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CENTRIFUGE MODELING OF SOIL-STRUCTURE INTERACTION IN ENERGY FOUNDATIONS

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Abstract: This study presents a centrifuge modeling approach to characterize the transient thermo-mechanical response of energy foundations during heating-cooling cycles in order to provide data for calibration and validation of soil-structure interaction models. This study focuses on the response of a scale-model energy foundation installed in an unsaturated silt layer with end-bearing boundary conditions. The foundation response was assessed using embedded strain gages and thermocouples. Other variables monitored include foundation head displacements, soil surface displacements, and changes in temperature and volumetric water content in the unsaturated silt at different depths and radial locations. Measurements during the initial heating process indicate that the thermal axial stress is greater near the toe of the foundation due to the restraint associated with mobilization of side shear resistance along the length of the foundation. The thermal axial strains were close to the free-expansion thermal strain near the soil surface and decreased with depth. The thermal axial displacements calculated by integrating the thermal axial strains correspond well with the independently-measured head displacements. The mobilized side stresses calculated from the thermal axial stresses increased with height and were consistent with the shear strength of unsaturated silt. During successive heating-cooling cycles, slight decreases in upward thermal head displacement were observed due to changes in stiffness of the unsaturated soil due to thermally-induced water flow away from the foundation and potential down-drag effects. However, little change in the thermal axial stress was observed during the heating-cooling cycles.

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23 INTRODUCTION

24 Energy foundations, or drilled-shaft foundations that incorporate heat exchange elements,
25 provide necessary structural support for buildings and act as heat sources or sinks for building
26 heating and cooling systems using the same construction materials (Brandl 1998; Ennigkeit and
27 Katzenbach 2001; Laloui et al. 2003; Brandl 2006). Energy foundations are a practical strategy
28 to reduce the installation cost of ground-source heat exchange systems, which has been identified
29 as one of the major barriers to implementation of this energy efficiency technology (Hughes
30 2008). However, an issue that should be carefully characterized is the potential for foundation
31 movements due to thermal expansion and contraction of the foundation element or surrounding
32 soil. Further, soil-structure interaction may restrain foundation movements, leading to generation
33 of thermally induced stresses. The mechanisms of thermo-mechanical soil-structure interaction
34 have been documented in several full-scale case histories in the field (Laloui et al. 2006; Bourne-
35 Webb et al. 2009; Laloui 2011; Bouazza et al. 2011; Amatya et al. 2012; McCartney and Murphy
36 2012). In addition, thermo-mechanical soil-structure interaction analyses (Knellwolf et al. 2011)
37 and thermo-elastic finite element analyses (Laloui et al 2006; Regueiro et al. 2012) have been
38 developed that permit prediction of changes in axial displacement, strain, and stress in energy
39 foundations during heating and cooling. The different analyses require empirical data for
40 calibration of parameters and verification of predictions, which can often be difficult to obtain
41 from full-scale case histories due to uncertain soil stratigraphy effects, varying foundation
42 geometries, uncertain installation effects, and complex end-restraint boundary conditions.

43 The experience obtained from full-scale energy foundation studies can be complemented
44 with the characterization of scale-model energy foundations in a geotechnical centrifuge to
45 measure empirical parameters for soil-structure interaction analyses in carefully controlled

46 conditions, or to develop a database of information for validation of analyses. In centrifuge
47 modeling tests, the properties of scale-model foundations and soil layers can be carefully
48 controlled and different configurations can be considered for lower costs than full-scale testing in
49 the field. Centrifuge modeling also permits incorporation of dense instrumentation arrays to
50 capture thermo-mechanical effects in the energy foundation as well as thermo-hydro-mechanical
51 effects in the surrounding soil, both of which are necessary to validate predictions from finite
52 element analyses. Centrifuge modeling may be especially relevant when considering the
53 behavior of energy foundations in some soil deposits that may have nonlinear behavior, such as
54 soft clays or unsaturated soils. An advantage of centrifuge modeling over full-scale foundation
55 testing is that scale-model energy foundations can be loaded to failure to destructively
56 characterize the effects of temperature on the load-settlement curve and the back-calculated
57 ultimate side shear resistance and end bearing (McCartney and Rosenberg 2011). McCartney and
58 Rosenberg (2011) observed an increase in the ultimate capacity of energy foundations with
59 increasing temperature, which was proposed to be due to an increase in side shear resistance
60 resulting from differential lateral expansion of the energy foundation into the surrounding soil.

61 The objective of this study is to present a centrifuge modeling approach to quantify the
62 thermo-mechanical soil-structure interaction behavior of a centrifuge-scale energy foundation
63 installed in an unsaturated silt layer during cyclic heating and cooling. The energy foundation
64 considered in this study has an end-bearing boundary condition, in which the tip of the
65 foundation is resting on a rigid layer, and contains embedded strain gages and thermocouples to
66 measure distributions in strain and temperature. The head of the foundation is permitted to
67 expand freely under a constant applied load. These conditions represent a typical energy
68 foundation installed beneath a light structure. Results from this test, as well as others following

69 the same approach, can be used to understand the role of energy foundation end-restraint
70 boundary conditions on the magnitude and distribution of thermally induced axial strains,
71 displacements, and stresses. Further, the results can be used to delineate the advantages and
72 limitations of using centrifuge physical modeling to study thermo-mechanical soil-structure
73 interaction problems in energy foundations.

74 **BACKGROUND**

75 **Soil-Structure Interaction in Energy Foundations**

76 As an energy foundation is heated or cooled, it may expand or contract, respectively,
77 depending on the restraint boundary conditions. For unconstrained conditions, the thermal axial
78 strain can be calculated as follows:

$$\varepsilon_{T,unconstrained} = \alpha_c \Delta T \quad (1)$$

79 where α_c is the coefficient of linear thermal expansion of reinforced concrete, and ΔT is the
80 change in temperature. Thermal strain is defined as positive for compression to be consistent
81 with geotechnical conventions. Accordingly, α_c for reinforced concrete will be negative as
82 structural elements expand during heating (positive ΔT). The coefficient of linear thermal
83 expansion of unreinforced concrete ranges from 9 to -14.5 $\mu\varepsilon/^\circ\text{C}$ depending on the aggregate
84 mineralogy, while that of the steel reinforcements is approximately -11.9 to -13 $\mu\varepsilon/^\circ\text{C}$ (Bourne-
85 Webb et al. 2009; Stewart 2012). Because these values are relatively similar, significant
86 differential thermal strains are not expected in reinforced concrete. The value of $\varepsilon_{T,unconstrained}$ is
87 an upper limit on the thermal axial strains that can occur in the reinforced concrete due to heating
88 or cooling. If the energy foundation were fully constrained by the end-restraint boundary
89 conditions or the mobilized side shear resistance, the thermal axial strain would be zero. In this

90 case, the change in temperature of the energy foundation would generate the maximum value of
91 thermal axial stress $\sigma_{T,constrained}$, which can be calculated as follows:

$$\sigma_{T,constrained} = -E\alpha_c\Delta T \quad (2)$$

92 where E is the Young's modulus of the reinforced concrete. The boundary conditions for energy
93 foundations are likely between unconstrained and constrained conditions, due to soil-structure
94 interaction and the finite stiffness restraint of an overlying structure. The thermal axial strains ε_T
95 in energy foundations will be between the free expansion and fully constrained limit states. In
96 this case, the thermal axial stresses σ_T induced during a change in temperature can be calculated
97 as follows:

$$\sigma_T = E(\varepsilon_T - \alpha_c\Delta T) \quad (3)$$

98 During heating, the thermal axial strains in the energy foundation will be negative (expansive)
99 and less than $\varepsilon_{T,unconstrained}$, so the thermal will be positive (compressive). For energy foundations
100 embedded in soil or rock, the side shear resistance, end bearing, and stiffness restraint of the
101 overlying building will lead to different distributions in thermal axial stresses and strains.

102 Several full-scale tests have used different approaches to evaluate the distributions in thermal
103 axial strain and stress in energy foundations. Laloui et al. (2006), Laloui and Nuth (2006),
104 Bourne-Webb et al. (2009), Laloui (2011), and Amatya et al. (2012) evaluated the stresses and
105 strains in full-scale energy foundations loaded axial from the surface using a load frame for
106 different temperature changes. Bouazza et al. (2011) and Wang et al. (2012) used a combination
107 of Osterberg cells embedded in an energy foundation to translate a section of the shaft upward
108 and downward to characterize changes in side shear resistance with temperature. McCartney and
109 Murphy (2012) evaluated the stresses and strains in full-scale energy foundations installed
110 beneath a building during typical heat pump operations, which incorporates actual head end-

111 restraint boundary conditions. The current study follows the first approach, in which the energy
112 foundation is heated and cooled back to ambient temperature within a load frame.

113 Bourne-Webb et al. (2009) proposed hypothetical representations of the mechanisms of
114 thermo-mechanical soil-structure interaction in “floating” energy foundations that have no end
115 bearing, and Amatya et al. (2012) extended these representations to cases with non-zero end-
116 bearing (semi-floating and end-bearing conditions). In these hypotheses, a floating foundation is
117 expected to expand about its center during uniform heating, an end-bearing foundation is expected
118 to expand upward from the base, and a semi-floating foundation is expected to have an
119 intermediate response. Knellwolf et al. (2011) referred to the point of zero thermal axial
120 displacement in the foundation as the null point, and noted that this is an important parameter in
121 thermo-mechanical soil-structure interaction analyses. The hypothetical representations of soil-
122 structure interaction mechanisms are useful when evaluating field measurements and the results
123 from analyses, especially when differentiating the effects of temperature from those of
124 mechanical loading on the distributions in axial stress and side shear resistance. Although the
125 results from full-scale tests generally confirm the hypothetical representations, centrifuge
126 modeling permits isolation of the effects of complex end-restraint boundary conditions, different
127 side shear resistance mechanisms (frictional vs. cohesive), issues such as thermal dragdown of
128 surrounding soils.

