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Associative Recall Properties of the Trion Model of Cortical Organization

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Abstract. We developed a cooperative model of the cortical column incorporating an idealized subunit, the trion (which represents a localized group of neurons), and a discrete time step for firing. We found that networks composed of a small number of trions (with symmetric interactions) supported up to thousands of quasi-stable, periodic firing patterns (MPs) which could be selected out with only small changes in interaction strengths using a Hebb-type algorithm. Here we report a study of the associative recall properties showing striking features: By considering all possible initial firing patterns (for a given set of network connections), we find 1) It takes on the average only 2–5 time steps to recall an MP. 2) Many of the MPs can be individually accessed by thousands of different initial patterns. The variety of examples presented illustrate the rich, general nature of the model.

One of the most important problems in the theoretical studies of memory is to investigate the retrieval of information. [See, e.g., (Hinton and Anderson 1981) and the references in the review article (Kohonen et al. 1981).] The associative recall properties of any neuronal memory model are of paramount interest. Although a particular model might be able to encode or store many “pieces of information” we believe that two crucial properties of associative retrieval should also be present: 1) Rapid recall of the information and 2) access of the information from *many* different stimuli. Both of these properties are present in human memory retrieval as contrasted to the *usual* retrieval of information in the digital computer. (Unless specially programmed, the recall of information in the computer is 1) searched for serially and 2) accessed via very specific cues.) The purpose of this paper is to report the results of a study of the associative recall properties of

the trion model. Motivated by Mountcastle’s organizational principle for neocortical function (Mountcastle 1978) and by Fisher’s model of physical spin systems (Fisher and Selke 1980, 1981), we (Shaw et al. 1985) developed a cooperative model of the cortical column incorporating i) an *idealized* subunit, the trion, which represents a localized group of neurons (~ 30 –100), and ii) a discrete time step for firing (~ 30 –100 ms). We found that networks comprised of a small number of trions (with symmetric interactions) supported up to thousands of quasi-stable, periodic firing patterns (*denoted* as MPs) which could be selected out [as in the selection principle of Edelman (1978)] using a Hebb-type algorithm for synaptic change (Hebb 1949). In the present study of the recall properties, (for a given set of network connections) by considering all possible initial firing patterns, we find 1) It takes on the average only 2–5 time steps for any initial pattern to project onto or recall an MP. 2) Many of the MPs can be individually accessed by *thousands* of different initial patterns. We present a variety of interesting examples for different couplings among the trions, illustrating the rich, general nature of the trion model. For example, we find (see Tables 1 and 2) MPs having cycle length of 18 time steps which are especially easy to recall by a huge number of initial states. We believe that these phenomena are of interest to fields of neurophysiology, cellular automata (Wolfram 1983) and molecular scale processors (Yates 1984), as possibly applied to a future generation of computers.

Despite the substantial theoretical efforts and results in modeling neural networks (see, e.g., references in MacGregor and Lewis 1977; Amari and Arbib 1982; Prisco 1984) the basis for the tremendous *magnitudes* of the processing capabilities and the memory storage capacities of mammals remain mysteries. We believe Mountcastle’s (1978) columnar organizing principle for the functioning of the neocortex will provide a basis for these phenomena and we

