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Authors

Hu, R
Wan, J
Yang, Z
et al.

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Key Points:

- A theoretical model is proposed to describe the crossover from fingering to stable flow as a function of contact angle and capillary number
- The phase diagram predicted by the model shows that decreasing contact angle θ stabilizes the displacement for $\theta \geq 45^\circ$
- The extended phase diagram also captures the boundary between corner flow and cooperative filling for contact angle smaller than 45°

Supporting Information:

- Supporting Information S1
- Movie S1
- Movie S2
- Movie S3
- Movie S4
- Movie S5
- Movie S6

Correspondence to:

Y.-F. Chen,
csyfchen@whu.edu.cn

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Wettability and Flow Rate Impacts on Immiscible Displacement: A Theoretical Model

Ran Hu¹ , Jiamin Wan² , Zhibing Yang¹, Yi-Feng Chen¹ , and Tetsu Tokunaga²
¹State Key Laboratory of Water Resources and Hydropower Engineering Science, Wuhan University, Wuhan, China,

²Energy Geosciences Division, Lawrence Berkeley National Laboratory, Berkeley, CA, USA

Abstract When a more viscous fluid displaces a less viscous one in porous media, viscous pressure drop stabilizes the displacement front against capillary pressure fluctuation. For this favorable viscous ratio conditions, previous studies focused on the front instability under slow flow conditions but did not address competing effects of wettability and flow rate. Here we study how this competition controls displacement patterns. We propose a theoretical model that describes the crossover from fingering to stable flow as a function of invading fluid contact angle θ and capillary number Ca . The phase diagram predicted by the model shows that decreasing θ stabilizes the displacement for $\theta \geq 45^\circ$ and the critical contact angle θ_c increases with Ca . The boundary between corner flow and cooperative filling for $\theta < 45^\circ$ is also described. This work extends the classic phase diagram and has potential applications in predicting CO₂ capillary trapping and manipulating wettability to enhance gas/oil displacement efficiency.

1. Introduction

The displacement of fluid by another immiscible one in porous media is a phenomenon of great importance in a variety of natural, engineering, and industrial processes, including geological CO₂ sequestration (Benson & Cole, 2008), enhanced oil/gas recovery (Mason & Morrow, 2013), and fuel cells (Anderson et al., 2010). A common phenomenon in two-phase flow is the instability of displacement front, which affects the CO₂ storage capacity and gas/oil recovery efficiency. When the gravity is negligible, the fluid-fluid displacement is governed by the competition between the capillary force and viscous force. This competition is complicated by the pore surface's wettability, and consequently, the immiscible displacement pattern can range from capillary fingering and viscous fingering to a stable/compact front (Lenormand et al., 1988; Trojer et al., 2015; Zhang et al., 2011; Zheng et al., 2017). In the drainage processes in which a nonwetting fluid (invading fluid contact angle $\theta > 90^\circ$) displaces a wetting fluid, Lenormand et al. (1988) proposed the classic phase diagram to distinguish displacement patterns via two dimensionless parameters: the capillary number Ca and the viscosity ratio M . Here $Ca = v_i \mu_i / \sigma$ and $M = \mu_i / \mu_d$, in which μ_i and v_i are, respectively, the viscosity and the characteristic velocity of the invading fluid, σ is the interfacial tension, and μ_d is the viscosity of the defending fluid. Although a $\cos \theta$ term can be included in the denominator of the capillary number (Cao et al., 2016; Jamaloei et al., 2012), it cannot quantitatively account for the impact of wettability on the immiscible displacement patterns in porous media (Trojer et al., 2015) because accurate scaling of capillary displacement with $\cos \theta$ is strictly limited to straight capillaries (Anderson, 1986; Philip, 1971).