129 **Centrifuge Modeling of Energy Foundations**

130 Centrifuge modeling relies on the concept of geometric similitude, which assumes that a full-
131 scale prototype soil layer will have the same stress state as a model-scale soil layer that is N
132 times smaller when spinning in a geotechnical centrifuge at a centripetal acceleration that is N
133 times larger than that of earth’s gravity (Ko 1988; Taylor 1995). The centripetal acceleration

134 generates increased body forces in the scale-model. Geometric similitude can be employed to
135 extrapolate the load-settlement behavior and thermal soil-structure interaction phenomena of
136 scale-model energy foundations to those representative of full-scale prototype foundations in the
137 real world. After scaling the length of the foundation by a factor of 1:N (model:prototype),
138 strains in the foundation scale by a factor of 1:1, and forces scale by a factor of 1:N² (Ko 1988;
139 Taylor 1995).

140 One issue in modeling energy foundations is that the temperature does not depend on the
141 increased body forces in the centrifuge. Spatial measurements of temperature in dry quartz sand
142 surrounding a cylindrical heat source during centrifugation at different g-levels by Krishnaiah
143 and Singh (2004) confirm that centrifugation does not lead to a change in the heat flow process.
144 However, if the dimensions associated with the spatial distribution of heat flow were scaled from
145 model to prototype scale (assuming the same thermal conductivity in both cases), the time
146 required for heat flow by conduction would be N² times faster in the centrifuge model (1:N²).

147 Savidou (1988) derived the scaling factor for the time required for heat flow for the case of
148 one-dimensional heat conduction in Cartesian coordinates using the diffusion equation, which
149 only involved scaling of the length. The same scaling factor of N² observed by Krishnaiah and
150 Singh (2004) was obtained. An implication of geometric similitude is that a greater volume of
151 soil surrounding the model-scale foundation will be affected by changes in temperature in a
152 given period of time than in a full-scale prototype. As soils change in volume with temperature, a
153 greater zone of soil around the foundation will be affected. Accordingly, the effects of
154 differential volume change of the foundation and soil may be emphasized in a centrifuge
155 modeling test. From this perspective, centrifuge modeling may provide a worst-case scenario for

156 temperature effects on soils surrounding an energy foundation, especially after reaching steady-
157 state conditions.

158 One solution to address the scaling conflict is to calibrate numerical finite element
159 simulations of the tests using the model-scale measurements. However, the experimental
160 approach can be modified depending on the goals of the test so that the prototype results can be
161 used for calibration of simple load-transfer analyses. If the goal of testing is to evaluate the
162 impact of temperature on the load-settlement curve of the foundations considering the role of the
163 surrounding soil, time should be provided to reach steady-state conditions. This is the only
164 approach that should be used for soft soils that experience plastic volume changes during
165 heating. This would provide a worst-case scenario as both the foundation and soil may
166 experience thermo-mechanical deformations that may affect soil-structure interaction. However,
167 as it may take a significant amount of time to reach steady-state conditions, this approach may
168 not be practical in centrifuge testing. An alternative that could be used when evaluating the
169 behavior of energy foundations in stiff soils or dry sands would be to wait until the foundation
170 reaches a steady temperature. In this case the load-settlement curve would only be representative
171 of transient conditions. Although this may not fully capture the effects of the soil on soil-
172 structure interaction, the behavior of energy foundation during transient heating and cooling is
173 still relevant as full-scale energy foundations often experience temperature reversals (McCartney
174 and Murphy 2012). Rosenberg (2010) measured the load-settlement curves of energy
175 foundations in compacted silt after the foundation reached a steady-state temperature, even
176 though the surrounding silt did not fully reach steady-state conditions, especially at a distance of
177 several foundation diameters away. When evaluating the impact of temperature on the thermal
178 axial strain distribution in energy foundation in stiff soils, tests can be performed until the

179 thermal axial strains within the foundation stabilize while its temperature is held constant. This
180 was the intention of the approach followed in this study to evaluate changes in foundation
181 behavior during transient changes in temperature over a short period of time.

182 **MATERIALS**

183 **Scale-Model Energy Foundation**

184 A scale-model energy foundation having a length of 533 mm and a diameter of 50.8 mm was
185 constructed for this study. When the foundation is installed in the centrifuge container used in
186 this study, which can accommodate a 533 mm-thick soil layer, its tip rests on the base of the
187 container, so it is referred to as an end-bearing foundation. A centrifuge acceleration of 24 was
188 used in this study, so the corresponding prototype-scale foundation length is 12.8 m with a
189 diameter of 1.22 m. A schematic cross-sectional view of the foundation is shown in Figure 1.

190 Although drilled shafts are typically cast in place in soil, the model energy foundation was
191 precast outside of the soil layer due to the large amount of instrumentation, cables, and heat
192 exchanger tubing within the assembly. The pre-cast foundation can also be reused in subsequent
193 tests, and can be tested outside of the soil layer to characterize its thermal and mechanical
194 properties. The reinforcing cages for the model foundation was constructed from a hoop of steel
195 wire mesh having a uniform opening size of 6.35 mm and a diameter of 40 mm. A cardboard
196 tube having an inside diameter of 50.8 mm was used as a form for the foundation, permitting a
197 concrete cover of 5 mm on the sides and 12.7 mm on the top and bottom. Cable stays (zip ties)
198 were used to provide spacing between the reinforcing cage and the cardboard tube.

199 Three heat exchanger loops (3 inlets and 3 outlets) were installed in the foundation so that the
200 distribution of heat across the circumference of the foundation would be as uniform as possible.
201 Perfluoroalkoxy (PFA) heat exchanger tubes having an inside diameter of 3.175 mm were used

202 because they can accommodate high fluid pressures under high temperatures (830 kPa at 65°C)
203 while remaining flexible. The inlet and outlet branches of each tubing loop were attached on the
204 inside of the reinforcing cages, approximately opposite from each other. At the bottom of the
205 foundation, the loops of tubing were pulled to the inside perimeter of the reinforcing cage to
206 avoid segregation of concrete during placement and to ensure that the center of the foundation
207 would be monolithic concrete.

208 Embedded strain gages and thermocouples were attached to the inside of the reinforcing cage
209 of the model foundation at the locations shown in Figure 1, with two gages at each depth on
210 opposite sides of the foundation. The strain gages used in this study were model CEA-13-
211 250UW-350 obtained from Vishay Precision Group. These particular gages were selected
212 because their coefficient of thermal expansion is similar to that of steel, and because they are
213 designed to have a stable response during cyclic heating, considering gage resilience and error
214 due to variations in temperature (Vishay Precision Group, personal communication 2011). The
215 gages were first attached with temperature resistant M-Bond AE-15 adhesive to 30 mm-long
216 steel tabs having a dog-bone shape with a hole punched at either end. This adhesive is cured at
217 an elevated temperature of 85 °C, which makes it less likely to slip during cyclic heating than
218 other adhesives that cure at room temperature. The gage was then covered with Teflon tape and
219 the central part of the tab containing the gage was coated with M-Coat J, which is a flexible
220 coating that protects against most fluids and mechanical damage during insulation. The steel tabs
221 were then attached to the inside of the reinforcing cage. Near the top of the foundation, the strain
222 gage leads were connected to a cable with shielded, twisted wire pairs to minimize the potential
223 effects of electrical noise associated with the loading system. Miniature thermocouples (Omega
224 fine wire Type K Model STC-TT-K-36 3C) were embedded within the foundation at the same

225 depths as the strain gages on one side of the foundation. The thermocouples were placed in
226 contact with the steel tabs.

227 After centering of the reinforcing cage (with the heat exchanger tubing and instrumentation
228 attached) within the cardboard mold, concrete having a mix ratio of 1:1.7:2.3:1
229 (water:cement:fine-aggregate:coarse-aggregate) was poured into the mold. No admixtures were
230 included. The fine aggregate was conventional concrete sand, while the coarse aggregate was
231 gravel having a maximum particle size less than 6 mm. The relatively large fraction of sand and
232 the smaller size of the coarse aggregate is expected to lead to a softer response than the concrete
233 used in full-scale drilled shafts, but this was necessary so that the concrete could flow around the
234 instrumentation in the small-diameter foundation and through the openings in the reinforcing
235 cage. After thorough mixing, the concrete was poured into the cardboard tube atop a shake table,
236 and a rod was used to ensure even distribution of aggregates. The completed reinforced concrete
237 foundation was placed in a curing room for 15 days, after which the cardboard tubing was
238 removed. Most of the concrete strength gain was expected over this time in the curing room,
239 although the foundation as not tested in the centrifuge until more than a month after construction.

240 A comprehensive set of characterization tests were performed on the pre-cast foundation to
241 determine the mechanical and thermal properties of the reinforced concrete, the detailed results
242 of which are presented in Stewart (2012). The first test involved application of incremental axial
243 loads under room temperature conditions, taking care to properly level the foundation and center
244 the load to avoid bending. The mechanical strains measured during application of an axial load
245 of 700 kPa were variable, but gage-specific calibration factors were defined using the overall
246 axial deformation of the foundation measured using a linearly-variable deformation transformer
247 (LVDT). Tests were repeated to ensure that the variability was not due to seating conditions, and

248 care was taken to minimize the potential for bending. The Young's modulus determined using
249 the corrected strain data was 7.17 GPa. As expected, this value is lower than that of reinforced
250 concrete used in full-scale energy foundations (~30 GPa) because of the lower fraction of coarse
251 aggregate.

