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**Title**

Important Distortion Factors in the Encoding of Very High Quality Images

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**Publication Date**

1994

Peer reviewed



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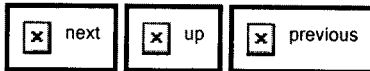
## INTRODUCTION

- Image impairments due to coders are spatially local and described as "end of block errors", "ringing", "jagged edges", "random errors" etc.
- Image impairments can be quantified by distortion factors  $F_i$ .
- A Picture Quality Scale(P Q S) which combine distortion factors into a single, perceptually meaningful, numerical measure has been reported previously.
- At high image quality, not all impairments are perceptible.

This paper examines distortion factors important at high quality to

- Predict perceptible impairments
  - Modify and simplify a Picture Quality Scale
  - Allow new design methods
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*Tue Sep 20 00:45:13 PDT 1994*



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## THE PQS SYSTEM

- The visibility of image impairments due to coding depends on coding errors and properties of the Human Visual System(HVS).
- Coding errors are perceptually weighted to account for Weber's Law in the perception of luminance and for the MTF of the HVS.

### 1.Perceptual Weighting of Errors

Luminance - Brightness

Errors are evaluated on a brightness scale.

Spatial Frequency Weighting

Anisotropic single channel weighting.

### 2.Perceived Impairments and Distortion Factors

Random Errors - Distortion Factors F1, F2

$$F_1 = \frac{\sum_m \sum_n [e_w(m, n)]^2}{\sum_m \sum_n [I(m, n)]^2}$$

$$F_2 = \frac{\sum_m \sum_n [e_w(m, n)]^2 T}{\sum_m \sum_n [I(m, n)]^2}$$

$F_1$  and  $F_2$  use different frequency weighs. T is zero-one indicator of visibility threshold.

Structured Errors - Distortion Factors F3,F4,F5

$F_3$  = End of Block Errors

End of blocks error discontinuities are horizontal and vertical structures measured by  $F_3$ ,

For  $M \times N$  block,

$$F_3 = \left[ \left[ E \left\{ \Delta e_w(iM, n) \right\} \right]^2 + \left[ E \left\{ \Delta e_w(m, jN) \right\} \right]^2 \right]^{\frac{1}{2}}$$

$$\Delta e_w(iM, n) = e_w(iM, n) - e_w(iM + 1, n)$$

$$\Delta e_w(m, jN) = e_w(m, jN) - e_w(m, jN + 1)$$

$F_4$ =General correlated errors

structure errors are quantified by their correlation

$$F4 = (R_x^2 + R_y^2)^{\frac{1}{2}}$$

$$R_x = \sum_{dm=1}^{M-1} \sum_{k=1}^N \left[ R \left\{ \frac{e_w(dm, k)}{e_{ox}} \right\} \right]^2$$

$$R_y = \sum_{\ell=1}^M \sum_{dn=1}^{N-1} \left[ R \left\{ \frac{e_w(\ell, dn)}{e_{oy}} \right\} \right]^2$$

$$R \left\{ e_w(dm, k) \right\} = E \left\{ e_w(m + dm, k) \cdot e_w(m, k) \right\}$$

$$R \left\{ e_w(\ell, dn) \right\} = E \left\{ e_w(\ell, n + dn) \cdot e_w(\ell, n) \right\}$$

$$e_{ox} = \max R \left\{ e_w(0, k) \right\}$$

$$e_{oy} = \max R \left\{ e_w(\ell, 0) \right\}$$

$F5$ =Random errors in the vicinity of high contrast image transitions

$$F5 = (e_x^2 + e_y^2)^{\frac{1}{2}}$$

$$e_x = E \sum_{j=-\ell}^{\ell} \left| e_w(p + j, q) S_x(p + j, q) \right|$$

$$e_y = E \sum_{j=-\ell}^{\ell} \left| e_w(p + j, q) S_y(p + j, q) \right|$$

and

$$S_x(r, s) = e^{\{-0.04V_x(r,s)\}}$$

$$S_y(r, s) = e^{\{-0.04V_y(r,s)\}}$$

and  $V_x(r, s)$  is the horizontal first order difference. Edges are located with a Kirsh operator.

