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## **Publication Date**

1961-08-01

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Lawrence Radiation Laboratory

Contract No. W-7405-eng-48

Berkeley, California

# The Crystal Structure of Cobalt Sulfate Hexahydrate

by Allan Zalkin
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August 1961

The Crystal Structure of Cobalt: Sulfate Hexahydrate\*

By Allan Zalkin, Helena Ruben, and David H. Templeton

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#### Abstract

 $\cos O_{4}$ .  $6H_{2}O$  crystallizes in the monoclinic system, C2/c. The cell dimensions are  $\underline{a}=10.032$  A,  $\underline{b}=7.233$  A,  $\underline{c}=24.261$  A, and  $\beta=98.37^{\circ}$ . There are 8 molecules in the unit cell; the X-ray density is 2.006 g/cc. The structure consists of sulfate tetrahedra and cobalt-centered water octahedra linked by a three dimensional network of hydrogen bonds. Eleven of the twelve hydrogen bonds are between water and sulfate oxygens; there is one water to water hydrogen bond. The average S-O sulfate distance is 1.46 A; the average Co-O distance in the water octahedra is 2.11A; and the average hydrogen bond  $(O-H^{\circ}\cdots O)$  is 2.8 A. There are two crystallographically different  $Co^{++}$  ions in the structure. The hydrogen atoms are assigned an ordered configuration which would not contribute to residual entropy at low temperatures.

<sup>\*</sup>Work done under the auspices of the U. S. Atomic Energy Commission.

# Introduction

Calorimetric measurements by Rao and Giauque (1960) showed some unaccountable residual entropy in crystals of  $\cos O_{4} \cdot 6H_{2}$ 0 at low temperatures. We have investigated the crystal structure in search of an explanation of the disorder. The resulting structure offers no possibility of disordered rings of hydrogen bonds such as were found in  $Na_{2}SO_{4} \cdot 10H_{2}O$  (Ruben, Templeton, Rosenstein and Olovsson, 1960), nor do we find any other explanation of the entropy discrepancy.

The crystal morphology was described by Marignac (1855), and Groth (1908).

# Experimental

Crystals of  $\cos O_4$ .  $6H_2O$  were grown from a saturated solution at 50 - 55°. The intensity data were obtained by multiple film Weissenberg techniques. The film photography was done using Fe K $\alpha$  ( $\lambda$ =1.9373 A) X rays, on Ilford Industrial G film. Intensities were estimated visually by comparison with a calibrated set of spots. The scaling factor used between multiple films of the same layer was  $\exp(2.0 \sec \mu)$ , where  $\mu$  is the equi-inclination angle and 2.0 is an empirically determined constant from the data; this scaling factor varied from 7.4 at the zero layer ( $\mu$ =0°), to 12.9 at the sixteenth layer ( $\mu$ =38.7°).

The first single crystal of  $\cos O_{4}$ .  $6H_{2}O$  was enclosed in a .1 mm. glass capillary. At the time we felt the crystals would be unstable in the open atmosphere, however, later we found the crystals to be sufficiently stable to handle in air. This first crystal was aligned about the [101] direction. Seventeen layers were photographed and 737 reflections were observed of which

125 were below the detection limit and called zero. Later a second crystal was aligned about its <u>b</u> axis and photographed in air. An additional 99 zero layer reflections were measured of which 10 were below the detection limit. The sum total of intensities used was 836, of which 135 were recorded as zero.

For greater accuracy, the cell dimensions of  $CoSO_4$ . $6H_2O$  were measured on a General Electric XRD-5 equipped with a goniostat using Mo K $\alpha$  ( $\lambda$ =.7107 A) X rays.

In order to solve the structure we found it necessary to take some reflection data from  ${\rm MgSeO_4.6H_2O}$  and  ${\rm MgSO_4.6H_2O}$  both of which are isomorphic with  ${\rm CoSO_h.6H_2O}$ .

A crystal of  ${\rm MgSO}_4$ .6H<sub>2</sub>O was grown from its saturated solution at 50-55°. It was aligned about its <u>b</u> axis and photographed with Fe K $\alpha$  X rays with the Weissenberg technique. Intensities were recorded of 102 h $\alpha$  reflections of which 6 were below the detection limit. Cell dimensions were measured on the goniostat as with the cobalt isomorph.

