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Force Decomposition Analysis: A method to decompose intermolecular forces into physically relevant component contributions

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Abstract

Computational quantum chemistry can be more than just numerical experiments when methods are specifically adapted to investigate chemical concepts. One important example is the development of energy decomposition analysis (EDA) to reveal the physical driving forces behind intermolecular interactions. In EDA, typically the interaction energy from a good-quality density functional theory (DFT) calculation is decomposed into multiple additive components that unveil permanent and induced electrostatics, Pauli repulsion, dispersion, and charge-transfer contributions to non-covalent interactions. Herein, we formulate, implement and investigate decomposing

the forces associated with intermolecular interactions into the same components. The resulting force decomposition analysis (FDA) is potentially useful as a complement to the EDA to understand chemistry, while also providing far more information than an EDA for data analysis purposes such as training physics-based force fields. We apply the FDA based on absolutely localized molecular orbitals (ALMOs) to analyze interactions of water with sodium and chloride ions as well as in the water dimer. We also analyze the forces responsible for geometric changes in carbon dioxide upon adsorption onto (and activation by) gold and silver anions. We also investigate how the force components of an EDA-based force field for water clusters, namely MB-UCB, compare to those from force decomposition analysis.

1 Introduction

Intermolecular interactions are important for understanding chemistry as they affect structures, properties, and reactivity of chemical systems. Examples include red- or blue-shifts in vibrational frequencies when forming hydrogen bonds,¹⁻⁷ wavelength tuning of organic chromophores by the solvation or protein environment,⁸⁻¹⁴ and modulation of the catalytic performance of molecular CO₂RR catalysts through interactions with ligands in complexes' second coordination sphere.¹⁵⁻²²

Decomposing non-covalent interactions has been increasingly important to understanding the origins of these interactions as well as the development of classical force fields for the simulation of chemical and biochemical systems.²³⁻³¹ Moreover, to obtain statistical mechanical ensembles of a condensed phase chemical system, molecular dynamics simulations are required, for which accurate and efficient evaluation of intermolecular forces is important for systems where quantum chemical calculations are impractical.

Many energy decomposition analysis (EDA) methods have been proposed for separating different physical contributions to the non-covalent interaction energy, which are reviewed elsewhere.³²⁻³⁸ **Alternatively, Quantum Chemical Topology (QCT) methods such as the so-**

called Interacting Quantum Atoms (IQA)^{39,40} also afford the decomposition of the total (or interaction) energies, in particular into atomic and diatomic terms. With such a strategy both the covalent and non-covalent interactions are treated on equal footing⁴¹ and, with the help of machine learning, force fields like FFLUX⁴² are being developed. In this work, we are using the absolutely localized molecular orbitals EDA (ALMO-EDA),^{38,43–46} which divides the interaction energy into frozen (interaction between unrelaxed monomers), polarization (energy lowering due to intra-fragment relaxation of monomer wavefunctions), and charge transfer (energy lowering due to electron delocalization between fragments) contributions. The adiabatic EDA⁴⁷ optimizes the geometry successively on each of the intermediate potential energy surfaces (frozen, polarized, and fully relaxed), in essence attributing geometric changes and shifts in other molecular properties upon the formation of intermolecular complexes to the same terms as in ALMO-EDA. The adiabatic EDA has been successfully used to understand geometric changes arising from intermolecular interactions in a wide variety of systems.^{6,47–52} For example, the \angle N-B-H angle in the ammonia-borane complex only bends when charge is allowed to flow from the ammonia to the borane molecule.^{47,52} The adiabatic EDA thus attributes changes in *observables* to the different EDA contributions, which can be crucial for connecting to experimental results. Relationships between observables and descriptors originating from QCT approaches have also been reported.^{53,54}

Many fixed-charge and polarizable force fields have been developed over the years for condensed-phase molecular simulations.^{27–29,31,55–61} Recently, the T. Head-Gordon lab developed the MB-UCB many-body force field for water-water and water-ion interactions,^{29,31} which employs terms that resemble those produced by ALMO-EDA of quantum mechanical calculations. For example, the polarization energy in the second-generation ALMO-EDA allows electrons to move to the space of dipolar and quadrupolar density response to an external electric field, while MB-UCB uses distributed multipole analysis of classical anisotropic dipolar polarization to evaluate the polarization energy. Impressively, the terms from the different methods are consistent with each other for a wide variety of water dimer geometries

despite being designed independently of each other.²⁹ While the total interaction energy and its breakdown given by MB-UCB and ALMO-EDA are in very good agreement, the forces remain to be compared to ensure the quality of dynamics driven by MB-UCB within a large ensemble of configurations.

In this work, we decompose the forces of an intermolecular interaction into constituent terms that directly correspond to those within the ALMO-EDA. After presenting the relevant theory, we demonstrate the usefulness of this decomposition for understanding chemistry with proof-of-concept examples of water interacting with sodium and chloride ions as well as the water dimer. We transform these forces to the internal coordinates using Wilson’s B-matrix,⁶² allowing us to see forces that are more intuitive and relatable to vibrational spectroscopy. For example, the H-O-H bending in the water molecule is used to understand the molecular environment.⁶³ We then study CO₂ adsorption and activation on Au and Ag anions and compare the two systems’ forces within internal coordinates. The force decomposition is also applied to validate the forces produced by the MB-UCB force field. The force decomposition results, based on high-quality DFT calculations of the forces, may also be useful for future force-field training. This work builds on the adiabatic EDA to advance the idea of “property decomposition” analysis, in which not only the interaction energy is broken down, but also other derivatives of the energy, which are molecular properties. This general approach can be extended to the effect of intermolecular interactions on other properties of interest, such as the hessian matrix, NMR chemical shieldings, dipole moments or polarizabilities, etc. The observable changes in properties associated with non-covalent interactions can then be attributed to the different physical effects at play.

2 Theory

2.1 Energy Decomposition Analysis

In the ALMO-EDA, the total binding energy of an intermolecular complex is broken down into four components coming from the successive removal of constraints to minimize the energy of the supersystem:

$$\Delta E_{\text{bind}} = \Delta E_{\text{GD}} + \Delta E_{\text{frz}} + \Delta E_{\text{pol}} + \Delta E_{\text{ct}} \quad (1)$$

The geometric distortion ΔE_{GD} refers to the energy consumed for each fragment to change its geometry from the equilibrium structure in isolation to that in the complex. The frozen (FRZ) interaction energy, ΔE_{frz} , is defined by the energy of the frozen wavefunction,⁶⁴ relative to that of the isolated non-interacting fragments (in distorted geometries). It corresponds to the energy change upon moving the isolated fragments into their positions in the complex while keeping their own electronic structure unchanged. The frozen wavefunction is the antisymmetric product of the isolated fragment wavefunctions, whose associated one-particle density matrix (1PDM), \mathbf{P}_{frz} , is given by

$$\mathbf{P}_{\text{frz}} = (\mathbf{C}_o)_{\text{frz}} \boldsymbol{\sigma}_{\text{frz}}^{-1} (\mathbf{C}_o)_{\text{frz}}^T, \quad (2)$$

where $(\mathbf{C}_o)_{\text{frz}}$ is the direct sum of the (occupied) AO-to-MO coefficient matrices of the isolated fragments and $\boldsymbol{\sigma}_{\text{frz}}$ is the overlap matrix of the orbitals coming from the $(\mathbf{C}_o)_{\text{frz}}$ matrix. This 1PDM definition gives us the frozen interaction energy definition:

$$\Delta E_{\text{frz}} = E[\mathbf{P}_{\text{frz}}] - \sum_A E[\mathbf{P}_A]. \quad (3)$$

The next contribution, the polarization energy (ΔE_{pol}), arises from allowing the occupied orbitals on each fragment to mix with the virtuals *only* on the same fragment. Minimizing

the energy subject to this constraint, also known as the SCF-MI procedure,⁶⁵⁻⁶⁹ leaves the AO-to-MO coefficient matrix still block-diagonal and the corresponding MOs "absolutely localized" on each fragment while also polarized in the presence of each other. The resulting electronic wavefunction is referred to as the polarized state, whose 1PDM is denoted as \mathbf{P}_{pol} . The polarization energy is then defined as the energy lowering of the polarized state relative to the frozen state:

$$\Delta E_{\text{pol}} = E[\mathbf{P}_{\text{pol}}] - E[\mathbf{P}_{\text{frz}}]. \quad (4)$$

Since the polarization density comes from variationally minimizing the energy, ΔE_{pol} is negative semi-definite. Lastly, by removing the ALMO constraint, we obtain the fully relaxed state for the intermolecular complex. The energy lowering due to electron delocalization is defined as the charge transfer term (ΔE_{ct}):

$$\Delta E_{\text{ct}} = E[\mathbf{P}_{\text{full}}] - E[\mathbf{P}_{\text{pol}}], \quad (5)$$

where \mathbf{P}_{full} is the 1PDM for the fully relaxed state.

