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1 LAY SUMMARY: The estimation of mating preference is essential to understand how
2 sexual selection through mate choice shapes both mating systems and sexual
3 dimorphisms. We present a new method for detecting and quantifying both stabilizing
4 and directional mating preferences and demonstrate the experimental and statistical
5 advantages of this method over previous approaches. We illustrate the method using data
6 from a mate choice experiment in which female sand crickets were provided a choice of
7 two males. Both directional and stabilizing preference are identified for components of
8 the male call song.

9

10 A NEW METHOD FOR STATISTICAL DETECTION OF DIRECTIONAL AND
11 STABILIZING MATING PREFERENCE

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18 Running title: Detection of directional and stabilizing mate preference

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23 ABSTRACT

24 Estimation of mating preferences is a prerequisite for understanding how sexual selection
25 through mate choice shapes both mating systems and sexual dimorphisms. Most studies
26 of mating preferences assay mate choice using either a no choice or a binary choice
27 design. Binary choice trials typically employ either an artificial signal or some fixed
28 difference (e.g. color or size) between the signaling individuals. Although statistically
29 more powerful than no choice designs, such experiments cannot be used to detect
30 stabilizing preference. Further, the use of artificial signals is problematic because signal
31 components tend to be varied in isolation, and hence do not reflect natural variation.
32 Here we present a new method that uses natural variation among individuals in choice
33 trials to determine if mating preference is absent, directional and/or stabilizing. The
34 protocol is tested using simulation and shown to be robust to the preference function, to
35 have the required statistical power, to be unbiased in almost all cases, and to give
36 confidence regions that modestly overestimate the desired 95% criterion. We
37 demonstrate the use of the method with data from mate choice trials of the sand cricket,
38 *Gryllus firmus*. Software to apply this new approach is provided in Dryad.

39 keywords: mate choice, preference, directional preference, stabilizing preference

40 INTRODUCTION

41 Mating preferences act as significant selective agents on traits that influence the
42 probability of being chosen (Jennions and Petrie 1997, Jennions et al. 2012). Such
43 selection may be directional, stabilizing or a combination of both. Preferences for traits
44 that function primarily in species recognition are likely to exert stabilizing selection
45 because directional preference could potentially drive the preferred trait values into
46 regions in which they might be confused with trait values found in other species (Ferreira
47 and Ferguson 2002, Zuk et al. 2008). Directional preferences (i.e., preferences for
48 increasing or for decreasing values of the preferred trait) are more likely to be found for
49 traits such as the amount of time spent displaying, duration of individual displays, or the
50 intensity of display (e.g., call loudness, color saturation or brightness: Jang and
51 Greenfield 1998, Bentsen et al. 2006). Such traits are less likely to function in species
52 recognition and more likely to vary with the health and condition of the signaler.
53 Therefore, the form of selection acting on traits in the chosen sex is likely to vary among
54 the target traits (hereafter, ‘preferred traits’). The extent to which preferred traits are
55 able to evolve independently in response to this selection depends upon the covariation
56 among traits. For example, if a trait that is essential for species recognition is highly
57 correlated with a trait that is initially subject to directional preference, the latter trait may
58 be constrained in its response to directional selection because of the indirect effects of
59 stabilizing selection on the correlated trait. Preference for this trait may ultimately shift
60 to being stabilizing if potential mates with extreme trait values are confused with another
61 species. Thus we might expect that directional selection through mate choice will

62 primarily target traits that are not constrained by overlap with trait values in other species
63 or by strong correlations with such traits.

64 Determining which traits are preferred and how selection through mate choice is
65 acting on these traits is clearly a prerequisite for understanding of how both preferences
66 and preferred traits evolve. For many species, traits likely to be assessed by the choosy
67 sex (hereafter denoted as females for convenience) are readily apparent: for example, in
68 orthopterans and anurans components of the call song would be a prime candidates. Call
69 songs can differ along many dimensions, such as loudness, carrier frequency, repetition
70 rate etc. Some of these characteristics may serve primarily as species recognition signals,
71 others as indices of mate quality, and others are signals that females may prefer for no
72 obvious reason (Bentsen et al. 2006).

73 Given that a number of traits or trait components may be preferred to a greater or
74 lesser degree, the initial goal of most investigations of mate choice has been to identify
75 which traits are preferred and if possible, measure the strength of the preference. The
76 general approach has been to conduct experiments in which individual components are
77 isolated and one or more measures of preference taken. This may be done using a no
78 choice or a choice design. An excellent example of the no choice design is the study of
79 female preference for the male calling song in the cricket *Gryllus integer* (Gray and Cade
80 1999). In this study artificially generated call songs that differed in pulses per trill were
81 broadcast to a female and her response measured using a Kugel apparatus. Female
82 preference was defined as the highest response elicited from the female. The experiment
83 showed that females preferred an intermediate number of pulses per trill, clearly

84 demonstrating stabilizing preference for this trait when varied independently of other
85 calling traits. In a choice design, several potential mates or the signals from several
86 potential mates are presented simultaneously to an individual of the choosing sex. The
87 potential mates differ with respect to some character or characters that the choosing sex
88 could use to discriminate amongst them. An example of this approach is the analysis of
89 female preference for acoustic traits in the gray tree frog, *Hyla versicolor*. Each female
90 was presented with two male calls from two speakers and her preference assessed
91 through her orientation to the speakers (Gerhardt et al. 2000). Females were observed to
92 prefer long duration calls with the strength of preference depending on whether the calls
93 were below or above the average call duration (Gerhardt et al. 2000).

94 A meta-analysis of experiments using both choice and no choice designs showed
95 that choice trials were more likely to detect significant preferences than no choice trials
96 (Dougherty and Shuker 2015). We reviewed the designs of published choice experiments
97 (supplemental material section 1) and discovered that in most (73%), the choosing sex
98 (usually females) was presented with a choice of potential mates that differed on the basis
99 of some *a priori* recognizable character such as condition or morphology. The remainder
100 of choice studies used artificial signals (e.g. physical models or computer generated
101 acoustical signals). In either case, the great majority of choice experiments (80%) parsed
102 the trait distributions of the chosen sex into very few (usually only two) predetermined,
103 discrete categories. In such cases statistical analysis was based on comparison of the
104 mean or median trait values in chosen versus not-chosen individuals using categorical
105 methods such as chi-square or Wilcoxon matched pairs. Use of such a limited number of

106 trait categories may increase the power to detect significant preferences, but it precludes
107 discrimination of directional from stabilizing preference as curvature cannot be
108 established.

109 The challenge addressed in the present study is to develop a method based on
110 choice experiments using natural signals that will allow researchers to determine not just
111 which traits are preferred but also the form of the preference function (directional,
112 stabilizing or both). Our method makes use of naturally occurring variation in the signal
113 and thus does not suffer from problems of lack of variation in the signal, variation of only
114 one component in isolation, or an unnatural mixture of components. Using our method,
115 researchers will be able to analyze multiple traits within a single choice experiment and
116 statistically test for the presence of directional and stabilizing selection. We first use a
117 simulation model of a two choice experimental design to describe the new method and
118 assess its statistical properties for hypothesis testing and parameter estimation. We then
119 provide a ‘real world’ illustration of the method using data from a binary choice
120 experiment using the sand cricket, *Gryllus firmus*. A “user-friendly” computer program
121 running in R(2016) is available on the Dryad site (<http://datadryad.org>).

122

123 METHODS

124 **Modeling a Mate Choice Experiment**

125 We consider experiments that consist of two males presented to a female in which
126 her choice is scored on a binary (0=rejected, 1=accepted) or continuous (e.g. number of
127 approaches to a male) scale, and the distribution of female choice is used to determine if

128 the female preference function is directional and/or stabilizing. The proposed method
 129 also estimates the population mean female preference.

130 Based on sample sizes typical of published choice experiments (see supplemental
 131 material, section 1) we set the sample size at 100 trials, each trial using a different female
 132 and a different pair of males. Male trait values were drawn at random from a normal
 133 distribution with a mean of 10 and a standard deviation of 1 or 3. In any trial one male
 134 was designated at random as the focal male and the other the non-focal male, their trait
 135 values being denoted as x_F and x_{NF} , respectively. Without loss of generality we assumed
 136 male trait values were always positive (this can always be made so by a suitable
 137 transformation). When choice is measured on a continuous scale, female preference is
 138 measured by either the relative preference, $R_p = n_F / (n_F + n_{NF})$, or the difference in
 139 preferences, $D_p = n_F - n_{NF}$, where n_F, n_{NF} are the measures of the female attraction,
 140 such as number of approaches, to the focal and non-focal males, respectively.

141 In trials with directional preference, we set the probability of the i th female
 142 selecting the focal male of the i th pair as

$$143 \quad P_{F,i} = x_{F,i} / (x_{F,i} + x_{NF,i}) \quad (1)$$

144 Thus, females preferred the male with the larger trait value (i.e., the preference was
 145 directional and positive).

146 For stabilizing preference the mean preference value for females was set either at
 147 9 or 10. When the male and female means differed (i.e., when the female mean was 9)
 148 the preference function has both directional and stabilizing components. We used two

149 different standard deviations (1 and 3) for both female preference and male trait values,
 150 because variances have been shown to influence the evolutionary trajectories of both
 151 preferences and preferred traits (Roff and Fairbairn 2014). In total, eight combinations of
 152 means and standard deviations were generated, including combinations in which the
 153 variance in female preference was less than that of the male trait and combinations in
 154 which the variance in female preference was substantially larger than the variance in
 155 male trait values.

