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Numerical Simulation of Deformation and Failure Behavior of Geosynthetic Reinforced Soil Bridge Abutments

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Abstract: This paper presents a numerical investigation of the deformation and failure behavior of geosynthetic reinforced soil (GRS) bridge abutments. The backfill soil was characterized using a nonlinear elasto-plastic constitutive model that incorporates a hyperbolic stress-strain relationship with strain softening behavior and the Mohr-Coulomb failure criterion. The geogrid reinforcement was characterized using a hyperbolic load-strain-time model. The abutments were numerically constructed in stages, including soil compaction effects, and then monotonically loaded in stages to failure. Simulation results indicate that a nonlinear reinforcement model is needed to characterize deformation behavior for high applied stress conditions. A parametric study was conducted to investigate the effects of reinforcement, backfill soil, and abutment geometry on abutment deformations and failure. Results indicate that reinforcement spacing, reinforcement stiffness, backfill soil friction angle, and abutment height are the most significant parameters. The shape of the failure surface is controlled by abutment geometry and can be approximated as bilinear.

Keywords: Geosynthetic reinforced soil; Bridge abutment; Numerical simulation; Service limit; Strength limit; Failure mechanism.

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Introduction

Geosynthetic reinforced soil (GRS) bridge abutments are becoming widely used in transportation infrastructure and provide many advantages over traditional pile-supported designs, including lower cost, faster and easier construction, and smoother transition between the bridge and approach roadway. Several case histories for in-service GRS bridge abutments have been reported and show good field performance (Won et al. 1996; Wu et al. 2001; Abu-Hejleh et al. 2002; Adams et al. 2011a; Saghebfar et al. 2017). Numerical studies also have been conducted for GRS bridge abutments under service load conditions (Helwany et al. 2003, 2007; Zheng et al. 2014, 2015; Ambauen et al. 2015; Zheng and Fox 2016a, 2017; Ardah et al. 2017). These studies considered perfectly plastic soil and linearly elastic geosynthetic reinforcement and indicate relatively small lateral facing displacements and vertical strains. Numerical modeling work on the deformation behavior and bearing capacity of GRS bridge abutments, associated with large deformations up to failure, is more limited and also has assumed perfectly plastic soil and linearly elastic geosynthetic reinforcement (Wu et al. 2006a). Based on other related research findings (e.g., Walters et al. 2002; Hatami and Bathurst 2006; Liu and Ling 2012; Yang et al. 2012; Zheng and Fox 2016b), strain softening of the backfill soil and nonlinear response of the geosynthetic reinforcement may be important for high applied stress conditions. An investigation considering these effects, including failure behavior, would represent a useful contribution to the literature.

This paper presents a numerical investigation of the deformation and failure behavior of GRS bridge abutments. Simulations were performed to identify the importance of strain softening soil and nonlinear reinforcement behavior for a baseline case, and a parametric study was conducted to investigate the effects of reinforcement, backfill soil, and abutment geometry.
on abutment deformations and failure. Results from this study provide insights with regard to the design of GRS bridge abutments for various loading conditions.

**Background**

Deformations, such as lateral facing displacements and vertical compressions, are important considerations in the design of GRS bridge abutments for the service limit condition, whereas bearing capacity is an important consideration for the strength limit condition. The Federal Highway Administration (FHWA) provides analytical and empirical design methods for both conditions (Adams et al. 2011a, 2011b). The FHWA analytical method calculates ultimate bearing capacity based on the soil-geosynthetic composite load bearing capacity, which accounts for the maximum aggregate size and friction angle of the backfill soil and the spacing and ultimate tensile strength of the geosynthetic reinforcement (Wu and Pham 2013; Wu et al. 2013). The allowable vertical stress for the service limit is then taken as 10% of the ultimate bearing capacity (Nicks et al. 2013, 2016). The FHWA empirical method is based on a vertical stress-strain relationship that is measured from performance tests (i.e., GRS mini-pier loading tests) conducted using project-specific soil and geosynthetic materials (Adams et al. 2011a, 2011b). In this case, the service limit is defined as an applied vertical stress of 200 kPa or the vertical stress at 0.5% vertical strain, and the strength limit is defined as the vertical stress at 5% vertical strain (Berg et al. 2009; Adams et al. 2011a, 2011b; Nicks et al. 2013).

Field and laboratory loading tests have been conducted on large-scale GRS piers and abutments and generally indicate satisfactory performance under service loads and relatively high bearing capacity (Adams 1997; Gotteland et al. 1997; Ketchart and Wu 1997; Wu et al. 2001, 2006a; Adams et al. 2011b, 2014; Nicks et al. 2013, 2016; Iwamoto et al. 2015). Lee and
Wu (2004) reviewed the results of several large-scale loading tests and suggested that bearing capacity can be as high as 900 kPa for closely spaced reinforcement and well-graded, well-compacted backfill soil. Nicks et al. (2013) conducted a series of performance tests on 2 m-high GRS mini-piers and found that reinforcement spacing and tensile strength have the most important effects on ultimate bearing capacity, and that well-graded backfill materials and increasing levels of backfill compaction can increase the stiffness of a GRS mini-pier.

Wu et al. (2006a) conducted numerical simulations on the deformation behavior of GRS bridge abutments using a geologic cap model for the backfill soil and a linearly elastic model for the geosynthetic reinforcement, and developed procedures to determine allowable vertical stress considering bridge seat type, reinforcement spacing, and backfill soil properties. Leshchinsky (2014) and Xie and Leshchinsky (2015) performed a series of parametric studies using limit analysis to investigate the optimal reinforcement design and failure mechanism of GRS bridge abutments, and found that reinforcement with closer vertical spacing in the upper section can efficiently increase the ultimate bearing capacity. Results also showed a curved failure surface extending downward from the heel of the bridge seat to the toe of the abutment for a bridge seat setback distance of 1.35 m or less and a compound failure surface for greater setback distances.

Numerical Model

The two-dimensional finite difference program FLAC Version 7.0 (Itasca Consulting Group 2011) was used for the current investigation. Zheng and Fox (2016a) developed a FLAC model to simulate the field performance of the Founders/Meadows GRS bridge abutment (Abu-Hejleh et al. 2000, 2001). Simulation results, including lateral facing displacements, bridge seat settlements, lateral and vertical earth pressures, and reinforcement tensile strains and forces,
were in good agreement with field measurements at various stages of construction. Using a similar modeling approach, Zheng and Fox (2017) simulated the response of a geosynthetic reinforced soil-integrated bridge system (GRS-IBS) abutment and found good agreement for abutment vertical compression measurements reported by Adams et al. (2011a). Based on these results, Zheng and Fox (2016a, 2017) concluded that this type of numerical model has the capability to simulate the performance of GRS bridge abutments under service load conditions.

