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Accessing tri-gluon correlations in the nucleon via the single spin asymmetry in open charm production

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We calculate the single transverse-spin asymmetry for open charm production in pp collisions within the QCD collinear factorization approach. We include contributions from both twist-three quark-gluon and tri-gluon correlation functions. We find that the quark-gluon correlation functions alone generate only a very small asymmetry for open charm production in the kinematic region of current interest at RHIC, so that the observation of any significant single-spin asymmetry would be a clear indication of the presence of tri-gluon correlations inside a polarized proton. We furthermore demonstrate that the tri-gluon contribution could be very different for the production of D and $\bar{D}$ mesons. These features make the single spin asymmetry in open charm production in polarized pp collisions at RHIC an excellent probe of tri-gluon correlation functions.

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I. INTRODUCTION

Large single transverse-spin asymmetries (SSAs) have been consistently observed in various experiments at different collision energies [1–3]. These experimental data have triggered much theoretical activity aiming at identifying the fundamental mechanism behind the measured asymmetries as well as the relevant components of hadron structure. Among the proposed theoretical mechanisms, the transverse momentum dependent (TMD) parton distribution approach [4–10] and the twist-3 quark-gluon correlation approach [11–14] have been the ones most widely discussed in the literature in recent years. The two approaches each have their kinematic domain of validity. For semi-inclusive deep inelastic scattering (SIDIS) and for the Drell-Yan process, they were shown to be consistent with each other in the kinematic regime where they both apply [9]. Both approaches have been applied extensively in phenomenological studies [12, 15–22].

For single hadron inclusive production in hadronic collisions, the large transverse momentum $P_{h\perp}$ of the produced hadron is the only hard momentum scale. For the SSAs in such single-scale hard processes, one expects the QCD collinear factorization approach to be valid [23]. It attributes the observed phenomenon of SSAs to three-parton correlations inside a polarized proton, commensurate with the twist-3 nature of the overall observable. At the leading power in the hard scale, such partonic correlations are represented by the twist-3 quark-gluon correlation function [11, 12],

$$T_{q,F}(x, x) = \int \frac{dy_1^- dy_2^-}{4\pi} e^{ixP^+ y_1^-} \langle P, s_T | \bar{\psi}_q(0) \gamma^+ [\epsilon^{s_T \sigma n \bar{n}} F_\sigma^+(y_2^-)] \psi_q(y_1^-) | P, s_T \rangle, \quad (1)$$

and by a twist-3 tri-gluon correlation function [24, 25],

$$T_G(x, x) = \int \frac{dy_1^- dy_2^-}{2\pi} e^{ixP^+ y_1^-} \frac{1}{xP^+} \langle P, s_T | F_\alpha^+(0) [\epsilon^{s_T \sigma n \bar{n}} F_\sigma^+(y_2^-)] F^{\alpha+}(y_1^-) | P, s_T \rangle, \quad (2)$$

where the proper gauge links have been suppressed. There is a quark-gluon correlation function, $T_{q,F}$, for each quark (anti-quark) flavor q ($\bar{q}$), and there are two independent tri-gluon correlation functions, $T_G^{(f)}(x, x)$ and $T_G^{(d)}(x, x)$,

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because of the fact that the color of the three gluon field strengths in Eq. (2) can be neutralized by contracting with either the antisymmetric if^{ABC} or the symmetric d^{ABC} tensors with color indices, A , B , and C [24, 25].

Most phenomenological studies of SSAs in the twist-3 formalism performed so far have concentrated on the contribution by the quark-gluon correlation functions [12, 15, 22]. The role of the tri-gluon correlation function in SSAs was first studied by Ji in the context of direct-photon production in hadronic collisions [24]. Recently, two of us investigated the contribution of this correlation function to the SSA for open charm production in SIDIS [25]. The twist-3 tri-gluon correlation functions have also been discussed in the context of spin asymmetries for di-jets (or di-hadrons) in hadronic scattering, calculated in the TMD framework [26]. Here they appear after weighting with the transverse-momentum imbalance of the two jets.

In this paper, we study the role of the tri-gluon correlation function in the SSA for open charm production in hadron-hadron collisions. We calculate both the quark-gluon and the tri-gluon contributions to the SSA, at leading order. We find that the quark-gluon correlation function, extracted from data on SSAs in pion production, leads to a very small SSA for open charm production in pp collisions at RHIC energy in almost all the accessible kinematic region. That is, any sizable SSAs observed for open charm production at RHIC will be a direct evidence of a non-vanishing tri-gluon correlation inside a polarized proton. Within a simple model for the $T_G^{(f)}(x, x)$ and $T_G^{(d)}(x, x)$, we find a fairly large SSA for open charm production at RHIC energies. The SSA tends to be maximal in the forward region of the polarized proton and becomes small or changes sign in the backward region. In addition, we find that our calculated SSAs for D and $\bar{D}$ mesons are the same if the tri-gluon correlation function $T_G^{(d)}$ vanishes. If $T_G^{(d)}$ is finite, the SSAs for D and $\bar{D}$ meson production could be very different and could in fact be used to disentangle the contributions from the two different tri-gluon correlation functions. With data on SSAs for open charm production becoming available from RHIC [27], we will be able to extract the tri-gluon correlation functions and to learn about the dynamics of quantum correlations of gluons inside a polarized proton. With additional data on the SSAs for other pp processes [3] and perhaps in the future for SSAs for D and $\bar{D}$ meson production in SIDIS, a global analysis of QCD dynamics beyond leading twist may become possible in the not too distant future.

