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Planck 2015 results XXII. A map of the thermal Sunyaev-Zeldovich effect

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ABSTRACT

We have constructed all-sky Compton parameters maps (y -maps) of the thermal Sunyaev-Zeldovich (tSZ) effect by applying specifically tailored component separation algorithms to the 30 to 857 GHz frequency channel maps from the *Planck* satellite survey. These reconstructed y -maps are delivered as part of the *Planck* 2015 release. The y -maps are characterized in terms of noise properties and residual foreground contamination, mainly thermal dust emission at large angular scales and CIB and extragalactic point sources at small angular scales. Specific masks are defined to minimize foreground residuals and systematics. Using these masks, we compute the y -map angular power spectrum and higher order statistics. From these we conclude that the y -map is dominated by tSZ signal in the multipole range, $20 < \ell < 600$. We compare the measured tSZ power spectrum and higher order statistics to various physically motivated models and discuss the implications of our results in terms of cluster physics and cosmology.

Key words. cosmological parameters – large-scale structure of Universe – Galaxies: clusters: general

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1. Introduction

This paper, one of a set associated with the 2015 release of data from the *Planck*¹ mission, describes the *Planck* Compton parameter (y) map, which is part of the *Planck* 2015 data release.

The thermal Sunyaev-Zeldovich (tSZ) effect (Sunyaev & Zeldovich, 1972) is produced by the inverse Compton scattering of cosmic microwave background (CMB) photons by hot electrons along the line of sight and in particular in clusters of galaxies. The tSZ effect has proved to be a major tool to study the physics of clusters of galaxies as well as structure formation in the Universe. Catalogues of clusters of galaxies selected via the tSZ effect have become available in the last few years, including for example those from the *Planck* satellite (Planck Collaboration VIII, 2011; Planck Collaboration XXIX, 2014), the Atacama Cosmology Telescope (ACT, Hasselfield et al., 2013) and the South Pole Telescope (SPT, Reichardt et al., 2013; Bleem et al., 2014). These catalogues and their associated sky surveys have been used to study the physics of clusters of galaxies (Planck Collaboration XII, 2011; Planck Collaboration XI, 2011; Planck Collaboration X, 2011) and their cosmological implications (Planck Collaboration XX, 2014; Benson et al., 2013; Das et al., 2013; Wilson et al., 2012; Mak & Pierpaoli, 2012).

The study of cluster number counts and their evolution with redshift using tSZ selected catalogues is an important cosmological test (Carlstrom et al., 2002; Dunkley et al., 2013; Benson et al., 2013; Planck Collaboration XX, 2014; Hou et al., 2014). This study is well complemented by the measurement of the tSZ effect power spectrum (Komatsu & Seljak, 2002), for which no explicit measurement of cluster masses is required. Low mass clusters, thus fainter in tSZ, which can not be detected individually, also contribute statistically to the measured signal (Battaglia et al., 2010; Shaw et al., 2010). Another complementary approach (as pointed out in Rubiño-Martín & Sunyaev, 2003) is to study the higher order statistics of the tSZ signal, and in particular the skewness or, equivalently, the bispectrum. The bispectrum of the tSZ effect signal is dominated by massive clusters at intermediate redshifts (Bhattacharya et al., 2012), for which high-precision X-ray observations exist. This contrasts with the power spectrum, for which most of the signal comes from the lower mass and higher redshift groups and clusters (e.g., Trac et al., 2011). Thus, theoretical uncertainties in the tSZ bispectrum are expected to be significantly smaller than those in the estimation of the tSZ power spectrum. Therefore, combined measurements of the power spectrum and the bispectrum can be used to distinguish the contribution to the power spectrum from different cluster masses and redshift ranges. However, contamination from point sources (Rubiño-Martín & Sunyaev, 2003; Taburet et al., 2010) and other foregrounds (Planck Collaboration XX, 2014) needs to be dealt with carefully.

As shown in the *Planck* 2013 results (Planck Collaboration XX, 2014), the all-sky coverage and unprecedented wide frequency range of *Planck* allowed us to produce all-sky tSZ Compton parameter maps, also referred to as y -maps. From this map an accurate measurement of the tSZ power spectrum at intermediate and large angular scales, for which the tSZ fluctuations are almost insensitive to the cluster core physics,

¹ *Planck* (<http://www.esa.int/Planck>) is a project of the European Space Agency (ESA) with instruments provided by two scientific consortia funded by ESA member states and led by Principal Investigators from France and Italy, telescope reflectors provided through a collaboration between ESA and a scientific consortium led and funded by Denmark, and additional contributions from NASA (USA).

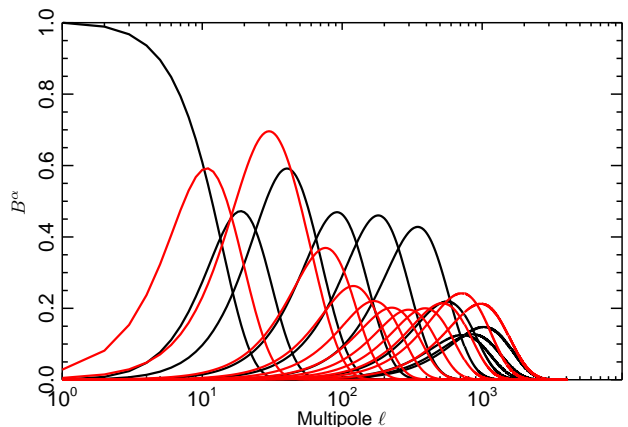


Fig. 1: Window functions corresponding to the spectral localisation of the NILC and MILCA algorithms. For NILC (black) there are 10 Gaussian window functions defining 10 needlet scales. MILCA (red) uses 11 Gaussian overlapping windows.

can be obtained. Furthermore, the expected non-Gaussianity properties of the tSZ signal can be studied using higher order statistical estimators, such as the skewness and the bispectrum. The y -map can be also used to extract the tSZ signal on regions centered at cluster positions and in particular to perform stacking analysis. Finally, this map may also be cross correlated with other cosmological probes (see for example Ma et al., 2014; Van Waerbeke et al., 2014; Hill & Spergel, 2014) as a consistency test.

In this paper we construct revised tSZ all-sky maps from the individual *Planck* frequency maps. With respect to the *Planck* Compton parameter map in the *Planck* 2013 results (Planck Collaboration XX, 2014) we have extended the analysis to the full mission data set and performed an in depth characterization of its statistical properties. This extended analysis allows us to deliver this map as part of the *Planck* 2015 data release. The paper is structured as follows. Section 2 describes the *Planck* data used to compute the tSZ all-sky maps and the simulations used to characterize it. Section 3 presents the reconstruction of the *Planck* all-sky Compton parameter map. In Sect. 4 we discuss the validation of the reconstructed y -map in the pixel domain including signal and noise characterization. Section 5 describes the power spectrum analysis. Cross-checks using higher order statistics are presented in Sect. 6. The cosmological interpretation of the results is discussed in Sect. 7, and we finally present our conclusions in Sect. 8.

2. Data and simulations

2.1. The *Planck* data

This paper is based on the *Planck*'s full mission, corresponding to five and eight full-sky surveys for the High Frequency Instrument (HFI) and Low Frequency Instrument (LFI) data respectively.

The *Planck* channel maps are provided in HEALPIX (Górski et al., 2005) pixelization scheme at $N_{\text{side}} = 2048$. A noise map is associated with each channel map. This map is obtained from the half difference of maps made from the first and second half of each stable pointing period (also called ring). In the half-

