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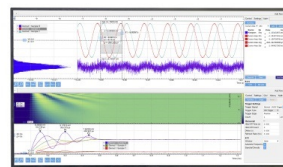
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# Molecular beam epitaxy of phase-pure antiperovskite $\text{Sr}_3\text{SnO}$ thin films

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## AFFILIATIONS

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## ABSTRACT

The antiperovskite oxide  $\text{Sr}_3\text{SnO}$  has attracted substantial interest due to its topologically non-trivial band structure. Sr-deficient  $\text{Sr}_{3-x}\text{SnO}$  can become superconducting, making it a candidate intrinsic topological superconductor. Here, we show that epitaxial, phase-pure  $\text{Sr}_{3-x}\text{SnO}$  films can be synthesized by molecular beam epitaxy (MBE) using solid Sr and  $\text{SnO}_2$  sources. We show that Sn-rich growth conditions result in a large amount of a Sn-rich impurity phase, which is challenging to detect in x-ray diffraction. Carrier densities and the amount of the impurity phase change systematically with the growth conditions, indicating that MBE provides excellent control over the films' stoichiometry. We discuss the electrical properties, including quantum interference phenomena, which support the topological nature of the films.

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Antiperovskite oxides with the chemical formula  $A_3BO$ , where  $A$  is an alkaline earth metal such as Ca, Ba, or Sr, and  $B$  stands for Sn or Pb, crystallize into a structure in which the positions of the  $A^{2+}$  and  $O^{2-}$  ions are exchanged relative to the well-known perovskite structure.<sup>1,2</sup> The metal ion on the  $B$ -site adopts an unusual 4-formal valence state.<sup>1,2</sup> The unusual electronic configuration is reflected in the band structures of these oxides, which feature band inversions, Dirac fermions, and topologically non-trivial Chern numbers.<sup>3–8</sup> For example,  $\text{Sr}_3\text{SnO}$  is a three-dimensional Dirac semimetal with a small bandgap (so is more correctly described as a topological crystalline insulator) that features six Dirac nodes along each of the six  $\Gamma$ -X directions.<sup>4</sup> Moreover, Sr-deficient  $\text{Sr}_{3-x}\text{SnO}$  is also superconducting.<sup>9–11</sup> The unusual combination of superconductivity and the topological band structure makes  $\text{Sr}_{3-x}\text{SnO}$  a candidate intrinsic topological superconductor,<sup>7</sup> which is very rare. Thus far, however, superconductivity has only been observed in highly Sr-deficient  $\text{Sr}_{3-x}\text{SnO}$  polycrystalline samples that also contain secondary phases.<sup>9–11</sup> The role of these impurity phases in observations of superconductivity in  $\text{Sr}_{3-x}\text{SnO}$  remains poorly understood.

Phase-pure, thin films of  $\text{Sr}_{3-x}\text{SnO}$  are of great interest for obtaining an improved understanding of its properties. Recently, molecular beam epitaxy (MBE) of  $\text{Sr}_3\text{SnO}$  and  $\text{Sr}_3\text{PbO}$  films has been reported.<sup>12–14</sup> These studies relied on x-ray diffraction (XRD) to ascertain phase purity of the films. Impurity phases in thin films can, however, be difficult to detect in XRD, especially if they are randomly oriented or poorly crystallized. Characterization of  $\text{Sr}_3\text{SnO}$  films by

electron microscopy techniques is challenging, because they are extremely reactive in air.