We note that predictions for the SSA in D meson production at RHIC have also been obtained within the TMD approach [28], assuming that a TMD factorization holds for the single-inclusive observable $pp \rightarrow DX$. The asymmetry was considered as a means to learn about the gluon Sivers function. In our opinion, however, the twist-3 approach provides the relevant and more appropriate framework here, as we described above. On the other hand, the transverse momentum dependent gluon Sivers function is related to the tri-gluon correlation functions. In a process with suitable kinematic regime where both approaches apply, such as Drell-Yan lepton pair production through the gluonic channel at intermediate pair transverse momentum, we expect that the two approaches will provide a consistent description, following the example of the quark Sivers function and the quark-gluon correlation $T_F(x, x)$ [9]. We will present a detailed study of this in a separate publication. We emphasize again that our approach naturally involves two separate tri-gluon correlation functions $T_G^{(f)}(x, x)$ and $T_G^{(d)}(x, x)$, whereas only one Sivers function occurs in the study of [28] (see also [29]). This is expected in general to lead to discernible differences also in phenomenological applications. To give one example, using a single gluon Sivers function, one will find the SSAs for D and $\bar{D}$ meson production to be equal, whereas in our approach they could potentially be very different, as we shall see below. We will return to these issues in our concluding remarks.

We also note that the recent work [30] considers the SSA in charm and anti-charm production at RHIC, through the twist-3 mechanism. In this paper, only the contribution by the quark-gluon correlation function was considered, and the fragmentation of the charm quark into a charmed meson was neglected.

The rest of our paper is organized as follows. In Sec. II, we present our calculation of the SSAs for open charm production in hadronic collisions in terms of the QCD collinear factorization approach. In Sec. III, we propose simple models for the tri-gluon correlation functions, and present our numerical estimates for the SSAs for open charm production in pp collisions at RHIC. Finally, we summarize our results in Sec. IV.

II. CALCULATION OF SINGLE TRANSVERSE-SPIN ASYMMETRY

We consider inclusive single charm meson production in a scattering process between a polarized proton A of momentum P and transverse spin vector s_T and an unpolarized proton B of momentum P' ,

$$A(P, s_T) + B(P') \rightarrow h(P_h) + X, \quad (3)$$

where h represents the observed open charm (D or $\bar{D}$) meson with momentum P_h and mass m_h .

The spin-averaged and spin-dependent cross sections $\sigma(P_h)$, $\Delta\sigma(P_h, s_T)$ are defined as

$$\sigma(P_h) \equiv \frac{1}{2} [\sigma(P_h, s_T) + \sigma(P_h, -s_T)], \quad \Delta\sigma(P_h, s_T) \equiv \frac{1}{2} [\sigma(P_h, s_T) - \sigma(P_h, -s_T)]. \quad (4)$$

The single transverse-spin asymmetry A_N is defined as the ratio of $\Delta\sigma(P_h, s_T)$ and $\sigma(P_h)$,

$$A_N = E_{P_h} \frac{d\Delta\sigma(P_h, s_T)}{d^3P_h} \bigg/ E_{P_h} \frac{d\sigma(P_h)}{d^3P_h}, \quad (5)$$

for the single hadron differential cross sections.

The spin-averaged differential cross section for D meson production at large transverse momentum, $P_{h\perp} > m_h$, can be written in the following factorized form [31, 32]:

$$E_{P_h} \frac{d\sigma}{d^3P_h} = \frac{\alpha_s^2}{S} \sum_{a,b} \int \frac{dz}{z^2} D_{c \rightarrow h}(z) \int \frac{dx'}{x'} \phi_{b/B}(x') \int \frac{dx}{x} \phi_{a/A}(x) \delta(\tilde{s} + \tilde{t} + \tilde{u}) H_{ab \rightarrow c}^U(\tilde{s}, \tilde{t}, \tilde{u}), \quad (6)$$

where $\sum_{a,b}$ represents the sum over all parton flavors and $S = (P + P')^2$ is the total collision energy squared. $\phi_{a/A}(x)$ and $\phi_{b/B}(x')$ are the standard parton distribution functions, and $D_{c \rightarrow h}(z)$ is the fragmentation function for a charm quark c fragmenting into a D meson. We have neglected all dependence on the factorization and renormalization scales in (6). When $P_{h\perp} \gg m_h$, a sizable amount of charm mesons could be produced from the fragmentation of a gluon or a light quark or anti-quark. Then, the sum $\sum_{a,b}$ in Eq. (6) would need to be complemented by an additional sum over the fragmenting parton, running over all possible light parton flavors as well as the charm. However, we do not expect a large fragmentation contribution from light partons to charm meson production at the current RHIC energies, and we will limit our calculations to the fragmentation of charm and anti-charm quarks in this paper.

In Eq. (6), $H_{ab \rightarrow c}^U$ is a short-distance hard part for two partons of flavor a and b to produce a charm quark c . At the lowest order, it gets contributions from the light quark-antiquark annihilation and gluon-gluon fusion subprocesses, as sketched in Fig. 1, and is given by

$$\begin{aligned} H_{q\bar{q} \rightarrow c}^U &= \frac{C_F}{N_C} \left[\frac{\tilde{t}^2 + \tilde{u}^2 + 2m_c^2 \tilde{s}}{\tilde{s}^2} \right], \\ H_{gg \rightarrow c}^U &= \frac{1}{2N_C} \left[\frac{1}{\tilde{t}\tilde{u}} - \frac{N_C}{C_F} \frac{1}{\tilde{s}^2} \right] \left[\tilde{t}^2 + \tilde{u}^2 + 4m_c^2 \tilde{s} - \frac{4m_c^4 \tilde{s}^2}{\tilde{t}\tilde{u}} \right], \end{aligned} \quad (7)$$

where $\tilde{s}, \tilde{t}, \tilde{u}$ are defined at the partonic level as

$$\tilde{s} = (xP + x'P')^2, \quad \tilde{t} = (xP - p_c)^2 - m_c^2, \quad \tilde{u} = (x'P' - p_c)^2 - m_c^2, \quad (8)$$

with p_c and m_c the momentum and mass of the charm quark that fragments into the D meson, respectively.

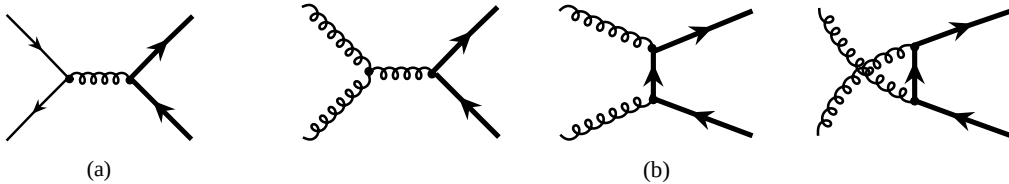


FIG. 1: Lowest order Feynman diagram for light quark-antiquark annihilation (a) and for gluon-gluon fusion to a pair of heavy quarks.