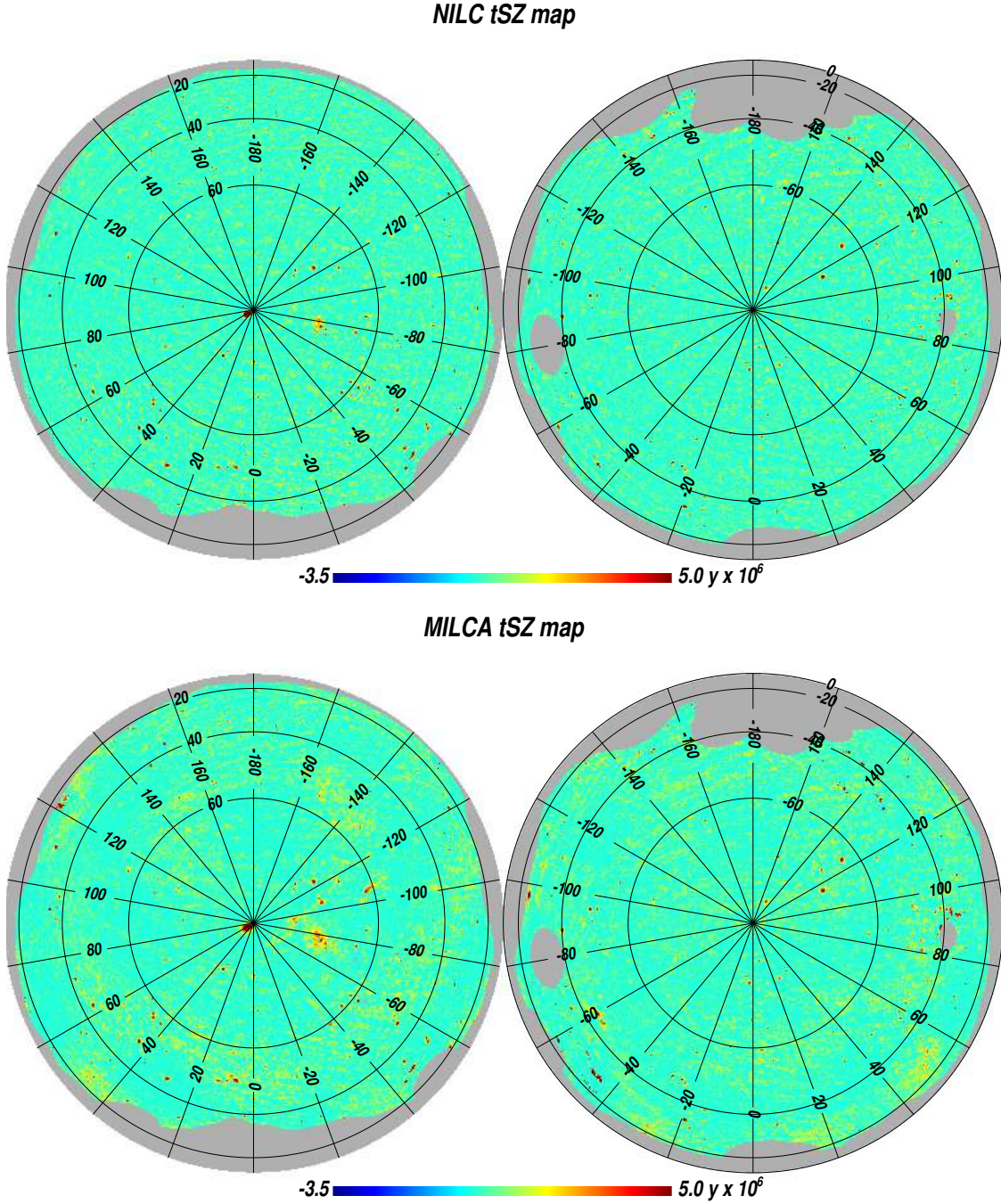


Fig. 2: Reconstructed *Planck* all-sky Compton parameter maps for NILC (*top*) and MILCA (*bottom*) in orthographic projections. The apparent difference in contrast observed between the NILC and MILCA maps comes from differences in the residual foreground contamination and from the differences in the filtering applied for display purposes to the original Compton parameter maps. For the MILCA method filtering out low multipoles reduces significantly the level of foreground emission in the final y -map. The wavelet basis used in the NILC method was tailored for tSZ extraction. For details see [Planck Collaboration XXII \(2015\)](#).

difference maps the astrophysical emission cancels out, which makes them a good representation of the statistical instrumental noise. These half-difference maps are used to estimate the noise in the final Compton parameter map. In addition, survey maps, which are also available for each channel, will be used to estimate possible residual systematic effects in the y -map.

For the purpose of this paper we approximate the *Planck* effective beams by circular Gaussians, the FWHM estimates of which are given in Table 1 for each frequency channel.

2.2. Simulations

We also use simulated *Planck* frequency maps obtained from the Full Focal Plane (FFP) simulations ([Planck Collaboration](#)

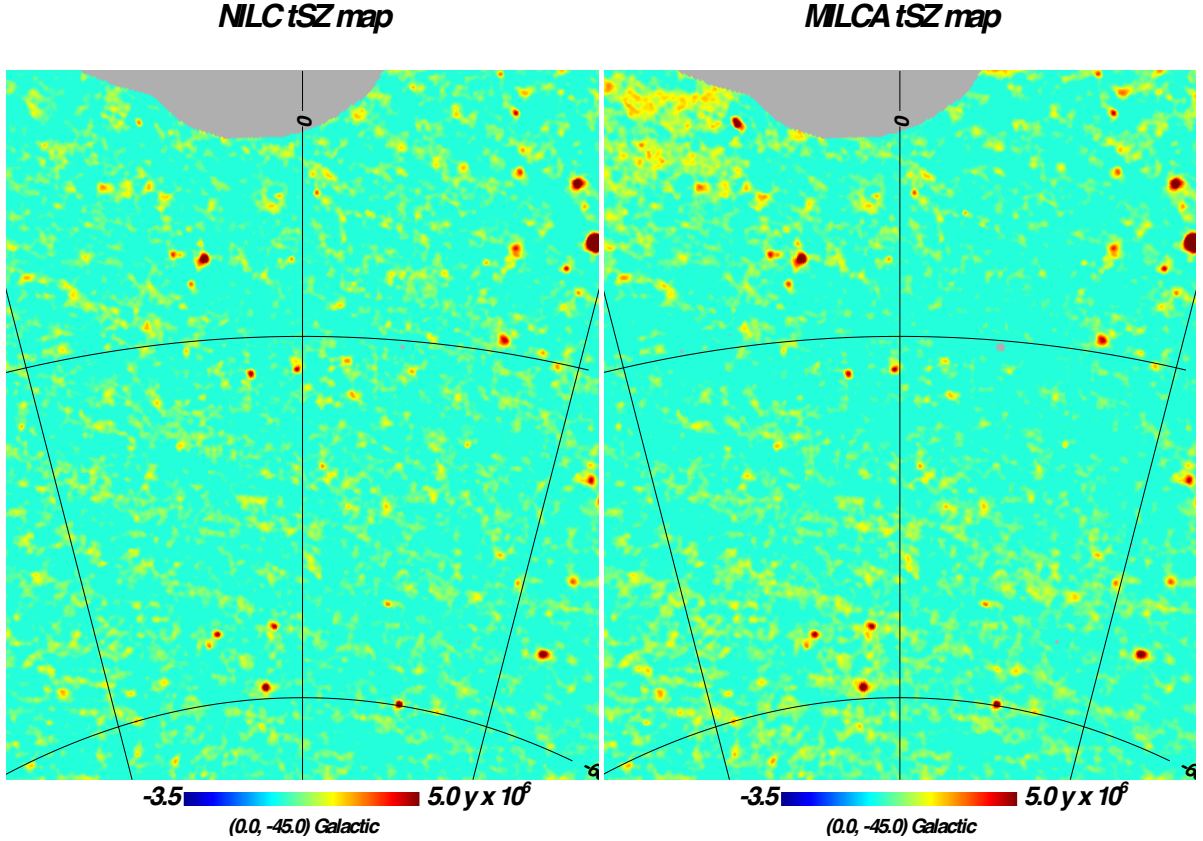


Fig. 3: A small region of the reconstructed *Planck* all-sky Compton parameter maps for NILC (left) and MILCA (right) at intermediate Galactic latitudes in the southern sky centered at $(0, -45)$ degrees in Galactic coordinates.

Table 1: Conversion factors for tSZ Compton parameter y to CMB temperature units and the FWHM of the beam of the *Planck* channel maps.

Frequency [GHz]	$T_{\text{CMB}} g(\nu)$ [K _{CMB}]	FWHM [arcmin]
100	-4.031	9.66
143	-2.785	7.27
217	0.187	5.01
353	6.205	4.86
545	14.455	4.84
857	26.335	4.63

XII, 2015), which are described in the *Planck* Explanatory Supplement (Planck Collaboration ES, 2013).

These simulated maps include the most relevant sky components at microwave and millimetre frequencies, based on foregrounds from the *Planck* Sky Model (PSM, Delabrouille et al., 2013): CMB, thermal SZ effect, diffuse Galactic emissions (synchrotron, free-free, thermal and spinning dust and CO), radio and infrared point sources, and the clustered CIB. The tSZ signal was constructed using hydrodynamical simulations of clusters of galaxies up to redshift 0.3. For higher redshifts pressure profile-based simulations of individual clusters of galaxies randomly drawn on the sky have been added. The noise in the maps was obtained from realizations of Gaussian random noise in the time domain and therefore accounts for noise inhomogeneities in the maps.

The simulation set also includes Monte Carlo noise-only realizations for each *Planck* channel map. These will also be used to estimate the noise properties in the final y -map.

3. Reconstruction of the all-sky tSZ maps

The thermal SZ Compton parameter (Sunyaev & Zeldovich, 1972) in a given direction, \mathbf{n} , can be expressed as

$$y(\mathbf{n}) = \int n_e \frac{k_B T_e}{m_e c^2} \sigma_T ds, \quad (1)$$

where k_B is the Boltzmann constant, m_e the electron mass, σ_T the Thomson cross-section, ds the distance along the line of sight, \mathbf{n} , and n_e and T_e are the electron number density and temperature.

In CMB temperature units the tSZ effect contribution to the *Planck* maps for a given observational frequency ν is given by

$$\frac{\Delta T}{T_{\text{CMB}}} = g(\nu) y. \quad (2)$$

Neglecting relativistic corrections, $g(\nu) = x \coth(x/2) - 4$, with $x = h\nu/(k_B T_{\text{CMB}})$. Table 1 presents the conversion factors for Compton parameter to CMB temperature, K_{CMB} , for each frequency channel, after integrating over the instrumental bandpass (Planck Collaboration IX, 2014).

3.1. Reconstruction methods

The tSZ effect signal in the *Planck* frequency maps is subdominant with respect to the CMB and other foreground emissions.