 ${
m MgSeO}_4$ .  ${
m 6H}_2{
m O}$  crystals were prepared at room temperature by allowing a filtered solution of dilute selenic acid and excess MgO to evaporate in an open dish. A crystal was aligned along its <u>b</u> axis and photographed with the Weissenberg technique with Fe K $\alpha$  X rays. Intensities were recorded of 102 hOl reflections of which 15 were below the detection limit. The cell dimensions were obtained from the Weissenberg films.

# Cell dimensions and space group

The cell dimensions of CoSO, 6H, 0 are:

$$\underline{a} = 10.032 \pm .004 \text{ A}$$
  $\beta = 98.37 \pm .03^{\circ} (98.7^{\circ} \text{ by Marignac (1855)})$ 

$$\underline{b} = 77.233 \pm 2003 \text{ A}$$
  $V = 1742 \pm 2 \text{ A}^3$ 

$$c = 24.261 \pm .010 A$$
  $Z = 8$ 

space group = C2/c  $(C_{2h}^6)$ 

$$\underline{a}:\underline{b}:\underline{c} = 1.387:1:3.354$$
 (1.396:1:3.381 by Marignac (1855))

X-ray density = 2.006 g/cc: measured density = 2.000 (Gosner, 1907),

2.019 (Thorpe and Watt, 1880), 2.017 (Handbook of Chemistry and Physics, 1957).

The characteristic extinctions of the intensities indicated space group Cc or C2/c. As there are 8 molecules in the unit cell and C2/c has an 8 fold general position as opposed to 4 for Cc, C2/c appeared intuitively to be the most likely space group. A "zero moment test" on the 3 dimensional data was computed (Howells, Phillips and Rogers, 1950) and the results indicated a center of symmetry, space group C2/c. The best evidence we have for the space group C2/c is the successful solution of a chemically reasonable structure. The cell dimensions of MgSO<sub>h</sub>.6H<sub>2</sub>O are:

$$\underline{a} = 10.110 \pm .005 A$$
  $\underline{c} = 24.41 \pm .01 A$ 

$$\underline{b}$$
 = 7.212 ± .004 A  $\beta$  = 98.30 ± .04 A

The cell dimensions of MgSeO4.6H2O are:

$$\underline{a}$$
 = 10.36 ± .03 A  $\underline{c}$  = 25.1 ± .1 A

$$\underline{b} = 7.38 \pm .04 \text{ A}$$
  $\beta = 98.1 \pm .2^{\circ}$ 

## Determination of Structure

The three-dimensional Patterson function of  $\cos O_4$ .  $6H_2O$  was computed. Attempts were made to associate the larger peaks with Co-Co, S-S, and Co-S vectors; however, two trial structures with Co atoms in general positions failed to give a reasonable Fourier projection in the <u>b</u> direction. Later it was learned that Co atoms are in two sets of special positions.

Crystals of the isomorphic compounds MgSO<sub>4</sub>.6H<sub>2</sub>O and MgSeO<sub>4</sub>.6H<sub>2</sub>O were prepared and photographed. From the Patterson projections calculated from the three sets of hO2 data we found the locations of the Co and S atoms.

A set of trial oxygen positions was obtained from an hole Fourier projection of the  ${\rm MgSO}_4$ .6H<sub>2</sub>O. The signs of 54 of the 96 non-zero structure factors were estimated from the location of the Mg and S positions. All of the ten oxygen atoms were found. A new calculation of signs led to a sign change in only two of the original 54 data used. A second Fourier projection using 86 non-zero terms clearly showed the basic arrangement of  ${\rm SO}_4$ = tetrahedra and  ${\rm Mg(H_2O)}_6^{++}$  octahedra.

The holdata for the MgSO  $_4$  .6H  $_2$ O and MgSeO  $_4$  .6H  $_2$ O is shown in tables 1 and 2.

In  $CoSO_{4}$ . $6H_{2}O$  eight cobalt atoms occupy positions 4(a) and 4(e): 4(a) 0,0,0; 0,0,1/2 + C centering.

4(e) 0,y,1/4; 0,-y,3/4 + C centering.

The sulfur atoms and ten sets of oxygen atoms occupy the general 8(f) positions:  $8(f) \times y,z; -x,-y,-z; -x,y,1/2-z; x,-y,1/2+z+C$  centering.

A fourier projection of the hOl data of  $CoSO_4$ .  $6H_2O$  was calculated and the x and z parameters of the cobalt, sulfur and oxygen positions were evaluated. The y parameters were estimated from expected S-O bond distances in the sulfate ion and O-O distances about the hydrated cobalt ion.