### 3. Picture Quality Scale(PQS)

The factors  $F1, \dots, F5$  are quite correlated.  
The largest three eigenvalues amount for 98% of the total error energy.

PQS is a linear combination of distortion factors, or of their principal components  $\{Z_j\}$ .  
Only 3 principal components needed.

$$PQS = a_0 + \sum_{j=1}^5 a_j \cdot F_j$$

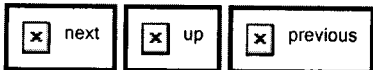
or

$$PQS = b_0 + \sum_{j=1}^3 b_j \cdot Z_j$$

The correlation of PQS versus MOS is quite good at 0.88 for the range of 2 to 4 in MOS.

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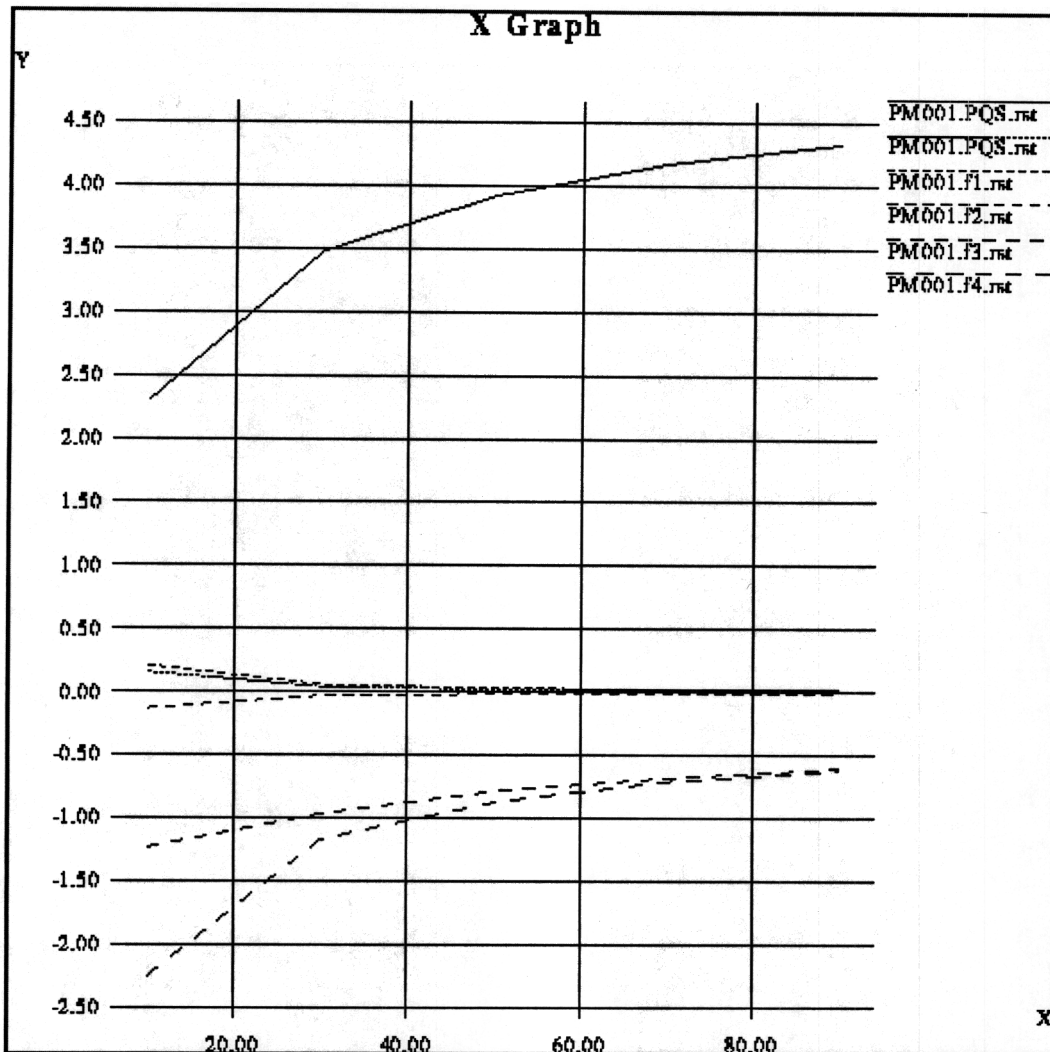
## IMPORTANT FACTORS AT HIGH QUALITY