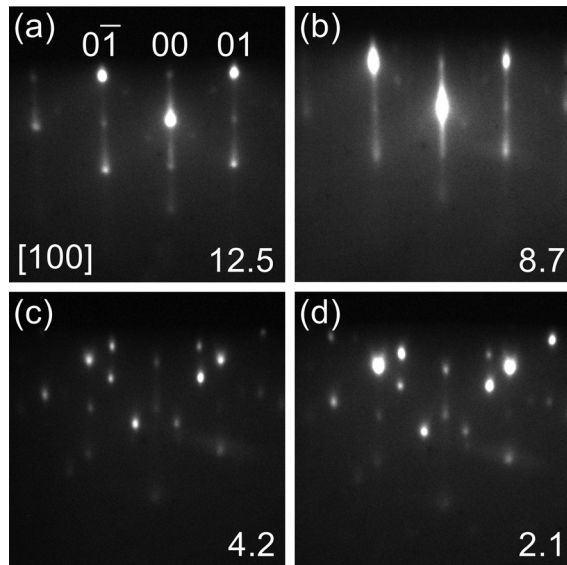
Here, we use a combination of XRD and *in situ* scanning electron microscopy (SEM) in a focused ion beam (FIB) instrument to investigate  $\text{Sr}_3\text{SnO}$  films grown by MBE. We show that phase-pure  $\text{Sr}_3\text{SnO}$  films can be grown. Under non-stoichiometric growth conditions, however, XRD is not able to detect large amount of a secondary phase even in films as thick as 850 nm. Moreover, transport properties are also surprisingly insensitive to the presence of a Sn-rich impurity phase.

$\text{Sr}_3\text{SnO}$  films were grown on (001)  $\text{LaAlO}_3$  substrates in an oxide MBE system (GEN 930, Veeco Instruments), by co-evaporation of high-purity elemental Sr (4N, Sigma Aldrich) and  $\text{SnO}_2$  (4N, Kurt J. Lesker) from solid source effusion cells (see the [supplementary material](#), Fig. S1 for a schematic of the sample structure). The solid  $\text{SnO}_2$  source supplies primarily SnO and  $\text{O}_2$ <sup>15</sup> and facilitates the growth of high-quality stannates by providing pre-oxidized Sn.<sup>16,17</sup>  $\text{Sr}_3\text{SnO}$  is cubic with a lattice parameter of  $a = 5.12 \text{ \AA}$ .<sup>1</sup> The lattice mismatch between  $\text{Sr}_3\text{SnO}$  and  $\text{LaAlO}_3$  [ $a = 3.79 \text{ \AA}$  (Ref. 18)] is about  $-5\%$ , assuming that  $\text{Sr}_3\text{SnO}$  grows with  $45^\circ$  in-plane rotation ( $5.12 \text{ \AA} / \sqrt{2} = 3.62 \text{ \AA}$ ), and we, therefore, expect epitaxial films to be fully relaxed. Substrates were backed with 350 nm Mo to improve the heat transfer from the substrate heater and were cleaned in acetone and isopropanol before loading into the entry/exit chamber. Prior to growth, the substrate was heated up to  $650^\circ\text{C}$  (thermocouple) and kept for about 10 min. The films' stoichiometry was controlled by keeping the Sr flux

constant and varying the flux from the  $\text{SnO}_2$  cell. Here, the Sr beam equivalent pressure (BEP) was  $5.0 \times 10^{-7}$  Torr, while the BEP from the  $\text{SnO}_2$  cell was varied between  $4.0 \times 10^{-8}$  and  $2.4 \times 10^{-7}$  Torr. The films discussed in the main text were grown with  $\text{Sr}/\text{SnO}_x$  BEP ratios of 12.5, 8.7, 4.2, and 2.1. The corresponding growth rates of these films were 140, 200, 480, and 850 nm/h, respectively, and are, therefore,  $\text{SnO}_x$ -flux limited. Film growth was monitored using *in situ* reflection high-energy electron diffraction (RHEED). Due to their extreme air sensitivity, samples for high-resolution XRD and FIB/SEM (FEI Helios dual beam) were protected by a layer of either  $\text{TiO}_2$  or  $\text{ZrO}_2$ . These capping layers were grown at  $375^\circ\text{C}$  in the same MBE chamber using titanium tetra isopropoxide and zirconium tert-butoxide as source materials.<sup>19,20</sup>