Table 1: The hOl observed structure factors for MgSO1.6H20

```
h= -10.-8 -6 -4.-2 00. 2 4.60.8 10
    28 49 25 40 38
    29 39 0 49 46 0 53 40 17 30 30
   37 24 39 34 45 22 64 9 30 34
   29 15 13 38 49 0 86 17 54 18
     0 35 40 42 64 34 7 14 45 44
       13 18 31 18 39 31 65 40 22
10.
      0 33 46 16 46 98 64 40 18
12
       6 43 27 33 32 25 26 19
14
       38 15 11 11 65 24 13 40
16
       20 21 10 37 33 71 33 34
18
          0 51 39 46 32 49
20
        14 13 17 9 39
22
            12 38 41
24
```

Table 2: The hOl observed structure factors for MgSeO, 6H,0

```
h= -10 -8 -6 -4 -2 00 2 4 6 8 10
1=0 0 47 17 51 25
 2 220 24 33 67 80 00 83 24537 0 16
    20 12 13 50 41 33 56 31 7 27
 6 21 00 20 20 73 00114 11 49 8
     0 38 34 0 71 42 10 26 17 24
   11 10 13 20 39 17 15 38 0 13
12
       16 16 59 0 50 55 48 11 7
14
      0 41 7 45 9 39 17 20
16
       23 0 10 0 58 15 12 21
18
       10 17 10 33 20 59 16 26
          0 32 15 33 15 34
20
         15 0 18 0 23
22
24
               13 23
```

Least squares refinement utilizing the full matrix (Busing and Levy, 1959) was performed for a total of 13 cycles on the IBM 704 computer. Atomic form factors of Co<sup>++</sup> (Watson and Freeman, 1961), neutral S (Tomile and Stam, 1958), and neutral O (Hartree and Hartree, 1939) were used in these calculations. 836 intensity data were used, 737 of which were obtained from a crystal rotated about the [101], and 99 of which were obtained from a zero layer about a [010] rotation. 18 scale factors, 34 positional parameters and 13 isotropic temperature factors for a total of 65 parameters were varied. The overall R factor, where  $R = \frac{\sum ||Fobs|| - |Fcalc|| ||x|| 100}{\sum |Fobs|}$ , was 54% before refinement commenced, dropped to 42% after the first refinement and then dropped steadily to the final value of 13%. The necessity to run so many cycles was in part due to certain blunders in the original estimate of the y parameters for the oxygen atoms. The final R factors are as follows:

R (including zeros) = 13.0%.

R (omitting zeros) = 10.9%.

The data are shown in table 3.

The atomic parameters are shown in table 4. By an oversight the dispersion correction of of about -1.8 electrons (for Fe Ka) was omitted from the cobalt form factor. As a result, the temperature factors for cobalt in Table 4 are larger than the true values by an unknown amount.

Table 3: Observed and calculated structure factors for  $\cos 0_4 \cdot 6 \rm{H}_2 \rm{O}$ . The observed values are listed above the calculated ones.

