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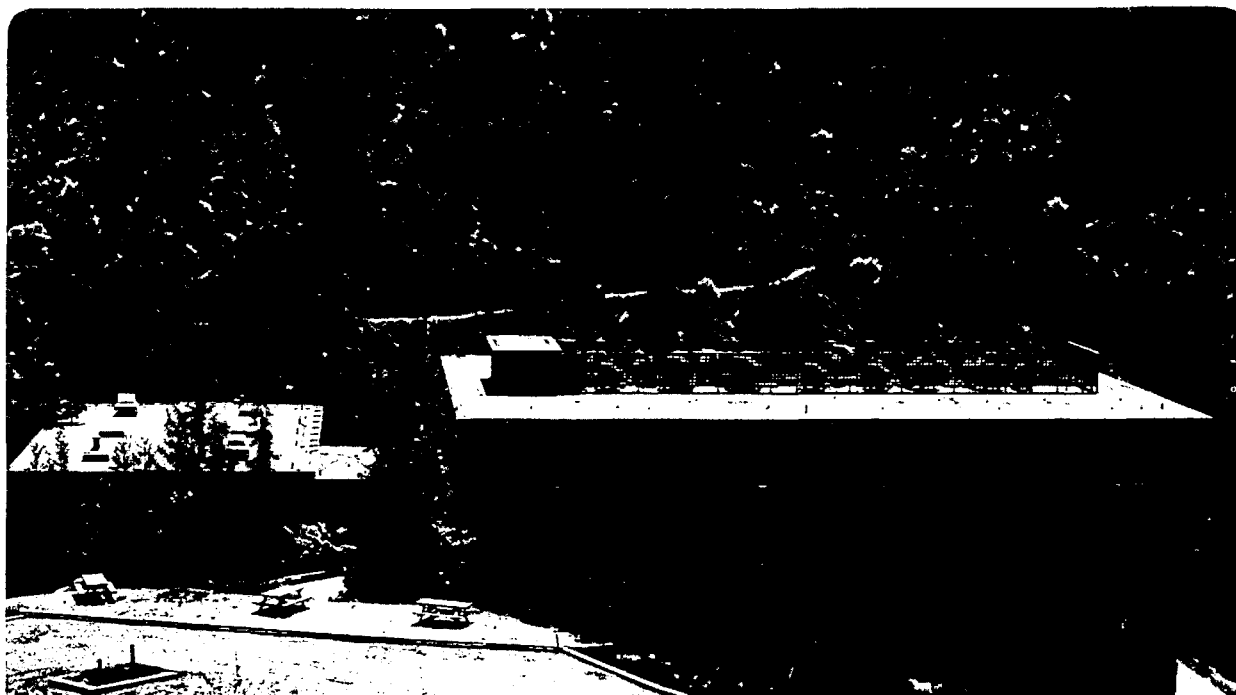
**The Formation of Barium Titanate Ceramics by
Solid State Reaction**

J.W. Bierach
(M.S. Thesis)

May 1988

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**THE FORMATION OF BARIUM TITANATE CERAMICS
BY SOLID STATE REACTION**

**Jeff W. Bierach
(M.S. Thesis)**

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May 1988

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Table of Contents

1	Introduction	1
1.1	Heterogeneous Solid State Reactions	2
1.2	Observed Intermediate Reaction Products	3
1.2.1	Ba ₂ TiO ₄ - Equilibrium Phase	3
1.2.2	BaTiO ₃ - Equilibrium Phase	4
1.2.3	Ba ₆ Ti ₁₇ O ₄₀ - Equilibrium Phase	4
1.2.4	Ba ₄ Ti ₁₃ O ₃₀ - Equilibrium Phase	4
1.2.5	BaTi ₄ O ₉ - Equilibrium Phase	4
1.2.6	Ba ₂ Ti ₉ O ₂₀ - Equilibrium Phase	5
1.2.7	BaTi ₅ O ₁₁ - Metastable Phase	5
1.2.8	BaTi ₆ O ₁₃ - Metastable Phase	5
1.2.9	BaTi ₂ O ₅ - Metastable Phase	5
1.2.10	Other Phases	6
2	Objective	7
3	Quantitative Analysis by X-ray Diffraction	8
3.1	General Principles	8
3.2	Working Equation	9
3.3	Detection Limit and Sources of Error	10
3.4	Peak Selection for Quantitative Analysis and Phase Identification	11
4	Experimental Procedures	13
4.1	Methods of Characterization	13
4.2	Raw Materials	13
4.3	Sample Preparation	14
5	Experimental Results and Data Reduction	15
5.1	SEM Observation	15
5.2	XRD Data Reduction	15
5.3	Phase Identification	17
5.4	Quantitative Analysis	18
6	Discussion	20
7	Conclusion	24
8	References	25
9	Tables	27
10	Figures	47

List of Tables

1. X-ray Diffraction Data for Barium Titanate Phases

A compilation of d-spacing, two-theta, and intensity values from the JCPDS card files. These values are sorted in order of increasing two-theta value. Also included in the list is data for Al_2O_3 (corundum) used as an internal standard for quantitative analysis.

2. Peaks Selected for Phase Identification and Quantitative Analysis

Peaks selected for quantitative analysis are marked QA.

3. Properties of Raw Materials

A list of manufacturer, batch numbers, impurities, particle size, and surface area of starting materials.

4. Summary of Samples

Weight fractions of Al_2O_3 and $\text{BaTiO}_3\text{-TiO}_2$ mixture and times at temperature for each sample.

5. Results of IDR Peak Search for All Samples

Observed d-spacing and intensity values for each sample as calculated by the Siemens Diffrac-11 IDR software. Additional data has been added for peaks which were found to be present based on the examination of the figures 11-14, but which were not found by the IDR program.

6. Intensity Data for Selected Peaks

Measured intensity values for the peaks selected for quantitative analysis, and the calculated reference intensity values (k_i) for BaTiO_3 and TiO_2 .

7. Results of Phase Identification and Quantitative Analysis

Weight fractions of BaTiO_3 and TiO_2 are reported for the various heat treatments. Phases which positively identified are marked ***. Phases which were not found to be present are marked with an X.

8. Data for the BaCO_3 - TiO_2 Reaction

A summary of the phases detected in equimolar samples of BaCO_3 and TiO_2 after various heat treatments, from Templeton and Pask[4].

List of Figures

1. BaCO_3 - TiO_2 Interface Reactions

Schematic of the possible BaCO_3 - TiO_2 interface reactions showing possible reaction products and the activity of TiO_2 for two cases:

- a. Simplified - shows only the Ba_2TiO_4 and BaTiO_3 phases.
- b. Complex - shows all possible phases between the reactants.

2. BaO - TiO_2 Phase Diagram

3. Possible Geometrical Arrangement of Product Phases During Solid State Reaction

A thin inner product phase is shown surrounded by a thicker outer phase.

4. X-ray Diffraction Patterns of Starting Materials

- a. BaTiO_3 b. TiO_2 (rutile) c. Al_2O_3 (corundum)

5. SEM Micrographs of Starting Materials

- a. BaTiO_3 (1000 $\times$) b. TiO_2 (77 $\times$)

6. SEM Micrograph of Unfired Mixed Powder (126 $\times$)

7. SEM Micrograph of Sample S06D (2400 $\times$)

The product of reaction of a TiO_2 particle with BaTiO_3 in which an agglomerate of sub-micron product phase particles is formed.

8. SEM Micrograph of Sample S08H (2240 $\times$)

A view of the fracture surface showing the sub-micron product phase particles.

9. X-ray Diffraction Patterns for All Samples

- a. 10-40° region. b. 40-70° region. c. 70-100° region.

From bottom to top the patterns correspond to samples:

Sraw - unfired; S24m - 24 minutes; S01h - 1 hour; S02h - 2 hours; S08h - 8 hours; S24h - 24 hours; S48h - 48 hours; S06d - 6 days; All samples were fired at 1050°C.

10. X-ray Diffraction Patterns Showing the Calculation of Background Lines

- a. 101 peak of TiO_2 - Sample S24m. b. 022,040 peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ - Sample S24m

11. X-ray Diffraction Patterns for the 031 Peak of BaTi_4O_9

12. X-ray Diffraction Patterns for the 022,040 Peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$

13. X-ray Diffraction Patterns for the 021 Peak of BaTi_4O_9 and the 102,131 Peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$

14. X-ray Diffraction Patterns for Selected Peaks of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$

- a. Peak at 60.806° (60.696). b. Peak at 71.446°.

15. Weight Fraction of TiO_2 , BaTiO_3 , and Total Amount of Intermediate Phases with Time

16. Normalized Intensity of Observed Intermediate Phases with Time

17. Normalized Intensity of Observed Intermediate Phases with Square Root of Time

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1 Introduction

Barium titanate ceramics have been widely investigated for many years because they have interesting and technically important properties. Perovskite type BaTiO_3 exhibits a positive temperature coefficient of resistivity, and is a piezoelectric ceramic. $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ exhibits useful properties for a microwave frequency dielectric[1].

The formation of these and other barium titanate ceramics by solid state reaction between BaCO_3 and TiO_2 is believed to be diffusion controlled and to proceed by the following reaction steps[2,3,4,5,6]: BaTiO_3 is formed first at the TiO_2 - BaCO_3 interface, with the diffusion of "BaO" into the TiO_2 accompanied by the evolution of CO_2 from the decomposition of BaCO_3 . After the initial layer of BaTiO_3 is formed, Ba_2TiO_4 forms at the BaTiO_3 - BaCO_3 interface, while BaTiO_3 advances into the TiO_2 by diffusion of "BaO" through the outer Ba_2TiO_4 and BaTiO_3 to the TiO_2 - BaTiO_3 interface (Figure 1a). When the BaCO_3 is all reacted, the outer Ba_2TiO_4 decomposes into BaTiO_3 with the diffusion of "BaO" through the inner BaTiO_3 where reaction with the remaining TiO_2 takes place to form BaTiO_3 .

The above reaction steps are oversimplified in terms of the nature of the diffusing species and of secondary phase formation. The quotation marks placed around BaO indicate that the nature of the diffusing species is unknown. If electrical neutrality is to be retained, the diffusion of Ba through BaTiO_3 and other product layers to react with TiO_2 must be accompanied by O diffusion or by a counter current of Ti. Diffusivities of Ba, Ti, and O in these ternary oxides are not known. The lattice diffusivity of Ba in rutile at 1070°C is $D_{\text{Ba}} \approx 2 \times 10^{-9} \text{ cm}^2/\text{s}$ compared to $D_{\text{Ti}} \approx 10^{-11} \text{ cm}^2/\text{s}$ and $D_{\text{O}} \approx 10^{-13} \text{ cm}^2/\text{s}$ for self diffusion of Ti and O in rutile[7]. Experimental work by Nakayama and Sasaki[8] has confirmed that Ba diffuses into rutile. Because the diffusivity of Ti is higher than that of O in TiO_2 , and because the volume change is large (200%) when TiO_2 is converted to BaTiO_3 , it seems likely that Ba ion diffusion through the ternary oxides is countered by Ti ion diffusion in the reverse direction in the ratio of $2\text{Ba}^{+2} : \text{Ti}^{+4}$ to maintain electrical neutrality. However, the possibility of Ba diffusion coupled by oxygen diffusion cannot be ruled out without experimental evidence.

This work addresses a different aspect of the analyses of the BaTiO_3 formation reaction will. The occurrence of titanate phases other than BaTiO_3 and Ba_2TiO_4 in the reaction of BaCO_3 and TiO_2 has been reported[2,3,4,9,10], but except in the study of Templeton and Pask[4] no systematic interpretation of these results has been formulated. The presence of secondary phases is usually attributed to such causes as insufficient mixing or other preparative factors[11], and in some cases the secondary phase is not even identified[5b]. It will be shown in this work that the occurrence of additional titanate phases during the course of the reaction is to be expected.

1.1 Heterogeneous Solid State Reactions

The formation of BaTiO_3 in the solid state is a heterogeneous reaction, meaning that the reactants become separated by phase boundaries and reaction products as soon as any product phase has formed. For the reaction to proceed, it is necessary for diffusion to occur across phase boundaries and intermediate phases, the driving force being the activity gradients between the two end members. For the BaCO_3 - TiO_2 reaction couple, the initial activity of TiO_2 decreases from unity on the TiO_2 -side to zero on the BaCO_3 -side of the boundary. This variation is shown schematically in Figure 1a for the reaction sequence described, as often assumed[5,6,11,12,13,14], if Ba_2TiO_4 is the only intermediate reaction product present during BaTiO_3 formation. Figure 1b shows schematically the activity variation expected from the BaO - TiO_2 phase diagram.

The BaO - TiO_2 phase diagram (Figure 2) shows that there are four equilibrium phases between the compositions BaTiO_3 and TiO_2 . It is possible that any of these phases might be formed between BaTiO_3 and TiO_2 during the course of solid state reaction if local thermodynamic equilibrium is approached. Figure 1b is a modification of Figure 1a where all of the possible intermediate phases, except those that have been reported[15,16,17,18,19] to be thermodynamically unstable ($\text{BaTi}_5\text{O}_{11}$, $\text{BaTi}_6\text{O}_{13}$, and BaTi_2O_5) have been included between the reactants BaCO_3 and TiO_2 .

Although any of the phases shown in Figure 1b might form, there are kinetic factors which could keep them from forming. A nucleation barrier could prevent a phase from forming. Some of the phases might only be formed transiently in a poorly

crystallized state or in such small amounts that detection would be difficult. If relatively thin inner layers of product phases are surrounded by a thick outer product layer, the inner phases could go undetected by the typical methods of characterization such as x-ray diffraction, optical microscopy, and scanning electron microscopy.

In both Figures 1a and 1b, the relative thicknesses of the various phases are not drawn to scale. In fact, the thickness of each phase depends inversely on the rate of diffusion through that phase[20]. Thus, if diffusion through a phase is rapid, it will form a relatively thin layer. If diffusion through a phase is slow, its layer will be relatively thick. A thin inner product phase surrounded by a thick layer of another phases or phases, as depicted in Figure 3 may be present. Such a circumstance could explain why many of the possible intermediate phases have not been observed.

If some of the stable intermediate phases do fail to nucleate, other barium titanates that are unstable at the temperature of study but which are easier to nucleate may be present during reaction. It is worthwhile, therefore, to seek evidence of the presence or absence of $\text{BaTi}_5\text{O}_{11}$, $\text{BaTi}_6\text{O}_{13}$, and BaTi_2O_5 which are not stable at the temperature of study of the reaction, but which have been reported to form at other temperatures.

1.2 Observed Intermediate Reaction Products

In this section, the various barium titanate phases which might be formed during solid state reaction will be discussed. There are six equilibrium phases between BaO and TiO_2 on the phase diagram (Figure 2), as well as the three metastable phases mentioned above. A number of these phases have been observed during the course of solid state reaction. Other phases which have been reported to exist are mentioned in section 1.2.10, but these phases are not expected to be found in this work.

1.2.1 Ba_2TiO_4 - Equilibrium Phase

Barium orthotitanate, Ba_2TiO_4 , which has been widely reported, is formed between the reactant BaCO_3 and initial product BaTiO_3 during the reaction of BaCO_3 and

TiO_2 [2-6]. The phase is easy to detect and its presence has an undesirable effect on the electrical properties of BaTiO_3 ceramics[11]. Templeton and Pask[4] have shown that the formation of Ba_2TiO_4 can be suppressed below 1100°C in one atmosphere of CO_2 .

1.2.2 BaTiO_3 - Equilibrium Phase

BaTiO_3 is the phase of most technological interest in the $\text{BaO} - \text{TiO}_2$ system. It is typically formed by solid state reaction between BaCO_3 and TiO_2 as described in the introduction. Many authors[2-6,9-11,13,14,21,22,23] have studied this reaction in an effort to determine the affect of particle size, mixing, atmosphere, and reaction temperature on the microstructure and electrical properties of sintered BaTiO_3 ceramics.

1.2.3 $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ - Equilibrium Phase

This phase has not been reported to form as an intermediate reaction product. It has been prepared[24] by quenching partially melted samples of composition $\text{BaCO}_3 : \text{TiO}_2 = 1 : 3$ from 1400°C , and it has also been prepared[24] by slowly cooling samples of composition $1 : 2.5$ after heating at 1400°C . Negas, et. al.[25], are the only authors to report the formation of $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ by solid state reaction. They observed $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ after reaction below 1300°C in mixtures which ranged in composition from $1\text{BaCO}_3 : 2\text{TiO}_2$ to $1\text{BaCO}_3 : 3\text{TiO}_2$. $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ was determined to exist as an equilibrium phase down to 800°C by slowly cooling samples from 1300°C and quenching from 800°C .

1.2.4 $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ - Equilibrium Phase

A phase previously reported in the earlier literature as BaTi_3O_7 , now known to be $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ [26], has been reported by many authors to be present in small amounts during the reaction of BaCO_3 and TiO_2 to form BaTiO_3 [2,3,4,9,22]. This phase forms readily by solid state reaction.

1.2.5 BaTi_4O_9 - Equilibrium Phase

Templeton and Pask reported very small amounts (≈ 1 mole %) of BaTi_4O_9 during the intermediate stages of reaction in BaCO_3 - TiO_2 mixtures. Rase and Roy[27] prepared

BaTi_4O_9 "very easily" by solid state reaction below 1400°C of a mixture of composition $\text{BaO} : \text{TiO}_2 = 1 : 4$. In studies of the formation of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ from TiO_2 and BaTiO_3 , O'Bryan and Thomson[28] observed BaTi_4O_9 as a second phase in the majority of their samples. BaTi_4O_9 has also been found to form at exposed surfaces of Ba-doped rutile ceramics heated under various conditions[7,29].

1.2.6 $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ - Equilibrium Phase

This phase has not been reported to form as an intermediate reaction product during reaction of BaCO_3 and TiO_2 . O'Bryan and Thomson prepared $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ from mixtures of BaTiO_3 and TiO_2 which were pre-fired in O_2 at 1350 - 1400°C for 6 hours, and then equilibrated for 12 hours in O_2 at temperatures between 1100°C and 1400°C .

1.2.7 $\text{BaTi}_5\text{O}_{11}$ - Metastable Phase

In mixtures of $\text{BaCO}_3 : \text{TiO}_2 = 1 : 4.5$ and $1 : 5$ heated at 1100°C , O'Bryan and Thomson observed several weak diffraction lines of this phase along with those of BaTi_4O_9 and TiO_2 [15]. When the composition $\text{BaO} : \text{TiO}_2 = 1 : 5$ was prepared from an aqueous solution of $\text{Ba}(\text{NO}_3)_2 + \text{Ti}(\text{OC}_3\text{H}_7)_4$ and prereacted at 1000°C for 2 hours, $\text{BaTi}_5\text{O}_{11}$ formed as the major phase. Tillmans[16] found crystals of $\text{BaTi}_5\text{O}_{11}$ in samples of composition $\text{BaO} : \text{TiO}_2 = 1 : 4$ which were melted and quenched from 1400° to 1500°C .

1.2.8 $\text{BaTi}_6\text{O}_{13}$ - Metastable Phase

The only evidence for the formation of this phase is by Tillmanns[17], who formed $\text{BaTi}_6\text{O}_{13}$ when a mixture of composition $\text{BaO} : \text{TiO}_2 = 1 : 4$ was melted and quenched from 1460°C . For the compositions $\text{BaCO}_3 : \text{TiO}_2 = 1 : 4.5$ and $1 : 5$ heated at 1100°C , O'Bryan and Thomson[15] identified only BaTi_4O_9 and $\text{BaTi}_5\text{O}_{11}$ by x-ray powder diffraction. $\text{BaTi}_6\text{O}_{13}$ is not expected to be found in the present study.

1.2.9 BaTi_2O_5 - Metastable Phase

Several authors have reported the formation of this phase from samples of composition between 60 and 78 mole % TiO_2 which were cooled from a

melt[18,19,25,27]. O'Bryan and Thomson[18] and Jonker and Kwestroo[19] have shown that BaTi_2O_5 is unstable at temperatures below 1312°C , and that this phase is not an equilibrium phase. Jonker and Kwestroo, and Negas et. al.[25], were unable to form this phase by solid state reaction. Therefore, the phase is not expected to be found in the present study at 1050°C .

1.2.10 Other Phases

It is believed that the list above includes all characterized phases of the $\text{BaO} - \text{TiO}_2$ system, and the structures of all of these phases are known. Several authors report the presence of unidentified phases which could be any of the above or some other phases such as the ones mentioned below.

Other phases which have been reported in the literature include those which have been named incorrectly, and others which are structurally similar to the barium titanates but exhibit chemical variations or contain other elements[30]. Phases reported as $\text{Ba}_2\text{Ti}_3\text{O}_8$, BaTi_3O_7 and $\text{Ba}_2\text{Ti}_5\text{O}_{12}$ are probably BaTiO_3 , $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$, respectively[19,25,30]. In the chemically variant phases, the Ti^{+4} ion can be partially substituted by Ti^{+3} ($\text{Ba}_2\text{Ti}_2^{3+}\text{Ti}_4^{4+}\text{O}_{13}$) or by a vacancy ($\text{Ba}_2\text{Ti}_{5.5}\text{O}_{13}$). The Ti^{+4} ion can also be partially substituted by Al^{+3} ($\text{Ba}_4\text{Ti}_{10}\text{Al}_2\text{O}_{27}$) and Pt^{+4} ($\text{Ba}_4[\text{Ti,Pt}]\text{O}_3$ and $\text{Ba}_4[\text{Ti,Pt}]_2\text{PtO}_{10}$),

2 Objective

The objective of the current research project is to investigate the existence of secondary phases between the reactants BaO and TiO₂ during the formation of barium titanate ceramics. It was stated earlier that BaTiO₃ is the first phase observed in the reaction of BaCO₃ and TiO₂, and only one phase (Ba₂TiO₄) has been detected on the BaO-rich side of BaTiO₃. To study the phases which form on the TiO₂-rich side of BaTiO₃, it is not necessary to start with BaCO₃ and TiO₂--it is sufficient to study the system BaTiO₃ - TiO₂. This simplification is valid because any solid state reaction, no matter how complex, can be broken down into interactions between pairs of solid phases. The use of BaTiO₃ and TiO₂ as reactants simplifies the problem of phase identification by eliminating two phases, BaCO₃ and Ba₂TiO₄, and it also eliminates problems with controlling extraneous reactions when these two phases are present. Mixtures of BaCO₃ and TiO₂ are highly reactive with common crucible materials such as Al₂O₃ and platinum. Mixtures of BaTiO₃ and TiO₂ can be fired at moderate temperatures (1100°C) in a platinum basket with little or no reaction with the platinum.

The reaction between BaTiO₃ and TiO₂ was studied at 1050°C. This temperature was selected because it was near temperatures used in earlier work in the literature[4] and because, when produced for practical applications, barium titanate ceramics are often pre-reacted at 1050-1100°C before being fired at temperatures greater than 1300°C. The compositions and relative amounts of phases formed as a function of time at 1050°C were identified by x-ray diffraction. The method of analysis increases the sensitivity with which phases can be detected over those of past studies, but it is emphasized that absence of x-ray diffraction evidence does not prove that a phase has not formed; the phase might be present in an amount below the detection limit for that phase.