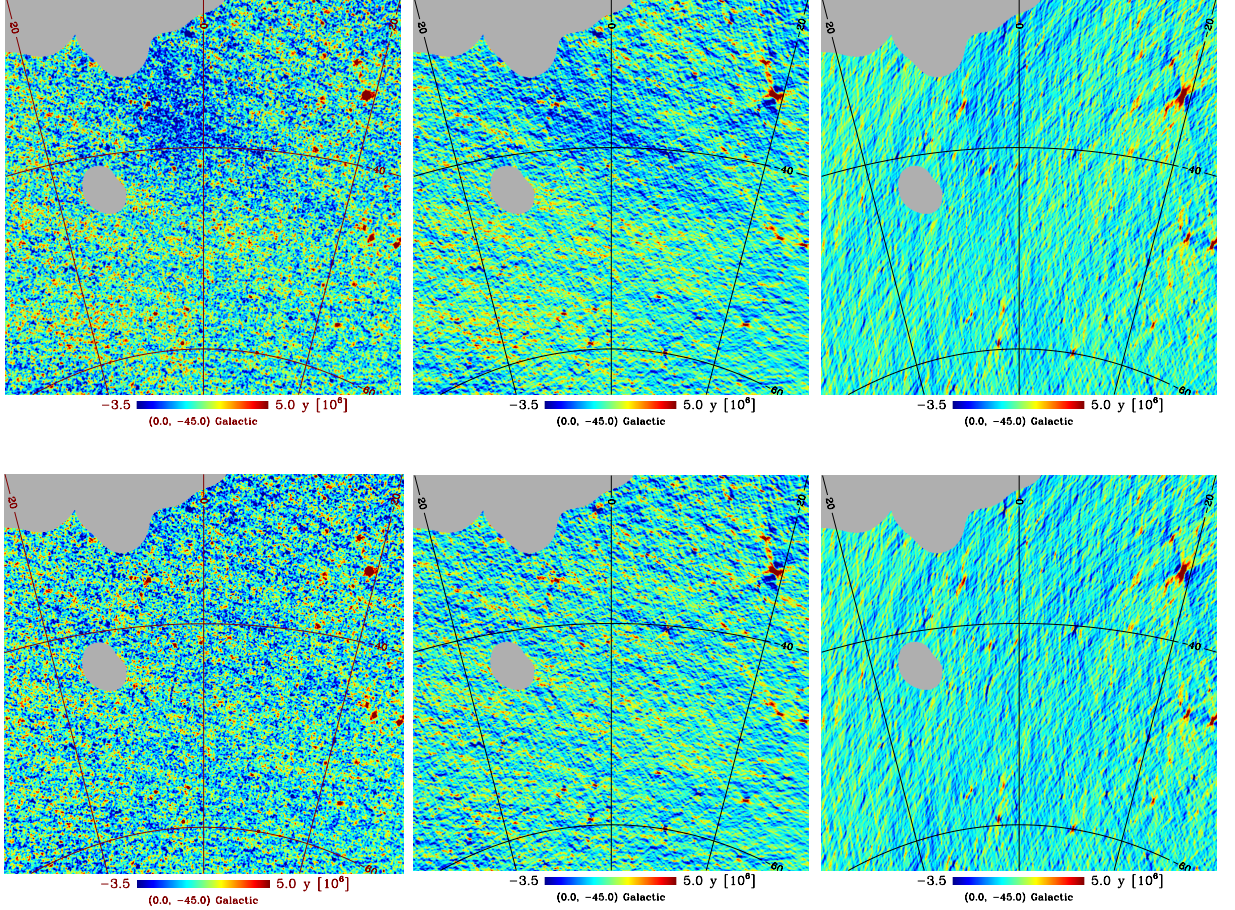


Fig. 4: In and cross scan contributions in the NILC (top line) and MILCA (bottom line) y-maps. From left to right we present the original y-maps, and their in and cross scan contributions for a small region at intermediate Galactic latitudes in the southern sky centered at $(0, -45)$ degrees in Galactic coordinates.

By contrast to the CMB emission, the tSZ effect from galaxy clusters is spatially localized and leads to a highly non-Gaussian signal. CMB-oriented component-separation methods (Planck Collaboration XII, 2014) are not adequate to recover the tSZ signal. We therefore use specifically tailored component separation algorithms to reconstruct the tSZ signal from the *Planck* frequency channel maps as in Planck Collaboration XX (2014). These algorithms rely on the spatial localization of the different astrophysical components and on their spectral diversity to separate them. As in Planck Collaboration XX (2014) we consider here the MILCA (Modified Internal Linear Combination Algorithm, Hurier et al., 2013) and NILC (Needlet Independent Linear Combination, Remazeilles et al., 2011) methods. Both are based on the Internal Linear Combination (ILC) approach that searches for the linear combination of the input maps that minimizes the variance of the final reconstructed map under the constraint of offering unit gain to the component of interest (here the tSZ effect, whose frequency dependence is known). Both algorithms have been extensively tested on simulated *Planck* data.

For both methods, the *Planck* HFI maps from 100 to 857 GHz, convolved to a common resolution of $10'$, are used. In the case of NILC we also use the LFI data at large angular scales ($\ell < 300$). Similarly, for both methods the 857 GHz map, which traces the thermal dust emission on large angular scales, is

only used for multipoles $\ell < 300$ to minimise residuals from IR point sources and clustered Cosmic Infrared Background (CIB) emission in the final y-maps.

3.1.1. NILC

In the multi-component extensions of NILC (Delabrouille et al., 2009; Remazeilles et al., 2011), initially developed to extract the CMB, the weights for component separation (i.e., covariances) are computed independently in domains of a needlet decomposition (in the spherical wavelet frame). The needlet decomposition provides localization of the ILC filters both in pixel and in multipole space, allowing us to deal with local contamination conditions varying both in position and in scale. We imposed constraints to remove the CMB contamination and preserve the tSZ effect. To avoid strong foreground effects, part of the Galactic plane (corresponding to about 2% of the sky) was masked before applying NILC to the *Planck* frequency maps.

The localisation in multipole space is achieved by using ten Gaussian window functions $\{h_j(\ell)\}_{1 \leq j \leq 10}$ as bandpass filters², so-called needlet bands, allowing for smooth localisation in ℓ (see

² Note that in Planck Collaboration XXI (2014) cosine window functions were used.

Fig. 1). NILC performs a weighted linear combination of the bandpass filtered Planck maps for each needlet scale independently. The localisation in the spatial domain is achieved by defining scale-dependent zones over the sky on which the covariance matrices and ILC weights are computed. More precisely, the pixel domain on which the covariance is computed, is defined from the smoothing of the product of the relevant needlet maps with a symmetric Gaussian window in pixel space whose FWHM depends on the needlet scale considered. This avoids artificial discontinuities at pixel edges. The localisation reduces the number of modes on which the statistics is computed, this may be responsible for an “ILC bias” due to chance correlations between SZ and foregrounds (Delabrouille et al., 2009). At the coarsest scale in particular (first needlet band), the area of the spatial localisation must be large enough to counterbalance the lack of modes in multipole space due to spectral localisation. In practice, the zones for spatial localisation are not pre-defined but their area is automatically adjusted to the needlet scale considered. The ILC bias b_{ILC} is related to the number of channels N_{ch} and to the number of modes N_m Delabrouille et al. (2009) as

$$b_{\text{ILC}} = -\sigma_{\text{SZ}}^2 \frac{N_{\text{ch}} - 1}{N_m}. \quad (3)$$

This offers the possibility to adapt N_m and N_{ch} in order to control the ILC bias to a set threshold, as discussed in Remazeilles et al. (2013): given both the number of channels and the number of spectral modes in ℓ -space at the needlet scale considered, our NILC algorithm consistently computes the number of spatial modes (similarly, the zone area for spatial localisation) required to control the ILC bias.

3.1.2. MILCA

MILCA (Hurier et al., 2013), when applied to the extraction of the tSZ signal, also uses two spectral constraints: preservation of the tSZ signal (the tSZ spectral signature discussed above is assumed); and removal of the CMB contamination in the final SZ map, making use of the well known spectrum of the CMB. In addition, to compute the weights of the linear combination, we have used the extra degrees of freedom in the linear system to minimize residuals from other components (two degrees of freedom) and from the noise (two additional degrees). The noise covariance matrix was estimated from the half-difference maps described in Section 2.1. To improve the efficiency of the MILCA algorithm, weights are allowed to vary as a function of multipole ℓ , and are computed independently on different sky regions. We have used 11 filters in ℓ space as shown in Figure 1. These filters have an overall transmission of one, except for $\ell < 8$. For these large angular scales we have used a Gaussian filter to reduce foreground contamination. To ensure sufficient spatial localisation for each required resolution the size of the independent sky regions was adapted to the multipole range. We used a minimum of 12 regions at low resolution and a maximum of 3072 regions at high resolution.

3.2. Reconstructed Compton parameter map

Figure 2 shows the reconstructed *Planck* all-sky Compton parameter map for NILC (top panel) and MILCA (bottom panel). For display purposes, the maps are filtered using the procedure described in the first paragraph of Sect. 6.1. Clusters appear as positive sources: the Coma cluster and Virgo supercluster are clearly visible near the north Galactic pole. The Galactic plane is

masked in both maps, leaving 67% of the sky. Residual Galactic contamination is also visible as diffuse positive structures in the MILCA y -map. We can also observe a granular structure in the NILC y -map that corresponds to an excess of noise at large angular scales as discussed in Sect. 4.2.

Weaker and more compact clusters are visible in the zoomed region of the Southern cap, shown in Fig. 3. Strong Galactic and extragalactic radio sources show up as negative bright spots on the maps and were masked prior to any scientific analysis, as discussed below in Sect. 4.4.1. We can again observe residual Galactic contamination around the edges of the masked area, which is more important for MILCA. Finally, we note in the NILC and MILCA y -maps the presence of systematic residuals along the scanning direction that show up as stripes. These are the consequence of stripes in the original *Planck* maps (see Planck Collaboration VIII, 2015, for a detailed discussion). We discuss the level of residual stripes in Sect. 4.1.

In addition to the full Compton parameter maps, we also produce the so-called first and last (F and L hereafter) Compton parameter maps from the first and second halves of the survey rings (i.e., pointing periods). These maps are used for power spectrum estimation in Sect. 5 as well as to estimate the noise properties in the y -maps (see Sect. 4.2).

3.3. Comparison to other Compton parameter maps in the literature

Van Waerbeke et al. (2014) and Hill & Spergel (2014) have used the *Planck* nominal data to reconstruct a Compton parameter map over a large fraction of the sky. As for the present work, they use an ILC approach imposing spectral constraints to have unitary gain for the SZ component and null contribution from CMB, but they do not use the spectral and spatial separation discussed above. Van Waerbeke et al. (2014) consider only the four HFI channels between 100 and 353 GHz and force a null contribution from dust emission. On their side Hill & Spergel (2014) also include the 545 GHz map, while using the 857 GHz channel only as a template for dust emission: a flux cut is imposed in order to build a mask that keeps only the 30% of the sky. They also apply a point source mask (radio and IR) before computing the ILC coefficients reducing the final sky fraction to about the 25%. Furthermore, Van Waerbeke et al. (2014) and Hill & Spergel (2014) aim mainly at studying the cross-correlation with the gravitational lensing mass map from the Canada France Hawaii Telescope Lensing Survey (CFHTLenS) and the publicly-released *Planck* CMB lensing potential map, respectively. Their y -map reconstruction methods are tailored to fulfill these objectives and as a consequence they present larger overall foreground contamination, in the case of Hill & Spergel (2014) also a significantly smaller sky fraction.