											K≖									
		L=	-19	-18	-17	-16	-15	-14	-13	-12	-11	-10	<del>-</del> 9	-8	-7	-6	<b>-</b> 5	-4	-3	-2
						105		89		135		42		192		208		232		169
Н	=	2				-79		-68	4	-114		.38		124	•	-160		221		172
Н	=	4				77 76		51 -49		223 217		77 65		165 150		58 46		143 148		162 168
					•			4,5				•		150		0		103		0
H		6													*	7	•	117		19
н	=	8					•				r			95 85		27 <b>-</b> 21		70 85		-46 -60
		_		•										· ·		40		69		26
Н	= 1	0														<b>-</b> 51		-77		30
											K=				•					
		L=	-19	-18	-17	-16	-15	-14	-13	-12	-11	-10	-9	<b>-</b> 8	<b>-</b> 7	-6	~5	-4	-3	-2
					15	76	0	105	37	64	77	108	135	47	68	137	96	323	52	131
Н	<b>#</b>	1			-17	-61	-9	84	-35	-56	68	-90	102	<del>-</del> 57		116	-88-			131
	_	2	26	27	48	152	75	51	3.8	0	0	- 0	30	237	74	59		128	105	97
п	=	2	3.2	22	38 0	151 112	-67 22	32 45	-50 33	10 77	0 69	2 77	30	213 157	<b>-</b> 66	-49 29	80 39	121 98	101-	
Н	=	5				-98		-48		-74	78		-58		-40	-29	<del>-</del> 45	116	1	91 94
										, • •			-		0	Ťó	39	89	õ	43
Н	=	7													13	-0		-8:8	-18	37
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• •													-20	74	0		-,	01	20	27
											K= :									
		L=	-19	-18	-17	-16	-15	-14	-13	-12	-11	-10	-9	-8	-7	., <b>–</b> 6	-5	-4	-3	<del>-</del> 2
						139	106	28	74	178	94	15	. 0	178	52	156	30	29	37	43
· H	=	0				-131		23	-58		86	<b>-</b> 5		-154		-124		-40		-41
		2	*	15	83	102	0	32		163	106		102		47	93	69	66	100	
н	=	2		-14	83 33	88 0	<b>-</b> 8	26 51	_	156 138	<b>-</b> 95	-16 21	100	130 94	-31 23	-71 0	55 159		-94- 67	·203 81
Н	#	4			47	<b>-</b> 5		-54		-134	75	-28		-96	-21		-150-		<b>-</b> 79	83
				31	,	0	53	69		37	. 0	56		39	23	0	0	72	0	49
H	=	6		38		18	-64	<del>-</del> 72		47	16	71			-23		-12	69	-7	55
н	<b>=</b>	8												90 -85	0 24	50 <b>~</b> 52	0 -1	0 -13	_0 -23	0 9
• •		•												0,5	24		•	13		
		٠		1.0			3.5	• •			K= :			_	_	_	_			
		_=	-19	-18	-17	-16	-15	-14	-13	-12	-11	-10	<del>-</del> 9	-8	<del>-</del> 7	<del>-</del> 6	<del>-</del> 5	-4	-3	-2
		_				42				91				117			87			17
Н		1		24	18	37		-40			-65				<b>-43</b>		85			
н	= ;	3	1	34 -46	30 <b>-</b> 12	66 -68	31 38	21 -12	51 <b>-</b> 51	34 -35	56 -61	49 <b>-</b> 48			133 141		174 •176 <b>-</b>		22 24	39 39
				. •	45	47	0	64	47	17	41	Ŏ		104	75	40	66	32	33	19
H		5			47	47	9		-48		<b>-3</b> 5	-11	88	98	<b>-77</b>		-64		<b>-</b> 42	-12
ы.	=	7						22	39 -43		56				25 <b>-</b> 21	27	19	62	56	0 3
111	-	•				÷		-24	-42	-11	61		0	48		18	<del>-</del> 20 56	49 37	61 24	33
Н	<b>=</b> (	9												-41			51			-32

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L= -19 -18 -17 -16 -15 -14 -13 -12 -11 -10
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               56 36
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                                                  66
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H= 2
              -68 -31
                           -49 -29 -43
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                       54
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H=6
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                                          -41
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H= 8
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   L= -19 -18 -17 -16 -15 -14 -13 -12 -11 -10
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H=7
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                                      K= 6.
   L= -19 -18 -17 -16 -15 -14 -13 -12 -11 -10 -9 -8 -7
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H= 4
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H= 6
                                      K = 7
 L= -19 -18 -17 -16 -15 -14 -13 -12 -11 -10
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H=1
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         -192
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                   -44
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H = 6
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          119
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H= 8
          122
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                    24
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H=10
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   L=
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       19 102
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43 20 18 31
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                                                                       74
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                                  5 125 -21 154
      21 102
                43-123 -69 276
                        14
                                         47 203
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       61 106
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H= 5
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H= 9
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H = 0 -78 - 222
               60 129 115
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      127 126
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                        97 81
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H= 2 -136 132
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       -7 126 128 -63 -46 122
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H = 6
       32 92 22 14
                                  0 16
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H= 8
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H=	4	150		. 46		148		168		21		-44		91		27		80
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Table 4: Atomic parameters for CoSO<sub>h</sub>.6H<sub>2</sub>O.