156 Lande (1981) modelled stabilizing female preference as a Gaussian type function,
 157 which, under the present terminology can be written for the i th male (whether focal or
 158 non-focal) as,

$$159 \quad P_i = e^{-\frac{1}{2} \left(\frac{x_i - y_i}{\nu} \right)^2} \quad (2)$$

160 where x_i is the male trait, y_i is the female trait and ν is the width of the tolerance
 161 function for female choice. Female choosiness decreases as ν increases. Lande (1981)
 162 assumed that the male and female traits (x, y) were normally distributed with means and
 163 variances that could be different. He assumed that ν was a constant. Under the latter
 164 assumption, ν and the constant $\frac{1}{2}$ can be absorbed into the male female traits creating the
 165 simplified model

$$166 \quad P_i = e^{-(x_i - y_i)^2} \quad (3)$$

167 which we shall refer to as the Exponential difference, or ED, function. This type of
 168 equation was chosen by Lande (1981) for mathematical convenience rather than the
 169 presence of empirical data indicating this as the appropriate function.

170 An alternative function that is equally plausible is that female preference declines
 171 as a function of the absolute difference between her preference and the male trait,

$$172 \quad P_i = f(|x_i - y_i|) \quad (4)$$

173 For the ED model the probability of the focal male being chosen, $P_{F,i}$ was given by

$$174 \quad P_{F,i} = \frac{e^{-(x_{F,i} - y_i)^2}}{e^{-(x_{F,i} - y_i)^2} + e^{-(x_{NF,i} - y_i)^2}} \quad (5)$$

175 For the second preference function, hereafter the AD function, we assumed that the
 176 probability of a female selecting the focal male was directly proportional to the distance
 177 from the preferred female value relative to the non-focal male,

$$178 \quad P_{F,i} = 1 - \frac{|x_{F,i} - y_i|}{|x_{F,i} - y_i| + |x_{NF,i} - y_i|} \quad (6)$$

179 The above preference functions are probability functions. Simple algorithms
 180 based on these functions were used to generate the observed female choices in each of
 181 our simulation trials (see supplemental material, section 2). For the combinations of
 182 parameter values used in the present simulations the focal male is generally either
 183 strongly preferred or strongly rejected under the ED function, whereas, under the AD
 184 function the strength of preference is centered about 0.5 (see supplemental material 3).
 185 We included both of the preference functions to test the robustness of our estimation
 186 procedure. The method estimates the mean female preference, assuming a normal
 187 distribution of female preferences.

188

189 **Quantifying Preference**

190 *Directional Preference*

191 Under directional preference we would expect that as the difference between the
 192 trait values of the two potential mates increases so will the preference in one direction.
 193 We can therefore predict that the probability of a female choosing the focal male over the
 194 non-focal male, P_F , will be a monotonic function of the focal and non-focal male traits:
 195 we consider here both the relative trait value of the focal male, $x_{F,i}/(x_{F,i} + x_{NF,i})$, and the
 196 difference in trait values, $x_{F,i} - x_{NF,i}$. A general test for directional preference is a
 197 regression of female preference on either of these male metrics. For binary data the
 198 estimated female preference for the focal male, $\hat{P}_{F,i}$ is measured as 1 for the chosen male
 199 and 0 for the other male. With continuous data the estimated female preference is
 200 measured as $\hat{P}_{F,i} = n_{F,i}/(n_{F,i} + n_{NF,i})$, where $n_{F,i}$ is the index of female preference for
 201 the focal male and $n_{NF,i}$ her preference for the non-focal male: for example, $n_{F,i}$ could be
 202 the number of times the female approached the focal male. If female choice is binary
 203 (0,1) a logistic regression is appropriate. For the continuous case the relationship may
 204 not be linear and hence a non-linear regression or suitable transformation may be
 205 necessary.

206 In real world experiments, if the pair of males differ by some standard category
 207 (e.g. well-fed vs under-fed, long-winged vs short-winged) then one of these categories
 208 can be designated the focal male and the other the non-focal male. In the case where
 209 there is no distinguishing category and data are binary, males should be randomly

210 assigned to be focal or non-focal males such that approximately 50% of focal males are
 211 preferred and 50% are not preferred by the female.

212

213 *Stabilizing Preference*

214 We first consider an experiment in which the data are 0,1. Suppose the mean
 215 female preference is μ . Consider the metric

$$216 \quad d_i = |x_{F,i} - \mu| - |x_{NF,i} - \mu| \quad (7)$$

217 Under the hypothesis of stabilizing preference, negative values of d_i should be associated
 218 with the focal male being preferred (because the absolute deviation of $x_{F,i}$ from μ is less
 219 than that of $x_{NF,i}$ from μ) and positive values with the non-focal male being preferred.

220 For each value of d_i we compute the number of correct predictions made using the simple
 221 formula “focal male if $|x_{F,i} - \mu| < |x_{NF,i} - \mu|$, otherwise non-focal male”. The best
 222 estimate of the mean female preference is the value that gives the greatest number of
 223 correct predictions, N_{max} .

224 The above procedure locates the best estimate of mean female preference, but it
 225 does not specify that the prediction is significantly better than chance. A suitable test is a
 226 logistic regression of female choice (0,1) on $|x_{F,i} - \hat{\mu}| - |x_{NF,i} - \hat{\mu}|$, where $\hat{\mu}$ is the best
 227 estimate of female preference. A statistically significant regression indicates significant
 228 stabilizing preference. This test is one-tailed as the slope must be negative under
 229 stabilizing preference.

230 When choice is a continuously varying measure we defined the independent
 231 variable as

$$232 \quad X_i = 1 - \frac{|x_{F,i} - \mu|}{|x_{F,i} - \mu| + |x_{NF,i} - \mu|} \quad (8)$$

233 which has the useful property $0 \leq X_i \leq 1$ that avoids possible extreme values. The metric
 234 d_i (equation (7)) could also be used but we have not examined its statistical properties for
 235 the continuous case. Under the assumption of stabilizing preference the probability of a
 236 female choosing the focal male will be a monotonically increasing function of X_i . For the
 237 present analysis we assumed a linear function. To obtain an estimate of μ we proceed in
 238 three steps:

- 239 1) First we select a trial value of μ , say μ_T and then for each pair of males we
 240 use μ_T to estimate X_i .
- 241 2) Second, we regress the estimated female preference, $\hat{P}_{F,i}$, for the focal male
 242 on X . As noted above, in the present case we modeled a linear function and
 243 therefore we used a linear regression: in an empirical study the relationship
 244 might not be so and a transformation or alternate regression function may be
 245 required.
- 246 3) The final step is to vary μ_T and for each such value calculate the variance
 247 accounted for by the regression of μ_T on X : the best estimate of mean female
 248 preference, $\hat{\mu}$, is that value which gives the highest r^2 , subject to the
 249 constraint that the slope of the regression of μ_T on X is positive. To be

250 statistically significant the probability associated with the regression must be
251 less than 0.05. To distinguish negative from positive slopes, we retain the
252 sign of the slope in the r^2 and designate this statistic as r_s^2 or signed r^2 .

253 Graphically, we plot r_s^2 on μ_T .

254 The above procedures provide a statistical test of stabilizing female preference
255 and an approximate estimate of the mean female preference, but not an estimate of the
256 standard error. To obtain an estimate of the standard error we used the bootstrap:
257 samples were drawn with replacement from the original data set and the estimate, $\hat{\mu}$,
258 computed. A total of 1000 bootstraps were drawn and the estimate and its standard error
259 computed as the mean and standard deviation of the 1000 bootstraps (Roff 2006).

260

261 **Empirical Example**

262 We provide an empirical example of the proposed method based on a two choice
263 experiment with sand crickets (*Gryllus firmus*) in which each female was given the
264 choice of two seven-day old males drawn at random from a recently established
265 laboratory population. The data consist of the male song components and a measure of
266 female attraction to these in 93 binary choice trials. These data were obtained using a
267 modification of the T-maze design reported in Crnokrak and Roff (1995) by moving the
268 tubes of the maze down so that they entered the buckets containing the males close to the
269 bottom. This allowed the females to move freely into and out of the buckets. As in the
270 original mazes, the males were held in containers within the buckets, preventing physical
271 contact between the sexes. We used motion detectors set at the entrances to the buckets

272 containing the males to monitor the activity of the females. Female preference for the
273 focal male was estimated as the number of times the female tripped the motion detector
274 on the focal male side divided by the total number of times both motion detectors were
275 tripped. A computer monitoring system checked each male every second and recorded if
276 the male was calling and the volume of the call. These data provided an estimate of time
277 spent calling and the mean volume. We also obtained samples of the call songs using
278 USB digital audio recorders. Song components were analyzed using Raven Pro (The
279 Cornell Lab of Ornithology) with the following components being measured: pulses per
280 chirp, pulse length, pulse rate, pulse period, chirp length, chirp rate and frequency. Pulse
281 rate was defined as the rate of pulses within a chirp and chirp rate as the number of chirps
282 per unit time within a singing bout, defined as a set of chirps less than 0.5 seconds apart.
283 From this set we chose three components that illustrate the situations of “no preference”,
284 “directional preference” and “stabilizing preference”. A complete analysis of the *G.*
285 *firmus* will be presented elsewhere. We present data on three components that illustrate
286 the situations of “no preference”, “directional preference” and “stabilizing preference”.
287 The predicted preference for the focal male was set as $x_{F,i}/(x_{F,i} + x_{NF,i})$ for directional
288 preference and as given in equation (8) for stabilizing preference.

289

290 RESULTS

291 **The Simulation model**

292 *General Patterns*

293 The protocol for determining stabilizing preference can be graphically displayed
294 by plotting r_s^2 (the signed r^2) for each trial value of μ , designated μ_T , on this trial value
295 (left columns, Fig. 1). Directional preference is displayed by plotting preference for the
296 focal male (P_F) on the relative value of the focal male (right columns, Fig. 1). Significant
297 stabilizing preference shows two patterns of variation. First, if both stabilizing and
298 directional preference are present, the function r_s^2 on μ_T shows both a peak and a rise
299 above the critical significance value between the peak and one of the extrema of μ_T (top
300 row, Fig. 1). In the case illustrated, the female mean preference was less than the mean
301 male trait value (9 vs 10) and hence the highest value of r_s^2 lies above the significance
302 value to the left of the peak. The second pattern of stabilizing preference is one in which
303 there is a single peak and no significant directional preference (middle row, Fig. 1),
304 which occurs when the mean female preference and mean male trait value coincide or the
305 variance in female preference or male trait value is relatively large.