The challenge in describing the impact of wettability on the displacement patterns in porous media is how to link the local pore-scale filling events governed by the Young-Laplace law to the regional cooperative and/or competitive filling behavior. In capillary-dominated displacement, Cieplak and Robbins (1988, 1990) proposed three modes of meniscus motion (burst, touch, and overlap) to capture the effect of wettability on the fluid invasion morphology. They found that as the pore surface becomes more and more wet to the invading phase (θ decreases), the typical width of fingers increases and appears to diverge at a critical contact angle θ_c . In the spirit of Cieplak and Robbins model, extensive studies followed with focus on the evaporation processes (Chapuis et al., 2008; Chraïbi et al., 2009), the square network (Koiller et al., 1992), disordered (Jung et al., 2016), and 3-D porous media (Singh et al., 2017). Jung et al. (2016) conducted micromodel experiments with θ ranging from 46° to 180° and found a consistent crossover from stable invasion to capillary fingering in the range of $80^\circ < \theta < 120^\circ$. A similar conclusion was reported in 3-D porous media experiments characterized with X-ray microtomography (Singh et al., 2017). These studies provide insights

into how wettability of pore surfaces impacts fluid invasion morphology via local menisci instability in the capillary-dominated flow regime, but the effect of the viscous force on the displacement pattern was not considered.

Under high flow rates, the viscous force plays a role in the fluid invasion processes and the displacement front propagation depends highly on the viscous ratio M . When a less viscous fluid displaces a more viscous one ($M < 1$), the viscous force acting against the capillary force produces unstable fronts, and the resulted pattern formation is sensitive to the wettability. Holtzman and Segre (2015) proposed a novel pore-scale model to explore the interplay between viscosity, capillarity, and the wettability properties in cases with $M < 1$, indicating that the increase of Ca enhances viscous fingering regardless of wettability. This is because at high flow rates the meniscus instability of bursts is almost independent of the contact angle, and the instability stimulates the viscous-fingering flow pattern. The impact of wettability on immiscible displacement has also been observed in glass beads-filled Hele-Shaw experiments (Trojer et al., 2015) and in patterned microfluidic systems (Zhao et al., 2016). These studies indicate that decreasing the invading fluid contact angle in the range of $180^\circ > \theta > \theta_c$ (i.e., from strong drainage to weak imbibition) stabilizes the displacement patterns, but the wettability effect is suppressed as flow rate increases.

Compared to the achievements in understanding wettability impacts in the limit of slow and unfavorable displacement conditions, less progress has been made in examining favorable displacement conditions ($M > 1$). Under favorable displacement conditions, the viscous pressure field resides behind the displacement front and the interface is stable against the capillary pressure fluctuations that roughen the interface (He et al., 1992; Wong, 1994). Since the role of the viscous force at the interface is stabilization in the case of $M > 1$, and different from that in the case of $M < 1$, the mechanism of wettability together with the flow rate controlling the invasion morphology cannot be captured by existing models (Holtzman & Segre, 2015). Therefore, how wettability and flow rate control the immiscible displacement under favorable conditions needs to be further investigated.

The impact of wettability on the immiscible displacement patterns under the favorable displacement conditions plays a key role in the geological CO_2 sequestration. During the postinjection stage, brine displaces the previously injected CO_2 . Since the viscosity of brine is higher than that of supercritical (scCO_2), the displacement front tends to become compact and stable as flow rate increases. However, change in wettability of rock surfaces resulting from the sorption of natural organic matter and hydrocarbons, or the long-term exposure to CO_2 (El-Maghraby & Blunt, 2013; Iglauer et al., 2015; Kim et al., 2012) significantly affects the stability of displacement fronts and directly impacts the scCO_2 capillary trapping (Chaudhary et al., 2013; Hu et al., 2017a). Therefore, quantifying the competing effects of wettability and flow rate on the displacement front instability during the postinjection stage becomes a critical issue to be addressed.

Here we investigate how the competing effects of wettability and flow rate control the fluid invasion processes under favorable displacement conditions. We propose a model for capturing the crossover from fingering to stable flow to elucidate the competing effects. Our work extends the classic phase diagram in the limits of drainage (Lenormand et al., 1988; Zhang et al., 2011) and imbibition conditions (Lenormand, 1990), and also explores the controls of wettability and flow rate on the transition of displacement fronts from fingering to stable under favorable displacement conditions.