Coj		<b>x</b> O	<b>y</b> O	<b>z</b> 0	B(A <sup>2</sup> ) 3·3
co <sub>2</sub>	٠,	0	.949 ± .001	1/4	3.0
s		.868 ± .001	.452 ± .001	.1244 ± .0003	2.2
Ol		.778 ± .001	:601 ± :002	.1352 ± .0006	2.6
02	sulfate	.980 ± .002	.446 ± .003	.1695 ± .0007	3.9
03	oxygens	.918 ± .002	.492 ± .003	.0698 ± .0007	3.9
0,4	s i	.799 ± .001	.276 ± .002	.1193 ± .0006	2.9
05	water	.592 ± .001	.723 ± .002	.0469 ± .0006	2.8.
06	octahedra about Col	.535 ±.0002	.325 ± .002	.0673 ± .0006	3.2
07		.305 ± .002	.557 ± .003	.0216 ± .0006	3.3
08	water	.885 ± .002	.159 ± .002	.2823 ± .0007	2.3
09	octahedra about Co	.886 ± .002	.740 ± .002	.2832 ± .0007	2.7
010	2	.858 ± .001	.949 ± .003	.1771 ± .0006	3.3

# Discussion of the Structure and Hydrogen Bonding

The structure consists of discrete  $SO_{4}$  = tetrahedra and  $Co(H_{2}O)_{6}^{++}$  octahedra, Fig. 1. There are just enough water molecules to satisfy this octahedral hydration of each cobalt ion.

Hydrogen bonds are assigned to the twelve shortest oxygen-oxygen distances (Table 5) after disregarding these between oxygen atoms of the same sulfate ion or of the same coordination octahedron. This assignment is checked by consideration of the hydrogen atom configuration and bond angles. Except for one water molecule  $(0_9)$  each water has two hydrogen bonds to sulfate oxygen atoms. Water molecule  $0_9$  has one such bond and also a bond to atom

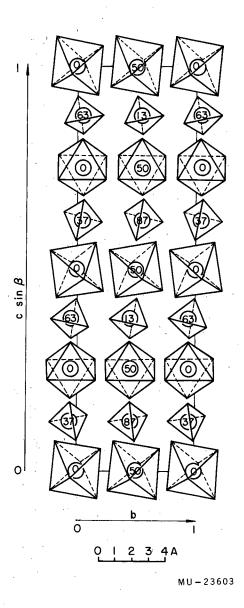


Fig. 1. Packing of  $SO_{l_1}$ = tetrahedra and  $Co(H_2O)_6^{++}$  octahedra. The encircled numbers are the parameters of the Co and S atoms in the <u>a</u> direction.

Table 5: Interatomic Distances in  $CoSO_{4}.6H_{2}O$ . Standard deviations are about  $\pm$  .03 A.

	<u>s</u>	ulfate	oxygens		а	bout Co	water o	a	bout Co	
	o <sub>l</sub>	02	03	04	o <sub>5</sub>	06	07	08	09	010
A					(0.11	G 05 1				
Col	ŧ				2.11	${2.05}$	2.14	·	· ·	<b>C</b>
$\operatorname{Co}_2$					<b>—</b> ,			2.13 $2.13$	$\begin{cases} 2.12 \\ 2.12 \end{cases}$	2.11 2.11
S	1.46 <sup>s</sup>	1.44 <sup>8</sup>	1.51 <sup>s</sup>	1.45 <sup>s</sup>					C	
o		2.36	2.40	2.40	2.77 <sup>h</sup>		egeneration of the second	2.79 <sup>h</sup>		2.79 <sup>h</sup>
02	2.36		2.43			7			2.69 <sup>h</sup>	·
03	2.40	2.43		2.40	2.72 <sup>k</sup>	2.68 <sup>h</sup>	2.93 <sup>h</sup>			· · ·
04	2.40	2.37	2.40	,	•		2.86 <sup>h</sup>			2.76 <sup>h</sup>
	2.77 <sup>h</sup>		2.72 <sup>h</sup>			2.89 2.99 2.94 2.99	2.90 3:10			
06			2.68 <sup>h</sup>	2.78 <sup>h</sup>	{2.89 {2.99		2.94			
07			2.93 <sup>h</sup>	2.86 <sup>h</sup>	2.90 3.10	$\begin{cases} 2.94 \\ 2.99 \end{cases}$			<u> </u>	
08 .	2.79 <sup>h</sup>	2.65 <sup>h</sup>		-				2.97	3.00 <sup>h</sup> 3.03 2.99	$\begin{cases} 2.94 \\ 3.04 \end{cases}$
09		2.69 <sup>h</sup>			•			{3.00 <sup>11</sup> {3.03	2.99	2.96 3.03
010	2.79 <sup>h</sup>			2.76 <sup>h</sup>				2.94	(2:96 (3.03	Mar B

h hydrogen bond distances.

s S-0 bond in  $SO_{14}$ =

 $0_8$ . In this bond geometry, there is only one configuration of hydrogen atoms with two hydrogen atoms on each water molecule. The angles between hydrogen bonds at these water molecules (Table 6) range from  $97^{\circ}$  to  $126^{\circ}$  and are within the range found for other hydrated sulfate crystals. The hydrogen bonds make angles of  $111^{\circ}$  to  $124^{\circ}$  with the water-cobalt vectors. The third hydrogen bond to  $0_8$  makes angles of  $80^{\circ}$  and  $117^{\circ}$  with the two hydrogen bonds for which  $0_8$  provides the hydrogen atoms.