4. Pixel space analysis

4.1. Stripes in the y -map

As discussed in Sect. 3.2, residual stripes are visible in the NILC and MILCA y -maps. These stripes are mainly due to residuals in-scan direction systematics after subtraction of an offset for each *Planck* stable pointing period (Planck Collaboration VIII, 2015). To study how these stripes contaminate the final y -maps we have decomposed them in their in-scan and cross-scan direction contributions. We first convert the y -maps from Galactic to Equatorial coordinates for which the scan direction corresponds mainly to a fixed longitude value. Secondly, we apply a Galactic

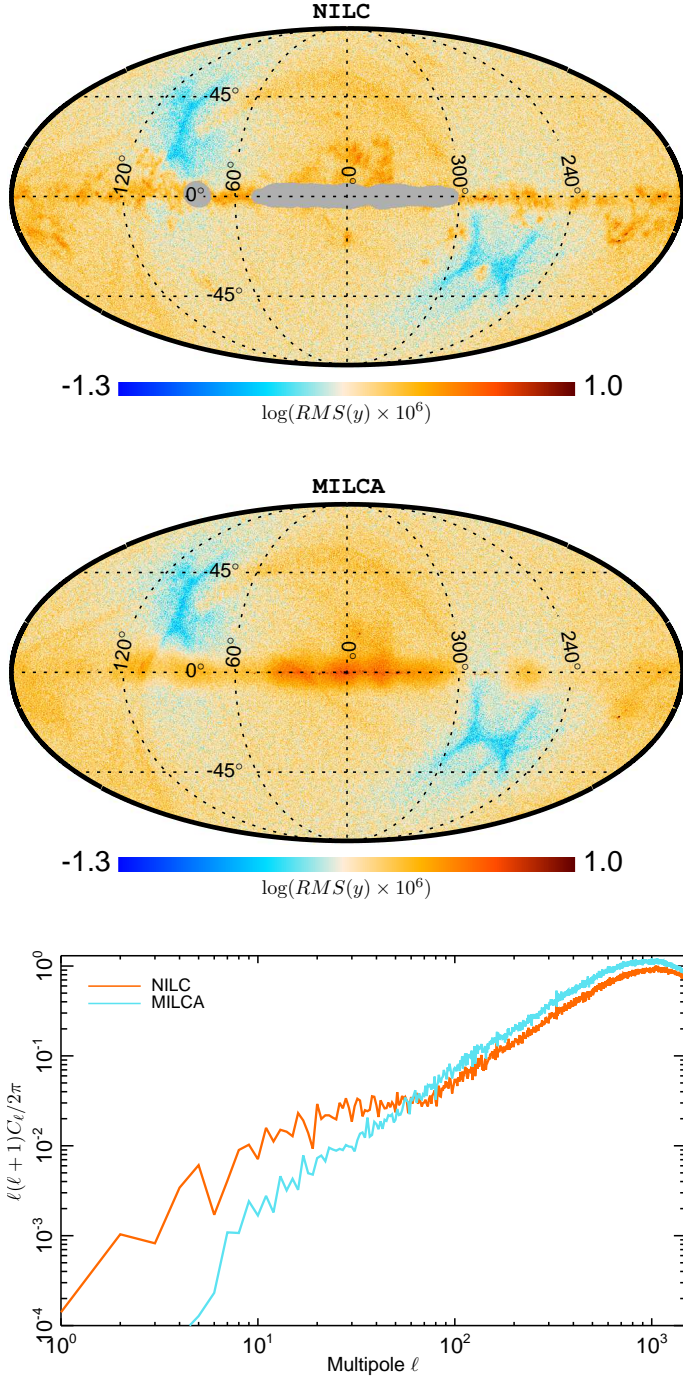


Fig. 5: *Top*: Standard deviation maps for the NILC (top) and MILCA (middle) y-maps corresponding to the inhomogeneous noise contribution computed from the half difference of the half-rings maps. *Bottom*: Angular power spectrum of the homogeneous noise contribution for the NILC (orange) and MILCA (blue) y-maps (see main text for details).

mask to the Equatorial y-maps and decompose them in spherical harmonics. Third, we select the in-scan (cross-scan) direction components by nullifying the spherical harmonic coefficients, $a_{\ell,m}$, for $\ell > m$ ($\ell < m$). Finally, we construct maps from those transformed coefficients and convert back to Galactic coordinates. We have chosen to mask the brightest 40% of the sky in the 857 GHz *Planck* map to keep Galactic ringing residuals negligible and a sufficiently large fraction of the sky for the analysis.

Figure 4 shows from left to the right the original, in-scan and cross-scan y-maps for NILC (top) and MILCA (bottom) in the southern sky region presented in Figure 3. We note that the y-maps look noisier as they are not filtered using the procedure described in the first paragraph of Sect. 6.1. The stripes are apparent in both the original and in-scan y-maps as expected. We find that the ratio of the rms of the in and cross scan maps is 1.16 (1.17) for NILC (MILCA), consistent with residual stripe contamination (for Gaussian noise only maps we find a ratio of 1). Here we have measured an overall increase of the rms of the maps due to stripe contamination, a more detailed estimate of the effect in terms of tSZ power spectrum is presented later in Sect. 5.2.1.

The in-scan and cross-scan decomposition method modifies the cluster signal significantly due to ringing effects – see positive and negative patterns around clusters in Figure 4. To explore this effect we have also applied the in-scan and cross-scan decomposition method to the simulated Compton parameter map for the detected and confirmed clusters of galaxies in the *Planck* catalogue (Planck Collaboration XXIX, 2014), which is presented in Section 5.3. We find that those negative and positive patterns are also present in the decomposed maps and the ratio between the rms of the in-scan and cross-scan maps is 1 as expected. We finally stress that the in-scan and cross-scan decomposition of the y-maps does not preserve the positiveness of the tSZ signal. As a consequence we can not use them to estimate the contamination of the stripe systematic effect in the analysis presented in Section 6.

4.2. Noise distribution on the y-map

The *Planck* maps present a highly non-homogeneous structure of the noise that is mainly due to the inhomogeneous scanning strategy. Such complicated structure is propagated into the y-map and needs to be considered for further analysis. Here, we have chosen to describe the noise structure in the y-map by A) a variance map, which will capture the inhomogeneity of the noise, and B) the angular power spectrum of an homogeneous noise map, which it is obtained after correcting for inhomogeneity. The variance map and homogeneous noise power spectrum have been obtained using two different methods:

1. *Half-difference*. The half difference of the half rings y-maps is used to obtain an estimate of the noise in the NILC and MILCA y-maps. From this half difference map we compute an estimate of the noise variance at lower resolution by squaring and downgrading it to Healpix $N_{\text{side}}=128$. The homogenous noise contribution is obtained by dividing the half difference map by the variance map after upgrading it to Healpix $N_{\text{side}}=2048$.
2. *Simulations-based*. 100 noise only realisation from the simulations described in Sect. 2.2 are used to compute an estimate of the variance per pixel at full resolution, which is then averaged to Healpix $N_{\text{side}}=128$ resolution. The homogenous noise contribution map is then computed as above.

The two methods give consistent results at high Galactic latitudes but differ at low Galactic latitudes where we expect larger foreground residuals that show up in the *Half-difference* method. This is visible in the top panel of Figure 5 where we display variance maps obtained from the *Half-difference* method for NILC (left) and MILCA (right). For a wide range of analyses with the y-map (i.e computing the radial profile, surface density or total flux of a cluster, stacking of faint sources, detection of shocks, study of the ICM) an estimate of the overall uncertainties per

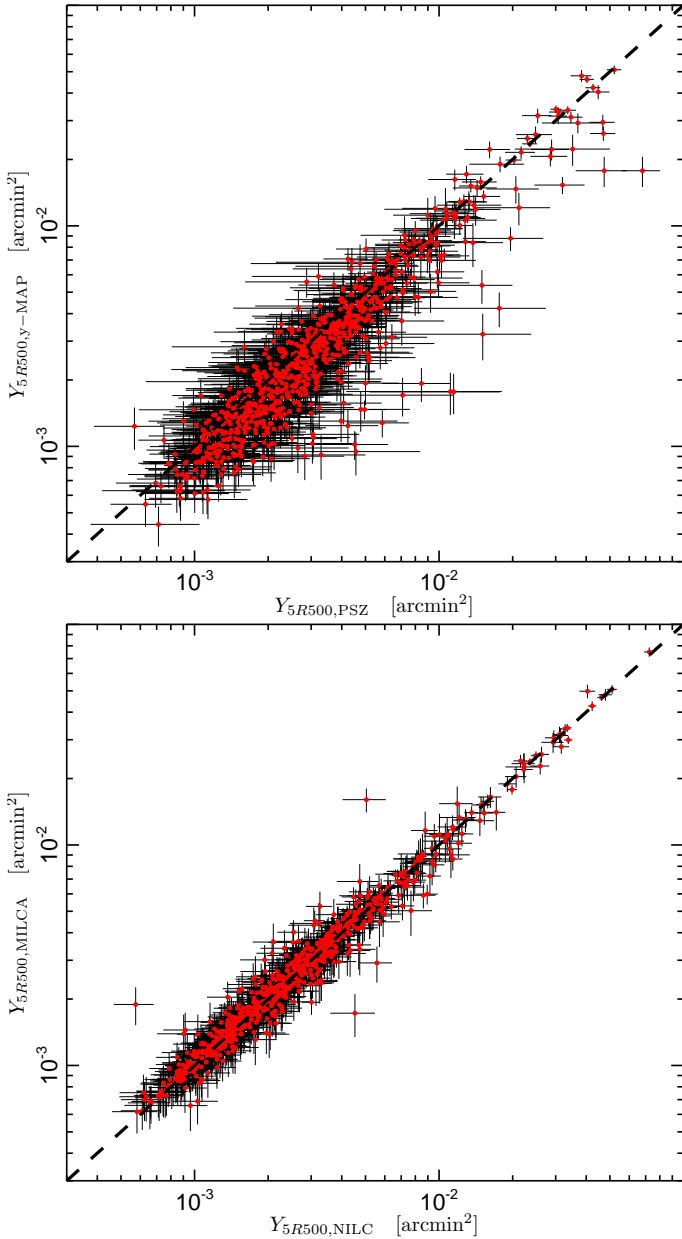


Fig. 6: *Top*: Comparison between the measured tSZ flux reported in the Planck cluster sample and that estimated directly on the NILC y-map for the blindly detected common sources. *Bottom*: As above but for the NILC and MILCA measured fluxes.

pixel (including foreground contribution) is required. Thus, the half difference maps are released with the y-map. We also show in the bottom panel of Figure 5 the power spectrum of the homogeneous noise contribution. We observe a significant large angular scale (low multipoles) component in the homogeneous noise contribution. This low multipole component is significantly larger for the NILC y-map than for the MILCA one.

