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# Complete framework for tau polarimetry in  $B \to D^{(*)} \tau \nu$  decays

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The meson decays  $B \to D\tau\nu$  and  $B \to D^*\tau\nu$  are sensitive probes of the  $b \to c\tau\nu$  transition. In this work, we present a complete framework to obtain the maximum information on the physics of  $B \to D^{(*)}\tau\nu$  with polarized  $\tau$  leptons and unpolarized  $D^{(*)}$  mesons. Focusing on the hadronic decays  $\tau \to \pi \nu$  and  $\tau \to \rho \nu$ , we show how to extract seven  $\tau$  asymmetries from a fully differential analysis of the final-state kinematics. At Belle II with 50 ab<sup>-1</sup> of data, these asymmetries could potentially be measured with percent-level statistical uncertainty. This would open a new window into possible new physics contributions in  $b \rightarrow c\tau\nu$  and would allow us to decipher its Lorentz and gauge structure.

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### I. INTRODUCTION

Leptonic and semileptonic hadron decays are important probes of the fundamental quark-lepton interactions within and beyond the Standard Model (SM). Decays of B mesons with  $\tau$  leptons in the final state, in particular, provide a unique way to determine the properties of fermion interactions involving the third generation. They allow us to test the flavor structure of the SM and search for New Physics (NP) predominantly coupled to the heavier fermions. In addition, the large  $\tau$  mass leads to an enhanced sensitivity to the scalar component of the weak interaction. Semitauonic B decays are therefore especially sensitive to the timelike component of the virtual  $W$  boson [\[1\]](#page-15-0) or to the exchange of new (pseudo)scalar particles [2–[4\].](#page-15-1)

At flavor experiments, the decays  $B \to D\tau \nu$  and  $B \to$  $D^* \tau \nu$ , both triggered by the charged-current transition  $b \rightarrow c\tau \nu$ , are the most accessible semitauonic hadron decays. The branching ratios of these decays normalized to those into light leptons,  $R_{D^{(*)}} = BR(B \to D^{(*)} \tau \nu) /$ <br> $\mathbb{P}(\mathbf{P} \to D^{(*)} \mathcal{L} \nu)$  with  $\mathcal{L} = a$ ,  $\mu$  have been measured  $BR(B \to D^{(*)} \ell \nu)$  with  $\ell = e$ ,  $\mu$ , have been measured<br>with good precision at *BARAR* 15.61 Belle 17–91 and with good precision at *BABAR* [\[5,6\],](#page-15-2) Belle [7–[9\],](#page-15-3) and LHCb [\[10,11\].](#page-15-4) Interestingly, the combination of these measurements appears to be about 20% larger than the SM prediction with a significance of  $3.08\sigma$  [\[12\]](#page-15-5). The normalized branching fraction of  $B_c \rightarrow J/\psi \tau \nu$ , which is based on the same  $b \to c\tau\nu$  transition, has been measured by LHCb and also appears to be larger than the SM expectation [\[13\]](#page-15-6). Beyond total rates, in  $B \to D^* \tau \nu$  the longitudinal  $\tau$ polarization  $P_L(\tau)$  [\[14,15\]](#page-15-7) and the fraction of longitudinally polarized  $D^*$  mesons  $F_L(D^*)$  [\[16,17\]](#page-15-8) have been measured.<br>This shows the potential of the current flavor experiments This shows the potential of the current flavor experiments, Belle II and LHCb, to extract the properties of the  $b \to c\tau\nu$ transition by measuring the  $\tau$  kinematics in the decay. Precise analyses of these transitions are important to understand the origin of the observed discrepancies with the SM and to decipher the structure of NP in case they persist.

Due to its fast decay, the production properties of the  $\tau$ lepton cannot be directly measured, but have to be extracted from the decay products where part of the information on the  $\tau$  momentum is carried away by at least one neutrino in the final state. Extracting the properties of the  $b \rightarrow c\tau \nu$  transition from the visible  $\tau$ -decay products in  $B \to D^{(*)}\tau\nu$  has evolved into a comprehensive research program [\[18](#page-15-9)–30]. One aims to construct the full differential decay rate and then integrate out all kinematic variables that are unobservable due to the presence of neutrinos [\[24,30\].](#page-16-0)

In this paper, we develop a complete framework to extract the full set of  $B \to D^{(*)}\tau\nu$  observables (with polarized  $\tau$  and unpolarized  $D^{(*)}$ ) from the visible final state. We focus on the hadronic  $\tau$  decays  $\tau \to \pi \nu$  and  $\tau \to \rho \nu$ , which preserve

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more information on the  $\tau$  kinematics than the leptonic decays  $\tau \to \ell \nu \nu$  [\[26\].](#page-16-1) In the two-body decays, the  $\tau$  spin orientation is directly imprinted on the pion or rho direction of flight. The  $\tau$  helicity and kinematics can thus be deduced from the energy and angular distributions of the visible final-state particles [\[21,26,31,32\]](#page-16-2). The main result of our paper allows us to express the differential decay rate of  $B \to D^{(*)}\tau (\to d\nu)\nu$  as

<span id="page-2-1"></span>
$$
\frac{d^3\Gamma_d}{dq^2 d\cos\theta_d ds_d} = n(q^2) \bigg( 1 + \sum_{\mathcal{O}} F^d_{\mathcal{O}}(q^2, \cos\theta_d, s_d) \mathcal{O}(q^2) \bigg). \tag{1.1}
$$

Here  $q^2$ ,  $\cos \theta_d$ , and  $s_d$  describe measurable kinematic quantities in the leptonic rest frame (the momentum transfer to the lepton pair, the angle between the  $\tau$  daughter d and the  $D^{(*)}$ , and the energy of the d), and  $n(q^2)$  is a<br>normalization factor. Importantly, the "leptonic functions" normalization factor. Importantly, the "leptonic functions"  $F_{\mathcal{O}}^{d}(q^2, \cos \theta_d, s_d)$  depend only on the  $\tau \to d\nu$  decay. The sum is over seven asymmetry observables of the  $B \to D^{(*)}\tau\nu$ transition,

<span id="page-2-0"></span>
$$
\mathcal{O} = A_{FB}, P_L, P_\perp, Z_L, Z_\perp, Z_Q, A_Q, \tag{1.2}
$$

to be defined in the next section. This formula directly relates these asymmetry observables to the kinematic distribution of the  $\tau$  daughter. By measuring the kinematics of the d particle, one can extract nearly all the physics of the  $b \to c\tau\nu$ transition, including the possible presence of new physics affecting the transition.

The asymmetry observables represent a useful intermediate step between the data and the underlying Wilson coefficients. Previous studies [\[2,31](#page-15-1)–49] have identified a subset of these asymmetries  $(A_{FB}, P_L, P_{\perp})$  and shown how to extract them from differential distributions of the final state. In this work, we show that a total of nine asymmetries, together with the differential decay rate  $d\Gamma_B/dq^2$ , suffice to describe the full physics of  $B \to D^{(*)}\tau\nu$  with unpolarized  $D^{(*)}$ . The remaining two not listed in Eq. [\(1.2\)](#page-2-0),  $P<sub>T</sub>$  and  $Z<sub>T</sub>$ , are nonzero only in the presence of CP violation, and furthermore are only accessible by including additional information—e.g., from  $D^{(*)}$  decays [\[30\]](#page-16-3)—in the kinematic distributions. We reserve a complete study of these additional observables for a future publication [\[50\]](#page-16-4).

We will demonstrate how one could theoretically measure the asymmetries by performing an unbinned maximum-likelihood fit to the  $d$  distribution [Eq. [\(1.1\)](#page-2-1)]. While we do not include realistic experimental considerations such as systematic uncertainties, detector acceptance, or backgrounds (these are beyond the scope of this work), we show that at least the statistical power with 50 ab<sup>−</sup><sup>1</sup> of Belle II data should be enough to measure the asymmetry observables to percent-level precision.

Analytic formulas like Eq. [\(1.1\)](#page-2-1) could prove useful in experimental studies. Besides being needed for maximumlikelihood fits, they could be adapted for Monte Carlo generators [\[51\]](#page-16-5). Another line in this direction has been providing efficient methods to reweight Monte Carlo event samples interpreting experimental data directly in terms of SM or NP parameters [\[19,25,29\]](#page-15-10).

The outline of the paper is as follows: In Sec. [II,](#page-2-2) we decompose the  $B \to D^{(*)}\tau\nu$  kinematics into a complete set of  $\tau$  asymmetries. These asymmetries contain all information that could be obtained if the  $\tau$  momentum were fully accessible. In Sec. [III,](#page-4-0) we show how to extract seven of the nine  $\tau$  asymmetries from the kinematics of the  $\tau$  decay products. By performing a full-fledged statistical analysis in Sec. [IV,](#page-6-0) we give a theoretical estimate of the expected sensitivity of Belle II to the asymmetries, assuming a given number of events and neglecting experimental effects. We also demonstrate how to decipher the structure of new physics in  $\tau$  production in the framework of an effective theory and in the context of the current anomalies found in the  $R_{D^{(*)}}$  ratios. We conclude in Sec. [V](#page-11-0) with a summary and outlook.

### <span id="page-2-2"></span>II. TAU ASYMMETRIES IN  $B \to D^{(*)} \tau \nu$

In this section, we focus on the  $B \to M\tau\nu$  decay kinematics, where  $M = D$  or  $D^*$ , without considering<br>the  $\tau$  decays vet. The narrow width of the  $\tau$  enables a the  $\tau$  decays yet. The narrow width of the  $\tau$  enables a factorization of the full decay chain into a  $\tau$ -production part and a  $\tau$ -decay part.