306 With only positive directional preference, the function of r_s^2 on μ_T shows an
307 increasing S-shaped function (bottom row, Fig. 1), with r_s^2 plateauing and no single value
308 of μ_T being “best”.

309

310 *Statistical Properties of Estimators*

311 Three primary statistical properties that an estimator must satisfy are sufficient
312 power, acceptably small bias and accurate standard errors (i.e. true mean is enclosed
313 within ± 2 standard errors 95% of the time). To determine the statistical power of the

314 above procedures we ran 1,000 simulations per combination with 100 male pairs per
315 simulation. In addition we ran simulations with directional preference only and also with
316 random female preference. The analysis proceeds in two steps: the first is an hypothesis
317 testing step that stabilizing preference exists and the second is parameter estimation. If
318 the first step is passed (i.e. stabilizing preference is not rejected) then we move to the
319 second step of parameter estimation. If the test for stabilizing preference is not
320 significant we could still estimate the parameters of the stabilizing preference but this
321 estimate is predicated on the unverified assumption that stabilizing preference is present.
322 In the case of an experiment in which a treatment is applied it is permissible to estimate
323 the effect of treatment even if it is non-significant because the difference between
324 treatments is quantitative. The present case is fundamentally different as it requires the
325 addition of an unverified assumption. Therefore, while we retained all simulations in the
326 test for statistical power, to test for bias and the efficacy of the bootstrap, we considered
327 only those simulations in which significant stabilizing preference was found. We
328 continued running simulations until 1000 data sets were created in which significant
329 stabilizing preference was found.

330 We present the statistical analyses for the continuous data here and the 0,1 data in
331 the supplemental material (section 4). Tests were done using both $x_F / (x_F + x_{NF})$ and
332 $x_F - x_{NF}$: as they gave the same qualitative performance we report the results only for the
333 former metric. Results for the ED and AD models were very similar with respect to both
334 statistical power, bias and standard error estimates (see below).

335

336 *Statistical Power*

337 The first criterion for accepting any model is that it must be significantly different
338 from the null model. A generally accepted desirable level for power (i.e. probability of
339 rejecting the null hypothesis when the alternate hypothesis is true) is 80% (Cohen 1988).
340 The method did an excellent job of statistically detecting pure directional preference.
341 The statistical power to detect directional preference when females showed only
342 directional preference was 100%. Type I error rates were also appropriate: directional
343 preference was detected in only 5% of cases when female preference was random.

344 The method also did a good job of statistically detecting stabilizing preference in
345 the absence of directional preference, although type I error rates were slightly higher and
346 power was slightly lower than for pure directional preference. With random female
347 preference apparent stabilizing preference was inferred in 6% of runs with SD of 1, and
348 10% of runs with SD of 3, which is slightly greater than the required 5% and indicates
349 that marginally significant values in tests of stabilizing preference should be treated with
350 circumspection.

351 The statistical power of the method for detecting stabilizing preference in the
352 simulations with only stabilizing preference ranged from 40% to 100%, with 6 of the 8
353 combinations exceeding 90% and all but one exceeding 50% (lower right panel, Fig. 2).
354 Power exceeds 90% if the variance in preference is equal or greater than the variance in
355 male trait values, but is much lower (40% - 60%) when the male trait variance greatly
356 exceeds the variance in female preference (ratio of 1:3 in lower right panel of Fig. 2).

357 With stabilizing preference and a female mean of 9 and a male mean of 10 there is
 358 both stabilizing and directional preference. The power to detect the stabilizing
 359 component of preference is high and similar to the power to detect pure stabilizing
 360 preference, being over 80% in 7 of 8 cases (bottom left panel, Fig. 2). When both male
 361 and female variances were 1, the power to also detect directional preference was 100%
 362 (top left panel, Fig. 2). However, for other combinations of variances, statistical power
 363 to detect the directional component of preference was lower. Therefore, when both
 364 stabilizing and directional preference occur the power to detect the latter is low unless
 365 both the male and female variances are small relative to the difference between the
 366 means: for example, in the present case directional preference was readily detected when
 367 the CV in females was 11% and in males 10% but not when the CV in females was 30%
 368 and in males 33%.

369 When female and male means are the same then a priori we might expect that
 370 there should be no directional preference. However, in the simulations directional
 371 preference was incorrectly detected in more than 5% of runs (top right panel, Fig. 2).
 372 Thus, the probability of a Type I statistical error is higher than ideal. Positive directional
 373 preference was more often detected than negative directional preference. We have not
 374 been able to demonstrate this effect analytically, but simulations using the simplified
 375 model of stabilizing female preference $P_F = |x_F - \mu| / (|x_F - \mu| + |x_{NF} - \mu|)$ on
 376 $x_F / (x_F + x_{NF})$ have verified that the effect is real and depends on the relative variances,
 377 i.e. stabilizing preference in which the female mean preference matches the mean male
 378 trait may generate both stabilizing and directional preference. The presence of x_F, x_{NF} in

379 both the predictor and response variables suggests that at least part of the correlation is
380 spurious. If the significance level is set at 0.01 rather than 0.05, the probability of
381 declaring significant directional preference falls close to 0.05 for the continuous data (
382 mean = 0.056) and considerably less than 0.05 for 0,1 data (mean=0.017).

383

384 *Bias and Standard error estimates*

385 Bias was calculated as the estimated value minus the true value of the mean
386 female preference divided by the actual value. There was no indication of a persistent
387 bias in the estimate of the mean. Standard errors were given by the standard deviation of
388 the bootstrap values. The two largest biases were -13% (AD model) and -17% (ED
389 model) at combinations which occurred when the female mean was 9 and both variances
390 equal to one. In all other cases the magnitude of percent bias was less than 5% and in all
391 combinations the estimated confidence interval was 95% or greater. The standard error
392 estimates were conservative in being generally larger than required.

393

394 *Summary of Simulation Results*

395 Overall, the simulation results indicate that the proposed methods for estimating
396 stabilizing preference and pure directional preference are satisfactory and robust to the
397 type of preference function. When preference is purely directional the statistical power is
398 100%. When selection is purely stabilizing, the statistical power is generally above 80%
399 and false positives are less than 10%. In our simulations, the power was low only if the
400 variance in male trait values greatly exceeded the variance in female preference, a

401 circumstance that we shall argue is unlikely to occur in natural situations (see below).
402 When preference is stabilizing but the female mean differs from the male mean, both
403 stabilizing and directional preference should be detected. In these cases, the power to
404 detect stabilizing preference remains high, but both type I and type II error rates for
405 detecting the directional component of preference are higher than ideal. Therefore, when
406 significant stabilizing preference is detected, conclusions about the concurrent presence
407 of directional preference should be made with caution.

408 The method also does a good job of parameter estimation. When preference is
409 stabilizing, mean female preference is estimated accurately and with negligible bias. The
410 standard errors of mean female preference are only slightly overestimated and potentially
411 troublesome bias only occurred in two combinations. Even in the latter cases the
412 confidence limits enclosed the true value at the required 95% level.

413

414 **Empirical Example**

415 *Single trait analysis*

416 Figures 3, 4 and 5 illustrate the three general results from the analysis: no
417 significant preference (Fig. 3), directional preference (Fig. 4), and stabilizing preference
418 with the possibility of a directional component (Fig.5). Females showed no preference
419 for any carrier frequency within the range observed (Fig.3). There was no evidence of
420 any directional preference ($P=0.480$) and in no trial did mean female preference value
421 cause the correlation between predicted and observed values to exceed the critical 5%
422 level. The bootstrap shows the mean female preference close to the population mean,

423 which is what we would expect if the trait was a species-recognition character under
424 stabilizing preference. However in this case such a preference, if it exists, is too weak to
425 be detected given the present sample size.

426 In contrast, there is strong evidence of female preference being correlated with
427 time spent calling by the male (Fig. 4). There was a highly significant regression between
428 observed and predicted preference values ($P=0.0008$) indicating directional preference
429 (top panel, Fig. 4). This directionality is also indicated by the stabilizing preference test,
430 which shows a continuous rise that exceeds the critical 5% level (compare this plot with
431 the bottom left plot in Fig 1).

432 The third example shows significant statistical evidence of a trait, chirp rate,
433 under stabilizing preference with a directional component (Fig.5). There was a highly
434 significant directional component ($P=0.005$) and a clear unimodal stabilizing function
435 with a probability of the signed r^2 at its peak of 0.0012 (compare to the top left panel in
436 Fig. 1). The bootstrap estimate was 2.28 (SE=0.28).

437

438 DISCUSSION

439 The simulation models demonstrated that the proposed method can successfully
440 detect both directional and stabilizing preference for sample sizes that are well within
441 logistical limits. The statistical properties of the test are generally good, with high power
442 to detect both stabilizing and pure directional preference. However, we did discover two
443 areas of potential statistical error indicating that caution should be taken when drawing
444 some statistical conclusions. The first problem area concerns the detection of directional

445 preference when stabilizing preference is also present. In this case, the power of the
446 method to detect the stabilizing component is good, but its power to also detect the
447 directional component is relatively low unless the variances in both male trait values and
448 female preferences are small. Thus, if the data follow a pattern similar to that illustrated
449 in the top panels of Fig. 1 or in Fig. 5, but only the stabilizing component of preference is
450 statistically significant, researchers should be cautious (i.e., tentative) in concluding the
451 absence of directional preference unless $P \gg 0.05$. The opposite statistical problem also
452 occurs: the type I error of incorrectly detecting of directional preference when preference
453 is purely stabilizing occurs at a rate greater than 5%. To alleviate this problem,
454 researchers should also be cautious in concluding that directional preference is present
455 unless the probability value is ≤ 0.01 .

