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# Why Does Attention to Web Articles Fall With Time?

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#### Abstract

We analyze access statistics of 150 blog entries and news articles for periods of up to 3 years. Access rate falls as an inverse power of time passed since publication. The power law holds for periods of up to 1,000 days. The exponents are different for different blogs and are distributed between 0.6 and 3.2. We argue that the decay of attention to a web article is caused by the link to it first dropping down the list of links on the website's front page and then disappearing from the front page and its subsequent movement further into background. The other proposed explanations that use a decaying with time novelty factor, or some intricate theory of human dynamics, cannot explain all of the experimental observations.

### Introduction

Soon after the Internet became popular with the development of the first browsers, researchers started to seek the laws of web surfing. Cunha, Bestavros, and Crovella (1995) studied the browsing patterns of the Internet users from Boston University. They found that the distribution of web pages by the total number of downloads by all users follows a power law. Nielsen (1997) had observed that the same power law holds for the number of downloads of different webpages from the Sun Microsystems website. Huberman, Pirolli, Pitkow, and Lukose (1998) looked at the number of webpages downloaded from the Georgia Tech website by particular users. They found that the distribution of the number of users by the number of clicks they perform follows a power law.

Later researchers studied the patterns of accessing particular webpages. Dezsö et al. (2006) studied the access log of one news website. They found that web documents are mostly accessed during first days after their creation, with the number of accesses decreasing with time as a power law,

$$n(t) \sim 1/t^{\beta}$$
 (1)

with  $\beta = 0.3$ . They explained this by using queuing-based human dynamics model. Wu and Huberman (2007) studied the time series of the number of "diggs" (bookmarks) on the Digg website. Their work is related to the work of Dezsö et al. (2006), because the number of new bookmarks should be proportional to the number of new accesses. Wu and Huberman found that the number of new "diggs" decreases as the time passed since the story appeared on the

website increases. They introduced the concept of a novelty factor, decaying with time as a stretched exponent, to explain their results.

Hogg and Lerman (2009), who also studied Digg, argued for visibility factor instead of novelty factor. The story first appears on website's front page; as time passes, newly added stories push it down to page 2, page 3, and so on. The farther the story is from the front page, the less visible it is, fewer people notice it, and the number of new "diggs" it generates drops. When new stories are added at a constant rate, the position of the story on the website is proportional to the time passed since its publication. The frequency of accessing the story is thus some decreasing function of time. To find the exact functional dependence, Hogg and Lerman (2009) devised a theory based on the model introduced by Huberman et al. (1998) to describe the distribution of the number of users by the number of pages views. The theory of Hogg and Lerman leads to Equation 1 with  $\beta = 1/2$ .

Leskovec, McGlohon, Faloutsos, Glance, and Hurst (2007) studied the evolution of connectivity in the blogo-sphere. They found that the average number of new in-links to a blog entry falls of as an inverse power of time passed since publication of the blog entry. The exponent of the power law is 1.5. We may reason that the number of new in-links is proportional to the number of views (just like the number of bookmarks).

This article analyzes the patterns of access of blog entries and news articles from more than 100 different websites, showing that for about 80% of them the access frequency decays according to Equation 1. The exponents are different for different websites and are distributed between 0.6 and 3.2 with the maximum of the distribution at about 1.5. We offer a theoretical explanation of these observations. Our explanation is similar to that of Hogg and Lerman (2009), in that it is also based on visibility factor. It is different, however, in other aspects and allows for different values of the exponent  $\beta$  in agreement with our data.

The article is organized as follows. The next section describes our data source and analyzes the data. The third section gives the theoretical explanation for our observations. The fourth section describes the earlier theories, and the fifth section explains why our theory is closer to reality.