<span id="page-2-3"></span>The basis for the  $\tau$  asymmetries is the differential decay rate for  $B \to M\tau\nu$  with the  $\tau$  spin quantized along an arbitrary direction  $\hat{\mathbf{e}}_a$ ,

$$
d\Gamma_B^{\lambda_r, a} = \frac{1}{2m_B} |\mathcal{M}_B^{\lambda_r, a}|^2 d\Phi_3(p_B; p_M, p_\tau, p_\nu).
$$
 (2.1)

Here  $\lambda_{\tau} = \pm$  is the direction of the  $\tau$  spin along the  $\hat{\mathbf{e}}_a$  axis, and the Lorentz-invariant phase space for a particle i decaying to  $n$  daughters is

$$
d\Phi_n(p_i; p_1, ..., p_n) = (2\pi)^4 \prod_{j=1}^n \frac{d^3 \mathbf{p}_j}{(2\pi)^3 2E_j} \delta^4 \left( p_i - \sum_{j=1}^n p_j \right).
$$
\n(2.2)

Throughout this work, we sum over the polarization states of the  $D^*$  meson.

<span id="page-2-4"></span>The total differential decay rate can be calculated from the spin-dependent decay rates along any axis as

$$
d\Gamma_B = d\Gamma_B^{+,a} + d\Gamma_B^{-,a}.\tag{2.3}
$$

On the contrary, a  $\tau$ -spin asymmetry

<span id="page-3-0"></span>

FIG. 1. The two decay planes of  $B \to M\tau\nu$  (black) and  $\tau \to d\nu$ (red) in the  $q^2$  frame. The angle between the two planes is denoted  $\zeta$ . The angle between the flight direction of the  $\tau$  and the negative direction of M is denoted  $\theta_{\tau}$ . In the decay plane of the  $\tau$ ,  $\varphi$  is the angle between the direction of the  $\tau$  and the direction of the daughter particle d. Finally, the angle  $\theta_d$  is the angle between the direction of the daughter particle (in the  $\tau$  decay plane) and the negative direction of  $M$  (in the  $B$ -decay plane).

$$
d\mathcal{P}_B^a = d\Gamma_B^{+,a} - d\Gamma_B^{-,a} \tag{2.4}
$$

is always defined along the particular axis  $\hat{\mathbf{e}}_a$ .

We work in the " $q^2$  frame," the center-of-mass frame of the lepton pair, with  $q^2 = (p_B - p_M)^2$  being the momentum squared transferred to the leptons. Figure [1](#page-3-0) illustrates the various momentum vectors, polarization vectors, and angles involved in the  $q^2$  frame. Let  $\{\hat{\mathbf{e}}_1, \hat{\mathbf{e}}_2, \hat{\mathbf{e}}_3\}$  be an orthonormal coordinate system in this frame and choose

$$
\hat{\mathbf{e}}_3 = \hat{\mathbf{p}}_\tau \equiv \hat{\mathbf{e}}_L,\tag{2.5}
$$

where  $\hat{\mathbf{p}}_{\tau}$  is the direction of the  $\tau$  momentum. The spindependent differential decay rate [\(2.1\)](#page-2-3) and the asymmetries [\(2.4\)](#page-2-4) can then be expressed using  $\tau$  helicity amplitudes  $\mathcal{M}_B^{\lambda_r,L}$ . From here on, the index  $a = L$  will be suppressed.<br>The resulting expressions for the asymmetries depend on The resulting expressions for the asymmetries depend on how the axes  $\hat{\mathbf{e}}_1$  and  $\hat{\mathbf{e}}_2$  are chosen. Choosing

<span id="page-3-1"></span>
$$
\hat{\mathbf{e}}_2 = \frac{\hat{\mathbf{p}}_M \times \hat{\mathbf{p}}_\tau}{|\hat{\mathbf{p}}_M \times \hat{\mathbf{p}}_\tau|} \equiv \hat{\mathbf{e}}_T, \qquad \hat{\mathbf{e}}_1 = \hat{\mathbf{e}}_T \times \hat{\mathbf{e}}_L \equiv \hat{\mathbf{e}}_\perp, \quad (2.6)
$$

where  $\hat{\mathbf{p}}_M$  is the direction of the M momentum, results in

$$
d\Gamma_B^{\lambda_\tau} = \frac{1}{2m_B} |\mathcal{M}_B^{\lambda_\tau}|^2 d\Phi_3(p_B; p_M, p_\tau, p_\nu),
$$
  
\n
$$
d\mathcal{P}_B^\perp = \frac{1}{2m_B} 2 \operatorname{Re}[\mathcal{M}_B^+(\mathcal{M}_B^-)^{\dagger}] d\Phi_3(p_B; p_M, p_\tau, p_\nu),
$$
  
\n
$$
d\mathcal{P}_B^T = \frac{1}{2m_B} 2 \operatorname{Im}[\mathcal{M}_B^+(\mathcal{M}_B^-)^{\dagger}] d\Phi_3(p_B; p_M, p_\tau, p_\nu).
$$
 (2.7)

These four differential distributions capture all the information in the matrix elements  $\mathcal{M}_{B}^{\pm}$  in the  $B \to D^{(*)}\tau\nu$ decay (with unpolarized  $D^*$ ).

The matrix elements do not depend on the azimuthal angle of the  $\tau$  momentum with respect to the M momentum; this angle is thus integrated out. The two remaining degrees of freedom in the final state are chosen to be  $q^2$  and  $\cos\theta_\tau$ , where  $\theta_{\tau}$  is the angle between the flight direction of the  $\tau$ and the negative direction of the M momentum in the  $q^2$ frame. The decay rates and asymmetries for  $B \to M\tau\nu$  can be expanded in spherical harmonics encoding the con-servation of angular momentum [\[1\]:](#page-15-0)

<span id="page-3-2"></span>
$$
\frac{d^2\Gamma_B^{\lambda_\tau}}{dq^2 d\cos\theta_\tau} = \frac{d\Gamma_B}{dq^2} \sum_{\ell=0}^2 B_{\ell}^{\lambda_\tau}(q^2) P_{\ell}^0(\cos\theta_\tau),
$$

$$
\frac{d^2\mathcal{P}_B^{\perp}}{dq^2 d\cos\theta_\tau} = \frac{d\Gamma_B}{dq^2} \sum_{\ell=1}^2 \text{Re}[C_{\ell}(q^2)] P_{\ell}^1(\cos\theta_\tau),
$$

$$
\frac{d^2\mathcal{P}_B^T}{dq^2 d\cos\theta_\tau} = \frac{d\Gamma_B}{dq^2} \sum_{\ell=1}^2 \text{Im}[C_{\ell}(q^2)] P_{\ell}^1(\cos\theta_\tau), \qquad (2.8)
$$

where  $P_e^{0,1}(\cos \theta_\tau)$  are the associated Legendre func-<br>tions. Together with the total differential rate  $d\Gamma/d\sigma^2$ tions. Together with the total differential rate  $d\Gamma_B/dq^2$ , the angular coefficient functions  $B_{0,1,2}^{\pm}(q^2) \in \mathbb{R}$  and  $C_{\pm}(q^2) \subset \mathbb{C}$  describe the full linear stic information in  $C_{1,2}(q^2) \in \mathbb{C}$  describe the full kinematic information in  $B \to M \tau \nu$  decays with unpolarized mesons.

Although the angular coefficient functions are themselves perfectly valid observables, it is more conventional (and physical) to work in terms of various asymmetries of the  $\tau$  angle cos  $\theta_{\tau}$  and spin direction  $\lambda_{\tau}$ . An equivalent and complete basis of  $\tau$  asymmetries is as follows:

<span id="page-3-3"></span>(1) The  $\tau$  forward-backward asymmetry is

$$
A_{FB}(q^2) = \left(\frac{d\Gamma_B}{dq^2}\right)^{-1} \left(\int_0^1 d\cos\theta_\tau - \int_{-1}^0 d\cos\theta_\tau\right)
$$

$$
\times \frac{d^2\Gamma_B}{dq^2 d\cos\theta_\tau} = B_1^+ + B_1^-.
$$
 (2.9)

(2) Pure spin asymmetries are given by

$$
P_a(q^2) = \left(\frac{d\Gamma_B}{dq^2}\right)^{-1} \int_{-1}^1 d\cos\theta_\tau \frac{d^2 \mathcal{P}_B^a}{dq^2 d\cos\theta_\tau}
$$

$$
= \begin{cases} 2(B_0^+ - B_0^-) & a = L \\ -\frac{\pi}{2} \text{Re}[\mathcal{C}_1] & a = \bot. \\ -\frac{\pi}{2} \text{Im}[\mathcal{C}_1] & a = T \end{cases} (2.10)
$$

The spin asymmetries  $P_a$  correspond to the net longitudinal, perpendicular, and transverse polarizations of the  $\tau$  in  $B \to M\tau\nu$  decays. The asymmetries we have described so far have been considered before in the literature [2,31–[49,52,53\].](#page-15-1)