Table 2. Same as Table 1

| Interactions | | | | Number of MPs: 39 | | | | | | | |
|--------------------------|-------|-------------|-------|---------------------------------------|--------|-------------|--------|-------------|-------|-------------|-------|
| $V: -1 \ 1 \ -1 \ 0 \ 0$ | | | | | | | | | | | |
| $W: 0 \ 1 \ -1 \ 1 \ 0$ | | | | | | | | | | | |
| Number of triggers: 81% | | | | Avg. no. of timesteps to trigger: 3.4 | | | | | | | |
| 1 | 455 | 2 | 728 | 3 | 1375 | 4 | 41328 | 5 | 41329 | 6 | 74056 |
| 300 | | 2996 | | 1464 | | 69228 | | 228756 | | 31068 | |
| + + + + + + | | + + + + + + | | ○ + + + + + | | - - + - - + | | ○ - + - - + | | ○ ○ + - + ○ | |
| - - - - - - | | - - - - - - | | ○ - - - - - | | + - - + - - | | + - - + - - | | + - + - ○ - | |
| ○ + ○ + ○ + | | | | + + + + + ○ | | ○ + - ○ + - | | - + - ○ + - | | - + - + - + | |
| ○ - ○ - ○ - | | | | - ○ - - - ○ | | - + + - + + | | - ○ + - + + | | ○ ○ ○ - + - | |
| + + + + + + | | | | + ○ + + + + | | + - + + - + | | + - + + - + | | + - + - + ○ | |
| - ○ - ○ - ○ | | | | ○ - - - - - | | + ○ - + ○ - | | + + - + ○ - | | - + - + - + | |
| | | | | ○ + ○ + + + | | - + - - + - | | - + ○ - + - | | + ○ ○ ○ + - | |
| | | | | - - ○ - - - | | - - + - - + | | - - + - - + | | ○ - + - + - | |
| | | | | + ○ + + + + | | + - ○ + - ○ | | + - - + - ○ | | - + - + - + | |
| | | | | - ○ - ○ - - | | + + - + + - | | + + - ○ + - | | + - ○ ○ ○ - | |
| | | | | + + + ○ + + | | - + + - + + | | - + + - + + | | + ○ + - + - | |
| | | | | - - ○ - - - | | ○ - + ○ - + | | ○ - + + - + | | - + - + - + | |
| | | | | + + ○ + ○ + | | + - - + - - | | + - - + ○ - | | + - + ○ ○ ○ | |
| | | | | - - - - ○ - | | - + - - + - | | - + - - + - | | + - ○ - + - | |
| | | | | + + + ○ + + | | - ○ + - ○ + | | - ○ + - - + | | - + - + - + | |
| | | | | - - - ○ - ○ | | + - + + - + | | + - + + - ○ | | ○ - + - ○ ○ | |
| | | | | + + + + + ○ | | + + - + + - | | + + - + + - | | + - + ○ + - | |
| | | | | - - - - ○ - | | - + ○ - + ○ | | - + ○ - + + | | - + - + - + | |
| 7 | 74175 | 8 | 93736 | 9 | 133042 | 10 | 265720 | | | | |
| 21804 | | 13452 | | 59424 | | 49 | | | | | |
| - + - + - + | | ○ - + - + ○ | | ○ ○ ○ ○ ○ ○ | | ○ ○ ○ ○ ○ ○ | | | | | |
| + - + - ○ - | | + - + ○ ○ - | | + - + - + - | | | | | | | |
| + ○ ○ ○ + - | | - + - + - + | | - + - + - + | | | | | | | |
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| ○ ○ ○ - + - | | - + - + - + | | | | | | | | | |

construct the trion model based on it. Following Mountcastle (1978), we consider the cortical column (roughly 500 microns in diameter) to be the basic network in the cortex which is comprised of small irreducible processing subunits (trions). These subunits are connected into columns or networks having the capability of complex spatial-temporal firing patterns. The creation and transformation of such patterns constitute the basic events of short-term memory and information processing. We strongly emphasize this *assumption*: that *higher*, complex mammalian cortical processes involve complex *spatial-temporal* network

firing patterns; this is in contrast to the usual assumption that the "coding" only involves sets of neurons firing with high frequency. We are *not* suggesting that average firing is not important or that it is not a communication code. In fact, we presume that there are several codes in the central nervous system for communication among various regions with the sophistication of the code being related to the sophistication of the information processing involved *and* to the urgency of the information. For example, the sensing of perilous information *must* be responded to immediately and presumably would involve a simple alerting