3 Quantitative Analysis by X-ray Diffraction

3.1 General Principles

Quantitative analysis by x-ray diffraction is based on the principle that the intensity of any diffraction peak of a particular phase in a mixture depends on the concentration of that phase in the mixture. The method used for quantitative analysis is the "matrix-flushing" technique developed by Chung[31] and is an extension of the internal standard method of Klug and Alexander[32]. An outline of the theory will be given below. The intensity equation for x-ray powder diffraction is

$$I_{hkl} = \left[\frac{I_0 e^4 \lambda^3 d}{32 \pi m^2 c^4 r} \right] \left[\frac{1 + \cos^2 2\theta}{\sin^2 \theta \cos \theta} \right] [N^2 F^2 p e^{-2M}] \frac{V}{2\mu} \quad (1)$$

- I_{hkl} = intensity of x-rays diffracted by the hkl plane
- I_0 = intensity of primary x-rays beam
- e = electron charge
- m = electron mass
- λ = wavelength of x-rays
- d = slit width of detector
- c = velocity of light
- r = radius of diffractometer circle
- θ = Bragg angle
- N = number of unit cells per unit volume
- p = multiplicity factor
- e^{-2M} = temperature factor
- F = structure factor
- μ = linear absorption coefficient
- V = volume of powder exposed to x-ray beam

A full derivation of this equation can be found in most advanced texts on x-ray diffraction. The first set of terms contains physical constants and machine-dependent terms and will be constant for the same machine operating under a given set of conditions, i.e. accelerating voltage and filament current. The second two sets of terms depend upon hkl . All of these terms in brackets can be combined into one term, K_{hkl} , which will be constant for any given diffraction peak under fixed operating conditions. Then one can write a simple expression for the intensity of a diffracted beam which depends only on K_{hkl} , on the volume of powder in the beam, V , and on the linear absorption coefficient of the powder, μ . This simplified expression is given below.

$$I_{hkl} = K_{hkl} \cdot \frac{V}{\mu} \quad (2)$$

To convert the above equation, which is for a single phase powder, to an equation for a multiphase mixture, V is replaced by V_i , the volume fraction of phase i in the mixture, and μ is replaced by μ_m , the linear absorption coefficient of the mixture.

$$I_i = K_i \cdot \frac{V_i}{\mu_m} \quad (3)$$

The hkl subscripts have been dropped from I_{hkl} and K_{hkl} , and the subscript i has been added. For I_i , this subscript identifies the intensity of a selected peak of phase i in the mixture. Similarly, K_i is a constant for a selected peak of phase i . It is desirable to convert V_i in equation 3 to X_i , the weight fraction of component i in the mixture. To do this, V_i is replaced by X_i/ρ_i , where ρ_i is the density of phase i . Thus,

$$I_i = K_i \cdot \frac{X_i}{\rho_i \mu_m} \quad (4)$$

3.2 Working Equation

By taking the ratio I_i/I_c , where I_c is the intensity for a given peak of a reference material which has been added to the mixture in a known quantity, X_c , one obtains the working equation for the quantitative analysis of mixtures.

$$\frac{I_i}{I_c} = \frac{K_i}{K_c} \cdot \frac{X_i}{X_c} \cdot \frac{\rho_c}{\rho_i} \cdot \frac{\mu_m}{\mu_m} = k_i \cdot \frac{X_i}{X_c} \quad (5)$$

The subscript c is used to denote corundum(α - Al_2O_3) which has been established by the Joint Committee on Powder Diffraction Standards as a standard reference material because of its purity, ready availability, and high stability. k_i is known as the reference intensity ratio for phase i in the mixture.

The selection of peaks for k_i determination is arbitrary. Typically, the most intense diffraction peak of each phase is chosen, but in multicomponent systems it is often necessary to choose not the most intense reflection, but the most intense resolved

reflections. If a peak is selected for k_i determination which is not the most intense peak for that phase, the measured intensity can be scaled to the value of the most intense peak by comparison with a pure sample of the phase, or the selected peak can be used directly. The only requirement is that consistency be maintained throughout. Values of k_i are tabulated for the strongest reflections of many phases in the JCPDS card file for $X_i = X_c = 0.5$. However, it is best to calculate the reference intensity ratios obtained for each material under the same instrumental conditions. This calculation is accomplished using equation 6, to calculate each k_i from data for a single multicomponent mixture of known composition.

$$k_i = \frac{I_i}{I_c} \cdot \frac{X_c}{X_i} \quad (6)$$

Once each of the k_i 's has been determined, one can calculate the weight fraction of each phase in mixtures of unknown composition from the equation

$$X_i = \frac{I_i}{I_c} \cdot \frac{X_c}{k_i} \quad (7)$$

The above equation allows each X_i to be determined independently from the others, allowing in theory for the calculation of the weight fraction of unknown or even amorphous phases in a mixture by summing all of the known X_i 's. The extent to which this determination can be accomplished depends on the error in measuring the individual X_i 's.

3.3 Detection Limit and Sources of Error

The detection limit for component i in a mixture, $X_i(\text{d.l.})$, is defined as the minimum concentration required to produce an observable signal above the background signal. The background intensity, I_b , is typically taken as $3\sqrt{N_b}/t$, where N_b is the number of background counts accumulated over t seconds. Substituting I_b for I_i in equation (7) gives,

$$X_i(\text{d.l.}) = \frac{X_c}{I_c} \cdot \frac{I_b}{k_i} = \frac{X_c}{I_c} \cdot \frac{3\sqrt{N_b}}{k_i t} \quad (8)$$

One of the main sources of error in quantitative analysis by x-ray powder diffraction is variation in sample preparation. Great care must be taken to prepare all samples in as similar a manner as possible, and to operate the diffractometer under the same operating conditions. Preferred orientation of the particles exposed to the x-ray beam can occur, particularly if the crystallites are needle or plate-like in habit. The basic intensity equation for x-ray diffraction was derived for a random distribution of crystalline particles and is inaccurate if any preferred orientation exists. Errors due to preferred orientation can be reduced by adding the intensities of several peaks for one phase. This method of adding intensities also improves the counting statistics by increasing the total measured intensity for each phase.

3.4 Peak Selection for Quantitative Analysis and Phase Identification

Table 1 is a compilation of d-spacing, two-theta, and intensity values for all of the peaks of the barium titanate phases which might form during a solid state reaction. These values were taken from the JCPDS card file and sorted by increasing two-theta values. Each peak is identified by its composition and if known, its *hkl* indices. Phases for which the JCPDS patterns were questionable or of low quality are $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ and BaTi_2O_5 . Also included in Table 1 is the pattern for $\alpha\text{-Al}_2\text{O}_3$ (corundum), which was used as a reference material. Table 1 was scanned for isolated peaks of each phase for purposes of quantitative analysis and phase identification. The selected peaks are shown in Table 2, with the peaks being used for quantitative analysis denoted by QA.

The majority of peaks in Table 1 are not useful for quantitative analysis because of peak overlap. In the previous work by Templeton and Pask[4], peaks were selected which are shown in Table 1 to overlap with other peaks and are therefore not suitable for quantitative analysis. They used the 402,431 peak of " BaTi_3O_7 " ($\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$) which coincides with a peak of BaTi_4O_9 , and the 121 peak of BaTi_4O_9 which overlaps a $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ peak. The peaks which they selected can not be fully resolved because of this overlap and also because of the close proximity of the selected peaks themselves (31.4° and 31.3°), and they did not measure integrated intensity--they used the maximum peak height which in itself increases the error in their measurements.

The peaks selected for quantitative analysis in the present study were not always those of maximum intensity, but were sufficiently separated from neighboring peaks to be useful. The criterion that each peak be separated from neighboring peaks by at least 0.3° was used to select peaks for phase identification. For purposes of quantitative analysis the nearest neighbor peak distance was required to be 0.5° or greater. After it was determined that certain phases were not present in the mixtures, peaks of those phases were eliminated from the possibilities considered in Table 1 making possible the selection of peaks such as the 110 peak of Al_2O_3 which is only 0.1° degrees from the neighboring BaTi_2O_5 peak.

It is interesting to note that many of the peaks listed in Table 1 have the same d-spacing. For example, the 110 peak of TiO_2 and the 411 peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ coincide exactly. There are numerous other cases of coincidence in Table 1. Some of these coincident values could be in error because the JCPDS patterns of little studied phases are unreliable, but much of the overlap is caused by the close structural similarities of the various barium titanate phases[30].

4 Experimental Procedures

4.1 Methods of Characterization

The BET method for determining the specific surface areas of the different starting materials was used. The equipment used was a QuantaChrome QuantaSorb Surface Area Analyzer Model S-7.

Scanning electron microscopy (SEM) was performed on an ISI Model DS-130 high resolution microscope to determine the particle size, shape, and morphology of the starting materials, mixed powders, and reaction products.

A Siemens Diffractometer Model D500 was used for x-ray diffraction analysis of starting materials and reaction products. The starting materials were scanned from 20° to 70° at 0.1° intervals with a dwell time of 1 second to locate the various peaks. All of the reaction mixtures were scanned from 10° to 100° with a step-scan of $0.4^\circ/\text{step}$ and a dwell time of 8 seconds. Duplicate runs of selected peaks were scanned over a 1° interval on each side of the peak with the same step-scan and dwell time. Data were stored on disk as a list of two-theta values and number of counts. These data were later analyzed using the Siemens Diffrac-11 software and computer programs written for the IBM-PC in Borland Turbo Pascal. Computer programs written for the IBM-PC were used to calculate a linear background line across each of the peaks selected for quantitative analysis and to calculate the integrated intensities of these peaks. The methods used for quantitative analysis were described in an earlier section.

4.2 Raw Materials

Both the TiO_2 (rutile) and BaTiO_3 powders were Puratronic grade purchased from Johnson Matthey Chemicals, Limited. Table 3 lists the batch numbers, impurities, and particle size data for each material. Indexed XRD patterns for each of the pure materials are shown in Figure 4. The pattern for rutile (Figure 4b) shows no trace of the anatase phase. SEM pictures of the two materials are shown in Figure 5. The TiO_2

powder consisted of agglomerates between 0.3 and 0.8 mm in diameter. These agglomerates were composed of irregularly shaped particles which ranged in size between 20 and 80 μm . The BaTiO_3 powder consisted of 8 - 40 μm particles.

The $\alpha\text{-Al}_2\text{O}_3$ used as an internal standard for quantitative analysis was reagent grade from J.T. Baker Chemical Co. The powder was sieved through a #325 mesh screen to obtain a particle size below 45 μm . The impurities and batch number for this material are given in Table 3.

4.3 Sample Preparation

A Mixture of BaTiO_3 and TiO_2 ceramics was weighed on a Mettler H20C balance to one tenth of a milligram. The batch consisted of 16.9694g BaTiO_3 and 20.3492g TiO_2 corresponding to an overall stoichiometry of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$. The powder mixture was milled in a plastic jar with ZrO_2 balls for 30 minutes in a high-speed planetary ball mill. Two gram pellets of the powder mixture were pressed to 50% theoretical density using a half inch die lubricated with zinc stearate.

The pellets were fired in air at 1050°C in a vertical tube furnace for various times from 24 minutes to 6 days, and removed from the furnace and allowed to air-cool. The pellets were then broken apart and one piece was saved for use in the SEM. The remainder was mixed with $\alpha\text{-Al}_2\text{O}_3$ (≈ 30 weight percent) and milled in the planetary ball mill using ZrO_2 balls in a plastic jar for 15 minutes. The exact weight proportions and sample identification codes for each sample are given in Table 4. The mixed fine powder was pressed into a lucite sample holder for use in XRD experiments. The dimensions in mm of the recessed area in the lucite sample block were $25 \times 25 \times 1.6$.

For examination in the SEM, powder samples of the raw materials were held to Al sample mounts with double stick tape and were gold coated in a Polaron sputtering apparatus. Fracture surfaces of fired pellets were examined after the pieces were mounted with epoxy onto a sample mount and gold coated.

5 Experimental Results and Data Reduction

5.1 SEM Observations

Figure 6 is an SEM micrograph (126 $\times$) of the unfired mixed powders mounted on double-stick tape after grinding in the planetary ball mill. The large TiO_2 agglomerates have been broken up so that the largest TiO_2 particles are $\approx 80 \mu\text{m}$ across. Higher magnification photographs (500 $\times$) of the TiO_2 particles revealed smooth surfaces.

As the reaction proceeded, sub-micron particles were formed out of the original TiO_2 particles. This process is shown in Figure 7. The micrograph of Figure 7 (2400 $\times$) was prepared from sample S06D after mixing with Al_2O_3 and grinding. The particle shown is roughly $50 \mu\text{m}$ across. Figure 8 is a micrograph (2240 $\times$) of a fracture surface from sample S08H which also shows the overall transformation of the large particle starting materials into sub-micron product phase particles.

5.2 XRD Data Reduction

X-ray patterns for each of the samples are shown in Figures 9. Figure 9a shows the data in the two-theta range 10-40°, Figure 9b shows the data in the range 40-70°, and Figure 9c shows the data in the range 70-100°. The d-spacings and integrated intensities for the peaks in each pattern are given in Table 5(a-h). The calculation of d-spacings and integrated intensities were done with the Siemens Diffrac-11 IDR software program. This program was found to give consistent values for the d-spacings, which were taken at the point where the second derivative of the curve fit through the raw data points was a minimum[33], but the integrated intensity values were suspected of being in error. It was found that the program did not correctly subtract out the background. The intensities calculated by the program appear to be fairly self-consistent, but for purposes of quantitative analysis it was necessary to calculate the integrated intensities of selected peaks by hand.

Another problem with using the IDR program was in adjusting the "sensitivity factor" which controls how the program determines the presence of peaks. In several instances low intensity peaks are not reported by the IDR program. When this occurred for peaks which were selected for quantitative analysis and phase identification, careful inspections of the peaks were made graphically. This process will be described in section 5.3 below. If a peak was found to be present, a line was added to the IDR data shown in Table 5.

The process of analyzing the x-ray data given in Table 5 for phase identification did not follow easily from the data in Table 1. In cases where a peak could be assigned to more than one phase, additional peaks for each of the phases were sought to confirm the presence of that phase. By eliminating phases which were not present (or below the detection limit), the number of phases in Table 1 could be reduced significantly so that each peak could be assigned unambiguously. However, where overlap occurred with two peaks from phases which were both known to be present, the peak was assigned to both phases. The resulting peak assignments are shown in Table 5 with the d-spacing and intensity data.

The raw data for quantitative analysis were analyzed in the following way. Data for selected peaks were extracted from the original data files. A linear background line was determined for each peak by averaging three background points on each side of the peak and fitting a straight line between them. The integrated intensity was taken as the area under the raw data curve above the calculated background line. An example of this procedure is shown in Figure 10a for the 101 peak of TiO_2 and Figure 10b for the 022,040 peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$. The resulting intensity values for each peak were averaged for the duplicate runs and the averaged values divided by the dwell time (8 seconds) to convert counts to counts per second (cps). The intensities for each of the phases followed by quantitative analysis were taken as the sum of the intensities of the selected peaks. These values are listed in Table 6a.

5.3 Phase Identification

Because the data of Table 5 did not always unambiguously establish the presence of the possible intermediate phases, careful examination was made of the peaks selected for this purpose as given in Table 2. The intensity of the 031 peak of BaTi_4O_9 as a function of time is shown in Figure 11. The intensity of the (022,040) peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ is shown in Figure 12, and both the 021 peak of BaTi_4O_9 and the (102, 131) peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ are shown in Figure 13. Both BaTi_4O_9 and $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ were detected after only 24 minutes.

The presence of BaTi_4O_9 after 24 minutes is clearly evident from inspection of Figure 11 and 13, but the presence of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ at this early time is not as obvious. To confirm the presence of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ the intensity data of the 022,040 peak was checked for statistical significance above the background level. The average background intensity on both sides of the peak is ~17 cps. Peak intensities were considered to be significant if they were three standard deviations above the background intensity. Three standard deviations corresponds to ~12 cps above background. From the data of Table 6, $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ is shown to be present with an intensity of 18 cps above background. Figure 10b shows the calculated background line and intensity data for the this peak after 24 minutes at temperature.

Although the overall sample stoichiometry was in the correct ratio for the formation of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$, this phase was not detected until after 8 hours at temperature. In Figure 14a, the $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ peak can be resolved for sample S08H, but the $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ peak which should be present in Figure 14b is not clearly resolved for any of the samples. The selected $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ peak should be found at 60.806° , but inspection of the Figure shows a peak between 60.68 and 60.72° . It is possible that the peak at 60.68° is the selected $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ peak and that the data in the JCPDS card file is in error. However, it is also possible that the peak at 60.68° is an unidentified peak from one of the other phases which were present. For sample S06D in Figure 14a, it appears as though a peak might be present at 60.80° , but due to the close proximity of the peak at 60.68° it is not possible to establish the presence of the $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ peak.

Careful examination was made of the two-theta range about the selected $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ peak. Although $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ is reported to be a thermodynamically stable phase of the $\text{BaO} - \text{TiO}_2$ system, there was no indication of its presence. Similarly, $\text{BaTi}_5\text{O}_{11}$, which O'Bryan and Thomson report to form when BaCO_3 and TiO_2 are heated together at 1100°C , was not observed and no evidence for the presence of the metastable phases $\text{BaTi}_6\text{O}_{13}$ or BaTi_2O_5 was found.

A summary of the phases which were positively identified for the various times at temperature is given in Table 7. Phases which were not found are marked with an X, and phases which were found are denoted ***.

5.4 Quantitative Analysis

Reference intensity ratios for BaTiO_3 and TiO_2 were calculated from equation 6 using the intensity values and weight fractions from sample Sraw. Using these reference intensity ratios, the weight fractions of TiO_2 and BaTiO_3 in each sample were calculated using equation 7. These results are plotted in Figure 15 where the weight fractions have been divided by $(1-X_c)$ to make them relative to the reaction mixture without the added Al_2O_3 . Also shown in Figure 15 is the weight fraction of intermediate phases calculated as one minus the weight fractions of BaTiO_3 and TiO_2 .

The amount of BaTiO_3 and TiO_2 after 6 days was 21.5 w/o and 28.9 w/o, respectively. The composition of the starting material was 45.5 w/o BaTiO_3 and 54.5 w/o TiO_2 . This large amount of unreacted powder can be attributed to the size of the original TiO_2 particles. These were intentionally chosen to be large so that by slowing the reaction rate the various intermediate phases might be observed more easily. It is also possible that the reaction mixture was heterogeneous and that local equilibrium was approached in isolated regions causing the rate of the reaction to decrease.

It was not possible to calculate reference intensity ratios for BaTi_4O_9 , $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$, and $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ directly because pure samples of these phases were not available. An attempt was made to determine k_i values for BaTi_4O_9 and $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ from the data of samples S24m, S01H, and S02H for which these were the only intermediate phases

present. These calculated k_i values could then be used to determine the amounts of these phases in each of the samples. In the samples which were heated for 8 hours or more, the amount of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ would be determined by $1 - \sum X_i$, where X_i includes all of the other phases which were present.

However, consistent values of k_i for BaTi_4O_9 and $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ could not be determined from the three samples due to the scatter in the data. Instead, a plot of normalized intensities for these two phases is shown in Figure 16. The intensities were normalized by use of the multiplier $(X_c/I_c)/(1-X_c)$. These values differ from the true weight fractions of these phases in the reaction mixture only by the reference intensity ratio. Normalized intensity values were not determined for $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ because overlapping of peaks made it difficult to get good intensity data for this phase.

An approximate value of the detection limit for each of the observed phases was determined from equation 8 by use of estimated relative intensity ratios. If a value of ~1-2 is taken for the relative intensity ratio and an average background intensity of ~130 counts/8s is used, a value of 2-4 w/o is calculated. At higher angles the background intensity is reduced to ~60 counts/8s, and for similar values of k_i the detection limit is calculated as 1.5 - 3 w/o. The detection limits for BaTi_4O_9 and for $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ were observed to be less than 3.5 w/o in sample S24M, where 3.5 w/o is the total amount of intermediate phases observed in the sample. The actual detection limits for BaTi_4O_9 and $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ are probably closer to 2 w/o. This value of the detection limit would be decreased if higher intensity peaks could be resolved without overlap with neighboring peaks.

6 Discussion

In this study the technique of quantitative analysis by x-ray diffraction has been applied to the study of intermediate phase formation between BaTiO_3 and TiO_2 . It seemed likely that some of the phases of compositions between BaTiO_3 and TiO_2 are present during reaction between BaCO_3 and TiO_2 , but have gone undetected a) because their quantities were low compared to those of the reactants and of BaTiO_3 and Ba_2TiO_4 and b) because overlap of the diffraction peaks of the various phases makes analysis difficult.

To increase the effective volume fraction of intermediate phases, the reaction of BaTiO_3 with large particles of TiO_2 was studied. The problem of peak overlap was greatly simplified by elimination of BaCO_3 and Ba_2TiO_4 from the system. A careful selection of reference peaks was made to establish the presence of the known barium titanate phases. Using computer assisted evaluations it then was possible to establish which phases were present and to determine the total amount of intermediate phases with greater accuracy than possible in previous studies.

Three phases were observed in the reaction between BaTiO_3 and TiO_2 : BaTi_4O_9 , $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$, and $\text{Ba}_2\text{Ti}_9\text{O}_{20}$. BaTi_4O_9 and $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ formed readily and were observed after only 24 minutes at 1050°C . Values of normalized intensity, which scale with the weight fraction of the phases, are plotted in Figure 16 as a function of time. BaTi_4O_9 initially grows rapidly in amount, but stays relatively constant after 24 hours. $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ also forms rapidly at the start of the reaction, but its amount continues to increase at a steady rate throughout the time interval examined in this study (144 hours). The data of Figure 16 is replotted in Figure 17 as normalized intensity against the square root of time. The essentially linear plot for $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ indicates that the formation of this phase could be diffusion controlled.

$\text{Ba}_2\text{Ti}_9\text{O}_{20}$ was not observed until after 8 hours into the reaction. This delay indicates that a nucleation barrier might exist for the formation of this phase. After 8 hours, the intensity of the selected $\text{Ba}_2\text{Ti}_9\text{O}_{20}$ peaks is seen to increase with time (Figure 14) indicating normal growth.

$\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ is the only equilibrium barium titanate phase of composition between those of the two reactants which was not observed during the course of the reaction. It is possible that $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ did form, but in an amount below the detection limit (~ 3 w/o). More probably, however, $\text{Ba}_6\text{Ti}_{17}\text{O}_{40}$ was prevented from forming by a nucleation barrier.

$\text{BaTi}_5\text{O}_{11}$, which was found by O'Bryan and Thomson in a mixture of the same stoichiometry as the mixture used in this study and at a similar reaction temperature (1100°C), was not observed during the course of reaction. Perhaps $\text{BaTi}_5\text{O}_{11}$ is stable at 1100°C , but not at 1050°C or perhaps it is stabilized by CO_2 or by impurities present in O'Bryan and Thomson's mixture but not present in the mixture used in this study. The detection techniques used in the present study should have identified $\text{BaTi}_5\text{O}_{11}$ if it were present in the quantities found by O'Bryan and Thomson. $\text{BaTi}_6\text{O}_{13}$ and BaTi_2O_5 were also not observed, but since these phases form only from samples which have been melted and are thought not to be equilibrium phases at 1050°C , their absence was expected.