In the current study, the model has been enhanced by incorporating strain softening behavior for the backfill soil and nonlinear behavior for the geosynthetic reinforcement to simulate the deformation of GRS bridge abutments up to failure conditions. The explicit Lagrangian calculation method and mixed-discretization zoning technique used in FLAC are well suited for this purpose, with the ability to characterize plastic deformations and strain localization. FLAC is applicable for plane strain conditions, which represents a simplification for these three-dimensional structures.

Baseline Case

Geometry

The finite difference grid and boundary conditions for the GRS bridge abutment baseline case are shown in Fig. 1. The model represents a single-span bridge system with span \( L_b = 30 \) m and symmetrical structures on both ends. Each end structure consists of a lower GRS wall, bridge seat, upper GRS fill, and approach roadway. Only the right-hand side of the bridge system was simulated due to symmetry. The GRS bridge abutment has height \( h = 5 \) m and 25 modular facing blocks with dimensions of 0.3 m (length) \( \times \) 0.2 m (height). An L-shaped bridge seat with a section thickness of 0.4 m rests on top of the GRS bridge abutment and has setback...
distance $a_0 = 0.2$ m from the wall facing. The clear distance between the top facing block and bridge beam $d_e$ is equal to the bridge seat thickness (0.4 m). The clearance height for the bridge beam above the foundation soil is 5.4 m, which satisfies the FHWA minimum requirement of 4.9 m for interstate highways (Stein and Neuman 2007). The bridge seat has upper surface contact length $L_c = 1.0$ m with the bridge beam and lower surface contact length $L_s = 1.5$ m with the soil. There is a 100 mm-wide vertical expansion joint between the bridge beam and bridge seat. Assuming a ratio of bridge beam span to depth $R_{sd} = L_b / D = 20$, the depth of the bridge beam $D = 1.5$ m. A 1.8 m-high upper GRS fill lies behind the bridge seat and is overlain by a 0.1 m-thick concrete roadway. The reinforcement has uniform length $L_r = 3.5$ m ($0.7h$) and vertical spacing $S_v = 0.2$ m for both the lower GRS wall and upper GRS fill. No secondary (i.e., bearing bed) reinforcement is included under the bridge seat for the baseline case.

To minimize the influence of boundary conditions on system response, the foundation soil has a depth of 10 m ($2h$) and the rear boundary is located at a distance of 20 m ($4h$) from the wall facing. Lateral boundaries are fixed in the horizontal direction and are free to move in the vertical direction, whereas the bottom boundary is fixed in both horizontal and vertical directions. Horizontal coordinate $x$ is measured to the right from the back side of the wall facing and vertical coordinate $z$ is measured upward from the top surface of the foundation soil.

**Soils**

Zheng and Fox (2016a) simulated the static response of the Founders/Meadows GRS bridge abutment using a nonlinear elasto-plastic model with a hyperbolic relationship and a Mohr-Coulomb failure criterion for the backfill soil. In the current investigation, the model is
enhanced by incorporating strain softening behavior at larger strain levels to simulate the response of GRS bridge abutments up to failure conditions. The tangent elastic modulus $E_t$, unloading-reloading modulus $E_{ur}$, bulk modulus $B$, and tangent Poisson’s ratio $\nu_t$ are expressed as (Duncan et al. 1980):

$$E_t = \left[1 - \frac{R_f (1 - \sin \phi') (\sigma'_i - \sigma'_3)}{2c' \cos \phi' + 2\sigma'_3 \sin \phi'}\right]^2 K p_a \left(\frac{\sigma'_3}{p_a}\right)^n$$

(1)

$$E_{ur} = K_{ur} p_a \left(\frac{\sigma'_3}{p_a}\right)^n$$

(2)

$$B = K_b p_a \left(\frac{\sigma'_3}{p_a}\right)^m$$

(3)

$$\nu_t = \frac{1}{2} \frac{E_t}{6B}$$

(4)

where $\sigma'_i$ and $\sigma'_3$ = major and minor principal effective stresses; $\phi'$ = friction angle; $c'$ = cohesion; $R_f$ = failure ratio; $K$ = elastic modulus number; $n$ = elastic modulus exponent; $p_a$ = atmospheric pressure; $K_{ur}$ = unloading-reloading modulus number; $K_b$ = bulk modulus number; $m$ = bulk modulus exponent; and $\nu_t$ is limited to a range of 0 to 0.49. Eqs. (1-4) were implemented into FLAC using FISH subroutines to update the stress-dependent soil moduli during the course of each simulation. To account for strain softening behavior, the friction angle and dilation angle were defined as piece-wise linear functions of incremental plastic shear strain and calibrated using triaxial test data.

Backfill soil properties are based on measurements for a well-graded angular sand with maximum particle size $d_{max} = 9.5$ mm, which meets the FHWA specifications for GRS bridge abutments (Berg et al. 2009; Adams et al. 2011b). Consolidated-drained triaxial compression
tests were conducted on sand specimens at five levels of effective confining stress. The specimens were compacted at a relative density of 80% with unit weight $\gamma = 17.3$ kN/m$^3$. The tests were numerically simulated and soil parameters were back-calculated from the experimental results. The resulting piece-wise linear relationships between incremental plastic shear strain $\varepsilon_p$, which occurs once the soil reaches the Mohr-Coulomb failure criterion, and the friction angle and dilation angle are shown in Fig. 2. The soil responds with peak values of friction angle and dilation angle of $\phi' = 46^\circ$ and $\psi = 18^\circ$, respectively, for $\varepsilon_p = 0$% to 4%. For $\varepsilon_p = 4$% to 15%, the soil experiences post-peak strain softening where both angles decrease linearly. For $\varepsilon_p \geq 15$, the soil responds with constant volume (i.e., steady state) friction angle and dilation angle of $\phi'_c = 43^\circ$ and $\psi_c = 0^\circ$, respectively. Using these relationships, a comparison of measured and simulated triaxial test results is shown in Fig. 3. The simulations slightly underestimate the deviator stress at the two lower confining stress levels; however, the nonlinear stress-strain behavior before peak strength and post-peak strain softening are characterized with good accuracy, especially for the higher confining stresses. The simulated response for soil dilation behavior is also in good agreement with the measured data.

The foundation soil was specified as dense silty sandy gravel and simulated using a linearly elastic-perfectly plastic model with a Mohr-Coulomb failure criterion. A firm foundation soil was used for all simulations for consistency. A summary of parameters for the backfill soil and foundation soil is provided in Table 1.