2. Crossover From Capillary Fingering to Stable Displacement

2.1. Pore-Scale Simulation

We study the immiscible displacement by performing simulations of the Navier-Stokes equations with OpenFOAM (Greenshields, 2015). The pore network is constructed by placing circles on a triangular lattice (x_0, y_0) with a constant space a_0 and specifying random center coordinate (x_i, y_i) and random radius (r_i) of circles, where $a_0 = 600 \mu\text{m}$, $r_0 = 285 \mu\text{m}$ (supporting information Figure S1). The length and width of the pore network are $L = 20 \text{ mm}$ and $W = 10 \text{ mm}$, respectively. The porosity ϕ is 0.261, and the pore volume is $2.10 \mu\text{L}$. The construction leads to some overlaps of the neighboring circles (posts) and result in some "dead" pores. The overlap is considered in this work to simulate the effects of grain consolidation in sintered bead packs and sandstone (Cieplak & Robbins, 1990). The pore network is fully saturated with scCO_2 and then brine is injected with constant flow rates Q , with $-5.04 \leq \log_{10} Ca \leq -2.74$, where $Ca = Q\mu_i/(A_c\sigma)$, A_c is the cross-sectional area of the inlet. The viscosity μ and the density ρ of brine and scCO_2 are, respectively, $\mu_{\text{brine}} = 5.972 \times 10^{-4} \text{ Pa}\cdot\text{s}$, $\mu_{\text{scCO}_2} = 2.276 \times 10^{-5} \text{ Pa}\cdot\text{s}$, $\rho_{\text{brine}} = 993.9 \text{ kg/m}^3$, and $\rho_{\text{scCO}_2} = 281.8 \text{ kg/m}^3$ and $\sigma = 3.3 \times 10^{-2}$

Figure 1. Evolution of the fluid-fluid displacement fronts with time for the imbibition (a, d), neutral (b, e), and drainage (c, f) processes under the intermediate (a–c) and lowest (d–f) flow rate conditions. These patterns (a–f) are characterized by the evolution of (g) the normalized fluid-fluid interface length l_{nw} and (h) the normalized displacement front x_{tip}^* with the invading fluid saturation S_w , and (i) the characteristic displacement front velocity $\bar{v}_{tip}^*$ as a function of θ . Also shown are the enlarged images (d', f') of the selected regions from (d) and (f). The water menisci advance at a time interval of 0.1 s during which 0.01 pore volume of brine is injected into the micromodel. The arrow indicates the direction of meniscus movement. The burst mode for the meniscus motion at the pore scale is given in (j).

N/m (Hu et al., 2017b). We simulate a total of 42 computational cases for the heterogeneous micromodel, with $\log_{10} Ca = -5.04, -4.74, -4.04, -3.74, -3.04$, and -2.74 and $\theta = 45^\circ, 60^\circ, 75^\circ, 90^\circ, 120^\circ, 150^\circ$, and 175° . Detailed descriptions of simulations are included in supporting information Text S1 and Figure S1.

Figures 1a–1f present the evolution of the fluid-fluid displacement front at the lowest Ca (Figures 1d–1f, $\log_{10} Ca = -5.04$) and at the capillary number of $\log_{10} Ca = -3.74$. The displacement patterns for the range of θ and Ca presented in Figure 1 and SI Figure S2 show that the increase of θ destabilizes the invasion morphology, shifting from stable at imbibition ($\theta = 45^\circ$) to fingering at drainage ($\theta = 175^\circ$). However, as Ca increases up to the highest Ca ($\log_{10} Ca = -2.74$), fluid invasion is stable for all θ , indicating that the impact of wettability on the fluid invasion processes becomes negligible, consistent with previous experimental and numerical results (Herring et al., 2015; Holtzman & Segre, 2015).