456 The second problem area concerns the low power of the test to detect stabilizing
457 selection when the variance in male trait values greatly exceeds the variance in female
458 preference (SD ratio of 1:3 in our simulations). This combination of variances also led to
459 the highest type I error rates for detecting directional selection in the presence of
460 stabilizing selection. Fortunately, this circumstance seems unlikely to be relevant in
461 nature. Although the variances of male traits and female preferences lie at the core of
462 models of the evolution of mate choice (Lande 1981; Roff and Fairbairn 2014), very few
463 empirical studies have estimated the variance in female preference. Nevertheless, the
464 evidence that does exist indicates relatively little difference in the variances: a range from
465 0.8 to 1.6 in the ratio of the variance in female preference to the variance in the male trait
466 (Roff and Fairbairn 2014). Further indication that the difference in variances is not great

467 comes from the observation that the estimated stabilizing preference function generally
468 seems to straddle and slightly exceed the distribution of the preferred trait (e.g. Ritchie et
469 al. 2001; Brooks et al. 2005; Bentsen et al. 2006; Steele et al. 2011; Moreno-Gomez et al.
470 2015).

471 We applied the approach to empirical data on three song components of the sand
472 cricket and with the approach identified a lack of preference, directional preference and
473 stabilizing preference. For purposes of illustration, we have treated these traits as
474 independent, but in many cases, different components of male displays are likely to be
475 correlated with each other. Our method can be extended to sets of correlated traits in two
476 possible ways. One method would be to initially analyze each trait independently, as we
477 have done in our examples, and then enter all statistically significant traits into a single
478 stepwise regression. A complementary approach in cases where the male traits are
479 correlated would be to use principal components analysis (PCA) and analyze female
480 preference for the resulting principal components.

481 The empirical results of the present analysis highlight the potential problems of
482 restricting assays of female choice to single variables as is likely to be the case when
483 artificial signals are used. Models for the evolution of preferential mating systems
484 generally assume preferences for single traits. However, there is no theoretical bar to the
485 evolution of multiple sexual preferences (Pomiankowski and Iwasa 1993) and evidence is
486 accumulating that different females (or males) within the same population may weigh
487 multiple traits differently in making their choice (e.g., Orthoptera: Hedrick and Weber
488 1998; Olvido and Wagner 2004; Bailey 2008; Verburgt et al. 2008; Stout et al. 2010;

489 Fowler-Finn and Rodriguez 2012; Hedrick and Kortet 2012; anurans: Murphy and
490 Gerhardt 2000; fish: Brooks and Endler 2001; Brooks 2002; Morris et al. 2003; Pierotti et
491 al. 2009; Labonne et al. 2009; Lehtonen et al. 2010; birds: Coleman et al. 2004; David
492 and Cezilly 2011; humans: Zietsch et al. 2012). This is another reason for testing
493 multiple males per female and for measuring multiple traits per male. Such variation
494 among females would tend to eliminate evidence of overall directional or stabilizing
495 preference on any single trait. By extension, finding strong directional preference for a
496 particular trait is itself evidence that this is a trait that the majority of females find
497 attractive (or repellent).

498 As a general recommendation, tests of female preference should be made relevant
499 to the natural history of the species. Analysis of no choice trials is relatively simple (e.g.
500 linear and quadratic regression comparisons), but the meta-analysis of Dougherty and
501 Shuker (2015) showed that this protocol has less statistical power to detect either
502 directional or stabilizing preference than choice experiments. Nevertheless, as noted by
503 Dougherty and Shuker, no choice trials may be realistic for species that meet potential
504 mates sequentially, and are hence preferable in these cases. We might be similarly
505 critical of choice trials if they use a number of males that differs from the number
506 typically encountered by a female in the wild. As most choice trials involve only two
507 males it is legitimate to ask if this represents a normal situation. A survey of published
508 estimates of the number of potential mates assessed by females in the wild showed that
509 females assessed a mean of 4.5, and a median of 2.9, potential mates before making their
510 choice (Roff and Fairbairn 2014). Thus, although the use of two males may not be

511 unrealistic for many species, it could greatly underestimate the sampling strategies of
512 females in others. We have developed the method for two-choice trials as this is the one
513 most commonly used: however, the approach can be readily extended to multi-choice
514 experiments.

515 The experimental and statistical protocols advanced and tested in this paper
516 overcome the problem of limitations of choice experiments in that outcomes are not
517 restricted to categorical designations (e.g. big vs small) nor to stimuli that may be warped
518 versions of the natural stimulus (e.g. artificially constructed songs that differ only in
519 frequency). In addition, both directional and stabilizing preferences can be statistically
520 tested both with respect to individual components and to more complex stimuli using, for
521 example, either multiple regression or principal components.

522

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527

528 REFERENCES

529 Bailey NW, 2008. Love will tear you apart: different components of female choice exert
530 contrasting selection pressures on male field crickets. *Behav Ecol.* 19:960-966.

- 531 Bentsen CL, Hunt J, Jennions MD, Brooks R, 2006. Complex multivariate sexual
532 selection on male acoustic signaling in a wild population of *Teleogryllus*
533 *commodus*. Am Nat. 167:E102-E116.
- 534 Brooks R, 2002. Variation in female mate choice within guppy populations: population
535 divergence, multiple ornaments and the maintenance of polymorphism. Genetica
536 116:343-358.
- 537 Brooks R, Endler JA, 2001. Female guppies agree to differ: Phenotypic and genetic
538 variation in mate-choice behavior and the consequences for sexual selection.
539 Evolution 55:1644-1655.
- 540 Brooks R, Hunt J, Blows MW, Smith MJ, Bussiere LF, Jennions MD, 2005.
541 Experimental evidence for multivariate stabilizing sexual selection. Evolution
542 59:871-880.
- 543 Cohen J, 1988. Statistical Power Analysis for the Behavioral Sciences. Hillsdale, New
544 Jersey: Lawrence Erlbaum Associates, Inc.
- 545 Coleman SW, Patricelli GL, Borgia G, 2004. Variable female preferences drive complex
546 male displays. Nature 428:742-745.
- 547 Crnokrak P, Roff DA, 1995. Fitness differences associated with calling behaviour in the
548 two wing morphs of male sand crickets, *Gryllus firmus*. Anim. Behav. 50:1475-
549 1481.
- 550 David M, Cezilly F, 2011. Personality may confound common measures of mate-choice.
551 PLoS One 6.

- 552 Dougherty LR, Shuker DM, 2015. The effect of experimental design on the measurement
553 of mate choice: a meta-analysis. *Behav Ecol.* 26:311-319.
- 554 Ferreira M, Ferguson JWH, 2002. Geographic variation in the calling song of the field
555 cricket *Gryllus bimaculatus* (Orthoptera : Gryllidae) and its relevance to mate
556 recognition and mate choice. *J Zool* 257:163-170
- 557 Fowler-Finn KD, Rodriguez RL, 2012. The evolution of experience-mediated plasticity
558 in mate preferences. *J Evol Biol.* 25:1855-1863.
- 559 Gerhardt HC, Tanner SD, Corrigan CM, Walton HC, 2000. Female preference functions
560 based on call duration in the gray tree frog (*Hyla versicolor*). *Behav Ecol.* 11:663-
561 669.
- 562 Gray DA, Cade WH, 1999. Quantitative genetics of sexual selection in the field cricket,
563 *Gryllus integer*. *Evolution* 53:848-854.
- 564 Hedrick A, Weber T, 1998. Variance in female responses to the fine structure of male
565 song in the field cricket, *Gryllus integer*. *Behav Ecol.* 9:582-591.
- 566 Hedrick AV, Kortet R, 2012. Effects of body size on selectivity for mating cues in
567 different sensory modalities. *Biol J Linn Soc.* 105:160-168.
- 568 Jang YW, Greenfield MD, 1998. Absolute versus relative measurements of sexual
569 selection: Assessing the contributions of ultrasonic signal characters to mate
570 attraction in lesser wax moths, *Achroia grisella* (Lepidoptera : Pyralidae).
571 *Evolution* 52:1383-1393.
- 572 Jennions MD, Petrie M, 1997. Variation in mate choice and mating preferences: A review
573 of causes and consequences. *Biol Rev.* 72:283-327.

- 574 Jennions MD, Kahn AT, Kelly CD, Kokko H, 2012. Meta-analysis and sexual selection:
575 past studies and future possibilities. *Evol Ecol.* 26:1119-1151.
- 576 Labonne J, Augery M, Parade M, Brinkert S, Prevost E, Heland M, Beall E, 2009.
577 Female preference for male body size in brown trout, *Salmo trutta*: is big still
578 fashionable? *Anim Behav.* 77:129-137
- 579 Lande R, 1981. Models of speciation by sexual selection on polygenic traits. *PNAS*
580 78:3721-3725.
- 581 Lehtonen TK, Wong BBM, Lindstrom K, 2010. Fluctuating mate preferences in a marine
582 fish. *Biol Lett* 6:21-23.
- 583 Moreno-Gómez FN, Bacigalupe LD, Silva-Escobar AA, Soto-Gamboa M, 2015. Female
584 and male phonotactic responses and the potential effect of sexual selection on the
585 advertisement calls of a frog. *Anim Behav.* 104:79-86.
- 586 Morris MR, Nicoletto PF, Hesselman E, 2003. A polymorphism in female preference for
587 a polymorphic male trait in the swordtail fish *Xiphophorus cortezi*. *Anim Behav.*
588 65:45-52.
- 589 Murphy CG, Gerhardt HC, 2000. Mating preference functions of individual female
590 barking treefrogs, *Hyla gratiosa*, for two properties of male advertisement calls.
591 *Evolution* 54:660-669.
- 592 Olvido AE, Wagner WE, 2004. Signal components, acoustic preference functions and
593 sexual selection in a cricket. *Biol J Linn Soc.* 83:461-472.