The transverse spin-dependent cross section also gets contributions from both the $q\bar{q}$ annihilation and gg fusion channels. Following the generalized factorization theorem [23], the cross section in the $q\bar{q}$ annihilation channel can be expressed in terms of a general twist-3 quark-gluon correlation function [22],

$$d\Delta\sigma(s_T) \propto \frac{1}{2S} \sum_q \int dz D_{c \rightarrow h}(z) \int \frac{dx'}{x'} \phi_{\bar{q}/B}(x') \int dx_1 dx_2 T_{q,F}(x_1, x_2) i\epsilon^{\rho s_T n \bar{n}} \lim_{k_\perp \rightarrow 0} \frac{\partial}{\partial k_\perp^\rho} H_{q\bar{q} \rightarrow c}(x_1, x_2, k_\perp), \quad (9)$$

with the quark-gluon correlation function $T_{q,F}(x_1, x_2)$ given by

$$T_{q,F}(x_1, x_2) = \int \frac{dy_1^- dy_2^-}{4\pi} e^{ix_1 P^+ y_1^- + i(x_2 - x_1) P^+ y_2^-} \langle P, s_T | \bar{\psi}_q(0) \gamma^+ [\epsilon^{s_T \sigma n \bar{n}} F_\sigma^+(y_2^-)] \psi_q(y_1^-) | P, s_T \rangle, \quad (10)$$

whose diagonal term, at $x_1 = x_2$, is equal to the correlation function in Eq. (1). In order to generate a non-vanishing SSA, a strong interaction phase is necessary, which comes from the interference between a real part of the scattering

amplitude and an imaginary part of the partonic scattering amplitude with an extra gluon, as shown in Fig. 2. Technically, the imaginary part arises when the virtual momentum integral of the extra gluon is evaluated by the residue of an unpinched pole from a propagator in the amplitude with an extra gluon. Such a propagator is indicated by the short bars in the diagrams in Fig. 2. The phase can arise from the attachment of the extra gluon to either the initial-state parton, or the final-state charm quark, which we will refer to as initial-state and final-state interactions, respectively.

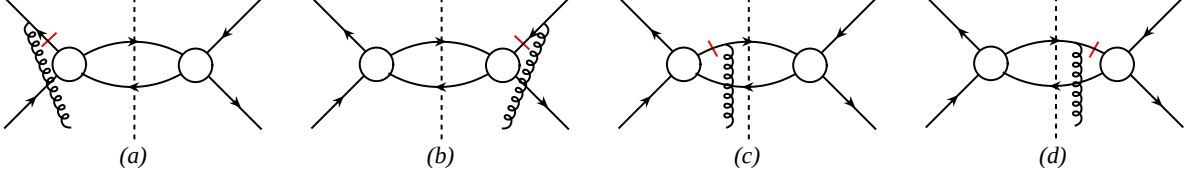


FIG. 2: Feynman diagrams that give the twist-3 contribution to the spin-dependent cross section in the quark-antiquark annihilation channel: initial-state interaction (a), (b), and final-state interaction (c), (d). The short bar indicates the propagator that produces the unpinched pole.

At lowest order, there are four diagrams contributing to the twist-3 polarized cross section in the quark-antiquark annihilation channel, as sketched in Fig. 2, where the blob is given by the diagram in Fig. 1(a). Using the techniques well established in literature (see, for example, [22]), we have

$$E_{P_h} \frac{d\Delta\sigma}{d^3P_h} \Big|_{q\bar{q} \rightarrow c\bar{c}} = \frac{\alpha_s^2}{S} \sum_q \int \frac{dz}{z^2} D_{c \rightarrow h}(z) \int \frac{dx'}{x'} \phi_{\bar{q}/B}(x') \int \frac{dx}{x} \sqrt{4\pi\alpha_s} \left(\frac{\epsilon^{P_h s T n \bar{n}}}{z\tilde{u}} \right) \delta(\tilde{s} + \tilde{t} + \tilde{u}) \\ \times \left[\left(T_{q,F}(x, x) - x \frac{d}{dx} T_{q,F}(x, x) \right) H_{q\bar{q} \rightarrow c}(\tilde{s}, \tilde{t}, \tilde{u}) + T_{q,F}(x, x) \mathcal{H}_{q\bar{q} \rightarrow c}(\tilde{s}, \tilde{t}, \tilde{u}) \right], \quad (11)$$

where $H_{q\bar{q} \rightarrow c}$ can be written as

$$H_{q\bar{q} \rightarrow c} = H_{q\bar{q} \rightarrow c}^I + H_{q\bar{q} \rightarrow c}^F \left(1 + \frac{\tilde{u}}{\tilde{t}} \right), \quad (12)$$

and likewise for $\mathcal{H}_{q\bar{q} \rightarrow c}$, and where the corresponding hard parts are given by

$$H_{q\bar{q} \rightarrow c}^I = \frac{1}{2N_C^2} \left[\frac{\tilde{t}^2 + \tilde{u}^2 + 2m_c^2 \tilde{s}}{\tilde{s}^2} \right], \\ H_{q\bar{q} \rightarrow c}^F = \frac{N_C^2 - 2}{2N_C^2} \left[\frac{\tilde{t}^2 + \tilde{u}^2 + 2m_c^2 \tilde{s}}{\tilde{s}^2} \right], \quad (13)$$

$$\mathcal{H}_{q\bar{q} \rightarrow c}^I = \frac{1}{2N_C^2} \left[\frac{2m_c^2}{\tilde{s}} \right], \\ \mathcal{H}_{q\bar{q} \rightarrow c}^F = \frac{N_C^2 - 2}{2N_C^2} \left[\frac{2m_c^2}{\tilde{s}} \right]. \quad (14)$$

Note that $\mathcal{H}_{q\bar{q} \rightarrow c}^I$ and $\mathcal{H}_{q\bar{q} \rightarrow c}^F$ are proportional to the charm quark mass. As a check of our results, when $m_c^2 \rightarrow 0$ the spin-dependent cross section in Eq. (11) becomes identical to the one for pion production through the $q\bar{q} \rightarrow q'\bar{q}'$ channel [22] (if one replaces the D meson fragmentation function by the pion fragmentation function).