To gain an insight into the invasion processes, we plot the evolution of the fluid-fluid displacement fronts for imbibition (Figures 1a and 1d), neutral (Figures 1b and 1e) and drainage (Figures 1c and 1f) conditions, respectively. We characterize these patterns via the normalized fluid-fluid interface length l_{nw} (Figure 1g), the normalized displacement front location x_{tip}^* (Figure 1h), and the characteristic front velocity $\bar{v}_{tip}^*$ (Figure 1i), with $l_{nw} = L_{nw}/W$ and $x_{tip}^* = x/L$, where L_{nw} is the fluid-fluid interface length and x is the distance from the front tip to the inlet. The smooth fluid-fluid interface provides $l_{nw} \approx 1$; and the larger the magnitude of l_{nw} is, the more irregular is the interface. For imbibition ($\theta = 45^\circ$, Figures 1a and 1d), the displacement is stable with l_{nw} almost remaining constant during the whole invasion processes (Figure 1g), whereas l_{nw} increases with a highest growth rate at $\theta = 175^\circ$, which indicates a highly fingered displacement pattern. The $x_{tip}^*-S_w$ curves (Figure 1h) illustrate how displacement front advances toward the outlet, which was introduced to classify the capillary-/viscous-fingering regimes (Chen et al., 2017; Tsuji et al., 2016; Yamabe et al., 2015). A higher slope of the $x_{tip}^*-S_w$ curves means a higher front velocity that leads to early breakthrough with less efficient displacement. To quantify the displacement front velocity during the whole invasion processes, we introduce a characteristic dimensionless front velocity $\bar{v}_{tip}^*$ by averaging the dimensionless front velocity $v_{tip}^*(t^*) = \partial x_{tip}^* / \partial t^*$ over the whole processes, where $t^* = tQ/(LWh_0)$ is the scaled time, Q is the flow rate, and h_0 is the depth of the pore network, $h_0 = 40 \mu\text{m}$. An analytical expression can be derived (supporting information Text S2):

$$\bar{v}_{tip}^* = \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{i=1}^N v_{tip}^*(t_i^*) = \frac{1}{\phi S_{wb}}, \quad (1)$$

where S_{wb} is the invading fluid saturation at the breakthrough time.

Equation (1) shows that $\bar{v}_{tip}^*$ is inversely proportional to the invading fluid saturation S_{wb} at the breakthrough time. For completely stable flow, $S_{wb} = 1$, and $\bar{v}_{tip}^*$ approaches the minimum value of $\bar{v}_{tip}^* = 1/\phi$, while $\bar{v}_{tip}^*$ increases as the displacement pattern shifts from stable to fingering flow. As shown in Figure 1i, for $\theta < 60^\circ$, $\bar{v}_{tip}^*$ almost remains constant at $1/\phi$, indicating that the corresponding displacements are stable. For $\theta > 60^\circ$, $\bar{v}_{tip}^*$ increases with θ and the slope of $\bar{v}_{tip}^*-\theta$ curve is smaller for higher Ca , demonstrating the stabilizing effect induced by the viscous pressure drop. For $\log_{10} Ca = -5.04$, the displacement pattern shifts from stable to fingering flow in the range of $\theta = 60^\circ$ and 90° (supporting information Figure S2). This is consistent with Figure 1i which shows significant increases of $\bar{v}_{tip}^*$ between $\theta = 60^\circ$ and 90° .

The menisci motion at the pore scale controls the fluid-fluid interface instability at the pore network scale. As shown in Figure 1d' (selected region in Figure 1d), at small contact angle $\theta = 45^\circ$, two or more neighboring water menisci overlap and merge into a new one, leading to a smooth displacement front at the pore network scale (Jung et al., 2016; Zhao et al., 2016). However, under drainage condition, a single meniscus (Figure 1f', selected region in Figure 1f) advances independently of the neighboring water menisci, which can be represented by the burst mode (Cieplak & Robbins, 1988, 1990). The increase of θ stimulates the burst events and hence leads to an unstable interface, but the destabilizing effect would be suppressed by viscous pressure drop.

2.2. A Theoretical Model

To quantify the interplay between wettability and flow rate, we consider the viscous pressure drop along the bulk flow direction that stabilizes the interface and the capillary pressure fluctuations (which lead to meniscus instabilities, i.e., bursts). The viscous pressure drop δP_v along the distance of δx can be written as (Homsy, 1987):

$$\delta P_v \sim (\mu_d - \mu_i) \frac{U}{K} \delta x, \quad (2)$$

where U is the velocity of the invading fluid, and K is the permeability of the medium. Since $\mu_i > \mu_d$ during brine flooding, the pressure drop given by equation (2) yields $\delta P_v < 0$, and hence any small perturbation diminishes, resulting in a stable interface.