**Reinforcement**

Geogrid reinforcement was included in the numerical model using cable elements rigidly connected to the facing blocks and characterized using the hyperbolic load-strain-time model.
proposed by Allen and Bathurst (2014a, 2014b). Yu et al. (2016) also used this model and
provided further discussion. Tensile force $T$ is calculated as the product of tensile strain $\varepsilon$ and
a strain- and time-dependent secant stiffness $J_s$ as:

$$T = J_s \varepsilon$$  \hspace{1cm} (5)$$

where

$$J_s = \frac{1}{\frac{1}{J_0} + \chi \varepsilon}$$  \hspace{1cm} (6)$$

and $J_0$ = initial tangent stiffness and $\chi$ = empirical fitting parameter, with both $J_0$ and $\chi$
expressed as functions of time $t$. Tangent stiffness $J_t$ of the reinforcement is calculated as:

$$J_t = \frac{1}{J_0 \left(\frac{1}{J_0} + \chi \varepsilon\right)^2}$$  \hspace{1cm} (7)$$

and the input parameter for elastic modulus is defined as:

$$E_r = J_t / t_r$$  \hspace{1cm} (8)$$

where $t_r$ = geogrid thickness (constant).

A high density polyethylene (HDPE) uniaxial geogrid was specified for the GRS bridge
abutment, with properties and tensile behavior shown as Geogrid-2 in Fig. 4. The stiffness
parameters are initial stiffness $J_0 = 1054t^{-0.0697}$ kN/m and $\chi = 0.0359$ m/kN. Yu et al. (2016)
reported that the stiffness values for several HDPE geogrids were not significantly affected by
practical construction times of interest and, for simplicity, can be taken as constant during
construction. Following this procedure, an end-of-construction time $t = 150$ days = 3600 hours
was specified for the current simulations. As such, the tensile behavior for Geogrid-2 is
characterized by $J_0 = 596$ kN/m and shows stiffness decreasing nonlinearly with increasing
strain. A summary of parameters for Geogrid-2 is provided in Table 2. Geogrid-1 and Geogrid-3 are discussed later for the parametric study.

Structural Components

The concrete facing blocks, bridge seat, and roadway were modeled as linearly elastic materials with unit weight $\gamma = 23.5$ kN/m$^3$, elastic modulus $E = 20$ GPa, and Poisson’s ratio $\nu = 0.2$. The bridge beam was modeled as a solid block $(L_b \times D \times 1)$ of linearly elastic material with $E = 20$ GPa and $\nu = 0.2$. The unit weight of the bridge beam $\gamma_b$ was changed to produce different values of applied vertical stress on the GRS bridge abutment during the loading stage of the numerical simulations. The vertical force per unit width on the GRS bridge abutment is $F_v = L_b D\gamma_b / 2$, and the corresponding average applied vertical stress on the lower surface of the bridge seat is $q_v = F_v / L_s$.

Interfaces

Table 3 presents parameters for the various interfaces between soil, geogrid, facing block, bridge seat, and bridge beam. Soil-geogrid interfaces were included with the respective cable elements, whereas specific interface elements were needed to define block-block, soil-block, soil-bridge seat, and bridge beam-bridge seat interfaces. The soil-geogrid interfaces account for shear stiffness $k_s$, friction angle $\delta_i'$, and adhesion $c_i'$, whereas the other interfaces account for these parameters and normal stiffness $k_n$ in addition. Soil interface strengths were characterized using a reduction factor $RF$ defined as
\[ RF = \frac{\tan \delta_i'}{\tan \phi_p'} = \frac{c_i'}{c'} \quad (9) \]

Considering the typical embedment of wall facing at the toe of a GRS bridge abutment in the field, a relatively high toe shear stiffness of 40 MPa/m, as suggested by Yu et al. (2016), was selected for the interface between the lowermost facing block and foundation soil. The frictional interface between the bridge beam and bridge seat produces a lateral restraining force on the abutment structure, which can have an important effect on abutment deformations (Zheng and Fox 2016a).

**Modeling Procedures**

For each numerical simulation, the GRS bridge abutment model was constructed in stages and then monotonically loaded in stages to failure. Initially, the foundation soil was placed and resolved to equilibrium under gravitational forces. The GRS bridge abutment was constructed in layers on top of the foundation soil, with each layer consisting of one soil lift, one facing block, and the necessary interfaces. Geogrid reinforcement layers were placed at specified elevations, depending on the simulation. Following Hatami and Bathurst (2006), Guler et al. (2007), Zheng and Fox (2017), and Zheng et al. (2017), a temporary uniform surcharge stress of 8 kPa was applied to the top surface of each soil lift to simulate the effect of compaction and then removed prior to application of the next lift. On removal of the surcharge stress, the soil follows an unloading path with higher stiffness, which is similar to the paths for axisymmetric unloading shown as examples for the simulated stress-strain relationships in Fig. 3(a). Reloading follows the same path and, as such, each soil lift has an initially stiffer response during placement of the next lift. Once the GRS bridge abutment was completed, the bridge seat was placed on the abutment, the upper GRS fill was similarly constructed in layers behind the
bridge seat, and the approach roadway was placed on the GRS fill. The bridge beam then was placed on the bridge seat with an initial unit weight $\gamma_b = 3.34$ kN/m$^3$, which was chosen to produce an initial average applied vertical stress of $q_v = 50$ kPa. During subsequent loading, the unit weight of the bridge beam was increased in stages to produce failure of the abutment. For each construction and loading stage, the numerical model was resolved to equilibrium under gravitational forces. Abutment failure was assumed to occur if FLAC could not converge to equilibrium or the abutment reached a vertical strain of 10%.

Results from the numerical simulations are assessed at conditions of service limit and strength limit for the GRS bridge abutment. Similar to Nicks et al. (2013, 2016), the service limit is defined according to two criteria. The first criterion is an average applied vertical stress of $q_v = 200$ kPa and the second criterion is an average vertical strain of $\varepsilon_v = 0.5\%$, where $\varepsilon_v$ is based on abutment compression defined as the difference between the average downward displacement of the bridge seat and the average downward displacement of the underlying foundation soil. The strength limit is defined as an average vertical strain of $\varepsilon_v = 5\%$ and is based on considerations of ultimate bearing capacity as per FHWA guidelines (Nicks et al. 2013).