The spin-dependent cross section for $\bar{D}$ meson production can be calculated in the same way. The Feynman diagrams are the same as those for D meson production in Fig. 2, except that the extra gluon should be attached to the anti-charm $\bar{c}$ quark for the final-state interaction. The cross section for $\bar{D}$ meson production has the same factorized form as that in Eq. (11), with the fragmentation function $D_{c \rightarrow D}(z)$ replaced by $D_{\bar{c} \rightarrow \bar{D}}(z)$, and the hard parts given by

$$H_{q\bar{q} \rightarrow \bar{c}}^I = \frac{1}{2N_C^2} \left[\frac{\tilde{t}^2 + \tilde{u}^2 + 2m_c^2 \tilde{s}}{\tilde{s}^2} \right], \\ H_{q\bar{q} \rightarrow \bar{c}}^F = \frac{1}{N_C^2} \left[\frac{\tilde{t}^2 + \tilde{u}^2 + 2m_c^2 \tilde{s}}{\tilde{s}^2} \right], \quad (15)$$

$$\begin{aligned}\mathcal{H}_{q\bar{q}\rightarrow\bar{c}}^I &= \frac{1}{2N_C^2} \left[\frac{2m_c^2}{\tilde{s}} \right], \\ \mathcal{H}_{q\bar{q}\rightarrow\bar{c}}^F &= \frac{1}{N_C^2} \left[\frac{2m_c^2}{\tilde{s}} \right].\end{aligned}\quad (16)$$

These short-distance hard parts are consistent with those presented in the calculation of the SSAs for heavy quark and anti-quark production in hadronic collisions [30]. We note that the hard parts for $\bar{q}q$ scattering are obtained from those for $q\bar{q}$ by $H_{q\bar{q}\rightarrow c}^{I,F} = -H_{q\bar{q}\rightarrow\bar{c}}^{I,F}$ and $H_{q\bar{q}\rightarrow\bar{c}}^{I,F} = -H_{q\bar{q}\rightarrow c}^{I,F}$, and likewise for the $\mathcal{H}^{I,F}$.

Similar to Eq. (9), the spin-dependent cross section for the gg fusion channel has the following factorized form:

$$d\Delta\sigma(s_T) \propto \frac{1}{2S} \int dz D_{c\rightarrow h}(z) \int \frac{dx'}{x'} \phi_{g/B}(x') \int dx_1 dx_2 \tilde{T}_G(x_1, x_2) i\epsilon^{\rho s_T n \bar{n}} \lim_{k_\perp \rightarrow 0} \frac{\partial}{\partial k_\perp^\rho} H_{gg\rightarrow c}(x_1, x_2, k_\perp), \quad (17)$$

where $\tilde{T}_G(x_1, x_2)$ is defined as

$$\tilde{T}_G(x_1, x_2) = \int \frac{P^+ dy_1^- dy_2^-}{2\pi} e^{ix_1 P^+ y_1^- + i(x_2 - x_1) P^+ y_2^-} d_{\alpha\beta}(P, s_T | A^\alpha(0) [\epsilon^{s_T \sigma n \bar{n}} F_\sigma^+(y_2^-)] A^\beta(y_1^-) | P, s_T), \quad (18)$$

with $d_{\alpha\beta} = -g_{\alpha\beta} + \bar{n}_\alpha n_\beta + \bar{n}_\beta n_\alpha$. $\tilde{T}_G(x_1, x_2)$ is related to the tri-gluon correlation function through $T_G(x, x) = x\tilde{T}_G(x, x)$.

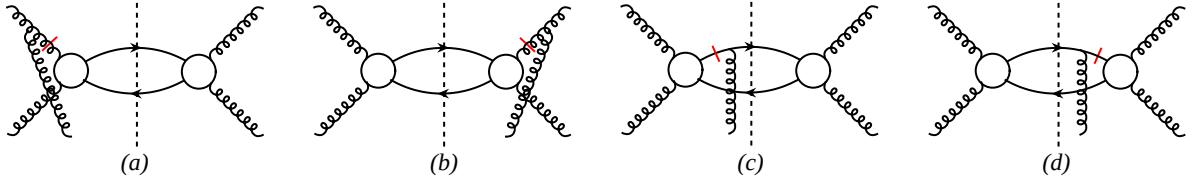


FIG. 3: Feynman diagrams that give the twist-3 contribution to the spin-dependent cross section in the gluon-gluon fusion channel: initial-state interaction (a), (b), and final-state interaction (c), (d). The short bar indicates the propagator that produces the pole.

To calculate the partonic hard part, $H_{gg\rightarrow c}$, in Eq. (17), we need to consider Feynman diagrams with either initial-state or final-state interactions, as sketched in Fig. 3, where the blob is given by the sum of the three diagrams in Fig. 1(b). Hence, each diagram in Fig. 3 corresponds to nine diagrams. Instead of four diagrams in Fig. 2 for the quark-antiquark annihilation subprocess, we have a total of 36 diagrams for gluon-gluon fusion. By evaluating these diagrams, we obtain the contribution to the spin-dependent cross section,

$$\begin{aligned}E_{P_h} \frac{d\Delta\sigma}{d^3P_h} \Big|_{gg\rightarrow c\bar{c}} &= \frac{\alpha_s^2}{S} \sum_{i=f,d} \int \frac{dz}{z^2} D_{c\rightarrow h}(z) \int \frac{dx'}{x'} \phi_{g/B}(x') \int \frac{dx}{x} \sqrt{4\pi\alpha_s} \left(\frac{\epsilon^{P_h s_T n \bar{n}}}{z\tilde{u}} \right) \delta(\tilde{s} + \tilde{t} + \tilde{u}) \\ &\times \left[\left(T_G^{(i)}(x, x) - x \frac{d}{dx} T_G^{(i)}(x, x) \right) H_{gg\rightarrow c}^{(i)}(\tilde{s}, \tilde{t}, \tilde{u}) + T_G^{(i)}(x, x) \mathcal{H}_{gg\rightarrow c}^{(i)}(\tilde{s}, \tilde{t}, \tilde{u}) \right],\end{aligned}\quad (19)$$