- The plot of distortion factors contributions to PQS shows that only F4 and F5 remain significant at high quality.
- We study more closely these factors for high quality images To correlate  $F_4$  and  $F_5$  with perceived errors To refine the evaluation of  $F_4$  and  $F_5$
- Test image and Coding Scheme

JPEG compression at Quality level 40

Four 512 by 512 pixels subimages from one of the NTT 2048 by 2048 pixels images are used for our tests.

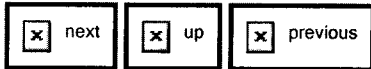
- Spatial contributions to  $F_4$  and  $F_5$  are shown as grey scale images or distortion maps DM4 and DM5.
- At high quality, only peak values of distortion maps are perceived.



PQS and Distortion Factors VS. JPEG Quality

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## PREDICTING VISIBLE DISTORTION WITH PQS DISTORTION MAPS

- We examine the ability of spatial distortion maps DM4 and DM5 to predict to the visible coding errors at high quality.
- The histograms of DM4 and DM5 show a large range of values.
- Small values of DM4 and DM5 do not correspond to visible errors.
- With suitable thresholds, DM4 and DM5 are fairly good predictors of perceptible distortion.
- sigmoid functions are used instead of an abrupt threshold
- with

$$\text{sigmoid}(\mathbf{x}) = e^{\alpha(\mathbf{x}-b)} / (e^{\alpha(\mathbf{x}-b)} + 1) \cong S(\mathbf{x})$$

We evaluate  $DMH4 = S4(\mathbf{x})DM4$   $DMH5 = S5(\mathbf{x})DM5$  where  $DMH()$  denotes the distortion map at high quality and  $S4(\mathbf{x})$  and  $S5(\mathbf{x})$  are adjusted experimentally.

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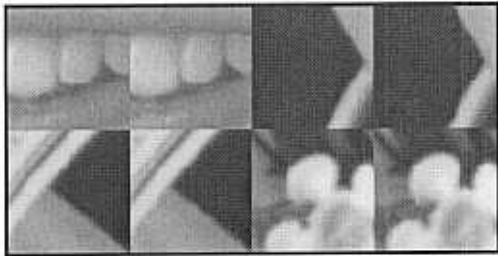
## EXPERIMENTAL RESULTS

### Perceived Errors

- Perceived errors correspond fairly well to image regions indicated by the high quality distortion maps DMH4 and DMH5.
- Only 5 % of the pixels in most images have visible errors.

### Distribution of Errors

Distortion maps and images encoded for high quality show that perceptible errors are associated with specific image features  
High contrast transitions or edges  
High detail regions adjacent to, or on a flat background  
Diagonal image structures



We observe the correspondence of distortion maps to perceived coding errors.