(3) We can additionally consider double asymmetries with respect to both  $\lambda_{\tau}$  and  $\cos \theta_{\tau}^{-1}$ :

$$
Z_a(q^2) = \left(\frac{d\Gamma_B}{dq^2}\right)^{-1} \left(\int_0^1 d\cos\theta_\tau - \int_{-1}^0 d\cos\theta_\tau\right)
$$

$$
\times \frac{d^2 \mathcal{P}_B^a}{dq^2 d\cos\theta_\tau} = \begin{cases} B_1^+ - B_1^- & a = L \\ -2\text{Re}[C_2] & a = \bot \\ -2\text{Im}[C_2] & a = T \end{cases} (2.11)
$$

These asymmetries have not been considered before and give access to the previously unexplored combinations of angular coefficient functions  $B_1^{\pm}$ and  $C_2$ <sup>2</sup>

(4) The angular coefficient functions  $B_2^{\pm}$  cannot be expressed in terms of simple asymmetries like the other functions. They denote the *quadrupole* part of the partial wave expansion in Eq.  $(2.7)$ . We combine these angular coefficient functions to define the following asymmetry observables:

<span id="page-4-2"></span>
$$
A_Q(q^2) = \left(\frac{d\Gamma_B}{dq^2}\right)^{-1} \frac{5}{2} \int_{-1}^1 d\cos\theta_\tau P_2^0(\cos\theta_\tau)
$$
  

$$
\times \frac{d^2\Gamma_B}{dq^2 d\cos\theta_\tau} = B_2^+ + B_2^-,
$$
  

$$
Z_Q(q^2) = \left(\frac{d\Gamma_B}{dq^2}\right)^{-1} \frac{5}{2} \int_{-1}^1 d\cos\theta_\tau P_2^0(\cos\theta_\tau)
$$
  

$$
\times \frac{d^2\mathcal{P}_B^L}{dq^2 d\cos\theta_\tau} = B_2^+ - B_2^-,
$$
 (2.12)

where the  $5/2$  prefactor captures the Legendre polynomial normalization.

(5) Finally, given that we have extracted an overall factor of  $d\Gamma_B/dq^2$  in the definition [\(2.8\)](#page-3-2) of the angular coefficient functions, they satisfy the relation  $B_0^+ + B_0^- = \frac{1}{2}$ .

### <span id="page-4-0"></span>III. TAU ASYMMETRIES FROM THE VISIBLE FINAL STATE

Since the  $\tau$  decays promptly in the detector with one or two neutrinos in the final state, it is generally not possible to reconstruct its full four-momentum.<sup>3</sup> Therefore, the  $\tau$ asymmetries in  $B \to M\tau\nu$  described in Sec. [II](#page-2-2) are not directly measurable. In this section, we will show how they can be extracted from final-state observables with fully reconstructed mesons M. We focus on the two-body decays  $\tau \to d\nu$  with  $d = \pi$ ,  $\rho$ , as they preserve more information compared to the three-body decay  $\tau \to \ell \nu \nu$ . However, our formalism can be straightforwardly generalized to  $\tau \rightarrow \ell \nu \nu$ or other  $\tau$ -decay modes.

Figure [1](#page-3-0) shows the two decay planes of  $B \to M\tau\nu$  and  $\tau \rightarrow d\nu$ , and the various angles and momenta involved in the decays in the  $q^2$  frame. The angle  $\theta_d$  between  $\vec{p}_d$  and  $-\vec{p}_M$  is the only directly measurable angle. Meanwhile,  $\varphi$ (the angle between  $\vec{p}_{\tau}$  and  $\vec{p}_d$ ),  $\zeta$  (the angle between the two decay planes), and  $\theta_{\tau}$  are not directly measurable. However,  $\varphi$  is completely determined by the kinematics of the twobody decay as

$$
\cos \varphi = \frac{(1 + r_\tau^2) s_d - (r_\tau^2 + r_d^2)}{(1 - r_\tau^2) \sqrt{s_d^2 - r_d^2}}.
$$
 (3.1)

Here we have introduced the notation

$$
s_d \equiv \frac{E_d}{\sqrt{q^2}}, \qquad r_\tau \equiv \frac{m_\tau}{\sqrt{q^2}}, \qquad r_d \equiv \frac{m_d}{\sqrt{q^2}}, \qquad (3.2)
$$

where  $E_d$  and  $m_d$  denote the energy and mass of the daughter particle in the  $q^2$  frame. It is straightforward to show that the allowed range of  $s_d$  is

$$
s_d \in \left[\frac{r_{\bar{t}}^2}{2}\left(1 + \frac{r_d^2}{r_{\bar{t}}^4}\right), \frac{1}{2}\left(1 + r_d^2\right)\right].\tag{3.3}
$$

<span id="page-4-1"></span>Finally, the angles  $\theta_{\tau}$  and  $\zeta$  are related to  $\varphi$  and  $\theta_{d}$  via

$$
\cos \theta_d = \cos \theta_\tau \cos \varphi + \sin \theta_\tau \sin \varphi \cos \zeta. \tag{3.4}
$$

The matrix element for the full  $B \to D^{(*)}\tau(\to d\nu_2)\nu_1$ decay is

$$
\mathcal{M}_{\text{tot}} = \frac{1}{p_{\tau}^2 - m_{\tau}^2 + i m_{\tau} \Gamma_{\tau}} \sum_{\lambda_{\tau} = \pm} \mathcal{M}_{B}^{\lambda_{\tau}} \mathcal{M}_{\tau}^{\lambda_{\tau}}, \qquad (3.5)
$$

where  $\mathcal{M}_B$  is the matrix element for  $B \to M\tau\nu$  as intro-duced in Sec. [II](#page-2-2),  $\Gamma_{\tau}$  is the total width of the  $\tau$ , and  $\mathcal{M}_{\tau}$  is the matrix element for  $\tau \rightarrow d\nu$ . In the narrow width approximation, the four-body phase space factorizes as

<sup>&</sup>lt;sup>1</sup>Z stands for zweifach.

<sup>&</sup>lt;sup>2</sup>In  $B \to D\tau \nu$ , some of the  $\tau$  asymmetries are absent because the pseudoscalar nature of the  $D$  meson restricts the possible angular coefficient functions. In particular, it has been shown that  $B_1^- = 0$  for the most general effective Lagrangian with scalar,<br>vector, and tensor operators (with left-handed neutrinos only) vector, and tensor operators (with left-handed neutrinos only) [\[27\].](#page-16-6) This implies that  $Z_L = A_{FB}$  in  $B \to D\tau \nu$  and no independent information is gained from  $Z_L$ . In  $B \to D^* \tau \nu$ ,  $B_1^-$  is generated by the transverse polarization of the  $D^*$  vector meson [\[24\],](#page-16-0) so that  $A_{FB}$  and  $Z_L$  carry independent information.

<sup>&</sup>lt;sup>3</sup>The full  $\tau$  kinematics could potentially be accessed with displaced three-prong decays [\[54\].](#page-16-7)

$$
\frac{1}{(p_{\tau}^2 - m_{\tau}^2)^2 + m_{\tau}^2 \Gamma_{\tau}^2} d\Phi_4(p_B; p_M, p_{\nu_1}, p_d, p_{\nu_2})
$$
\n
$$
\longrightarrow \frac{1}{2m_{\tau} \Gamma_{\tau}} d\Phi_3(p_B; p_M, p_{\tau}, p_{\nu_1}) d\Phi_2(p_{\tau}; p_d, p_{\nu_2}), \quad (3.6)
$$

<span id="page-5-0"></span>with the  $\tau$  set on shell. Then the full fourfold differential decay rate is

$$
\frac{d^4\Gamma_d}{dq^2 d\cos\theta_\tau ds_d d\zeta}
$$
\n
$$
= \frac{E_\tau}{\Gamma_\tau m_\tau} \left( \frac{d^2\Gamma_B^{\lambda_\tau}}{dq^2 d\cos\theta_\tau} \frac{d^2\Gamma_\tau^{\lambda_\tau}}{ds_d d\zeta} + \frac{1}{2} \left[ \frac{d^2\mathcal{P}_B^{\perp}}{dq^2 d\cos\theta_\tau} \frac{d^2\mathcal{P}_B^{\perp}}{ds_d d\zeta} - \frac{d^2\mathcal{P}_B^T}{dq^2 d\cos\theta_\tau} \frac{d^2\mathcal{P}_\tau^T}{ds_d d\zeta} \right] \right), \quad (3.7)
$$

<span id="page-5-1"></span>where repeated  $\lambda_{\tau}$  indices are summed over. All terms are factorized into a B-decay part [see Eq.  $(2.8)$ ] and a  $\tau$ -decay part defined as

$$
d\Gamma_{\tau}^{\lambda_{\tau}} = \frac{1}{2E_{\tau}} |\mathcal{M}_{\tau}^{\lambda_{\tau}}|^{2} d\Phi_{2}(p_{\tau}; p_{d}, p_{\nu_{2}}),
$$
  
\n
$$
d\mathcal{P}_{\tau}^{\perp} = \frac{1}{2E_{\tau}} 2 \operatorname{Re}[\mathcal{M}_{\tau}^{+}(\mathcal{M}_{\tau}^{-})^{\dagger}] d\Phi_{2}(p_{\tau}; p_{d}, p_{\nu_{2}}),
$$
  
\n
$$
d\mathcal{P}_{\tau}^{T} = \frac{1}{2E_{\tau}} 2 \operatorname{Im}[\mathcal{M}_{\tau}^{+}(\mathcal{M}_{\tau}^{-})^{\dagger}] d\Phi_{2}(p_{\tau}; p_{d}, p_{\nu_{2}}).
$$
\n(3.8)