# The Data Set and Its Analysis

Let us now look at some of our data. Figure 1 shows access statistics for three fixed-content webpages from the website reverent.org (more examples are given by Simkin & Roychowdhury, 2008), which are apparently not affected by any decaying novelty factor. The absolute maximum of daily downloads happens 2 years after webpage publication (Figure 1A,B) and 5 years after publication (Figure 1C). The webpages mentioned are only two clicks away from site's front page. This ensures that they have prominent placement in Internet search. For example, during the year 2010, 737 Internet searches for "Donald Judd" led to the webpage shown in Figure 1A, and 590 searches for "famous artist" led to the webpage shown in Figure 1C. This means that the webpages have some small but constant traffic, directed by search engines. Sometimes visitors mention the webpage, which they found on a blog, forum, or social networking website. Sometimes a visitor to that blog reposts links in his blog, similarly to how scientific citations travel from one paper into

another (Simkin & Roychowdhury, 2007). Sometimes this results in avalanches of blog entries. They lead to spikes of downloads, which are seen in Figure 1. In a previous article (Simkin & Roychowdhury, 2008) we modeled these avalanches using the theory of branching processes (Simkin & Roychowdhury, 2011), so we are not going to repeat the analysis in the present article. One reason why we included Figure 1 in this article is that it helps to question the "novelty factor." Another reason is that it explains how we managed to find access statistics of web articles from many other websites.

Obviously, the number of referrals is proportional to the number of visitors to the referring webpage. Thus, when a blog links to one of the webpages of the website for which we have the access log, we can estimate the access statistics of that blog from the number of referrals. Here is a typical line from the access log.

```
67.188.206.95 - - [09/Feb/2008:12:03:46 -0700] "GET/an_artist_or_an_ape.html HTTP/1.1" 200 3347 http://www.metafilter.com/68935/Hey-my-Cheetah-could-paint-that "Mozilla/5.0 (Windows; U; Windows NT 5.1; en-US; rv:1.8.1.12) Gecko/20080201 Firefox/2.0.0.12
```

At the beginning of the line is the user's IP address. Next is the date and time of access. Afterward is the particular webpage that was downloaded; 200 is the code that the download was successful; 3,347 is the size in bytes. Next is the referrer's URL, and at the end is the browser information. We will need only three of these parameters for our research: date/time, downloaded webpage, and referring webpage.

In the above example, http://www.metafilter.com/68935/Hey-my-Cheetah-could-paint-that is the particular blog entry, which linked to the webpage http://reverent.org/ an\_artist\_or\_an\_ape.html. However, although the blog entry is fresh, it appears on the blog's front page, so one does not have to visit the specific webpage containing the separate blog entry but can be referred from the blog's front page. Thus, the majority of referrers look like http://www.metafilter.com/. The front page is not the only additional referrer. There are also referrals from the next pages (for example, http://www.metafilter.com/index.cfm?page=8) or from tags (e.g., http://www.metafilter.com/tags/art). Therefore, to get all the referrals, one has to select (e.g., using the "grep" command) all the lines in the access log files that contain domain name "metafilter.com." This, however, creates another complication. Metafilter.com has in addition the entry http://www.metafilter.com/60584/My-mother-is-a-fish, which links to another webpage from the same site, http://reverent.org/sounds\_like\_faulkner.html. Therefore, we have to select from all the access log lines that contain "metafilter.com" the lines that in addition contain "an\_artist\_or\_an\_ape.html". These will be all the referrals to http://reverent.org/an artist or an ape.html generated by the http://www.metafilter.com/ 68935/Hey-my-Cheetah-could-paint-that blog entry.

Figure 2 shows the number of referrals as a function of time for four different blogs. We use not calendar days to plot the data but 24-hr days since first referrals. Thus, if the first referral occurred at time t on day d, the first 24-hr day includes referrals up to time t on day d+1, and so on. We computed the average number of daily referrals using logarithmic binning

with base 2. The error bars show the 95% confidence interval. We computed them by using the number of referrals in the bin and assuming that referrals follow a Poisson process. The assumption is probably not justified, but at least it allows some estimate of errors. We selected for Figure 2 the blogs that linked to two or three different webpages from reverent.org. These were two or three separate entries, not links to several webpages in a single blog entry. Different symbols in Figure 2 refer to different webpages. Lines are linear fits of these log–log plots, and the parameters of fits are next to the lines. One can see a power law decay of the number of referrals as a function of time since link publication. One can also see that the exponents of the power law, though very different for different blogs, are very close for different entries of the same blog.