**PPS and LER Cases**

In addition to the baseline case defined by the above modeling conditions and parameters, simulations were also performed for two additional cases to investigate the effects of soil strain softening and nonlinear reinforcement behavior on the deformation response of the GRS bridge abutment. The first additional case assumes perfectly plastic soil (PPS) with constant values of friction angle and dilation angle ($\phi' = 46^\circ$ and $\psi = 18^\circ$) and nonlinear reinforcement (as per the baseline case). The second additional case assumes linearly elastic reinforcement (LER) with
constant stiffness equal to the secant stiffness at 5% tensile strain $J_{5\%} = 620$ kN/m, and strain
softening soil (as per the baseline case).

Simulation Results

Lateral facing displacement profiles for the baseline, PPS, and LER cases and two levels
of average applied vertical stress $q_v = 400$ kPa and $q_v = 800$ kPa are presented in Fig. 5(a). At
$q_v = 400$ kPa for the baseline case, a maximum lateral displacement of 60.6 mm occurs near the
top of the wall at elevation $z = 4.2$ m above the foundation soil. Lateral displacements for the
baseline and PPS cases are in close agreement and larger than for the LER case. At $q_v = 800$
kPa, lateral displacements increase significantly and the trends are similar. The baseline case
yields the largest lateral displacements with a maximum value of 148.4 mm at $z = 4.0$ m.

Maximum lateral displacements for the PPS and LER cases are 138.0 mm and 75.0 mm,
respectively. Corresponding profiles of maximum tensile force in the geogrid reinforcement are
presented in Fig. 5(b). At $q_v = 400$ kPa, the maximum tensile force (13.9 kN/m) occurs at $z =
4.8$ m for the baseline case with an associated tensile strain of 4.7%. The factor of safety (FS)
against reinforcement rupture is 5.0, based on the ultimate tensile strength $T_{ult} = 70$ kN/m (Table
2). For the PPS and LER cases, maximum tensile forces are 13.7 kN/m and 16.1 kN/m, and FS
= 5.1 and 4.3, respectively. Maximum tensile forces for the baseline and PPS cases are in close
agreement and slightly smaller than for the LER case. At $q_v = 800$ kPa, maximum tensile forces
increase significantly and the trends are similar; however, maximum tensile forces for the LER
case are much larger than for the baseline and PPS cases near the top of the wall. The maximum
tensile force of 21.3 kN/m occurs at $z = 4.6$ m for the baseline case with a corresponding tensile
strain of 14.4% and FS = 3.3. Maximum tensile forces are 21.0 kN/m and 33.6 kN/m for the PPS and LER cases, respectively, with corresponding values of FS = 3.3 and FS = 2.1.

The results of Fig. 5 show that, at the higher applied vertical stress $q_v = 800$ kPa, lateral displacements and maximum tensile forces are nearly equal for the baseline and PPS cases. This suggests that post-peak strain softening behavior for the soil is not a critical consideration for the conditions simulated. On the other hand, lateral displacements are much lower and maximum tensile forces are much higher for the LER case, which suggests that the geosynthetic constitutive model (i.e., linear vs. nonlinear) has a significant effect. Reinforcement stiffness is constant for the LER case and decreases significantly with increasing strain for the baseline and PPS cases (Fig. 4). As the applied vertical stress on the abutment increases and soil stiffness decreases, the reinforcement picks up a greater fraction of this load for the LER case.

Plots of maximum lateral facing displacement, average abutment compression, and corresponding average abutment vertical strain ($\varepsilon_v$) vs. average applied vertical stress ($q_v$) for the three simulation cases are shown in Fig. 6. In general, the results indicate that the baseline and PPS cases display nonlinear responses, whereas the LER case shows a nearly linear response. On both plots, deformations are essentially equal for the baseline and PPS cases for $q_v \leq 600$ kPa because the soil has not yet reached a strain softening condition. Beyond 600 kPa, the baseline case indicates lower stiffness than the PPS case. Deformations for the LER case are close to the baseline case for $q_v \leq 200$ kPa, and then deviate substantially with increasing applied vertical stress. This suggests that, for the conditions simulated, a linearly elastic reinforcement model can capture the deformation behavior of GRS bridge abutments at the service limit but not for higher applied stress conditions approaching failure. As such, the selection of a constant
reinforcement stiffness value may be difficult. In the current study, the $J_{5\%}$ value (620 kN/m) gives good accuracy for $q_v \leq 200$ kPa.

Based on the data in Fig. 6, Table 4 provides values of maximum lateral facing displacement $\Delta_{h,200}$ and average abutment compression $\Delta_{v,200}$ at the service limit of $q_v = 200$ kPa, vertical stress $q_{0.5\%}$ at the service limit of $\varepsilon_v = 0.5\%$, and vertical stress $q_{5\%}$ at the strength limit of $\varepsilon_v = 5\%$. Consistent with the trends in Fig. 5, the service limit values indicate essentially no effect for strain softening soil and a relatively minor effect for nonlinear reinforcement. In comparison, FHWA guidelines (Nicks et al. 2013) specify the allowable vertical stress at the service limit $q_{0.5\%}$ as 10% of the ultimate bearing capacity $q_{ult}$ (Wu and Pham 2013, Wu et al. 2013), where $q_{ult}$ is calculated as:

$$q_{ult} = \left[ \sigma_c' + 0.7 \frac{T_{ult}}{S_v} \right] K_p + 2c' \sqrt{K_p} \tag{10}$$

and $\sigma_c' = \text{effective confining stress}$ (typically taken as zero to be conservative), and $K_p =$ Rankine passive earth pressure coefficient. Using Eq. (10) and $\sigma_c' = 0$, the calculated value of $q_{0.5\%}$ is 61 kPa for the baseline case, which is approximately one-half of the simulated value (118 kPa). Similar conservative results using Eq. (10) were reported by Nicks et al. (2016) for loading tests on GRS mini-piers constructed using a well-graded soil. At the strength limit of $\varepsilon_v = 5\%$, the PPS simulation yielded a higher vertical stress by 14% and the LER simulation yielded a higher vertical stress by 75% than the baseline case. Thus, beyond the service limit, the effects of strain softening soil and nonlinear reinforcement can become significant and both should be taken into account as needed.
Parametric Study

A parametric study was conducted to investigate the effects of various reinforcement, backfill soil, and geometry parameters on the deformation behavior of GRS bridge abutments. The variables are reinforcement spacing, reinforcement stiffness, reinforcement length, secondary reinforcement, backfill soil cohesion, backfill soil friction angle, backfill soil dilation angle, bridge seat setback distance, bridge seat length, and abutment height. For each series of simulations, only the variable of interest was changed and the other variables were held constant and equal to the baseline case. Results are presented for maximum lateral facing displacement, vertical compression, and vertical strain of the GRS bridge abutment with increasing average applied vertical stress. A summary of values obtained at the service limit and strength limit is presented in Table 5.