An additional Pt protection layer was deposited on a  $15 \times 2 \mu\text{m}^2$  rectangular area for cross-sectional SEM in the FIB instrument. Samples were imaged in the immersion mode using secondary electrons with sample surface tilted  $52^\circ$  relative to the electron beam. Films used for electrical measurements were uncapped. To avoid air-exposure, In contacts were soldered in van der Pauw geometry inside a  $\text{N}_2$  glove bag. The exposed sample surface was then covered by a layer of Apiezon-N grease. (Magneto-)transport measurements were performed in a physical property measurement system (Quantum Design) between 280 and 2 K. The thicknesses of the films used for electrical measurement was about 300 nm. The measured longitudinal magnetoresistance was symmetrized to cancel out the contribution from the Hall effect:  $R_{xx}^{sym}(B) = \frac{R_{xx}(B) + R_{xx}(-B)}{2}$ , where  $R_{xx}$  is the longitudinal resistance and  $B$  is the magnetic field and inverted to convert it into magnetoconductance.

Figure 1 shows RHEED patterns of  $\text{Sr}_3\text{SnO}$  films grown with different  $\text{Sr}/\text{SnO}_x$  BEP ratios [from (a) to (d): 12.5, 8.7, 4.2, and 2.1, respectively]. Spotty features are observed in all patterns, indicating three-dimensional (island) growth. The spotty-ness in RHEED is



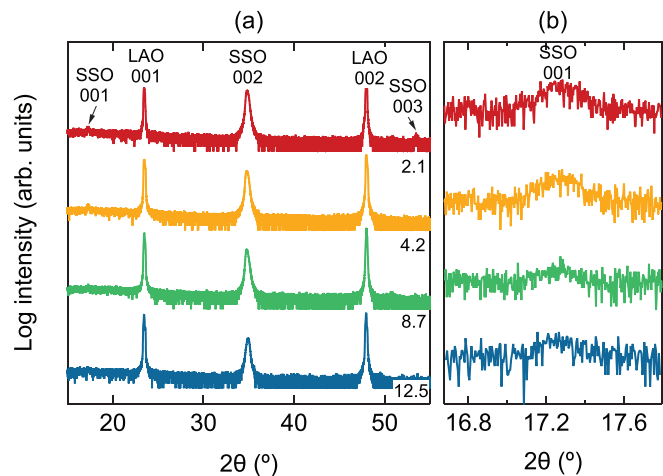
**FIG. 1.** RHEED patterns of  $\text{Sr}_3\text{SnO}$  films grown by MBE with four different  $\text{Sr}/\text{SnO}_x$  BEP ratios: (a) 12.5, (b) 8.7, (c) 4.2, and (d) 2.1, as indicated by the labels. The  $\text{LaAlO}_3$  substrate temperature was  $650^\circ\text{C}$  for all films.

much more pronounced for the films grown with  $\text{Sr}/\text{SnO}_x$  BEP ratios of 4.2 and 2.1, compared to those grown under less Sn-rich conditions. As discussed below, the film grown with the highest  $\text{Sr}/\text{SnO}_x$  BEP ratio [Fig. 1(a)] is phase pure.