Figure 3A shows the histogram of the power-law exponents for 151 blog entries and news articles from 111 different websites. The data include eight different blog entries from five different bloggers on Blogspot.com, 12 blog entries from 10 different bloggers on livejournal.com, numerous blogs housed by lesser known sites such as livedoor.jp, 12 news articles on lesser known news sites such as thestranger.com, and several articles in well-known journals such as economist.com. The total number of referrals in the data set ranges from 38,512 (this came from ayacnews2nd.com) to 109. In Figure 3B we give the Zipf's plot of the number of referrals. One can notice that the plot is fairly close to a straight line. So we have another power law, in the distribution of the number of referrals. This law is related to Zipf's law in the number of webpage downloads observed by Cunha et al. (1995) and Nielsen (1997).

To obtain the data for Figure 3 we studied all blog entries and news articles (there was a restriction that the referrals should not be from forums for a reason we discuss later) linking to reverent.org or ecclesiastes911.net websites, which produced more than 100 referrals. There were 188 suitable articles, and 151 of them showed a power law and 37 did not.

## Our Theory of the Power-Law Decay of Attention

We propose the following explanation. The probability that visitors to the webpage follow a certain link, posted on this webpage, depends on the position of the link. They follow the current top link with highest probability. The second link they follow with lower probability than the first, and the tenth with even lower probability. One would not expect that position changing from first to second would have the same effect as changing from 10th to 11th. It would be more natural to assume that proportional decrease in position results in proportional decrease in access probability. Falling from first to second place reduces access probability by the same factor as falling from 10th place to 20th. Mathematically this is expressed as

$$\frac{\Delta n(r)}{n(r)} = -\beta \frac{\Delta r}{r}.$$
 (2)

Here n(r) is the access rate, and r is the position rank (so that the top link has rank 1, the second 2, and so on), and  $\beta$  is some proportionality coefficient. This results in a power law decay of access probability with link position,

$$n(r) \sim 1/r^{\beta}$$
. (3)

We cannot determine the value of the exponent  $\beta$  by this reasoning. To do this, we have to say by how much probability of access decreases when the position falls from first to second. For example, if it decreases twice, then the exponent will be exactly 1.

How is this related to the time dependence of access probability? The simplest case is the "Reality Carnival" site (see Figure 2A). This is a webpage containing links to other webpages, which the owner, Dr. Pickover, found interesting. There is no separate blog entry for each link, just the link and a brief description. Dr. Pickover adds one link per day. The new link goes on the top of the list, and all links already present fall in their position by 1. A year's worth of links is on the page at a time. Thus, the number of days passed since link addition exactly corresponds to the link's position in the list. Therefore, r = t, where t is time passed since link publishication measured in days. We thus get Equation 1.

The probability of following a link depends not only on its position in the list but also on how attractive is the link s description. The attractiveness factor is constant and does not vary from day to day. Naturally, it influences only a prefactor and not the power law exponent. At different times, Reality Carnival linked to two webpages from reverent.org. One can see from Figure 2A that the prefactors differ by a factor of 1.5, but the exponents are the same within 1%. A similar pattern holds for three other blogs shown in Figure 2.

One may argue that our derivation has a flaw in that it implicitly assumes that users' clicking behavior is independent of their previous visits to the website. In reality, it is likely that the user is not going to follow a link that he had followed during the previous visit. At the same time, Equation 3 gives a nonzero probability for such an event. Fortunately, it is enough to assume that each user reads only a small fraction of news stories or blog entries appearing on any given news site or blog. Suppose that this fraction is 10%, and let us assume that the user never reads the same story twice. Let us also assume that the number of people who look at the link to the story is given by the power law:  $n_l(t) \sim 1/t^{\beta}$ . Suppose that the fraction of the users who have read the article of age t is f(t). The effect of not reading the same thing twice will be that the number of the users who follow the link will be  $n(t) = (1 - f(t))n_l(t) \sim (1 - f(t)/t^{\beta}$ . Obviously, f(0) = 0 and, in our example,  $f(\infty) = 0.1$ . Thus, the power law will be multiplied by a function of time, which falls from 1 to 0.9 as the story grows older. We are not going to notice this on a logarithmic scale.