Reinforcement Spacing

Numerical simulations were conducted for reinforcement vertical spacing $S_v = 0.2$ m, 0.4 m, and 0.6 m. In each case, a soil lift thickness of 0.2 m was maintained for the numerical construction procedure. Fig. 7 indicates that abutment deformations increase significantly with increasing reinforcement spacing. For instance, at the service limit of $q_v = 200$ kPa, $\Delta_{v,200}$ increases from 38.0 mm to 93.6 mm and $\Delta_{v,200}$ increases from 33.6 mm to 70.2 mm when $S_v$ increases from 0.2 m to 0.6 m. At the service limit of $\varepsilon_v = 0.5\%$, the value of $q_{0.5\%} = 118$ kPa for $S_v = 0.2$ m is nearly twice that for $S_v = 0.6$ m (65 kPa). At the strength limit, $q_{5\%}$ decreases significantly and nonlinearly from 917 kPa to 519 kPa to 364 kPa when $S_v$ increases from 0.2 m to 0.4 m to 0.6 m.
Reinforcement Stiffness

Simulations were conducted for three HDPE geogrids, Geogrid-1, Geogrid-2 (baseline case), and Geogrid-3, as originally described by Yu et al. (2016). Material properties are provided in Table 2 and nonlinear tensile behavior is illustrated in Fig. 4. Geogrid-1 has the lowest stiffness, Geogrid-2 is intermediate, and Geogrid-3 has the highest stiffness. Fig. 8 indicates that the maximum lateral facing displacement and vertical compression of the abutment decrease significantly with increasing reinforcement stiffness. At \( q_v = 200 \text{kPa} \), \( \Delta_{h,200} \) decreases from 47.6 mm to 30.7 mm and \( \Delta_{r,200} \) decreases from 41.5 mm to 28.8 mm when reinforcement changes from Geogrid-1 to Geogrid-3. Correspondingly, \( q_{0.5\%} \) increases from 104 kPa to 143 kPa and \( q_{5\%} \) increases from 500 kPa to 1121 kPa.

Reinforcement Length

Abutment deformations for reinforcement length \( L_r = 0.3 \, h, 0.5 \, h, 0.7 \, h, 0.9 \, h, \) and 1.1 \( h \) are presented in Fig. 9 and decrease only slightly with increasing reinforcement length for \( L_r \geq 0.5 \, h \), which is consistent with the findings of Zheng and Fox (2016a) for service load conditions. At the strength limit, \( q_{5\%} \) increases from 898 kPa to 948 kPa when \( L_r \) increases from 0.5 \( h \) to 1.1 \( h \). For \( L_r = 0.3 \, h \) (\( = 1.5 \) m), the deformations are much larger than the other cases and failure occurs at a lower applied vertical stress (523 kPa). In this case, the reinforcement does not extend beyond the failure surface, which intersects the heel of the bridge seat at the top of the wall (distance from wall facing \( x = 1.7 \) m).
Secondary Reinforcement

Secondary reinforcement layers often are included below the bridge seat to provide additional support, and are specified for the GRS-IBS design method (Adams et al. 2011b). In the current study, numerical simulations were conducted for secondary reinforcement layer number $n_{sr} = 0, 5, 10, \text{ and } 15$, where $n_{sr} = 0$ indicates no secondary reinforcement and $n_{sr} = 15$ indicates 15 layers of secondary reinforcement between elevations $z = 2.0 \text{ m and } 5.0 \text{ m}$. The secondary reinforcement layers have length $L_{s} + 2d_{p} (= 1.9 \text{ m})$ and are not connected to the facing blocks. The results in Fig. 10 show that, when $n_{sr}$ increases from 0 to 15, abutment deformations are only slightly reduced for $q_{v} \leq 200 \text{ kPa}$. At higher stress levels, abutment deformations decrease significantly with an increasing number of secondary reinforcement layers. For example, at the strength limit, $q_{5\%}$ increases from 917 kPa for $n_{sr} = 0$ to 1232 kPa for $n_{sr} = 15$. These results are consistent with the findings from large-scale loading tests on GRS mini-piers, which indicate that secondary reinforcement is unlikely to reduce abutment compression for service loads but can increase the ultimate bearing capacity (Nicks et al. 2013).

Backfill Soil Cohesion

Abutment deformations for backfill soil cohesion $c' = 0, 5 \text{ kPa}, 10 \text{ kPa}, \text{ and } 15 \text{ kPa}$ are presented in Fig. 11. Corresponding values of adhesion for soil-block and soil-geogrid interfaces were obtained using Equation (9). The effect of increasing soil cohesion on abutment deformations is small for service limit conditions, and becomes more important at higher stress levels. As the cohesion increases from 0 to 15 kPa, $q_{0.5\%}$ increases from 118 kPa to 135 kPa and $q_{5\%}$ increases from 917 kPa to 1008 kPa.
Backfill Soil Friction Angle

Simulations were conducted for backfill soil friction angle $\phi_p' = 38^\circ, 42^\circ, 46^\circ,$ and $52^\circ,$ with $\phi_{cv}' = 35^\circ, 39^\circ, 43^\circ,$ and $49^\circ,$ respectively. Corresponding friction angles for soil-block and soil-geogrid interfaces were obtained using Equation (9). The results in Fig. 12 indicate that friction angle has a significant effect on abutment deformations, including both the service limit and strength limit. For instance, $\Delta_{h,200}$ decreases from 51.4 mm to 34.3 mm and $\Delta_{v,200}$ decreases from 40.7 mm to 31.2 mm when $\phi_p'$ increases from $38^\circ$ to $52^\circ.$ Correspondingly, $q_{0.5\%}$ increases from 99 kPa to 127 kPa at the service limit of $\varepsilon_v = 0.5\%$ and $q_{5\%}$ increases from 682 kPa to 1059 kPa at the strength limit of $\varepsilon_v = 5\%.$

Backfill Soil Dilation Angle

Simulations were conducted for soil dilation angle $\psi_p = 6^\circ, 12^\circ, 18^\circ,$ and $24^\circ,$ and the results are presented in Fig. 13. In general, maximum lateral facing displacements are not significantly affected by dilation angle. Conversely, abutment vertical compression decreases with increasing $\psi_p,$ especially at higher stress levels. For instance, at the strength limit, $q_{5\%}$ increases from 777 kPa to 968 kPa when $\psi_p$ increases from $6^\circ$ to $24^\circ.$

Bridge Seat Setback Distance

Abutment deformations for bridge seat setback distance $a_b = 0.2$ m, 0.6 m, 1.0 m, and 1.4 m are presented in Fig. 14. Bridge seat setback has little effect on maximum lateral facing displacement for $q_v \leq 600$ kPa, whereas these values decrease with increasing $a_b$ at higher
applied vertical stress levels. Similarly, abutment vertical compression decreases and $q_{5\%}$ increases from 917 kPa to 1127 kPa as $a_{b}$ increases from 0.2 m to 1.4 m. The effect of bridge seat setback is insignificant for service limit conditions.