Templeton and Pask[4] studied the formation of BaTiO_3 from equimolar mixtures of BaCO_3 and TiO_2 , heated at different temperatures and in different atmospheres. Their data for an equimolar mixture of BaCO_3 and TiO_2 , heated at 1050°C in air, are shown in Table 8 for comparison with the data of Table 7. At the time of their work, not all of the phases in the BaO-TiO_2 system were known, but they were able to identify Ba_2TiO_4 , BaTiO_3 , $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$, and BaTi_4O_9 after only 15 minutes at 1050°C . In their Table, they report the mole fractions of these phases, but the peaks which they selected for quantitative analysis have been shown to overlap with peaks from other phases.

Templeton and Pask concluded that BaTiO_3 forms initially at the $\text{BaCO}_3 - \text{TiO}_2$ interface. After this initial step, Ba_2TiO_4 is reported to form between the BaTiO_3 layer and BaCO_3 , and $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 to form between the BaTiO_3 layer and TiO_2 . Assuming this model, the reaction which proceeds into the TiO_2 ceramic can be viewed

as a reaction between BaTiO_3 and TiO_2 , and the formation of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 is expected from examination of the phase diagram (Figure 2) if local thermodynamic equilibrium is approached and if nucleation occurs.

The results of the present study, as well as the results of Templeton and Pask, show that $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 form readily with no apparent nucleation barrier. With this fact in mind, it does not seem likely that BaTiO_3 is the first phase formed at the TiO_2 interface. It is more likely that BaTi_4O_9 , $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$, and BaTiO_3 all form as soon as a reaction begins in order of their variation in BaO/TiO_2 content. This new model is consistent with the experimental observation that all of the phases described above are present in the reaction mixture of BaCO_3 and TiO_2 after only 15 minutes at 1050°C (Table 8). If diffusion through $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 is rapid, the relative thickness of these phases will be small, and hence the volume fractions will be small compared with those of BaTiO_3 and Ba_2TiO_4 .

In mixtures of BaCO_3 and TiO_2 heated at temperatures below 800°C , Cournil, Soustelle, and Thomas[6a] report that BaTiO_3 was the only phase formed. For the same reaction, Templeton and Pask[4] report a small amount (1 mole %) of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ after only one hour at 900°C and after 36 hours at 750°C , and they report a small amount of BaTi_4O_9 (1 mole %) after 22 hours at 750°C . Therefore, it is probable that these phases were also present in the samples of Cournil, et. al., but in amounts which were too small to detect.

In a second paper, Cournil, et. al.[6b] develop a detailed model in which TiO_2 is converted directly to BaTiO_3 during reaction with BaCO_3 by a series of reaction steps at various assumed interfaces. The authors then try to explain the effect of different gaseous atmospheres on the reaction rates in terms of their model. Their mechanistic approach should be considered with caution, however, because of their assumption that higher titanate phases do not form at the TiO_2 interface.

In a study of the formation of BaTiO_3 , Beauger, Mutin, and Niepce[5b] examined various interface reactions by scanning electron microscopy and electron probe microanalysis. Their samples consisted of sintered pellets of BaCO_3 , Ba_2TiO_4 , BaTiO_3 ,

and TiO_2 which were stacked together in different ways and heated at various temperatures. In their study of the BaTiO_3 - TiO_2 interface, they report the formation of a phase richer in titanium than BaTiO_3 in the TiO_2 ceramic, but the composition of the phase was not determined. They attribute the formation of this phase to the "excessive thickness" of the BaTiO_3 layer because they did not observe this phase when they calcined intimately mixed micrometric powders.

The results of the present study show that $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 form readily by reaction of BaTiO_3 and TiO_2 . Therefore, the unknown "phase" which was observed in the TiO_2 was most likely two phases: $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$, and BaTi_4O_9 . The statement about the excessive thickness of the BaTiO_3 layer being responsible for the formation of these phases deserves comment. The formation of a reaction product at an interface between two reactants depends only on the activity of each species at the interface and on the kinetic barrier which might keep a phase from forming. The thickness of the two reactants is unlikely to determine which phases are formed, but might determine which phases are detected if the reactants are much thicker than the product phases. The fact that these phases were not observed in the reaction of fine powders can be explained by the rapid rate of BaTiO_3 formation from fine powders.

In the work by Amin, Spears, and Kulwicki[22], the reaction of BaCO_3 with anatase and with rutile was followed by several techniques including x-ray diffraction. Their report of the presence of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ is based on the identification of a diffraction peak at 28.4° as the "principal peak" of this phase. The position of this peak from the data of Table 1 is 28.267° . The 022,040 peak of BaTi_4O_9 lies at 28.358° . Therefore, the peak found by Amin, et. al. at 28.5° might alternatively be attributed to this phase. Furthermore, their measurements, which are reported only for the two-theta range $22.7 - 35.5^\circ$, show the presence of a peak at $\sim 26.0^\circ$ after 1800s and 3600s at 910°C . If $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 are considered to be the only intermediate phases formed, this peak could be assigned as the 302 peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ (26.178° in Table 1). A peak at $\sim 23.0^\circ$ is observed in their data for the sample heated 1800s. It is possible that this is the 031 peak of BaTi_4O_9 (at 23.197° in Table 1).

7 Conclusion

Careful analysis of the BaTiO_3 - TiO_2 reaction by x-ray diffraction has shown that $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 form readily without a significant nucleation barrier. The work of several other authors[4,5,6,22] was reexamined in light of these observations. The assumption that BaTiO_3 is the first phase formed at the TiO_2 interface during reaction of BaCO_3 and TiO_2 has been questioned. An alternate model is suggested in which each of the barium titanate phases which form without a significant nucleation barrier are formed in order of highest TiO_2 content by diffusion into TiO_2 . Thus, BaTi_4O_9 is the first phase formed, followed by the formation of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$, and BaTiO_3 . The reported absence of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$ and BaTi_4O_9 in many studies can be attributed to their being present in low volume fractions because diffusion through their layers is rapid.

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TABLE 1 : Xray Diffraction Data For Barium Titanate Phases

2θ (deg)	$d(\text{\AA})$	I/I_{max}	hkl	Phase
11.406	7.7519	20	120	Ba ₆ Ti ₁₇ O ₄₀
13.981	6.3291	11	220	Ba ₆ Ti ₁₇ O ₄₀
15.316	5.7803	20	011	BaTi ₄ O ₉
16.296	5.4348	15	211, 220	Ba ₄ Ti ₁₃ O ₃₀
17.189	5.1546	10	120	BaTi ₅ O ₁₁
18.619	4.7619	15	021	BaTi ₄ O ₉
18.976	4.6729	15	131	Ba ₆ Ti ₁₇ O ₄₀
19.066	4.6512	25	102, 131	Ba ₄ Ti ₁₃ O ₃₀
19.334	4.5872	30	200	BaTi ₂ O ₅
20.769	4.2735	60	022, 040	Ba ₄ Ti ₁₃ O ₃₀
21.307	4.1667	50	140	Ba ₆ Ti ₁₇ O ₄₀
21.577	4.1152	10	-104, 004	BaTi ₂ O ₅
22.026	4.0323	40	231	Ba ₄ Ti ₁₃ O ₃₀
22.026	4.0323	12	001	BaTiO ₃
22.296	3.9841	25	100	BaTiO ₃
22.476	3.9526	25	031	BaTi ₅ O ₁₁
23.197	3.8314	40	031	BaTi ₄ O ₉
23.467	3.7879	50	200	BaTi ₅ O ₁₁
23.828	3.7313	35	-322, 331	Ba ₆ Ti ₁₇ O ₄₀
23.828	3.7313	35	002	BaTi ₅ O ₁₁
23.918	3.7175	15		Ba ₂ Ti ₉ O ₂₀
24.640	3.6101	9	-511	Ba ₆ Ti ₁₇ O ₄₀
25.182	3.5336	35		Ba ₂ Ti ₉ O ₂₀
25.273	3.5211	12	400	Ba ₄ Ti ₁₃ O ₃₀
25.363	3.5088	40	040	BaTi ₅ O ₁₁
25.545	3.4843	15	-204, 104	BaTi ₂ O ₅
25.907	3.4364	40	11-2	BaTi ₅ O ₁₁
26.178	3.4014	30	302	Ba ₄ Ti ₁₃ O ₃₀
26.269	3.3898	60		Ba ₂ Ti ₉ O ₂₀
25.545	3.4843	75	210	Al ₂ O ₃
26.632	3.3445	40	220	BaTi ₅ O ₁₁
27.085	3.2895	45	022	BaTi ₅ O ₁₁
27.085	3.2895	55		Ba ₂ Ti ₉ O ₂₀
27.267	3.2680	30	431, 511	Ba ₆ Ti ₁₇ O ₄₀
27.42	3.25	40	100	BaTi ₄ O ₉
27.448	3.2468	60	411	Ba ₄ Ti ₁₃ O ₃₀
27.448	3.2468	100	110	TiO ₂
27.631	3.2258	30	051	Ba ₆ Ti ₁₇ O ₄₀
27.903	3.1949	30	013	Ba ₆ Ti ₁₇ O ₄₀
27.994	3.1847	50	-213	Ba ₆ Ti ₁₇ O ₄₀
27.994	3.1847	100	140, 041	BaTi ₅ O ₁₁
28.267	3.1546	60	402	Ba ₆ Ti ₁₇ O ₄₀
28.267	3.1546	100	322, 113+	Ba ₄ Ti ₁₃ O ₃₀
28.267	3.1546	10	-113	BaTi ₂ O ₅
28.358	3.1447	80	002, 041	BaTi ₄ O ₉
28.449	3.1348	100		Ba ₂ Ti ₉ O ₂₀
28.631	3.1153	20	600	Ba ₆ Ti ₁₇ O ₄₀
28.723	3.1056	10	-302	BaTi ₂ O ₅
28.814	3.0960	85	-251, -531	Ba ₆ Ti ₁₇ O ₄₀
29.179	3.0581	90	-611, 113+	Ba ₆ Ti ₁₇ O ₄₀
29.179	3.0581	85		Ba ₂ Ti ₉ O ₂₀
29.270	3.0488	30	300	BaTi ₂ O ₅
29.726	3.0030	100	---	BaTi ₂ O ₅
29.909	2.9851	60	-342	Ba ₆ Ti ₁₇ O ₄₀
29.909	2.9851	100	130	BaTi ₄ O ₉
30.000	2.9762	25		Ba ₂ Ti ₉ O ₂₀
30.091	2.9674	100	121	BaTi ₄ O ₉
30.274	2.9499	7	242	Ba ₆ Ti ₁₇ O ₄₀
30.457	2.9326	30	213, 242	Ba ₄ Ti ₁₃ O ₃₀
30.732	2.9070	100	221	BaTi ₅ O ₁₁

TABLE 1 (cont.) : Xray Diffraction Data For Barium Titanate Phases

2θ (deg)	$d(\text{\AA})$	$I/I_{\max}$	hkl	Phase
30.732	2.9070	15	113	BaTi ₂ O ₅
30.732	2.9070	20		Ba ₂ Ti ₉ O ₂₀
30.915	2.8902	50	20-2	BaTi ₅ O ₁₁
31.190	2.8653	10	211	BaTi ₂ O ₅
31.282	2.8571	85	402, 431	Ba ₄ Ti ₁₃ O ₃₀
31.282	2.8571	5	???	BaTi ₄ O ₉
31.373	2.8490	100	-133, 060	Ba ₆ Ti ₁₇ O ₄₀
31.465	2.8409	40	13-2	BaTi ₅ O ₁₁
31.465	2.8409	100	101	BaTiO ₃
31.648	2.8249	100	110	BaTiO ₃
31.832	2.8090	40	351	Ba ₆ Ti ₁₇ O ₄₀
32.015	2.7933	60	133	Ba ₄ Ti ₁₃ O ₃₀
32.015	2.7933	55		Ba ₂ Ti ₉ O ₂₀
32.291	2.7701	30	-304	BaTi ₂ O ₅
32.475	2.7548	8	342	Ba ₆ Ti ₁₇ O ₄₀
32.659	2.7397	10	006	BaTi ₂ O ₅
32.751	2.7322	9	-631	Ba ₆ Ti ₁₇ O ₄₀
32.751	2.7322	30		Ba ₂ Ti ₉ O ₂₀
32.935	2.7174	12	422, 440	Ba ₄ Ti ₁₃ O ₃₀
33.488	2.6738	10	302	BaTi ₂ O ₅
33.579	2.6667	25		Ba ₂ Ti ₉ O ₂₀
33.672	2.6596	75	313, 342+	Ba ₄ Ti ₁₃ O ₃₀
33.949	2.6385	20	522	Ba ₆ Ti ₁₇ O ₄₀
33.949	2.6385	10	260	Ba ₄ Ti ₁₃ O ₃₀
33.949	2.6385	50	032, 051	BaTi ₄ O ₉
34.041	2.6316	9	-513	Ba ₆ Ti ₁₇ O ₄₀
34.503	2.5974	20	451	Ba ₆ Ti ₁₇ O ₄₀
35.151	2.5510	90	104	Al ₂ O ₃
35.151	2.5510	9	720	Ba ₆ Ti ₁₇ O ₄₀
35.706	2.5126	50	-301, 24-1	BaTi ₅ O ₁₁
36.077	2.4876	50	101	TiO ₂
36.448	2.4631	11	602, 062+	Ba ₆ Ti ₁₇ O ₄₀
36.448	2.4631	10	004, 062	Ba ₄ Ti ₁₃ O ₃₀
36.635	2.4510	25		Ba ₂ Ti ₉ O ₂₀
36.728	2.4450	15	502, 531	Ba ₄ Ti ₁₃ O ₃₀
37.007	2.4272	11	-731, -262	Ba ₆ Ti ₁₇ O ₄₀
37.100	2.4213	20	102, 060	BaTi ₄ O ₉
37.287	2.4096	20		Ba ₂ Ti ₉ O ₂₀
37.752	2.3810	40	110	Al ₂ O ₃
37.846	2.3753	10	-313	BaTi ₂ O ₅
38.407	2.3419	8	262	Ba ₆ Ti ₁₇ O ₄₀
38.501	2.3364	15	124, 153+	Ba ₄ Ti ₁₃ O ₃₀
38.593	2.3310	15	542	Ba ₆ Ti ₁₇ O ₄₀
38.593	2.3310	15	115, 311	BaTi ₂ O ₅
38.874	2.3148	45	111	BaTiO ₃
39.062	2.3041	10	122, 150	BaTi ₄ O ₉
39.154	2.2989	20		Ba ₂ Ti ₉ O ₂₀
39.154	2.2989	8	200	TiO ₂
39.248	2.2936	50	400	BaTi ₂ O ₅
39.436	2.2831	35	204, 271	Ba ₆ Ti ₁₇ O ₄₀
39.998	2.2523	35	-462	Ba ₆ Ti ₁₇ O ₄₀
40.186	2.2422	15	253, 271	Ba ₄ Ti ₁₃ O ₃₀
40.186	2.2422	55		Ba ₂ Ti ₉ O ₂₀
40.282	2.2371	20		BaTi ₂ O ₅
40.376	2.2321	11	362, 253	Ba ₆ Ti ₁₇ O ₄₀
41.222	2.1882	25	111	TiO ₂
41.412	2.1786	80	304, 362	Ba ₄ Ti ₁₃ O ₃₀
41.412	2.1786	50	232	BaTi ₅ O ₁₁
41.695	2.1645	1	006	Al ₂ O ₃
41.790	2.1598	20	132, 151	BaTi ₄ O ₉

TABLE 1 (cont.) : Xray Diffraction Data For Barium Titanate Phases

2θ (deg)	$d(\text{\AA})$	I/I_{max}	hkl	Phase
41.979 42.073 42.735 42.735 42.830	2.1505 2.1459 2.1142 2.1142 2.1097	75 25 65 25 20	-471 462 602, 324 161	Ba ₂ Ti ₉ O ₂₀ Ba ₆ Ti ₁₇ O ₄₀ Ba ₆ Ti ₁₇ O ₄₀ Ba ₄ Ti ₁₃ O ₃₀ BaTi ₅ O ₁₁
43.021 43.209 43.400 43.400 43.495	2.1008 2.0921 2.0833 2.0833 2.0790	55 50 100 45 45	402 113 -604 144	Ba ₂ Ti ₉ O ₂₀ BaTi ₂ O ₅ Al ₂ O ₃ Ba ₆ Ti ₁₇ O ₄₀ Ba ₆ Ti ₁₇ O ₄₀
43.971 44.065 44.065 44.160 44.352	2.0576 2.0534 2.0534 2.0492 2.0408	20 11 10 50 8	-208, -117 640 210 340 404, -813+	BaTi ₂ O ₅ Ba ₄ Ti ₁₃ O ₃₀ TiO ₂ BaTi ₅ O ₁₁ Ba ₆ Ti ₁₇ O ₄₀
44.542 44.637 44.828 44.828 44.828	2.0325 2.0284 2.0202 2.0202 2.0202	20 30 8 15 12	242 380, 453 017 002	Ba ₂ Ti ₉ O ₂₀ BaTi ₅ O ₁₁ Ba ₆ Ti ₁₇ O ₄₀ BaTi ₂ O ₅ BaTiO ₃
44.924 45.019 45.116 45.306 45.402	2.0161 2.0121 2.0080 2.0000 1.9960	55 40 15 11 10	404, 462 -662 533 -217	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉ Ba ₆ Ti ₁₇ O ₄₀ Ba ₄ Ti ₁₃ O ₃₀ BaTi ₂ O ₅
45.402 45.593 46.169 46.169 46.264	1.9960 1.9881 1.9646 1.9646 1.9608	35 15 2 15 15	200 562, 424 202 020 471, 711	BaTiO ₃ Ba ₆ Ti ₁₇ O ₄₀ Al ₂ O ₃ BaTi ₂ O ₅ Ba ₄ Ti ₁₃ O ₃₀
46.361 46.553 46.746 47.225 47.225	1.9569 1.9493 1.9417 1.9231 1.9231	20 20 25 20 10	-544, 073 27-3 115, 173+ -671 120	Ba ₆ Ti ₁₇ O ₄₀ Ba ₆ Ti ₁₇ O ₄₀ Ba ₄ Ti ₁₃ O ₃₀ Ba ₆ Ti ₁₇ O ₄₀ BaTi ₂ O ₅
47.225 47.225 47.902 47.999 48.577	1.9231 1.9231 1.8975 1.8939 1.8727	25 25 5 25 10	642 524, 940	BaTi ₄ O ₉ Ba ₂ Ti ₉ O ₂₀ Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉ Ba ₆ Ti ₁₇ O ₄₀
48.771 48.967 48.967 49.062 49.355	1.8657 1.8587 1.8587 1.8553 1.8450	35 50 10 40 15	931, 662 504, 562 215, -335+	Ba ₆ Ti ₁₇ O ₄₀ BaTi ₅ O ₁₁ BaTi ₄ O ₉ Ba ₄ Ti ₁₃ O ₃₀ Ba ₆ Ti ₁₇ O ₄₀
49.645 49.645 49.743 49.938 50.035	1.8349 1.8349 1.8315 1.8248 1.8215	20 15 10 20 35	-804 -504, 404	Ba ₆ Ti ₁₇ O ₄₀ BaTi ₂ O ₅ BaTi ₄ O ₉ BaTi ₄ O ₉ Ba ₂ Ti ₉ O ₂₀
50.425 50.620 50.620 50.620 51.011	1.8083 1.8018 1.8018 1.8018 1.7889	9 15 10 6 8	660, 315 235, 291 -222, 315 102 201	Ba ₄ Ti ₁₃ O ₃₀ Ba ₄ Ti ₁₃ O ₃₀ BaTi ₂ O ₅ BaTiO ₃ BaTiO ₃
51.109 51.208 51.303 51.502 51.794	1.7857 1.7825 1.7794 1.7730 1.7637	7 20 11 10 11	210 -582, -744 -862, 680	BaTiO ₃ Ba ₂ Ti ₉ O ₂₀ Ba ₆ Ti ₁₇ O ₄₀ BaTi ₄ O ₉ Ba ₆ Ti ₁₇ O ₄₀

TABLE 1 (cont.) : Xray Diffraction Data For Barium Titanate Phases

2 θ (deg)	d(Å)	I/I _{max}	hkl	Phase
51.892	1.7606	11	-535	Ba ₆ Ti ₁₇ O ₄₀
52.582	1.7391	45	202	Al ₂ O ₃
52.877	1.7301	5	364	Ba ₄ Ti ₁₃ O ₃₀
53.171	1.7212	11	811	Ba ₄ Ti ₁₃ O ₃₀
53.568	1.7094	15	335	Ba ₆ Ti ₁₇ O ₄₀
53.963	1.6978	7	544, 604	Ba ₄ Ti ₁₃ O ₃₀
54.063	1.6949	25		BaTi ₄ O ₉
54.260	1.6892	15	-513, -511	BaTi ₂ O ₅
54.260	1.6892	15		Ba ₂ Ti ₉ O ₂₀
54.361	1.6863	60	211	TiO ₂
55.354	1.6584	10	2.10.0	Ba ₄ Ti ₁₃ O ₃₀
55.455	1.6556	15	820, 831	Ba ₄ Ti ₁₃ O ₃₀
55.653	1.6502	20		BaTi ₅ O ₁₁
55.855	1.6447	20	435, 464+	Ba ₄ Ti ₁₃ O ₃₀
55.955	1.6420	15	112	BaTiO ₃
56.253	1.6340	35	211	BaTiO ₃
56.653	1.6234	20	220	TiO ₂
56.756	1.6207	10		BaTi ₄ O ₉
57.056	1.6129	40		Ba ₂ Ti ₉ O ₂₀
57.257	1.6077	15	515, 573+	Ba ₄ Ti ₁₃ O ₃₀
57.359	1.6051	15	-324, 224	BaTi ₂ O ₅
57.559	1.6000	80	116	Al ₂ O ₃
57.559	1.6000	45		Ba ₂ Ti ₉ O ₂₀
58.264	1.5823	30		BaTi ₄ O ₉
58.467	1.5773	6	644	Ba ₄ Ti ₁₃ O ₃₀
58.769	1.5699	25		BaTi ₄ O ₉
59.175	1.5601	30	1.0.10	BaTi ₂ O ₅
59.279	1.5576	25	704, 762	Ba ₄ Ti ₁₃ O ₃₀
59.684	1.5480	10		BaTi ₄ O ₉
59.786	1.5456	4		Al ₂ O ₃
60.194	1.5361	20		BaTi ₄ O ₉
60.806	1.5221	15		Ba ₂ Ti ₉ O ₂₀
61.215	1.5129	6	122	Al ₂ O ₃
61.318	1.5106	8	018	Al ₂ O ₃
61.526	1.5060	15	513, 4.0.10	BaTi ₂ O ₅
61.626	1.5038	15		Ba ₂ Ti ₉ O ₂₀
61.936	1.4970	10		BaTi ₄ O ₉
62.038	1.4948	15	-419	BaTi ₂ O ₅
62.246	1.4903	10	420	BaTi ₂ O ₅
62.761	1.4793	10	002	TiO ₂
63.175	1.4706	25		BaTi ₅ O ₁₁
64.006	1.4535	10		BaTi ₄ O ₉
64.006	1.4535	10	210	TiO ₂
64.633	1.4409	25		Ba ₂ Ti ₉ O ₂₀
64.739	1.4388	25		BaTi ₅ O ₁₁
65.156	1.4306	10	422	BaTi ₂ O ₅
65.366	1.4265	30		Ba ₂ Ti ₉ O ₂₀
65.470	1.4245	10	-2.1.11, 228	BaTi ₂ O ₅
65.470	1.4245	2	221	TiO ₂
65.787	1.4184	12	202	BaTiO ₃
65.996	1.4144	25		Ba ₂ Ti ₉ O ₂₀
66.102	1.4124	10	220	BaTiO ₃
66.522	1.4045	30	124	Al ₂ O ₃
67.051	1.3947	30	611	BaTi ₂ O ₅
67.154	1.3928	35	-5.0.10	BaTi ₂ O ₅
67.368	1.3889	35	417, -3.1.11	BaTi ₂ O ₅
68.221	1.3736	50	030	Al ₂ O ₃
68.221	1.3736	10	-328, 128	BaTi ₂ O ₅
68.970	1.3605	20	301	TiO ₂
69.290	1.3550	20		Ba ₂ Ti ₉ O ₂₀