252 The energy foundation was then heated to a temperature of 62 °C by circulating fluid through
253 the heat exchange tubes within the foundation while maintaining a constant axial stress of
254 439 kPa. The foundation was permitted to expand freely under this axial stress, permitting
255 definition of the coefficient of linear thermal expansion of the foundation using the LVDT. The
256 value of α_c calculated from the LVDT measurements was found to be $-7.5 \mu\epsilon/^\circ\text{C}$, where $\mu\epsilon$ is
257 micro-strain ($\text{m/m} \times 10^6$), with compressive strain defined as positive. Although the temperature
258 of each of the gages was within 2 °C during the heating test, the thermal response of each strain
259 gage was different, likely due to differences in curing of the adhesive bonding the strain gage to
260 the steel tab, or due to differential thermal expansion of the gage, adhesive, and the steel tab.
261 However, because the thermal axial strain should theoretically be the same at each location along
262 the length of the foundation for free expansion, thermal correction factors were defined using the
263 reading from the LVDT and the gage specific temperature. The thermal correction developed in
264 a subsequent study by Goode (2013) was used to reinterpret the strains reported by Stewart
265 (2012). Before application of the thermal correction factors, the gages were corrected for the
266 thermal offset error specific to this batch of gages and for differential expansion of the steel tabs
267 ($\alpha_s = -8.5 \mu\epsilon/^\circ\text{C}$) and concrete which was assumed to be the same as the foundation overall
268 ($\alpha_c = -7.5 \mu\epsilon/^\circ\text{C}$).

269

270 **Soil**

271 Soil obtained from the Bonny dam near the Colorado-Kansas border was used in the energy
272 foundation test in this study. Relevant geotechnical properties of Bonny silt are summarized in
273 Table 1, and additional information on the compaction curve, shear strength, soil-water retention
274 curve, and shear modulus can be obtained from Stewart (2012). The liquid and plastic limits of
275 the soil measured according to ASTM D 4318 are 26 and 24, and the fines content of this soil is
276 84%, so this soil classifies as ML (inorganic silt) according to the Unified Soil Classification
277 System (USCS). The silt has a specific gravity G_s of 2.6. The reasons for using this soil in this
278 study are that it has low plasticity, so temperature is not expected to lead to changes in soil-pore
279 water interactions (i.e., diffuse double layer effects). Further, it has a high fines content so the silt
280 will behave like a low-permeability material where thermal consolidation may occur.

281 Although a wider suite of soil preparation and saturation conditions are currently under
282 investigation, the tests performed in this study involve a soil layer prepared using compaction to
283 permit fast model preparation times and to reach uniform initial unit weight and water content
284 distributions with height at the beginning of the tests. Further, compaction was expected to lead
285 to a stiff soil response that would not lead to significant long-term settlement under the change in
286 stress associated with centrifuge testing. The soil layer was prepared by compacting silt having a
287 gravimetric water content of 14% in 76.2 mm-thick lifts around the foundation to reach a target
288 dry density of 1451 kg/m^3 . A vibratory hammer with a flat-plate adaptor having a width of
289 75 mm was used to compact the soil around the foundation to reach lifts with a final thickness of
290 75 mm. The centrifuge test was performed on the soil layer in as-compacted (unsaturated)
291 conditions.

292 **EXPERIMENTAL SETUP**

293 **Container and Load Control System**

294 A schematic of the container used in this study to evaluate the thermo-mechanical strain
295 distributions in the end-bearing energy foundation is shown in Figure 2. The container is a
296 cylindrical aluminum tank with an inside diameter of 0.6 m, wall thickness of 13 mm, and a
297 height of 0.54 m. A 13 mm-thick insulation sheet was wrapped around the container to prevent
298 heat transfer through the sides of the cylinder (no-flow boundary). The bottom of the container
299 permits some loss of heat, but it was preferred not to install insulation beneath the container to
300 provide a stiff platform for loading. All sides of the container are impermeable, and post-test
301 analysis of gravimetric water content values and measurements from embedded water content
302 sensors indicated very little change in soil water content except near the foundation. The load
303 frame consists of two steel frames mounted atop a rectangular steel platform. A horizontal
304 brushed DC electric motor mounted between the steel frames is used to apply vertical loads to
305 the top of the foundation through a coupling to a vertical worm drive. The applied load was
306 measured using a load cell attached to the shaft of the worm drive, and a force-feedback control
307 loop implemented using a National Instruments motor control module was used to maintain a
308 constant axial load during testing. Additional pictures of the container and load frame are shown
309 in Stewart (2012).

310 **Soil Instrumentation**

311 The locations of instrumentation incorporated into the centrifuge container are shown in
312 Figure 2. An LVDT was placed on top of the foundation and three others were placed on the soil
313 surface at different radial distances from the foundation. The LVDTs were mounted on cantilever
314 arms connected to a support beam across the top of the container. The LVDTs, each having a

315 range of ± 12.7 mm, were used to measure the self-weight settlement of the soil layer as well as a
316 potential settlement basin created by movement of the foundation in the soil. The LVDT
317 readings reported by Stewart (2012) were corrected to account for the change in the ambient
318 temperature of the centrifuge chamber. Goode (2013) observed that the ambient temperature of
319 the centrifuge led to a phantom model-scale settlement in mm of $0.0246\Delta T_{\text{ambient}}$, where $\Delta T_{\text{ambient}}$
320 is the change in temperature of the centrifuge chamber from the beginning of the test.

321 Four thermocouple profile probes equipped with six thermocouples at different locations
322 along the probe were inserted into the soil at different radial locations from the foundation. The
323 probes were passed through the support beam and were used to measure transient changes in
324 temperature of the soil surrounding the foundation to assess heat transfer processes. Dielectric
325 sensors (model EC-TM from Decagon Devices), capable of inferring the volumetric water
326 content and temperature of the soil, were placed in the soil layer during compaction in a vertical
327 array 50.8 mm away from the foundation at different depths, and in a horizontal array at a depth
328 of 266.7 mm. These sensors were useful in monitoring thermally induced water flow in the
329 unsaturated soil layer away from the foundation, and provided a backup measurement of soil
330 temperatures.

331 **Foundation Temperature Control System**

332 The temperature control system used in this study was developed so that the energy
333 foundation would reach a desired value. A heat pump, operated outside the centrifuge, was used
334 to control the temperature of fluid circulating through the scale-model foundation. The F25-ME
335 refrigerated/heated circulator manufactured by Julabo, Inc. was connected to the foundation via
336 the hydraulic slip ring stack as shown in Figure 3. The heat pump consists of an automated
337 temperature control system and circulating pump, with a working temperature range of -28 to

338 200 °C. The circulating pump can supply a pressure up to 38 kPa and a flow rate up to 16 l/min.
339 An in-line high-capacity cartridge flow pump was attached to the inflow line to double the flow
340 rate, which is important to ensure turbulent flow conditions in the heat exchange tubing and to
341 overcome potential friction losses through the slip ring stack. Pure ethylene glycol was used as
342 the heat exchange fluid because it could be safely circulated through the hydraulic slip rings of
343 the centrifuge, which are intended for oil-based fluids only. The ethylene glycol has a thermal
344 conductivity of 0.258 W/m°C and a viscosity ranging from 0.1 to 3.8 cP for temperatures from
345 30 to 71 °C. The foundation flow valve and bypass flow valve shown in Figure 3 are critical
346 components used to control the temperature of the foundation. In order to pre-heat the ethylene
347 glycol, the bypass valve was opened while the foundation flow valve was closed. This permitted
348 the fluid in the supply and return lines to reach a steady-state temperature. The foundation and
349 bypass flow valves were opened or closed in increments using LabView machine control
350 software, which supplied varying flow rates of pre-heated fluid to the foundation. The
351 temperatures of the fluid entering and exiting the foundation are monitored using pipe-plug
352 thermocouples, as these temperatures permit evaluation of the heat energy input into the
353 foundation. The average flow rate of the ethylene glycol during testing at elevated temperatures
354 was 5 ml/s.

355 **EXPERIMENTAL PROCEDURES**

356 After assembly of the container within the load frame on the centrifuge basket, the centrifuge
357 was spun to a target centripetal acceleration of 24 g's (defined at the center of the container).
358 After the LVDTs on the foundation indicated that it was at equilibrium, a prototype-scale axial
359 load of 443 kN (axial stress of 384 kPa) was applied to the end-bearing foundation to simulate a

360 constant building load. Because load-control conditions were employed, the top of the
361 foundation was free to deform upward or downward during cyclic heating.

362 After the foundation settlement due to application of the building load ceased, the foundation
363 was heated in increments. The inlet and outlet fluid temperatures (at the point the fluid enters and
364 exits the foundation) during this process are shown in Figures 4(a), along with the ambient air
365 temperature of the soil surface. The difference in inlet and outlet fluid temperatures reflects the
366 heat shed from the fluid into the foundation and surrounding soil, but these temperatures are
367 otherwise not important to consider as they fluctuated frequently to maintain a constant
368 foundation temperature. The ambient temperature was relatively steady during testing, showing a
369 temperature rise of less than 4 °C due to the friction of the centrifuge moving through the air in
370 the centrifuge chamber. The temperatures at different depths in the end-bearing foundation
371 measured using the embedded thermocouples are shown in Figure 4(b). Different from the fluid
372 temperatures, the foundation temperature is relatively stable as the temperature was stepped up in
373 increments to 39°C. The thermocouples at the top and bottom of the foundation show slightly
374 lower temperatures than those in the center of the foundation due to higher heat flow through the
375 steel base and because of the surface boundary conditions. Nonetheless, the temperature along
376 the length of the foundation is relatively uniform. After reaching a temperature of 39 °C, the
377 foundation was cooled back to ambient temperature, then reheated in four cycles.

378 **EXPERIMENTAL RESULTS**

379 Comparisons of the average foundation temperature and the temperatures in the middle of the
380 soil layer at different radial locations are show in Figure 4(c). The temperatures of the soil,
381 measured by the thermocouple profile probes in the case of the end-bearing foundation lag
382 behind the foundation temperatures due to the heat flow process. Further, they do not reach the

383 same magnitude of temperature as that of the foundation, even at a radial distance of 50.8 mm
384 from the foundation. During the time that the foundation experienced changes in temperature of
385 19 °C, the soil experienced a maximum increase in temperature of approximately 5 °C. This
386 small change in temperature may still have led to thermo-mechanical deformations of the silt.
387 Uchaipichat and Khalili (2009) characterized the isotropic thermal volume change of compacted
388 silt, and observed a transition in behavior from elastic expansion to plastic contraction during
389 heating of compacted silt between net stresses of 100 and 150 kPa. Accordingly, for the stress-
390 state in this study (average vertical net stress of approximately 120 kPa), the compacted silt may
391 show either thermal expansion or contraction depending on the depth.