**Bridge Seat Length**

Abutment deformations for bridge seat length $L_s = 1.0$ m, 1.5 m, 2.0 m, and 2.5 m are presented in Fig. 15. Bridge seat length has little effect for service limit conditions. At higher stress levels, the maximum lateral facing displacement and abutment compression generally increase with increasing $L_s$. At the strength limit, $q_{5\%}$ decreases nonlinearly from 983 kPa to 917 kPa to 907 kPa when $L_s$ increases from 1.0 m to 1.5 m to 2.0 m. However, for $L_s = 2.5$ m, the maximum lateral displacement curve is similar to $L_s = 1.5$ m and the abutment compression curve is similar to $L_s = 1.0$ m.

**Abutment Height**

Numerical simulations were conducted for GRS bridge abutments with height $h = 3$ m, 5 m, 7 m, and 9 m. Fig. 16 indicates that maximum lateral facing displacement and abutment compression increase with increasing abutment height. For example, at $q_v = 200$ kPa, $\Delta_{h,200}$ increases from 26.7 mm to 60.6 mm and $\Delta_{v,200}$ increases from 23.9 mm to 43.1 mm when $h$ increases from 3 m to 9 m. Normalized relationships for maximum lateral facing displacement divided by abutment height are shown in Fig. 16(c). The four relationships essentially converge for $q_v \leq 200$ kPa and thus indicate that maximum lateral facing displacements are proportional to abutment height for service limit conditions. Interestingly, at higher applied stress levels,
normalized maximum lateral facing displacement decreases as $h$ increases from 3 m to 9 m for the same applied vertical stress. Corresponding vertical stress-strain relationships, in which abutment vertical compression is normalized by abutment height, are presented in Fig. 16(d) and show similar trends. Thus, taller abutments have a stiffer response. This is attributed to higher average effective stress conditions and associated larger soil stiffness for the taller abutments. The results in Fig. 16(c) and Fig. 16(d) suggest that, all else being equal, laboratory or field tests conducted on reduced-scale physical models with lower average effective stress conditions may yield conservative (i.e., less stiff) vertical stress-strain relationships for the design of GRS bridge abutments.

**Failure Surface**

The failure surface for the GRS bridge abutment develops as shear strains increase during the loading stage. Contours of shear strain magnitude for the baseline case at the service limit ($\varepsilon_v = 0.5\%$) and strength limit ($\varepsilon_v = 5\%$) are shown in Fig. 17. At the service limit, shear strains are concentrated at the heel of the bridge seat and suggest a potential failure surface that moves downward from the heel to the toe of the abutment. At the strength limit, the abutment is approaching failure as manifested by the formation of large shear strain zones. The failure mechanism is a combination of punching shear failure of the bridge seat and internal shear failure of the GRS bridge abutment. The internal failure surface migrates vertically downward from the heel of the bridge seat to approximately the mid-height of the abutment, and then diagonally to the toe of the abutment. A similar failure surface shape for GRS bridge abutments was identified by Leshchinsky (2014) based on limit analysis.
Following an approach similar to Fig. 17(b), a bilinear failure surface was constructed at the strength limit for each simulation of the parametric study based on contours of shear strain magnitude. These simplified diagrams are presented together for comparison in Fig. 18. In general, the geometry of these surfaces show close similarity over a wide range of simulated conditions, with some exceptions. The bilinear surface consistently starts at the heel of bridge seat and migrates downward to the mid-height of the GRS bridge abutment and then diagonally to the toe of the abutment. Failure surfaces show essentially no effect from changing vertical reinforcement spacing in Fig. 18(a), and similar close agreement for variable geogrid stiffness and geogrid length in Fig. 18(b) and Fig. 18(c), respectively. The failure surfaces in Fig. 18(d) indicate that the intersection point of the bilinear surface moves downward with increasing number of secondary reinforcement layers, as might be expected. The failure surfaces in Figs. 18(e)–(g) indicate that backfill soil cohesion, friction angle, and dilation angle have little effect on failure surface geometry. Conversely, the failure surfaces in Figs. 18(h)–(j) show that abutment geometry has an important effect. Fig. 18(h) indicates that increasing the bridge seat setback distance changes the slope of the upper line of the bilinear failure surface but, interestingly, has no effect on the intersection point or lower line for the conditions investigated. Fig. 18(i) indicates that increasing the bridge seat length changes the geometry for both sections of the failure surface but the vertical elevation of the intersection point remains consistent. Finally, Fig. 18(j) indicates that abutments with heights of 5 m, 7 m, and 9 m have the same relative geometry when plotted as \( z/h \); however, the lower height of \( h = 3 \text{ m} \) displays a clearly different geometry that is similar to the failure surfaces for abutments with larger \( a_b \) and \( L_s \).

Based on the trends in Fig. 18, a general bilinear failure surface is proposed and illustrated in Fig. 19 for GRS bridge abutments with conditions similar to those investigated in
the current study. The failure surface starts at the heel of the bridge seat and moves downward to an intersection point at mid-height \((z = h/2)\) and then diagonally to the toe of the abutment.

The horizontal location of the intersection point is controlled by geometry. For \(a_b + L_s \leq h/3\), the upper line is vertical and the intersection point is located at \(x = a_b + L_s\). For \(a_b + L_s > h/3\), the upper line is not vertical and the intersection point is located at \(x = h/3\). The proposed failure surface is predicated on the assumption that secondary reinforcement, if present, is contained within the top half of the abutment.