- 594 Pierotti MER, Martin-Fernandez JA, Seehausen O, 2009. Mapping individual variation in
595 male mating preference space: multiple choice in a color polymorphic cichlid fish.
596 Evolution 63:2372-2388.
- 597 Pomiankowski A, Iwasa Y, 1993. Evolution of multiple sexual preferences by fisher
598 runaway process of sexual selection. Proc Roy Soc B-Biol Sci 253:173-181.
- 599 R 2016. R: A language and environment for statistical computing. R Foundation for
600 Statistical Computing, Vienna, Austria.
- 601 Ritchie MG, Saarikettu M, Livingstone S, Hoikkala A, 2001. Characterization of female
602 preference functions for *Drosophila montana* courtship song and a test of the
603 temperature coupling hypothesis. Evolution 55:721-727.
- 604 Roff DA, 2006. Introduction to Computer-Intensive Methods of Data Analysis in
605 Biology. Cambridge: Cambridge University Press.
- 606 Roff DA, Fairbairn DJ, 2014. The evolution of phenotypes and genetic parameters under
607 preferential mating. Ecol Evol 4:2759-2776
- 608 Steele DB, Siepielski AM, McPeck MA, 2011. Sexual selection and temporal phenotypic
609 variation in a damselfly population. J Evol Biol 24:1517-1532.
- 610 Stout J, Navia B, Jeffery J, Samuel L, Hartwig L, Butlin A, Chung M, Wilson J, Dashner
611 E, Atkins G, 2010. Plasticity of the phonotactic selectiveness of four species of
612 chirping crickets (Gryllidae): Implications for call recognition. Physiol Ent.
613 35:99-116.

- 614 Verburgt L, Ferguson JWH, Weber T, 2008. Phonotactic response of female crickets on
615 the Kramer treadmill: methodology, sensory and behavioural implications. J
616 Comp Physiol a-Neuroethol Sens Neur and Behavl Physiol. 194:79-96.
- 617 Zietsch BP, Verweij KJH, Burri AV, 2012. Heritability of preferences for multiple cues
618 of mate quality in humans. Evolution 66:1762-1772.
- 619 Zuk M, Rebar D, Scott SP, 2008. Courtship song is more variable than calling song in the
620 field cricket *Teleogryllus oceanicus*. Anim Behav 76:1065-1071.
- 621

622 FIGURE CAPTIONS

623 Figure 1: Characteristic patterns for functions detecting stabilizing and directional preference.

624 The left column shows the signed r^2 (r_s^2) as a function of the trial value of the mean
 625 female preference, μ_T . The dashed line shows the 5% probability value for the signed r^2 :
 626 Values above this line have a probability of occurring by chance of less than 0.05. The
 627 right column shows the estimate of female preference for the focal male, \hat{P}_F , against the
 628 preference estimated as the relative value of the focal male trait. The solid line shows the
 629 fitted regression line.

630 Top row: Female preference is stabilizing with a mean of 9 and a standard deviation of 1, mean
 631 male value is at 10 and standard deviation of 1: this produces both significant stabilizing
 632 and directional preference. Middle row: Female preference is stabilizing with a mean at
 633 9 and a standard deviation of 3, mean male value is at 10 with a standard deviation of 1:
 634 this results in significant stabilizing preference but not significant directional preference.

635 Bottom row: Significant directional preference but no stabilizing preference.

636

637 Figure 2: Proportion of times directional (top) and stabilizing (bottom) preference was detected
 638 when female preference was stabilizing with or without a directional component. Results
 639 for AD model shown in black, those for the ED model are in stippled white. The mean
 640 male trait value is 10 with left panels showing results for female mean=9, and right
 641 panels showing results for female mean=10. Note that when male and female means are
 642 the same then directional selection should be detected only 5% of times. Both directional
 643 and stabilizing selection should be detected in the left panels but only stabilizing in the
 644 right panels.

645

646 Figure 3. An example of a song trait, (Frequency) that shows no statistical indication of female
647 preference.

648 Top panel: Regression of estimated preference for the focal male, P_F , on the preference predicted
649 from the male trait values. Solid line=fitted regression.

650 Bottom panel: Signed r^2 on the trial mean female preference, μ_T . Solid red line indicates the fit
651 at the trial female preference. Only values lying above the 5% line (dotted blue line) are
652 significant. The dotted line shows the normal distribution based on the bootstrap values.

653

654 Figure 4. An example of a song trait, (Duration of time male called) that shows statistical
655 indication of directional female preference.

656 Top panel: Regression of estimated preference for the focal male, P_F , on the preference predicted
657 from the male trait values. Solid line=fitted regression.

658 Bottom panel: Signed r^2 on the trial mean female preference, μ_T . Solid red line indicates the fit
659 at the trial female preference. Only values lying above the 5% line (dotted blue line) are
660 significant.

661

662 Figure 5. An example of a song trait, (Chirp rate) that shows statistical indication of stabilizing
663 female preference, with the possibility of a directional component.

664 Top panel: Regression of estimated preference for the focal male, P_F , on the preference predicted
665 from the male trait values. Solid line=fitted regression.

666 Bottom panel: Signed r^2 on the trial mean female preference, μ_T . Solid red line indicates the fit
667 at the trial female preference. Only values lying above the 5% line (dotted blue line) are
668 significant. The dotted line shows the normal distribution based on the bootstrap values.
669

Figure 1: Characteristic patterns for functions detecting stabilizing and directional preference. The left column shows the signed r^2 (r_s^2) as a function of the trial value of the mean female preference, μ_T . The dashed line shows the 5% probability value for the signed r^2 : Values above this line have a probability of occurring by chance of less than 0.05. The right column shows the estimate of female preference for the focal male, \hat{P}_F , against the preference estimated as the relative value of the focal male trait. The solid line shows the fitted regression line.

Top row: Female preference is stabilizing with a mean of 9 and a standard deviation of 1, mean male value is at 10 and standard deviation of 1: this produces both significant stabilizing and directional preference. Middle row: Female preference is stabilizing with a mean at 9 and a standard deviation of 3, mean male value is at 10 with a standard deviation of 1: this results in significant stabilizing preference but not significant directional preference. Bottom row: Significant directional preference but no stabilizing preference.

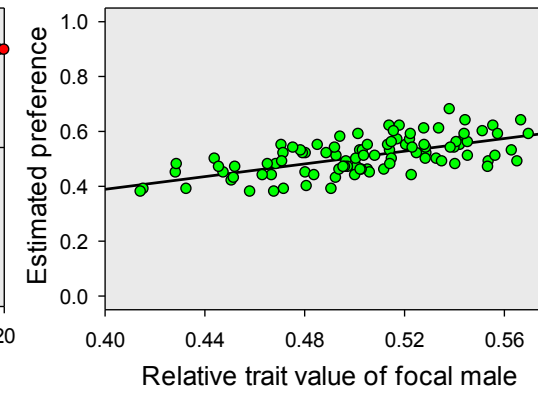
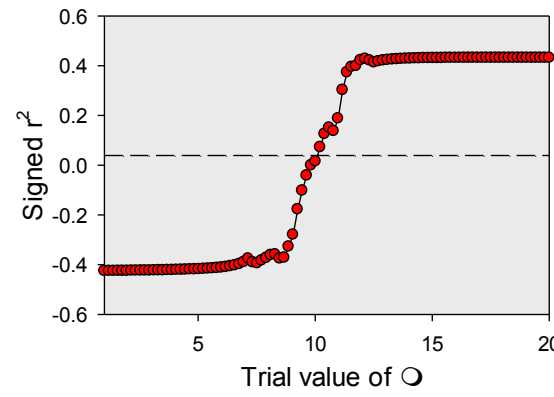
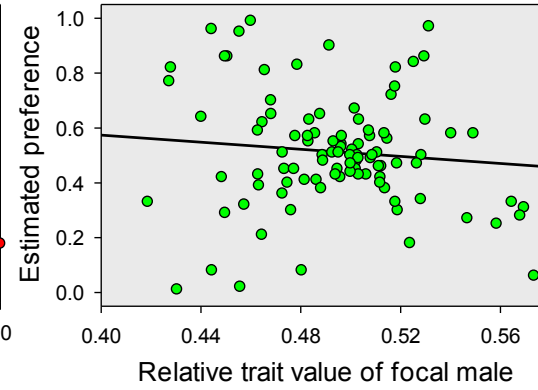
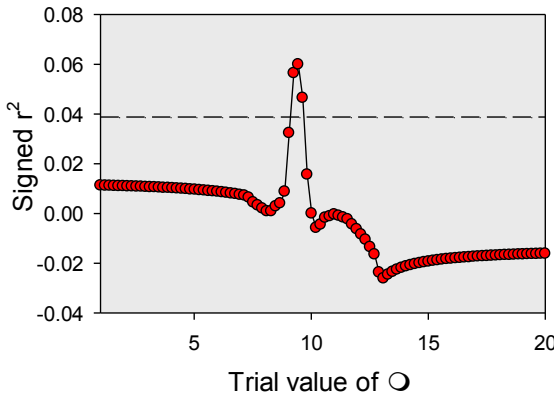
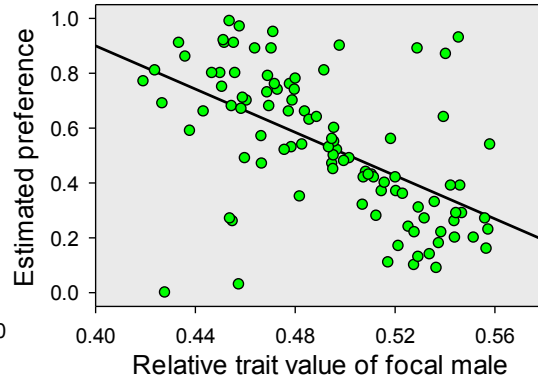
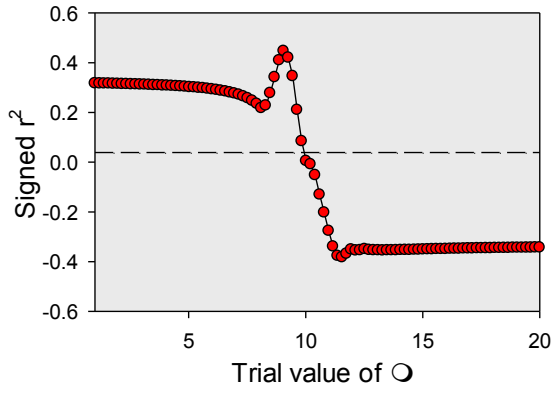


Figure 2: Proportion of times directional (top) and stabilizing (bottom) preference was detected when female preference was stabilizing with or without a directional component. Results for AD model shown in purple and blue, those for the ED model are in Cyan and Green. The mean male trait value is 10 with left panels showing results for female mean=9, and right panels showing results for female mean=10. Note that when male and female means are the same then directional selection should be detected only 5% of times. Both directional and stabilizing selection should be detected in the left panels but only stabilizing in the right panels.