2.2 Force Decomposition Analysis

Within a variational EDA scheme like the ALMO-EDA, the analytic nuclear forces associated with each of the intermediate (including the initial and final) states can be obtained. Following the derivations in our previous work,⁴⁷ namely the adiabatic EDA scheme where the nuclear forces were used to optimize the complex geometry on the frozen, polarized, and fully relaxed surfaces, here we introduce the ALMO-based force decomposition analysis (FDA) method, where the nuclear derivatives of the frozen (ΔE_{frz}), polarization (ΔE_{pol}), and charge transfer (ΔE_{ct}) components of the interaction energy, as well as that of the classical electrostatics component of the frozen interaction ($\Delta E_{\text{cls-elec}}$), are obtained. Note that many of the derivations here can be applied to other variational EDA schemes.

Just as ALMO-EDA decomposes an interaction energy, the ALMO-based FDA decom-

poses *intermolecular forces* into frozen, polarization, and charge transfer components:

$$\Delta \mathbf{F}_{\text{bind}} = \Delta \mathbf{F}_{\text{GD}} + \Delta \mathbf{F}_{\text{frz}} + \Delta \mathbf{F}_{\text{pol}} + \Delta \mathbf{F}_{\text{ct}} \quad (6)$$

We define the geometric distortion force $\Delta \mathbf{F}_{\text{GD}}$ consistently with the ΔE_{GD} term. Thus $\Delta \mathbf{F}_{\text{GD}}$ consists of the forces associated with deforming to the complex geometry:

$$\Delta \mathbf{F}_{\text{GD}} = \sum_A \mathbf{F}_A[\mathbf{P}_A] - \sum_A \mathbf{F}_A^{\text{iso.geom.}}[\mathbf{P}_A] \quad (7)$$

The second term typically vanishes since the isolated fragment geometry has zero forces for a stable geometry. As for ΔE_{GD} , the geometric distortion force, $\Delta \mathbf{F}_{\text{GD}}$, is non-zero if the fragment geometries in the complex are different from the isolated ones. All of these forces are standard electronic structure derivatives, and we do not discuss them further.

The frozen component of the intermolecular forces ($\Delta \mathbf{F}_{\text{frz}}$) can be obtained by differentiating Eq. (3) with respect to the nuclear coordinates:

$$\Delta \mathbf{F}_{\text{frz}} = \mathbf{F}_{\text{frz}}[\mathbf{P}_{\text{frz}}] - \sum_A \mathbf{F}_A[\mathbf{P}_A] \quad (8)$$

where \mathbf{F}_{frz} denotes the forces on the frozen PES, and the term being subtracted on the right-hand side is the collection of isolated fragment forces that arises from the distortion of fragment structures within the complex. Note that these isolated fragment forces can be compared to the nuclear derivatives of the bonded terms in molecular mechanical force fields, while in this work we focus on the intermolecular force components. With superscripts “ x ” signifying derivatives with respect to the x -th nuclear coordinate (and superscripts “ \mathbf{S} ” and “ Δ_A ” in the same fashion), based on the derivation in our previous work,⁴⁷ the x -th component of forces on the frozen surface, $(F_{\text{frz}})_x$, is given by

$$(F_{\text{frz}})_x = - \left[V_{\text{nn}}^x + \mathbf{P}_{\text{frz}} \cdot \mathbf{h}^x + \frac{1}{2} \mathbf{P}_{\text{frz}} \cdot \mathbf{H}^x \cdot \mathbf{P}_{\text{frz}} + E_{\text{xc}}^x + E_{\text{frz}}^{\mathbf{S}} \cdot \mathbf{S}^x + \sum_A (E_{\text{frz}}^{\Delta_A} \cdot \Delta_A^x) \right], \quad (9)$$

where V_{nn} is the nuclear-nuclear coulomb repulsion potential, \mathbf{h} is the core Hamiltonian (kinetic energy and nuclei-electron attractions), \mathbf{II} is the AO two-electron integrals, E_{xc} is the Kohn-Sham (KS) exchange-correlation energy, \mathbf{S} is the AO overlap matrix, and $\mathbf{\Delta}_A$ is the matrix of occupied-virtual orbital rotations (variational parameters) within a given fragment. The first four terms are identical to those in the KS-DFT nuclear forces, while the last two terms require treatments that are specific to the frozen PES. The reader is referred to Ref. 47 for details.

Similarly, the polarization contribution to the intermolecular forces can be evaluated by differentiating Eq. (4):

$$\Delta \mathbf{F}_{\text{pol}} = \mathbf{F}_{\text{pol}}[\mathbf{P}_{\text{pol}}] - \mathbf{F}_{\text{frz}}[\mathbf{P}_{\text{frz}}] \quad (10)$$

The derivation of \mathbf{F}_{pol} depends on the definition of fragment polarization subspaces in the SCF-MI calculation,⁷⁰ i.e., the degrees of freedom for each fragment’s occupied-virtual mixing to occur. In the simplest case where the full AO space of each fragment is active in the polarization (SCF-MI) calculation as in the 1st-generation ALMO-EDA,⁴³ \mathbf{F}_{pol} has a similar expression to Eq. (9) except that the last term vanishes due to the stationary condition of SCF-MI ($E_{\text{pol}}^{\Delta A} = \mathbf{0}$):

$$(F_{\text{pol}})_x = - \left[V_{\text{nn}}^x + \mathbf{P}_{\text{pol}} \cdot \mathbf{h}^x + \frac{1}{2} \mathbf{P}_{\text{pol}} \cdot \mathbf{II}^x \cdot \mathbf{P}_{\text{pol}} + E_{\text{xc}}^x + E_{\text{pol}}^{\mathbf{S}} \cdot \mathbf{S}^x \right] \quad (11)$$

Note that in this simplest case, $E_{\text{pol}}^{\mathbf{S}}$ has an identical form to that in the standard SCF energy gradient.⁴⁷ Finally, the charge-transfer contribution to the intermolecular forces can be obtained by differentiating Eq. (5):

$$\Delta \mathbf{F}_{\text{ct}} = \mathbf{F}_{\text{full}}[\mathbf{P}_{\text{full}}] - \mathbf{F}_{\text{pol}}[\mathbf{P}_{\text{pol}}] \quad (12)$$

where \mathbf{F}_{full} stands for the standard KS-DFT forces for the fully relaxed complex.

The frozen interaction term in ALMO-EDA comprises contributions from permanent elec-

trostatics, Pauli repulsion, and dispersion.⁷¹ To improve the interpretability of FDA results and to facilitate comparison with terms in polarizable force fields, here we introduce how one can evaluate forces arising from “quasi-classical” electrostatics ($\Delta\mathbf{F}_{\text{cls-elec}}$), i.e., coulomb interactions between charge distributions (nuclei and electrons) of different fragments, which can be employed to benchmark forces arising from permanent charge and multipole interactions in a force field. The remainder of $\Delta\mathbf{F}_{\text{frz}}$ then incorporates contributions from the non-electrostatic components of the frozen interaction (Pauli repulsion and dispersion), which we refer to as the van der Waals (vdW) contribution since it corresponds roughly to the sum of attractive and repulsive vdW potential in a force field:

$$\Delta\mathbf{F}_{\text{frz}} = \Delta\mathbf{F}_{\text{cls-elec}} + \Delta\mathbf{F}_{\text{vdw}} \quad (13)$$

The quasi-classical electrostatic interaction among N fragments can be expressed in the following compact form:

$$\Delta E_{\text{cls-elec}} = \frac{1}{2} \sum_{A \neq B}^N [\mathbf{P}_A \cdot \mathbf{V}_{\text{ee+en}}^B + V_{\text{nn}}^{AB}] \quad (14)$$

where \mathbf{P}_A is the AO-basis 1PDM of isolated fragment A , $\mathbf{V}_{\text{ee+en}}^B$ is the coulomb potential (nuclear and electronic) arising from fragment B , also in the AO basis, and V_{nn}^{AB} is the nuclear-nuclear repulsion potential between fragments A and B . Differentiating Eq. (14) yields

$$(\Delta F_{\text{cls-elec}})_x = -\frac{1}{2} \sum_{A \neq B} [(\mathbf{P}_A)^x \cdot \mathbf{V}_{\text{ee+en}}^B + \mathbf{P}_A \cdot (\mathbf{V}_{\text{ee+en}}^B)^x + (V_{\text{nn}}^{AB})^x], \quad (15)$$

where the derivative of isolated fragment density \mathbf{P}_A can be further expanded based on its dependence on fragment A 's AO overlap matrix (\mathbf{S}_A) and occupied-virtual orbital rotation (Δ_A):

$$(\mathbf{P}_A)^x = \mathbf{P}_A^{\mathbf{S}_A} \cdot (\mathbf{S}_A)^x + \mathbf{P}_A^{\Delta_A} \cdot (\Delta_A)^x \quad (16)$$

Note that the detailed forms of $\mathbf{P}_A^{\mathbf{S}_A}$ and $\mathbf{P}_A^{\Delta_A}$ have been derived in our previous work.^{47,72}

For completeness here we show the mathematical details regarding these two derivatives in SI Sec. S1.