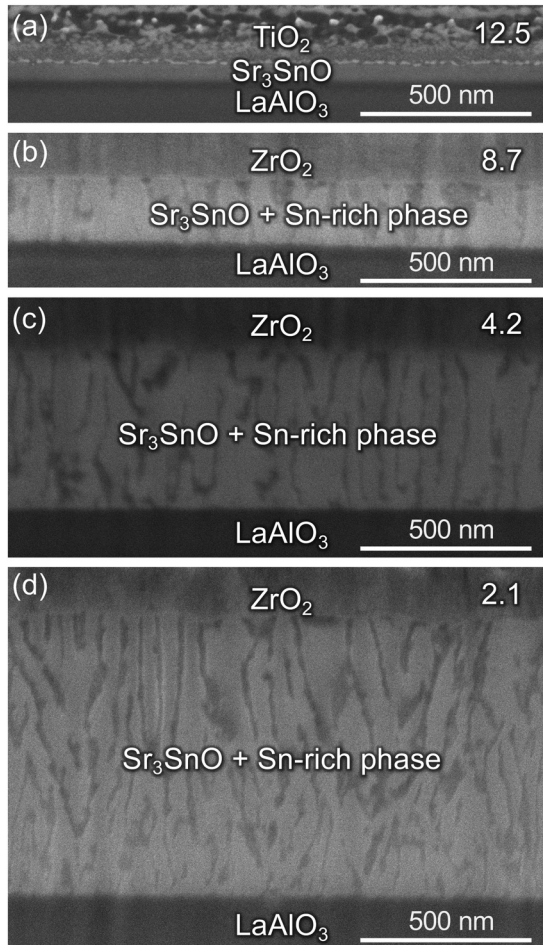
Figure 2 shows on-axis XRD scans of the films shown in Fig. 1. All reflections can be assigned to a (001)-oriented  $\text{Sr}_3\text{SnO}$  film and the substrate, with no additional reflections detected for all growth parameters. One issue is that SrO, which has a lattice constant close to that of  $\text{Sr}_3\text{SnO}$ , is a possible impurity phase in  $\text{Sr}_3\text{SnO}$ .<sup>10</sup>  $\text{Sr}_3\text{SnO}$  can be distinguished from SrO by the presence of  $00l$  ( $l = \text{odd}$ ) reflections, which are forbidden in face-centered SrO. All films show 001 and 003 reflections [see also Fig. 2(b)]. The greater intensity of the 001 reflections of films grown with lower  $\text{Sr}/\text{SnO}_x$  BEP ratios is due to increased growth rate at higher  $\text{SnO}_x$  fluxes, which results in thicker films for similar growth times (see Fig. 3 for the films' thicknesses). The presence of  $00l$  ( $l = \text{odd}$ ) reflections is, however, not sufficient to rule out SrO impurities. In addition, as mentioned above, impurity phases may be difficult to detect in XRD, especially if they are poorly crystallized.

To gain a better understanding of the phase purity of the films, we show in Fig. 3 cross-section SEM images of the same films. Images of the film grown with a  $\text{Sr}/\text{SnO}_x$  BEP ratio of 12.5 confirm the absence of secondary phases [Fig. 3(a)]. In conjunction with the XRD data, this shows that this film is phase-pure  $\text{Sr}_3\text{SnO}$ .

In contrast, films grown under Sn-rich conditions, shown in Figs. 3(b)–3(d), contain a secondary phase that appears as a columnar, dark region in SEM. The volume fraction of the secondary phase increases with an increasing  $\text{SnO}_x$  flux and corresponds to 25%, 30%, and 45%, respectively, for the films shown in Figs. 3(b)–3(d). The systematic increase in volume fraction indicates that the secondary phase is a Sn-rich alloy (not SrO). Importantly, the Sn-rich impurity phase is not detected in XRD even for films as thick as 850 nm. Reflections associated with the Sn-rich secondary phase can only be detected in XRD for extremely Sn-rich growth conditions, when the Sn-rich phase adopts a distinctly different morphology (see the [supplementary material](#)). We conclude that XRD alone is insufficient to ascertain phase-



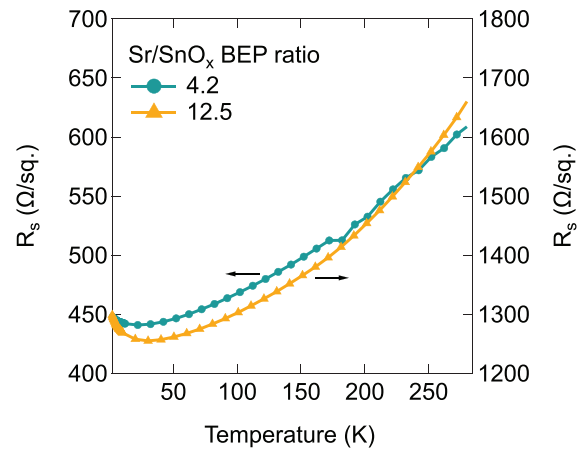
**FIG. 2.** (a) XRD  $2\theta$ - $\omega$  scans of  $\text{Sr}_3\text{SnO}$  films grown on (001)  $\text{LaAlO}_3$  substrates with different  $\text{Sr}/\text{SnO}_x$  BEP ratios, as indicated by the labels. (b) High resolution XRD  $2\theta$ - $\omega$  scan around the 001 reflection of  $\text{Sr}_3\text{SnO}$ . SSO:  $\text{Sr}_3\text{SnO}$  and LAO:  $\text{LaAlO}_3$ .