392 A time series of the axial stress applied to the head of the end-bearing foundation is shown in
393 Figure 5(a), along with the average foundation temperature. Although a feedback loop was used
394 to control the axial load, the system is particularly stiff, so minor vibrations occasionally led to
395 instability. There were two occasions when the system became unstable and applied stresses
396 greater than the target value. However, the head displacements and the thermal axial strains
397 shown in Figures 5(b) and 5(c), respectively, indicate that the temporary increase in axial stress
398 led to elastic mechanical deformations of the foundation and did not have a major impact on the
399 thermal expansion of the foundation at the end of each heating phase. The prototype head
400 displacement in Figure 5(b) was calculated by zeroing the model-scale head displacement at the
401 end of spin-up and multiplying the scale factor of 24. The thermal head displacement was then
402 calculated by zeroing the prototype head displacement at the start of the heating stages. As
403 expected, the prototype head displacements indicate downward (positive) head movement during
404 application of the mechanical load, and an upward head movement during heating. The
405 foundation did not return to its original location during cooling as it was not cooled back to

406 ambient temperature. During successive heating cycles, a slight decrease in the amount of
407 upward head movement was observed.

408 The measurements from the LVDT on the soil surface at a model-scale distance of 76.2 mm
409 are also shown in Figure 5(c). Although not shown, the soil surface experienced an elastic
410 model-scale settlement of 0.48 mm during spin-up of the centrifuge. Over the course of the test,
411 an additional model-scale soil surface settlement of 0.19 mm occurred, corresponding to the
412 4.5 mm of prototype-scale soil surface settlement shown in Figure 5(c). This corresponds to a
413 vertical strain of 0.14%. The soil surface settlement does not appear to be correlated to the
414 temperature changes in the energy foundation. Nonetheless, the differential settlement between
415 the foundation and soil may have led to drag-down effects that may partially explain the slight
416 decrease in axial expansion during the heating stages.

417 The thermal axial strains were defined by zeroing the strain readings at the beginning of
418 heating and applying the thermal correction factors obtained from 1-g tests. The mechanical axial
419 strains for both foundations are reported by Stewart (2012), and are not included here because
420 their magnitude was insufficient to draw conclusions as to the distribution in side shear
421 resistance due to mechanical loading. The thermal axial strains indicate consistently negative
422 (expansive) strains in the foundation during heating which followed the same trends as the
423 imposed temperatures, even during heating cycles, as the foundation was never cooled below the
424 initial ambient temperature. The magnitude of the thermal axial strains were consistently lower
425 than the free expansion strain of the foundation $\varepsilon_{T,unconstrained}$ defined using Eq. (1).

426 The changes in volumetric water content at different depths in the soil layer at a model-scale
427 radial location of 50.8 mm are shown in Figure 5(d). The results in this figure indicate that
428 shortly after heating started, the soil adjacent to the foundation started to become wetter as water

429 is driven away from the foundation, with greater water flow near the top of the foundation. The
430 maximum increase in volumetric water content of $0.02 \text{ m}^3/\text{m}^3$ corresponds to an increase in
431 degree of saturation from 0.59 to 0.64. It is reasonable to assume that the soil closest to the
432 foundation decreased in volumetric water content by a similar amount, leading to a decrease in
433 degree of saturation from 0.59 to 0.54. The drying process of the soil closest to the foundation
434 will lead to an increase in effective stress, leading to an increase in ultimate side shear resistance.

435 **ANALYSIS OF RESULTS**

436 The thermal axial strains were synthesized to define profiles with height for different changes
437 in temperature during the initial heating stages, as shown in Figure 6(a). In general, the largest
438 thermal axial strains are observed near the top of the foundation, as the foundation is able to
439 expand freely as the axial stress was applied in load-control conditions. The thermal axial strains
440 at the top of the foundation (depth of zero) in this figure were calculated using the value of α_c for
441 the reinforced concrete, while the rest of the thermal axial strain values were obtained from the
442 measurements in Figure 5(c). The smallest thermal axial strain in the end-bearing foundation was
443 observed near the bottom of the foundation, which reflects greater constraint of foundation
444 movement. This is possibly due to the higher lateral stresses in the soil at the base of the
445 foundation.

446 Assuming that the thermal axial displacement was zero at the base of the container, which is
447 reasonable due to the relatively rigid base, the thermal axial strains were integrated over the
448 length of the foundation to define the thermal axial displacement at different depths, as follows:

$$\delta_{T,i} = \delta_{T,i-1} + \frac{1}{2}(\varepsilon_{T,i-1} + \varepsilon_{T,i})\Delta l \quad (4)$$

449 where $\delta_{T,i}$ is the thermal axial displacement at the midpoint between two gages at different
450 depths, $\varepsilon_{T,i}$ is the thermal axial strain at gauge i , and Δl is the distance between two gages. The

451 thermal axial displacement profiles calculated using Eq. (4) are shown in Figure 6(b), along with
452 the thermal head displacements from Figure 5(b) at a depth of zero. The thermal axial
453 displacement profiles obtained from the strain gages correspond reasonably well with the
454 measured thermal head movement, indicating a nonlinear increase in thermal axial displacement
455 with height. As mentioned, the location of the smallest thermal axial displacement is referred to
456 as the null-point (Knellwolf et al. 2011), which represents the point about which the foundation
457 expands during heating. The location of the smallest thermal axial displacement in the end-
458 bearing foundation is located at the bottom of the foundation, as expected from the hypothetical
459 representations of soil-structure interaction proposed by Amatya et al. (2012).

460 Thermal axial stress profiles for the end-bearing foundation calculated using Eq. (3) are
461 shown in Figure 6(c). The greatest thermal axial stresses in the end-bearing foundation occur
462 near the base of the foundation, slightly above the location of the null-point. The nonlinear
463 change in stress with depth is due to the mobilized side shear stresses at the silt-foundation
464 interface, which may also be affected by the increased radial stresses during heating (McCartney
465 and Rosenberg 2011). The compacted silt is relatively stiff, and has a uniform density along the
466 length of the foundation. Some drainage may have occurred during centrifugation and heating,
467 making the soil near the toe have a greater undrained shear strength. In a natural soil deposit, it
468 would be expected that drained conditions would occur, leading to a distribution in side shear
469 resistance following the shape of the effective stress distribution in the soil layer. Nonetheless,
470 the thermal stress distributions in the scale-model foundation corresponds well with those
471 observed in field tests on end-bearing foundations by Laloui et al. (2006), Bourne-Webb et al.
472 (2009), and McCartney and Murphy (2012). These observations confirm the utility of centrifuge

473 modeling in defining soil-structure interaction data during transient temperature changes that can
474 be used to calibrate and validate numerical analyses.

475 The mobilized side shear stresses at different depths can be calculated without the use of a
476 load-transfer analysis because the head of the energy foundation was permitted to freely expand
477 during heating. This would not have been the case if the energy foundation were restrained by
478 the stiffness of an overlying structure, as the thermal axial stress at the foundation head would
479 not be zero (Knellwolf et al. 2011). For the case of zero thermal axial stress at the head of the
480 foundation, the mobilized side shear stress $f_{s,mob}$ can be calculated as follows:

$$f_{s,mob,j} = \frac{(\sigma_{T,j-1} - \sigma_{T,j})D}{4\Delta l} \quad (5)$$

481 where j is a counter from the top of the foundation, D is diameter of the foundation, and Δl is the
482 distance between two locations of known thermal axial stress. The distribution in mobilized side
483 shear stress with height calculated from the thermal axial stresses in Figure 6(c) is shown in
484 Figure 7(a). The maximum mobilized side shear stress is less than the shear strength expected for
485 unsaturated silt (Uchaipichat and Khalili 2009), and the mobilized side shear stress increases
486 with height consistent with the strain distribution within the energy foundation during heating.
487 The total mobilized side shear forces calculated by integrating the profiles of mobilized side
488 shear stress in Figure 7(a) are shown in Figure 7(b) as a function of the change in temperature.
489 The total mobilized side shear force is downward and negative, but is shown as a positive value
490 in this figure. As expected, the total mobilized side shear force increases approximately linearly
491 with increasing changes in temperature. The total mobilized side shear force should be equal and
492 opposite to the end bearing of the foundation to ensure external equilibrium. It is important to
493 note that the end bearing due to heating of the foundation should be less than or equal to the
494 maximum thermal axial stress for fully constrained conditions calculated using Equation (2). The

495 maximum thermal axial stress for each change in temperature is also shown in Figure 7(b), and
496 except in the first two heating increments where the thermal axial stress profile does not
497 monotonically increase with depth due to strain gage variability, the total mobilized side shear
498 force is less than the maximum possible thermal axial stress.

499 Profiles of the thermal axial strain, displacement, and stress after each of heating and cooling
500 cycles are shown in Figures 8(a), 8(b), and 8(c), respectively. During cooling from 39 to 30 °C,
501 negative, expansive strains are still present in the foundation. The thermal axial strain near the
502 head of the foundation decreases by a greater amount than deeper in the soil layer. The
503 theoretical free-expansion thermal axial strain values calculated using Eq. (1) are shown in
504 Figure 8(a) at a depth of 0 m, and they correspond well with the measured thermal axial strain
505 values. The thermal axial displacements in the energy foundation do not change significantly
506 except at the head of the foundation, and the thermal head displacements obtained from Figure
507 5(b) are relatively consistent with the thermal strain measurements. The thermal axial stress
508 remained higher near the base of the foundation during the cooling process.