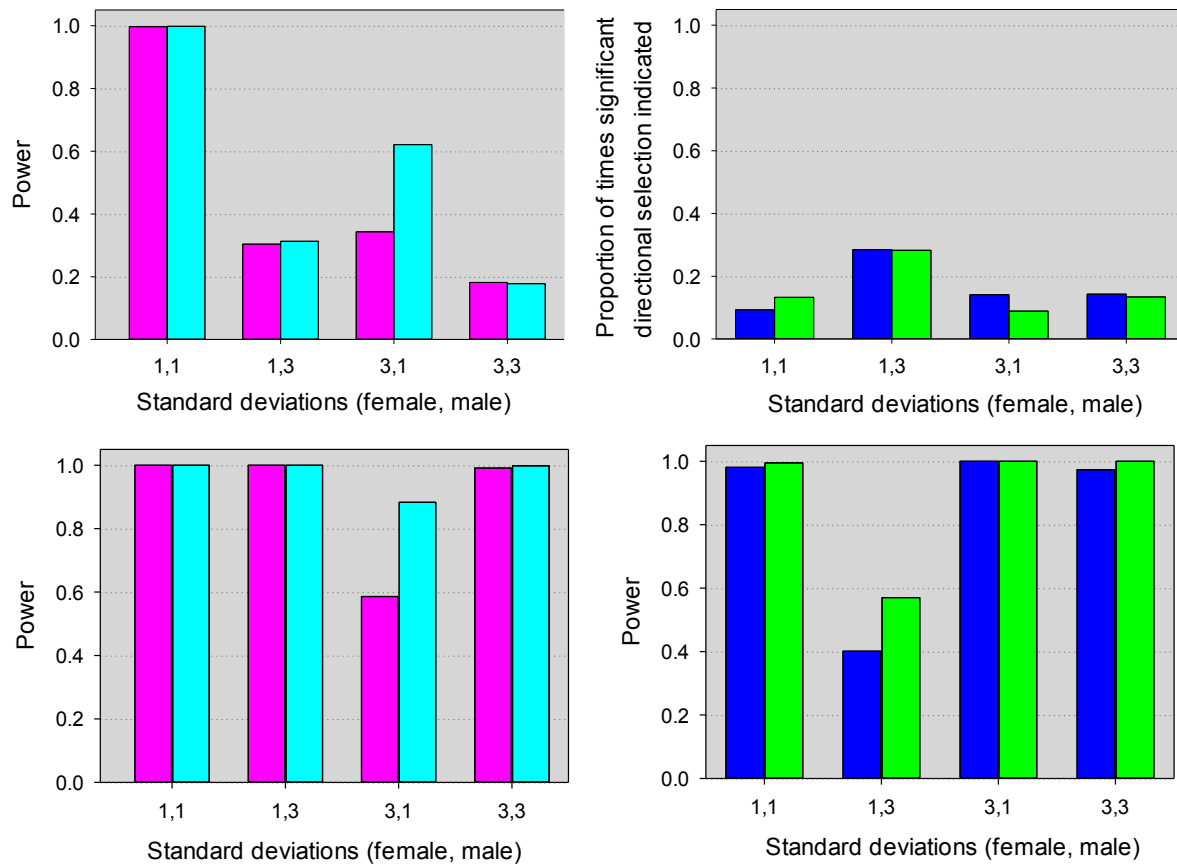


Figure 3. An example of a song trait, (Frequency) that shows no statistical indication of female preference.

Top panel: Regression of estimated preference for the focal male, P_F , on the preference predicted from the male trait values. Solid line=fitted regression.

Bottom panel: Signed r^2 on the trial mean female preference, μ_T . Solid red line indicates the fit at the trial female preference. Only values lying above the 5% line (dotted blue line) are significant. The dotted line shows the normal distribution based on the bootstrap values.

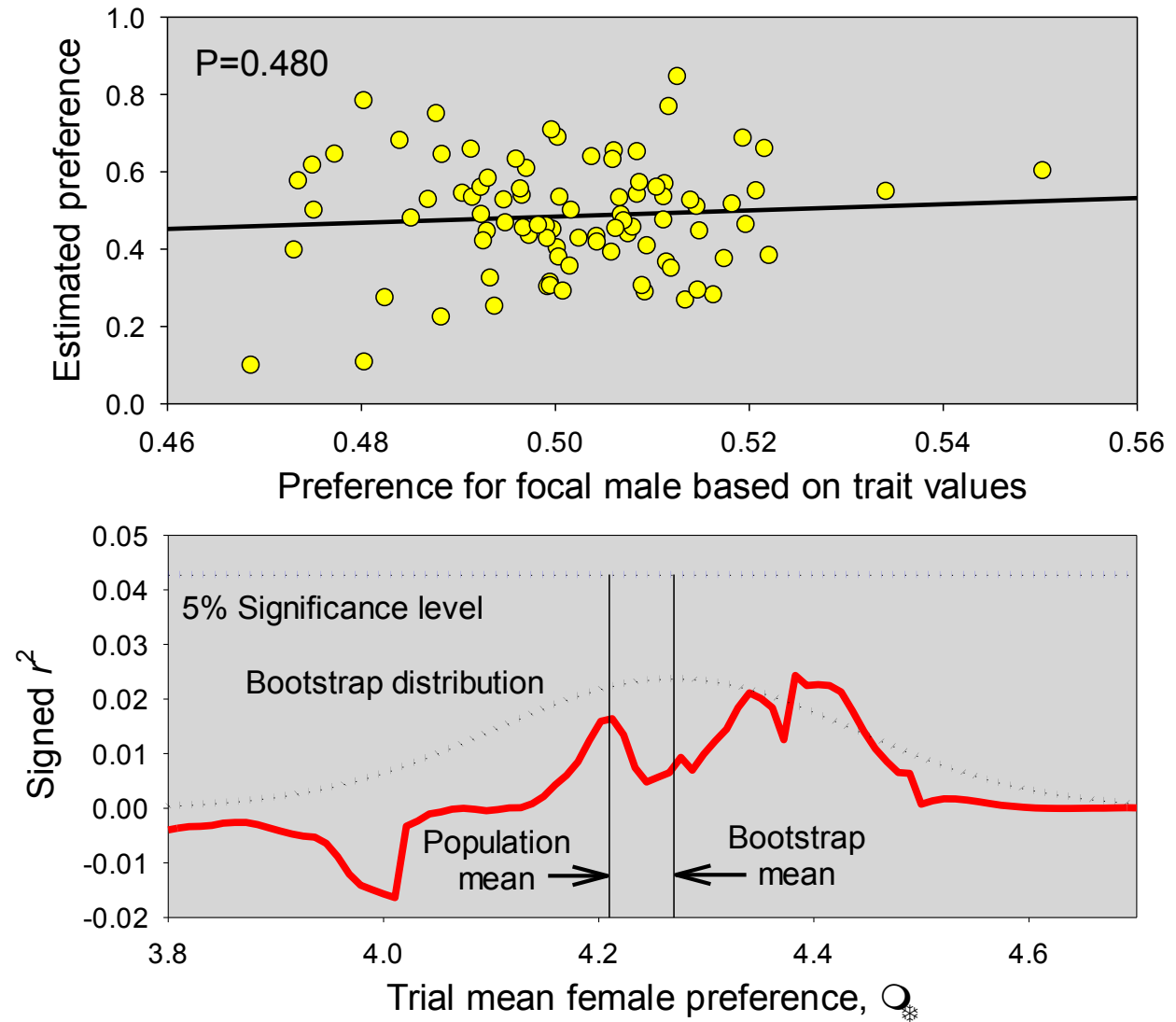


Figure 4. An example of a song trait, (Duration of time male called) that shows statistical indication of directional female preference.

Top panel: Regression of estimated preference for the focal male, P_F , on the preference predicted from the male trait values. Solid line=fitted regression.

Bottom panel: Signed r^2 on the trial mean female preference, μ_T . Solid red line indicates the fit at the trial female preference. Only values lying above the 5% line (dotted blue line) are significant.