where the sum, $\sum_{i=f,d}$, is over the two correlation functions $T_G^{(f)}(x, x)$ and $T_G^{(d)}(x, x)$. The partonic hard part $H_{gg\rightarrow c}^{(i)}$ can be written as

$$H_{gg\rightarrow c}^{(i)} = H_{gg\rightarrow c}^{I(i)} + H_{gg\rightarrow c}^{F(i)} \left(1 + \frac{\tilde{u}}{\tilde{t}} \right), \quad (20)$$

and likewise for $\mathcal{H}_{gg\rightarrow c}^{(i)}$, and we find

$$H_{gg\rightarrow c}^{I(f)} = -\frac{1}{8C_F} \frac{\tilde{t}^2 + \tilde{u}^2}{\tilde{t}\tilde{u}\tilde{s}^2} \left[\tilde{t}^2 + \tilde{u}^2 + 4m_c^2\tilde{s} - \frac{4m_c^4\tilde{s}^2}{\tilde{t}\tilde{u}} \right],$$

$$H_{gg\rightarrow c}^{I(d)} = -\frac{1}{8C_F} \frac{\tilde{u} - \tilde{t}}{\tilde{t}\tilde{u}\tilde{s}} \left[\tilde{t}^2 + \tilde{u}^2 + 4m_c^2\tilde{s} - \frac{4m_c^4\tilde{s}^2}{\tilde{t}\tilde{u}} \right], \quad (21)$$

$$H_{gg\rightarrow c}^{F(f)} = H_{gg\rightarrow c}^{F(d)} = \left[\frac{N_C}{4(N_C^2 - 1)} \frac{\tilde{u}}{\tilde{t}\tilde{s}^2} - \frac{1}{4N_C(N_C^2 - 1)} \frac{1}{\tilde{t}\tilde{u}} \right] \left[\tilde{t}^2 + \tilde{u}^2 + 4m_c^2\tilde{s} - \frac{4m_c^4\tilde{s}^2}{\tilde{t}\tilde{u}} \right], \quad (22)$$

and

$$\begin{aligned}
\mathcal{H}_{gg \rightarrow c}^{I(f)} &= -\frac{1}{2C_F} \frac{m_c^2 (\tilde{t}^2 + \tilde{u}^2) (\tilde{t}\tilde{u} - 2m_c^2 \tilde{s})}{\tilde{s}\tilde{t}^2\tilde{u}^2}, \\
\mathcal{H}_{gg \rightarrow c}^{I(d)} &= -\frac{1}{2C_F} \frac{m_c^2 (\tilde{u} - \tilde{t}) (\tilde{t}\tilde{u} - 2m_c^2 \tilde{s})}{\tilde{t}^2\tilde{u}^2}, \\
\mathcal{H}_{gg \rightarrow c}^{F(f)} &= \mathcal{H}_{gg \rightarrow c}^{F(d)} = -\left[\frac{1}{N_C(N_C^2 - 1)} \frac{1}{\tilde{u}^2} - \frac{N_C}{N_C^2 - 1} \frac{1}{\tilde{s}^2} \right] \frac{m_c^2 \tilde{s} (\tilde{t}\tilde{u} - 2m_c^2 \tilde{s})}{\tilde{t}^2}.
\end{aligned} \tag{23}$$

The gluon-gluon subprocess of course also contributes to the cross section for $\bar{D}$ meson production. The corresponding partonic hard parts for producing an anti-charm quark are given by

$$\begin{aligned}
H_{gg \rightarrow \bar{c}}^{(f)} &= H_{gg \rightarrow c}^{(f)}, & H_{gg \rightarrow \bar{c}}^{(d)} &= -H_{gg \rightarrow c}^{(d)}, \\
\mathcal{H}_{gg \rightarrow \bar{c}}^{(f)} &= \mathcal{H}_{gg \rightarrow c}^{(f)}, & \mathcal{H}_{gg \rightarrow \bar{c}}^{(d)} &= -\mathcal{H}_{gg \rightarrow c}^{(d)},
\end{aligned} \tag{24}$$

where the sign difference of the partonic hard parts for the $T_G^{(d)}$ contribution will be responsible for the difference of the SSAs for D and $\bar{D}$ meson production that will be discussed in the next section. We note that this sign difference can also be observed in the expressions for the “gluonic pole matrix elements” given in [26].

We point out that the compact dependence of the spin-dependent cross section on the combinations $T(x, x) - xT'(x, x)$ of the twist-3 correlation functions found in Ref. [22] for the “massless” case of pion production in hadronic collisions, is violated for the production of D (or $\bar{D}$) mesons by the additional non-derivative terms in Eqs. (11) and (19). The violation is caused by the heavy quark mass since the additional terms vanish when $m_c \rightarrow 0$. In fact, we observe that the hard parts we have derived satisfy the following relation:

$$\mathcal{H}_{ab \rightarrow c}^{I,F} = m_c^2 \frac{dH_{ab \rightarrow c}^{I,F}}{dm_c^2}, \tag{25}$$

separately for any of the various contributions considered above (and likewise for $\bar{c}$ production). This connection is likely a consequence of the “master formula” for twist-3 soft-gluon-pole contributions derived in [14].

We also note that “soft-fermion pole” contributions [12], for which the pole in the hard-scattering function is taken in such a way that the initial quark, rather than the initial gluon, becomes soft, are absent for the $q\bar{q}$ process at the leading order. This is because $q\bar{q}$ annihilation proceeds through an s -channel diagram, whereas soft-fermion poles would only appear in t -channel diagrams. If they were present, such contributions would involve the function $T_{q,F}(0, x)$. For the tri-gluon correlation contribution, terms proportional to $T_G^{(f)}(0, x)$ and $T_G^{(d)}(0, x)$ are automatically included in our calculations. This is due to the symmetry of the partonic hard part under interchange of two gluon lines, and to the fact that field operators commute on the light-cone [23]. This leads to the symmetry properties $T_G(x, x) = T_G(0, x) = T_G(x, 0)$ [24].