<span id="page-5-4"></span>Similarly to how  $d\Gamma_B^{\lambda_\tau}$  and  $d\mathcal{P}_B^{\perp,T}$  could be expanded in  $\cos \theta_{\tau}$ , the expressions above can be expanded in the angles  $\varphi$  and ζ. For a two-body  $\tau \to d\nu$  decay,

$$
\frac{d\Gamma_{\tau}^{\lambda_{\tau}}}{ds_{d}d\zeta} = \frac{m_{\tau}\Gamma_{\tau \to d\nu}}{\pi E_{\tau}} g_{d}^{\lambda_{\tau}}(q^{2}, s_{d}),
$$
\n
$$
\frac{d\mathcal{P}_{\tau}^{\perp}}{ds_{d}d\zeta} = \frac{2m_{\tau}\Gamma_{\tau \to d\nu}}{\pi E_{\tau}} h_{d}(q^{2}, s_{d}) \sin \varphi(q^{2}, s_{d}) \cos \zeta,
$$
\n
$$
\frac{d\mathcal{P}_{\tau}^{T}}{ds_{d}d\zeta} = \frac{2m_{\tau}\Gamma_{\tau \to d\nu}}{\pi E_{\tau}} h_{d}(q^{2}, s_{d}) \sin \varphi(q^{2}, s_{d}) \sin \zeta,
$$
\n(3.9)

where the coefficient functions for  $d = \pi$ ,  $\rho$  are given by

$$
g_{\pi}^{\pm} = \frac{1}{1 - r_{\tau}^{2}} \left( 1 \pm \frac{4s_{\pi} - (1 + r_{\tau}^{2})}{(1 - r_{\tau}^{2})} \right),
$$
  
\n
$$
g_{\rho}^{\pm} = \frac{r_{\tau}^{2}((1 - r_{\tau}^{2})(r_{\tau}^{2} - r_{\rho}^{2})(2r_{\rho}^{2} + r_{\tau}^{2}) \pm (r_{\tau}^{2} - 2r_{\rho}^{2})(4s_{\rho}r_{\tau}^{2} - (1 + r_{\tau}^{2})(r_{\tau}^{2} + r_{\rho}^{2})))}{(r_{\tau}^{2} - r_{\rho}^{2})^{2}(2r_{\rho}^{2} + r_{\tau}^{2})(1 - r_{\tau}^{2})^{2}},
$$
  
\n
$$
h_{\pi} = \frac{2}{1 - r_{\tau}^{2}} \frac{s_{\pi}}{r_{\tau}},
$$
  
\n
$$
h_{\rho} = \frac{2}{1 - r_{\tau}^{2}} \left( \frac{r_{\tau}^{2} - 2r_{\rho}^{2}}{2r_{\rho}^{2} + r_{\tau}^{2}} \right) \sqrt{s_{\rho}^{2} - r_{\rho}^{2}} \frac{r_{\tau}^{3}}{(r_{\tau}^{2} - r_{\rho}^{2})^{2}}.
$$
  
\n(3.10)

Throughout our analysis, we neglect the  $\pi$  mass but not the  $\rho$  mass.

<span id="page-5-5"></span>To transform Eq. [\(3.7\)](#page-5-0) into a fully observable, fully differential decay rate, we need to integrate over the two unobservable angles  $\theta_{\tau}$  and  $\zeta$  and replace them with the single observable angle  $\theta_d$ . Formally, this can be accomplished using Eq. [\(3.4\)](#page-4-1) to obtain

$$
\frac{d^3\Gamma_d}{dq^2 d\cos\theta_d ds_d} = \int_{-1}^1 d\cos\theta_\tau \int_{-\pi}^\pi d\zeta \frac{d^4\Gamma_d}{dq^2 d\cos\theta_\tau ds_d d\zeta} \delta(\cos\theta_d - \cos\theta_\tau \cos\varphi - \sin\theta_\tau \sin\varphi \cos\zeta). \tag{3.11}
$$

<span id="page-5-3"></span>In Appendix [A,](#page-12-0) we carry out these integrals explicitly. The result is given by

$$
\frac{d^3\Gamma_d}{dq^2d\cos\theta_d ds_d} = \text{BR}(\tau \to d\nu) \frac{d\Gamma_B}{dq^2} \sum_{\ell=0}^2 P_{\ell}(\cos\theta_d) I_{\ell}(q^2, s_d),
$$
  
\n
$$
I_0 = \frac{1}{2} (f_0^d(q^2) + f_L^d(q^2, s_d) P_L(q^2)),
$$
  
\n
$$
I_1 = f_{A_{FB}}^d(q^2, s_d) A_{FB}(q^2) + f_{\perp}^d(q^2, s_d) P_{\perp}(q^2) + f_{Z_L}^d(q^2, s_d) Z_L(q^2),
$$
  
\n
$$
I_2 = f_{Z_{\perp}}^d(q^2, s_d) Z_{\perp}(q^2) + f_{Z_Q}^d(q^2, s_d) Z_Q(q^2) + f_{A_Q}^d(q^2, s_d) A_Q(q^2).
$$
\n(3.12)

<span id="page-5-2"></span>Here we have used Eqs. [\(2.9\)](#page-3-3)–[\(2.12\)](#page-4-2) to connect the differential distribution to the  $\tau$  asymmetries, and we have defined the leptonic functions

$$
f_0^d(q^2) = g_d^+(q^2, s_d) + g_d^-(q^2, s_d),
$$
  
\n
$$
f_L^d(q^2, s_d) = g_d^+(q^2, s_d) - g_d^-(q^2, s_d),
$$
  
\n
$$
f_\perp^d(q^2, s_d) = \frac{4}{\pi} \sin^2 \varphi h_d(q^2, s_d),
$$
  
\n
$$
f_{A_{FB}}^d(q^2, s_d) = \cos \varphi f_0^d(q^2),
$$
  
\n
$$
f_{Z_L}^d(q^2, s_d) = \cos \varphi f_L^d(q^2, s_d),
$$
  
\n
$$
f_{Z_L}^d(q^2, s_d) = \frac{3\pi}{4} \cos \varphi f_\perp^d(q^2, s_d),
$$
  
\n
$$
f_{A_Q}^d(q^2, s_d) = \frac{1}{2} (3 \cos^2 \varphi - 1) f_0^d(q^2),
$$
  
\n
$$
f_{Z_Q}^d(q^2, s_d) = \frac{1}{2} (3 \cos^2 \varphi - 1) f_L^d(q^2).
$$
  
\n(3.13)

One can verify using Eq. [\(3.10\)](#page-5-1) that the first four leptonic functions in Eq. [\(3.13\)](#page-5-2) agree precisely with those considered in Ref. [\[26\].](#page-16-1)

We see that the fully differential final-state decay rate breaks down into a linear combination of the asymmetries, or equivalently, of the angular coefficient functions  $B_{0,1,2}^{\pm}$ and  $Re[C_{1,2}]$ . We emphasize that Eq. [\(3.12\)](#page-5-3) is completely general even in the presence of arbitrary heavy new physics altering the  $b \to c\tau \nu$  transition. The leptonic functions are independent of the  $b \to c\tau\nu$  transition and depend only on the  $\tau$ -decay mode. Therefore, one could use Eq. [\(3.12\)](#page-5-3) to directly extract the asymmetries from the data in a completely model-independent way. We will investigate the theoretical sensitivity of such an approach in the next section.

### <span id="page-6-0"></span>IV. SENSITIVITY TO ASYMMETRY OBSERVABLES AT BELLE II

Having derived analytic expressions for the fully differential final-state decay rate and related them to the  $B \to M\tau\nu$  asymmetry observables, we now turn to a toy study of how the asymmetry observables could be measured in practice, and what precision one could hope to achieve. We cannot comment on the systematic uncertainties associated with our proposal at different experiments. A detailed simulation of backgrounds and detector effects is also beyond the scope of this work. We will limit ourselves to calculating the achievable statistical uncertainty; this should furnish a "best-case scenario" for the sensitivity of any future measurement.

For the analysis in this section, we will need explicit numerical formulas for all the asymmetries in terms of the dimension-6 effective Hamiltonian. The dependence of the asymmetries  $P_a(q^2)$   $(a = L, \perp, T)$  and  $A_{FB}(q^2)$  on all the relevant dimension-6 operators has already been calculated [\[27\]](#page-16-6). Following the notation of Refs. [\[27,55\],](#page-16-6) we include the analytic expressions for the new asymmetries  $A_{\mathcal{O}}(q^2)$  and  $Z_a(q^2)$  ( $a = L, \perp, T, Q$ ) in Appendix [B.](#page-13-0)

#### A. Maximum likelihood method

The energy  $s_d$  and the angle  $\cos \theta_d$  of the daughter in  $\tau \rightarrow d\nu$  decays are directly measurable at Belle II. Using the fully differential distribution [Eq. [\(3.12\)](#page-5-3)], we apply the unbinned maximum likelihood method in  $s_d$  and cos  $\theta_d$  to fit for the asymmetry observables in  $q^2$  bins and determine the covariance matrices around the best-fit values. We do not assume any templates for the  $q^2$  dependence from the SM or otherwise; we consider a separate and independent measurement of the asymmetries in each  $q^2$  bin.<sup>4</sup>

Let  $\mathcal{O}(q_i^2)$  for  $\mathcal{O} = A_{FB}$ ,  $P_L$ , etc., be the parameters that we want to fit for in  $q^2$  bin *i*. According to Eq. [\(3.12\),](#page-5-3) the probability distribution of events in  $q^2$  bin i in terms of these parameters is given by

$$
p_i(s_d, \cos\theta_d | \mathcal{O}(q_i^2)) = \frac{1}{2} (f_0^d(q_i^2) + f_L^d(s_d, q_i^2) P_L(q_i^2)) P_0(\cos\theta_d)
$$
  