4.3. Foreground contamination and masking

4.3.1. Galactic emission

As discussed above, residual galactic foreground contribution is observed at low Galactic latitudes in both the NILC and MILCA y-maps, while being more important for the MILCA y-map. This

contribution is mainly induced by thermal dust emission, as discussed in details in Planck Collaboration XXIX (2014), and is therefore mainly associated to the Galactic plane. When dealing with individual objects or with the stacking of faint objects we recommend to account for it using the variance maps discussed above. For statistical analyses as those presented in Sect. 5 and 6, specific masks need to be defined and they are fully discussed in those sections.

4.4. tSZ signal from resolved sources

4.4.1. Point sources

Point source contamination is an important issue for the cosmological interpretation of the *Planck* Compton parameter map.

In the reconstructed tSZ maps radio sources will appear as negative peaks, while infrared sources will show up as positive peaks, mimicking the cluster signal. To avoid contamination from these sources we introduce a point source mask (PSMASK, hereafter). This mask is the union of the individual frequency point-source masks discussed in Planck Collaboration XXVIII (2014). The reliability of this mask was verified by looking at the 1D PDF of the pixel signal (as it will be discussed in Section 6.1). We found that a more robust mask can be obtained by enlarging the mask size around the strongest radio sources in order to minimize their contribution.

Alternatively, we have also performed a blind search for negative sources in the y-maps using the MHW2 algorithm (López-Cañiego et al., 2006). We have detected 997 and 992 negative sources for NILC and MILCA respectively. We find that 67 and 42 (for NILC and MILCA, respectively) of those detected sources are not masked by the PSMASK. However, most of them (54 for NILC and 36 for MILCA) are false detections made by the algorithm in regions surrounding very strong positive sources (i.e. galaxy clusters). For those detected as additional negative sources, the PSMASK has been updated to account for them, even though the strongest are already excluded when applying the 50% Galactic mask used for the cosmological analysis below.

For infrared sources, estimating the efficiency of the masking is hampered by the tSZ signal itself. The residual contamination from point sources is discussed in Sects. 5.2 and 6. It is also important to note that the PSMASK may also exclude some clusters of galaxies. This is particularly true in the case of clusters with strong central radio sources, such as the Perseus cluster (see Planck Collaboration XXIX, 2014).

4.4.2. Blind search for clusters

Following Planck Collaboration XXI (2014) a blind search for tSZ (positive) sources has been also performed on the all-sky NILC and MILCA y-maps. We use the IFCAMEX (MHW2, González-Nuevo et al., 2006; López-Cañiego et al., 2006) and the single frequency matched filter (MF, Melin et al. 2006) methods. The detected sources with signal-to-noise ratio > 4 have been matched to the Planck cluster catalogue (PSZ2, Planck Collaboration XXVII, 2015). We have associated the detected sources to PSZ2 objects if the distance between their positions is smaller than $10'$ (the resolution of the SZ all-sky maps). The MHW2 algorithm finds 1018 and 1522 candidates for NILC and MILCA respectively, out of which 500 and 457 correspond to objects present within the PSZ2 catalogue. For NILC (MILCA) we have 41 (25) positions that are not masked by the PSMASK and that do not correspond to PSZ2 clusters. However 14 (5) are

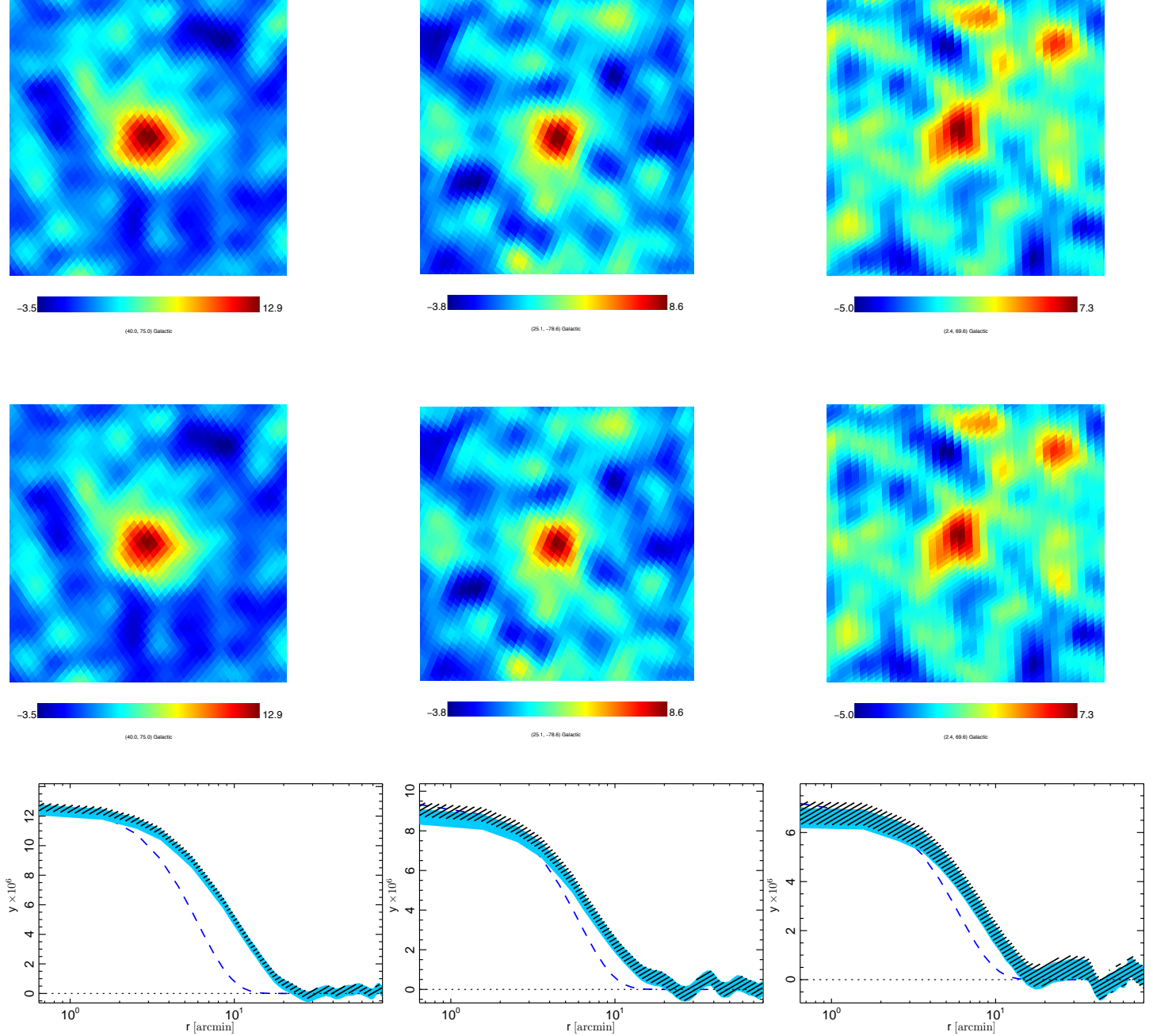


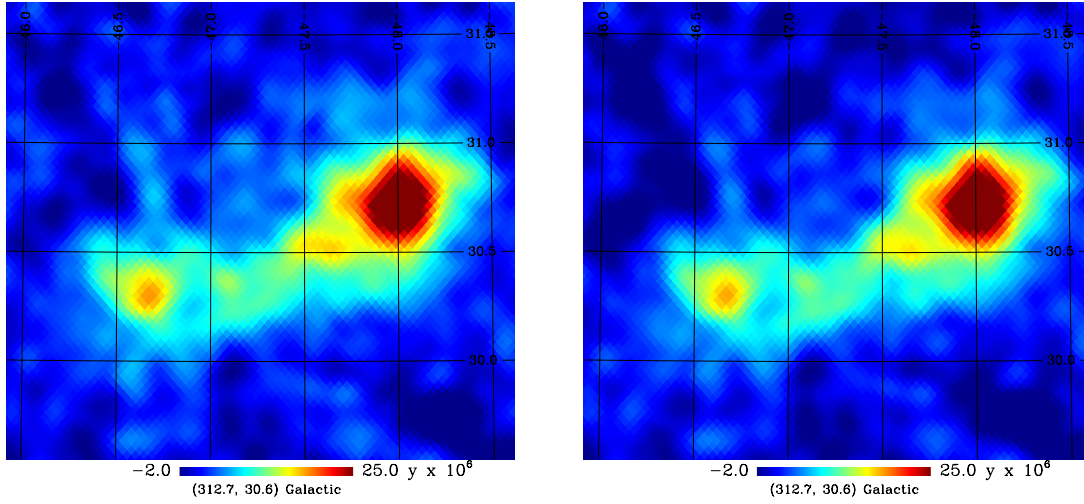
Fig. 7: Compton parameter MILCA (top row) and NILC (middle row) maps for a selection of PSZ2 cluster candidates with signal to noise ratio of 9.3, 6.2 and 4.6 from left to right. The maps are centred at the positions of the clusters in galactic coordinates, which are given at the bottom of the plot. Color scale is in units of $y \times 10^{-6}$. The bottom row presents the cluster radial profiles for MILCA (black) and NILC (blue). The beam profile is shown as a blue dashed line.

located in regions excluded by the mask used to build the PSZ2 catalogue. With the MF method we have 1472 and 1502 candidates for NILC and MILCA, out of which 1107 and 1096 correspond to objects present within the PSZ2 catalogue (867 and 835 corresponding to already validated objects, respectively). This implies a good agreement between the cluster sample and the detected sources in the y -maps.