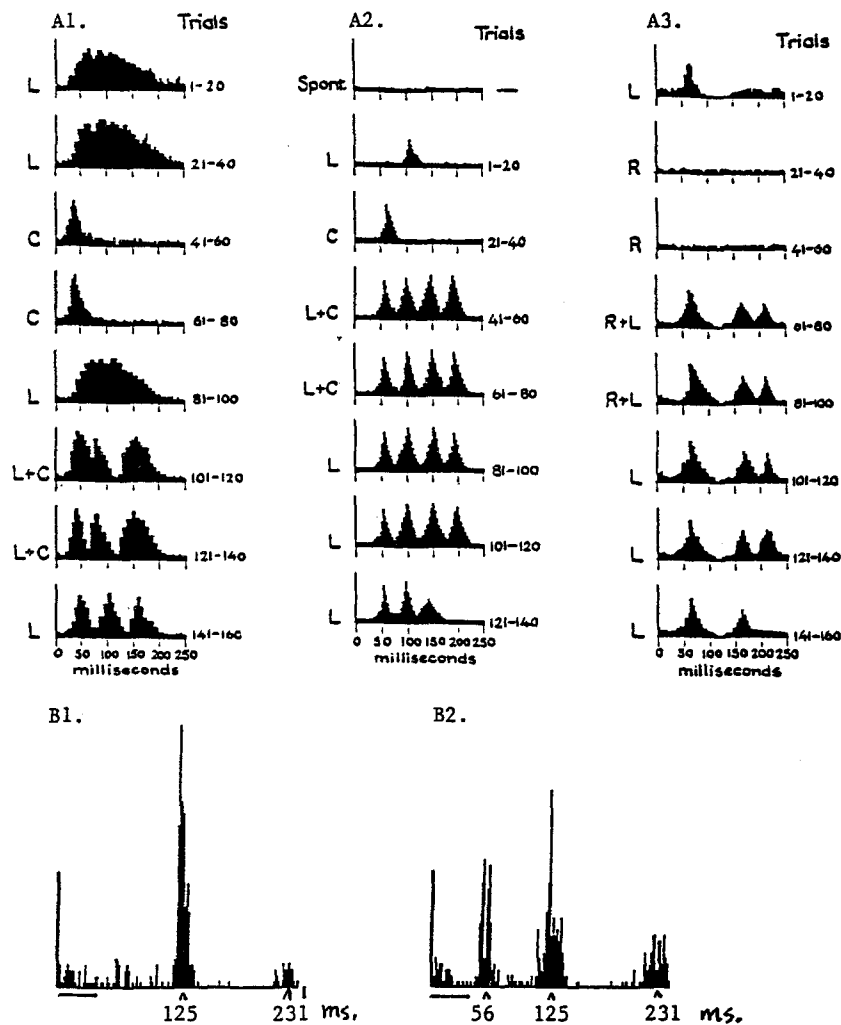


Fig. 1A and B. Single-unit data from visual area III of cat from the published work of Morrell (1967) and Morrell et al. (1983). A1, A2, and A3 are derived from Figs. 11, 14, and 12 respectively of Morrell (1967). B1 and B2 are derived from Fig. 2 of Morrell et al. (1983). **A** All stimuli were presented during the 0 to 50 ms interval. In A1 and A2 (*L*) denotes a light line, (*C*) denotes an auditory click, and (*L+C*) denotes simultaneous presentation of the light line and the click. In A3 the same light line was presented to the left eye (*L*), the right eye (*R*), and to both eyes (*R+L*). In A2 *spont.* denotes the spontaneous or background level of discharge. The data displayed in each histogram were acquired in consecutive sets of 20 trials, as indicated. The calibration bar at time 0 equals 20 spikes. **B** The visual stimulus was a light line presented during the time marked below the axis.