+ 
$$
(f_{A_{FB}}^d(s_d, q_i^2) A_{FB}(q_i^2) + f_L^d(s_d, q_i^2) P_\perp(q_i^2) + f_{Z_L}^d(s_d, q_i^2) Z_L(q_i^2)) P_1(\cos\theta_d)
$$
  
+ 
$$
(f_{Z_\perp}^d(s_d, q_i^2) Z_\perp(q_i^2) + f_{Z_Q}^d(s_d, q_i^2) Z_Q(q_i^2) + f_{A_Q}^d(s_d, q_i^2) A_Q(q_i^2)) P_2(\cos\theta_d).
$$
 (4.1)

We assume that the event numbers in each  $q^2$  bin are large enough that the asymptotic form of the maximum likelihood method can be used. Then the log-likelihood statistic to be maximized is

$$
L(\mathcal{O}(q_i^2)) = Nf_i \int ds_d d\cos\theta_d p_i(s_d, \cos\theta_d | \hat{\mathcal{O}}(q_i^2)) \log p_i(s_d, \cos\theta_d | \mathcal{O}(q_i^2)), \tag{4.2}
$$

<sup>&</sup>lt;sup>4</sup>The statistical analysis outlined in this section expands on a previous analysis of  $B \to D\tau\nu$  [\[26\]](#page-16-1). In the analysis of Ref. [\[26\],](#page-16-1) instead of a fit to the complete distribution of events in cos  $\hat{\theta}_d$ , only two bins distinguished by sgn(cos  $\theta_d$ ) are considered. By fitting to the full distribution, we get access to the new observables  $Z_{\perp}$ ,  $Z_L$ ,  $Z_Q$ , and  $A_Q$ , and we also increase the sensitivity to the remaining asymmetries.

<span id="page-7-1"></span>

FIG. 2. Distributions of  $A_{FB}$ ,  $P_L$ ,  $P_{\perp}$ ,  $Z_L$ ,  $Z_{\perp}$ ,  $Z_Q$ , and  $A_Q$  for the decays  $B \to D\tau\nu$  (green) and  $B \to D^*\tau\nu$  (orange). The solid curves show the SM predictions. The dashed (dotted) curves refer to two NP scenarios with  $U_1$  (S<sub>1</sub> – R<sub>2</sub>) leptoquarks discussed in Sec. [IV C.](#page-10-0) The statistical uncertainties obtained from our maximum-likelihood analysis are shown as purple bands for  $N = 3000$  events in the  $\tau \to \pi \nu$  channel.

where  $\hat{\mathcal{O}}(q_i^2)$  are the true values of the asymmetry ob-<br>servables N is the total number of events and servables, N is the total number of events, and

$$
f_i \equiv \Delta q^2 \Gamma_B^{-1} \frac{d\Gamma_B}{dq^2} (q_i^2)
$$
 (4.3)

is the fraction of events in  $q^2$  bin i with bin width  $\Delta q^2$ . The elements of the inverse covariance matrix for bin  $i$  are given by

$$
(\Sigma^i)^{-1}_{ab} = -\partial_{\mathcal{O}_a(q_i^2)} \partial_{\mathcal{O}_b(q_i^2)} L(\mathcal{O}(q_i^2))|_{\mathcal{O}(q_i^2) = \hat{\mathcal{O}}(q_i^2)}.
$$
 (4.4)

<span id="page-7-0"></span>In the following, we report the sensitivity to the  $q^2$ integrated asymmetries, defined by

$$
\mathcal{O} = \frac{1}{\Gamma_B} \int dq^2 \frac{d\Gamma_B}{dq^2} \mathcal{O}(q^2),\tag{4.5}
$$

where  $\mathcal{O} = A_{FB}, P_L$ , etc. These integrated asymmetries provide us with a sensitivity estimate in the case of limited

<span id="page-8-0"></span>

FIG. 3. 68% (solid) and 95% (dashed) confidence intervals for the statistical sensitivity to the  $\tau$  asymmetries in the SM in  $B \to D\tau(\to \pi\nu)\nu$  (pink) and  $B \to D\tau(\to \rho\nu)\nu$  (blue) decays. The central values are marked for the SM (pink star), as well as for the NP scenarios  $U_1$  (yellow square) and  $S_1 - R_2$  (green diamond). The correlation coefficients  $\rho_{\pi}$  and  $\rho_{\rho}$  for each pair of asymmetries are shown in a boxed insert. Assumed is a dataset of  $N = 3000$  total events in each channel.

event statistics. To combine the covariance matrices in each  $q^2$  bin into a total covariance matrix for the integrated observables, we use the discretized form of Eq. [\(4.5\),](#page-7-0)

$$
\mathcal{O} \approx \sum_{i} f_i \mathcal{O}(q_i^2). \tag{4.6}
$$

The total covariance matrix is then

$$
\Sigma = \sum_{i} f_i^2 \Sigma^i. \tag{4.7}
$$

In the following subsections, we will report values and make plots of the variances  $\sigma_a^2$  (the diagonal elements of  $\Sigma$ ) and the correlation coefficients  $\rho_{ab} = \sigma_{ab}/(\sigma_a \sigma_b)$  (derived from the off-diagonal elements of  $\Sigma$ ).

<span id="page-9-0"></span>

FIG. 4. 68% (solid) and 95% (dashed) confidence intervals for the statistical sensitivity to the  $\tau$  asymmetries in the SM in  $B \to D^*\tau(\to \pi\nu)\nu$  (pink) and  $B \to D^*\tau(\to \rho\nu)\nu$  (blue) decays. The central values are marked for the SM (pink star), as well as for the NP<br>scenarios *U*, (vellow square) and *S*,  $-R_2$  (green diamond). The correlation coef scenarios  $U_1$  (yellow square) and  $S_1 - R_2$  (green diamond). The correlation coefficients  $\rho_{\pi}$  and  $\rho_{\rho}$  for each pair of asymmetries are shown in a boxed insert. Assumed is a dataset of  $N = 3000$  total events in each channel.

### B. Standard Model sensitivity

Using this method, we determine the theoretical sensitivity to the  $q^2$ -integrated asymmetries, assuming the SM prediction for all the parameters—i.e.,  $\hat{\mathcal{O}}(q_i^2) = \mathcal{O}_{SM}(q_i^2)$ .<br>It is trivial to repeat the englysis for a segmente with a It is trivial to repeat the analysis for a scenario with a different prior.

Figure [2](#page-7-1) shows the asymmetries as functions of  $q^2$  in the SM for  $B \to D\tau\nu$  and  $B \to D^*\tau\nu$ , using hadronic form factors of Ref. [\[24\]](#page-16-0). In addition to the SM predictions, we also show the predictions from two benchmark NP scenarios, which are discussed in detail in Sec. [IV C.](#page-10-0)

The values of the integrated asymmetries in the SM are displayed in Table [I,](#page-10-1) along with the projected statistical

<span id="page-10-1"></span>TABLE I. Numerical predictions of the integrated observables in the SM, together with their theoretical uncertainties  $\sigma_{th}$  and the estimated statistical uncertainties in the  $\pi$  and  $\rho$  channels,  $\sigma_{\pi}$  and  $\sigma_{\rho}$ . The theoretical uncertainties are obtained by scanning theoretical inputs as in Ref. [\[24\].](#page-16-0) The statistical uncertainties assume a dataset of  $N = 3000$  events for each final state. Both the theoretical and statistical uncertainties refer to the 68% confidence level.

		<b>SM</b>	$\sigma_{\text{th}}$	$\sigma_{\pi}$	$\sigma_{\rho}$	Measured
$B \to D \tau \nu$	$A_{\text{FB}}$	$-0.359$	0.003	0.020	0.024	$\cdots$
	$P_L$	0.34	0.03	0.029	0.069	$\cdots$
	$P_{\perp}$	$-0.839$	0.007	0.028	0.094	$\cdot$ $\cdot$ $\cdot$
	$Z_\perp$	0.224	0.012	0.024	0.091	$\cdots$
	$Z_Q$	0.243	0.012	0.037	0.118	$\cdots$
	$A_Q$	$-0.088$	0.004	0.031	0.042	$\cdots$
$B \to D^* \tau \nu$	$A_{\text{FB}}$	0.07	0.02	0.031	0.037	$\cdots$
	$P_L$	$-0.50$	0.02	0.029	0.070	$-0.38(54)$ [14,15]
	$P_{\perp}$	$-0.49$	0.02	0.039	0.113	$\cdots$
	$Z_L$	$-0.323$	0.007	0.037	0.104	$\cdots$
	$Z_{\perp}$	0.054	0.002	0.041	0.101	.
	$Z_Q$	0.058	0.002	0.055	0.046	$\cdots$
	$A_Q$	$-0.0189$	0.0005	0.146	0.050	$\cdots$

sensitivities for  $N = 3000$  total events in each final-state  $\pi$ or  $\rho$ <sup>5</sup>. Figs. [3](#page-8-0) and [4](#page-9-0) visualize these numbers and provide the correlation between each asymmetry pair. The achievable sensitivities for these observables are at the percent level, comparable to the projected sensitivity to  $R_{D^{(*)}}$  [\[57\]](#page-16-8).