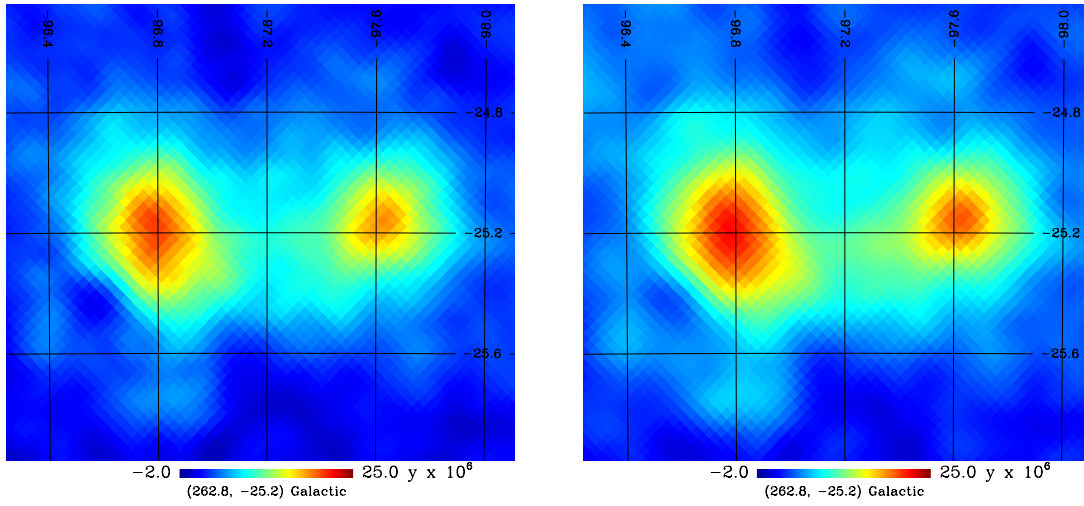
This agreement is improved by taking the union of the MHW2 and the MF catalogues. In this case, and considering only validated sources in the PSZ2 catalogue (1070 sources), we find 907 and 870 matches with blind detected cluster candidates for

NILC and MILCA, respectively. We have also performed a visual inspection of the NILC and MILCA y -maps at the position of validated PSZ2 sources for which we find no counterpart and we find evidence of an excess of signal. For most of these sources low signal-to-noise ratio and/or foreground contamination can explain why they are not detected blindly in the y -map. This is consistent with the fact that we expect blind detection methods in the y -map to be less sensitive than multifrequency ones (Melin et al., 2012). In some cases these non-detected sources are extended but with a relatively high signal-to-noise (between 6 and 12). We notice that the MHW2 and MF methods are tuned to detect

(a) Shapley supercluster



(b) A3395-A3391 merger system



(c) A339-A401 merger system

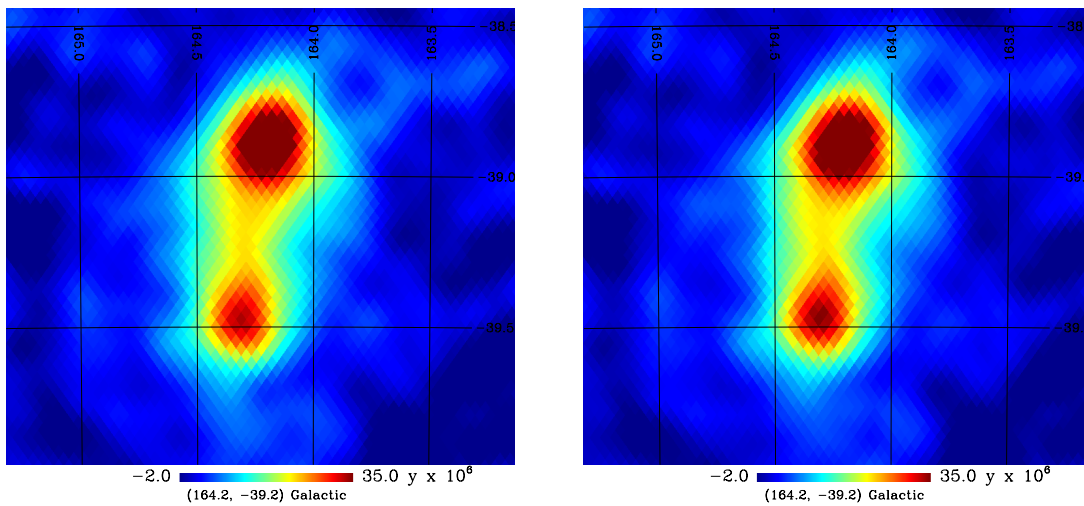


Fig. 8: Compton parameter maps of well known merging systems for MILCA (left column) and for NILC (right column).

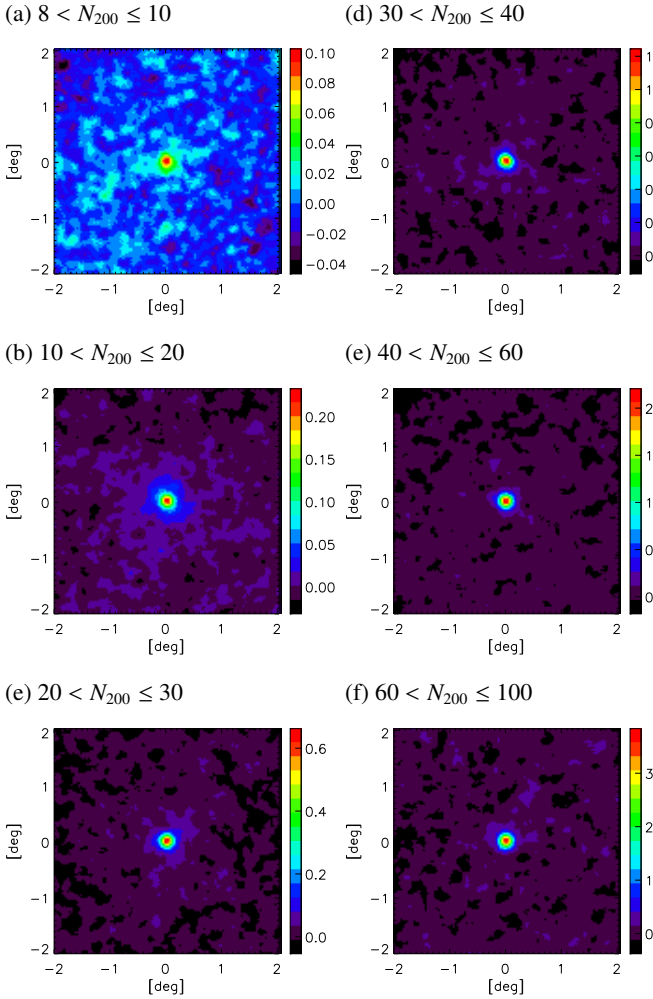


Fig. 9: $4^\circ \times 4^\circ$ average maps for different ranges in N_{200} from 8 to 100. The color scale is in unit of 10^{-6} y.

point-like and compact sources primarily, and thus they may fail for extended ones.

We present in the top panel of Figure 6 a comparison of the flux measured for these common sources in the NILC y-map with that derived from the PSZ2. The $Y_{5r_{500}}$ correspond to the integrated signal within a radius equal to $5 \times r_{500}$ ³. We observe a good agreement between the two. Most of the observed outliers (low y-map flux with respect to the PSZ2 one) correspond to cluster candidates detected close to masked point sources, or in regions with strong Galactic contamination. We also show in the bottom panel a comparison of the flux measured with the NILC and MILCA y-maps. We find good agreement between the two with three outliers corresponding to sources lying either in a region badly affected by radio and/or infrared point sources or for which we observe large uncertainties in the estimated characteristic radius of the cluster candidate. For both maps (NILC and MILCA), the average signal-to-noise ratio of the recovered clusters with the MHW2 algorithm is ~ 10 , while the signal-to-noise ratio of PSZ2 clusters only found with the matched filter technique is, as expected, lower (~ 6).

³ r_{500} is the cluster-centric distance at which the mean cluster density is equal to 500 times the critical density of the Universe

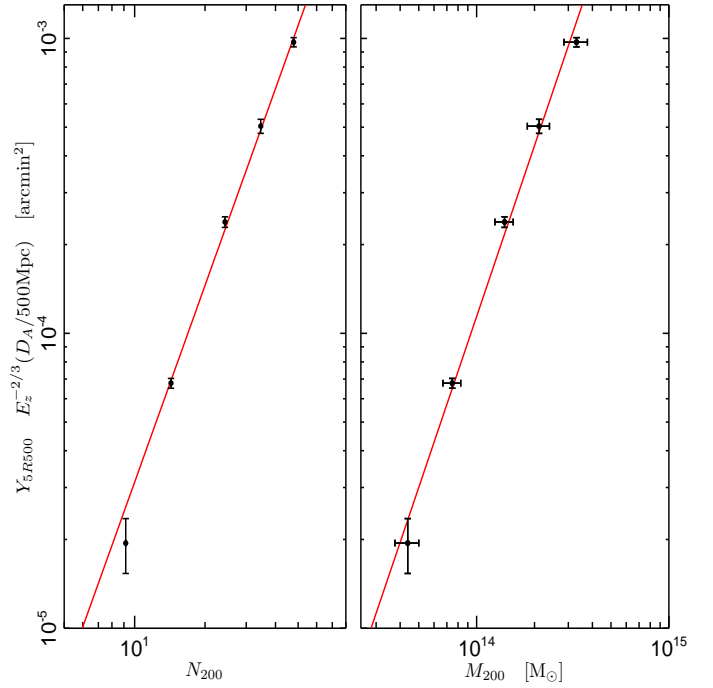


Fig. 10: Integrated tSZ signal as a function of cluster richness (left) and total mass (right). The black points correspond to the average signal obtained for the richness bins considered in Figure 9. The red line represents the corresponding best-fit power law (Eqs. 4 and 6 respectively). Considering $z \leq 0.42$, there are 13814 objects for $8 < N_{200} \leq 10$, 37250 for $10 < N_{200} \leq 20$, 7458 for $20 < N_{200} \leq 30$, 2069 for $30 < N_{200} \leq 40$, and 1133 for $40 < N_{200} \leq 60$.