The calibration bar indicates 20 spikes and about 150 trials were given. In B1 the light line was vertical while in B2 it was horizontal. These data demonstrate *possible* complex coding occurring at burst intervals of roughly 50 ms with burst levels of large, small or no peaks

code of high neuronal population firing producing a response such as the removal of a hand from a hot stove. In the opposite extreme, the composing (or recall) of a Beethoven symphony must involve incredibly precise, sophisticated spatial-temporal neuronal processes. Most processing of information probably involves several simultaneous types of coding with cortical-cortical coding and processing being more sophisticated than cortical-subcortical. We believe that the key to finding the more complex coding lies in designing multielectrode experiments (in sensory cortex) not only looking at the appropriate spatial and temporal "separations" (we suggest $\sim 50\text{--}200\ \mu$ and $\sim 30\text{--}100\ \text{ms}$, respectively) but also presenting the appropriately simple, yet sophisticated stimuli.

We developed the trion model from the level of individual neurons to the next level or scale of phenomenological relevance which we believe to be a subunit of perhaps $\sim 30\text{--}100$ neurons (with only three levels of relevant firing output) and a synchronous time step $\sim 30\text{--}100\ \text{ms}$. In making this change of scale we

drew on the cortical principle of Mountcastle, our previous theoretical studies (Little and Shaw 1975, 1978; Shaw 1978; Roney and Shaw 1980) using a physical spin analogy (Ising model), the exciting work of Fisher who showed that a simple extension of the Ising model led to an *enormous* increase in richness of the solutions, our studies (Shaw et al. 1982) which suggest a subunit size of $\sim 30\text{--}100$ neurons, and experiments (see, e.g., Shaw et al. 1983; Morrell 1967) which show a time step of $\sim 50\ \text{ms}$ for groups of neurons bursting. [For a recent anatomical study which shows evidence for a spatial scale relevant to our trion size, see Fig. 12a of Gilbert and Wiesel (1983) which shows a clustering of axonal boutons at spacings of $90\ \mu$.]

The concept of a synchronous discrete time step $\tau \sim 50\ \text{ms}$ for groups of neurons to burst is crucial to our model. This should be contrasted to essentially all other models of neuronal networks (see, e.g., Hopfield 1982) in that they specifically have no "clock-like" timing. To establish the *plausibility* of such a τ , we note

the observation of periodic bursting in cortex has a long history see, in particular, Morrell (1967) and Morrell et al. (1983) who found multipeak responses in cat visual cortex with peak separation of approximately 50 ms. In addition, Morrell (1967; Morrell et al. 1983) observed dramatic changes in these bursting patterns when he paired stimuli in conditioning experiments. Some of these data are shown in Fig. 1. We suggest that these burst pattern data might be *consistent* with exciting or enhancing different periodic firing patterns (MPs) in our trion model. In addition to the simulation studies reported in this paper, we have conducted neurophysiological experiments (Shaw et al. 1983; Pearson 1985) to test certain assumptions of the model. We presented in Fig. 2 of Shaw et al. (1985) some of our data from cat primary visual cortex recording from a group of 2–3 neurons which show *four equally spaced peaks* in the post-stimulus histogram in response to a flashed bar [also see Fig. 1 of (Shaw et al. 1983)]. These peaks are separated by approximately 50 ms in close agreement with Morrell's data in Fig. 1. Also, as a result of showing time sequences of different bar orientations we observed burst patterns which might be consistent with exciting MPs. An excellent example of these data is given in Fig. 2. Clearly, it would be very interesting to record simultaneously from two or more closely spaced microelectrodes to test our assumption of a discrete time step τ .

The following features of the trion model are all necessary for its qualitative richness:

a) Finite fluctuations due to the random nature of synaptic transmission as well as other sources of noise.

b) Three possible firing states S (of each trion) denoted by $+(+1)$, 0 , $-(-1)$ which represent, respectively, a large "burst" of firing, an average burst, and a below average firing.

c) Associated with each of the three trion states S is a statistical weighting term $g(S)$ with $g(0) \gg g(+)$, $g(-)$ which takes into account the number of equivalent firing configurations of the trion's internal neuronal constituents. (For example, in a group of 90 neurons, firing levels of $+$, 0 , and $-$ could correspond to 90–61, 60–31, 30–0 neurons firing. There are many more combinatorial ways of generating the 60–31 level.) This crucial feature $g(0) \gg g(+)$, $g(-)$ gives the firing patterns stability.

d) Synchronous discrete time steps τ (\gg the firing time \sim ms of the individual neurons). We update the state of the system at time $n\tau$ in a probabilistic way related to the states at the *two* previous time steps $(n-1)\tau$ and $(n-2)\tau$.

e) A highly symmetrical interplay of inhibition and excitation among the interactions connecting the trions.