Combining the factorized cross sections in Eqs. (11) and (19) with the corresponding partonic hard parts, we have

$$E_{P_h} \frac{d\Delta\sigma}{d^3P_h} = E_{P_h} \frac{d\Delta\sigma}{d^3P_h} \Big|_{q\bar{q} \rightarrow c\bar{c}} + E_{P_h} \frac{d\Delta\sigma}{d^3P_h} \Big|_{gg \rightarrow c\bar{c}} \tag{26}$$

for the leading-order contribution to the transverse-spin-dependent cross section for D (or $\bar{D}$) meson production in hadronic collisions. The corresponding single transverse-spin asymmetry is obtained by substituting Eqs. (6) and (26) into Eq. (5).

III. PHENOMENOLOGY

We now use the expressions we have derived in the previous section to obtain phenomenological results suitable for RHIC. We will propose simple models for the tri-gluon correlation functions $T_G^{(f)}(x, x)$ and $T_G^{(d)}(x, x)$, and then estimate the size of the SSA for D and $\bar{D}$ meson production in $p^\uparrow p$ collisions at RHIC at $\sqrt{s} = 200$ GeV.

In our studies, we adopt the CTEQ6L parton distribution functions [33] for the unpolarized proton. We use the charm-to- D meson fragmentation function of Ref. [34]. In order to treat the kinematic charm mass effects in the fragmentation process, we adopt one of the choices introduced in Ref. [35], which corresponds to setting $P_{h\perp} = zp_{c\perp}$

and $y_D = y_c \equiv y$, where $P_{h\perp}$ ($p_{c\perp}$) and y_D (y_c) are the transverse momentum and rapidity of the D meson (charm quark), respectively. With this choice, we then have for $\tilde{s}, \tilde{t}, \tilde{u}$ and the Feynman variable x_F :

$$\tilde{s} = x'xS, \quad \tilde{t} = -xm_{c\perp}\sqrt{S}e^{-y}, \quad \tilde{u} = -x'm_{c\perp}\sqrt{S}e^y, \quad x_F = \frac{m_{h\perp}}{\sqrt{S}}(e^y - e^{-y}), \quad (27)$$

where $m_{c\perp} = \sqrt{m_c^2 + p_{c\perp}^2}$ and $m_{h\perp} = \sqrt{m_h^2 + P_{h\perp}^2}$. We further assume that $D_{\bar{c} \rightarrow \bar{D}}(z) = D_{c \rightarrow D}(z)$ for the $\bar{D}$ meson fragmentation functions. We choose the factorization scale to be equal to the renormalization scale throughout, and set $\mu = \sqrt{m_c^2 + P_{h\perp}^2}$ with $m_c = 1.3$ GeV.

In order to calculate numerical values for the SSAs for the production of D or $\bar{D}$ mesons, we need the unknown, but universal, tri-gluon correlation functions $T_G^{(f,d)}(x, x)$. Because of their nonperturbative nature, both the quark-gluon correlation functions $T_{q,F}(x, x)$ and the tri-gluon correlation functions $T_G^{(f,d)}(x, x)$ should in principle be extracted from experimental data on SSAs. For the $T_{q,F}(x, x)$, this was done in Ref. [22] by fits to the experimental data [1, 3] for the SSA in $pp \rightarrow \pi X$. We adopt in the following the set referred to as “Fit II” in [22]. We note that the tri-gluon correlations were not taken into account in [22], so that no direct information on these is available so far. For the purpose of estimating the SSAs and motivating future experimental measurements, we therefore follow the arguments given in Sec. IV of Ref. [12] and model the $T_G^{(f,d)}(x, x)$ as

$$T_G^{(f)}(x, x) = \lambda_f G(x), \quad T_G^{(d)}(x, x) = \lambda_d G(x), \quad (28)$$

with $G(x)$ the ordinary unpolarized gluon distribution function. We emphasize that the above parameterizations are only guidelines and rough estimates. As stated earlier, we hope that the experimental study of heavy flavor SSAs at RHIC will provide more information on these correlation functions. In order to cover a range of possibilities for the nonperturbative correlation functions, we introduce three sets of values for the parameters λ_f and λ_d : (1) $\lambda_f = \lambda_d = 0.07$ GeV, (2) $\lambda_f = \lambda_d = 0$, and (3) $\lambda_f = -\lambda_d = 0.07$ GeV, corresponding to the assumptions: $T_G^{(f)} = T_G^{(d)}$, $T_G^{(f)} = T_G^{(d)} = 0$, and $T_G^{(f)} = -T_G^{(d)}$, respectively. In principle, the signs and the values of λ_f and λ_d , as well as the functional form of the correlation functions should be fixed by future data. Comparing SSAs for physical cross sections involving the same non-perturbative twist-three correlation functions but different partonic hard subprocesses will provide stringent tests of QCD dynamics and the twist-3 factorization we use.

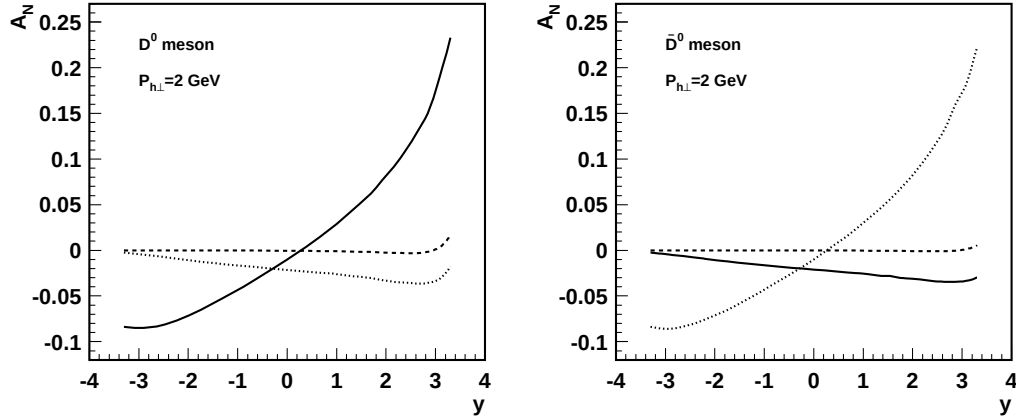


FIG. 4: The SSA as a function of rapidity y for D^0 meson (left) and $\bar{D}^0$ meson production (right) at $\sqrt{s} = 200$ GeV and $P_{h\perp} = 2$ GeV. The curves are: solid ($\lambda_f = \lambda_d = 0.07$ GeV), dashed ($\lambda_f = \lambda_d = 0$), dotted ($\lambda_f = -\lambda_d = 0.07$ GeV).