### Conclusions

A numerical investigation of deformation and failure behavior for geosynthetic reinforced soil (GRS) bridge abutments was conducted using finite difference analysis. The backfill soil was characterized using a nonlinear elasto-plastic model that incorporates a hyperbolic stress-strain relationship with strain softening behavior and the Mohr-Coulomb failure criterion. The geogrid reinforcement was characterized using a hyperbolic load-strain-time model. For each numerical simulation, the GRS bridge abutment model was constructed in stages, including soil compaction effects, and then monotonically loaded in stages to failure. A parametric study was conducted to investigate the effects of various parameters on abutment deformation and failure behavior. The following conclusions are reached for the conditions investigated in this study:

1. As compared to simulations for elastic-perfectly plastic soil and linearly elastic reinforcement, strain softening behavior of the backfill soil and nonlinear behavior of the geogrid reinforcement had relatively small effects on abutment deformations at the service limit \((\varepsilon_s = 0.5\% \text{ or } q_s = 200 \text{ kPa})\). However, these effects, and especially nonlinear
reinforcement, became significant above the service limit leading to the strength limit ($\varepsilon_v = 5\%$). A linearly elastic reinforcement model was able to characterize deformation behavior of GRS bridge abutments at the service limit, but not for higher applied vertical stress conditions approaching failure. Bearing capacity at the strength limit was slightly overestimated using a perfectly plastic soil model and significantly overestimated using a linearly elastic reinforcement model.

2. Reinforcement spacing, reinforcement stiffness, backfill soil friction angle, and abutment height had the most significant effects on abutment deformations. The maximum lateral facing displacement and abutment vertical compression decreased significantly with decreasing reinforcement spacing, increasing reinforcement stiffness, and increasing backfill soil friction angle. As abutment height increased, the maximum lateral facing displacement and abutment vertical compression increased; however, the normalized maximum lateral facing displacement and vertical strain decreased. Secondary reinforcement had a relatively small effect at the service limit and significantly increased the bearing capacity at the strength limit.

3. Reinforcement and backfill soil properties had little effect on the geometry of the failure surface. Conversely, parameters associated with abutment geometry, such as bridge seat length, bridge seat setback distance, and abutment height, had important effects. The failure surface can be approximated as bilinear, starting at the heel of the bridge seat, moving downward to an intersection point at mid-height of the abutment, and then diagonally to the toe of the abutment, as illustrated in Fig. 19.

Acknowledgements
Financial support for this investigation was provided by the California Department of Transportation (Caltrans) and is gratefully acknowledged. The authors thank Dr. Charles S. Sikorsky of the Caltrans Office of Earthquake Engineering for his support and assistance with the project and Dr. P. Benson Shing, Professor and Chair of the Department of Structural Engineering at University of California, San Diego, for several helpful discussions on the design of bridge systems.

**Notation**

_The following symbols are used in this paper:_

- $A_r$: reinforcement cross-sectional area
- $a_b$: bridge seat setback distance
- $B$: bulk modulus
- $c'$: soil cohesion
- $c_i'$: interface adhesion
- $D$: bridge beam depth
- $d_{\text{max}}$: soil maximum particle size
- $d_e$: distance between top facing block and bridge beam
- $E$: elastic modulus
- $E_r$: reinforcement elastic modulus
- $E_t$: soil tangent elastic modulus
- $E_{ur}$: soil unloading-reloading elastic modulus
- $F_v$: vertical force per unit width on bridge abutment
553  \( h \) = abutment height
554  \( J_t \) = reinforcement tangent stiffness
555  \( J_s \) = reinforcement secant stiffness
556  \( J_0 \) = reinforcement initial stiffness
557  \( J_{5\%} \) = reinforcement secant stiffness at 5% strain
558  \( K \) = elastic modulus number
559  \( K_b \) = bulk modulus number
560  \( k_n \) = interface normal stiffness
561  \( K_p \) = Rankine passive earth pressure coefficient
562  \( k_s \) = interface shear stiffness
563  \( K_{ur} \) = unloading-reloading modulus number
564  \( L_b \) = bridge span
565  \( L_c \) = contact length between bridge beam and bridge seat
566  \( L_s \) = bridge seat length
567  \( L_r \) = reinforcement length
568  \( m \) = bulk modulus exponent
569  \( n \) = elastic modulus exponent
570  \( n_{sr} \) = number of secondary reinforcement layers
571  \( p_a \) = atmospheric pressure
572  \( q_{ult} \) = ultimate bearing capacity
\( q_v \) = average applied vertical stress on GRS bridge abutment

\( q_{0.5\%} \) = average applied vertical stress on GRS bridge abutment at 0.5\% strain

\( q_{5\%} \) = average applied vertical stress on GRS bridge abutment at 5\% strain

\( RF \) = interface shear strength reduction factor

\( R_f \) = failure ratio

\( R_{sd} \) = ratio of bridge beam span to bridge beam depth

\( S_v \) = reinforcement vertical spacing

\( T \) = reinforcement tensile force

\( T_{ult} \) = reinforcement ultimate tensile strength

\( T_{5\%} \) = reinforcement tensile force at 5\% strain

\( t \) = time

\( t_r \) = reinforcement thickness

\( x \) = horizontal distance from back side of wall facing

\( z \) = vertical distance above top surface of foundation soil

\( \chi \) = empirical fitting parameter

\( \Delta_{h,200} \) = maximum lateral facing displacement for \( q_v \) = 200 kPa

\( \Delta_{v,200} \) = average abutment compression for \( q_v \) = 200 kPa

\( \delta_i' \) = interface friction angle

\( \varepsilon \) = reinforcement tensile strain

\( \varepsilon_p \) = soil incremental plastic shear strain

\( \varepsilon_v \) = average abutment vertical strain
\( \phi' = \text{soil friction angle} \)

\( \phi'_{cv} = \text{soil constant volume friction angle} \)

\( \phi'_{p} = \text{soil peak friction angle} \)

\( \gamma = \text{soil unit weight} \)

\( \gamma_{b} = \text{bridge beam unit weight} \)

\( \nu = \text{Poisson’s ratio} \)

\( \nu_{t} = \text{tangent Poisson’s ratio} \)

\( \sigma'_{c} = \text{effective confining stress} \)

\( \sigma'_{1} = \text{major principal effective stress} \)

\( \sigma'_{3} = \text{minor principal effective stress} \)

\( \psi = \text{soil dilation angle} \)

\( \psi_{cv} = \text{soil constant volume dilation angle} \)

\( \psi_{p} = \text{soil peak dilation angle} \)

References


*FLAC2D Version 7.0* [Computer software]. (2011). Itasca Consulting Group, Minneapolis, MN, USA.


block wall structure to support bridge abutments.” *Earth Reinforcement*, Vol. 1, Balkema,
Rotterdam, Netherlands, 543–548.

No. FHWA-RD-00-038*, U.S. DOT, Washington, D.C.

guidelines for geosynthetic-reinforced soil bridge abutments with a flexible facing.” *NCHRP
Report 556*, Transportation Research Board, Washington, D.C.

on GRS bridge abutments with flexible facing.” *Journal of Geotechnical and

strength of closely spaced soil-geosynthetic composites.” *Journal of Geotechnical and


19, No. 1, 62–78.