TABLE 1 (cont.) : Xray Diffraction Data For Barium Titanate Phases

2θ (deg)	$d(\text{\AA})$	$I/I_{\max}$	hkl	Phase
69.501	1.3514	10		BaTi ₄ O ₉
69.828	1.3459	12	112	TiO ₂
70.040	1.3423	15	-524, 424	BaTi ₂ O ₅
70.365	1.3369	2	125	Al ₂ O ₃
70.365	1.3369	5	212	BaTiO ₃
70.687	1.3316	2	221	BaTiO ₃
71.446	1.3193	15		Ba ₂ Ti ₉ O ₂₀
72.429	1.3038	2	311	TiO ₂
74.302	1.2755	4	208	Al ₂ O ₃
74.302	1.2755	5	103	BaTiO ₃
75.080	1.2642	7	301	BaTiO ₃
75.192	1.2626	9	310	BaTiO ₃
76.199	1.2484	20		BaTi ₄ O ₉
76.532	1.2438	4	202	TiO ₂
76.868	1.2392	15	1.0.10	Al ₂ O ₃
77.207	1.2346	8	119	Al ₂ O ₃
78.001	1.2240	10	330	BaTi ₄ O ₉
78.799	1.2136	3	113	BaTiO ₃
78.915	1.2121	20		BaTi ₄ O ₉
79.488	1.2048	5	311	BaTiO ₃
79.830	1.2005	2	212	TiO ₂
80.637	1.1905	10		BaTi ₄ O ₉
80.752	1.1891	8	220	Al ₂ O ₃
80.990	1.1862	15	-626	BaTi ₂ O ₅
81.222	1.1834	10	3.1.11	BaTi ₂ O ₅
82.387	1.1696	6	321	TiO ₂
83.097	1.1614	10	6.1.11, -7.0.10	BaTi ₂ O ₅
83.210	1.1601	1	306	Al ₂ O ₃
83.333	1.1587	10		BaTi ₄ O ₉
83.448	1.1574	7	222	BaTiO ₃
84.278	1.1481	4	400	TiO ₂
84.396	1.1468	6	223	Al ₂ O ₃
85.230	1.1377	2	311	Al ₂ O ₃
86.321	1.1261	6	312	Al ₂ O ₃
86.560	1.1236	4	128	Al ₂ O ₃
87.043	1.1186	1	203	BaTiO ₃
87.287	1.1161	1	302	BaTiO ₃
87.533	1.1136	20		BaTi ₄ O ₉
87.533	1.1136	2	410	TiO ₂
88.149	1.1074	1	320	BaTiO ₃
89.134	1.0977	8	0.2.10	Al ₂ O ₃
89.506	1.0941	8	222	TiO ₂
90.663	1.0834	4	0.0.12	Al ₂ O ₃
90.633	1.0834	4	330	TiO ₂
91.258	1.0776	8	134	Al ₂ O ₃
91.509	1.0753	7	213	BaTiO ₃
92.149	1.0695	12	312	BaTiO ₃
92.272	1.0684	12	321	BaTiO ₃
95.372	1.0417	15	226	Al ₂ O ₃
95.372	1.0417	6	411	TiO ₂
96.030	1.0363	6	312	TiO ₂
97.227	1.0267	4	420	TiO ₂
98.436	1.0173	2	402	Al ₂ O ₃
99.521	1.0091	1	004	BaTiO ₃

**Table 2: Peaks Selected for Phase Identification
and Quantitative Analysis**

Phase	2 θ (degrees)	d(Å)	hkl	I/I _{max} (%)	
BaTiO ₃	92.149	1.0695	312	12	QA†
	92.272	1.0684	321	12	QA
Ba ₆ Ti ₁₇ O ₄₀	34.503	2.5974	451	20	QA
Ba ₄ Ti ₁₃ O ₃₀	19.066	4.6512	102, 131	25	QA
	20.769	4.2735	022, 040	60	
BaTi ₄ O ₉	18.619	4.7619	021	15	QA
	23.197	3.8314	031	40	
Ba ₂ Ti ₉ O ₂₀	60.806	1.5221	---	15	
	71.446	1.3193	---	15	
BaTi ₅ O ₁₁	17.189	5.1546	120	10	
	63.175	1.4706	---	25	
TiO ₂	36.077	2.4876	101	50	QA
	62.761	1.4793	002	10	QA
Al ₂ O ₃	37.752	2.3810	110	40	QA
	52.556	1.7399	024	42	QA

† Denotes peaks which are used for quantitative analysis.

Table 3: Properties of Raw Materials

Material	TiO ₂ (Rutile)	BaTiO ₃	Al ₂ O ₃
Manufacturer	Johnson Mathey Co. Puratronic Grade	Johnson Mathey Co. Puratronic Grade	Baker Chemical Co. Reagent Grade
Batch No.	S94967C	S93020C	106177
Manufacturers List- ed Impurities	Ca 10 ppm Mg 2 ppm Si 5 ppm Ag 1 ppm	Si 10 ppm Mg 1 ppm Ca < 1 ppm	Cl 0.002 % SO ₄ < 0.003 % Pb < 0.0005 % Fe < 0.02 %
Largest Particle Size (SEM)	< 80 μ m	< 40 μ m	< 75 μ m
Surface Area (BET)	1.3 m ² /g	2.7 m ² /g	---
Equivalent Spherical Radius (BET)	0.53 μ m	0.29 μ m	---

Table 4: Summary of Samples

Sample ID	Time at 1050 °C	Weight Fraction Al ₂ O ₃ [†]
Sraw	Unfired	0.2982
S24M	0.4 Hr	0.3001
S01H	1 Hr	0.3001
S02H	2 Hr	0.3003
S08H	8 Hr	0.3001
S24H	24 Hr	0.2999
S48H	48 Hr	0.3000
S06D	144 Hr	0.3000

[†] Added after reaction as standard for quantitative analysis.

Table 5a: Results of IDR Peak Search for Sample Sraw

Peak	2 θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2 θ (deg)
1	22.147	4.0106	14235	0.421	BaTiO ₃	001, 100	22.208
2	23.942	3.7138	1137	0.527	?		
3	25.589	3.4784	3890	0.200	Al ₂ O ₃	210	25.545
4	27.439	3.2479	19231	0.227	TiO ₂	110	27.448
5	31.529	2.8353	72521	0.360	BaTiO ₃	101,110	31.506
6	35.152	2.5509	6219	0.200	Al ₂ O ₃	104	35.151
7	36.075	2.4877	8710	0.220	TiO ₂	101	36.077
8	37.791	2.3786	2747	0.232	Al ₂ O ₃	110	37.752
9	38.885	2.3142	19779	0.309	BaTiO ₃	111	38.874
10	41.246	2.1870	4241	0.232	TiO ₂	111	41.222
11	43.376	2.0844	6561	0.215	Al ₂ O ₃	113	43.400
12	44.090	2.0523	1053	0.194	TiO ₂	210	44.065
13	45.332	1.9989	23556	0.598	BaTiO ₃	200	45.402
14	50.972	1.7902	6649	0.612	BaTiO ₃	201, 210	51.057
15	52.572	1.7394	3211	0.238	Al ₂ O ₃	202	52.582
16	54.341	1.6869	12073	0.274	TiO ₂	211	54.361
17	56.238	1.6344	26911	0.581	BaTiO ₃	211	56.253
18	57.527	1.6008	7427	0.268	Al ₂ O ₃	116	57.559
19	61.305	1.5109	1065	0.367	Al ₂ O ₃	122, 018	61.274
20	62.775	1.4790	1581	0.256	TiO ₂	002	62.761
21	64.095	1.4517	1613	0.269	TiO ₂	210	64.006
22	65.881	1.4166	12462	0.630	BaTiO ₃	202, 220	65.930
23	66.522	1.4045	2912	0.288	Al ₂ O ₃	124	66.522
24	68.226	1.3735	4070	0.315	Al ₂ O ₃	030	68.221
25	69.045	1.3592	2983	0.226	TiO ₂	301	68.970
26	69.820	1.3460	1521	0.227	TiO ₂	112	69.826
27	70.456	1.3354	3034	0.544	Al ₂ O ₃	125	70.365
					BaTiO ₃	212, 221	70.457
28	75.067	1.2644	10369	0.925	BaTiO ₃	301, 310	75.143
29	76.875	1.2391	2422	0.503	Al ₂ O ₃	1.0.10	76.868
30	79.393	1.2060	4521	0.824	BaTiO ₃	113, 311	79.230
31	80.670	1.1901	742	0.401	Al ₂ O ₃	220	80.752
32	82.369	1.1698	1071	0.349	TiO ₂	321	82.387
33	83.483	1.1570	3113	0.453	BaTiO ₃	222	83.448
34	87.780	1.1111	1416	0.792	TiO ₂	410	87.533
35	89.547	1.0937	1386	0.309	TiO ₂	222	89.506
36	90.740	1.0824	751	0.236	Al ₂ O ₃	00.12	90.663
					TiO ₂	330	90.633
37	92.027	1.0706	12970	1.027	BaTiO ₃	312, 321	92.211
38	95.263	1.0426	2736	0.421	Al ₂ O ₃	226	95.372
					TiO ₂	411	95.372

Table 5b: Results of IDR Peak Search for Sample S24M

Peak	2 θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2 θ (deg)
1					BaTi ₄ O ₉	021	18.619
2					Ba ₄ Ti ₁₃ O ₃₀	102, 131	19.066
3					Ba ₄ Ti ₁₃ O ₃₀	022, 040	20.769
4	22.254	3.9916	12810	0.378	BaTiO ₃	001, 100	22.208
5	25.647	3.4706	3953	0.217	Al ₂ O ₃	210	25.545
6	27.523	3.2382	18726	0.202	Ba ₄ Ti ₁₃ O ₃₀	411	27.448
7	28.410	3.1391	1131	0.236	TiO ₂	110	27.448
8	29.995	2.9767	1253	0.287	Ba ₄ Ti ₁₃ O ₃₀	322, 113	28.267
					BaTi ₄ O ₉	002, 041	28.358
					BaTi ₄ O ₉	130, 121	30.000
9	31.616	2.8277	68432	0.337	BaTiO ₃	101, 110	31.506
10	34.031	2.6323	870	0.315	Ba ₄ Ti ₁₃ O ₃₀	260	33.949
					BaTi ₄ O ₉	032, 051	33.949
11	35.245	2.5444	6775	0.206	Al ₂ O ₃	104	35.151
12	36.167	2.4816	7684	0.194	TiO ₂	101	36.077
13	37.886	2.3729	2520	0.234	Al ₂ O ₃	110	37.752
14	38.971	2.3093	17843	0.290	BaTiO ₃	111	38.874
					BaTi ₄ O ₉	122, 150	39.062
15	41.323	2.1831	3835	0.200	TiO ₂	111	41.222
					Ba ₄ Ti ₁₃ O ₃₀	304, 362	41.412
16	43.440	2.0815	7343	0.241	Al ₂ O ₃	113	43.400
17	44.153	2.0495	793	0.172	Ba ₄ Ti ₁₃ O ₃₀	640	44.065
					TiO ₂	210	44.065
18	45.416	1.9954	21068	0.569	Ba ₄ Ti ₁₃ O ₃₀	533	45.306
					BaTiO ₃	200	45.402
19	51.057	1.7874	6210	0.587	BaTiO ₃	201, 210	51.057
20	52.654	1.7369	2930	0.226	Al ₂ O ₃	202	52.582
21	54.421	1.6846	11804	0.250	TiO ₂	211	54.361
22	56.309	1.6325	25385	0.546	BaTiO ₃	211	56.253
23	57.614	1.5986	7177	0.277	Al ₂ O ₃	116	57.559
24	61.390	1.5090	811	0.312	Al ₂ O ₃	122, 018	61.274
25	62.818	1.4781	1601	0.259	TiO ₂	002	62.761
26	64.174	1.4501	1670	0.265	TiO ₂	210	64.006
					BaTi ₄ O ₉	202, 220	64.006
27	65.939	1.4155	11680	0.620	BaTiO ₃		65.930
28	66.597	1.4031	2699	0.274	Al ₂ O ₃	124	66.522
29	68.289	1.3724	3684	0.282	Al ₂ O ₃	030	68.221
30	69.097	1.3583	3027	0.238	TiO ₂	301	68.970
31	69.850	1.3455	1809	0.236	TiO ₂	112	69.826
32	70.553	1.3338	3060	0.556	Al ₂ O ₃	125	70.365
					BaTiO ₃	212, 221	70.457
33	75.164	1.2630	9721	0.918	BaTiO ₃	301, 310	75.143
34					BaTi ₄ O ₉	330	78.001
35	79.480	1.2049	4584	0.824	BaTiO ₃	113, 311	79.230
36	83.545	1.1563	3180	0.444	BaTiO ₃	222	83.448
37	84.387	1.1469	1002	0.388	TiO ₂	400	84.278
					Al ₂ O ₃	223	84.396
38	89.599	1.0932	945	0.164	TiO ₂	222	89.506
39	90.815	1.0817	858	0.260	Al ₂ O ₃	0.0.12	90.663
					TiO ₂	330	90.633
40	92.094	1.0700	11568	0.921	BaTiO ₃	312, 321	92.211
41	95.323	1.0421	2790	0.426	Al ₂ O ₃	226	95.372
					TiO ₂	411	95.372
42	97.278	1.0263	710	0.486	TiO ₂	420	97.227

Table 5c: Results of IDR Peak Search for Sample S01H

Peak	2 θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2 θ (deg)
1					BaTi ₄ O ₉	021	18.619
2					Ba ₄ Ti ₁₃ O ₃₀	102, 131	19.066
3					Ba ₄ Ti ₁₃ O ₃₀	022, 040	20.769
4	22.148	4.0104	10401	0.364	BaTiO ₃	001, 100	22.208
5	25.583	3.4791	3532	0.223	Al ₂ O ₃	210	25.545
6	27.440	3.2478	18952	0.191	Ba ₄ Ti ₁₃ O ₃₀	411	27.448
7	28.322	3.1486	1918	0.284	TiO ₂	110	27.448
8	30.025	2.9738	2512	0.373	Ba ₄ Ti ₁₃ O ₃₀	322, 113	28.267
9	31.532	2.8350	57658	0.348	BaTi ₄ O ₉	002, 041	28.358
10	33.942	2.6390	1186	0.336	BaTi ₄ O ₉	130, 121	30.000
11	35.161	2.5503	5925	0.221	BaTiO ₃	101, 110	31.506
12	36.086	2.4870	7503	0.199	Ba ₄ Ti ₁₃ O ₃₀	260	33.949
13	37.796	2.3783	2448	0.232	BaTi ₄ O ₉	032, 051	33.949
14	38.892	2.3138	15676	0.292	Al ₂ O ₃	104	35.151
15	41.254	2.1866	4046	0.201	TiO ₂	101	36.077
16	43.372	2.0846	6496	0.240	Al ₂ O ₃	110	37.752
17	44.088	2.0524	1047	0.202	BaTiO ₃	111	38.874
18	45.335	1.9988	20599	0.599	BaTi ₄ O ₉	122, 150	39.062
19	47.891	1.8979	655	0.307	TiO ₂	111	41.222
20	50.975	1.7901	5278	0.534	Ba ₄ Ti ₁₃ O ₃₀	304, 362	41.412
21	52.575	1.7393	3032	0.254	Al ₂ O ₃	113	43.400
22	54.341	1.6869	11774	0.253	Ba ₄ Ti ₁₃ O ₃₀	640	44.065
23	56.234	1.6345	20396	0.490	TiO ₂	210	44.065
24	56.642	1.6237	3895	0.215	Ba ₄ Ti ₁₃ O ₃₀	533	45.306
25	57.535	1.6006	5700	0.245	BaTiO ₃	200	45.402
26	61.314	1.5107	687	0.259	BaTi ₄ O ₉	642	47.902
27	62.737	1.4798	1572	0.255	BaTi ₄ O ₉	201, 210	47.999
28	64.095	1.4517	1747	0.279	Al ₂ O ₃	202	51.057
29	65.860	1.4170	11095	0.637	TiO ₂	211	52.582
30	66.522	1.4045	2712	0.273	TiO ₂	211	54.361
31	68.209	1.3738	3284	0.256	BaTiO ₃	211	56.253
32	69.016	1.3597	2966	0.255	TiO ₂	220	56.653
33	69.802	1.3463	1501	0.230	BaTi ₄ O ₉	116	56.756
34	70.462	1.3353	2673	0.549	Al ₂ O ₃	122, 018	57.559
35	75.080	1.2642	8975	0.860	Al ₂ O ₃	122, 018	61.274
36	79.401	1.2059	4265	0.812	TiO ₂	002	62.761
37	82.369	1.1698	994	0.343	TiO ₂	210	64.006
38	83.492	1.1569	2787	0.441	BaTi ₄ O ₉	202, 220	64.006
39	84.288	1.1480	1230	0.450	BaTiO ₃	124	65.930
40	86.397	1.1253	711	0.584	Al ₂ O ₃	030	66.522
41	87.592	1.1130	1119	0.832	TiO ₂	301	68.221
42	89.516	1.0940	1259	0.260	TiO ₂	112	68.970
43	90.740	1.0824	711	0.256	Al ₂ O ₃	125	69.826
44	92.038	1.0705	10483	0.921	BaTiO ₃	212, 221	70.457
45	95.275	1.0425	2802	0.454	BaTi ₄ O ₉	301, 310	75.143
46	97.215	1.0268	757	0.429	BaTiO ₃	330	78.001
47					TiO ₂	113, 311	79.230
					BaTi ₄ O ₉	321	82.387
					BaTiO ₃	222	83.333
					TiO ₂	400	84.278
					Al ₂ O ₃	223	84.396
					Al ₂ O ₃	312, 128	86.417
					BaTi ₄ O ₉	410	87.533
					TiO ₂	222	87.533
					TiO ₂	0012	90.663
					TiO ₂	330	90.633
					BaTiO ₃	312, 321	92.211
					Al ₂ O ₃	226	95.372
					TiO ₂	411	95.372
					TiO ₂	420	97.227

Table 5d: Results of IDR Peak Search for Sample S02H

Peak	2 θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2 θ (deg)
1					BaTi ₄ O ₉	021	18.619
2					Ba ₄ Ti ₁₃ O ₃₀	102, 131	19.066
3					Ba ₄ Ti ₁₃ O ₃₀	022, 040	20.769
4	22.182	4.0043	10798	0.371	Ba ₄ Ti ₁₃ O ₃₀	231	22.026
5	23.169	3.8359	843	0.248	BaTiO ₃	001, 100	22.208
					BaTi ₄ O ₉	031	23.197
6	25.587	3.4786	3768	0.200	Al ₂ O ₃	210	25.545
7	27.461	3.2453	18697	0.201	Ba ₄ Ti ₁₃ O ₃₀	411	27.448
					TiO ₂	110	27.448
8	28.343	3.1463	1733	0.224	Ba ₄ Ti ₁₃ O ₃₀	322, 113	28.267
					BaTi ₄ O ₉	002, 041	28.358
9	29.914	2.9846	1284	0.206	BaTi ₄ O ₉	130, 121	30.000
10	30.099	2.9666	1659	0.168	BaTi ₄ O ₉	130, 121	30.000
11	31.549	2.8335	59109	0.333	BaTiO ₃	101, 110	31.506
12	33.953	2.6382	1269	0.189	Ba ₄ Ti ₁₃ O ₃₀	260	33.949
					BaTi ₄ O ₉	032, 051	33.949
13	35.168	2.5498	6228	0.218	Al ₂ O ₃	104	35.151
14	36.087	2.4869	7793	0.193	TiO ₂	101	36.077
15	37.795	2.3784	2696	0.200	Al ₂ O ₃	110	37.752
16	38.911	2.3127	16175	0.291	BaTiO ₃	111	38.874
					BaTi ₄ O ₉	122, 150	39.062
17	41.262	2.1862	4070	0.220	TiO ₂	111	41.222
					Ba ₄ Ti ₁₃ O ₃₀	304, 362	41.412
18	43.374	2.0845	6930	0.223	Al ₂ O ₃	113	43.400
19	44.074	2.0530	1169	0.165	Ba ₄ Ti ₁₃ O ₃₀	640	44.065
					TiO ₂	210	44.065
20	45.376	1.9971	19097	0.573	Ba ₄ Ti ₁₃ O ₃₀	533	45.306
					BaTiO ₃	200	45.402
21	47.883	1.8982	733	0.211	Ba ₄ Ti ₁₃ O ₃₀	642	47.902
					BaTi ₄ O ₉	201, 210	47.999
22	51.002	1.7892	5709	0.574	BaTiO ₃		51.057
23	52.585	1.7390	3260	0.251	Al ₂ O ₃	202	52.582
24	54.375	1.6859	11334	0.252	TiO ₂	211	54.361
25	56.242	1.6343	20188	0.472	BaTiO ₃	211	56.253
26	56.680	1.6227	3978	0.225	TiO ₂	220	56.653
					BaTi ₄ O ₉		56.756
27	57.539	1.6005	6384	0.251	Al ₂ O ₃	116	57.559
28	60.009	1.5404	681	0.332	BaTi ₄ O ₉		60.194
29	61.318	1.5106	712	0.277	Al ₂ O ₃	122, 018	61.274
30	62.770	1.4791	1581	0.248	TiO ₂	002	62.761
31	64.095	1.4517	1741	0.301	BaTi ₄ O ₉		64.006
					TiO ₂	210	64.006
32	65.855	1.4171	11106	0.624	BaTiO ₃	202, 220	65.930
33	66.522	1.4045	2900	0.277	Al ₂ O ₃	124	66.522
34	68.221	1.3736	4025	0.312	Al ₂ O ₃	030	68.221
35	69.051	1.3591	2951	0.228	TiO ₂	301	68.970
36	69.814	1.3461	1454	0.209	TiO ₂	112	69.826
37	70.462	1.3353	2692	0.531	Al ₂ O ₃	125	70.365
					BaTiO ₃	212, 221	70.457
38	75.108	1.2638	8949	0.852	BaTiO ₃	301, 310	75.143
39	76.882	1.2390	1321	0.273	Al ₂ O ₃	1.0.10	76.868
40					BaTi ₄ O ₉	330	78.001
41	79.401	1.2059	4176	0.748	BaTiO ₃	113, 311	79.230
42	83.510	1.1567	2955	0.445	BaTi ₄ O ₉		83.333
					BaTiO ₃	222	83.448
43	84.351	1.1473	889	0.323	TiO ₂	400	84.278
					Al ₂ O ₃	223	84.396
44	89.537	1.0938	808	0.148	TiO ₂	222	89.506
45	90.772	1.0821	877	0.264	Al ₂ O ₃	0.0.12	90.663
					TiO ₂	330	90.633
46	92.094	1.0700	10957	0.908	BaTiO ₃	312, 321	92.210
47	95.287	1.0424	1750	0.264	Al ₂ O ₃	226	95.372
					TiO ₂	411	95.372