For the burst event in 2-D systems where the thin film is not considered, if the pressure drop between the two phases is larger than the maximum capillary pressure, no stable arc-shaped interface connecting to the two disks can exist (Figure 1j). The critical capillary force δP_{cr} corresponding to the minimum (critical) curvature

Figure 2. Phase diagram in the θ - $\log_{10}Ca$ plane with θ ranging from 45° to 175° under the favorable displacement conditions ($M > 1$). The theoretical model predicts the crossover (θ_c, Ca_c) from capillary fingering to stable displacement with the characteristic length $\lambda_d = 0.95$ (solid curve) and $\lambda_d = 0.99$ (dashed curve). The dots represent the numerical conditions. The displacement patterns can be classified into a capillary fingering regime (square), a stable displacement regime (circle), and a crossover zone (diamond). The red color represents higher-invading fluid saturation S_{wb} at the breakthrough time, whereas the blue color represents lower-invading fluid saturation. The values of S_{wb} under all of the numerical conditions are listed in supporting information Table S1.

$R_c = \frac{a}{2} \cdot \left(\sqrt{1 - \lambda_d^2 \sin^2 \theta} + \lambda_d \cos \theta \right)$ (Holtzman & Segre, 2015) is introduced to represent the occurrence of burst mode (Figure 1j):

$$\delta P_{cr} \sim \frac{\sigma}{R_c} = \frac{\sigma}{\frac{a}{2} \cdot \left(\sqrt{1 - \lambda_d^2 \sin^2 \theta} + \lambda_d \cos \theta \right)}, \quad (3)$$

where λ_d is the microscopic characteristic length of the pore network, $\lambda_d = \bar{d}/\bar{a}$, $\bar{d}$ is the average diameter of the discoid-shaped grains and $\bar{a}$ is the average spacing between their centers in the triangular lattices. In this study, $\bar{d} = 570 \mu\text{m}$ and $\bar{a} = 600 \mu\text{m}$.

The transition from fingering to stable flow indicates that the magnitude of δP_v is the same as δP_{cr} :

$$|\delta P_v| = \delta P_{cr}. \quad (4)$$

Since the permeability K and the distance δx can be respectively scaled by $K \sim a^2$, and $\delta x \sim a$ (Blunt & Scher, 1995; Holtzman & Segre, 2015), substituting equations (2) and (3) into equation (4) with $Ca = U\mu_i/\sigma$ yields the relation between critical capillary number Ca_c and the critical contact angle θ_c :

$$\left(1 - \frac{1}{M}\right) Ca_c = \frac{2c_0}{\sqrt{1 - \lambda_d^2 \sin^2 \theta_c} + \lambda_d \cos \theta_c}, \quad (5)$$

where c_0 is a coefficient. We determine c_0 using a specific critical contact angle $\theta_c^* \approx 75^\circ$ corresponding to the crossover point at a specific capillary number $Ca_c^* \approx 10^{-5.04}$, as supported by numerical evidence (bottom row in SI Figure S2). Substituting Ca_c^* and θ_c^* into equation (5), we have

$$\frac{Ca_c}{Ca_c^*} = \frac{\sqrt{1 - \lambda_d^2 \sin^2 \theta_c^*} + \lambda_d \cos \theta_c^*}{\sqrt{1 - \lambda_d^2 \sin^2 \theta_c} + \lambda_d \cos \theta_c}. \quad (6)$$

Consequently, we obtain a theoretical model for capturing the transition from fingering to stable flow influenced by wettability and flow rate:

$$Ca_c = \lambda_0 \left(\sqrt{1 - \lambda_d^2 \sin^2 \theta_c} - \lambda_d \cos \theta_c \right), \quad (7)$$

where $\lambda_0 = Ca_c^* / \left(\sqrt{1 - \lambda_d^2 \sin^2 \theta_c^*} - \lambda_d \cos \theta_c^* \right)$ is a parameter dependent on the microscopic characteristic length λ_d , the specific critical contact angle θ_c^* , and the specific capillary number Ca_c^* , which are in turn dependent on the pore and pore network heterogeneity.