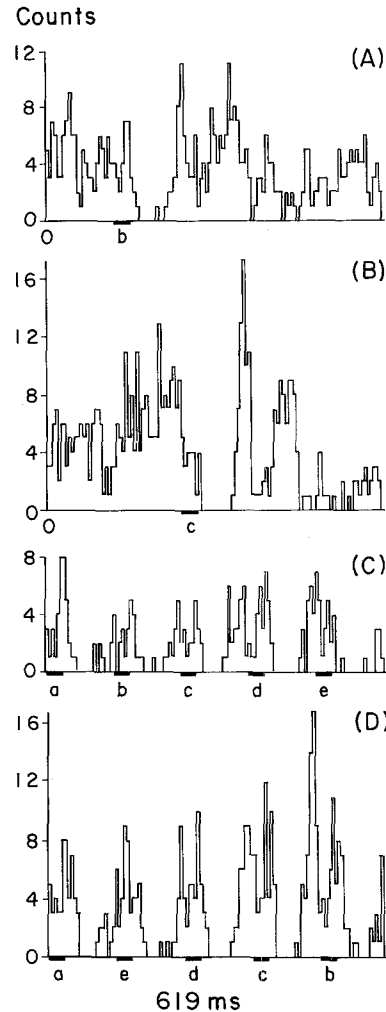


Fig. 2A–D. Spike firing responses of a cluster of three neurons in area 17 of a cat to four different time sequences of an oriented, flashed bar [see Shaw et al. (1983) and Pearson (1985) for more details]. There were 30 (continuous) cycles of 619 ms duration for each poststimulus histogram. The on times for the flashed bar on each cycle are denoted by the bars (33 ms duration) on the time axis and the subscripts a, b, c, d, e represent orientation angles of $0^\circ, 36^\circ, 72^\circ, 108^\circ, 144^\circ$ respectively. We point out two major experimental results indicated by these data, relevant to our trion model. i) In response to each bar, there are two peaks, separated by ~ 100 ms in the presentations **A** and **B** of a single bar per cycle and by ~ 50 ms in the clockwise **C** and counter clockwise **D** series of 5 bars. ii) The response in the counterclockwise sequence **D** is substantially greater than that for the clockwise sequence **C**. We believe that both these striking effects i) and ii) for these preliminary data are consistent with exciting MPs in our trion model with a time step $\tau \sim 50$ ms

The probability $P_i(S)$ of the i^{th} trion attaining state S at time $n\tau$, is given by:

$$P_i(S) = \frac{g(S) \cdot \exp[B \cdot M_i \cdot S]}{\sum_s g(s) \cdot \exp[B \cdot M_i \cdot s]}, \quad (1)$$

$$M_i = \sum_j [V_{ij} \cdot S_j + W_{ij} \cdot S_j'] - V_i^T,$$

then instructed to search for all the quasi-stable, periodic firing patterns (MPs) which have a high probability of cycling. The MPs are found by computing the most probable temporal evolution of the trion states from each of the possible initial conditions using (1) and determining if that evolution leads to a pattern that repeats after some time steps with a high probability (an MP). Thus this calculation for a given network (set of parameters) yields all the MPs as well as how many of the 531,441 initial conditions lead to each MP and how many time steps it takes. We have computed more than 40 examples of such six trion networks, each of which takes several hours of VAX 780 time.