Interestingly, Table [I](#page-10-1) suggests that the new observables  $Z_L$ ,  $Z_{\perp}$ ,  $Z_{\cdot}$ ,  $A_{\cdot}$  could be measured with comparable precision to the previously studied observables  $P_L$ ,  $P_{\perp}$ , and  $A_{FB}$ . We also find that the sensitivities to the asymmetries are comparable in both  $B \to D\tau \nu$  and  $B \to D^* \tau \nu$ decays. However, there is a stark difference between  $\pi$  and  $ρ$ : for all the observables, the  $τ → πν$  channel has a better sensitivity compared to the  $\tau \to \rho \nu$  channel. Measuring the  $\rho$  polarizations would presumably enhance the sensitivity in the latter channel.

Of all the asymmetries in Table [I,](#page-10-1) only  $P_L$  for  $B \to D^* \tau \nu$ has been measured so far. The projected statistical uncertainty (obtained by rescaling the current measurement with luminosity) is  $\pm 0.06$ —see Table 50 in Ref. [\[57\]](#page-16-8)—this is in the same ballpark as our projection in Table [I.](#page-10-1) The difference may be attributable in part to the background effects we have neglected, as well as detector acceptance and efficiency. Nonetheless, the fact that our purely theoretical estimate of the sensitivity is within a factor of 2 of the official projection provides some confidence in the sensitivity estimates for the other observables.

#### C. New physics in  $b \to c\tau\nu$

<span id="page-10-0"></span>Heavy new physics at scales  $\Lambda \gg m_W$  can modify the total rates and kinematic distributions of the  $\tau$  lepton and

<span id="page-10-2"></span>the  $D^{(*)}$  meson in the  $B \to D^{(*)}\tau\nu$  decays. Such modifications can be parametrized in a model-independent way in terms of an effective Hamiltonian

$$
\mathcal{H}_{\text{eff}} = \frac{4G_F V_{cb}}{\sqrt{2}} \left( O_{LL}^V + \sum_{X,Y=L,R} (C_{XY}^S O_{XY}^S + C_{XY}^V O_{XY}^V) + \sum_{X=L,R} C_{XX}^T O_{XX}^T \right),
$$
\n(4.8)

where  $G_F = 1/\sqrt{2}v^2$  and  $V_{cb}$  is the CKM element. The various effective operators describe local scalar vector and various effective operators describe local scalar, vector, and tensor four-fermion interactions, defined as

$$
O_{XY}^{S} = (\bar{c}P_{X}b)(\bar{\tau}P_{Y}\nu),
$$
  
\n
$$
O_{XY}^{V} = (\bar{c}\gamma^{\mu}P_{X}b)(\bar{\tau}\gamma_{\mu}P_{Y}\nu),
$$
  
\n
$$
O_{XX}^{T} = (\bar{c}\sigma^{\mu\nu}P_{X}b)(\bar{\tau}\sigma_{\mu\nu}P_{X}\nu).
$$
\n(4.9)

The Wilson coefficients  $C_{XY}^i$  in Eq. [\(4.8\)](#page-10-2) contain information pertaining to the short-distance structure of the  $b \rightarrow$  $c\tau\nu$  transitions induced by new physics above the weak scale. In our conventions, the SM corresponds to  $C_{XY}^i = 0$ .<br>A given NP model induces specific modifications of the A given NP model induces specific modifications of the Wilson coefficients that can be analyzed by measuring various observables in these decays. We neglect corrections of  $\mathcal{O}(v/\Lambda)$  that arise from higher-dimensional operators in the effective theory.

As we discussed in the Introduction, current measurements of total rates in terms of the ratios  $R_{D^{(*)}}$  are in tension with the SM at a significance of about  $3\sigma$ , which could be due to the presence of new physics in  $b \to c\tau\nu$ transitions. Several models have been proposed that can explain this difference [\[55,58](#page-16-9)–102]. One class of models particularly favored by data involve a vector leptoquark  $U_1$ 

<sup>&</sup>lt;sup>5</sup>The number  $N = 3000$  is meant to be a *very* rough estimate of  $R \rightarrow D^{(*)}\tau (\rightarrow d\tau)$  events expected with 50 ab<sup>-1</sup> the number of  $B \to D^{(*)}\tau (\to d\nu)\nu$  events expected with 50 ab<sup>-1</sup> of Belle II data [26.56]. of Belle II data [\[26,56\]](#page-16-1).

<span id="page-11-1"></span>

FIG. 5. Theoretical (blue bands) and statistical (black bars) uncertainties on the asymmetries at the 68% confidence level for  $B \to D\tau\nu$ (left) and  $B \to D^* \tau \nu$  (right). The statistical uncertainties correspond to the  $\tau \to \pi \nu$  channel, assuming 3000 events. The deviations of the central values for the NP scenarios  $U_1$  (yellow square) and  $S_1 - R_2$  (green diamond) from the SM central values are also shown.

transforming as  $(3, 1, +2/3)$  under the SM gauge group  $SU(3) \times SU(2) \times U(1)$ . The exchange of such a leptoquark induces  $b \rightarrow c\tau\nu$  transitions at tree level and generates the operators  $O_{LL}^V$  and  $O_{RL}^S$  [61–[77\].](#page-17-0) Another possibility are the scalar leptoquarks  $S_1$ :  $(\bar{3}, 1, +1/3)$  and  $R_2$ :  $(3, 2, +7/6)$  which produce a correlated effect in the  $R_2$ ∶(3, 2, +7/6), which produce a correlated effect in the scalar and tensor operators  $O_{LL}^S$  and  $O_{LL}^T$  [\[55,78](#page-16-9)–83].<sup>6</sup>

We use these two models to demonstrate the sensitivity of our asymmetries to new physics. Our benchmarks correspond to

"U<sub>1</sub> vector leptoquark": 
$$
C_{LL}^V = 0.08
$$
,  $C_{RL}^S = -0.05$ ,  
"S<sub>1</sub> - R<sub>2</sub>scalar leptoquarks":  $C_{LL}^S = 0.07$ ,  $C_{LL}^T = -0.03$ ,  
(4.10)

where the Wilson coefficients are evaluated at the bottomquark mass scale. Both benchmarks are motivated by a fit to the current  $R_D$  and  $R_{D^*}$  measurements [\[49\].](#page-16-10)

In Fig. [2](#page-7-1), we show the  $q^2$  dependence of all the asymmetry observables in the  $U_1$  (dashed) and the  $S_1 - R_2$  (dotted) leptoquark scenarios. We also show the predictions of the  $q^2$ -inclusive observables in these models in Figs. [3](#page-8-0) and [4](#page-9-0) as yellow squares and green diamonds, respectively. We have not included the expected confidence regions around the NP points, but we have checked that the statistical sensitivities are nearly indistinguishable in size and shape from the SM ellipses. Finally, in Fig. [5,](#page-11-1) we show the  $q^2$ -integrated results of the observables, including both the theoretical and statistical uncertainties for the SM predictions [\[24\].](#page-16-0)<sup>7</sup>

As can be seen from the figures, in the  $U_1$  leptoquark scenario, most of the observables are very similar to the SM. Only  $P_L$  in  $B \to D\tau \nu$  causes an appreciable deviation from the SM prediction. The reason is that the vector leptoquark primarily induces the operator  $O_{LL}^V$ . This effect merely changes the overall normalization of the decay rate in the SM and cancels out in the normalized asymmetry observables. Any observable effect of the  $U_1$  leptoquark is due to the small scalar contribution to  $O_{RL}^S$ , which  $P_L$  is especially sensitive to. On the other hand, in the scalar leptoquark scenario the deviation from the SM is quite significant for many of the observables. This scenario involves a combination of scalar and tensor operators, which significantly affect the angular distributions in the  $b \rightarrow c \tau \nu$  decay.

All in all, we conclude from Fig. [5](#page-11-1) that the most promising single observables for distinguishing between these two NP scenarios are  $P_L(D)$ ,  $P_{\perp}(D^*)$ , and  $Z_L(D^*)$ .<br>At the same time, no single observable presents a "slam At the same time, no single observable presents a "slam dunk" case for one NP scenario or the other; differences are at  $1\sigma$ - $2\sigma$  at best. However, Fig. [5](#page-11-1) and Figs. 3-4 indicate that the combination of multiple observables offers a way to achieve higher sensitivity. This emphasizes the potential of a simultaneous measurement of all of these observables to clarify the nature of the currently observed discrepancies.

#### V. DISCUSSION AND CONCLUSION

<span id="page-11-0"></span>The study of  $B \to D^{(*)}\tau\nu$  transitions offers a unique window into couplings between quarks and leptons involving the third generation. In this work, we have shown how to extract the maximum information about the  $b \rightarrow c\tau\nu$ transition from kinematic distributions of the observable particles in  $B \to D^{(*)}\tau (\to \pi \nu, \rho \nu) \nu$  decays. The physics of  $B \to D^{(*)}\tau\nu$  decays with polarized  $\tau$  leptons and unpolarized  $D^{(*)}$  mesons beyond total rates can be fully captured by nine coefficient functions in a partial wave expansion. Linear combinations of some of these functions correspond to widely studied  $\tau$  observables, such as the longitudinal

<sup>&</sup>lt;sup>6</sup>Other models involving colorless gauge bosons  $W'$  [84–[89\],](#page-17-1) extending the Higgs sector [90–[95\],](#page-17-2) or adding right-handed neutrinos [96–[100\]](#page-17-3) could explain the discrepancy, but they are more in tension with other low-energy observables or collider searches [103-[105\].](#page-18-0)

Figure [5](#page-11-1) indicates that the theoretical uncertainties on the observables are always comparable to or smaller than the statistical uncertainties. This further motivates performing the measurement at Belle II, as the precision will not be theoretically limited.

polarization asymmetry  $P_L$  and the forward-backward asymmetry  $A_{FB}$ . We showed that seven of the nine coefficient functions can be recovered from the kinematic distributions of the observable particles  $D^{(*)}$  and  $\pi$ ,  $\rho$ . The remaining two functions are sensitive to CP violation and can only be extracted by including additional information, for instance from the  $D^{(*)}$  decay [\[30\]](#page-16-3). We leave such a study for future work [\[50\]](#page-16-4).