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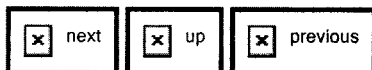
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## APPLICATIONS OF PQS

- Comparison of Transforms (DCT), Subband and Wavelet representations.
- Design of quantization matrix for improved performance.
- Optimization of overall coder.
- Example 1: Comparison of Representations.
- Example 2: Optimization of quantization matrix for Wavelet coder, with and without adaptive noise reduction

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## MODIFICATION OF PQS AT HIGH QUALITY

- We propose a modification of PQS for high quality that uses only structured errors and modified distortion factors  $F_{4H}$  and  $F_{5H}$ .
- $F_{4H}$  and  $F_{5H}$  make use of the high quality distortion maps DMH4 and DMH5 with suitable summation over the entire image.
- Therefore

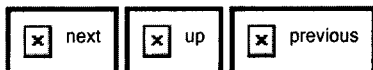
$$PQS_H = a_0 + a_1 F_{4H} + a_2 F_{5H}$$

where the weights  $\{a_i\}$  are determined

by fitting the high end of the performance curves.

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## CONCLUSIONS

- Study of distortion factors at high quality shows that only structured errors for factors **F4** and **F5** are important.
- Experimental study shows that at high quality perceived errors are associated with specific image structures and account only for 5% of the pixels.
- A modified Picture Quality Scale is proposed.
- Examples of applications of PQS are shown.
- Research to be done:  
Relate PQS4H to more complete perceptual models.

Systematically develop new design strategies and verify results experimentally.

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## Original Image and Encoded Image



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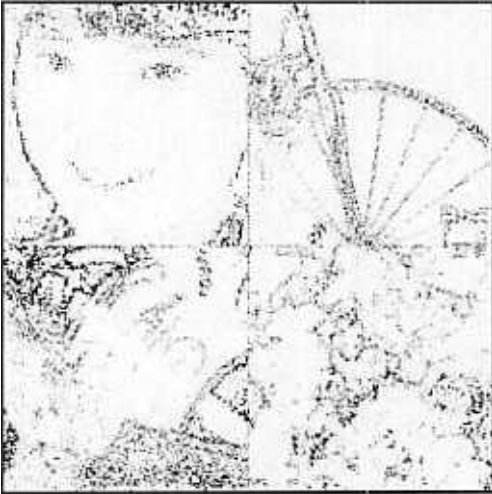
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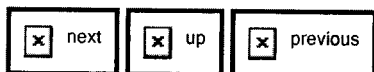
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## Combined Distortion Map (DM4 , DM5)



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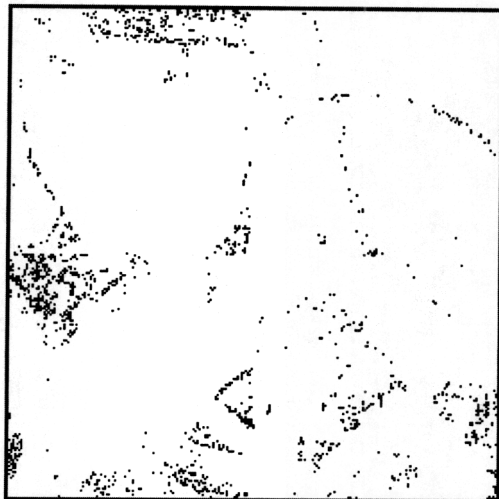
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## Distortion Map with Threshold(DM4, DM5



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## Image Feature Used in the Experiments



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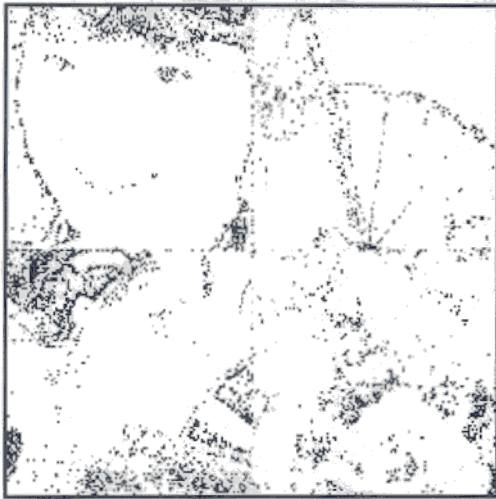
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## Combined Distortion Map with Sigmoid



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