509 The maximum and minimum thermal head displacements during each of the heating cycles
510 for the end-bearing foundation are shown in Figure 9(a). At the end of the first heating stage, the
511 head of the foundation has an upward, prototype-scale displacement of -1.40 mm. During
512 cooling back to a temperature of 30 °C, the foundation did not contract back to its original
513 position as it was not cooled back to ambient temperature. During each subsequent heating stage,
514 the foundation expanded slightly less than the previous cycle, although the difference between
515 the expansion and contraction of the foundation during each cycle was similar (upward
516 expansion of -1.26 mm after 4 cycles). The reason for the lower magnitude of axial expansion
517 during each heating cycle could be due to either changes in the effective stress state around the

518 foundation arising from thermally-induced water flow away from the foundation, or the effects
519 of the differential settlement between the soil and foundation during centrifugation. During the
520 heating cycles, the maximum and minimum thermal axial stress in the end-bearing foundation,
521 shown in Figure 9(b), showed no significant change. This indicates that the changes in the soil
522 behavior during transient heating and cooling did not have a major impact on the thermo-
523 mechanical response of the energy foundation.

524 The results from the centrifuge physical modeling test presented in this study highlight some
525 of the advantages and limitations of centrifuge physical modeling of thermo-mechanical soil-
526 structure interaction in energy foundations. Advantages include the incorporation of dense
527 instrumentation arrays, control of soil layering and end-restraint boundary conditions, and the
528 ability to follow mechanical and thermal loading paths that may be difficult to perform in the
529 field. The centrifuge may also be useful for evaluating the role of soil behavior on the response
530 of energy foundations, especially in the case for challenging soil profiles such as unsaturated
531 soils or soft clays. It is often easier to assess the transient behavior of these soil profiles in a
532 centrifuge model than in a full-scale soil layer. One issue with centrifuge modeling of this type
533 of problem is that waiting for steady-state heat flow may be time consuming, especially when
534 studying the effects of heating and cooling. Although an understanding of the response of energy
535 foundations during transient heating and cooling is useful, reaching steady-state conditions will
536 ensure that all effects of thermo-mechanical soil behavior have been expressed and will lead to
537 the most accurate calibration of load-transfer analyses. Another issue is that application of
538 scaling relationships causes events related to heat transfer by conduction to occur faster in the
539 model than in the prototype, meaning that a greater volume of soil will be affected by
540 temperature changes in the model than in the prototype. Although the results from thermo-

541 mechanical tests may represent a worst-case scenario due to the greater zone of influence of the
542 foundation, evaluation of time-dependent processes is complicated to consider. Nonetheless,
543 finite element models can still be validated using the model-scale response of the energy
544 foundations. Another issue is that the method of installing the energy foundations in the
545 centrifuge can never replicate the process of installation and curing encountered in the field. An
546 implication of this issue is that the soil-foundation interface cannot be replicated in a centrifuge
547 model, even though the interface may have an important effect on the restraint of thermal
548 movements of an energy foundation.

549 **CONCLUSIONS**

550 The behavior of a scale-model energy foundation tested in a geotechnical centrifuge during
551 transient heating and cooling agrees well with observations from full-scale end-bearing energy
552 foundations reported in the literature. Although limitations may be encountered in scaling of heat
553 transfer processes and the use of transient heating and cooling for characterization, the results
554 from this study confirm the relevance of centrifuge modeling of energy foundations to provide
555 data for calibration and validation of soil-structure interaction models or to verify hypotheses
556 about the relative impacts of end-restraint boundary conditions and side shear resistance. The
557 results from staged heating tests on an end-bearing foundation indicate that the maximum
558 thermal axial stress occurs near the base, likely due to an increase in side shear resistance with
559 depth. The thermal axial strains were consistently less than the free-expansion thermal strain, and
560 the thermal axial displacements calculated by integrating the thermal axial strains correspond
561 well with the thermal head displacements measured independently with an LVDT. The
562 mobilized side stresses calculated from the thermal axial stresses increased with height and were
563 consistent with the shear strength of unsaturated silt. The instrumentation in the centrifuge

564 experiment was found to permit assessment of possible mechanisms leading to changes in soil
565 behavior during cyclic heating, an aspect which would have been difficult in a full-scale
566 foundation. During successive heating-cooling cycles, slight decreases in upward thermal head
567 displacement were observed due to changes in stiffness of the unsaturated soil due to thermally-
568 induced water flow away from the foundation and potential down-drag effects. Nonetheless, little
569 change in the maximum thermal axial stress was observed during the heating-cooling cycles
570 indicating that the foundation was relatively unaffected by the heating and cooling cycles.
571 Although the results in this study do not indicate that thermo-hydro-mechanical effects in the soil
572 layer lead to significant changes in foundation behavior, they are important to consider when
573 interpreting the thermal axial strain, displacement and stress response of energy foundations.

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641

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667

668 **Table 1:** Geotechnical properties of Bonny silt and soil placement conditions in the energy
 669 foundation test

Parameter	Value
D ₁₀	< 0.0013 mm
D ₃₀	0.022 mm
D ₅₀	0.039 mm
% Passing No. 200 Sieve	83.9 %
% Clay Size	14.0 %
% Silt Size	69.9 %
% Sand Size	16.1 %
G _s	2.6
Liquid Limit, LL	25
Plastic Limit, PL	21
Plasticity Index, PI	4
Activity, A	0.29
Effective friction angle, ϕ	32.4°
Compression index, C _c	0.015
Recompression index, C _r	0.0017
Std. Proctor Max. Dry Unit Weight	16.9 kN/m ³
Std. Proctor Max. Opt. Water Content	13.6%
Drying-path soil water retention curve*	$a_{VG} = 0.035 \text{ kPa}^{-1}$, $N_{VG} = 1.77$, $\theta_r = 4\%$
Initial void ratio, e ₀	0.63
Initial water content, w ₀	14.2%
Initial degree of saturation, S ₀	0.59
Saturated hydraulic conductivity, k _s	$7.6 \times 10^{-8} \text{ m/s}$
Thermal conductivity for e ₀ and S ₀ , λ	1.147 W/mK

670 *Defined using the van Genuchten (1980) model

671

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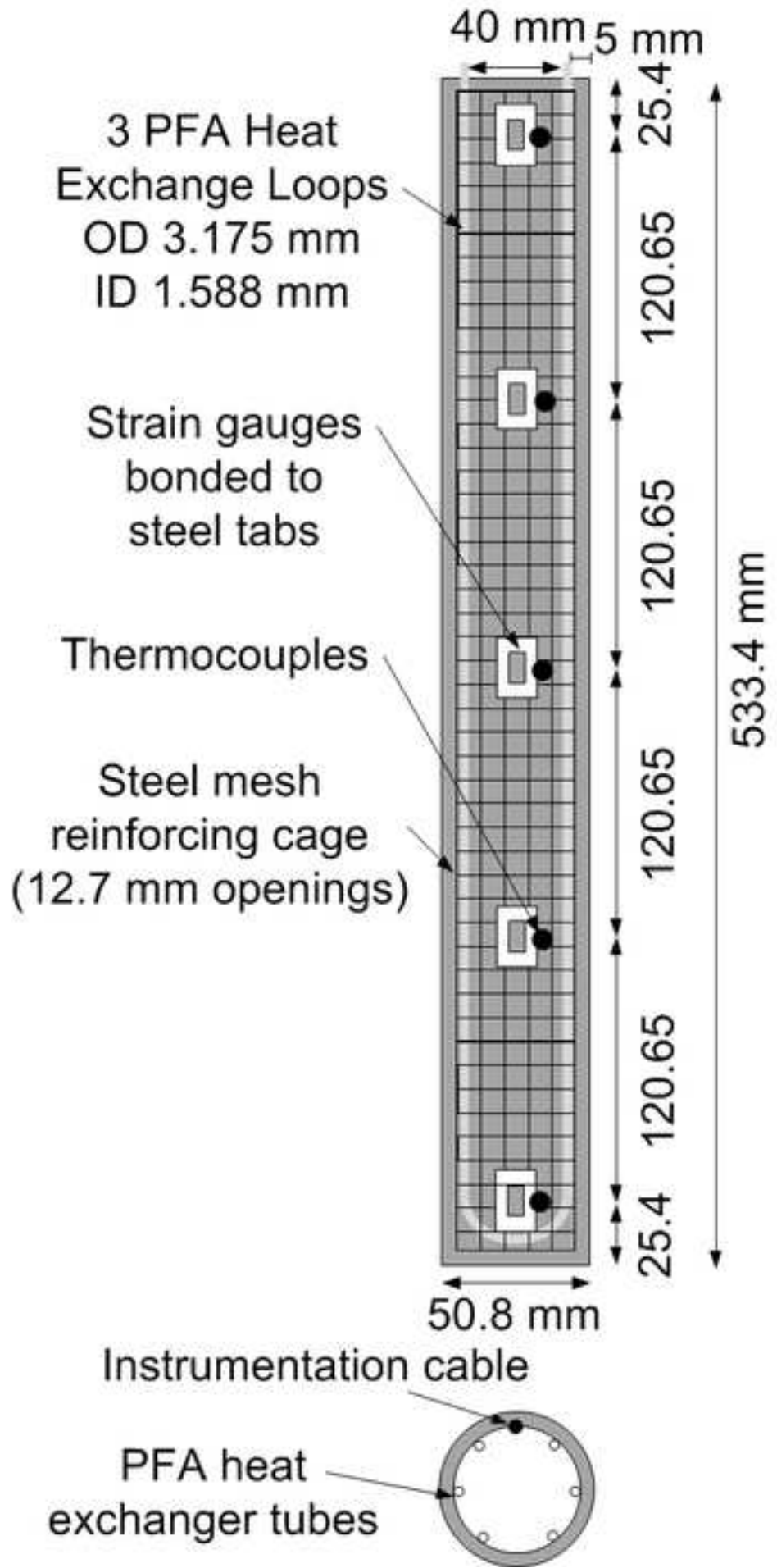