Table 5e: Results of IDR Peak Search for Sample S08H

Peak	2θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2θ (deg)
1					BaTi ₄ O ₉	021	18.619
2					Ba ₄ Ti ₁₃ O ₃₀	102, 131	19.066
3	20.822	4.2626	813	0.199	Ba ₄ Ti ₁₃ O ₃₀	022, 040	20.769
4	22.170	4.0064	11966	0.423	Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃	231 001, 100	22.026 22.208
5	23.154	3.8384	939	0.187	BaTi ₄ O ₉	031	23.197
6	25.599	3.4770	4388	0.212	Al ₂ O ₃	210	25.545
7	27.473	3.2440	17215	0.198	Ba ₄ Ti ₁₃ O ₃₀ TiO ₂	411 110	27.448 27.448
8	28.350	3.1456	3322	0.210	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉	322, 113 002, 041	28.267 28.358
9	29.992	2.9843	4662	0.225	Ba ₂ Ti ₉ O ₂₀ BaTi ₄ O ₉ Ba ₂ Ti ₉ O ₂₀	130, 121 30.000 30.000	28.449 30.000 30.000
10	31.561	2.8325	56969	0.330	BaTiO ₃	101, 110	31.506
11	33.721	2.6558	1063	0.233	Ba ₂ Ti ₉ O ₂₀		33.579
12	33.962	2.6375	1690	0.192	Ba ₄ Ti ₁₃ O ₃₀ Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉	313, 342 260 032, 051	33.672 33.949 33.949
13	35.175	2.5493	6286	0.206	Al ₂ O ₃	104	35.151
14	36.107	2.4856	6736	0.209	TiO ₂	101	36.077
15	37.803	2.3779	2864	0.232	Al ₂ O ₃	110	37.752
16	38.916	2.3124	16047	0.292	BaTiO ₃ BaTi ₄ O ₉	111 122, 150	38.874 39.062
17	41.280	2.1853	4194	0.250	TiO ₂	111	41.222
18	43.387	2.0839	6623	0.225	Ba ₄ Ti ₁₃ O ₃₀	304, 362	41.412
19	44.079	2.0528	1151	0.188	Al ₂ O ₃ Ba ₄ Ti ₁₃ O ₃₀ TiO ₂	113 640 210	43.400 44.065 44.065
20	45.371	1.9973	19156	0.592	Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃	533 200	45.306 45.402
21	47.899	1.8976	1035	0.200	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉ BaTiO ₃	642 201, 210	47.902 47.999 51.057
22	51.002	1.7892	5845	0.608			
23	52.588	1.7389	3309	0.279	Al ₂ O ₃	202	52.582
24	54.375	1.6859	10062	0.231	Ba ₂ Ti ₉ O ₂₀		54.260
25	56.264	1.6337	20590	0.485	TiO ₂	211	54.361
26	56.680	1.6227	3437	0.198	BaTiO ₃ TiO ₂ BaTi ₄ O ₉	211 220	56.253 56.653 56.756
27	57.539	1.6005	6473	0.241	Al ₂ O ₃	116	57.559
28	60.013	1.5403	745	0.279	Ba ₂ Ti ₉ O ₂₀ BaTi ₄ O ₉		57.559 60.194
29					Ba ₂ Ti ₉ O ₂₀	122, 018	60.806
30	61.332	1.5103	676	0.246	Al ₂ O ₃		61.274
31	62.775	1.4790	1433	0.267	TiO ₂	002	62.761
32	64.129	1.4510	1816	0.366	BaTi ₄ O ₉		64.006
33	65.844	1.4173	10834	0.597	TiO ₂ BaTiO ₃ Ba ₂ Ti ₉ O ₂₀	210 202, 220	64.006 65.930 65.996
34	66.559	1.4038	3188	0.314	Al ₂ O ₃	124	66.522
35	68.249	1.3731	3807	0.272	Al ₂ O ₃	030	68.221
36	69.051	1.3591	2492	0.230	TiO ₂	301	68.970
37	69.808	1.3462	853	0.137	TiO ₂	112	69.826
38	70.517	1.3344	2689	0.512	Al ₂ O ₃ BaTiO ₃	125 212, 221	70.365 70.457
39					Ba ₂ Ti ₉ O ₂₀		71.446
40	75.094	1.2640	4966	0.525	BaTiO ₃	301, 310	75.143
41	76.919	1.2385	1392	0.298	Al ₂ O ₃	1.0.10	76.868
42					BaTi ₄ O ₉	330	78.001
43	79.048	1.2104	874	0.291	BaTi ₄ O ₉		78.915

Table 5e: Results of IDR Peak Search for Sample S08H (cont.)

44	79.417	1.2057	2448	0.463	BaTiO ₃	113, 311	79.230
45	83.501	1.1568	3131	0.475	BaTi ₄ O ₉		83.333
					BaTiO ₃	222	83.448
46	84.324	1.1476	1212	0.469	TiO ₂	400	84.278
					Al ₂ O ₃	223	84.396
47	87.760	1.1113	1356	0.524			
48	89.568	1.0935	847	0.157	TiO ₂	222	89.506
49	90.772	1.0821	985	0.269	Al ₂ O ₃	0.0.12	90.663
					TiO ₂	330	90.633
50	92.027	1.0706	9812	0.853	BaTiO ₃	312, 321	92.210
51	95.287	1.0424	1592	0.251	Al ₂ O ₃	226	95.372
					TiO ₂	411	95.372

Table 5f: Results of IDR Peak Search for Sample S24H

Peak	2 θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2 θ (deg)
1					BaTi ₄ O ₉	021	18.619
2					Ba ₄ Ti ₁₃ O ₃₀	102, 131	19.066
3					Ba ₄ Ti ₁₃ O ₃₀	022, 040	20.769
4	22.207	3.9999	15085	0.604	Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃	231 001, 100	22.026 22.208
5	25.620	3.4742	5161	0.265	Al ₂ O ₃	210	25.545
6	27.464	3.2459	5210	0.236	Ba ₄ Ti ₁₃ O ₃₀ TiO ₂	411 110	27.448 27.448
7	30.093	2.9672	7393	0.382	BaTi ₄ O ₉ Ba ₂ Ti ₉ O ₂₀	130, 121	30.000 30.000
8	31.555	2.8330	52989	0.373	BaTiO ₃	101, 110	31.506
9	35.145	2.5514	6576	0.217	Al ₂ O ₃	104	35.151
10					TiO ₂	101	36.077
11	37.803	2.3779	2774	0.229	Al ₂ O ₃	110	37.752
12	38.925	2.3119	13837	0.312	BaTiO ₃ BaTi ₄ O ₉	111 122, 150	38.874 39.062
13	41.266	2.1860	5789	0.304	TiO ₂	111	41.222
14	43.354	2.0854	7193	0.260	Ba ₄ Ti ₁₃ O ₃₀	304, 362	41.412
15	44.083	2.0526	2110	0.252	Al ₂ O ₃ Ba ₄ Ti ₁₃ O ₃₀ TiO ₂	113 640 210	43.400 44.065 44.065
16	45.277	2.0012	18180	0.633	Ba ₄ Ti ₁₃ O ₃₀	533	45.306
17	49.105	1.8538	1249	0.416	BaTiO ₃ BaTi ₄ O ₉	200 504, 562	45.402 48.967
18	50.978	1.7900	5965	0.742	Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃	201, 210	49.062 51.057
19	52.592	1.7388	2935	0.271	Al ₂ O ₃	202	52.582
20	54.361	1.6863	10576	0.234	Ba ₂ Ti ₉ O ₂₀ TiO ₂		54.260 54.361
21	56.249	1.6341	20869	0.592	BaTiO ₃	211	56.253
22	57.527	1.6008	5793	0.232	Al ₂ O ₃ Ba ₂ Ti ₉ O ₂₀	116	57.559 57.559
23	58.519	1.5760	651	0.379	Ba ₄ Ti ₁₃ O ₃₀	644	58.467
24	60.009	1.5404	1045	0.332	BaTi ₄ O ₉		60.194
25					Ba ₂ Ti ₉ O ₂₀		60.806
26	61.318	1.5106	637	0.254	Al ₂ O ₃	122, 018	61.274
27	62.761	1.4793	1436	0.250	TiO ₂	002	62.761
28	64.095	1.4517	1905	0.280	BaTi ₄ O ₉		64.006
29	65.886	1.4165	9179	0.680	TiO ₂ BaTiO ₃	210 202, 220	64.006 65.930
30	66.522	1.4045	3604	0.353	Ba ₂ Ti ₉ O ₂₀ Al ₂ O ₃	124	65.996 66.522
31	68.260	1.3729	3667	0.296	Al ₂ O ₃	030	68.221
32	69.068	1.3588	2455	0.218	TiO ₂	301	68.970
33	69.832	1.3458	1400	0.219	TiO ₂	112	69.826
34					Ba ₂ Ti ₉ O ₂₀		71.446
35	75.060	1.2645	7920	0.967	BaTiO ₃	301, 310	75.143
36	76.912	1.2386	2318	0.536	Al ₂ O ₃	1.0.10	76.868
37					BaTi ₄ O ₉	330	78.001
38	79.378	1.2062	3496	0.846	BaTiO ₃	113, 311	79.230
39	80.727	1.1894	967	0.504	BaTi ₄ O ₉ Al ₂ O ₃		80.637 80.752
40	82.438	1.1690	1037	0.375	TiO ₂	321	82.387
41	83.536	1.1564	1805	0.423	BaTiO ₃	222	83.448
42	87.582	1.1131	1075	0.759	BaTi ₄ O ₉		87.533
43	89.578	1.0934	1695	0.472	TiO ₂ TiO ₂	410 222	87.533 89.506
44	92.082	1.0701	10365	1.056	BaTiO ₃	312, 321	92.210
45	95.299	1.0423	3002	0.462	Al ₂ O ₃ TiO ₂	226 411	95.372 95.372
46	97.278	1.0263	771	0.482	TiO ₂	420	97.227

Table 5g: Results of IDR Peak Search for Sample S48H

Peak	2 θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2 θ (deg)
1	18.641	4.7562	595	0.209	BaTi ₄ O ₉	021	18.619
2	19.076	4.6487	798	0.246	Ba ₄ Ti ₁₃ O ₃₀	102, 131	19.066
3	20.802	4.2667	1401	0.170	Ba ₄ Ti ₁₃ O ₃₀	022, 040	20.769
4	22.158	4.0086	8576	0.401	Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃	231 001, 100	22.026 22.208
5	23.154	3.8383	1441	0.210	BaTi ₄ O ₉	031	23.197
6	25.589	3.4783	5021	0.233	Al ₂ O ₃	210	25.545
7	26.224	3.3956	687	0.192	Ba ₄ Ti ₁₃ O ₃₀	302	26.178
8	27.462	3.2452	17204	0.202	Ba ₂ Ti ₉ O ₂₀ Ba ₄ Ti ₁₃ O ₃₀ TiO ₂	411 110	26.269 27.448 27.448
9	28.345	3.1461	5788	0.221	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉	322, 113 002, 041	28.267 28.358
10	29.900	2.9859	3232	0.230	Ba ₂ Ti ₉ O ₂₀ BaTi ₄ O ₉ Ba ₂ Ti ₉ O ₂₀	130, 121	28.449 30.000 30.000
11	30.467	2.9316	549	0.158	Ba ₆ Ti ₁₇ O ₄₀	242	30.274
12	31.547	2.8337	44730	0.344	Ba ₄ Ti ₁₃ O ₃₀	213, 242	30.457
13	32.040	2.7912	2094	0.212	BaTiO ₃ Ba ₄ Ti ₁₃ O ₃₀ Ba ₂ Ti ₉ O ₂₀	101, 110 133	31.506 32.015 32.015
14	33.712	2.6565	2373	0.249	Ba ₂ Ti ₉ O ₂₀		33.579
15	33.960	2.6377	2004	0.169	Ba ₄ Ti ₁₃ O ₃₀ Ba ₄ Ti ₁₃ O ₃₀	313, 342 260	33.672 33.949
16	35.166	2.5499	6694	0.212	BaTi ₄ O ₉ Al ₂ O ₃	032, 051 104	33.949 35.151
17	36.090	2.4867	6011	0.186	TiO ₂	101	36.077
18	37.099	2.4214	476	0.178	BaTi ₄ O ₉	102, 060	37.100
19	37.796	2.3783	2976	0.230	Ba ₂ Ti ₉ O ₂₀	110	37.287
20	38.913	2.3126	13381	0.315	Al ₂ O ₃ BaTiO ₃ BaTi ₄ O ₉	111 122, 150	37.752 38.874 39.062
21	41.289	2.1848	4763	0.281	TiO ₂	111	41.222
22	41.640	2.1672	763	0.197	Ba ₄ Ti ₁₃ O ₃₀ Al ₂ O ₃	304, 362 006	41.412 41.695
23	42.760	2.1130	575	0.274	BaTi ₄ O ₉ Ba ₄ Ti ₁₃ O ₃₀	132, 151 602, 324	41.790 42.735
24	43.376	2.0844	6461	0.221	Al ₂ O ₃	113	43.400
25	44.074	2.0530	1328	0.196	Ba ₄ Ti ₁₃ O ₃₀	640	44.065
26	44.988	2.0134	6495	0.366	TiO ₂ Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉	210 404, 462	44.160 44.924 45.019
27	45.352	1.9981	8920	0.340	Ba ₄ Ti ₁₃ O ₃₀	533	45.306
28	46.192	1.9637	595	0.218	BaTiO ₃	200	45.402
29	46.782	1.9403	707	0.226	Al ₂ O ₃ Ba ₄ Ti ₁₃ O ₃₀ Ba ₄ Ti ₁₃ O ₃₀	202 471, 711 115, 173	46.169 46.264 46.746
30	47.204	1.9239	459	0.244	BaTi ₄ O ₉		47.225
31	47.889	1.8980	1418	0.240	Ba ₂ Ti ₉ O ₂₀ Ba ₄ Ti ₁₃ O ₃₀	642	47.225 47.902
32	49.113	1.8535	1554	0.339	BaTi ₄ O ₉ BaTi ₄ O ₉ Ba ₄ Ti ₁₃ O ₃₀	504, 562	47.999 48.967 49.062
33	50.173	1.8168	624	0.231	Ba ₂ Ti ₉ O ₂₀		50.035
34	51.048	1.7877	3928	0.338	BaTiO ₃ Ba ₂ Ti ₉ O ₂₀	201, 210 202	51.057 51.208
35	52.572	1.7394	3458	0.273	Al ₂ O ₃	544, 604	52.582
36	53.881	1.7002	518	0.169	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉		53.963 54.063

Table 5g: Results of IDR Peak Search for Sample S48H (cont.)

37	54.348	1.6867	5265	0.146	Ba ₂ Ti ₉ O ₂₀		54.260
38	56.253	1.6340	16573	0.490	TiO ₂	211	54.361
39	56.642	1.6237	3709	0.231	BaTiO ₃	211	56.253
					TiO ₂	220	56.653
					BaTi ₄ O ₉		56.756
40	57.515	1.6011	6506	0.251	Al ₂ O ₃	116	57.559
41	59.317	1.5567	622	0.203	Ba ₂ Ti ₉ O ₂₀	704, 762	57.559
42					Ba ₄ Ti ₁₃ O ₃₀		59.279
43	61.309	1.5108	574	0.236	Ba ₂ Ti ₉ O ₂₀	122, 018	60.806
					Al ₂ O ₃		61.274
44	61.941	1.4969	615	0.329	BaTi ₄ O ₉		61.936
45	62.747	1.4796	661	0.139	TiO ₂	002	62.761
46	64.085	1.4519	832	0.195	BaTi ₄ O ₉		64.006
					TiO ₂	210	64.006
47	65.787	1.4184	3296	0.275	BaTiO ₃	202, 220	65.930
48	66.522	1.4045	3144	0.288	Al ₂ O ₃	124	66.522
49	68.221	1.3736	2053	0.170	Al ₂ O ₃	030	68.221
50	69.028	1.3595	1557	0.157	TiO ₂	301	68.970
51	69.796	1.3464	1101	0.178	TiO ₂	112	69.826
52	70.420	1.3360	2121	0.561	Al ₂ O ₃	125	70.365
					BaTiO ₃	212, 221	70.457
53					Ba ₂ Ti ₉ O ₂₀		71.446
54	75.108	1.2638	5165	0.479	BaTiO ₃	301, 310	75.143
55	76.882	1.2390	850	0.146	Al ₂ O ₃	1.0.10	76.868
56					BaTi ₄ O ₉	330	78.001
57	78.768	1.2140	495	0.278	BaTiO ₃	113	78.799
					BaTi ₄ O ₉		78.915
58	79.401	1.2059	2909	0.728	BaTiO ₃	311	79.488
59	80.703	1.1897	841	0.443	BaTi ₄ O ₉		80.637
					Al ₂ O ₃	220	80.752
60	82.352	1.1700	504	0.186	TiO ₂	321	82.387
61	83.501	1.1568	2066	0.406	BaTi ₄ O ₉		83.333
					BaTiO ₃	222	83.448
62	89.547	1.0937	696	0.129	TiO ₂	222	89.506
63	90.762	1.0822	535	0.193	Al ₂ O ₃	0.0.12	90.663
					TiO ₂	330	90.633
64	92.049	1.0704	4434	0.438	BaTiO ₃	312	92.149
65	92.238	1.0687	1228	0.310	BaTiO ₃	312, 321	92.210
66	95.275	1.0425	1513	0.265	Al ₂ O ₃	226	95.372
					TiO ₂	411	95.372
67	96.017	1.0364	578	0.173	TiO ₂	312	96.030

Table 5h: Results of IDR Peak Search for Sample S06D

Peak	2 θ (deg)	d-spacing	Intensity	FWHM	Phase	hkl	2 θ (deg)
1	18.635	4.7576	523	0.187	BaTi ₄ O ₉	021	18.619
2	19.063	4.6519	978	0.173	Ba ₄ Ti ₁₃ O ₃₀	102, 131	19.066
3	20.797	4.2677	2579	0.201	Ba ₄ Ti ₁₃ O ₃₀	022, 040	20.769
4	22.052	4.0276	8838	0.434	Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃	231 001, 100	22.026 22.208
5	23.146	3.8397	1068	0.177	BaTi ₄ O ₉	031	23.197
6	25.590	3.4782	5059	0.242	Al ₂ O ₃	210	25.545
7	26.222	3.3958	987	0.184	Ba ₄ Ti ₁₃ O ₃₀ Ba ₂ Ti ₉ O ₂₀	302 411	26.178 26.269
8	27.446	3.2471	16566	0.186	Ba ₄ Ti ₁₃ O ₃₀ TiO ₂	110	27.448 27.448
9	28.342	3.1464	7903	0.227	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉	322, 113 002, 041	28.267 28.358
10	29.901	2.9858	1513	0.153	Ba ₂ Ti ₉ O ₂₀ BaTi ₄ O ₉ Ba ₂ Ti ₉ O ₂₀	130, 121	28.449 30.000 30.000
11	30.464	2.9319	1039	0.168	Ba ₄ Ti ₁₃ O ₃₀	213, 242	30.457
12	31.546	2.8338	36605	0.359	BaTiO ₃	101, 110	31.506
13	32.040	2.7912	2776	0.219	Ba ₄ Ti ₁₃ O ₃₀	133	32.015
14	33.000	2.7122	446	0.153	Ba ₂ Ti ₉ O ₂₀ Ba ₄ Ti ₁₃ O ₃₀	422, 440	32.015 32.935
15	33.709	2.6567	3702	0.254	Ba ₂ Ti ₉ O ₂₀		33.579
16	33.960	2.6377	1763	0.165	Ba ₄ Ti ₁₃ O ₃₀ Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉	313, 342 260 032, 051	33.672 33.949 33.949
17	35.166	2.5499	6319	0.209	Al ₂ O ₃	104	35.151
18	36.084	2.4871	5617	0.194	TiO ₂	101	36.077
19	36.800	2.4404	437	0.185	Ba ₂ Ti ₉ O ₂₀		36.635
20	37.798	2.3782	2921	0.229	Ba ₄ Ti ₁₃ O ₃₀ Al ₂ O ₃	502, 531 110	36.728 37.752
21	38.909	2.3128	10690	0.325	BaTiO ₃	111	38.874
22	40.199	2.2415	775	0.296	BaTi ₄ O ₉ Ba ₄ Ti ₁₃ O ₃₀	122, 150 253, 271	39.062 40.186
23	41.317	2.1834	5584	0.285	Ba ₂ Ti ₉ O ₂₀ TiO ₂ Ba ₄ Ti ₁₃ O ₃₀	111 304, 362	40.186 41.222 41.412
24	42.752	2.1134	672	0.240	Ba ₄ Ti ₁₃ O ₃₀	602, 324	42.735
25	43.370	2.0847	6448	0.230	Al ₂ O ₃	113	43.400
26	44.070	2.0532	1422	0.227	Ba ₄ Ti ₁₃ O ₃₀ TiO ₂	640 210	44.065 44.065
27	44.964	2.0144	6240	0.353	BaTiO ₃ Ba ₄ Ti ₁₃ O ₃₀	002 404, 462	44.828 44.924
28	45.366	1.9975	7459	0.352	BaTi ₄ O ₉ Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃	533 200	45.019 45.306 45.402
29	46.197	1.9635	793	0.275	Al ₂ O ₃	202	46.169
30	46.776	1.9405	1125	0.231	Ba ₄ Ti ₁₃ O ₃₀	471, 711	46.264
31	47.267	1.9215	468	0.287	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉ Ba ₂ Ti ₉ O ₂₀	115, 173	46.746 47.225 47.225
32	47.891	1.8979	1275	0.222	Ba ₄ Ti ₁₃ O ₃₀	642	47.902
33	49.108	1.8537	2108	0.298	BaTi ₄ O ₉ BaTi ₄ O ₉	504, 562 235, 291	47.999 48.967
34	50.155	1.8174	489	0.214	Ba ₄ Ti ₁₃ O ₃₀ Ba ₂ Ti ₉ O ₂₀	102 201	49.062 50.035
35	50.689	1.7995	1026	0.313	Ba ₄ Ti ₁₃ O ₃₀ BaTiO ₃		50.620 50.620
36	50.880	1.7932	2459	0.447	BaTiO ₃	202	51.011
37	52.569	1.7395	3311	0.276	Al ₂ O ₃	544, 604	52.582
38	53.864	1.7007	430	0.139	Ba ₄ Ti ₁₃ O ₃₀ BaTi ₄ O ₉		53.963 54.063

Table 5h: Results of IDR Peak Search for Sample S06D (cont.)