4.4.3. Maps of selected clusters

We have performed a more detailed analysis for some of the cluster candidates in the PSZ2 sample. In Figure 7 we present Compton parameter maps centred at the position of three of the newly discovered *Planck* clusters with signal-to-noise ratio of 9.3 (left), 6.2 (middle) and 4.6 (right) both for MILCA (top row) and NILC (middle row). In the bottom row of the figure we present the radial profiles of these clusters as obtained from the MILCA (black lines) and NILC (blue) maps. We find that the profiles are consistent between MILCA and NILC. For comparison we also show as a blue dashed line the radial profile of a $10'$ gaussian beam. We observe that even for low-signal-to-noise and compact clusters we are able to detect extended emission. Thus, these maps could be used to extend the pressure profile analysis presented in [Planck Collaboration Int. V \(2013\)](#); [Durret \(2011\)](#) to fainter and higher redshift clusters.

One of the major outcomes of the NILC and MILCA y-maps is the possibility to study diffuse faint emission between clusters as well as the emission in the cluster outskirts. We show in Figure 8 some well known merging systems including the Shapley supercluster, and the A3395–A3391 and the A339–A401 interacting systems (see [Planck Collaboration et al., 2013](#), for a detailed description). We observe that the clusters themselves, their outskirts and the inter cluster emission are well reconstructed in the NILC and MILCA y-maps, which show consistent results. The quality of these maps will permit analyses

similar to the one presented in [Planck Collaboration et al. \(2013\)](#) with a significant increase of the signal-to-noise ratio.

4.5. SZ signal below the noise level

We use the catalog of 132684 clusters of galaxies identified from the Sloan Digital Sky Survey III ([Wen et al., 2012](#)) in order to quantify the tSZ signal below the noise level in the y -map. This catalogue provides estimates of cluster redshift, richness (N_{200}) and characteristic radius (r_{200}).

We focus on unresolved groups and clusters for which the richness is $8 \leq N_{200} \leq 100$. These objects are expected to be at signal-to-noise ratio well below 1 in the y -map and so their direct detection is not possible. However, their average tSZ signal can be detected using a stacking approach on the y -maps. Figure 9 shows the stacked maps (obtained with the *IAS stacking library*, [Bavouzet 2008](#); [Béthermin et al. 2010](#)) for 6 richness intervals with N_{200} going from 8 to 100, on patches of $4^\circ \times 4^\circ$, for the full sky NILC y -map. For the stacking we exclude all the positions for which point sources are found within a radius of 10 arcmin from the center of the object. The noise of the stacked maps scales as expected with $1/\sqrt{N}$ and the average signal increases for increasing richness. Then, when considering a sufficiently large number of objects, we are able to significantly detect the average SZ signal, even for small groups (Fig. 9). We obtain consistent results for the MILCA and NILC y -maps.

For the N_{200} intervals reported in Fig. 9 we have estimated the total stacked fluxes ($Y_{5r_{500}}$) as the integrated signal within a radius $5 \times r_{500}$, with $r_{500} = 0.7\langle r_{200} \rangle$, $\langle r_{200} \rangle$ being the mean of the r_{200} reported by [Wen et al. \(2012\)](#) for clusters belonging to each considered subsample. The average values and associated errors have been obtained with a bootstrap approach. For this, we have constructed and stacked cluster samples obtained by randomly replacing sources from the original sample, so that each of them contains a number of clusters equal to the initial one. By repeating the process several times, we have determined the statistical properties of the population being stacked. In Figure 10 (left panel) we report $Y_{5r_{500}}$ as a function of richness (N_{200}) for all the objects with $z \leq 0.42$. In fact higher redshift clusters present in this catalogue may have a biased lower richness because of incompleteness of member galaxies, as detailed in [Wen et al. \(2012\)](#). Following [Planck Collaboration et al. \(2011\)](#), we have fitted a power law of the form

$$Y_{5r_{500}} E_z^{-2/3} \left(\frac{D_A(z)}{500 \text{ Mpc}} \right)^2 = Y_{20} \left(\frac{N_{200}}{20} \right)^\alpha, \quad (4)$$

with $E(z)^2 = (H(z)/H_0)^2$ and D_A the angular diameter distance of the cluster.

By considering only $N_{200} \leq 60$ (for which the number of clusters in each richness bin is > 1000), we find a slope $\alpha = 2.21 \pm 0.10$, which is consistent with the scaling obtained by [Planck Collaboration et al. \(2011\)](#). We have verified that the scaling obtained is insensitive to whether we limit our cluster sample to high Galactic latitude objects or not, and that a change in the integration radius only affects the normalization Y_{20} . With $Y_{500} = Y_{5r_{500}}/1.79$ ([Planck Collaboration XXIX, 2014](#)), we obtain $Y_{20} = (8.07 \pm 0.41) \times 10^{-5} \text{ arcmin}^2$. However, for independent cluster datasets, different choices are made for the fainter magnitude of the member galaxies contributing to N_{200} . Then this may affect the richness associated to an object of given mass and complicate the comparison of the constant term Y_{20} for analyses that are based on different cluster datasets.

The mass-richness scaling relation,

$$M_{200} = M_0 \left(\frac{N_{200}}{20} \right)^\beta, \quad (5)$$

can then be used to also derive the Y_{500} - M_{tot} scaling (see Figure 10, right panel), by fitting a power law of the form

$$Y_{5r_{500}} E_z^{-2/3} \left(\frac{D_A(z)}{500 \text{ Mpc}} \right)^2 = Y_0 (M_{200})^B. \quad (6)$$

[Ford et al. \(2014\)](#) compares different results for the scaling of the mass with richness, in the form of Eq. 5. In particular they discuss those obtained by [Wen et al. \(2012\)](#), for a subsample of clusters with already known masses, and by [Covone et al. \(2014\)](#), from weak lensing mass measurements of 1,176 clusters of the catalogue used here. Assuming $\beta = 1.2 \pm 0.1$ and $M_0 = (1.1 \pm 1.1) \times 10^{14} M_\odot$ ([Wen et al., 2012](#); [Covone et al., 2014](#), and a ten percent error) in Eq. 5, we compute via a Monte Carlo approach the average M_{200} and associated uncertainties for each $Y_{5r_{500}}$ bin. From this we find $B = 1.92 \pm 0.42$ for the $Y_{5r_{500}}$ - M_{200} scaling (Eq. 6). This is consistent with the self-similar value (5/3) and with what is expected for this mass range according to simulations ([Sembolini et al., 2014](#)). Through a weak lensing analysis of $\gtrsim 18000$ clusters in the CFHTLenS (Canada-France-Hawaii Telescope Lensing Survey), [Ford et al. \(2014\)](#) obtain a steeper calibration for the mass-richness relation, with $\beta = 1.4 \pm 0.1$. For an higher β , the $Y_{5r_{500}}$ - M_{200} slope B gets lower ($B = 1.66 \pm 0.37$), but still consistent with the value obtained before. Again comparison of M_0 and Y_0 is complicated by the different choices of the fainter limit on galaxies contributing to N_{200} . By exploring the range $0.2 \lesssim z \lesssim 0.9$, [Ford et al. \(2014\)](#) finds no evolution with redshift. Thus, we do not expect our result to be biased by the $z \leq 0.42$ cut.

5. Angular power spectrum

We now consider the validation of the Compton parameter maps at the power spectrum level.

5.1. Power spectrum estimation

To estimate the power spectrum of the tSZ signal we use the XSPECT method ([Tristram et al., 2005](#)) initially developed for the cross-correlation of independent detector maps. XSPECT uses standard MASTER-like techniques ([Hivon et al., 2002](#)) to correct for the beam convolution and the pixelization, as well as the mode-coupling induced by masking foreground contaminated sky regions.

In the following, all the spectra will use a common multipole binning scheme, which was defined in order to minimize the correlation between adjacent bins at low multipoles and to increase the signal-to-noise at high multipole values. We will also only consider cross angular power spectra between the y -maps reconstructed from the first (F) and second (L) halves of the data. This allows us to avoid the bias induced by the noise in the auto angular power spectrum, the correction of which would require a large number of noise simulations. The cross angular spectra are named in the following NILC F/L and MILCA F/L. Error bars in the spectrum are computed analytically from the auto-power and cross-power spectra of the pairs of maps, as described in [Tristram et al. \(2005\)](#). We do not consider here higher order terms to the power spectrum variance. All of our Compton parameter maps assume a circular Gaussian beam of

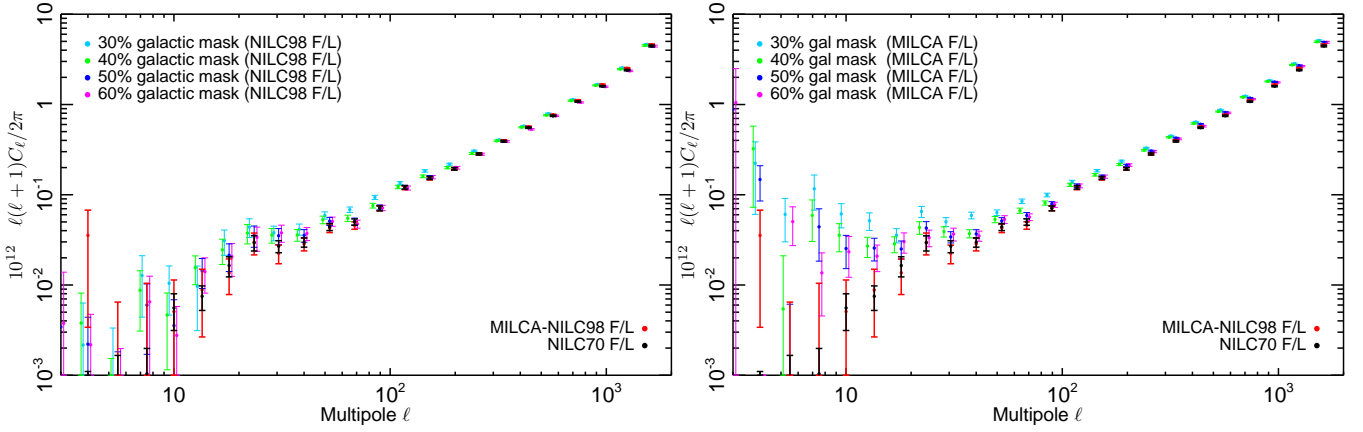


Fig. 11: Angular cross-power spectra of the *Planck* NILC F/L (left) and MILCA F/L (right) reconstructed Compton parameter maps for different Galactic masks corresponding to 30 % (cyan), 40 % (green), 50 % (blue) and 60 % (pink) of the sky. For comparison we also show MILCA-NILC F/L (red) and NILC70 F/L (black) on 50 % of the sky. See text for details.