Figure 2 shows the boundary between fingering and stable flow regimes as a function of θ and Ca described by equation (7) with $\lambda_d = 0.95$ (solid curve). Note that, unity for nonoverlapping disks. Larger pore body-throat aspect ratios correspond to higher λ_d (closer to 1). In this study, the overlapping disks induce “dead” pores and thus increase the permeability contrast, and eventually the value of λ_d should be larger than 0.95 which is originally defined for the nonoverlapping pore network (Holtzman & Segre, 2015). Figure 2a shows that $\lambda_d = 0.99$ could well describe the boundary between the crossover zone and the stable flow. As shown in Figure 2, the region between $\lambda_d = 0.95$ (solid curve) and $\lambda_d = 0.99$ (dashed curve) well captures the crossover from fingering to stable flow regimes. For any point above the dashed curve, the viscous pressure drop stabilizing the displacement front is dominant over the capillary force (Figure 2b), whereas for the points below the solid curve, the burst events at local scale control the fluid invasion processes and the flow exhibits capillary fingering (Figure 2d). The effects of viscous force and capillary force are comparable in the regime between the two curves, which results in the crossover from fingering to stable flow (Figure 2c).

3. Phase Diagram With Corner Flow

The phase diagram (Figure 2) proposed by the scaling analysis in the 2-D system does not account for corner flow. Under very slow flow rate conditions, if $\theta < 90^\circ - \alpha/2$ (Concus & Finn, 1969), where α is the corner angle (here $\alpha = 90^\circ$), the invading fluid advances in the corners where the posts touch the bottom and top surfaces, known as corner flow (Dong & Chatzis, 2004; Ransohoff & Radke, 1988). Experimental investigations show that the precursor wetting films move ahead of the primary displacement front (Dong & Chatzis, 2010; Tzimas et al., 1997; Vizika & Payatakes, 1989; Vizika et al., 1994). The length of the wetting film in the corner (l_{cor}), defined as the distance between the wetting film tip and the primary front tip and determined from the invading fluid distribution (supporting information Figure S6), decreases with increasing Ca and θ . Specifically, when Ca approaches up to a critical value Ca_{cf} , corner flow vanishes and l_{cor} is comparable to or smaller than the diameter of the post (i.e., $l_{cor}/d_0 \leq 1$) (Tzimas et al., 1997; Vizika & Payatakes, 1989). This critical capillary number Ca_{cf} is evidently a function of contact angle θ , that is, $Ca_{cf} = Ca_{cf}(\theta)$.

To extend the above phase diagram from $\theta = 45^\circ$ down to $\theta = 5^\circ$ with consideration of corner flow, we numerically determine the relation between Ca_{cf} and θ . Since the scale of wetting film is microscale or even nanoscale (Tokunaga, 2012) and numerical simulation is mesh dependent, we first determine the reasonable mesh size by validating numerical results with analytical solutions in a $40 \mu\text{m}$ square capillary tube (Dong & Chatzis, 1995). The simulation shows that numerical results with mesh size of $2 \mu\text{m}$ can reasonably reproduce the analytical results (supporting information Figure S3). We then perform pore-scale simulation with mesh size of $2 \mu\text{m}$ in a subdomain ($2.2 \text{ mm} \times 1.6 \text{ mm} \times 40 \mu\text{m}$) selected from the pore network, with a total of 8,581,760 cells and 9,368,224 points (supporting information Figure S4).

Figures 3a–3l show the phase distribution of invading fluid (brine) when the tip of front touches the outlet of the subdomain. For the lowest Ca ($\log_{10} Ca = -5.04$) and the smallest θ ($\theta = 5^\circ$) shown in Figure 3i, the wetting film advances ahead of the primary front along the corners formed by the posts and the top/bottom surfaces (Figure 3i; supporting information Movie S1), which agrees with microfluidic experimental observations (Zhao, 2017; Zhao et al., 2016). Note that since the posts are nonoverlapping in the subdomain considered, the wetting films connect from post to post on the boundary (see supporting information Figure S5 and Movie S1). Figures 3a–3l also suggests that corner flow is suppressed by increasing Ca and θ (supporting information Movies S2 and S3). To quantify the occurrence of corner flow, we plot the variations of the normalized wetting film length l_{cor}/d_0 with Ca and θ (Figure 3m). It shows that the contour of $l_{cor}/d_0 = 1$ roughly follows a linear trend. As an approximation, we characterize the trend by