39	54.348	1.6867	8236	0.242	Ba ₂ Ti ₉ O ₂₀		54.260
40	56.257	1.6339	11285	0.467	TiO ₂	211	54.361
41	56.642	1.6237	2399	0.181	BaTiO ₃	211	56.253
					TiO ₂	220	56.653
					BaTi ₄ O ₉		56.756
42	57.515	1.6011	6927	0.275	Al ₂ O ₃	116	57.559
43	58.135	1.5855	409	0.205	Ba ₂ Ti ₉ O ₂₀		57.559
44	58.609	1.5738	432	0.222	BaTi ₄ O ₉	644	58.264
					Ba ₄ Ti ₁₃ O ₃₀		58.467
					BaTi ₄ O ₉		58.769
45	59.313	1.5568	570	0.136	Ba ₄ Ti ₁₃ O ₃₀	704, 762	59.279
46	60.696	1.5246	536	0.211	Ba ₂ Ti ₉ O ₂₀		60.806
47	61.314	1.5107	579	0.235	Al ₂ O ₃	122, 018	61.274
48	61.950	1.4967	497	0.195	BaTi ₄ O ₉		61.936
49	62.775	1.4790	1021	0.244	TiO ₂	002	62.761
50	64.065	1.4523	660	0.147	BaTi ₄ O ₉		64.006
51	65.176	1.4302	689	0.270	TiO ₂	210	64.006
52	65.902	1.4162	5473	0.621	Ba ₂ Ti ₉ O ₂₀		65.366
					BaTiO ₃	202, 220	65.930
					Ba ₂ Ti ₉ O ₂₀		65.996
53	66.511	1.4047	2822	0.284	Al ₂ O ₃	124	66.522
54	68.226	1.3735	4370	0.243	Al ₂ O ₃	030	68.221
55	69.028	1.3595	1525	0.162	TiO ₂	301	68.970
56	69.796	1.3464	908	0.158	TiO ₂	112	69.826
57	70.438	1.3357	1167	0.419	Al ₂ O ₃	125	70.365
					BaTiO ₃	212, 221	70.457
58					Ba ₂ Ti ₉ O ₂₀		71.446
59	75.094	1.2640	2216	0.491	BaTiO ₃	301, 310	75.143
60	76.882	1.2390	688	0.173	Al ₂ O ₃	1.0.10	76.868
61					BaTi ₄ O ₉	330	78.001
62	82.344	1.1701	1178	0.260	TiO ₂	321	82.387
63	83.492	1.1569	1611	0.434	BaTi ₄ O ₉		83.333
					BaTiO ₃	222	83.448
64	86.349	1.1258	369	0.259	Al ₂ O ₃	312	86.321
65	89.021	1.0988	595	0.316	Al ₂ O ₃	0.2.10	89.134
66	89.547	1.0937	655	0.158	TiO ₂	222	89.506
67	90.740	1.0824	569	0.151	Al ₂ O ₃	0.0.12	90.663
					TiO ₂	330	90.633
68	92.205	1.0690	2342	0.381	BaTiO ₃	312, 321	92.210
69	95.263	1.0426	1319	0.231	Al ₂ O ₃	226	95.372
					TiO ₂	411	95.372
70	95.993	1.0366	489	0.183	TiO ₂	312	96.030

Table 6: Intensity Data for Selected Peaks

Sample	Al ₂ O ₃ 110	Al ₂ O ₃ 024	Al ₂ O ₃ SUM	TiO ₂ 101	TiO ₂ 102	TiO ₂ SUM	BaTiO ₃ 213	BaTi ₄ O ₉ 031	Ba ₄ Ti ₁₃ O ₃₀ 022,040
Sraw	381	521	901	1491	276	1767	1939	0	0
S24M	391	508	900	1352	243	1595	1971	52	17
S01H	393	492	886	1369	245	1614	1835	65	19
S02H	431	541	972	1267	241	1509	1856	102	34
S08H	409	538	947	1117	207	1323	1680	127	118
S24H	436	516	952	1109	197	1306	1389	148	170
S48H	469	568	1036	1011	180	1191	1319	175	268
S06D	461	543	1004	915	119	1033	1012	170	417
k _i						1.53	2.01		

Table 7: Results of Phase Identification and Quantitative Analysis

Time (hours)	Wt % BaTiO ₃	Wt % Int. Phases	Wt % Ba ₆ Ti ₁₇ O ₄₀	Wt % Ba ₄ Ti ₁₃ O ₃₀	Wt % BaTi ₄ O ₉	Wt % Ba ₂ Ti ₉ O ₂₀	Wt % TiO ₂
0	0.455	0.000	--	--	--	--	0.545
0.4	0.467	0.035	X	***	***	X	0.498
1	0.442	0.046	X	***	***	X	0.512
2	0.408	0.156	X	***	***	X	0.436
8	0.378	0.229	X	***	***	***	0.392
24	0.311	0.305	X	***	***	***	0.385
48	0.271	0.406	X	***	***	***	0.323
144	0.215	0.496	X	***	***	***	0.289

Table 8: Data for the BaCO₃ - TiO₂ ReactionEquimolar BaCO₃ - TiO₂ Mixture Heated at 1050°C in Air

Time (hours)	Mole % BaCO ₃	Mole % Ba ₂ TiO ₄	Mole % BaTiO ₃	Mole % Ba ₄ Ti ₁₃ O ₃₀	Mole % BaTi ₄ O ₉	Mole % TiO ₂
0	50	--	--	--	--	50
0.25	13	41	12	6	1?	28
0.50	5	51	17	4	1?	23
1.0	0	48	30	4	1?	17
2.0	0	44	37	4	1?	14

From Templeton and Pask[4]

Notes:

1. Ba₄Ti₁₃O₃₀ reported as BaTi₃O₇.
2. Detectability of BaTi₄O₉ and Ba₄Ti₁₃O₃₀ reported as 2-3 mole %.

Figure 1a
Simplified BaCO_3 - TiO_2 Interface Reactions

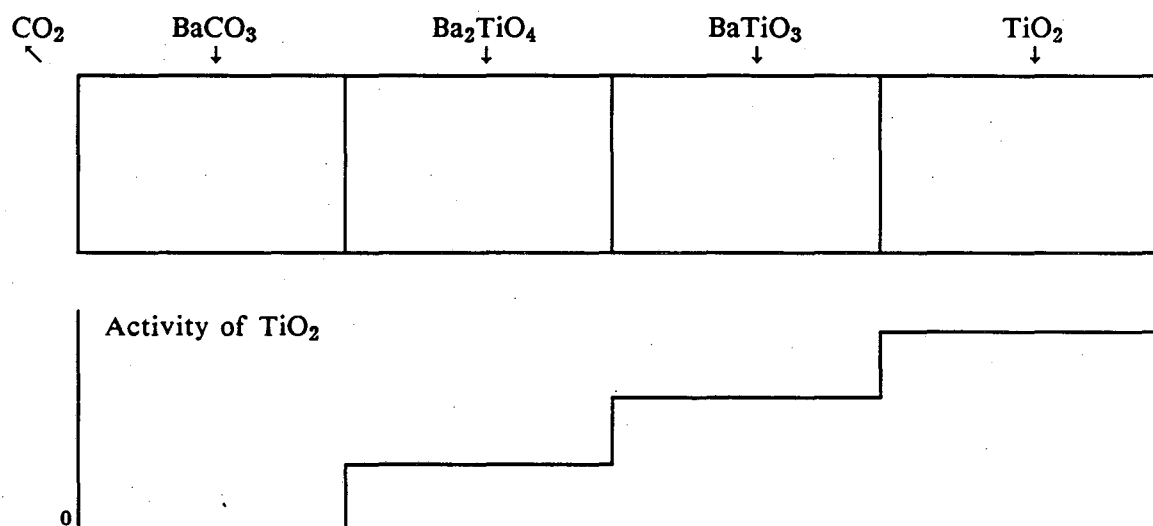


Figure 1b
Complex BaCO_3 - TiO_2 Interface Reactions

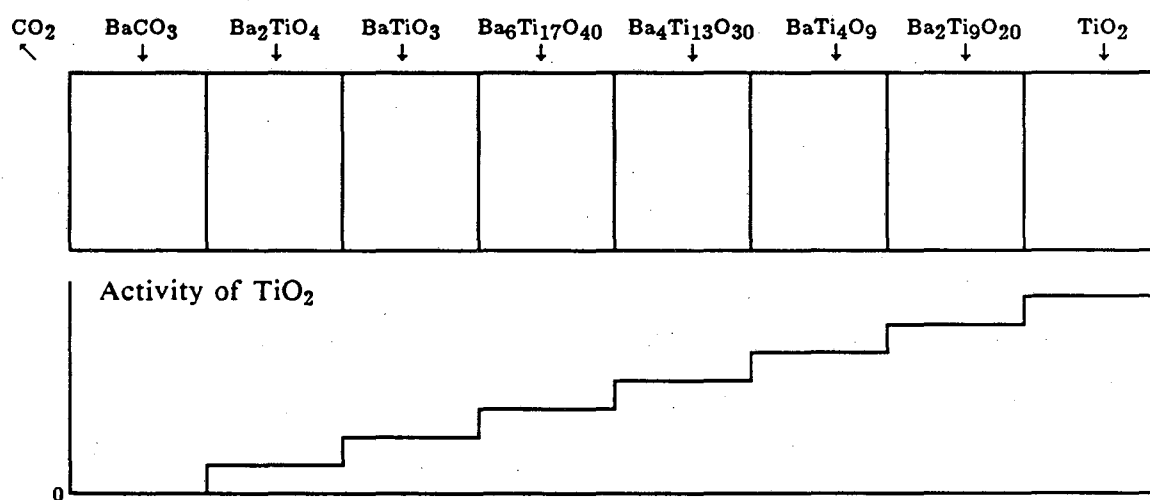
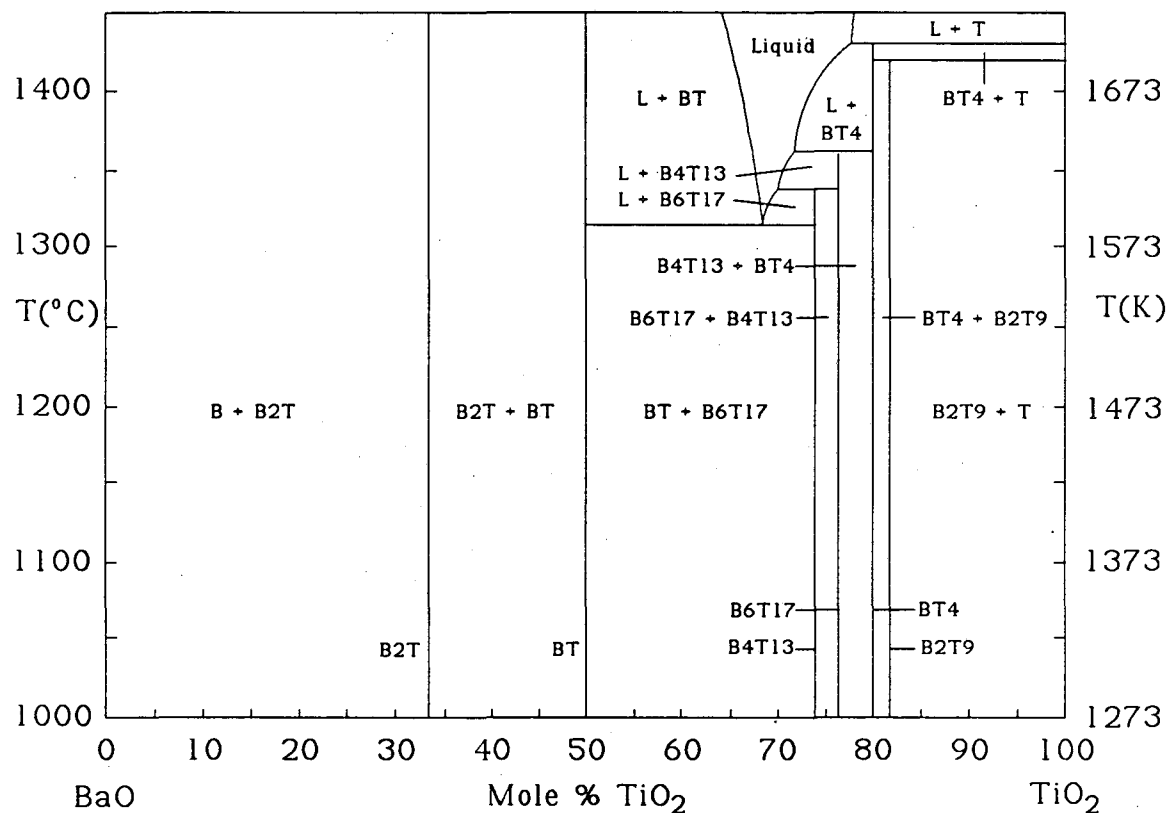


Figure 2
BaO - TiO₂ Phase Diagram



Key:

L=Liquid; B=BaO; B2T=Ba₂TiO₄; BT=BaTiO₃; B6T17=Ba₆Ti₁₇O₄₀;
B4T13=Ba₄Ti₁₃O₃₀; BT4=BaTi₄O₉; B2T9=Ba₂Ti₉O₂₀; T=TiO₂;

References:

1. W. Trzebiatowski, M. Drys, and J. Berak, *Roczniki Chemii* **28** 21-28 (1954)
2. D. E. Rase, R. Roy, *J. Amer. Cer. Soc.* **38**(3) 102-113 (1955)
3. T. Negas, R.S. Roth, H.S. Parker, and D. Minor, *J. Sol. State Chem.* **9** 297-307 (1974)
4. H.M. O'Bryan, Jr., and J. Thomson, *J. Amer. Cer. Soc.* **57**(12) 522-526 (1974)

Figure 3
Possible Geometric Arrangement of Product Phases
During Solid State Reaction

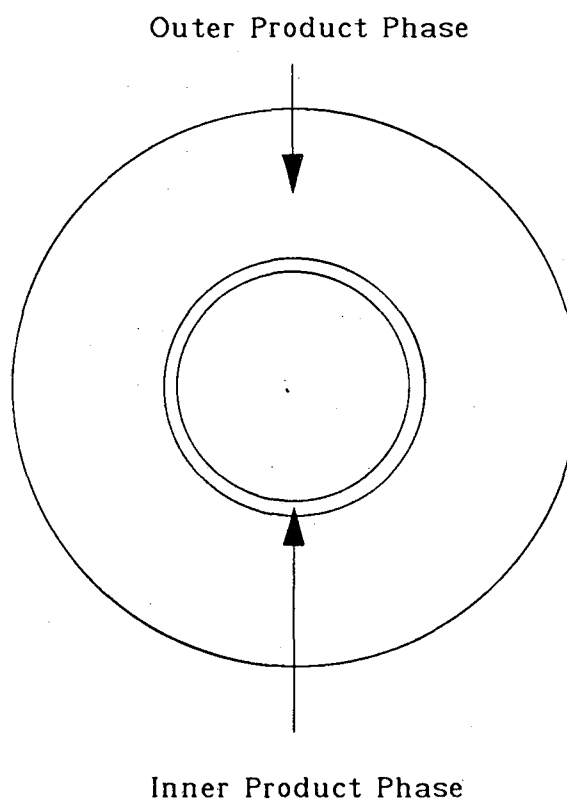
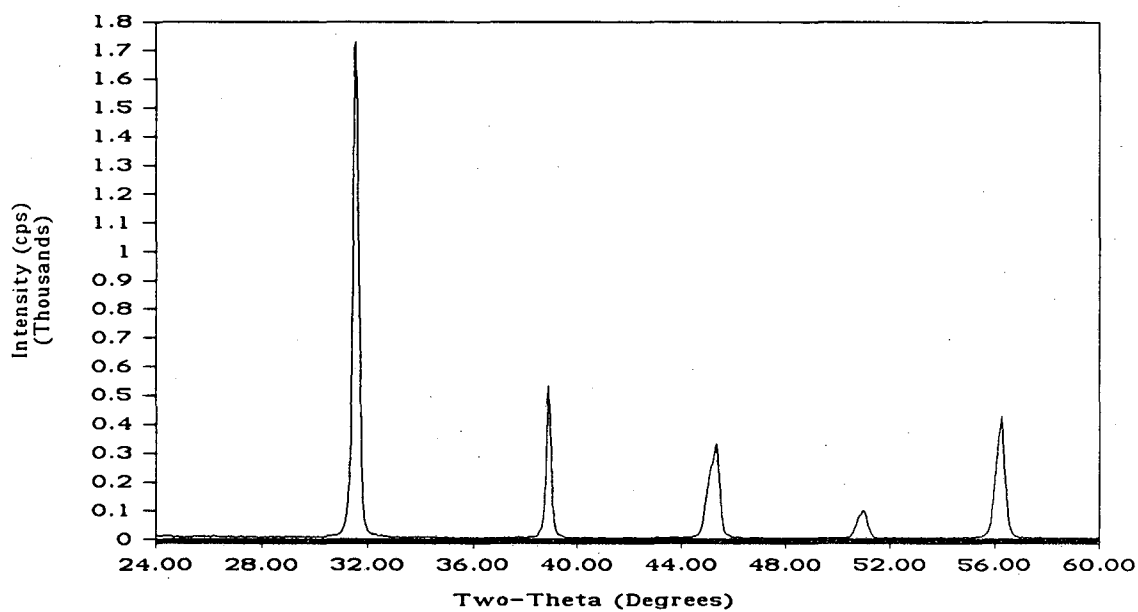
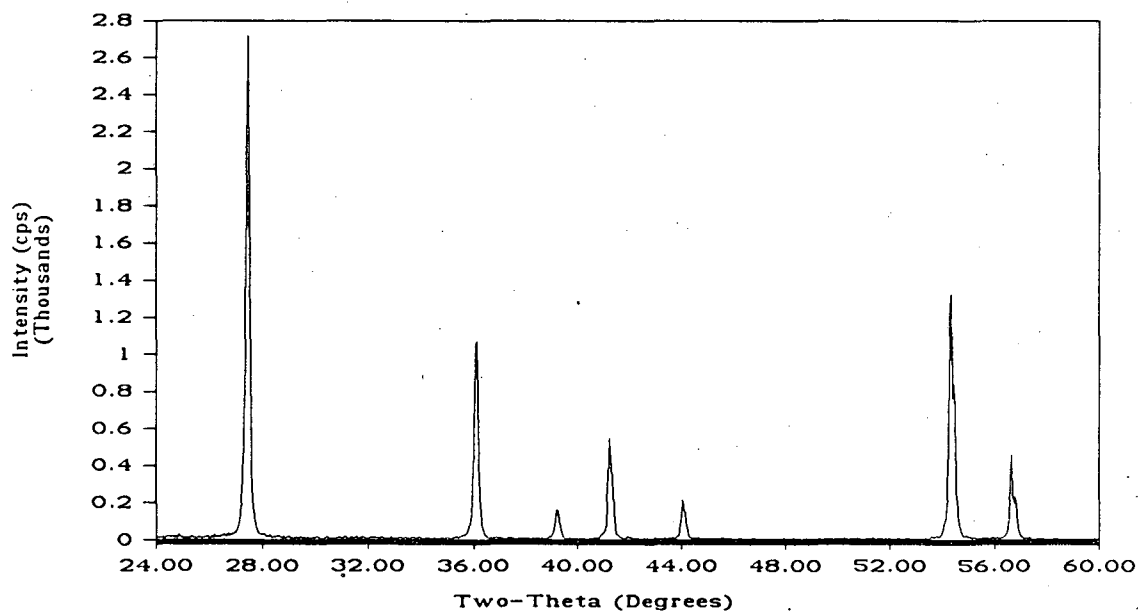


Figure 4
X-ray Diffraction Patterns of Starting Materials



a. BaTiO₃



b. TiO₂

Figure 4 (continued)