2.3 The MB-UCB Force Field

The MB-UCB force field^{29,31} was developed based on the principles of the many-body expansion combined with ALMO-EDA variational energy decomposition analysis for each of the terms of the total intermolecular energy

$$E_{\text{inter}} = E_{\text{elec}} + E_{\text{pol}} + E_{\text{CT}} + E_{\text{disp}} + E_{\text{Pauli}} \quad (17)$$

This advanced non-reactive force field introduced anisotropic atomic polarizability of the water molecule,⁷³ as well as explicit treatment of charge transfer and charge penetration contributions for both water and aqueous alkali metal and halogen ions.^{29,31}

The permanent electrostatics for the MB-UCB force field uses atom centered point multipoles

$$E_{\text{elec}} = \sum_{i < j} \mathbf{M}_i^T \mathbf{T}_{ij} \mathbf{M}_j \quad (18)$$

where \mathbf{M}_i^T is the multipole coefficient vector and \mathbf{T}_{ij} is the multipole interaction tensor that consists of appropriate associated derivatives of $1/r_{ij}$. The monopole-monopole term is modified to describe charge penetration (CP) via separation of the atomic charge into a core nuclear charge, Z_i and smeared electron cloud charge $Z - q_i$. Hence the modified charge-charge electrostatic interactions between two atoms A and B with atomic charges q_A and q_B are expressed as

$$E_{\text{elec}}^{q-q} = \frac{Z_A Z_B}{r} - \frac{Z_A (Z_B - q_B)}{r} f_{\text{damp}} - \frac{Z_B (Z_A - q_A)}{r} f_{\text{damp}} + \frac{(Z_A - q_A) (Z_B - q_B)}{r} f_{\text{damp}}^{\text{overlap}} \quad (19)$$

The two damping functions,

$$\begin{aligned} f_{damp} &= (1 - \exp(-\alpha r)) \\ f_{damp}^{overlap} &= (1 - \exp(-\beta_A r))(1 - \exp(-\beta_B r)) \end{aligned} \tag{20}$$

require two parameters, α and β , to control the damping of core–electron and electron–electron interactions, respectively, in order for the charge penetration effects to vanish rapidly and to recover the classical Coulombic multipolar interactions at longer distances. We use the CP model parameterization due to Piquemal and co-workers.⁷⁴

Many-body polarization is explicitly incorporated by point induced dipoles, μ_{ind} , at each atomic center⁵⁵

$$\boldsymbol{\mu}_i^{ind} = \alpha_i \left[\sum_j \mathbf{T}_{ij} \mathbf{M}_j - \sum_{j \neq i} \mathbf{T}_{ij}^{d-d} \boldsymbol{\mu}_j^{ind} \right] \tag{21}$$

where α_i is the atomic polarizability and $\mathbf{T}_{ij} \mathbf{M}_j$ formulates the permanent electric field. \mathbf{T}_{ij}^{d-d} is the dipole-dipole interaction tensor in which the off-diagonal blocks of \mathbf{T}^{d-d} are Thole damped⁷⁵ Cartesian interaction tensors between induced dipoles of two polarizable sites i and j . Unlike other polarizable force fields such as AMOEBA and AMOEBA+ that use rotationally invariant isotropic atomic polarizabilities^{28,59,76}, MB-UCB uses a rank two anisotropic atomic polarizability tensor. The polarization energy can be expressed in terms of induced dipoles as

$$E_{pol} = -\frac{1}{2} \sum_i \boldsymbol{\mu}_i^{ind} \mathbf{E}_i \tag{22}$$

and the induced dipoles at each multipole site are obtained by solving Equation 21 self-consistently.^{77,78}

MB-UCB uses an empirical many-body function similar to the polarization energy induced multipoles to incorporate the many-body charge transfer energy.⁷⁹

$$\begin{aligned}
E_{\text{CT-ind}} &= -\frac{1}{2} \sum_i \boldsymbol{\mu}_i^{\text{ct-ind}} \mathbf{E}_i^{\text{ct}} \\
\boldsymbol{\mu}_i^{\text{ct-ind}} &= \alpha_i^{\text{ct}} \left[\sum_j \mathbf{T}_{ij}^{\text{ct}} \mathbf{M}_j - \sum_{j \neq i} \mathbf{T}_{ij}^{\text{ct}[d-d]} \boldsymbol{\mu}_j^{\text{ct-ind}} \right]
\end{aligned} \tag{23}$$

where α_i^{ct} controls the charge transfer energy between two multipole sites through a response to the permanent electrostatics, and the multipole interaction matrix (\mathbf{T}^{ct}) elements are damped with an exponential damping function.

$$\mathbf{T}_{\zeta}^{\text{ct}} = - \left[1 - d \exp(-bu^3) \right] \frac{r_{\zeta}}{r_{ij}^3}, \quad \zeta = x, y, z \quad u = \frac{r_{ij}}{(\alpha_i^{\text{ct}} \alpha_j^{\text{ct}})^{1/6}} \tag{24}$$

The three parameters α_i^{ct} , b and d are responsible for the fast exponential decay of the charge transfer energy, which should be more short-ranged than polarization.^{29,31}

The remaining energy terms are Pauli repulsion and dispersion, and are modeled in MB-UCB as a van der Waals interaction using a buffered 14-7 pairwise-additive function proposed by Halgren⁸⁰ and utilized in all AMOEBA force fields.^{55,59,76}

$$E_{\text{vdW}} = \sum_{i < j} \epsilon_{ij} \left(\frac{1 + \delta}{\sigma_{ij} + \delta} \right)^7 \left(\frac{1 + \gamma}{\sigma_{ij}^7 + \gamma} - 2 \right) \tag{25}$$

where ϵ defines the energy scale, $\sigma = R_0/r$ is the distance between two atoms, and R_0 is the distance corresponding to the minimum energy. Like AMOEBA,⁸¹ we set the two constants δ and γ to 0.12 and 0.07, respectively. Given the total functional forms of the energy terms of MB-UCB, the corresponding force terms are easily defined through the usual chain rule formulations and easily compared to the FDA analysis proposed here.

2.4 Computational details

The force decomposition analysis method discussed here was implemented in a developer version of Q-Chem 5.⁸² The geometries used for molecular calculations were optimized and run at the $\omega\text{B97X-D}^{83}/\text{def2-TZVPPD}^{84}$ level of theory, with exception to the gold/silver

CO₂ complex, where ω B97X-V⁸⁵ density functional instead along with the appropriate def2-ECP.⁸⁶ To diagnose the atomic forces of MB-UCB, we use the same level of theory used in the original paper,²⁹ namely ω B97X-V⁸⁵/def2-QZVPPD.⁸⁴ DFT numerical integration was performed on (99,590) grid for XC functional and SG-1⁸⁷ for non-local correlation. All geometries are included in the supporting information (SI).

Fifty water dimer geometries were used to compare the atomic force contributions between FDA and MB-UCB. The geometries were taken from the iAMOEBA training data set,⁵⁷ where pairs of molecules were randomly picked from AMOEBA liquid water simulation between 257.15 - 373.15 K such that it is representative of a wide range of the phase space. The geometries are provided in the SI.

Forces are turned into internal coordinates by a linear transformation using the pseudo-inverse of Wilson’s B matrix.^{62,88,89} The B matrix was generated using Q-Chem 5.⁸² Details are included in SI Sec. S2

3 Results and discussion

3.1 H₂O \cdots Na⁺, Cl⁻ \cdots HOH and the water dimer

First we look at the water molecule interacting with an innocent cation, Na⁺, and a simple anion, Cl⁻. Aside from the importance of these examples in understanding water-ion interactions, they will illustrate the nature of the FDA information, as well as its representation in internal coordinates. We use geometries where the position of the ion is optimized relative to a water molecule constrained to its isolated geometry. This is a convenient choice because $\mathbf{F}_{\text{tot}} = \Delta\mathbf{F}_{\text{int}}$ since $\mathbf{F}_A = \mathbf{0}$ for $A = \text{H}_2\text{O}$. As a result, the interfragment degrees of freedom will have zero net force, as well as zero resultant force in the FDA in order to see how the FDA components cancel each other out. By contrast, there will be nonzero $\Delta\mathbf{F}_{\text{int}}$ for intramolecular degrees of freedom, which will indicate how such internal coordinates will deform in a fully optimized complex. The FDA will reveal which component contributions

are primarily responsible for such changes.