Listed in Tables 1-6 are 6 examples of six trion networks [all with $g(\pm)=1$, $g(0)=500$, and $V_i^T=0$]. All MPs having a probability of cycling $>10\%$ for (fluctuation parameter) $B=10$ are given in each table. The MP pattern number is a two time step firing configuration number as a 12 digit ternary number (with $- = 0$, $0 = 1$ and $+ = 2$) converted to a base 10 number and (along with the interaction strengths) completely defines the pattern. Thus the first MP in Table 1 has pattern number 0 which is $- - - - -$ as the starting configuration. The given interactions are readily used in (1) to calculate the full 6 cycle MP as

$$\begin{array}{cccccc}
 - & - & - & - & - & - \\
 - & - & - & - & - & - \\
 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 \\
 + & + & + & + & + & + \\
 + & + & + & + & + & +
 \end{array} \tag{2}$$

In Table 1, the second MP has pattern number 1 corresponding to $0 - - - -$ and the time evo-

lution leads to an 18 cycle pattern. For this 18 cycle MP there are 18 *equivalent* starting positions (or time rotations), only the lowest pattern number is listed. In addition, this MP has 6 *inequivalent* spatial rotations; we regard each individual trion as distinguishable. Thus we consider this MP to have 5 *additional distinguishable* spatial rotations; however only the lowest pattern number is listed. [Note that MP pattern number 0, (2), has *no distinguishable* spatial rotations.] We list the number of starting conditions which lead to that MP (along with all the MP's time and spatial rotations). Since the major computing effort is to find the MPs for a given network, these tables represent a *valuable* data base for readily performing *many* other calculations in the trion model, e.g., reinforcing individual MPs using the Hebb algorithm (3). [Substantial changes ($\lesssim 20\%$) in the interactions away from the "symmetric" values listed in the tables introduce no new MPs.] As another example, Fig. 4 gives the probabilities of cycling for two of the MPs in Table 6 as a function of the fluctuations parameter B for the symmetric interaction case and a somewhat asymmetric case. (This figure was *readily* calculated using the MP pattern numbers from Table 6.) Figure 4 illustrates an important feature of the trion model: Both for small fluctuations (large B) and large fluctuations [small B , where roughly we compare $\exp(BM_i)$ in (1) to $g(S)$], the probabilities of cycling go to zero (for asymmetry in the interactions) for any MP having $S=0$ (together with $S=\pm 1$) levels. Thus finite fluctuations are *crucial* for the full richness of the model.

Now we discuss the striking results of our calculations:

1) *Rapid Nature of the Recall Process.* The average number of time steps that it takes a starting configuration to trigger an MP ranges from $\sim 2-5$. Each of the 3^{12} starting configurations is followed (for a given network) for up to 24 time steps until it triggers or excites an MP, and an average number of time steps is

Table 4. Same as Table 1

| Interactions | | Number of MPs: 216 | | | | | | | | | |
|-------------------------|-----|---------------------------------------|-----|---------|-----|--------|-----|--------|-----|---------|-----|
| V: 0 -1 1 -1 0 | | | | | | | | | | | |
| W: 0 1 -1 1 0 | | | | | | | | | | | |
| Number of triggers: all | | Avg. no. of timesteps to trigger: 4.1 | | | | | | | | | |
| 1 | 215 | 2 | 239 | 3 | 455 | 4 | 728 | 5 | 944 | 6 | 968 |
| 288 | | 288 | | 300 | | 7988 | | 132 | | 384 | |
| +++o+- | | +o++++ | | +o+o+o | | ++++++ | | +++o+- | | +o++++ | |
| ----- | | ----- | | ----- | | ----- | | o----- | | o----- | |
| o++++- | | -++++o | | o+o+o+ | | | | ++++-+ | | o++++o | |
| ---o-+ | | -o----+ | | -o-o-o- | | | | ---o-+ | | -o----+ | |
| +++++ | | +++++ | | +++++ | | | | o+++++ | | o+++++ | |
| o---+- | | +---o- | | o-o-o- | | | | ---+- | | o---o- | |