Table 6: Hydrogen bond angles. 0 through  $0_4$  are sulfate oxygens.  $0_5$  through  $0_{10}$  are water molecules.

atoms	angles
01 - 05 - 03	117°
	105°
03 - 07 - 04	126°
01 - 08 - 02	97 <sup>°</sup>
02 - 09 - 08	116°
01 - 01004	124°

The hydrogen bond lengths are 2.65 to 2.93 A for the bonds to sulfate and 3.00 A for the water-water bond. The shortest non-bonded oxygen-oxygen distances other than edges of the octahedra, are 3.13 A between 07 pairs (through a center of symmetry) and 3.22 A between 09 and 04.

We find no reasonable alternative to this hydrogen configuration, and the entropyy discrepancy is not explained by our work.

The hydrogen bonds tie the sulfate ions and water octahedra together in a three-dimensional network as indicated in Fig. 2. In this figure, the

hydrogen configuration is indicated by small circles on the hydrogen bonds. Because of the bond angles the hydrogen atoms are expected to fall slightly off these lines joining oxygen atoms. We do not have a direct determination of the hydrogen positions from the diffraction data.

The two cobalt ions,  $\mathrm{Co}_1$  and  $\mathrm{Co}_2$ , have point symmetries  $\overline{1}$  and 2 respectively. The water octahedron about  $\mathrm{Co}_{\underline{1}}$  is hydrogen bonded exclusively to sulfate ions. The  $\mathrm{Co}_2$  water octahedron has ten hydrogen bonds to sulfate ions and four involving water molecules of neighboring  $\mathrm{Co}_2$ -type octahedra.

The average interatomic distances are as follows:

S - 0 (SO<sub>$$\mu$$</sub><sup>=</sup>) 1.46 A  
O - 0 (SO <sub>$\mu$</sub> <sup>=</sup>) 2.39 A  
Co- 0 (Co(H<sub>2</sub>O)<sup>++</sup><sub>6</sub>)2.11 A  
O-H-O (hydrogen bond) 2.79 A...

Several other substances have the same structure as  $CoSO_4$ .  $6H_2O$ . In addition to the two magnesium compounds,  $CoSeO_4$ .  $6H_2O$ ,  $ZnSO_4$ .  $6H_2O$ , and one form of  $NiSO_4$ .  $6H_2O$  are isomorphous (Groth, 1908). This structure has been recognized in nature as the minerals hexahydrite,  $MgSO_4$ .  $6H_2O$ , and bianchite,  $ZnSO_4$ .  $6H_2O$  (Palache, Berman and Frondel, 1952).

A more thorough study of the structure of MgSO<sub>14</sub>.6H<sub>2</sub>O is in progress, and the location and refinement of the hydrogen parameters in that crystal will be the topic of another article shortly.

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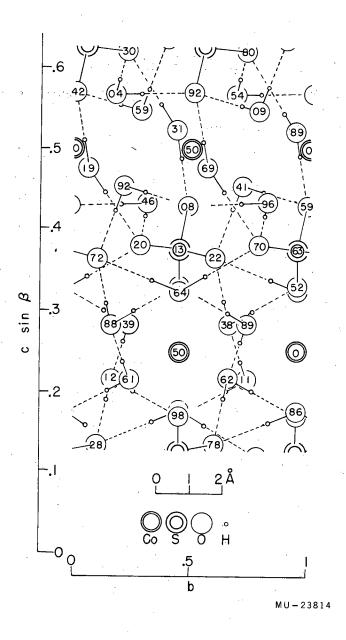


Fig. 2. Hydrogen bond network in  $\cos O_4 \cdot 6H_2^\circ$ . The numbers are the parameters along the <u>a</u> axis of the Co, S, and O atoms. The complete environment about each of the two different  $\cos(H_2O)_6^{++}$  and  $sO_4$  = is shown.

# Aknowledgement

We thank Dr. Rao and Professor Giauque for their unpublished thermodynamic data and for valuable discussions.

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