At equilibrium, the $\text{Na}^+ - \text{O}$ vector is aligned with the water dipole vector, optimizing the charge-dipole interaction. With C_{2v} symmetry, there are only three non-redundant internal coordinates, namely $\text{O}-\text{H}$, $\text{O}-\text{Na}$, and $\angle\text{HOH}$. The FDA is shown in the left panel of Fig. 1. By far the most interesting result is $\Delta\mathbf{F}_{\text{int}}(\text{O} - \text{Na}^+)$, which is overall zero, as a result of a strong force of extension due to Pauli repulsion (the van der Waals term in Fig. 1) being compensated by an equally strong force of contraction due to electrostatic attraction. The electrostatic attraction force is about 80% due to the permanent electrostatics, and only 20% due to polarization (of water by Na^+). There is negligible contribution from charge transfer, emphasizing the innocent nature of Na^+ as an ineffective Lewis acid. The $\text{O}-\text{H}$ bonds are remote from Na^+ , so the forces distorting the optimal monomer geometry in the complex are small. The largest formation force is $\Delta\mathbf{F}_{\text{int}}(\text{O} - \text{H})$, which has a small force of extension driven by polarization. We can understand this effect as a result of promotion of a fraction of an electron from the σ_{OH} orbitals to antibonding orbitals, presumably with σ_{OH}^* character.

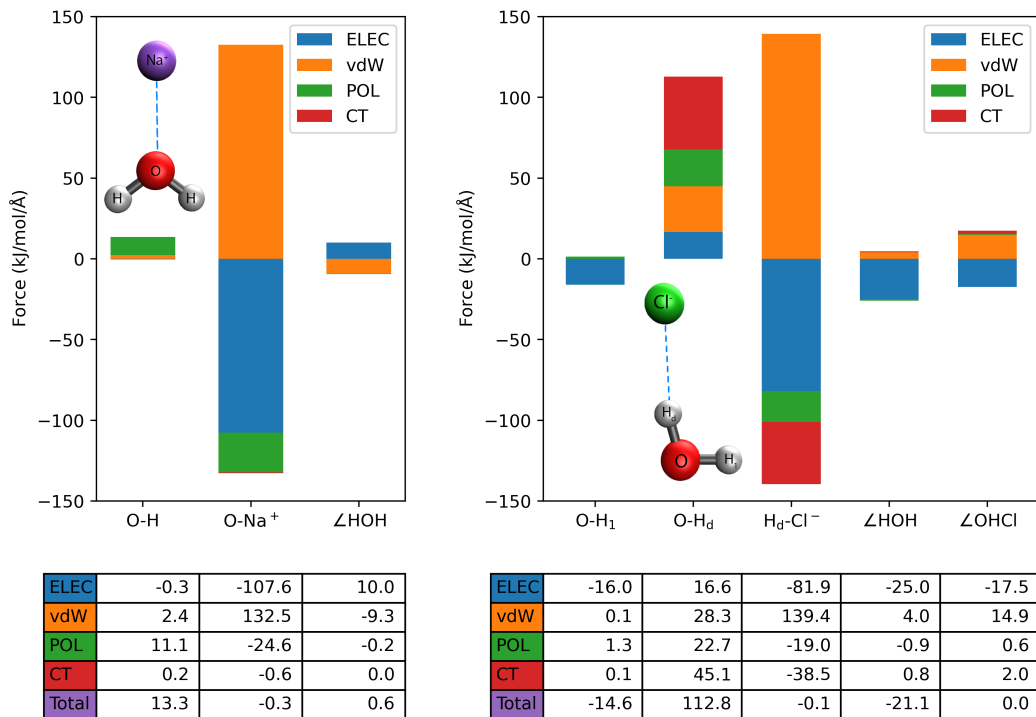


Figure 1: FDA results in the internal coordinates for H_2O interacting with Na^+ (left) and Cl^- (right). These forces are evaluated at the PES minima, keeping the water molecule at its isolated geometry. The tables at the bottom replicate the data with numbers for easier comparison.

FDA for the hydrogen-bonded complex formed between water and the chloride anion, as given in the right panel of Fig. 1, presents an interesting contrast with the $\text{H}_2\text{O} \cdots \text{Na}^+$ case, which was previously analyzed by the ALMO-EDA.^{72,90} Despite on-going debate,^{91–95} it is fairly well-established that hydrogen-bonds involve significant contributions from permanent and induced electrostatics, and charge transfer,^{44,47,95} in competition with Pauli repulsion. Focusing first on the inter-fragment H_d-Cl^- force, which is optimized to zero, we see three forces of contraction (permanent electrostatics $>$ charge transfer $>$ polarization) balanced by the extension force due to Pauli repulsion. From a force equilibrium perspective, this very nicely illustrates the “driving forces” that give rise to the hydrogen bond. The other interfragment coordinate, $\angle\text{OH}_d\text{Cl}$, is optimized as a balance between permanent electrostatics (attempting to shrink the angle), and Pauli repulsion (attempting to enlarge the angle). This competition is controlled by the frozen part of the interaction energy, as previously

noted for the water dimer.⁴⁷ Within the water molecule, there is a strong force of extension along the OH_d bond. Its primary origin is charge transfer, followed by Pauli repulsion, induced electrostatics and permanent electrostatics. Both CT and polarization can be readily understood in terms of partial occupation of the $\sigma_{\text{OH}_d}^*$ orbitals.

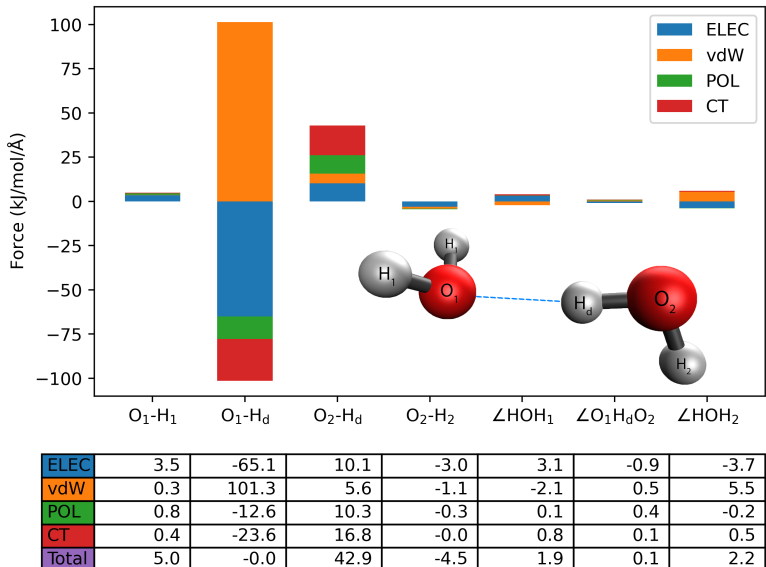


Figure 2: FDA results in the internal coordinates for the water dimer at the minimum-energy distance, with the monomers fixed in their isolated geometries. The table at the bottom replicates the data with numbers for easier comparison.

Next, we examine FDA for the hydrogen-bonded water dimer, as shown in Fig. 2; this system has also been carefully analyzed previously by the ALMO-EDA.^{72,93} The zero net force on the hydrogen-bond coordinate, O_1H_d , shows the FDA view of this characteristic hydrogen-bond interaction. Classical electrostatics dominates the forces seeking to further shorten the hydrogen bond, consistent with force-field viewpoints. Intermolecular charge transfer is the second strongest force of contraction, followed by polarization. Pauli repulsion provides an exactly balancing force of extension. Within the proton-donor water molecule (which of course is the electron pair acceptor), the intramolecular O_2H_d bond constrained to the geometry of the free water molecule experiences a force of extension to which all components contribute with the same sign. Similar to the water-chloride complex, charge

transfer and polarization partially occupy the antibonding $\sigma_{\text{O}_2\text{H}_d}^*$ orbitals and are the leading drivers of O_2H_d bond elongation.