Other blogs are different from Reality Carnival; they may add several new items per day or may add only one item in several days. The great majority of them move earlier entries to next pages. In such a case, we can plot the number of referrals as a function of page number. Figure 4 shows such data. The number of referrals falls as a power of the page number. This gives more credence to our claim that the probability of following a link is determined by its position on the website.

### **Earlier Theories**

Dezsö et al. (2006) analyzed a month of access logs for a Hungarian news website. They reported that the average rate of accessing a news story falls as a power law of the time passed since its publication (see Equation 1) with  $\beta=0.3\pm0.1$ . They proposed the following theoretical explanation: The distribution of time intervals between the visits by the same visitor follows a power law  $p(\tau) \sim 1/\tau^{\alpha}$ , with  $\alpha=1.2\pm0.1$ . They speculated that visitors access all news items of interest to them that have appeared on the website since their last visit. The number of visitors who did not yet see the document of age t is

 $n(t){\sim}\widetilde{\int}\,1/\tau^\alpha{\sim}1/t^{\alpha-1}$ , which means that  $\beta = \alpha - 1$ . The observed values of  $\alpha$  and  $\beta$  agree with this theory. There are, however, problems with this explanation. First, it is not clear from the article what are visitors and what are times between visits. There are two ways of tracing visitors, through cookies and through IP addresses. There is more uncertainty in the definition of a visit. For instance, the popular web analytic tool AWStats (2010) separates visits when there was over 1 hour between requests from the same IP. This is quite arbitrary. Therefore, we had to ask the authors what they meant by their words. It turned out (Z. Dezsö, 2009, personal communication) that the visitors were determined from IPs, and "visits" were all HTML requests, that is, every line in the access log. This includes not only webpages but also all image files. Thus downloading one webpage with several images produces a number of "visits" with several intervals between them. That is why the power law in Figure 4A of Dezsö et al. (2006) spreads into the region of 1-second intervals between "visits." One still could separate real visits: those with an interval of 1 day or more can without doubt be called different visits. However, Dezsö et al. (2006) did no analysis showing that after a long absence a visitor looks at more webpages than after a short absence.

Another concern is that many different users have the same IP; this is certainly a problem studying access log of a major news website of a small country. This problem, however, would not affect the work of Chmiel, Kowalska, and Holyst (2009), who investigated the access logs of two Polish portals. They separated different users not by IP addresses but by using cookies. Nonetheless, their Figure 4 is very similar to Figure 4A of Dezsö et al. (2006). The exponent they report is about 1.3, which is very close to the 1.2 value reported by Dezsö et al. Note, however, that Figure 4 of Chmiel et al. (2009), which shows the same type of data as Figure 4A of Dezsö et al. (2006), has a different caption. The figure from Dezsö et al. has the caption "The distribution of time intervals between two consecutive visits of a given user"; the corresponding figure from Chmiel et al. is called "The distribution of time spent by the user on one subpage," which is, of course, a far more reasonable interpretation when we talk about intervals of a few minutes.

Another problem arises if we try to apply the theory of Dezsö et al. (2006) to our data. Some of the referrers show power law decay for several years (see Figures 3 and 4). It is unlikely that some users visit with several years' intervals and then look up everything they missed.