Table 5. Same as Table 1

| Interactions | | | | | | Number of MPs: 85 | | | | | |
|--------------------------|----------|---------|----------|----------|----------|---------------------------------------|----------|----------|----------|----------|----------|
| V: 0 -1 1 1 0 | | | | | | | | | | | |
| W: -1 0 -1 0 1 | | | | | | | | | | | |
| Number of triggers: 100% | | | | | | Avg. no. of timesteps to trigger: 3.8 | | | | | |
| 1 | 0 | 2 | 91 | 3 | 5856 | 4 | 12444 | 5 | 18300 | 6 | 19032 |
| 54 | | 44 | | 114198 | | 20958 | | 12312 | | 105954 | |
| ----- | o-o-o-o- | -++---- | -++o--- | -o++++- | -++++-- | o++++-- | o++++-- | o++++-- | o++++-- | o++++-- | o++++-- |
| o-o-o-o-o | -o-o-o-o | +-----+ | +o-----+ | +o-----+ | +o-----+ | +o-----+ | +o-----+ | +o-----+ | +o-----+ | +o-----+ | +o-----+ |
| +++++++ | o+o+o+o | -----+ | o-----+ | o-----+ | o-----+ | o-----+ | o-----+ | o-----+ | o-----+ | o-----+ | o-----+ |
| +++++++ | +++++++ | -----+ | -----+ | -----+ | -----+ | -----+ | -----+ | -----+ | -----+ | -----+ | -----+ |
| o-o-o-o-o | +o+o+o+ | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- |
| 7 | 38064 | 8 | 38796 | 9 | 40992 | 10 | 40993 | 11 | 43206 | 12 | 51972 |
| 2232 | | 12312 | | 19914 | | 34056 | | 32376 | | 20844 | |
| -o+o+o- | -++++o- | -+---+- | o+---+- | -+---+- | o+---+- | -+---+- | o+---+- | -+---+- | o+---+- | -+---+- | o+---+- |
| o+o+o-- | +++o-- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| +o+o--o | +o+o--+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ |
| +o--o+o | +o--+++ | -++-++ | -++-++ | -++-++ | -++-++ | -++-++ | -++-++ | -++-++ | -++-++ | -++-++ | -++-++ |
| o--o+o+ | o--+++ | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| --o+o+ | --+++ | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- |
| | | -+---+- | -+---+- | -+---+- | -+---+- | -+---+- | -+---+- | -+---+- | -+---+- | -+---+- | -+---+- |
| | | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- | +o+o- |
| | | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| | | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ |
| | | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| | | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- |
| | | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- |
| | | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| | | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| | | o+o+o- | o+o+o- | o+o+o- | o+o+o- | o+o+o- | o+o+o- | o+o+o- | o+o+o- | o+o+o- | o+o+o- |
| | | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| | | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- |
| | | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- | -+o+o- |
| | | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| | | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- | +---+- |
| | | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ | o+o+o+ |
| | | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- | --+++- |
| 13 | 53436 | 14 | 57828 | 15 | 58560 | 16 | 66430 | 17 | 66521 | 18 | 132860 |
| 20844 | | 20958 | | 114198 | | 28 | | 44 | | 54 | |
| -o+o+o- | -o+o+o- | -+++++- | -+++++- | -+++++- | -+++++- | -+++++- | -+++++- | -+++++- | -+++++- | -+++++- | -+++++- |
| o+o+o-- | o+o+o-- | +++++- | +++++- | +++++- | +++++- | +++++- | +++++- | +++++- | +++++- | +++++- | +++++- |
| -+o+o--o | +o+o--o | +o+o+o+ | +o+o+o+ | +o+o+o+ | +o+o+o+ | +o+o+o+ | +o+o+o+ | +o+o+o+ | +o+o+o+ | +o+o+o+ | +o+o+o+ |
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| --o+o+o | --o+o+o | --+++++ | --+++++ | --+++++ | --+++++ | --+++++ | --+++++ | --+++++ | --+++++ | --+++++ | --+++++ |
| 19 | 265720 | | | | | | | | | | |
| 1 | | | | | | | | | | | |
| o-o-o-o-o | | | | | | | | | | | |

computed from that (large) percentage of the 3¹² that trigger in the 24 time steps.