3.2 Assessing force components of an advanced water force field

Generating the force vectors corresponding to each energy term in the ALMO-EDA yields a greatly augmented set of data at each geometry. Such data can in principle be employed to aid in the development or validation of advanced force fields, perhaps in conjunction with powerful existing tools such as Force Balance^{76,96} or machine learning.^{97,98} To illustrate the use of FDA data, we assess the forces that are obtained from a recently reported force field for water, MB-UCB.²⁹ Although the energies of MB-UCB have already shown to be in excellent agreement with ALMO-EDA,²⁹ no comparable assessment of the decomposed forces has yet been done, although total and force components of the complete energy derivative have been assessed for other force fields such as iAMOEBA⁵⁷ and AMOEBA14⁵⁹ to which we compare below. The term-by-term force contributions from the FDA against MB-UCB has been assessed for a set of 50 water dimer geometries extracted from finite temperature MD trajectory as described in the computational details section. For these snapshots, the ALMO-EDA energy components and the corresponding contributions for MB-UCB, shown in SI Sec. S3, show excellent agreement, as expected based on our previous work.²⁹

We begin our assessment by comparing the FDA and MB-UCB force components on the center of mass (CoM) of each water molecule in the data set broken down by interaction. The COM forces are a sum of all atomic forces on a molecule, also referred to as molecular forces or net forces.^{57,99} The results are shown as correlation plots in Fig. 3 in which the RMS error in the total CoM force is ~ 8 kJ/mol/Å. This is a reasonably small error when considering the fact that a DFT geometry optimization is considered converged at a maximum force of ~ 1 -2 kJ/mol/Å, and is comparable to the ~ 10 kJ/mol/Å RMS error in AMOEBA and iAMOEBA forces versus ab initio forces reported for water clusters.^{57,59} Perhaps the most important point that emerges from Fig. 3 is the fact that the RMSD in each non-bonded

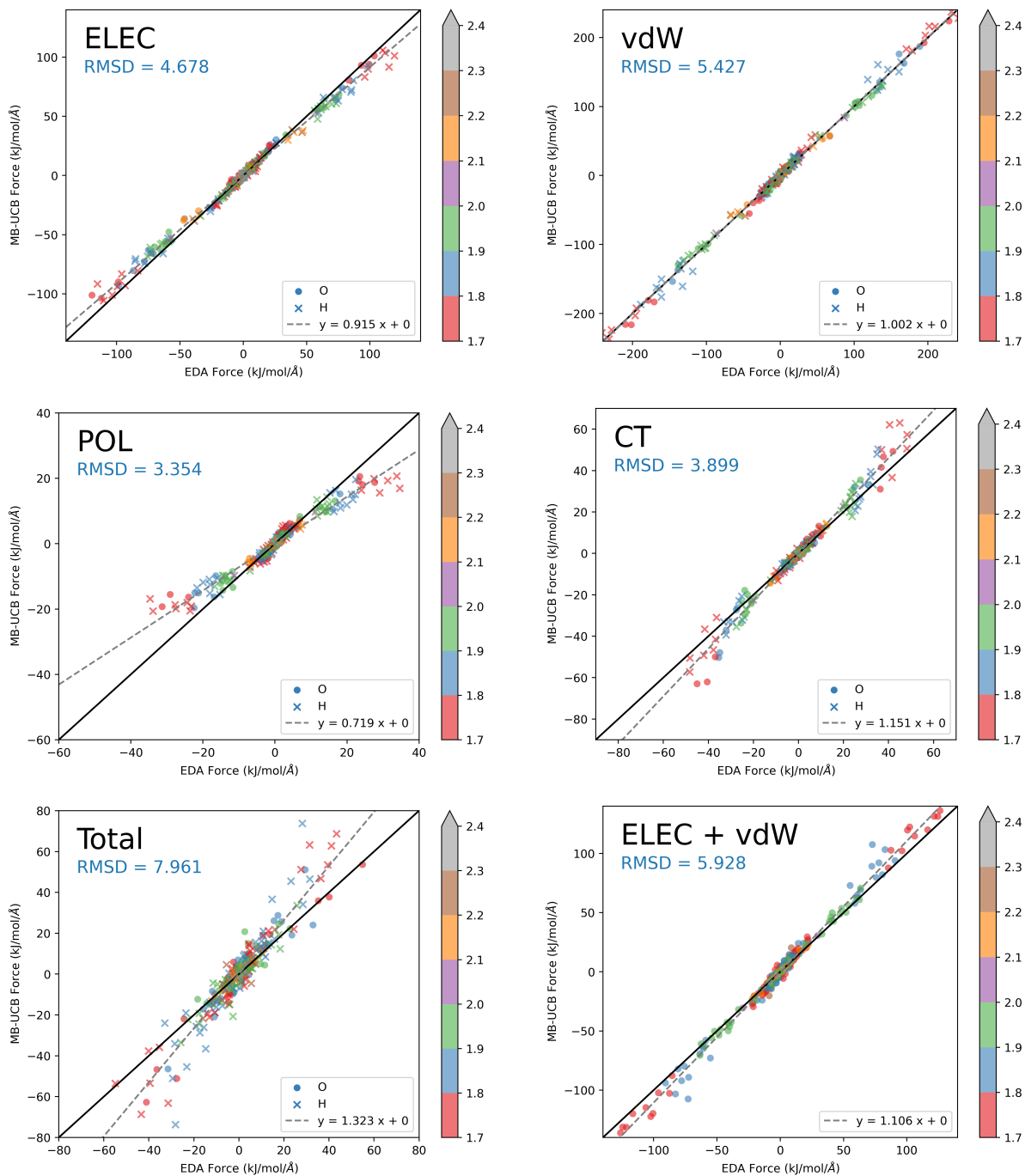


Figure 3: Correlation between FDA decomposed forces and the corresponding MB-UCB forces on the centers of mass of each water molecule for a sample of 50 water dimer geometries. The force decompositions considered are electrostatics (ELEC), van der Waals (vdW), polarization (POL), and charge transfer (CT), and the total intermolecular interaction (TOT). The color bins indicate the distance to the closest atom of the other fragment, i.e., small numbers indicate the dimer is in the compressed region. The equilibrium water dimer closest contact atoms sit at 1.9 Å, which corresponds to the data points colored in blue. The dashed line corresponds to a least squares fit of the errors, where the line fit equation is shown in the legend of each plot.

contribution to the MB-UCB CoM force is smaller than the RMSD in the MB-UCB total force. Even the very large ELEC and vdW forces exhibit RMSD values of only 4.7 and 5.4 kJ/mol/Å, respectively. The largest deviations are associated with the largest forces, as expected, where short-range damping, such as Thole damping of polarization,⁷⁵ are likely to exert an influence. Overall, we can conclude that the decomposed contributions to the CoM forces via MB-UCB are as good or better behaved than the total MB-UCB CoM forces.

A more stringent FDA test is to assess the errors in the Cartesian forces on each atom, for which a correlation plot between the FDA and MB-UCB decompositions is shown in Fig. 4. The overall RMSD value is increased by only $\sim 10\%$ for the atomic forces vs the CoM forces, rising to ~ 8.8 kJ/mol/Å, which is encouragingly good performance when compared to iAMOEBA or AMOEBA, in which atomic forces showed RMS errors more than twice as large as CoM forces.⁵⁷ Although the RMS of the ELEC atomic forces increases relative to the COM electrostatic forces, they are still comparable to the total atomic force errors.

However, the vdW term shows a significantly larger atomic force error compared to the total or COM force error. It is pertinent to mention that MB-UCB situates the vdW centers for the hydrogen atoms at a fixed fraction (0.91) of the OH bond length, rather than at the atomic centers themselves. Hence the virtual site forces must be redistributed over the particles with mass in a consistent way, which only guarantees that the total force is preserved, and may explain some of the vdW force deviations observed. Even so, there is some error cancellation between ELEC and vdW atomic forces as seen in the ELEC+vdW plot in Fig. 4, which was not the case in the CoM force components. Finally, the more challenging nature of the atomic force components (and the total atomic force) is also evident in the fact that the largest errors no longer occur predominantly at the largest absolute force values. Fig. 4 shows RMS errors when either MB-UCB predicts near zero atomic forces compared to finite FDA forces (such as for POL or CT) or that finite MB-UCB atomic forces are found when FDA forces are near zero (for example, vdW).