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<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Backfill Soil</strong></td>
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<tr>
<td>Unit weight, $\gamma$ (kN/m$^3$)</td>
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<td>Unloading-reloading elastic modulus number, $K_{ur}$</td>
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<td>Elastic modulus exponent, $n$</td>
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<td>Failure ratio, $R_f$</td>
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<td>Bulk modulus number, $B$</td>
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<tr>
<td>Bulk modulus exponent, $m$</td>
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<td>Atmospheric pressure, $p_a$ (kPa)</td>
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<tr>
<td>Cohesion, $c'$ (kPa)</td>
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<td>Peak friction angle, $\phi_p'$ (°)</td>
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<td>Constant volume friction angle, $\phi_{cv}'$ (°)</td>
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<td>Peak dilation angle, $\psi_p$ (°)</td>
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<td>Constant volume dilation angle, $\psi_{cv}$ (°)</td>
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<tr>
<td><strong>Foundation Soil</strong></td>
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<td>Unit weight, $\gamma$ (kN/m$^3$)</td>
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<tr>
<td>Elastic modulus, $E$ (MPa)</td>
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<td>Poisson’s ratio, $\nu$</td>
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<td>Cohesion, $c'$ (kPa)</td>
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<td>Friction angle, $\phi$ (°)</td>
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<td>Dilation angle, $\psi$ (°)</td>
<td>14</td>
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</table>

$^a$ from Yu et al. (2016).
Table 2. Reinforcement parameters.

<table>
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<tr>
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<th>Geogrid-1</th>
<th>Geogrid-2</th>
<th>Geogrid-3</th>
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</thead>
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<td>Elastic modulus, $E_r$</td>
<td>Variable $^a$</td>
<td>Variable $^a$</td>
<td>Variable $^a$</td>
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<td>Cross-sectional area, $A_r$</td>
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<td>0.002 m$^2$</td>
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<td>Thickness, $t_r$</td>
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<td>2 mm</td>
<td>2 mm</td>
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<tr>
<td>Tensile strength @5% strain, $T_{5%}$ $^b$</td>
<td>27 kN/m</td>
<td>31 kN/m</td>
<td>52 kN/m</td>
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<tr>
<td>Ultimate tensile strength, $T_{ult}$ $^b$</td>
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<td>70 kN/m</td>
<td>114 kN/m</td>
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<tr>
<td>Initial tensile stiffness, $J_0$ $^c$</td>
<td>524 kN/m</td>
<td>596 kN/m</td>
<td>1085 kN/m</td>
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<tr>
<td>Fitting parameter, $\chi$ $^c$</td>
<td>0.0958 m/kN</td>
<td>0.0359 m/kN</td>
<td>0.0326 m/kN</td>
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$^a$ Calculated using Eqs. (7-8) based on parameters reported by Yu et al. (2016).

$^b$ Provided by manufacturer.

$^c$ Calculated for $t = 3600$ hours.
**Table 3. Interface parameters.**

<table>
<thead>
<tr>
<th>Property</th>
<th>Soil-geogrid</th>
<th>Soil-block/bridge seat</th>
<th>Block-block</th>
<th>Bridge beam-bridge seat</th>
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<td>100,000 MPa/m</td>
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<tr>
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<tr>
<td>Friction angle, $\delta_i$</td>
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<td>33.9°  b</td>
<td>36.0°  c</td>
<td>21.8°  d</td>
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<td>0</td>
<td>0</td>
<td>58 kPa c</td>
<td>0</td>
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</table>

a Based on average of data ($RF = 0.85$) from Vieira et al. (2013).
b Based on data ($RF = 0.65$) from Ling et al. (2010).
c Based on Yu et al. (2016).
d Based on a friction coefficient of 0.4 for bearing pads from Caltrans (1994).
Table 4. Deformations and vertical stresses for three simulation cases at the service limit and strength limit.

<table>
<thead>
<tr>
<th>Case</th>
<th>Service limit</th>
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<th>Strength limit</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>$\Delta_{h,200}$ (mm)</td>
<td>$\Delta_{v,200}$ (mm)</td>
<td>$q_{0.5%}$ (kPa)</td>
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<td>Baseline</td>
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<tr>
<td>Perfectly plastic soil</td>
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<td>Linearly elastic reinforcement</td>
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Table 5. Results from parametric study at the service limit and strength limit.

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<th>Strength limit</th>
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<tr>
<td>0.4 m</td>
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Fig. 2. Relationships for soil parameters with incremental plastic shear strain: (a) friction angle; (b) dilation angle.
Fig. 3. Comparison of measured and simulated triaxial test results: (a) deviator stress vs. axial strain; (b) volumetric strain vs. axial strain.
Fig. 4. Tensile behavior for three HDPE geogrids at $t = 3600$ hours: (a) tensile force-strain relationship; (b) tangent stiffness (parameters from Yu et al. 2016).
Fig. 5. Simulation results for $q_v = 400$ kPa and $q_v = 800$ kPa: (a) lateral facing displacement; (b) maximum tensile force in reinforcement.
Fig. 6. Simulation results: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
Fig. 7. Effect of reinforcement spacing: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
**Fig. 8.** Effect of reinforcement stiffness: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
**Fig. 9.** Effect of reinforcement length: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
Fig. 10. Effect of secondary reinforcement: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
Fig. 11. Effect of backfill soil cohesion: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
Fig. 12. Effect of backfill soil friction angle: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
Fig. 13. Effect of backfill soil dilation angle: (a) maximum lateral facing displacement; (b) abutment compression and vertical strain.
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Fig. 17. Contours of shear strain magnitude for baseline case: (a) service limit ($\varepsilon_v = 0.5\%$); (b) strength limit ($\varepsilon_v = 5\%$).
Fig. 18. Bilinear failure surfaces for parametric study: (a) reinforcement spacing; (b) reinforcement stiffness; (c) reinforcement length; (d) secondary reinforcement; (e) backfill soil cohesion; (f) backfill soil friction angle; (g) backfill soil dilation angle; (h) bridge seat setback distance; (i) bridge seat length; (j) abutment height.
Fig. 19. Proposed general bilinear failure surface for GRS bridge abutments: (a) $a_b + L_s \leq h/3$; (b) $a_b + L_s > h/3$. 

\[ -a_b + L_s \]

\[ \frac{h}{2} \]

\[ a_b + L_s \]

\[ \frac{h}{3} \]

\[ 1 \]

\[ \frac{h}{2} \]
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