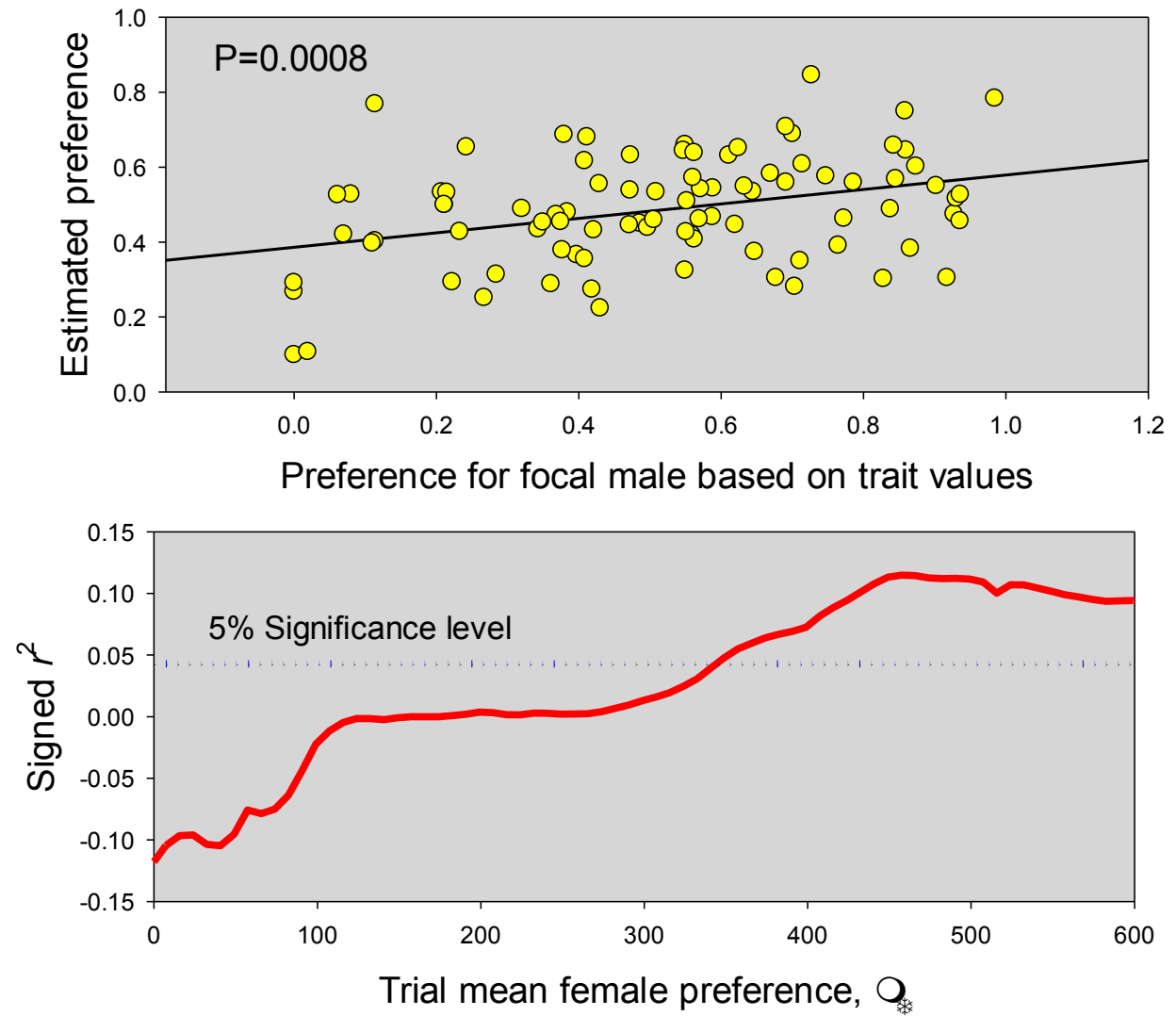
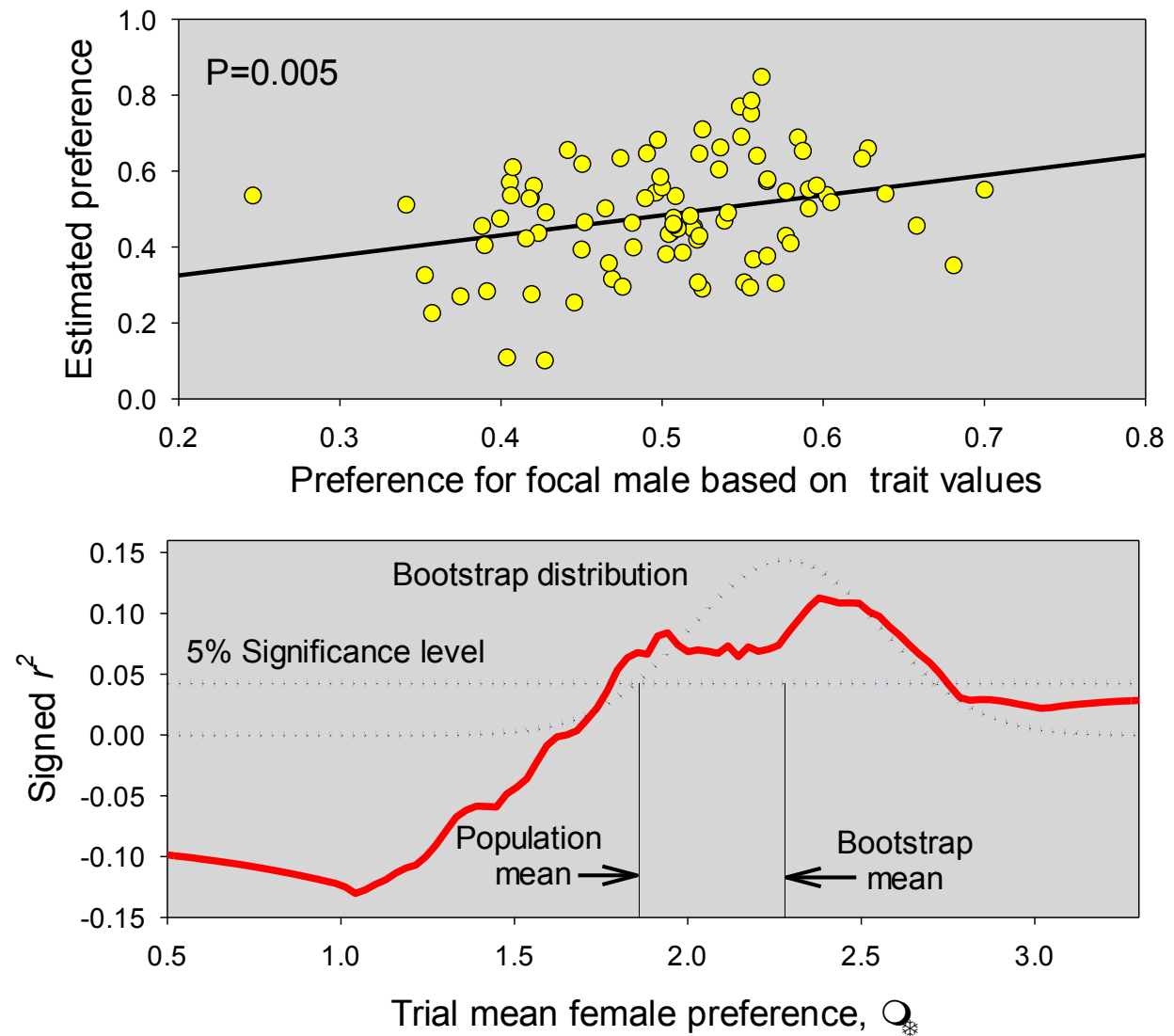


Figure 5. An example of a song trait, (Chirp rate) that shows statistical indication of stabilizing female preference, with the possibility of a directional component.

Top panel: Regression of estimated preference for the focal male, P_F , on the preference predicted from the male trait values. Solid line=fitted regression.

Bottom panel: Signed r^2 on the trial mean female preference, μ_T . Solid red line indicates the fit at the trial female preference. Only values lying above the 5% line (dotted blue line) are significant. The dotted line shows the normal distribution based on the bootstrap values.



SUPPLEMENTAL MATERIAL

1. A Review of current practice in choice experiments

To establish a representative sample of studies using choice designs to evaluate mate choice, we conducted a literature search using Web of Science. We first searched using the keywords "stabilizing, mate choice" and then searched again using the keywords "directional, mate choice". All studies that tested for stabilizing preference also tested for directional preference, but some studies only evaluated directional preference. For our sample, we retained only studies that included statistical tests for stabilizing or directional selection. Our search retrieved 365 papers, of which 38 described no choice experiments and 41 described choice experiments (Table S1). While the resulting sample of studies is not exhaustive, the data are sufficient to deduce general patterns. Choice experiments typically involved discrimination between two potential mates (mean= 2.4, median=2, SD=1.66, SE=0.04), and the mean number of trials (i.e., number of individuals of the choosy sex tested) ranged from 12 to 2400 (mean=147, median=28, SD=411). As indicated by the differences between the mean and median, the distribution of sample sizes was strongly skewed to the right, with only 9 studies (22%) having more than 100 trials.

We scored signal type as artificial, manipulated or natural. Artificial signals such as physical models or computer generated acoustic signals were used in 27% of choice experiments in our sample. The majority of experiments (73%) used manipulated signals, in which the potential mates to be compared were selected by the experimenter so that they differed measurably on the basis of an *a priori* recognizable character such as condition or morphology. Almost all (26 of 30) of these experiments compared males assigned to only two categories, and so were unable to distinguish directional from stabilizing preference as curvature cannot be

established. In these studies, statistical analysis was based on the comparison of means or medians (C. of. M) and used categorical methods such as chi-square, Wilcoxon matched pairs or Mann-Whitney.

The third signal type used, natural signals, consisted of experiments in which the potential mates were selected at random from a population and not selected on the basis of some particular character. This type of variation was hardly ever used (no examples were found in choice experiments and only two examples in no choice experiments) though it more closely represents a natural situation than the other two.