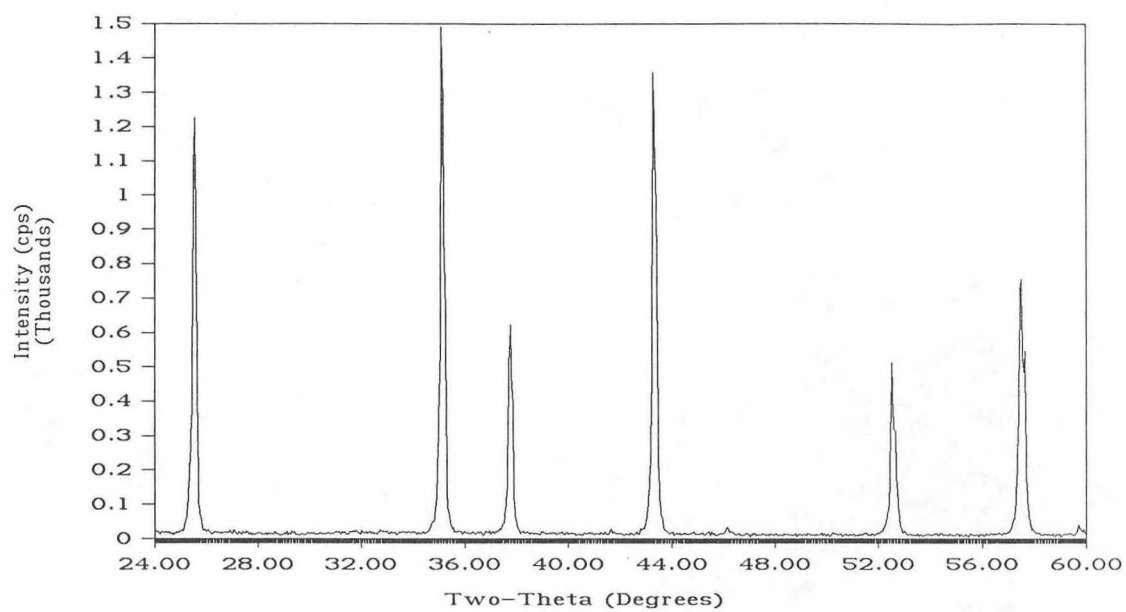
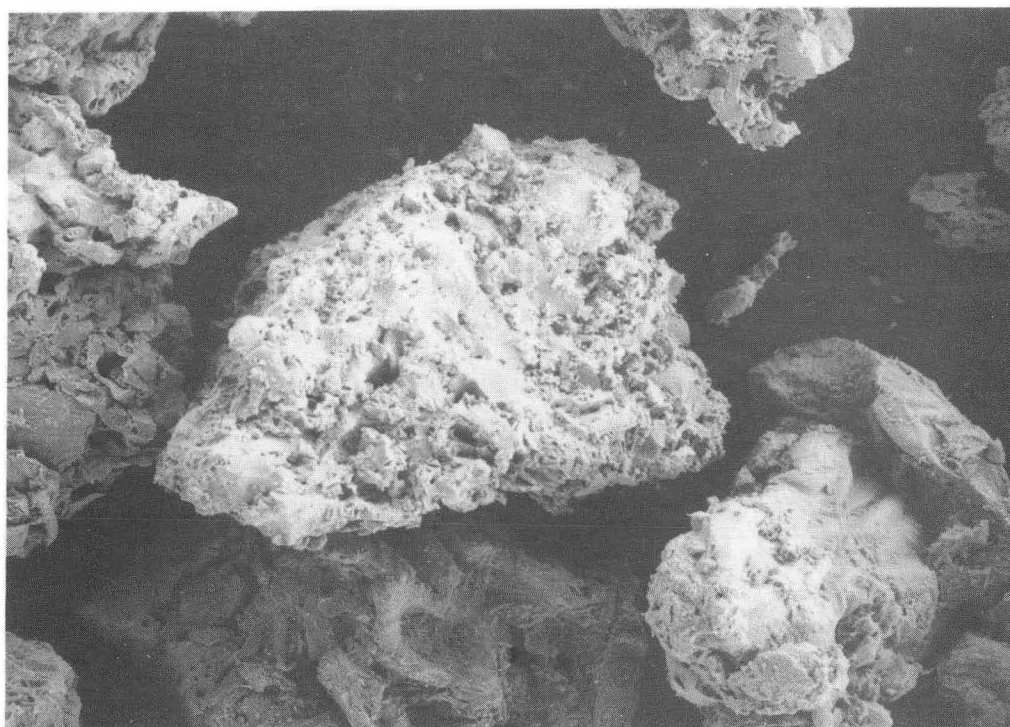
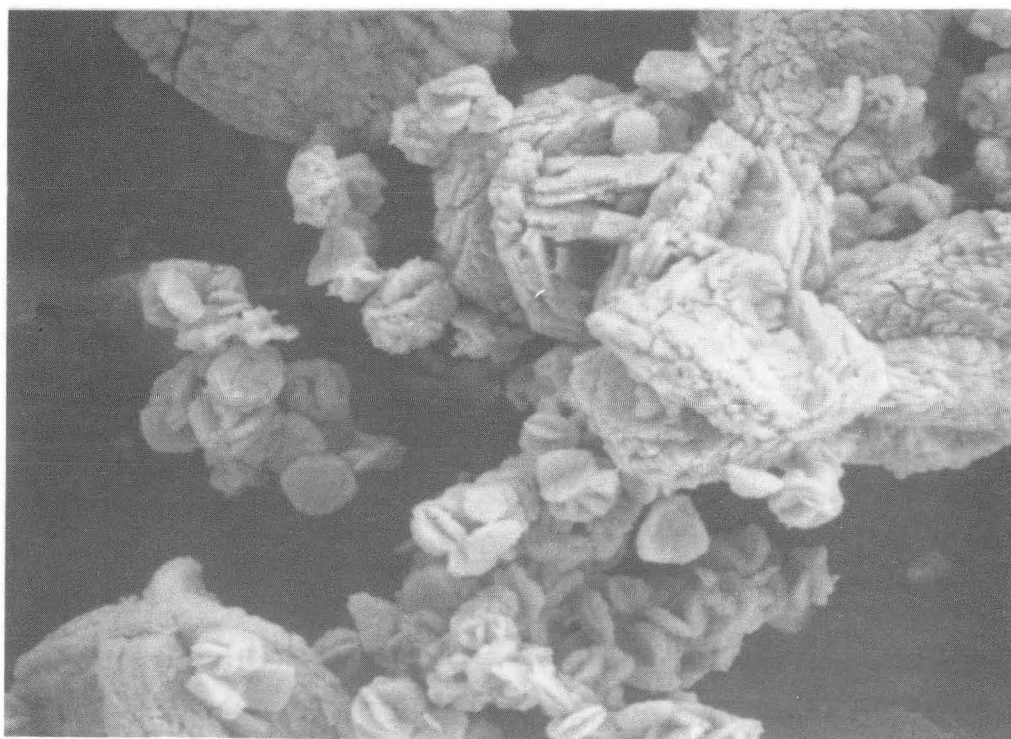
c. Al_2O_3

Figure 5
SEM Micrographs of Starting Materials



a. BaTiO_3 1000 $\times$ — 10.0 μm



b. TiO_2 77 $\times$ — 130 μm

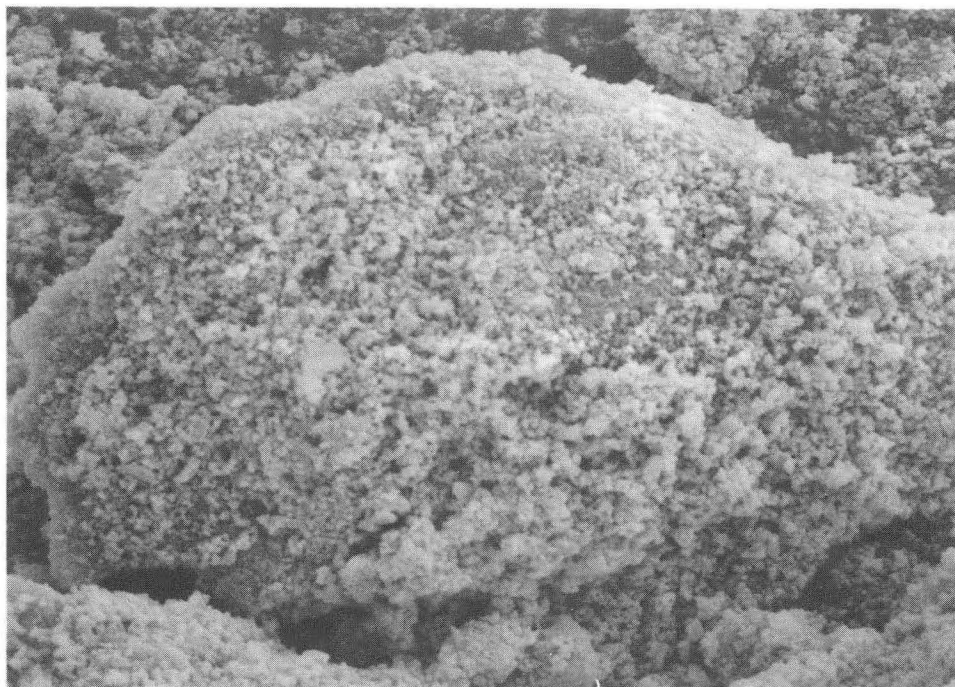
Figure 6
SEM Micrograph of Unfired Mixed Powder



126× ——— 79.4 μ m

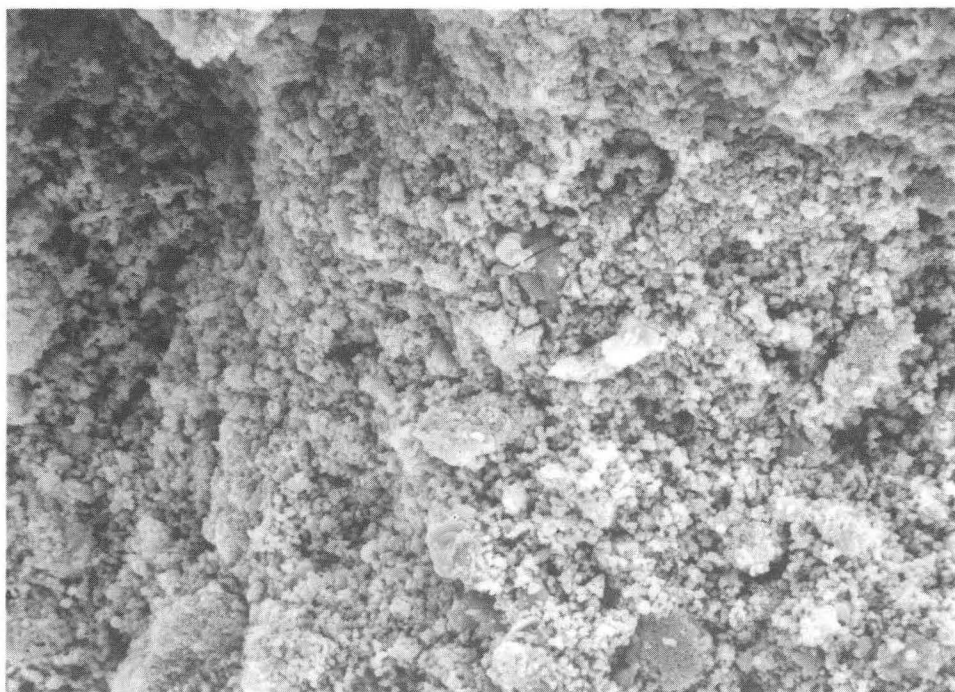
XBB 885-4851

Figure 7
SEM Micrograph of Sample S06D



2400× — 4.17 μ m

Figure 8
SEM Micrograph of Sample S08H



2240× — 4.46 μ m

XBB 885-4852

Figure 9a
Xray Diffraction Patterns for All Samples

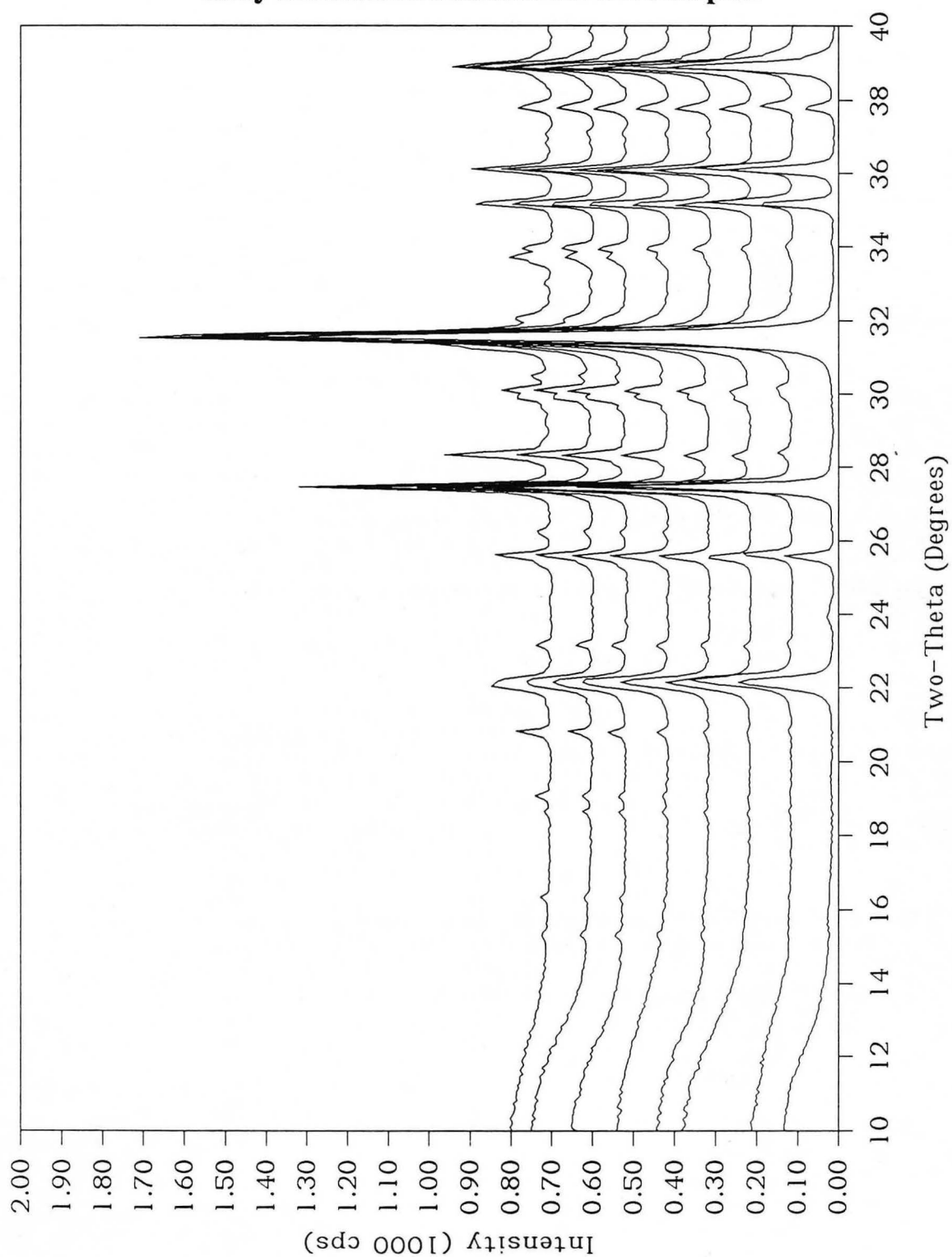


Figure 9b
Xray Diffraction Patterns for All Samples

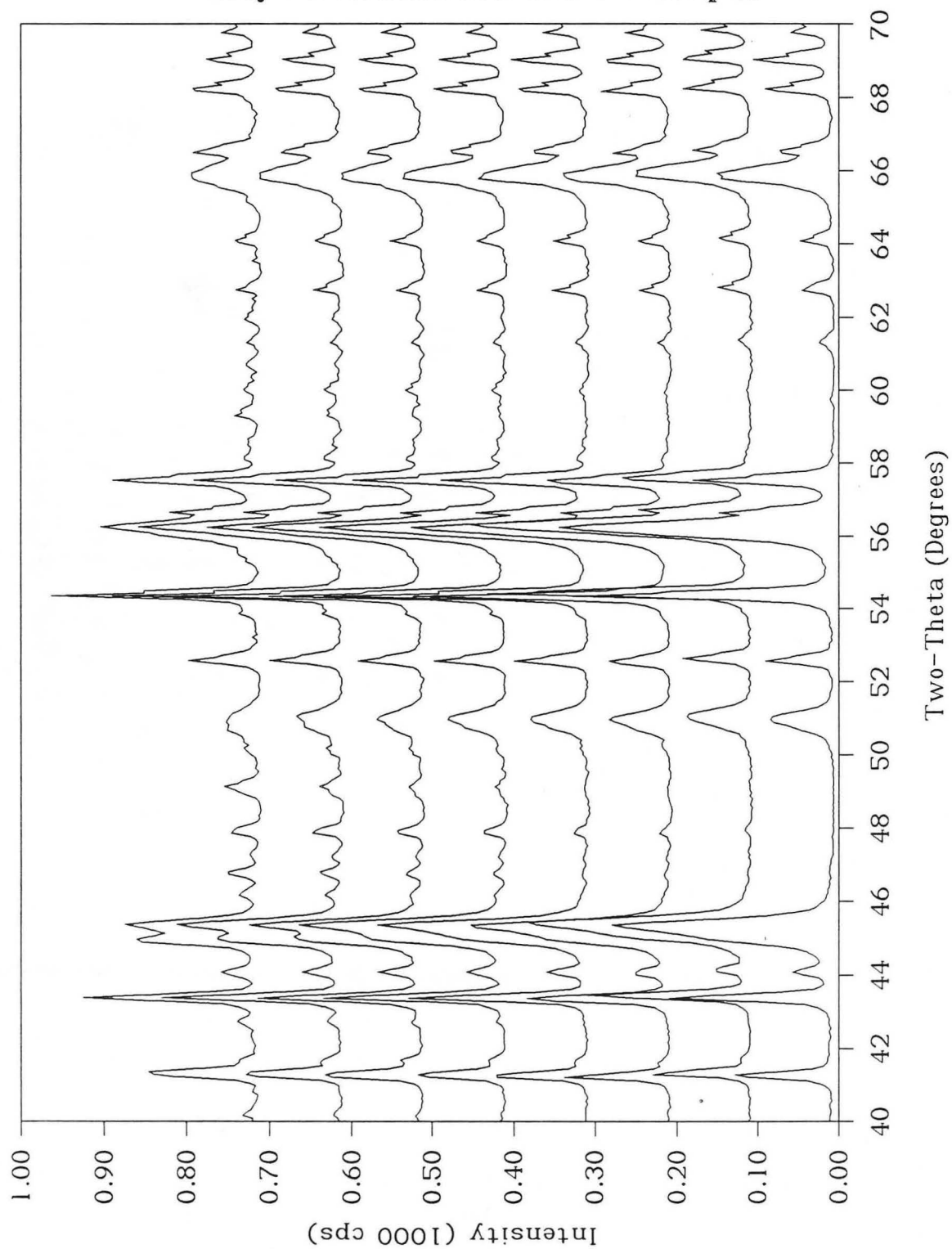


Figure 9c
Xray Diffraction Patterns for All Samples

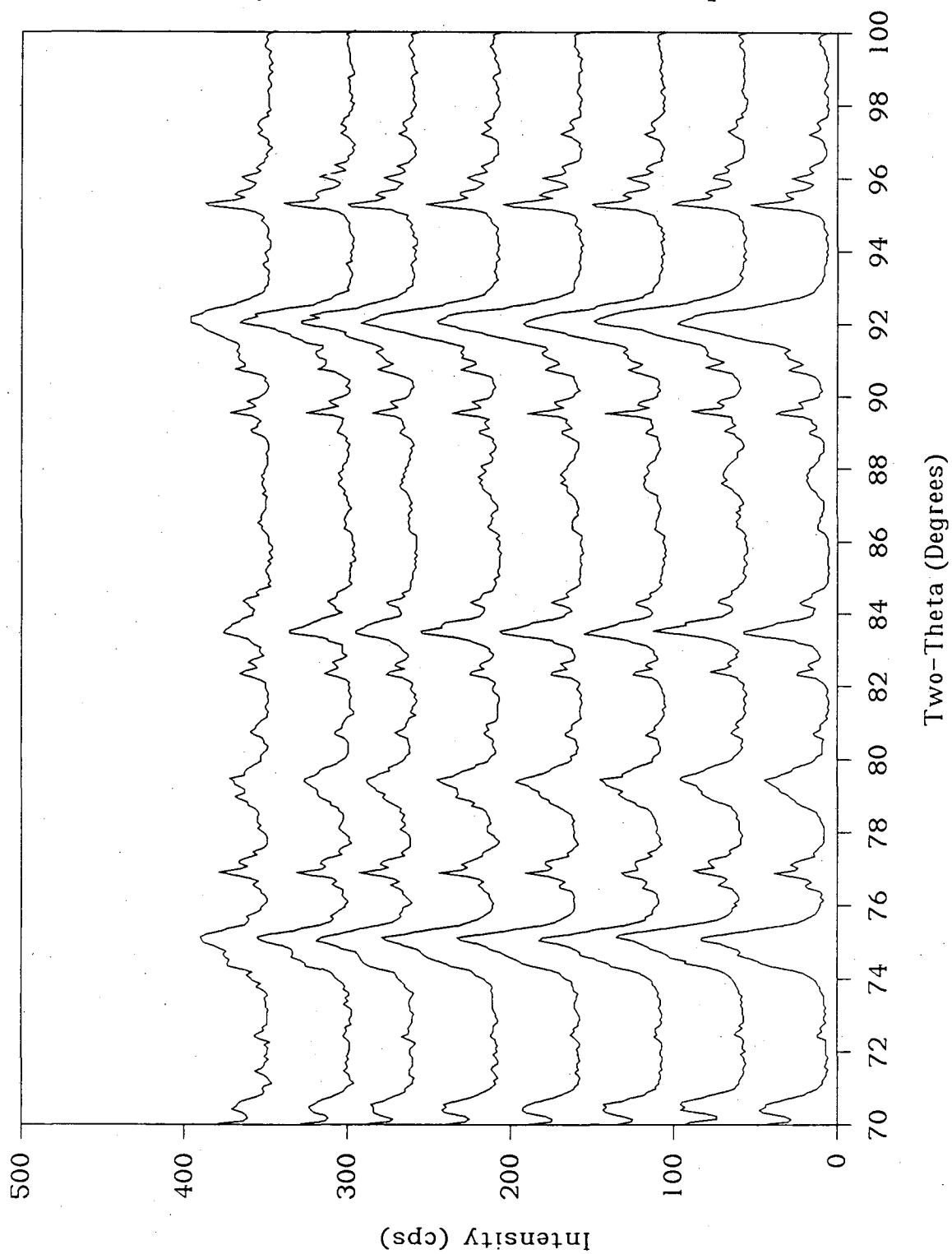
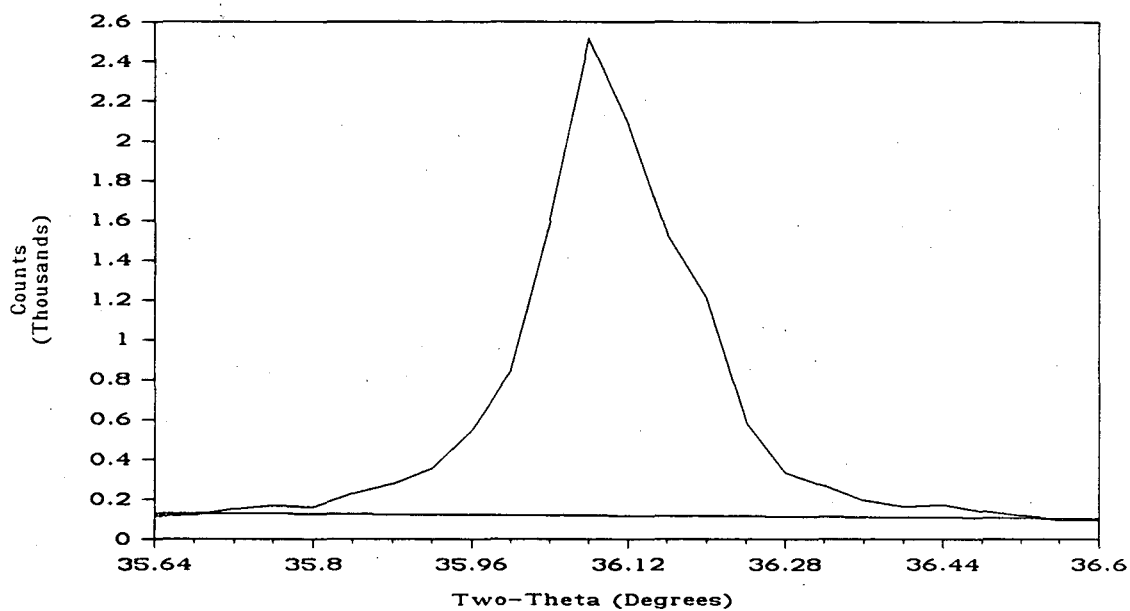
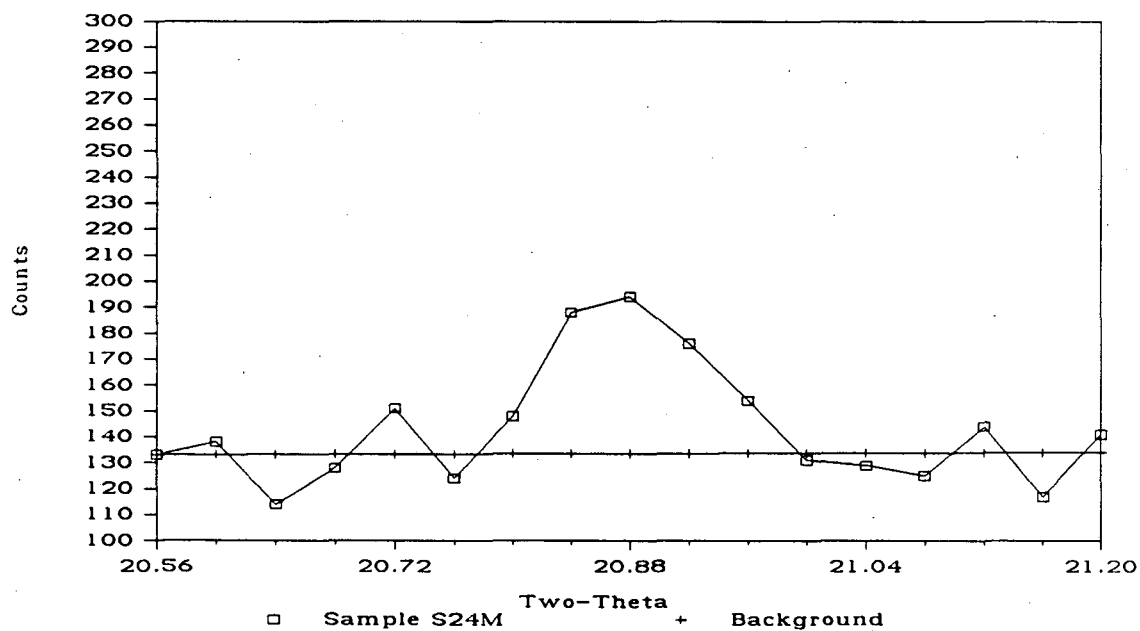