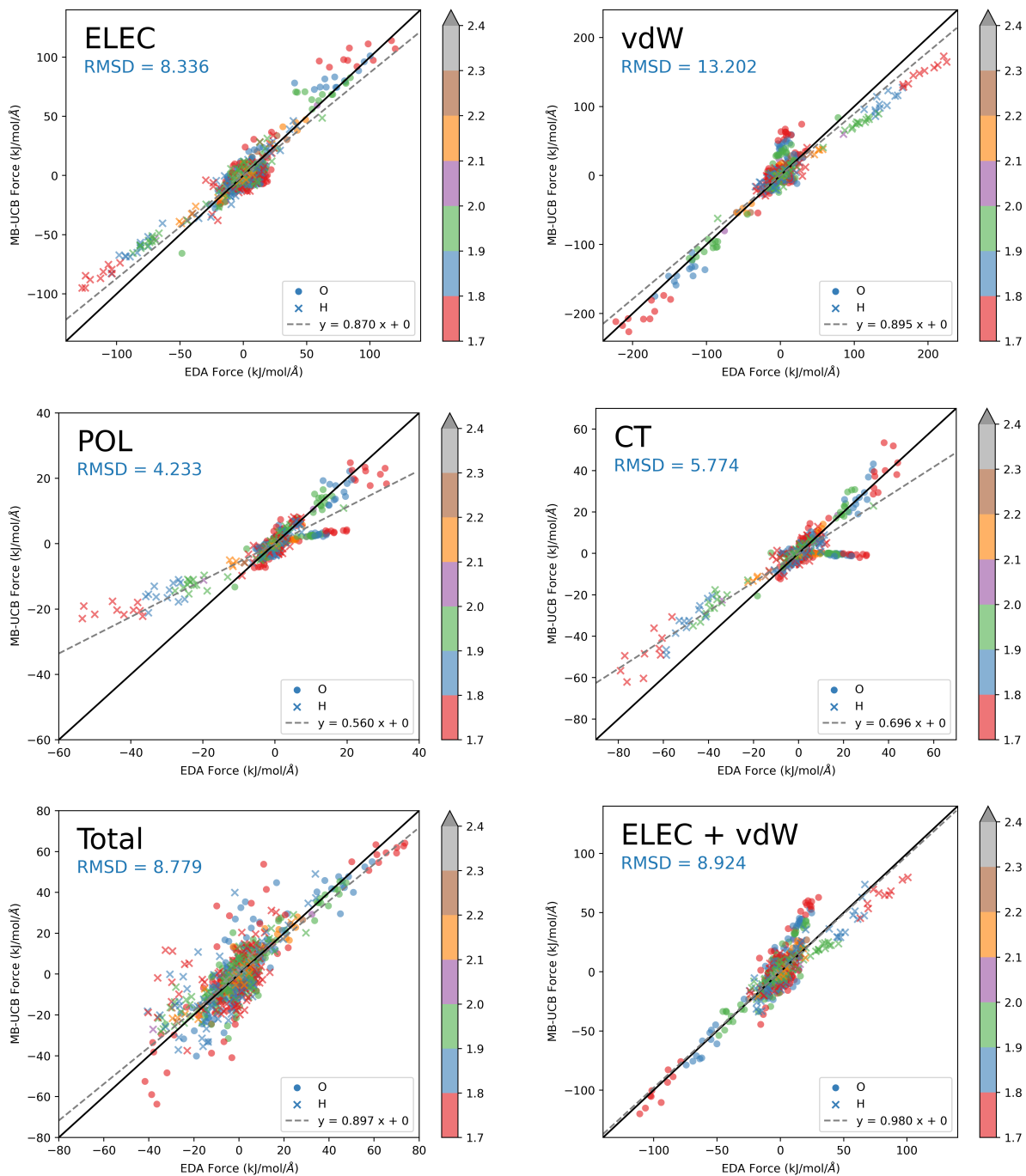


Figure 4: Correlation between FDA decomposed component forces and the corresponding MB-UCB forces on the atomic centers of each water molecule for a sample of 50 water dimer geometries. Other details are as defined in Fig. 3.

One more way to compare MB-UCB forces against the FDA results, is to separately evaluate the RMS deviations in the total CoM force (left panel) and the atomic forces (right

panel) as a function of the closest intermolecular distance in Fig. 5. These plots make it clear that errors decay rapidly as a function of intermolecular separation. The plots also serves to emphasize the fact that the quality of the individual MB-UCB decomposed CoM force is statistically better than the MB-UCB total force. On the other hand, at intermolecular distances of 2 Å and shorter, errors in the MB-UCB vdW force contribution are larger than the total MB-UCB RMSD; in other words, there is partial error compensation with the ELEC term in particular. It is encouraging that the errors associated with the MB-UCB description of charge transfer and polarization contributions remain relatively low even in the compressed region for both the atomic force and CoM force, although their magnitude increases with the reduction of the closest contact distance. The CT term shows more scope for improvement, which is likely to be a result of the less physically appropriate form that was employed within MB-UCB.²⁹

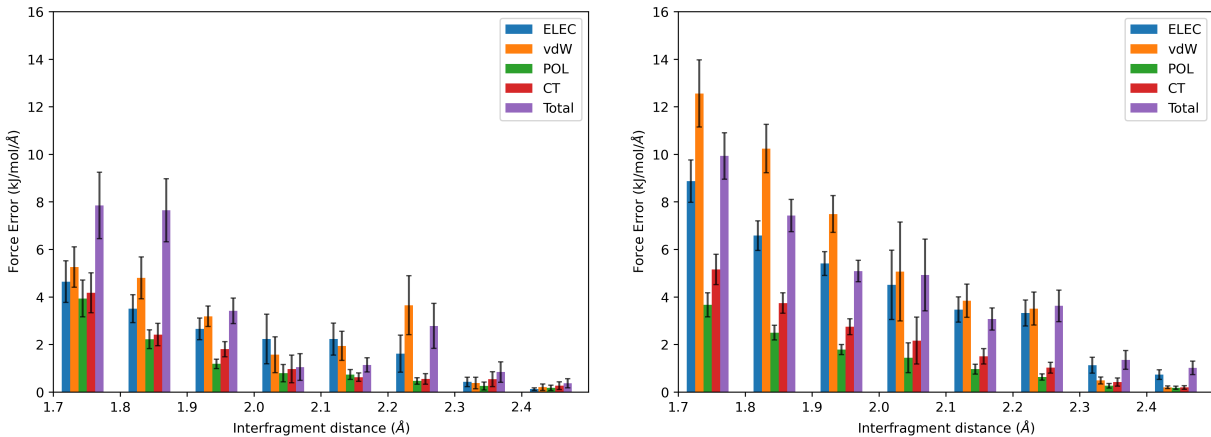


Figure 5: Mean absolute deviations in the total CoM force (left panel) and the atomic forces (right panel) as a function of the closest intermolecular distance. The mean errors in MB-UCB forces plotted against the closest contact between the two water molecules broken down into the non-bonded components of interaction. The left panel applies to the CoM force on each water molecule, while the right panel applies to the atomic forces. Values plotted are the RMSDs for all data points within each 0.1 Å bin of closest intermolecular distance. The error bars indicate 95% confidence interval.

3.3 Interaction of CO₂ with Au⁻ and Ag⁻

The reduction of CO₂ to CO₂^{•-} is the first step on the pathway towards conversion of CO₂ into fuels, of which the simplest is 2-electron reduction to CO₂.¹⁰⁰ The reverse reaction, CO oxidation to CO₂, is also well-studied.¹⁰¹ At the level of model systems, negatively charged gold oxide clusters have been shown to react with CO to yield CO₂,¹⁰² via reactions as simple as AuO⁻ + CO → Au⁻ + CO₂. The exit channel complex, [Au⋯CO₂]⁻, has been studied as part of that reaction,¹⁰² as well as characterized by separate experiments and computations.^{103–105} Remarkably, as shown in Fig. 6(a) and (b), there are two local minima in the exit channel: a strongly bound chemisorbed structure, which exhibits significant activation (i.e., reduction) of the CO₂ (∠OCO = 143°), and a physisorbed complex where CO₂ is not activated (∠OCO = 172°).

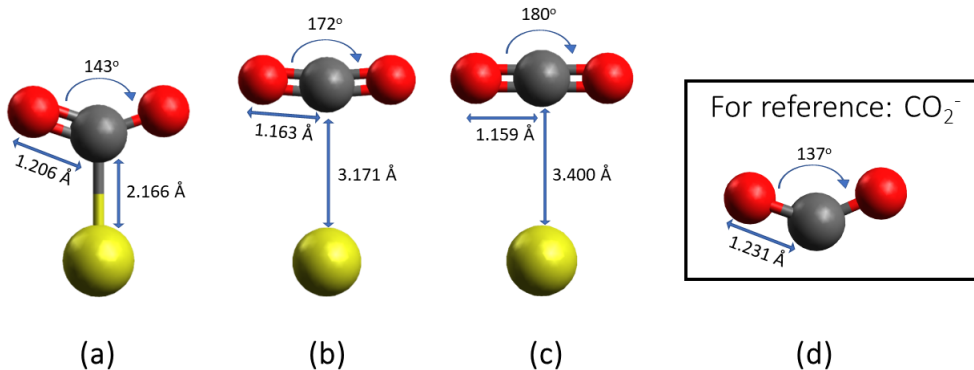


Figure 6: A diagram showing the different configurations of the Au⁻CO₂ with the labeled bond distances and angles; due to C_{2v} symmetry, there are only 3 non-redundant internal coordinates, which are the Au–C distance, the C–O bond length, and the CO₂ bending coordinate. (a) the chemisorbed species at $R(\text{AuC}) \sim 2.2 \text{ \AA}$, (b) the physisorbed species at $R(\text{AuC}) \sim 3.2 \text{ \AA}$, (c) a constrained geometry ($R(\text{AuC})$ optimized with CO₂ fixed at its optimal isolated geometry) exhibiting a minimum at $R(\text{AuC}) \sim 3.4 \text{ \AA}$, (d) the charged anion of CO₂^{•-}.