**FIG. 3.** Cross-sectional SEM images of  $\text{Sr}_3\text{SnO}$  films grown on  $\text{LaAlO}_3$  with four different  $\text{Sr}/\text{SnO}_x$  BEP ratios: (a) 12.5, (b) 8.7, (c) 4.2, and (d) 2.1. The films are capped by either  $\text{TiO}_2$  (a) or  $\text{ZrO}_2$  (b)–(d) to prevent the reaction in air.

purity of  $\text{Sr}_3\text{SnO}$  films even in cases where a secondary, Sn-rich phase constitutes a large volume fraction.

We next turn to the electrical properties. Figure 4 shows the sheet resistance,  $R_s$ , as a function of temperature for two films grown with  $\text{Sr}/\text{SnO}_x$  BEP ratios of 12.5 (phase pure film) and 4.2 (Sn-rich), respectively. Both films show metallic behavior followed by an upturn in resistance at low temperatures, similar to  $\text{Sr}_3\text{SnO}$  films reported in the literature,<sup>13,21</sup> and consistent with the negligible bandgap of  $\text{Sr}_3\text{SnO}$ . Both films are p-type (see the [supplementary material](#), Fig. S3). Their carrier concentrations are  $9.6 \times 10^{18} \text{ cm}^{-3}$  and  $1.5 \times 10^{19} \text{ cm}^{-3}$ , respectively. The carrier density in the films is well below the doping needed to induce superconductivity in  $\text{Sr}_{3-x}\text{SnO}$ , which requires Sr deficiency corresponding to at least  $x = 0.35$ .<sup>10</sup> Hole doping has been attributed to the presence of Sr vacancies.<sup>9,10</sup> The higher carrier density in the film grown under Sn-rich (Sr-poor) conditions is consistent with this interpretation. We note, however, that an increase of  $>200\%$  in the  $\text{SnO}_x$  flux only increases the carrier density by 50%. This is because the change in growth conditions results not only in increased Sr deficiency of  $\text{Sr}_{3-x}\text{SnO}$  but also in the formation of Sn-rich phases,



**FIG. 4.** Sheet resistance measured between 280 and 2 K of two  $\text{Sr}_3\text{SnO}$  films grown with different  $\text{Sr}/\text{SnO}_x$  BEP ratios of 12.5 and 4.2, respectively.

as discussed above. Comparing the two films, we see that the temperature dependence of  $R_s$  is qualitatively similar, while the higher  $R_s$  in the phase pure film is due to its lower carrier density. Both of these observations indicate that the secondary phase present in the Sn-rich film has surprisingly little influence on transport, likely because it is not percolated in this film.

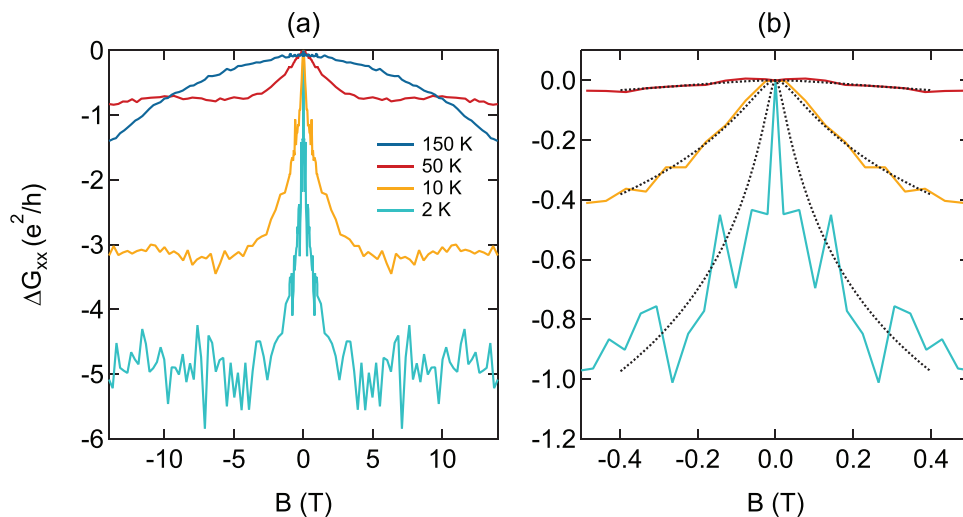
As shown in Fig. 5(a), phase pure films exhibit negative magnetoconductance at low temperatures under perpendicular magnetic fields (B). The magnetoconductance data at 50, 10, and 2 K can be fitted [see Fig. 5(b)] to the Hikami–Larkin–Nagaoka equation for weak antilocalization (WAL) in the strong spin–orbit coupling limit<sup>22</sup>