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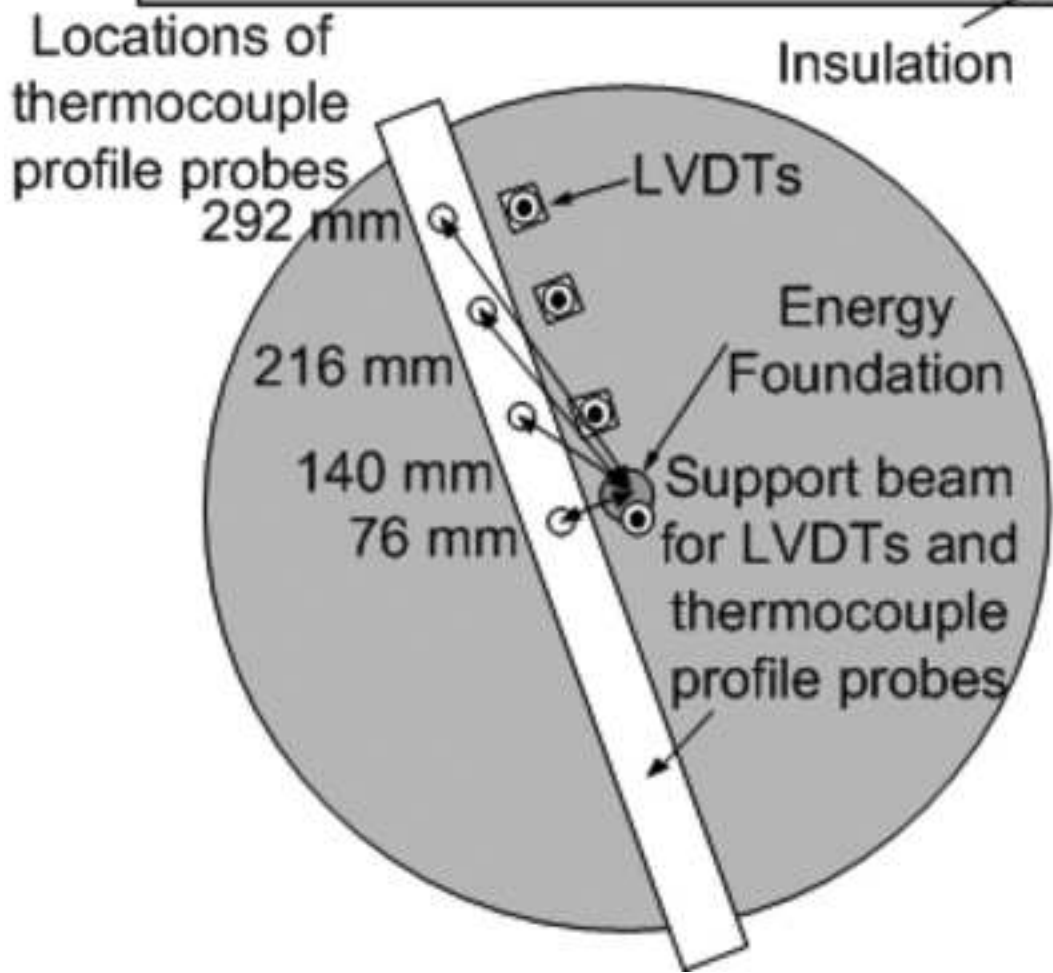
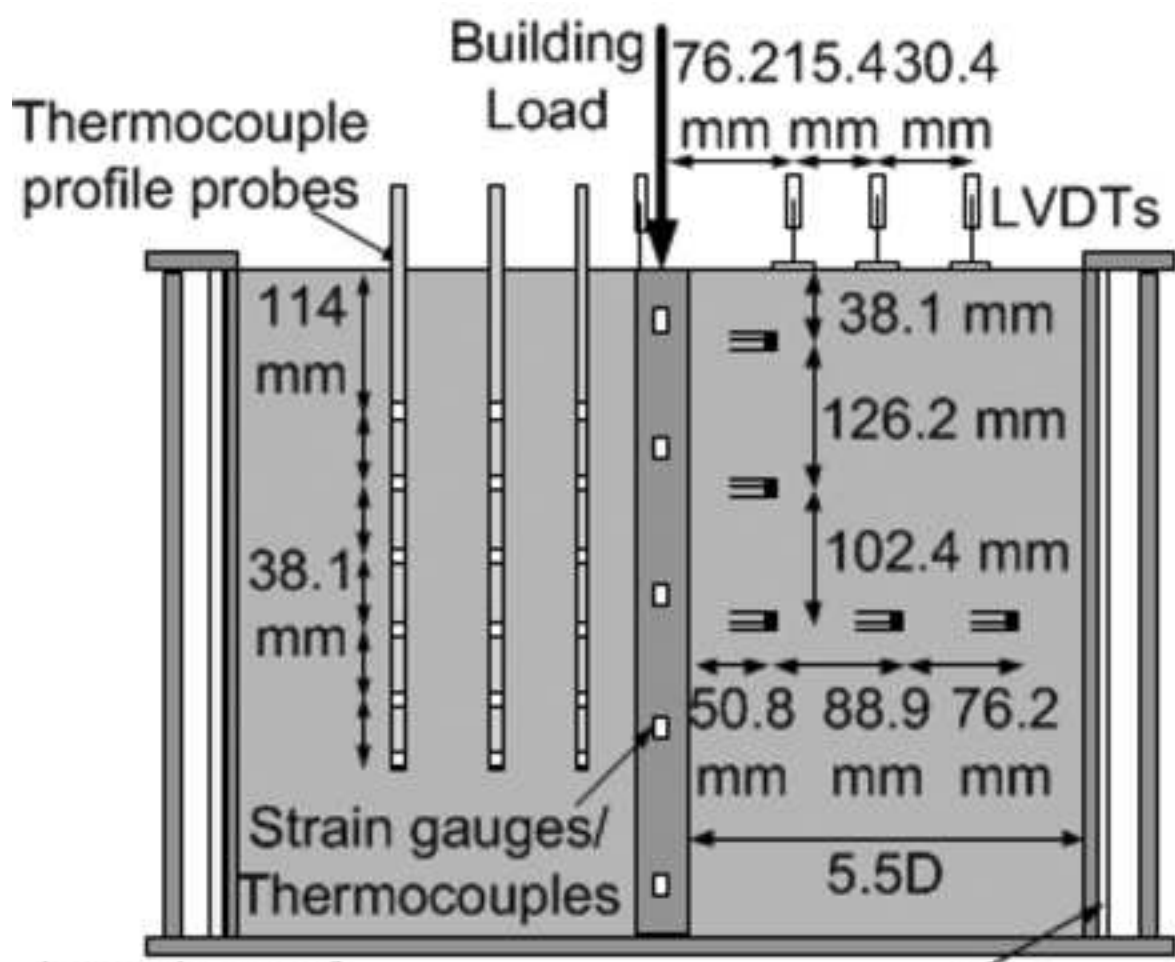