Wu and Huberman (2007) studied the time series of the number of "diggs" (bookmarks) on the Digg website. They proposed the following model. The evolution of the cumulative number of diggs, N(t), is described by the equation

$$\frac{dN(t)}{dt} = N(t)r(t)$$

where r(t) is a decay factor. The equation has the solution

$$N(t) {=} N(0) {\exp \left(\int\limits_0^t dt^{'} r(t^{'})
ight)}$$

The number of new diggs is equal to

$$n(t) = \frac{dN(t)}{dt} = N(0) \exp\left(\int_{0}^{t} dt' r(t')\right) r(t).$$

In the limit of large t, this becomes

$$n(t) = N(0) \exp\left(\int_{0}^{\infty} dt' r(t')\right) r(t) \sim r(t).$$

They obtained the best fit to the actual data using the decay factor  $r(t) = \exp(-0.4t^{0.4})$ . Note that a stretched exponential looks very similar to a power law. By looking at Figure 3 of Wu and Huberman (2007), one can guess that  $r(t) = 1/t^{1.5}$  would do almost as well. This agrees nicely with our data.

Hogg and Lerman (2009), who also studied Digg, explained decay of attention by using visibility factor instead of novelty factor. The story first appears on the website's front page; as time passes, newly added stories push it down to page 2, page 3, and so on. The farther the story is from the front page, the less visible it is, fewer people notice it, and fewer new "diggs" are generated. When new stories are added at a constant rate, the position of the story on the website is proportional to the time passed since its publication. The frequency of accessing the story is thus some decreasing function of time. To find the exact functional dependence, Hogg and Lerman (2009) used the model introduced by Huberman et al. (1998) to describe the probability distribution of the number of webpages that a user views on a certain website.

The model assumes that each page, i, the user visits has a certain value,  $V_i$ , for this user. In addition, it assumes that the value of the next page that the user visits is stochastically related to the value of the current page:  $V_i + 1 = V_i + \varepsilon_i$ , where  $\varepsilon_i$  are independent and

identically distributed Gauss-ian random variables. Thus the value performs a Brownian motion. The user continues to browse the website until the value becomes negative. The distribution of the number of viewed webpages, k, is thus the distribution of the first passage times. This distribution is inverse Gaussian. In the case of zero drift, it has a large k asymptotic

$$p(k) \sim k^{-3/2}$$
. (4)

Actually, if instead of a Gaussian distribution we take a distribution in which  $\epsilon_i$  is +1 or -1, then we will get an ordinary random walk, and the last result will be a bit easier to derive (see Feller, 1957).

Hogg and Lerman assumed that the user starts browsing Digg starting with the front page and afterward proceeds to page 2, page 3, and so on. Thus, the page k will get the users who visited k or more pages of the website. This will be a cumulative distribution of Equation 4:  $p(k) \sim k^{-1/2}$ . Because the page number on which the story appears is proportional to time passed since story publication, the theory of Hogg and Lerman leads to Equation 1 with  $\beta = 1/2$ . This appears to be at odds with what we see in Figure 3 of Wu and Huberman (2007), which is consistent with  $\beta = 1.5$ .

### **Discussion**

Although the functional form of the frequency of access decay function reported by Dezsö et al. (2006) agrees with our data, the value of the exponent does not. They reported  $\beta=0.3$ , whereass we always get  $\beta>0.6$  and in 98% of the cases  $\beta>0.8$ . Why did Dezsö et al. (2006) observe  $\beta=0.3$ ? Earlier we mentioned that 37 of 188 studied blogs and news articles did not show power law decay. Figure 5 shows a typical example. This is an article in *Significance* magazine. From Figure 5A we see that there is no power law fit, and from Figure 5B we can see why: Apart from the initial peak at the release of the article, there are several other peaks. The reason is that the article was discussed in several blogs and forums. The visitors were coming to the article from these blogs and forums, and the position of the article on the website of *Significance* magazine was irrelevant. Dezsö et al. (2006) show in their Figure 3 only average data (more than almost 4,000 news items). We suspect that, if the data for separate news stories were available, the plots would look for some news item similar to Figure 5. The power law with  $\beta=0.3$  could be an artifact of averaging over many news items with different access patterns.

In a related study, Leskovec et al. (2007) reported that the average number of new in-links to a blog entry falls off as an inverse power of time passed since publication of the blog entry. The exponent of the power law is 1.5. We may reason that the number of new in-links is proportional to the number of views (just like the number of referrals). The findings of Leskovec et al. (2007) agree with our results (see Figure 3A of Leskovec et al.).