$$\log_{10} Ca_{cf} = \lambda_c \theta + b_c. \quad (8)$$

Figure 3. Corner flow and cooperative filling. (a–l) The 2-D distribution of invading fluid at the time when the front tip reaches the outlet of the subdomain. The invading fluid contact angle θ increases from left to right, while the flow rate (or $\log_{10}Ca$) increases from bottom to top. The blue color is brine and the gray is $scCO_2$. The primary displacement front tip and the wetting film tip are respectively denoted with circle and pentagram. (i) The distance between the wetting film tip and the primary front tip, l_{cor} , can be easily determined from the simulated phase distribution, and the details are shown in supporting information Figure S6. (i') The 3-D distribution of the invading phase. Under strong imbibition ($\theta = 5^\circ$) and slow flow rate ($\log_{10}Ca = -5.04$) conditions, precursor wetting films form and advance in the corners, ahead of the primary front. (m) The variation of the normalized wetting film length l_{cor}/d_0 with Ca and θ . Black dots represent 28 numerical simulations. The isoline of $l_{cor}/d_0 = 1$ (solid line) shows the occurrence of corner flow. The log of the critical capillary number decreases roughly linearly with θ .

The expression of $Ca_{cf}(\theta)$ is determined by assigning $\log_{10}Ca_{cf}(5^\circ) = -4.04$ and $\log_{10}Ca_{cf}(45^\circ) = -5.04$, leading to $\lambda_c = -0.025$ and $b_c = -3.915$. We will show below that this approximate relation is supported by experiments shown in Figure 4. A more accurate relation, however, needs further investigation.

The empirical relation given by equation (8) indicates that for $Ca > Ca_{cf}(\theta)$, corner flow vanishes, and cooperative filling of multiple neighboring menisci dominates the displacement processes. But as Ca gradually increases beyond a limit Ca_{ic} , the pore-scale displacement becomes incomplete, that is, the defending fluid is partially displaced behind the displacement front. For unfavorable case of $M < 1$, the invading fluid advances along the top and bottom surfaces with thin films under strong imbibition conditions ($\theta \approx 7^\circ$) (Levaché & Bartolo, 2014), whereas it advances along the center between the top and bottom surfaces under strong drainage conditions ($\theta \approx 150^\circ$) (Zhao, 2017; Zhao et al., 2016). On the other hand, for favorable case $M > 1$ considered in this paper, the invading fluid phase only moves along the center regardless of θ (Chan et al., 2013) if $Ca > Ca_{ic}$. To obtain the critical capillary number Ca_{ic} that corresponds to the occurrence of the incomplete

Figure 4. Phase diagram in the θ - $\log_{10}Ca$ plane depicting the crossover (CZ) from capillary fingering (CF) to stable displacement (SD) ($45^\circ \leq \theta \leq 175^\circ$) and the boundary between corner flow (CRF) and stable displacement (or cooperative filling) ($5^\circ \leq \theta < 45^\circ$) under favorable displacement conditions. Four experiment data sets (Jung et al., 2016; Tzimas et al., 1997; Vizika & Payatakes, 1989; Zhang et al., 2011) are selected to evaluate the proposed phase diagram. For $45^\circ \leq \theta \leq 175^\circ$, the crossover from capillary fingering to stable displacement is predicted by our theoretical model (equation (7)). Note that in the experiments of Zhang et al. (2011) (open and solid triangles), the post diameter is 300 μm and the pore throat's size is 40 μm , resulting in a characteristic length $\lambda_d = \bar{d}/\bar{a} = 0.938$ (red solid curve). The dashed curve corresponds to the characteristic length $\lambda_d = 0.99$, also shown in Figure 2. Under conditions of $5^\circ \leq \theta < 45^\circ$, the boundary between corner flow and stable displacement (cooperative filling) is given by equation (8). The horizontal bars of the values by Jung et al. (2016) indicate standard deviations of contact angle measurements.

displacement, we solve a four-dimensional dynamical system for the force-balance equation that describes the meniscus shape with various Ca and θ values (supporting information Figure S7). As Ca increases up to a critical value (Ca_{ic}), no stationary solution is obtained (Levaché & Bartolo, 2014), indicating the occurrence of incomplete displacement. The numerical solutions show that Ca_{ic} decreases with θ , approaching a minimum of $\log_{10}Ca_{ic} = -2.30$ at $\theta = 175^\circ$ (supporting information Figures S8 and S9). The minimum of Ca_{ic} is larger than the maximum Ca in Figure 2, indicating that the incomplete displacement cannot occur in the domain of stable displacement considered in this study ($\log_{10}Ca < -2.74$).