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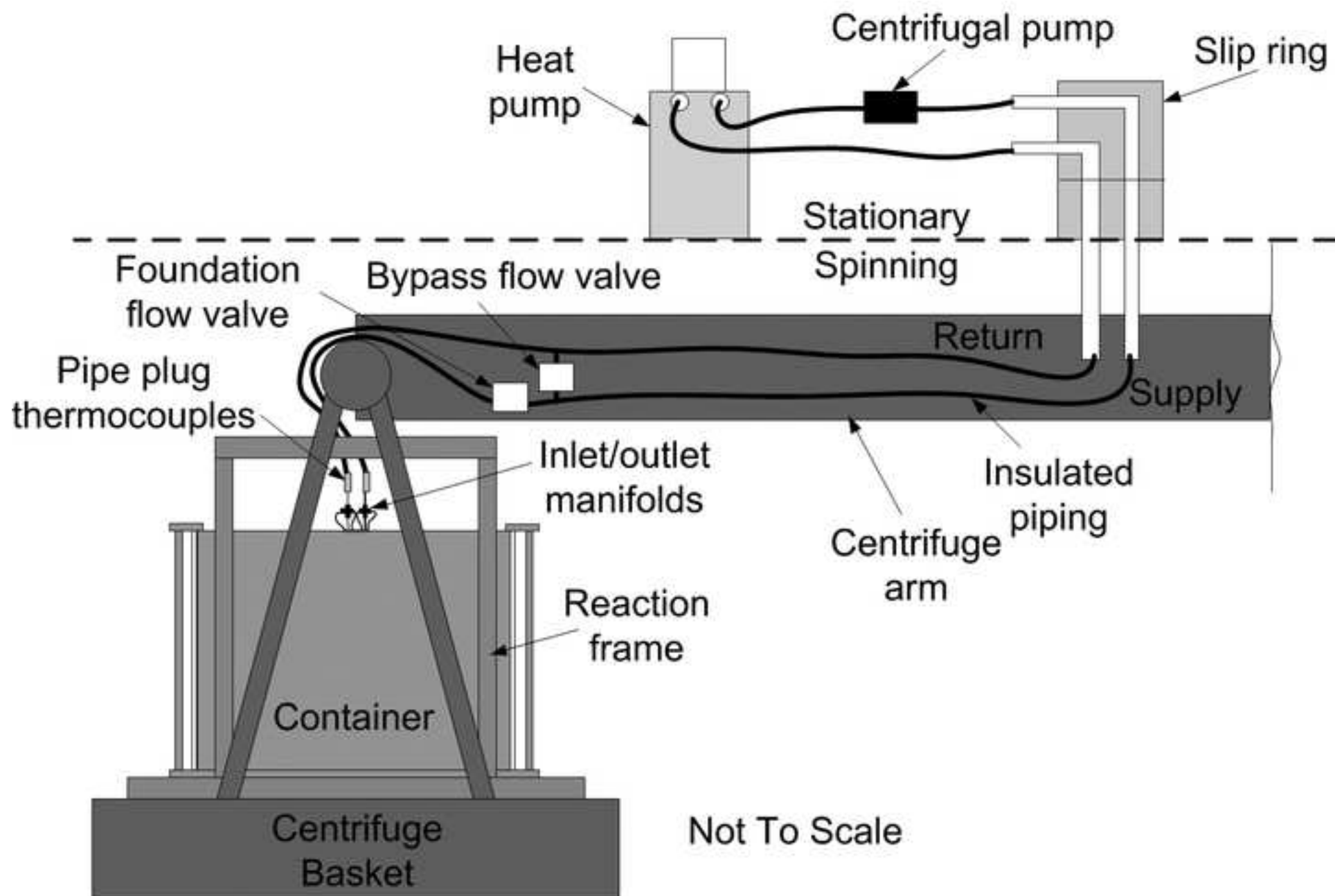
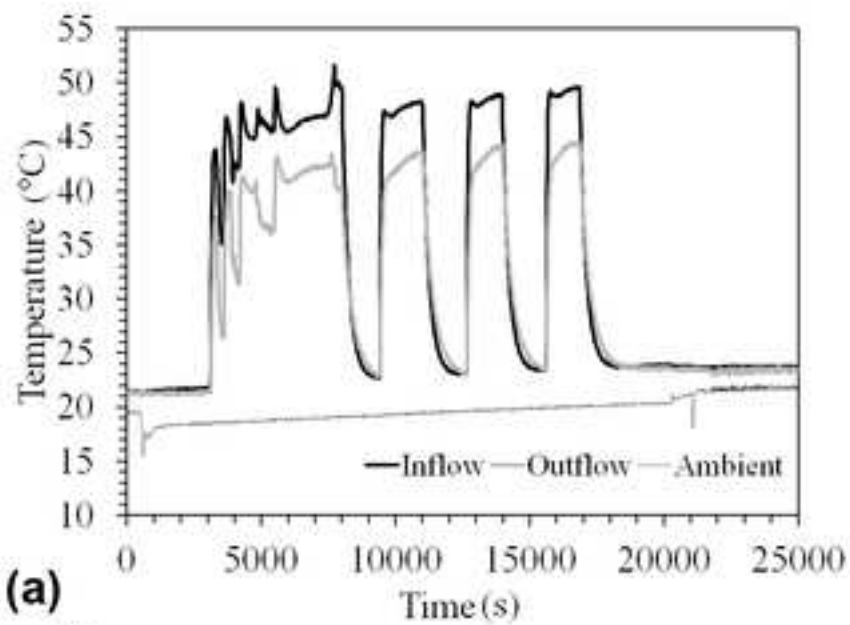
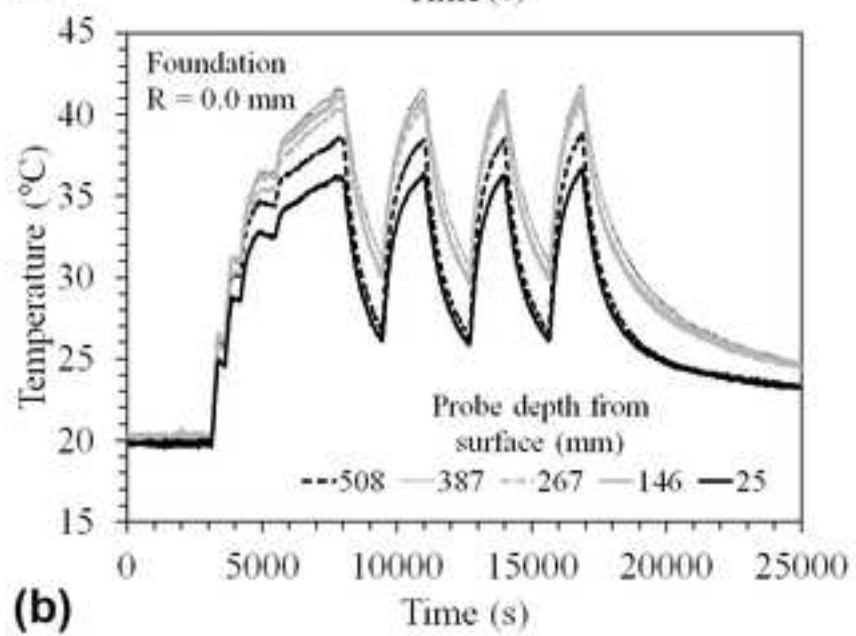


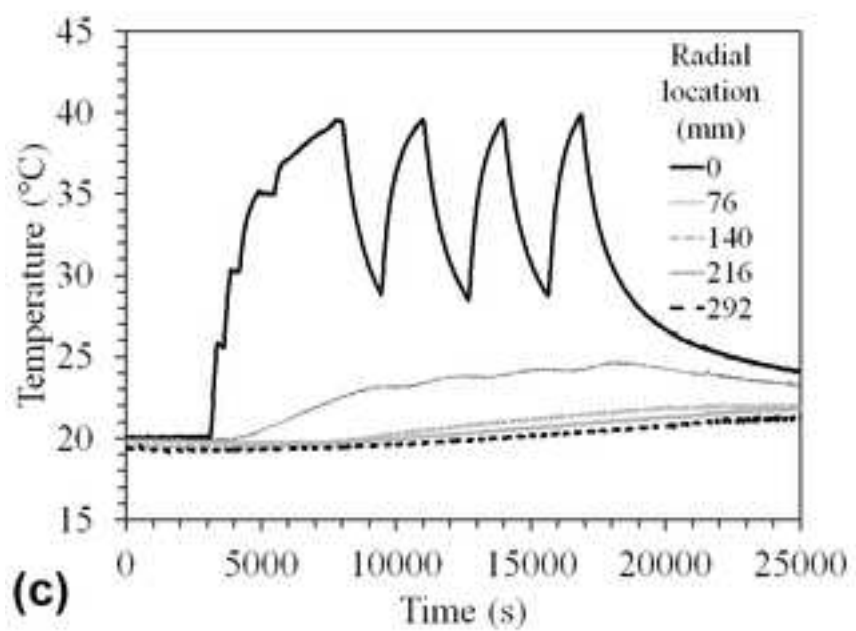
Figure 4

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(a)



(b)



(c)

Figure 5

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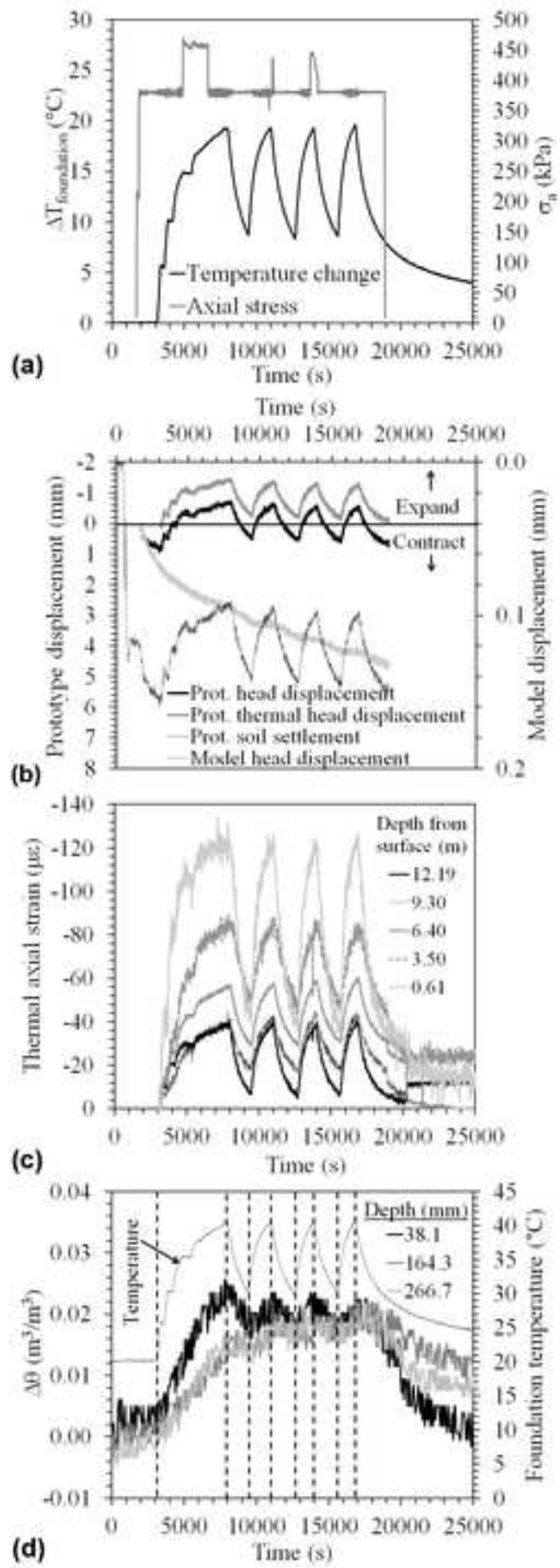