A similar analysis has previously been performed for a subset of the asymmetries in  $B \to D\tau\nu$  [\[26\].](#page-16-1) In this work, we generalized this analysis to include  $B \to D^{(*)}\tau\nu$  and developed a common framework to describe both processes. Using this framework, we discovered four new asymmetries,  $Z_L$ ,  $Z_{\perp}$ ,  $Z_Q$ , and  $A_Q$ . These observables probe independent fundamental properties of  $b \rightarrow c\tau\nu$ transitions and can also be extracted from the observable kinematic distributions, which previously had not been realized.

To assess the potential of the Belle II experiment to measure the seven asymmetries, we have performed a statistical analysis assuming the full dataset of 50  $ab^{-1}$ . Our unbinned maximum-likelihood fit to the fully differential final-state distribution in  $B \to D^{(*)}\tau(\to \pi \nu, \rho \nu) \nu$  decays<br>shows that almost all asymmetries could be accessed with shows that almost all asymmetries could be accessed with a statistical uncertainty of a few percent. These predictions do not include realistic experimental effects such as detector acceptance/efficiency/smearing, backgrounds, or systematic uncertainties—see, e.g., Ref. [\[29\]](#page-16-11) for further discussion. It would be interesting to further our study by taking these issues into account.

Additional sensitivity can be obtained by combining the  $\tau \to \pi \nu$  and  $\tau \to \rho \nu$  channels with each other and with the leptonic decay modes  $\tau \to \ell \nu \nu$ . While the lepton kinematics do not contain as much information about the asymmetries as the  $\pi$  or  $\rho$ , the leptonic decays occur at a higher rate and should be included in a global analysis of all  $\tau$ -decay modes.

These positive measurement prospects and the precise predictions of the asymmetries in the SM allow us to detect possible deviations in the presence of heavy new physics. For two new physics scenarios with scalar and vector leptoquarks, motivated by the currently observed deviations in  $B \to D^{(*)}\tau\nu$  decays, we have determined the statistical sensitivity compared to the SM expectations. In  $B \to D\tau \nu$ , the longitudinal  $\tau$  polarization asymmetry  $P_L$ discriminates particularly well between the two NP models; in  $B \to D^* \tau \nu$  the perpendicular polarization asymmetry  $P_{\perp}$ and the double asymmetry  $Z_L$  show the best individual discriminating power. Of course, the ability to discriminate between different NP models increases by combining all seven asymmetries in a global fit.

In this paper, we have endeavored to demonstrate the usefulness of the asymmetries in  $B \to D^{(*)}\tau\nu$  decays and the feasibility of measuring them at Belle II. The asymmetries furnish an important intermediate step between the raw data and the underlying Lagrangian parameters, e.g., the Wilson coefficients. The framework developed in this paper provides us with a solid interpretation scheme for  $\tau$ polarimetry in  $B \to D^{(*)}\tau\nu$  decays, ready to be confronted with fresh data at Belle II.

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### <span id="page-12-0"></span>APPENDIX A: ANGULAR INTEGRALS

<span id="page-12-2"></span>In this Appendix, we give details about the integration over angles that are not observable in the final state. Using the angular expansions of Eqs. [\(2.8\)](#page-3-2) and [\(3.9\),](#page-5-4) the angular integrals in Eq. [\(3.11\)](#page-5-5) are found to be of the form

$$
u(\cos \theta_d) = \int_{-1}^1 d \cos \theta_\tau \int_{-\pi}^\pi d\zeta f(\zeta) g(\cos \theta_\tau)
$$
  
 
$$
\times \delta(\cos \theta_\tau \cos \varphi + \sin \theta_\tau \sin \varphi \cos \zeta - \cos \theta_d).
$$
 (A1)

<span id="page-12-1"></span>If f is an odd function of  $\zeta$ , the integral vanishes. This is the reason why  $P_T$  and  $Z_T$ , which are proportional to sin  $\zeta$  in the total decay rate, vanish. Changing variables from  $\zeta$  to cos ζ, it is straightforward to calculate

$$
2\int_{-\pi}^{0} d\zeta f(\zeta) \delta(\cos\theta_{\tau}\cos\varphi - \sin\theta_{\tau}\sin\varphi\cos\zeta - \cos\theta_{d})
$$
  
= 
$$
2\int_{-1}^{1} d\cos\zeta f(\cos\zeta) \frac{1}{\sqrt{1-\cos^{2}\zeta}} \frac{1}{|\sin\theta_{\tau}\sin\varphi|}
$$
  

$$
\times \delta(\cos\zeta - \cos\zeta_{0})
$$
  
= 
$$
2|\det \mathbf{J}|f(\cos\zeta_{0}),
$$
 (A2)

where

$$
\cos \zeta_0 = \frac{\cos \theta_d - \cos \theta_\tau \cos \varphi}{\sin \theta_\tau \sin \varphi}, \tag{A3}
$$

and the Jacobian is given by

$$
|\det \mathbf{J}| = (1 - \cos^2 \theta_d - \cos^2 \theta_r - \cos^2 \varphi + 2 \cos \theta_d \cos \theta_r \cos \varphi)^{-1/2}.
$$
 (A4)

After integrating over  $\zeta$ , the delta function in Eq. [\(A2\)](#page-12-1) restricts the possible range of  $\theta_{\tau}$ . Solving Eq. [\(3.4\)](#page-4-1) for  $\cos \theta_{\tau}$  and inserting the  $\zeta$  integration limits gives

$$
\cos \theta_{\tau}|_{\zeta=0} = \cos(\theta_d \mp \varphi), \qquad \cos \theta_{\tau}|_{\zeta=\pm \pi} = \cos(\theta_d \pm \varphi).
$$
\n(A5)

The choice of sign configuration does not matter, since the other configuration can be obtained by sending  $\varphi \rightarrow -\varphi$ ; this angle is only defined in terms of cos  $\varphi$ . Choosing  $\varphi \ge 0$  and  $\cos(\theta_d + \varphi)$  as the lower integration limit gives

$$
u(\cos \theta_d) = \int_{-1}^{1} d \cos \theta_{\tau} g(\cos \theta_{\tau}) \int_{-\pi}^{\pi} d\zeta f(\zeta)
$$
  
 
$$
\times \delta(\cos \theta_{\tau} \cos \varphi - \sin \theta_{\tau} \sin \varphi \cos \zeta - \cos \theta_{d})
$$
  

$$
= 2 \int_{\cos(\theta_d + \varphi)}^{\cos(\theta_d - \varphi)} d \cos \theta_{\tau} |\det \mathbf{J}| f(\cos \zeta_{0}) g(\cos \theta_{\tau}).
$$
  
(A6)

The procedure above is equivalent to the change of variables in Ref. [\[24\].](#page-16-0) The resulting functions  $u(\cos \theta_d)$ 

<span id="page-13-1"></span>TABLE II. Angular integrals from Eq. [\(A1\)](#page-12-2).

$u(\cos\theta_d)$
$2\pi$
$2\pi \cos \theta_d \cos \varphi$
$2\pi(\cos^2\theta_d\cos^2\varphi+\frac{1}{2}\sin^2\theta_d\sin^2\varphi)$
$2\pi \cos \theta_d \sin \varphi$
$\pi$ sin $\varphi$ cos $\varphi$ (3 cos <sup>2</sup> $\theta_d$ – 1)
$\left( \right)$

for all functions  $f(\zeta)g(\cos\theta_\tau)$  present in the full decay rate are listed in Table [II](#page-13-1).