The above discussion not only extends the phase diagram to strong imbibition ($\theta = 5^\circ$) with the inclusion of a corner flow regime but also provides a constraint for the proposed theoretical model (equation (7)) that Ca should be no more than $Ca_{ic}(\theta)$. Figure 4 presents the extended phase diagram for the full range of θ , which integrates theoretical crossover from fingering to stable flow regimes (equation (7)) and the empirical boundary between corner flow and stable displacement (equation (8)).

We evaluate the proposed phase diagram using available experimental data. Since the experimental data under favorable conditions, including immiscible displacements with various wetting conditions and flow rates is rather limited in the literature, only four data sets were selected herein. Under drainage condition, Zhang et al. (2011) conducted a series of experiments for $M > 1$, showing that for a specific contact angle $\theta = 163^\circ$, the displacement patterns at $\log_{10}Ca = -4.92$ and $\log_{10}Ca = -4.22$ are capillary fingering (solid triangle in Figure 4), whereas for higher Ca ($\log_{10}Ca = -3.82$ and $\log_{10}Ca = -3.52$) the patterns are the crossover from fingering to stable displacement (open triangle), which can be captured by our proposed phase diagram. In experiments by Tzimas et al. (1997), for $M > 1$ at $\theta = 10^\circ$, wetting films were observed at $\log_{10}Ca = -5$ with length $l_{cor}/d_0 \approx 1-2$, which represents corner flow (open square), whereas no wetting films were observed at $\log_{10}Ca = -4$ (solid square). The experiments by Vizika and Payatakes (1989) also show that favorable displacement pattern is stable at $\theta = 40^\circ$ and $\log_{10}Ca = -4$ (solid circle). Recently, Jung et al. (2016) reported that for water-air system under conditions of $\theta = 46^\circ$, $\log_{10}Ca = -3.96$ and $\theta = 79^\circ$, $\log_{10}Ca = -4.25$, stable fronts were observed (solid diamond). In summary, the phase diagram boundaries given by equations (7) and (8) generally capture the displacement patterns observed in existing experiments. Note that although the location of the boundaries for different patterns is dependent on the pore structure and the roughness of the pore surface (Dullien, 1992), the phase diagram provides a general picture for the pattern formations jointly influenced by wettability and flow rate.

4. Conclusions

We proposed a theoretical model to elucidate the competing effects of wettability and flow rate on the displacement patterns. The phase diagram predicted by the theoretical model describes the crossover from fingering to stable flow regimes with consideration of wettability, and therefore, extends the classic phase diagram (Lenormand, 1990; Lenormand et al., 1988; Zhang et al., 2011) to consider the wettability within the range from strong imbibition ($\theta = 5^\circ$) to strong drainage ($\theta = 175^\circ$). Our phase diagram also captures the crossover from corner flow to cooperative filling (stable displacement) under strong imbibition conditions ($5^\circ \leq \theta < 45^\circ$). Thus, our work extends the previous studies about the wettability effect on displacement patterns in the capillary-dominated flow regime (Cieplak & Robbins, 1988, 1990; Jung et al., 2016). Our work bridges understanding of menisci advancement at the pore scale and displacement front instability at the pore network scale, providing not only an insight into the effects of wettability and flow rate, but also a basis for an upscaling methodology that directly relates Darcy scale flow parameters to menisci dynamics (Armstrong et al., 2016). This analysis could become of practical significance for geologic carbon sequestration

and enhanced gas recovery through targeting desirable regions in the phase diagram by adjusting injection rates and potentially the wettability to enhance either capillary trapping or displacement efficiency.

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