In another related work, Johansen and Sornette (2000) studied how the number of downloads of their paper behaved after the url was published in a newspaper. They found that after an initial peak the number of downloads fell off as a power law with an exponent

of 0.6. We indeed had once seen such a shallow exponent; however, Johansen and Sornette did not look at the same thing we did. They studied the total number of downloads, not the number of referrals from newspaper. It is certain that the newspaper article triggered a cascade of blog entries linking to the paper. Thus, exponent 0.6 describes not the decay of accessing the newspaper article but the effect of the whole cascade. We can illustrate this with our data. Figure 1A shows a peak in October 2009. This is a result of a cascade triggered by the publication of the link in the popular blog boingboing.net. Figure 6 shows the number of total downloads and the number of referrals from boingboing.net. Although the number of downloads relaxes as a power law with exponent 0.9, the number of referrals from boingboing.net falls off with the exponent 1.5.

The idea of novelty factor is reasonable, and the effects discussed by Dezsö et al. (2006) may also take place. However, these theories cannot account for all of the experimental observations.

Some evidence in support of the importance of the visibility factor comes from the study of forums. The forums differ from blogs and news sites in how comments affect the position of the story. In the case of blogs and news articles, the comments do not change their position on the website. In contrast, when somebody adds a new reply to the forum thread, the thread goes to the top of the forum. Figure 7 shows referrals from two forums together with the number of posts added to the thread on a given day. One can see that each spike in referrals is accompanied by at least one new post. This means that some forum user resurrects the old thread by posting into it and raising it to the top of the forum. Interestingly, for Figure 7B, the highest peak of referrals happens 2 month after the thread was started. If one attempted to use the "novelty factor" of Wu and Huberman (2007) to explain this, one would have to assume that the novelty increased as time passed. Dezsö et al.'s (2006) theory will not account for this as well.

We performed an experiment to test explicitly the effect of link position on clicking probability. We used one already existing webpage, which contained a list of 23 links. For the purposes of this study, we added to the webpage a PHP script, which rotated these 23 links on a daily basis, so that the next day the second link becomes the first, the third becomes second, and the first becomes 23rd. The rotation was implemented to average out the effect of different links being not equally attractive to the visitors. The data shown in Figure 8 were collected over 4 months. The data clearly show a decay of the number of clicks with a link's position, which can be approximated by a power law with  $\beta = 0.4$ . This shows that the position effect obviously exists. However, the value  $\beta = 0.4$  is much less than the typical  $\beta = 1.5$  (see Figure 3) that describes the decay of attention to news articles with time. Therefore, the position effect probably is not the sole reason for the decay of attention. Probably, this decay is the result of a combination of several factors, including those suggested in earlier theories.

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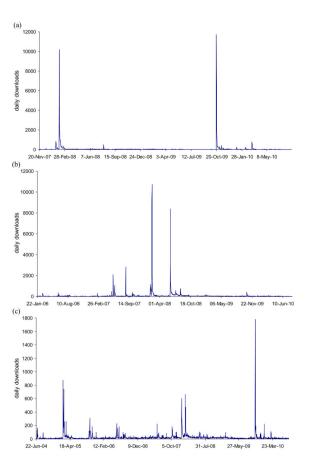


FIG. 1.
Access statistics for three webpages. A: http://reverent.org/
donald\_judd\_or\_cheap\_furniture.html. B: http://reverent.org/an\_artist\_or\_an\_ape.html. C:
http://reverent.org/great\_art\_or\_not.html since the day of their release and until 8/12/2010.
[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

