spat Econ* 18:1–32. <https://doi.org/10.1007/s11067-017-9354-1>
- van der Maaten L, Hinton G (2008) Visualizing Data using t-SNE. *J Mach Learn Res* 9:2579–2605
- Wang J (2015) Resilience of self-organised and top-down planned cities—a case study on London and Beijing street networks. *PLoS One* 10:e0141736. <https://doi.org/10.1371/journal.pone.0141736>
- Wirth L (1928) *The ghetto*. University of Chicago Press, Chicago
- Xu Y (2008) Urban communities, state, spatial order, and modernity: studies of Imperial and republican Beijing in perspective. *China Rev Int* 15:1–38. <https://doi.org/10.1353/cri.0.0139>
- Yeh AG-O, Li X (2001) Measuring and monitoring of urban sprawl in a rapidly growing region using entropy. *Photogramm Eng Remote Sens* 67:83–90
- Zielstra D, Hochmair HH, Neis P (2013) Assessing the effect of data imports on the completeness of OpenStreetMap – a United States case study. *Trans GIS* 17:315–334. <https://doi.org/10.1111/tgis.12037>

Publisher's Note

Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.