$$\Delta G_{xx} = \alpha \frac{e^2}{h} \left[ \ln \left( \frac{B_\phi}{B} \right) - \psi \left( \frac{B_\phi}{B} + \frac{1}{2} \right) \right], \quad (1)$$

where  $e$  is the elementary charge,  $h$  is Planck's constant,  $B_\phi$  is a phase coherence characteristic field, and  $\psi$  is the digamma function. The pre-factor  $\alpha$  takes the values -1 for weak localization and  $1/2$  for WAL. The extracted values for  $\alpha$  are 0.08 (50 K), 0.30 (10 K), and 0.45 (2 K). The corresponding values for the phase coherence length, given as  $l_\phi = \sqrt{\hbar/(8\pi e B_\phi)}$ , are 44, 87, and 146 nm. Strong WAL has previously been observed in  $\text{Sr}_3\text{SnO}$  films<sup>14</sup> and perovskites containing Sn.<sup>23</sup> The WAL is commonly observed in topological insulators and semimetals,<sup>24,25</sup> which can be understood to be the result of a  $\pi$  Berry phase associated with a spin-momentum-locked Fermi surface<sup>26</sup> or strong spin–orbit coupling.<sup>22</sup> The fact that  $\alpha$  approaches 0.5 at 2 K points to a Berry phase of  $\pi$  is consistent with a topological material. We note that the resistance upturn seen in the temperature-dependence of  $R_s$  (Fig. 4) is characteristic of weak localization, not WAL. Similar apparently contradictory behavior has been observed in topological insulators.<sup>24,27</sup> One possible explanation is that electron correlation effects are dominating the temperature dependence (Altshuler–Aronov correction<sup>28</sup>) while the magnetoconductance is dominated by WAL.<sup>24,27</sup>

In summary, we have shown that phase-pure conducting  $\text{Sr}_{3-x}\text{SnO}$  films can be grown by MBE, and their carrier densities (hole doping) can be controlled via the MBE growth parameters. Sn-rich growth conditions, which are needed for the high doping





**FIG. 5.** (a) Magnetoconductance of the phase pure film grown with a Sr/SnO<sub>x</sub> BEP ratio of 12.5 measured between -14 and 14 T at different temperatures. (b) A zoomed-in subset of the data in (a) at lower magnetic fields. The dotted lines are a Hikami-Larkin-Nagaoka fit. The data are symmetrized.

concentrations required for superconductivity in Sr<sub>3-x</sub>SnO, result in films that contain a large amount of a Sn-rich secondary phase. These secondary phases are difficult to detect in XRD but can readily be observed in electron microscopy images. Phase-pure films with carefully controlled doping densities, as afforded by MBE, are an ideal platform for future studies of topological transport phenomena.

See the [supplementary material](#) for a schematic of the sample structure, XRD and SEM images of extremely Sn-rich films, and the Hall measurements of the films shown in [Fig. 4](#).

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## AUTHOR DECLARATIONS

### Conflict of Interest

The authors have no conflicts to disclose.

### DATA AVAILABILITY

The data that support the findings of this study are available within the article.

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