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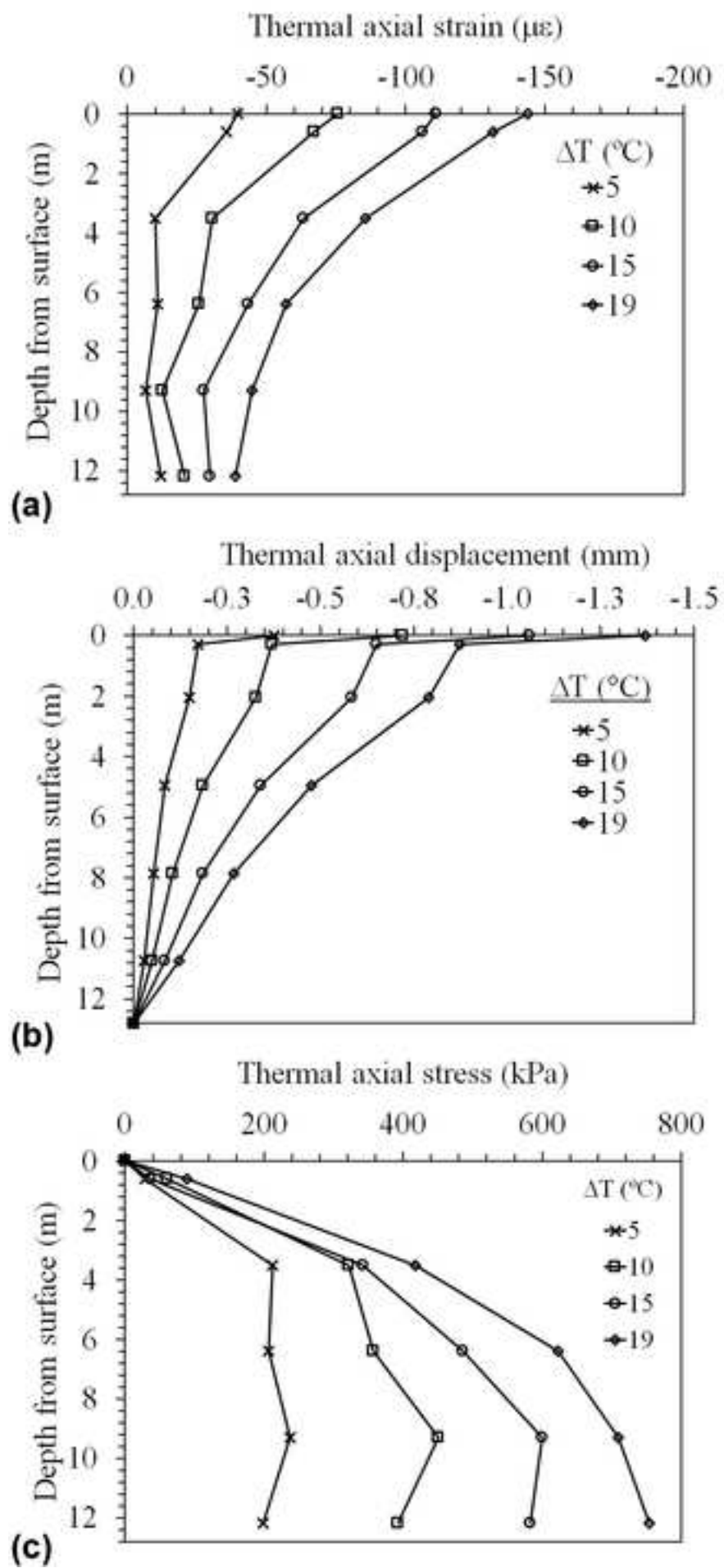


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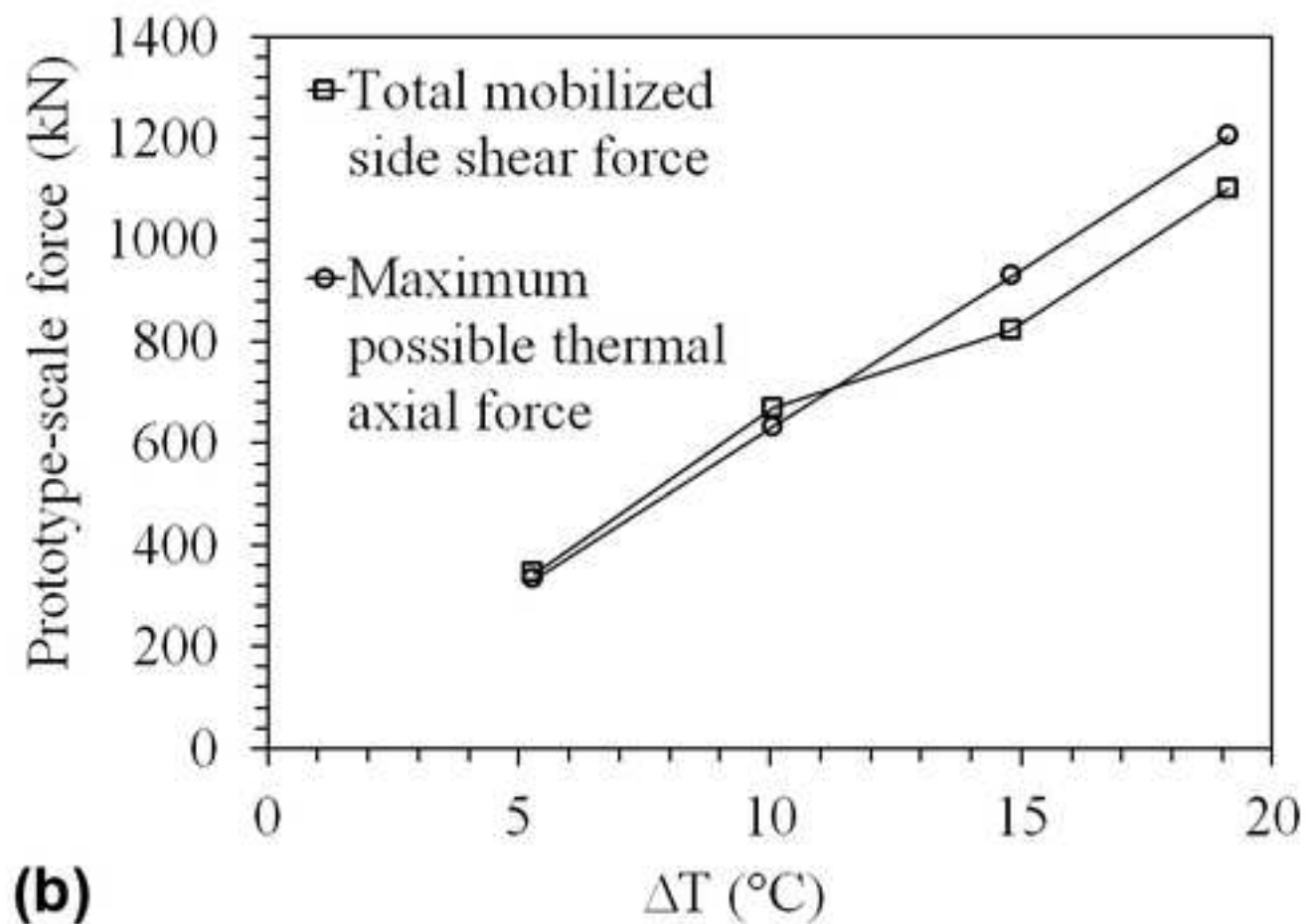
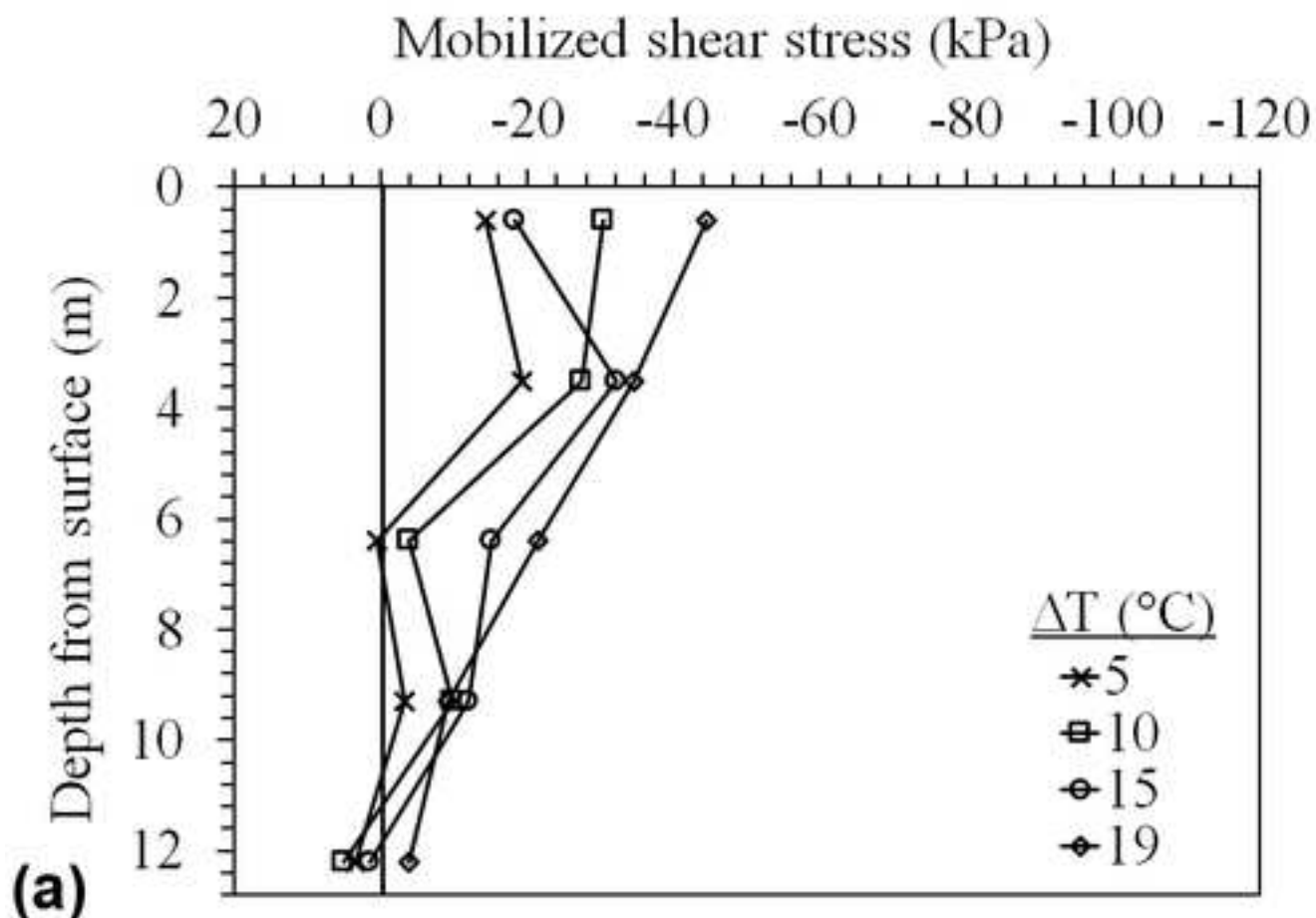


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