On the other hand, the silver anion was reported experimentally to exhibit only the physisorbed species,¹⁰⁵ perhaps reflecting the smaller size of the gold atom compared to silver due to relativistic contraction. We show a fully relaxed potential energy scan along the

M–C distance with the energy decomposition analysis results in Fig. 7. General agreement with the experimental facts is evident in the PES scan. The size effect is already clear with Ag showing more repulsive van der Waals interactions (sum of Pauli repulsion and dispersion) at 4 Å and stronger electrostatic attraction than Au. Despite charge transfer being a dominant contribution to the interaction, CT is very comparable for Au and Ag at shorter M–C distances, although Ag’s CT is stronger than Au’s at longer distances due to size. With an ionization energy of only 126 kJ/mol,¹⁰⁶ Ag[−] is a stronger electron donor (Lewis base) than Au[−], whose ionization energy is 223 kJ/mol.¹⁰⁷

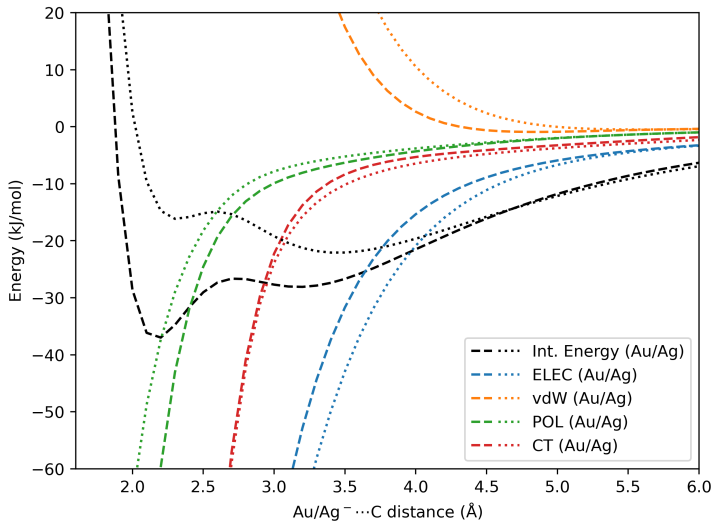


Figure 7: Fully relaxed potential energy surface scans (kJ/mol) for Au[−]CO₂ (black dashes) and Ag[−]CO₂ (black dots) with the EDA components (dashes for Au[−]CO₂ and dots for Ag[−]CO₂).

Next, we look into the forces for both the physisorbed and chemisorbed species. For easier comparison, we take the geometries of two minima for the gold complex and use these same geometries for silver. Since the CO₂ molecule in these geometries is distorted compared to the isolated molecule, we will refer to that difference in energy as a geometric distortion (GD) energy. Similarly, we refer to the forces that arise from the geometric distortion energy (which will cause the CO₂ to relax back to its isolated geometry) as the geometric distortion force. The FDA results at the physisorbed geometry are shown in Fig. 8, while results at

the chemisorbed geometry are shown in Fig. 9.

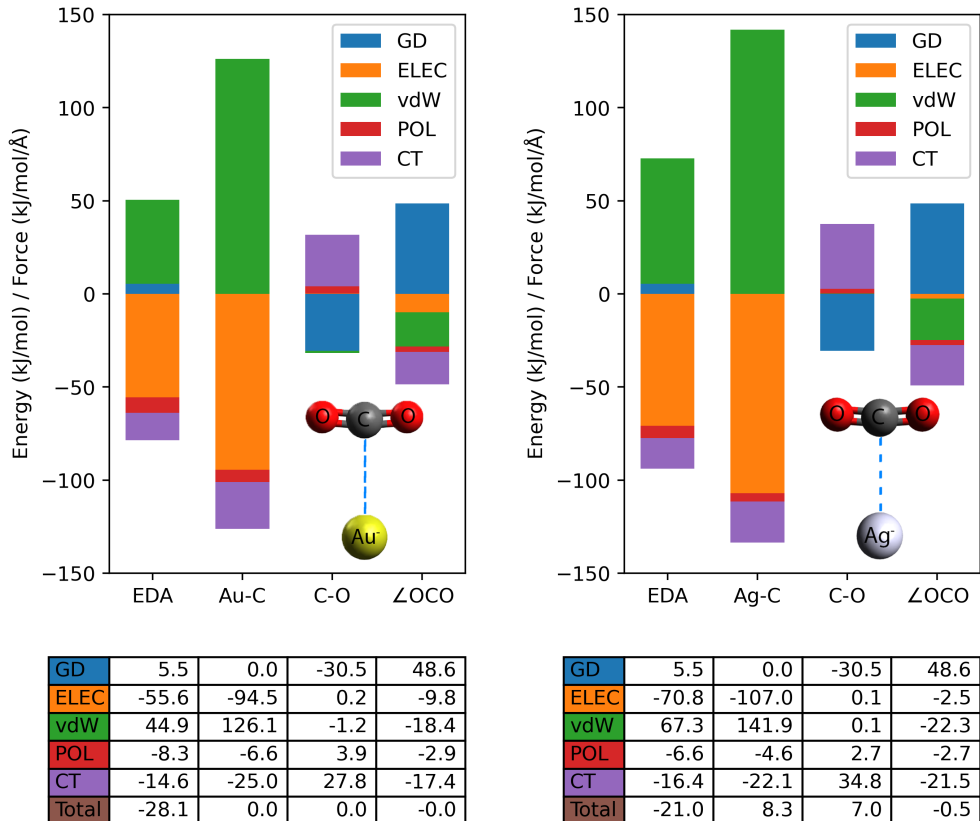


Figure 8: Comparison of the EDA components (in kJ/mol) and the decomposed forces (in kJ/mol/Å) in internal coordinates for physisorbed $\text{Au}^- \cdots \text{CO}_2$ (left panel) and $\text{Ag}^- \cdots \text{CO}_2$ (right panel) complexes, both evaluated at the nuclear coordinates optimized for $\text{Au}^- \cdots \text{CO}_2$. The energies and forces are decomposed into geometric distortion (GD), electrostatics (ELEC), van der Waals (vdW), polarization (POL), and charge transfer (CT), and the total intermolecular interaction (Total). The table summarizes the same data with additional significant figures.

We first discuss the physisorption results shown in Fig. 8. The larger size of Ag^- versus Au^- results in a more attractive electrostatic interaction as well as stronger Pauli repulsion in the van der Waals term, with no significant difference in polarization and charge transfer terms. As we use the optimized $\text{Au}^- \cdots \text{CO}_2$ nuclear coordinates, the net force along each internal coordinate is exactly zero for the $\text{Au}^- \cdots \text{CO}_2$ complex. Thus inspection of the FDA reveals an exact force balance. Along the Au-C coordinate, van der Waals repulsion is primarily balanced by electrostatics, with small contributions from polarization and CT also

favoring shorter bonds. The fact that those latter contributions are so small indicates that CO_2 is scarcely activated, consistent with the near linearity of its optimized geometry. The geometric distortion force favors removing the slight lengthening of the CO bond and very slight bending of the CO_2 . In opposition, the drive for CO bond lengthening comes almost entirely from CT, while van der Waals and CT both favor increased angle bending. Comparing $\text{Ag}^- \cdots \text{CO}_2$ against $\text{Au}^- \cdots \text{CO}_2$ shows relatively subtle differences associated with the stronger Pauli repulsion forces in the Ag system, which favor longer Ag–C separation, and extension of the C–O distance as a result of its stronger CT (due to better donor-acceptor overlap, as well as Ag^- being a stronger Lewis base). Finally, as regards the physical driving forces behind the physisorbed complex, both EDA and FDA reveal it to be synergy between dispersion (as indicated by the net binding provided by ELEC+vdW), charge transfer, and polarization.

For the chemisorbed $\text{Au}^- - \text{CO}_2$ and $\text{Ag}^- - \text{CO}_2$ species shown in Fig. 9, at the coordinates of the optimized $\text{Au}^- - \text{CO}_2$ complex, there is a binding energy difference of 24 kJ/mol in favor of the Au complex. Note that the scale for Fig. 9 is 10 times larger than for the physisorbed structures given in Fig. 8. By far the dominant driving force behind the chemisorption geometry is charge transfer. The smaller gold anion exhibits stronger binding from electrostatics, polarization, and charge transfer as well as more repulsive van der Waals interaction compared to the more diffuse silver anion. Despite the lower ionization energy of Ag^- vs. Au^- , the compactness of the gold anion makes charge transfer in $\text{Au}^- - \text{CO}_2$ significantly more attractive than that in $\text{Ag}^- - \text{CO}_2$ in which the anion is more diffuse. Accordingly, FDA on $\text{Ag}^- - \text{CO}_2$ shows a net force for Ag–C elongation. Turning to FDA within the CO_2 subunit, CT (elongation) vs. GD (contraction) determine the net force on the C–O bond. On the other hand, the net $\angle\text{OCO}$ force displays an interesting synergy between the van der Waals repulsion and charge transfer (both favoring bending), versus the geometric distortion force (favoring linearization). To sum up, the compactness of the gold versus silver anion trumps the stronger Lewis basicity of the silver anion in leading to much

stronger chemisorption in the Au complex.