2) *MPs Recalled by Many Initial Patterns.* We note that large numbers of individual MPs are accessed or triggered by many *thousands* of initial configurations.

3) *Long Time Cycle MPs Triggered by Huge Number of Initial States.* MPs with cycle lengths of 18τ are given in Tables 1, 2, and 5. Especially interesting are MPs 12962 in Table 1 and 41329 in Table 2 each of

which is accessed by almost half of the 3¹² initial patterns!

4) *Rich, general nature of the trion model.* These examples of networks with different connections among the trions illustrate the great variety of different behaviour possible in the model: We examined six trion networks that supported *very large* numbers of MPs. For example the network having interactions V: 0 1 0 1 0 and W: -1 0 0 0 -1 (see Table 1 for notation) had 1804 MPs; the network with V:

MP (due to the error) to the triggering of the final MP is small (e.g. average 1–5). Thus, as with the input mapping type of recall shown in Tables 1–6, recall is rapid. 2) The probability of the most probable sequence of states between MPs is very high. Thus, once an error is made in an initial MP, the identity of the final MP is almost certain – i.e., such transitions are reliable. 3) The MPs are organized into classes. Each class is defined by the MPs which it can trigger, and by the MPs which can trigger it. Thus, even though these transitions are triggered by chance events, they form an ordered “sequence” when viewed as a whole. As an example of these sequences of spontaneous transitions among MPs, see Fig. 1 of Shaw et al. (1985) which shows a Monte Carlo simulation (of the network in Table 1) with 6 rapid transitions.

Previously, we had shown (Shaw et al. 1985) that introducing an idealized substructure, the trion, in modeling the cortical column led to a selective, adaptive network. Networks composed of a small number of trions (with symmetric interactions) supported up to thousands of MPs, any of which could be selected out with only small changes in interaction strengths using the Hebb-type algorithm

$$\Delta V_{ij} = \varepsilon \sum_{\text{cycle}} S_i(\tau) S_j(\tau - 1) \quad (3)$$

$$\Delta W_{ij} = \varepsilon \sum_{\text{cycle}} S_i(\tau) S_j(\tau - 2), \quad \varepsilon > 0.$$

We note that the 18 cycle MPs in Tables 1, 2, and 5 found in the present study were also able to be enhanced using (3). We speculate that these symmetrical interactions might be specified genetically giving a “naive” network which could initially respond to many different input signals. Experience or learning could then modify the connections via a Hebb type mechanism (3) to select out (as in the work of Edelman 1978) the appropriate responses or MPs.

The striking results presented here on the associative recall properties of the trion model give further encouragement to continued theoretical studies on this rich, general model which we believe embodies a basis for a theory of information processing and memory. However, the success of this (or any model) rests on possible experimental verification. Experiments which present dynamical sequences of stimuli to awake animals and record spikes from multiple micro-electrodes in (somatosensory) cortex will be performed in the laboratory of M. Merzenich. We believe that the results of these experiments (looking for spatial-temporal neuronal firing patterns) will indeed test the trion model. We conclude by stressing the importance in our model (of the cortical column, ~ 500 – 100μ diameter) of having both a spatial subunit scale

(~ 50 – 200μ) and a clock-like temporal scale (~ 30 – 100 ms) present. Clearly there is no conclusive evidence for these scales, however, more and more supportive data are being found in the central nervous system of mammals in both anatomical and physiological experiments (Gilbert and Wiesel 1983; Morrell 1967; Morrell et al. 1983; Mountcastle 1978; Pearson 1985; Shaw et al. 1982, 1983).

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