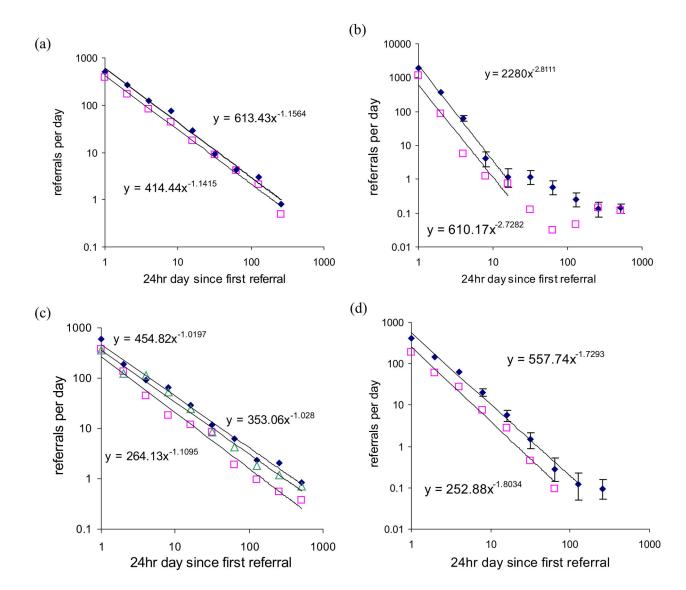
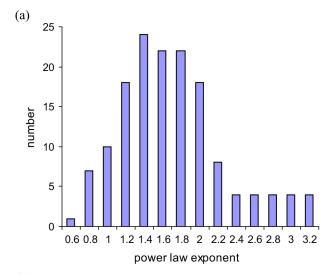
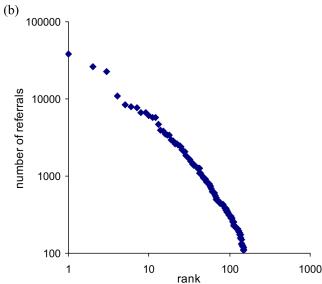


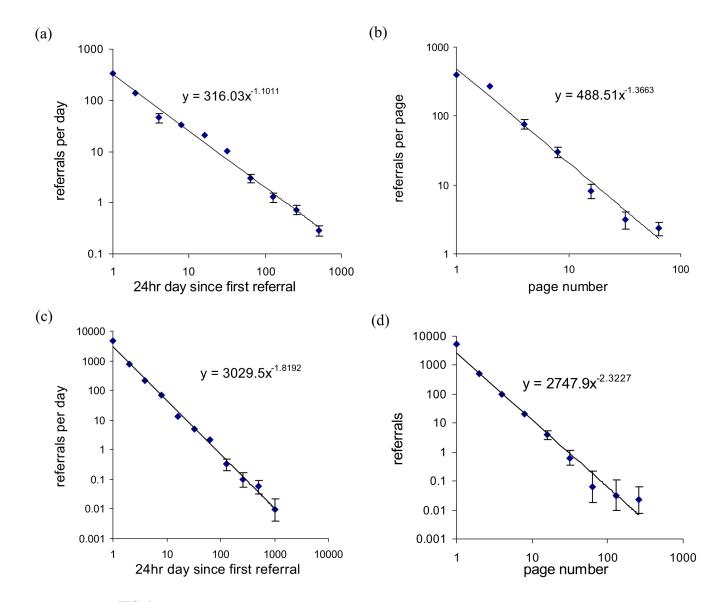
FIG. 2.

A: Referrals from http://sprott.physics.wisc.edu/pickover/pc/realitycarnival.html. It at different times linked to two webpages from reverent.org. One of them is shown by solid rhombs and another by open squares. The lines are the least-square fits to a power law. Although prefactors are 50% different, the exponents differ by only 2%. B: Referrals from http://www.metafilter.com/. C: Referrals from http://howaboutorange.blogspot.com, which linked to three different pages from reverent.org. Note that it was not a single post linking to three webpages but three different posts widely separated in time. D: Referrals from http://krylov.livejournal.com/. We show errors for one data series (solid rhombs) in each plot in the case when those errors are larger than symbol size. We do not show errors for other data series to avoid confusion. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

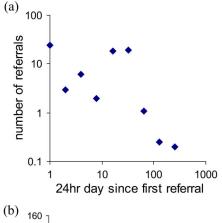




**FIG. 3. A:** Histogram of the power-law exponents for 151 blogs/news articles. The bin is 0.2. **B:** Distribution of the number of referrals. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]