In Figs. 4 and 5 we plot the SSAs, A_N , for the production of D and $\bar{D}$ mesons as functions of rapidity y and Feynman- x_F , respectively. We count positive rapidity in the forward direction of the polarized proton. The solid, dashed, and dotted curves correspond to the three sets of parameters: $\lambda_f = \lambda_d = 0.07$ GeV, $\lambda_f = \lambda_d = 0$, and $\lambda_f = -\lambda_d = 0.07$ GeV, respectively. From the dashed curves in Figs. 4 and 5, it is clear that the quark-gluon correlation function $T_{q,F}$ alone generates a very small single transverse-spin asymmetry at RHIC energy. This is because of the dominance of the gg fusion contribution over the $q\bar{q}$ one in the spin-averaged cross section in the denominator of A_N . In other words, any significant size of the SSA in open charm production signals the discovery of tri-gluon correlations inside a polarized proton.

The difference between the solid and dotted curves in Figs. 4 and 5 indicates that the two tri-gluon correlation functions, $T_G^{(f)}$ and $T_G^{(d)}$, may both play very important, but different, roles for the SSA in D and $\bar{D}$ meson production.

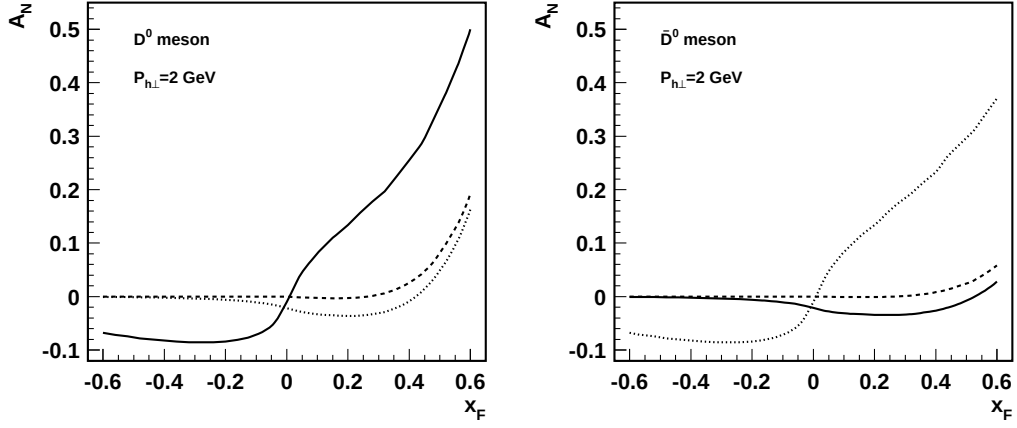


FIG. 5: Same as Fig. 4, but as a function of Feynman- x_F .

In the case of D mesons, a large A_N (see the solid curve) is obtained when $\lambda_f = \lambda_d = 0.07$ GeV, i.e., when $T_G^{(f)}$ and $T_G^{(d)}$ have the same sign. However, when their signs are opposite, their contributions to the SSA tend to cancel, leading to a much smaller SSA (dotted curve). On the contrary, for $\bar{D}$ meson production, the largest A_N is found when $T_G^{(f)}$ and $T_G^{(d)}$ have opposite signs. This is due to the fact that, as shown in Eq. (24), the partonic hard parts associated with $T_G^{(d)}$ change sign when going from charm to anti-charm production, while the hard parts for $T_G^{(f)}$ remain the same. As a result, the SSA for $\bar{D}$ mesons is much smaller if $T_G^{(f)}$ and $T_G^{(d)}$ have the same sign. In addition, as seen from Figs. 4 and 5, scans of the SSA from the forward to the backward region may provide good sources of information on the x -dependence or the functional form of the tri-gluon correlation functions, in particular if a sign change occurs. It is also striking to see that the asymmetry for either D or $\bar{D}$ mesons may become very large at forward rapidities at RHIC (but not for both simultaneously).

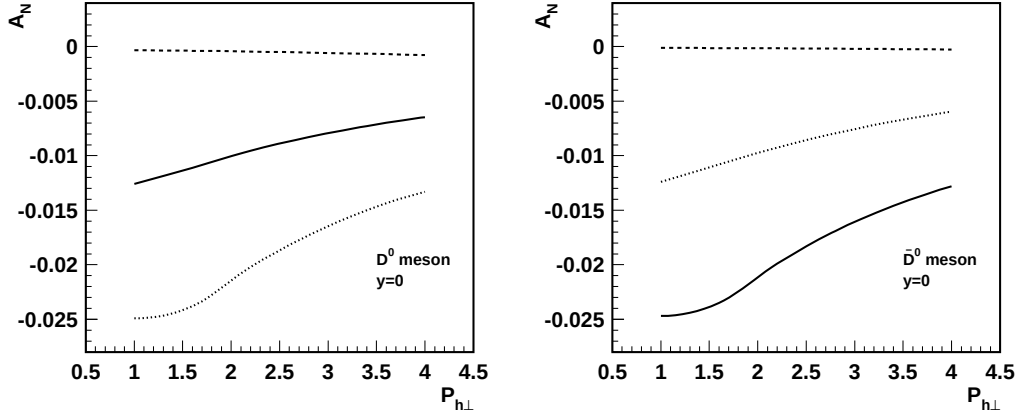


FIG. 6: The SSA as a function of $P_{h\perp}$ for D^0 (left) and $\bar{D}^0$ mesons (right) at mid-rapidity, $y = 0$, and $\sqrt{s} = 200$ GeV. The curves are: solid ($\lambda_f = \lambda_d = 0.07$ GeV), dashed ($\lambda_f = \lambda_d = 0$), dotted ($\lambda_f = -\lambda_d = 0.07$ GeV).