### <span id="page-13-0"></span>APPENDIX B: ANALYTICAL EXPRESSIONS FOR THE NEW ASYMMETRIES

In this Appendix, we report the analytic expressions for all new asymmetries introduced in Sec. [II](#page-2-2)—i.e.,  $Z_L$ ,  $Z_{\perp}$ ,  $Z_T$ ,  $A_O$ , and  $Z_O$ . Similar formulas for the remaining asymmetries can be found in the Appendix of Ref. [\[27\].](#page-16-6)<sup>8</sup> In  $B \to D\tau \nu$ , the asymmetries are

$$
Z_L(q^2) = A_{FB}(q^2),
$$
  
\n
$$
\frac{d\Gamma}{dq^2} Z_{\perp}(q^2) = \mathcal{N}(m_D, q^2) \text{Re}[\Xi],
$$
  
\n
$$
\frac{d\Gamma}{dq^2} Z_T(q^2) = -\mathcal{N}(m_D, q^2) \text{Im}[\Xi],
$$
 (B1)

with

$$
\Xi = \left( (1 + C_{LL}^V + C_{RL}^V) \sqrt{q^2} H_{V,0}^s - 4C_{LL}^T m_{\tau} H_T^s \right) \left( (1 + C_{LL}^V + C_{RL}^V)^* m_{\tau} H_{V,0}^s - 4C_{LL}^T \sqrt{q^2} H_T^s \right),
$$
  

$$
\mathcal{N}(m_D, q^2) = \frac{G_F^2 V_{cb}^2}{192 m_B^3 \pi^3} \sqrt{((m_B - m_D)^2 - q^2)((m_B + m_D)^2 - q^2)} \left( 1 - \frac{m_{\tau}^2}{q^2} \right)^2,
$$
 (B2)

where  $C_{YZ}^X$  refer to the Wilson coefficients of the relevant dimension-6 operators; see Eq. [\(4.8\).](#page-10-2) The hadronic functions H can be found in Refs. [\[27,55\].](#page-16-6)

The quadrupole observables for the same decay are given as

$$
\frac{d\Gamma}{dq^2}A_Q(q^2) = \frac{\mathcal{N}(m_D, q^2)}{2} \left\{ \left| (1 + C_{LL}^V + C_{RL}^V)m_\tau H_{V,0}^s - 4C_{LL}^T \sqrt{q^2} H_T^s \right|^2 - \left| (1 + C_{LL}^V + C_{RL}^V) \sqrt{q^2} H_{V,0}^s - 4C_{LL}^T m_\tau H_T^s \right|^2 \right\},\tag{B3}
$$

<sup>&</sup>lt;sup>8</sup>What we call  $\frac{d\Gamma}{dq^2}O(q^2)$  in this work corresponds to  $\frac{dO}{dq^2}$  in Ref. [\[27\]](#page-16-6).

$$
\frac{d\Gamma}{dq^2} Z_Q(q^2) = \frac{\mathcal{N}(m_D, q^2)}{2} \left\{ \left| (1 + C_{LL}^V + C_{RL}^V) m_\tau H_{V,0}^s - 4C_{LL}^T \sqrt{q^2} H_T^s \right|^2 \right. \\ \left. + \left| (1 + C_{LL}^V + C_{RL}^V) \sqrt{q^2} H_{V,0}^s - 4C_{LL}^T m_\tau H_T^s \right|^2 \right\} . \tag{B4}
$$

Similarly, for  $B \to D^* \tau \nu$ , the asymmetries are given by

$$
\frac{d\Gamma}{dq^2} Z_L(q^2) = \frac{4\mathcal{N}(m_{D^*}, q^2)}{3} \text{Re} \Big\{ 2 \Big( (C_{RL}^S - C_{LL}^S) \sqrt{q^2} H_S + (1 + C_{LL}^V - C_{RL}^V) m_{\tau} H_{V,t} \Big) \times \Big( -(1 + C_{LL}^V - C_{RL}^V)^* m_{\tau} H_{V,0} + 4C_{LL}^T \sqrt{q^2} H_{T,0} \Big) \Big\} - \Big( (1 + C_{LL}^V - C_{RL}^V) \sqrt{q^2} (H_{V,-} + H_{V,+}) + 4C_{LL}^T m_{\tau} (H_{T,-} - H_{T,+}) \Big) \times \Big( (1 + C_{LL}^V + C_{RL}^V)^* \sqrt{q^2} (H_{V,-} - H_{V,+}) + 4C_{LL}^T^* m_{\tau} (H_{T,-} + H_{T,+}) \Big) \Big\},\n\frac{d\Gamma}{dq^2} Z_{\perp}(q^2) = -\frac{\mathcal{N}(m_{D^*}, q^2)}{2} \text{Re} [\Xi^*],\n\frac{d\Gamma}{dq^2} Z_T(q^2) = \frac{\mathcal{N}(m_{D^*}, q^2)}{2} \text{Im} [\Xi^*],
$$
\n(B5)

where

$$
\begin{split}\n\Xi^* &= \Big\{ (|1 + C_{LL}^V|^2 + |C_{RL}^V|^2) m_\tau \sqrt{q^2} (H_{V,+}^2 + H_{V,-}^2) \\
&- 2|1 + C_{LL}^V - C_{RL}^V|^2 m_\tau \sqrt{q^2} H_{V,0}^2 + 16|C_{LL}^T|^2 m_\tau \sqrt{q^2} (H_{T,-}^2 + H_{T,+}^2 - 2H_{T,0}^2) \\
&+ 8((1 + C_{LL}^V - C_{RL}^V) C_{LL}^T \cdot q^2 + (1 + C_{LL}^V - C_{RL}^V)^* C_{LL}^T m_\tau^2) H_{V,0} H_{T,0} \\
&- 4H_{V,+}((C_{RL}^V C_{LL}^T \cdot q^2 + C_{RL}^V)^* C_{LL}^T m_\tau^2) H_{T,-} + ((1 + C_{LL}^V) C_{LL}^T \cdot q^2 + C_{LL}^T (1 + C_{LL}^V)^* m_\tau^2) H_{T,+}) \\
&+ 2H_{V,-} \Big( -2\text{Re}[(1 + C_{LL}^V)^* C_{RL}^V] m_\tau \sqrt{q^2} H_{V,+} + 2(1 + C_{LL}^V)^* C_{LL}^T m_\tau^2 H_{T,-} \\
&+ 2C_{RL}^V \cdot C_{LL}^T m_\tau^2 H_{T,+} + 2(1 + C_{LL}^V) C_{LL}^T \cdot q^2 H_{T,-} + 2C_{RL}^V C_{LL}^T \cdot q^2 H_{T,+}) \Big\},\n\end{split} \tag{B6}
$$

while the quadrupole observables  $A_Q$  and  $Z_Q$  are

$$
\frac{d\Gamma}{dq^2}A_Q(q^2) = -\frac{\mathcal{N}(m_{D^*}, q^2)}{4}\Big\{ (|1 + C_{LL}^V|^2 + |C_{RL}^V|^2)m_\tau^2(H_{V,-}^2 + H_{V,+}^2) - 2|1 + C_{LL}^V - C_{RL}^V|^2m_\tau^2H_{V,0}^2 + 16|C_{LL}^T|^2q^2(H_{T,-}^2 - 2H_{T,0}^2 + H_{T,+}^2) + 4m_\tau H_{V,-}\text{Re}\Big[-(1 + C_{LL}^V)C_{RL}^{V*}m_\tau H_{V,+} + 2C_{LL}^T\sqrt{q^2}((1 + C_{LL}^V)^*H_{T,-} + C_{RL}^V^*H_{T,+})\Big] - 8m_\tau\sqrt{q^2}H_{V,+}(\text{Re}[C_{LL}^T C_{RL}^{V*}]H_{T,-} + \text{Re}[C_{LL}^T(1 + C_{LL}^V)^*]H_{T,+}) + 16\text{Re}[C_{LL}^T(1 + C_{LL}^V - C_{RL}^V)^*]m_\tau\sqrt{q^2}H_{V,0}H_{T,0} - |\sqrt{q^2}((1 + C_{LL}^V)H_{V,-} - C_{RL}^V H_{V,+}) + 4C_{LL}^Tm_\tau H_{T,-}|^2 + 2|\sqrt{q^2}(1 + C_{LL}^V - C_{RL}^V)H_{V,0} - 4C_{LL}^Tm_\tau H_{T,0}|^2 - |\sqrt{q^2}(C_{RL}^V H_{V,-} - (1 + C_{LL}^V)H_{V,+}) + 4C_{LL}^Tm_\tau H_{T,+}|^2 \Big\},
$$
\n(B7)

$$
\frac{d\Gamma}{dq^2} Z_Q(q^2) = -\frac{\mathcal{N}(m_{D^*}, q^2)}{4} \Big\{ (|1 + C_{LL}^V|^2 + |C_{RL}^V|^2) m_\tau^2 (H_{V,-}^2 + H_{V,+}^2) - 2|1 + C_{LL}^V - C_{RL}^V|^2 m_\tau^2 H_{V,0}^2 + 16|C_{LL}^T|^2 q^2 (H_{T,-}^2 - 2H_{T,0}^2 + H_{T,+}^2) + 4m_\tau H_{V,-} \text{Re}\Big[-(1 + C_{LL}^V) C_{RL}^V * m_\tau H_{V,+} + 2C_{LL}^T \sqrt{q^2} ((1 + C_{LL}^V)^* H_{T,-} + C_{RL}^V * H_{T,+})\Big] \n- 8m_\tau \sqrt{q^2} H_{V,+} (\text{Re}[C_{LL}^T C_{RL}^V^*] H_{T,-} + \text{Re}[C_{LL}^T (1 + C_{LL}^V)^*] H_{T,+}) \n+ 16 \text{Re}[C_{LL}^T (1 + C_{LL}^V - C_{RL}^V)^*] m_\tau \sqrt{q^2} H_{V,0} H_{T,0} \n+ |\sqrt{q^2} ((1 + C_{LL}^V) H_{V,-} - C_{RL}^V H_{V,+}) + 4C_{LL}^T m_\tau H_{T,-}|^2 \n- 2 |\sqrt{q^2} (1 + C_{LL}^V - C_{RL}^V) H_{V,0} - 4C_{LL}^T m_\tau H_{T,0}|^2 \n+ |\sqrt{q^2} (C_{RL}^V H_{V,-} - (1 + C_{LL}^V) H_{V,+}) + 4C_{LL}^T m_\tau H_{T,+}|^2 \Big\}.
$$
\n(B8)

The hadronic functions H are pure functions of  $q^2$  and contain the hadronic matrix elements. All theory uncertainties are therefore contained in these functions.

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