**FIG. 4. A:** Referrals from http://www.museumofhoaxes.com. **B:** Distribution of the referrals by page number. Distribution of referrals from http://www.flabber.nl/ by day (**C**) by page number (**D**). [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]



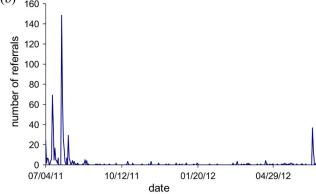


FIG. 5.
Referrals from http://www.significancemagazine.org/details/webexclusive/1237447/PhDs-couldnt-tell-an-actor-from-a-renowned-scientist.html in log-log coordinates (**A**) and in linear coordinates (**B**). [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

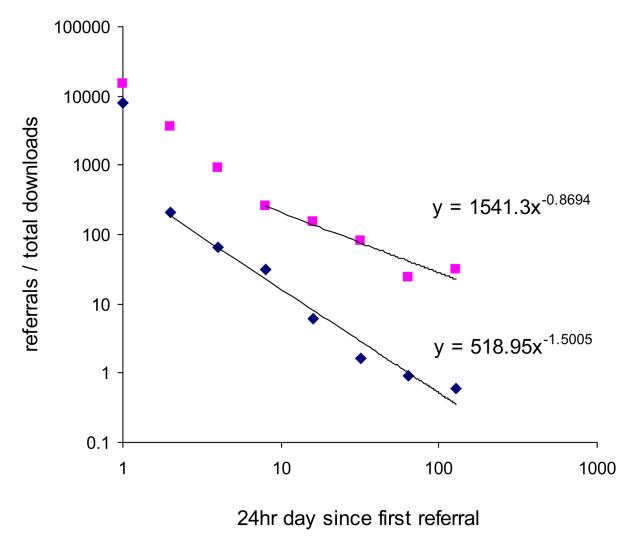


FIG. 6.

The rhombs show referrals from boingboing.net, which linked on 10/19/2009 to the webpage whose access statistics are given in Figure 1A. The squares show the total number of downloads of the webpage in question. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

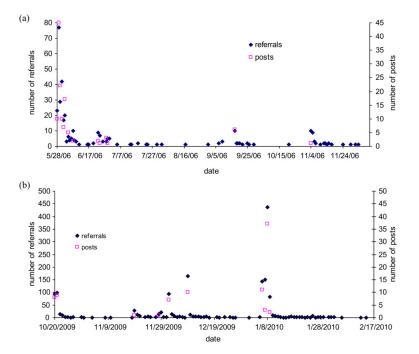


FIG. 7.

A: Daily referrals to http://reverent.org/ru/quizzes.html from http://forum.ixbt.com/
topic.cgi?id=65:1292 shown alongside with the daily number of posts in the thread. B: The
same for referrals to http://reverent.org/true\_art\_or\_fake\_art.html from http://
www.douban.com/group/topic/8380611/. We did not plot zero numbers in the figure, so, a
rhomb very close to a horizontal axis corresponds to at least one referral. [Color figure can
be viewed in the online issue, which is available at wileyonlinelibrary.com.]

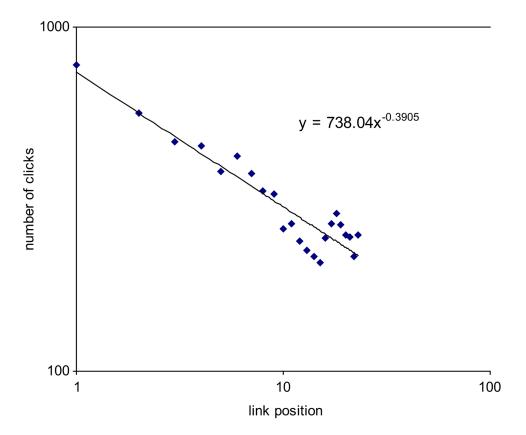


FIG. 8.

Number of clicks versus link position. The webpage's 23 links were rotated on a daily basis for 4 months. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]