2. Determination of female choice in the simulations

Our preference function (equation 1) is a probability function. To determine which of the two males was actually chosen in each trial of the simulation, we used the following algorithms. For the binary measurement experiment we generated a uniform random number, r_i , between 0 and 1 and determined that the female selected the focal male whenever $P_{F,i} \geq r_i$. In the continuous case we modeled female preference as 100 separate trials with the probability for any single trial being given by $P_{F,i}$. The number of times the female selected the focal male, $n_{F,i}$, was generated and the relative preference, R_P , then computed as $n_{F,i}/100$ and the difference preference, D_P , as $2n_{F,i} - 100$.

3. The probability distribution of a focal male being chosen

To determine the probability distribution of a focal male being chosen we generated 100,000 triplets and calculated this probability from equations 5 or 6 (in main text), as required

by the assumed female preference model. The distributions were almost entirely determined by the type of model and the standard deviations but not the means: hence, we have plotted only the results using means of 10 for both female preferences and the male trait (Fig. S1). Under the ED function the focal male is generally either strongly preferred or strongly rejected. In contrast, under the AD function the probability distributions take their highest values around 0.5 and hence the strength of preference is much lower than in the ED model.

4. Statistical analysis of the simulation model: 0,1 choice experiments

Not surprisingly, for the same sample size tests using 0,1 data were less satisfactory than using continuous data. Results for the ED and AD models were similar but the values for the AP model are consistently less than those of the ED model (Fig. S2). The statistical power of the protocols for detecting stabilizing preference in the simulations with stabilizing preference where data was coded as 0,1 exceeded 80% in 10 of the 16 combinations (Lower panels, Fig. S2). Power to detect directional preference was also low in most combinations (upper left panel, Fig. S2). The detection of apparent directional selection when male and female means were the same was typically about 5% (Upper right panel, Fig.S2)

Statistical power to detect directional preference when females showed only directional preference was less than 80% for 0,1 data (11.6% and 62.9% for male combinations 10:1 and 10:3, respectively) but 100% for the continuous data. For both 0,1 and continuous data directional preference was detected in only 5% of cases when female preference was random. The bias in parameter estimates was less than 5% and negative in 13 of the 16 combinations for the 0,1 data, indicating that the estimates tended to underestimate the true mean.

REFERENCES

- Ahuja A, Singh RS, 2008. Variation and evolution of male sex combs in *Drosophila*: Nature of selection response and theories of genetic variation for sexual traits. *Genetics* 179:503-509.
- Barry KL, Holwell GI, Herberstein ME, 2010. Multimodal mate assessment by male praying mantids in a sexually cannibalistic mating system. *Anim Behav.* 79:1165-1172.
- Beckers OM, Wagner Jr WE, 2011. Mate sampling strategy in a field cricket: evidence for a fixed threshold strategy with last chance option. *Anim Behav.* 81:519-527
- Bentsen CL, Hunt J, Jennions MD, Brooks R, 2006. Complex multivariate sexual selection on male acoustic signaling in a wild population of *Teleogryllus commodus*. *Am Nat.* 167:E102-E116.
- Boake CRB, Poulsen T, 1997. Correlates versus predictors of courtship success: courtship song in *Drosophila silvestris* and *D. heteroneura*. *Anim Behav.* 54:699-704.
- Brooks R, Hunt J, Blows MW, Smith MJ, Bussiere LF, Jennions MD, 2005. Experimental evidence for multivariate stabilizing sexual selection. *Evolution* 59:871-880
- Chenoweth SF, Blows MW, 2005. Contrasting mutual sexual selection on homologous signal traits in *Drosophila serrata*. *Am Nat.* 165:281-289.
- Cook SE, Vernon JG, Bateson M, Guildford T, 1994. Mate choice in the polymorphic African swallowtail butterfly, *Papilio dardanus*: male-like females may avoid sexual harassment. *Anim. Behav.* 47:389-397.
- Crnokrak P, Roff DA, 1995. Fitness differences associated with calling behaviour in the two wing morphs of male sand crickets, *Gryllus firmus*. *Anim. Behav.* 50:1475-1481

- Crnokrak P, Roff DA, 1998. The genetic basis of the trade-off between calling and wing morph in males of the cricket *Gryllus firmus*. *Evolution* 52:1111-1118.
- Gabor CR, Krenz JD, Jaeger RG, 2000. Female choice, male interference, and sperm precedence in the red-spotted newt. *Behav Ecol.* 11:115-124.
- Gerhardt HC, Tanner SD, Corrigan CM, Walton HC, 2000. Female preference functions based on call duration in the gray tree frog (*Hyla versicolor*). *Behav Ecol.* 11:663-669.
- Gershman SN, Sakaluk SK, 2009. No Coolidge effect in decorated crickets. *Ethology* 115:774-780.
- Gillingham MA, Richardson DS, Lovlie H, Moynihan A, Worley K, Pizzari T, 2009. Cryptic preference for MHC-dissimilar females in male red junglefowl, *Gallus gallus*. *Proc Roy Soc B-Biol Sci.* 276:1083-1092.
- Hoikkala A, Aspi J, 1993. Criteria of female mate choice in *Drosophila littoralis*, *D. montana* and *D. ezoana*. *Evolution* 47:768-777.
- Houde AE, 1987. Mate choice based upon naturally-occurring color-pattern variation in a guppy population. *Evolution* 41:1-10.
- Itzkowitz M, Draud MJ, Barnes JL, Haley M, 1998. Does it matter that male beaugregory damselfish have a mate preference? *Behav Ecol Sociobiol.* 42:149-155.
- Jamieson IG, Colgan PW, 1989. Eggs in the nests of males and their effect on mate choice in the three-spined stickleback. *Anim Behav.* 38:859-865.
- Jang Y, Gerhardt HC, 2006. Divergence in female calling song discrimination between sympatric and allopatric populations of the southern wood cricket *Gryllus fultoni* (Orthoptera : Gryllidae). *Behav Ecol and Sociobiol.* 60:150-158.

- Jang YW, Greenfield MD, 1998. Absolute versus relative measurements of sexual selection: Assessing the contributions of ultrasonic signal characters to mate attraction in lesser wax moths, *Achroia grisella* (Lepidoptera : Pyralidae). *Evolution* 52:1383-1393.
- King BH, Saporito KB, Ellison JH, Bratzke RM, 2004. Unattractiveness of mated females to males in the parasitoid wasp *Spalangia endius*. *Behav Ecol and Sociobiol.* 57:350-356.
- Lehmann GUC, Lehmann AW, 2007. Bushcricket song as a clue for spermatophore size? *Behav Ecol and Sociobiol.* 62:569-578.
- MacLaren RD, Rowland WJ, 2006. Differences in female preference for male body size in *Poecilia latipinna* using simultaneous versus sequential stimulus presentation designs. *Behav.* 143:273-292.
- McNamara KB, Jones TeM, Elgar MA, 2004. Female reproductive status and mate choice in the hide beetle, *Dermestes maculatus*. *J Ins Behav.* 17:337-352.
- Oh KP, Shaw KL, 2013. Multivariate sexual selection in a rapidly evolving speciation phenotype. *Proc Roy Soc Biol Sci.* 280:20130482.
- Owen MA, Rohrer K, Howard RD, 2012. Mate choice for a novel male phenotype in zebrafish, *Danio rerio*. *Anim Behav.* 83:811-820.
- Parri S, Alatalo RV, Kotiaho J, Mappes J, 1997. Female choice for male drumming in the wolf spider *Hygrolycosa rubrofasciata*. *Anim Behav.* 53:305-312.
- Phelps SM, Rand AS, Ryan MJ, 2006. A cognitive framework for mate choice and species recognition. *Am Nat.* 167:28-42.
- Reading KL, Backwell PRY, 2007. Can beggars be choosers? Male mate choice in a fiddler crab. *Anim Behav.* 74:867-872.

- Roff DA, Crnokrak P, Fairbairn DJ, 2003. The evolution of trade-offs: geographic variation in call duration and flight ability in the sand cricket, *Gryllus firmus*. J Evol Biol. 16:744-753.
- Rosenblum EB, 2008. Preference for local mates in a recently diverged population of the lesser earless lizard (*Holbrookia maculata*) at white sands. J Herp. 42:572-583.
- Rowland WJ, 1982. Mate Choice by Male Sticklebacks, *Gasterosteus-Aculeatus*. Anim Behav. 30:1093-1098.
- Rutstein AN, Brazill-Boast J, Griffith SC, 2007. Evaluating mate choice in the zebra finch. Anim Behav. 74:1277-1284.
- Schofl G, Dill A, Heckel DG, Groot AT, 2011. Allochronic separation versus mate choice: nonrandom patterns of mating between fall armyworm host strains. Am Nat. 177:470-485.
- Steiger S, Capodeanu-Nagler A, Gershman SN, Weddle CB, Rapkin J, Sakaluk SK, Hunt J, 2015. Female choice for male cuticular hydrocarbon profile in decorated crickets is not based on similarity to their own profile. J Evol Biol 28:2175-2186.
- Suk HY, Choe JC, 2002. Females prefer males with larger first dorsal fins in the common freshwater goby. J Fish Biol. 61:899-914.
- Sztepanacz JL, Rundle HD, 2012. Reduced genetic variance among high fitness individuals: Inferring stabilizing selection on male sexual displays in *Drosophila serrata*. Evolution 66:3101-3110.
- Verrell PA, 1995. Males choose larger females as mates in the salamander *Desmognathus santeetlab*. Ethology 99:162-171.

- Wagner Jr WE, Murray AM, Cade WH, 1995. Phenotypic variation in the mating preferences of female field crickets, *Gryllus integer*. *Anim Behav.* 49:1269-1281.
- Wong BBM, Svensson PA, 2009. Strategic male signalling effort in a desert-dwelling fish. *Behav Ecol and Sociobiol.* 63:543-549.
- Xu J, Wang Q, 2009. A polyandrous female moth discriminates against previous mates to gain genetic diversity. *Anim Behav.* 78:1309-1315.