In Figs. 6 and 7, we show A_N for D^0 and $\bar{D}^0$ meson production as a function of $P_{h\perp}$, at mid-rapidity ($y = 0$) and forward-rapidity ($y = 1.8$), respectively. The absolute values of the SSAs decrease as a function of $P_{h\perp}$, which is a natural behavior of the twist-3 effect in QCD collinear factorization. As before, while the contribution by the quark-gluon correlation functions is very small, the two tri-gluon correlation functions can make sizable, and very different, contributions to the SSA, thanks to the difference in the partonic hard parts in Eq. (24).

We finally note that first experimental data on the SSAs for open-charm production are now emerging from RHIC [27]. The uncertainties are currently too large to allow distinction of the various models we have proposed, but the measurements are certainly very encouraging.

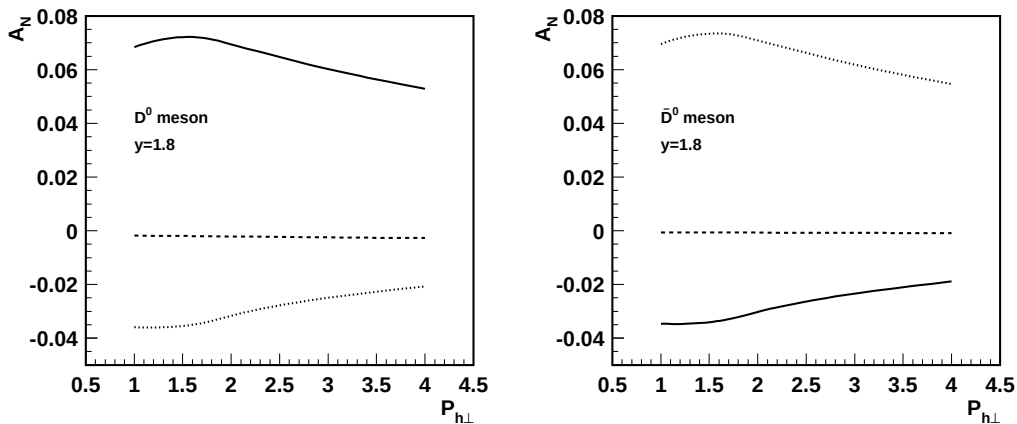


FIG. 7: Same as Fig. 6, but at forward rapidity, $y = 1.8$.

IV. SUMMARY AND CONCLUSIONS

We have studied the single transverse-spin asymmetries for D and $\bar{D}$ meson production in hadronic collisions. Within the QCD collinear factorization approach, we have calculated both the derivative and the non-derivative contributions to the SSAs. We have included the contributions by the twist-3 quark-gluon correlation functions, shown in Eq. (11), as well as by the twist-3 tri-gluon correlation functions, given in Eq. (19). We have found that the quark-gluon correlation functions alone generate a negligible SSA for open charm production in almost all the kinematic region of interest at RHIC. We thus conclude that any sizable SSAs observed in D or $\bar{D}$ production will be a discovery of tri-gluon correlations inside a polarized proton.

We have proposed several simple models for the two unknown tri-gluon correlation functions and used these to make predictions for the SSAs in D meson and $\bar{D}$ meson production in polarized proton-proton collisions at RHIC. We have found that within our models, the asymmetries could be sizable and provide an important source of information on the two unknown tri-gluon correlation functions. We also found that the two correlation functions play a very different role in generating SSAs for D and $\bar{D}$ mesons, due to the sign difference between the partonic hard parts for charm and anti-charm production (see Eq. (24)). Comparison of the SSAs for D and $\bar{D}$ mesons could thus provide an excellent tool for separating the two tri-gluon correlation functions. With data for the SSAs in open charm production arriving from RHIC [27], we will be able to learn for the first time about the dynamics of multi-gluon correlations inside a polarized proton.

We close this paper with a theoretical observation. As we mentioned in the Introduction, two approaches are commonly used for the study of SSAs in high energy collisions: the collinear factorization we have used in this paper, and the transverse momentum dependent (TMD) factorization approach. The two are known to be closely connected and complementary to each other [9]. As was shown in Ref. [7], the twist-three quark-gluon correlation function, $T_{q,F}(x, x)$, is related to a moment in transverse momentum of the corresponding quark Sivers function, $q_T(x, k_\perp)$:

$$T_{q,F}(x, x) = \frac{1}{M_p} \int d^2 \vec{k}_\perp \vec{k}_\perp^2 q_T(x, k_\perp), \quad (29)$$

up to ultraviolet renormalization. Here M_p is a hadronic mass scale. Applying the same method used to derive the above relation to the TMD gluon distribution, we would obtain an identical relation between the tri-gluon correlation function $T_G^{(f)}(x, x)$ and the moment of the gluon Sivers function. The occurrence of the antisymmetric color contraction of the three gluonic field strengths in the tri-gluon correlation function is a natural consequence of the expansion of the gauge link in the adjoint representation when taking the transverse momentum moment of the gluon Sivers function. It is interesting to note that the other tri-gluon correlation function, $T_G^{(d)}(x, x)$, does not appear to have a simple relation connecting it to the operator definition of the gluonic Sivers function. That said, in the TMD approach one can define tri-gluon correlators with both the f and d color structures [26] when considering general QCD hard-scattering processes, which correspond to our $T_G^{(d)}$ and $T_G^{(f)}$ after transverse-momentum weighting. In any case, both $T_G^{(d)}(x, x)$ and $T_G^{(f)}(x, x)$ are allowed and in general present in the collinear factorization approach. It is therefore very important to measure the difference of SSAs in D and $\bar{D}$ meson production, in order to identify the role of $T_G^{(d)}(x, x)$.

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