Figure 10
Xray Diffraction Pattern Showing the
Calculation of Background Lines



a. 101 Peak of TiO_2 - Sample S24M



b. 022,040 Peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{40}$ - Sample S24M

Figure 11
X-ray Diffraction Patterns for the 031 Peak of BaTi_4O_9

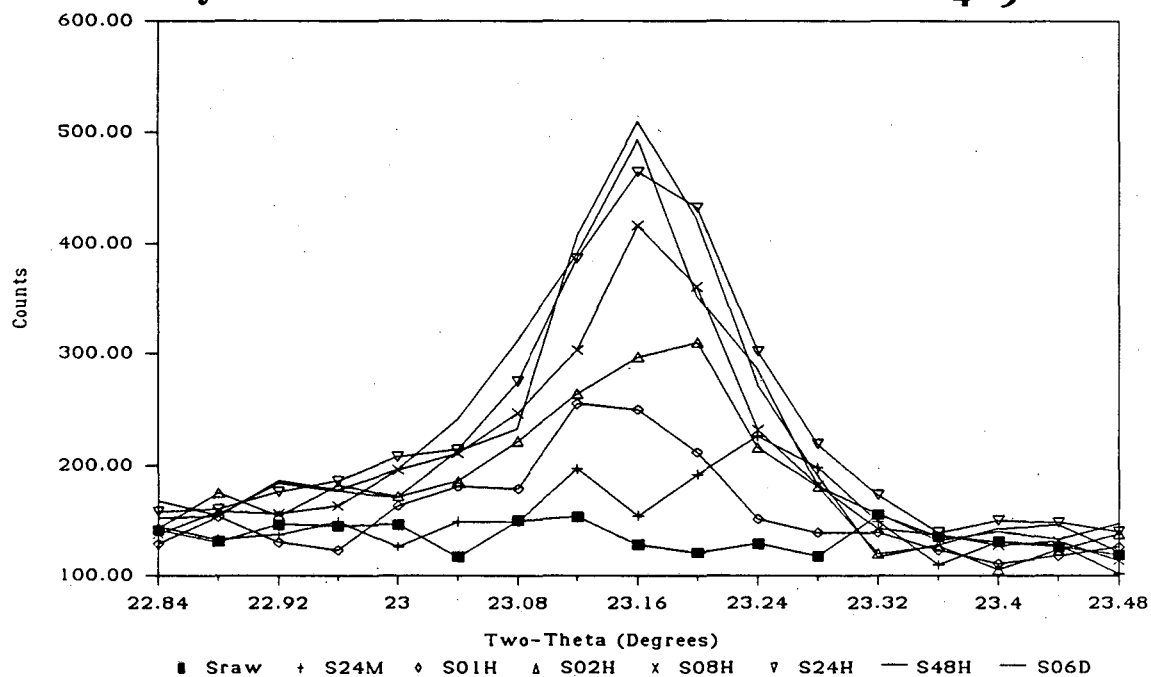


Figure 12
X-ray Diffraction Patterns for the 022,040 Peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$

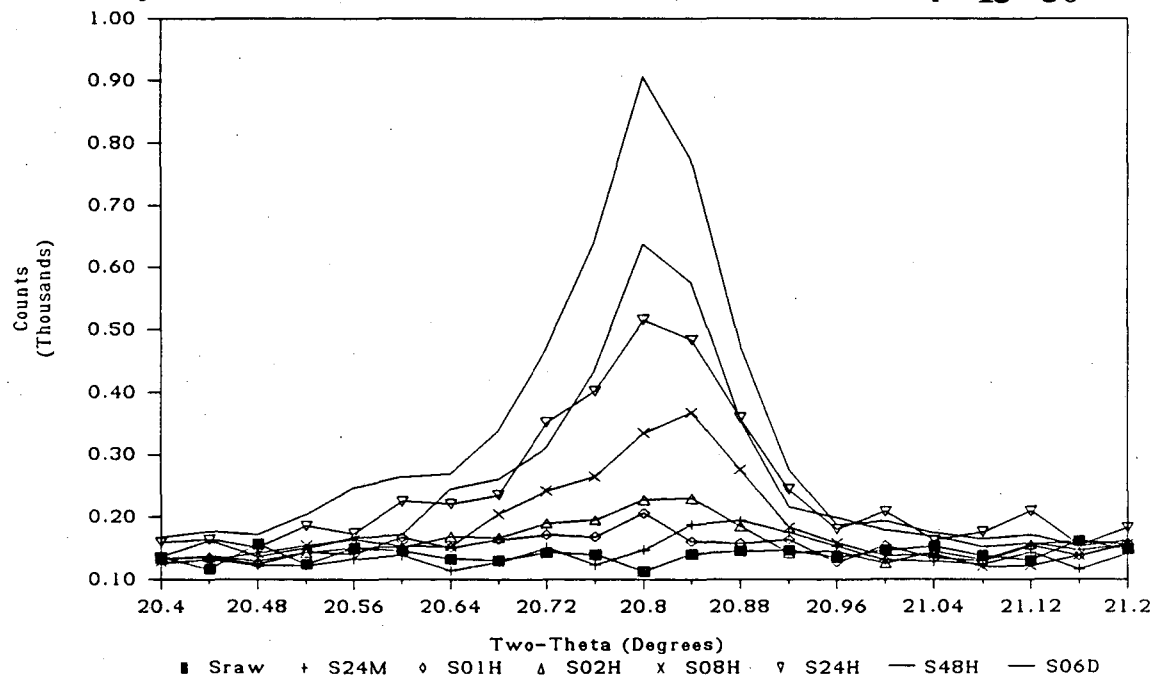


Figure 13
Xray Diffraction Patterns for the 021 Peak of BaTi_4O_9
and the 102,131 Peak of $\text{Ba}_4\text{Ti}_{13}\text{O}_{30}$

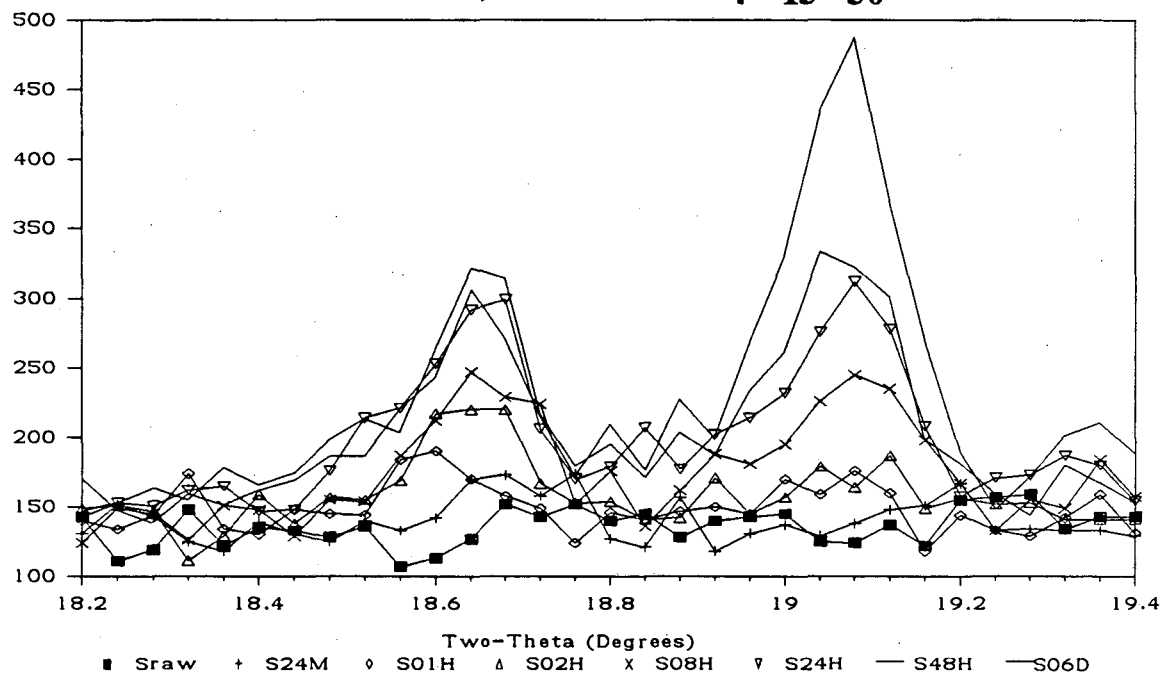
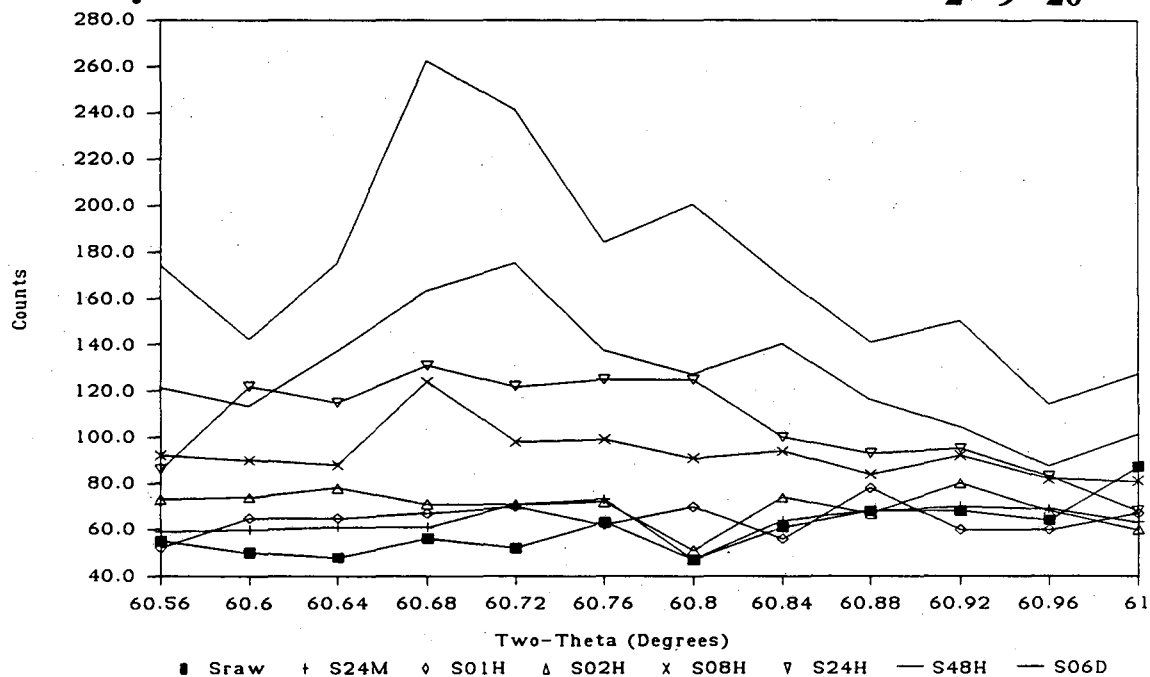
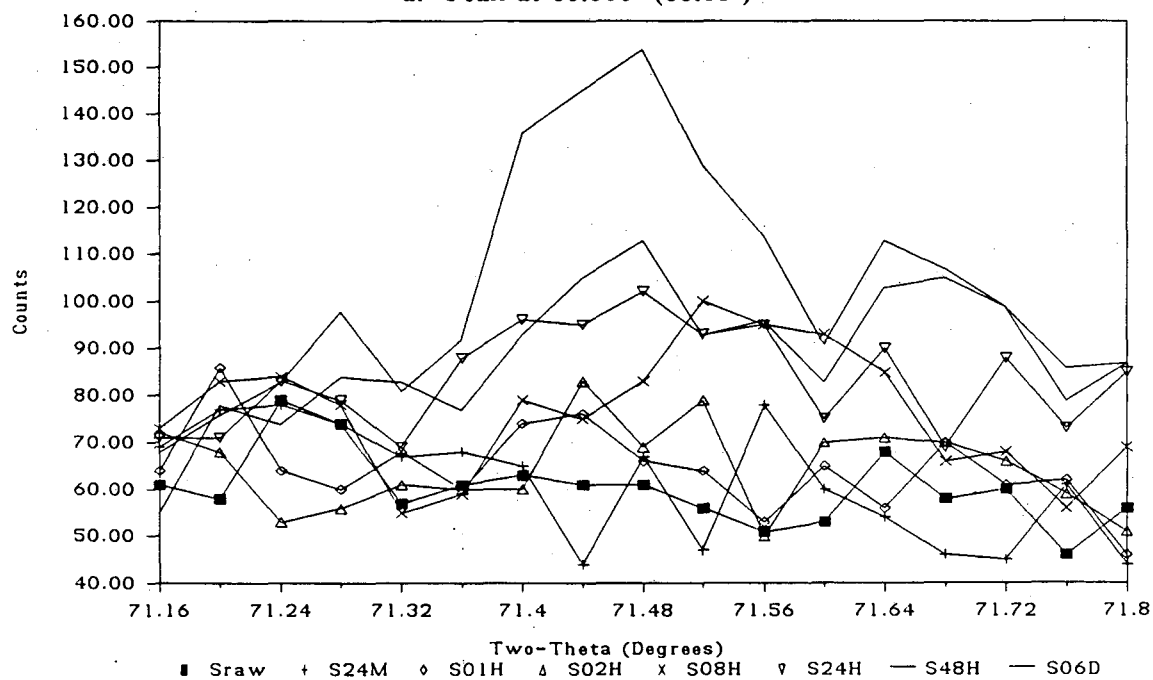


Figure 14
Xray Diffraction Patterns for the Selected Peaks of $\text{Ba}_2\text{Ti}_9\text{O}_{20}$



a. Peak at 60.806° (60.68°)



b. Peak at 71.446°

Figure 15
Weight Fraction of TiO_2 , BaTiO_3 , and Total Amount
of Intermediate Phases with Time

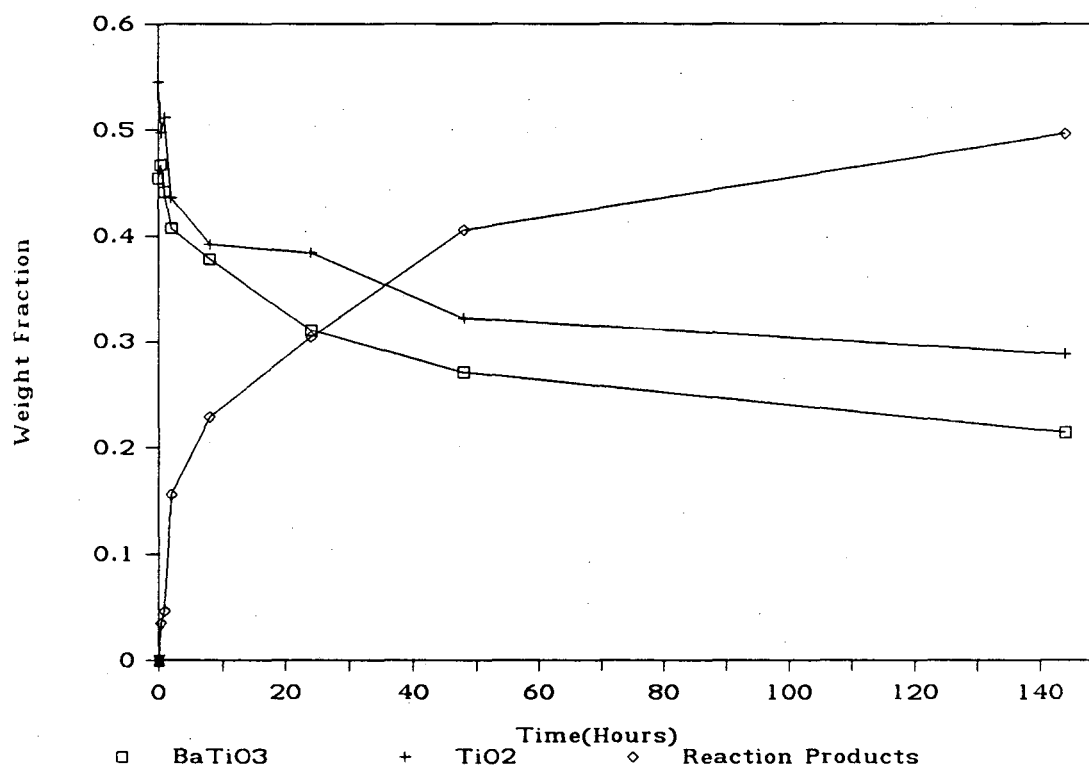


Figure 16
Normalized Intensity of Observed Intermediate Phases with Time

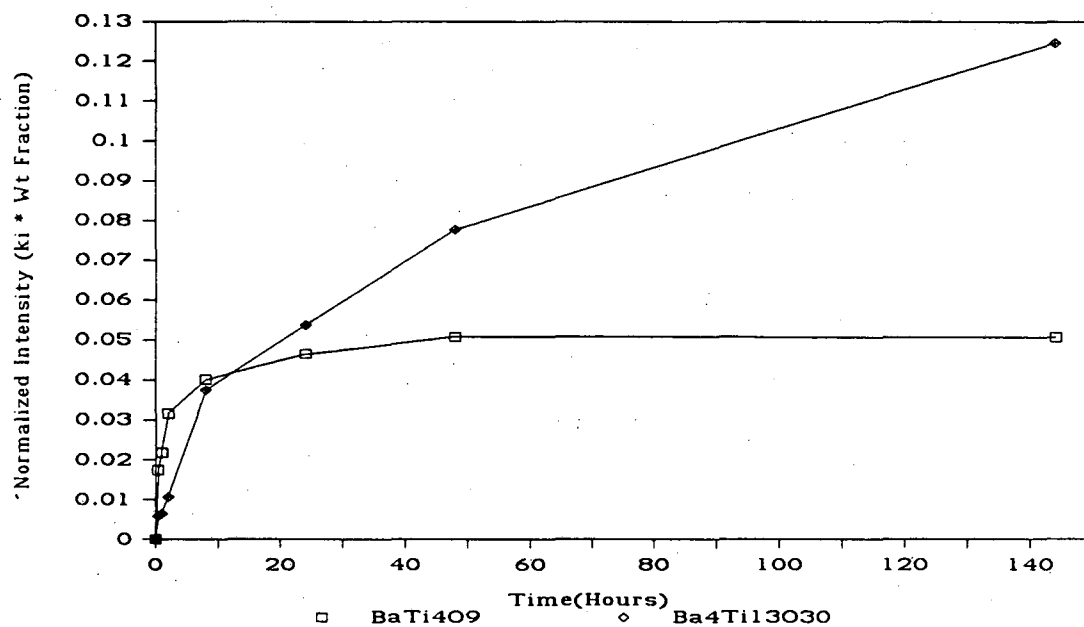
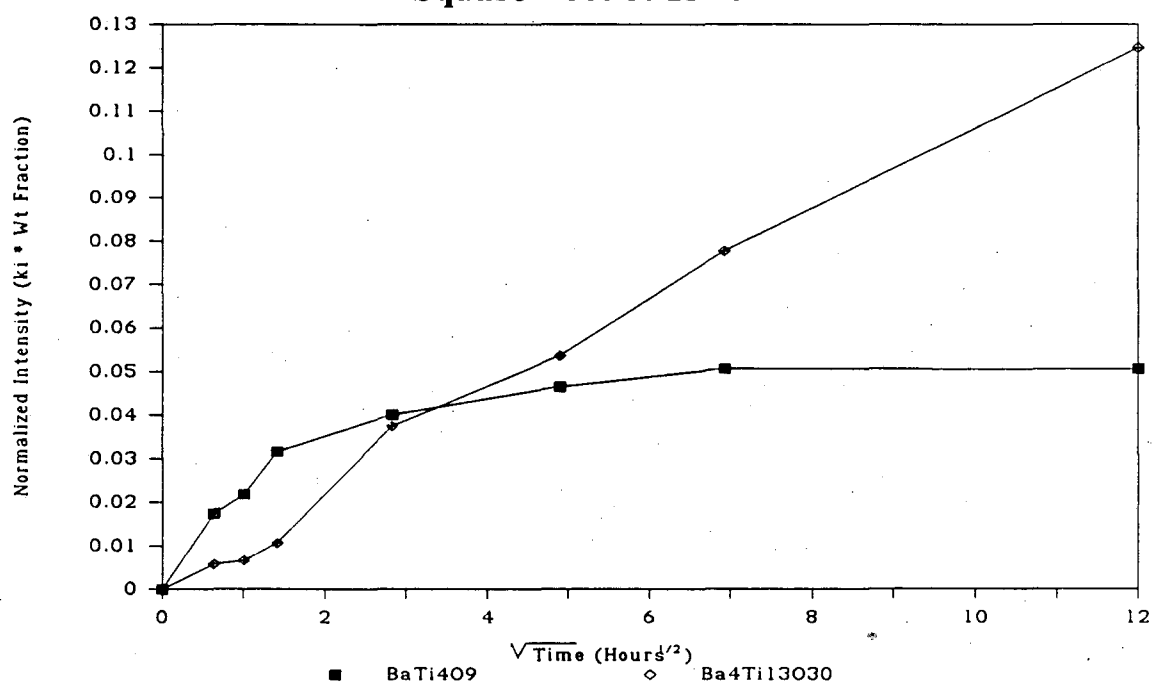


Figure 17
Normalized Intensity of Observed Intermediate Phases with Square Root of Time



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