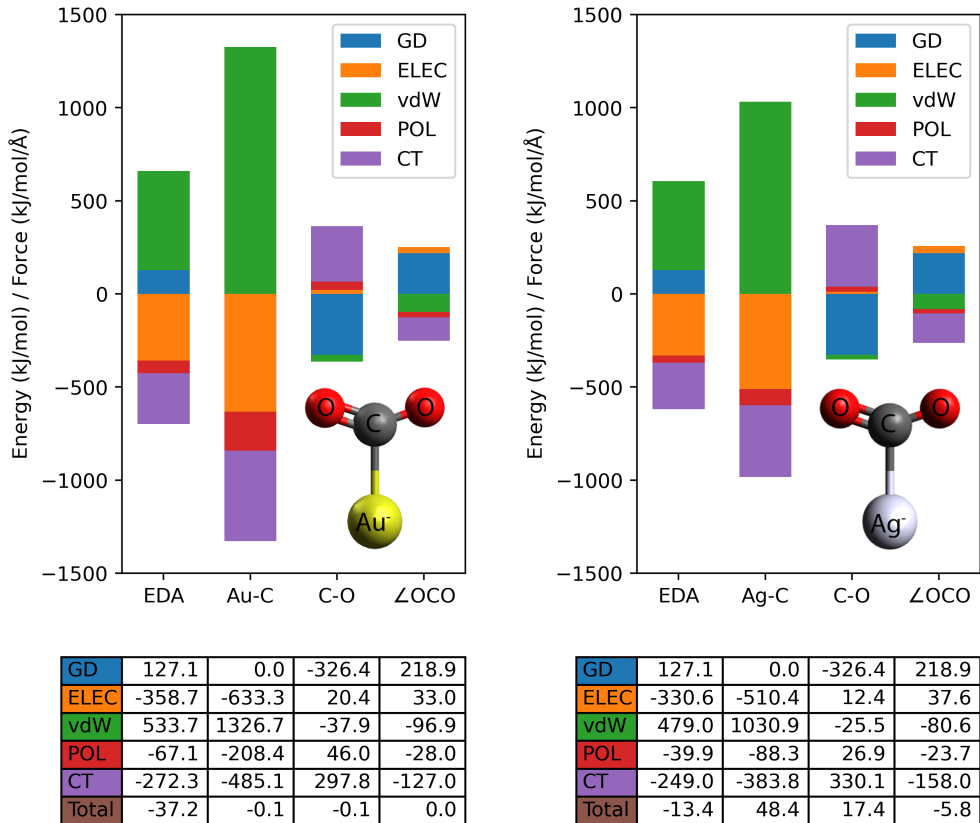


Figure 9: Comparison of the EDA components (in kJ/mol) and the decomposed forces (in kJ/mol/Å) in internal coordinates for chemisorbed $\text{Au}^- - \text{CO}_2$ (left panel) and $\text{Ag}^- - \text{CO}_2$ (right panel) complexes, both evaluated at the nuclear coordinates optimized for $\text{Au}^- - \text{CO}_2$. The energies and forces are decomposed into geometric distortion (GD), electrostatics (ELEC), van der Waals (vdW), polarization (POL), charge transfer (CT), and the total intermolecular interaction (Total). The table summarizes the same data with additional significant figures.

4 Conclusions

We have reported theory, implementation, and model applications of an extension to the adiabatic energy decomposition analysis⁴⁷ to perform force decomposition analysis of the force components obtained from an EDA method. In particular, the variational absolutely localized molecular orbital EDA (ALMO-EDA) approach³⁸ is used to analyze Kohn-Sham density functional theory calculations on molecular complexes by differentiating key interme-

diate energies associated with each non-bonded term. The result is a more information-rich vector of how the different physical driving forces of intermolecular interactions affect each atomic or internal coordinate force within a complex. We expect that our FDA approach can be readily applied to other variational EDA schemes and extended to other molecular properties besides nuclear forces.

More specifically, the net force on either each atom or each internal coordinate of a molecular complex is decomposed into the following physically interpretable contributions.

1. A geometric distortion force (GD), which results from deforming a fragment optimized in isolation to its geometry in the complex. The geometric distortion force will always favor restoring the fragment to its isolated geometry.
2. Forces associated with quasi-classical electrostatics (ELEC), and van der Waals (vdW) interactions (including attractive dispersion and repulsive Pauli interactions) are obtained which sum to the net force resulting from the frozen interaction energy⁷¹ of the ALMO-EDA method. For strongly interacting complexes ELEC and vdW forces are strong and opposite in sign, and it can be advantageous to instead examine the frozen force.
3. Forces associated with the polarization (POL) of the complex,⁷⁰ as described by the self-consistent field for molecular interactions (SCF-MI) approach⁶⁵⁻⁶⁹ in the basis of fragment atomic orbitals.
4. Forces associated with charge delocalization or charge transfer^{72,108} between the fragments comprising the complex, which represent the final increment to obtain the total forces.

The model applications presented here are of some intrinsic interest, as well as serving to illustrate the future utility of the FDA for more advanced problems. We presented three sets of examples:

1. We used FDA to examine the $\text{Na}^+\text{H}_2\text{O}$ and $\text{Cl}^-\text{H}_2\text{O}$ complexes, keeping H_2O constrained to its free-molecule geometry. The resulting force balance along the intermolecular distance revealed a greater role for CT in the chloride complex. The net forces within the water molecule showed the role of different components on the intermolecular interaction in distorting the geometry.
2. To illustrate the potential value of FDA to the advanced force field development community, we assessed the fidelity of contributions to the MB-UCB water force field against the FDA components on snapshots of the water dimer. The results showed very good performance for the total atomic forces, and particularly good performance for the center of mass force decompositions, whose RMSD vs FDA components was smaller than the total RMSD.
3. The FDA was also employed to analyze the physisorbed and chemisorbed complexes formed between Au^- and CO_2 , and to compare them against the corresponding Ag^-CO_2 complexes. The results showed that while Ag^- is a stronger electron donor than Au^- , the smaller size of Au^- is crucial to the stronger chemisorption of CO_2 to it.

Supporting Information

- Further details about deriving the classical electrostatics force, internal coordinate transformation, energy comparison between MB-UCB and ALMO-EDA for the water clusters, reduced basis set calculation for force decomposition, and potential energy surfaces of the gold and silver anions interaction with the carbon dioxide using wavefunction-based methods (PDF)
- All molecular geometries used in this article (XYZ)

Conflicts of Interest

MHG is a part-owner of Q-Chem Inc, whose software was used for all developments and calculations reported here.

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Force Decomposition Analysis (FDA)

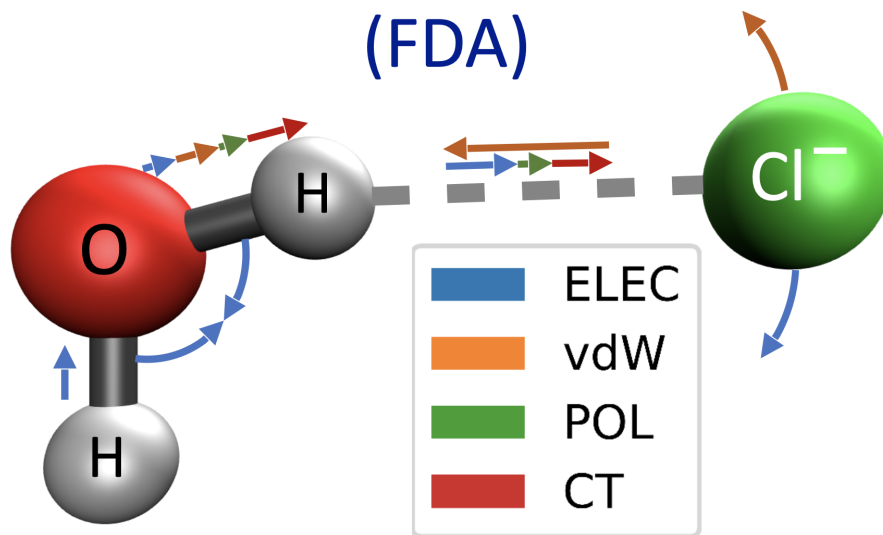


Figure 10: TOC graphic.