10' FWHM. The additional filtering at large angular scales in the MILCA Compton parameter maps is also accounted for and deconvolved.

5.2. Foreground contamination

In *Planck Collaboration XXI (2014)* we have identified the dominant foreground contributions to the angular power spectrum of the reconstructed y -maps using the FFP6 simulated data set. We have repeated here the same analysis on updated simulated data sets (see Sect. 2.2) for which the description of foreground components has been improved according to our current knowledge (*Planck Collaboration XII, 2015*). We find no major difference between the two analyses and therefore we do not repeat the discussion here. At large angular scales the dominant foreground contribution is the Galactic thermal dust emission as we have already discussed in Section 4.3.1. At intermediate and small angular scales the major contribution comes from the clustered CIB emission. Equally important at small angular scales are the residual contribution from radio and IR sources.

5.2.1. Low-multipole contribution

Assuming that at large angular scales the Compton parameter maps are mainly affected by diffuse Galactic dust emission, we have tested several Galactic masks by imposing flux cuts on the *Planck* 857 GHz channel intensity map. In particular we investigated masking out 30%, 40%, 50% and 60% of the sky. The edges of these masks have been apodized to limit ringing effects on the reconstruction of the angular power spectrum. Figure 11 shows the power spectra for NILC (left) and MILCA (right). We observe that the MILCA F/L large angular scales power decreases when imposing a more severe masking (larger fraction of the sky is masked out). A similar effect, but significantly smaller, is also observed for the MILCA F/L cross power spectrum. The MILCA y -map is significantly more contaminated by thermal dust emission at multipoles below 30. However, we also observe for NILC F/L an extra noise contribution at large angular scales as discussed in Section 4.2. These two problems limit the reliability of the results at multipoles below 30.

To extend the measurement of the angular power spectrum of the tSZ emission to multipoles below 30 we have considered two options: 1) as in *Planck Collaboration XXI (2014)* we ap-

ply a more severe galactic mask (30 % of the sky is masked) before the computation of the NILC weights to produce the y -map (NILC70), and 2) compute the cross-correlation of NILC and MILCA y -maps. Considering 50% of the sky we show in Figure 11 the angular power spectrum of the NILC70 y -map (black) and the cross spectrum of the NILC first half and MILCA second half (NILC-MILCA F/L) y -maps. We observe that the two are compatible within error bars in the multipole range $10 < \ell < 1500$. As expected the cross spectrum NILC-MILCA F/L shows larger error bars.

Although the NILC70 y -map seems to be the best choice in terms of power spectrum estimation, it results in a significant reduction of the available sky area for other kind of studies as those presented in Section 4. Furthermore, it is difficult to accurately estimate the ultimate residual foreground contribution at very large angular scales. Because of this and to preserve the coherence of the delivered products and the analysis presented in this paper, we have chosen the cross angular power spectrum of NILC-MILCA F/L as a baseline. This is obviously a more conservative choice in terms of noise induced uncertainties. The NILC-MILCA F/L cross angular power spectrum bandpowers and uncertainties are further discussed in Sect. 7. Using the in-scan and cross-scan y -maps presented in Section 4.1 we find that stripe contamination accounts for less than 10% of the total signal in the NILC-MILCA F/L cross angular power spectrum. We have enlarged the error bars to account for this systematic effect.

5.2.2. High-multipole contribution

At small angular scales the measured tSZ power spectrum is affected by residual foreground contamination coming from clustered CIB emission as well as radio and IR point sources. They show up in the MILCA-NILC F/L cross power spectrum (see Figure 11) as an excess of power at large multipoles.

To deal with those we adopt the same strategy as in *Planck Collaboration XXI (2014)*. We define physically motivated models of the angular power spectrum of the foreground components for each observation channel, including cross correlations between channels. In contrast to *Planck Collaboration XXI (2014)* we also account for the cross correlation between the clustered CIB and the tSZ emission. A detailed description of this cross correlation as well as of the clustered CIB model is presented in *Planck Collaboration XXIII (2015)*. For the radio and IR point source models we refer to *Planck Collaboration XXI (2014)*.

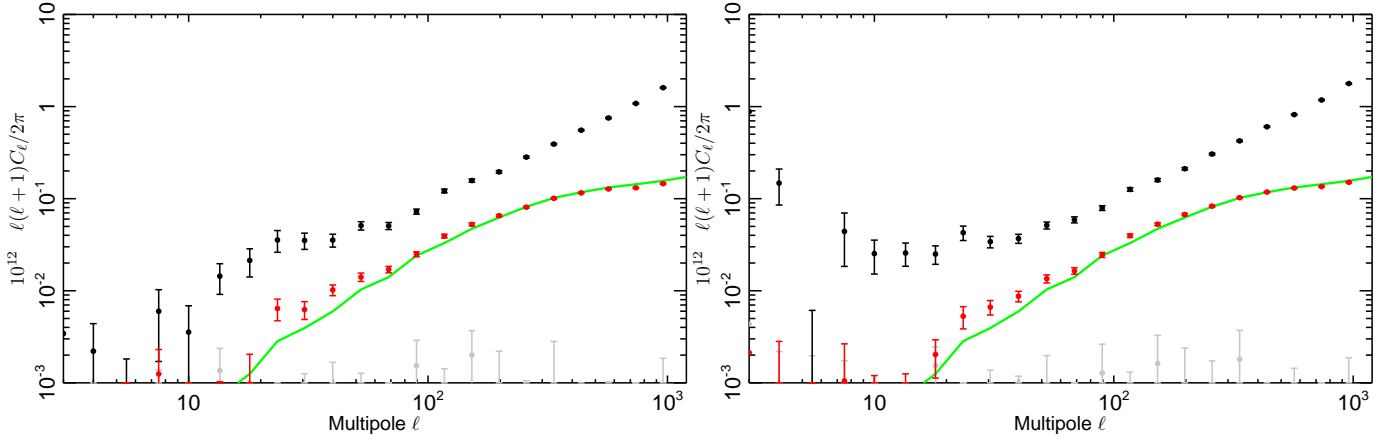


Fig. 12: Comparison of the tSZ angular power spectrum estimated from the cross-power-spectrum of the NILC (left) and MILCA (right) F/L maps (black) with the expected angular power spectrum of the confirmed clusters in the *Planck* Cluster Sample (green line). The angular cross-power spectrum between the NILCA and MILCA Compton parameter maps and the simulated detected cluster map is shown in red. The correlation between the reconstructed y-map and the simulated detected cluster map, to which an arbitrary rotation has been applied, is plotted in grey.

Using the models described above we compute Gaussian realizations of the foreground contribution for each HFI frequency channel between 100 and 857 GHz. Note that the LFI channels are only used at large angular scales. We apply the MILCA or NILC weights to these simulated maps. From these simulations we find that the cross correlation between the CIB and tSZ contribution can be neglected to first order with respect to the others and it will therefore not be considered hereafter. Uncertainties on the parameters describing the foreground models were also propagated using simulations. We find that the clustered CIB model uncertainties might be as large as 50% in amplitude. In addition, we notice that the amplitude of the point source models can vary significantly with the point source mask applied. These uncertainties are taken into account hereafter. The amplitude of the residual foreground models are jointly fitted with the cosmology-dependent tSZ model, as detailed in Sect. 7.1.

5.3. Contribution of resolved clusters to the tSZ power spectrum

We simulate the expected Compton parameter map for the detected and confirmed clusters of galaxies in the *Planck* catalogue (Planck Collaboration XXIX, 2014) from their measured integrated Compton parameter, Y_{5r500} and redshift, z . We assume hydrostatic equilibrium and an Arnaud et al. (2010) pressure profile. The green solid line in Fig. 12 shows the power spectrum of this simulated map. Figure 12 also shows the cross-power spectra of the NILC and MILCA F/L maps (in black). We also compute the cross-power spectrum of the simulated cluster map and the *Planck* reconstructed NILC and MILCA Compton parameter maps. This is shown in red in the figure. Here again, the signal is consistent with the expected power spectrum of the confirmed *Planck* clusters of galaxies. These results show that the tSZ signal from clusters is preserved in the y-maps.

6. Higher order statistics

The power spectrum analysis presented above only provides information on the 2-point statistics of the Compton parameter distribution over the sky. An extended characterization of the field can be performed by studying the higher-order moments in the

1D PDF of the map, or by measuring 3-point statistics, i.e., the bispectrum.

6.1. 1D PDF analysis

Following Planck Collaboration XXI (2014) we perform an analysis of the 1D PDF of the NILC and MILCA reconstructed Compton parameter maps. For the tSZ effect we expect an asymmetric distribution with a significantly positive tail (Rubiño-Martín & Sunyaev, 2003). We thus focus on the asymmetry of the distribution and its unnormalized skewness. First, we filter the maps in order to enhance the tSZ signal with respect to foreground contamination and noise. We apodise the combined PSMASK and Galactic mask to avoid residual point source ringing. We follow the approach of Wilson et al. (2012) and use a filter in harmonic space. For each multipole ℓ , the filter is constructed as the ratio between the angular power spectrum of the expected tSZ signal (C_ℓ^{tSZ} , obtained from the simulations in Sect. 2.2) and the power spectrum of the half-difference y maps (C_ℓ^{N} , see Sect. 4.2) such that $F_\ell = C_\ell^{\text{tSZ}}/C_\ell^{\text{N}}$. We smooth this filter function in multipole space using a 21-point square kernel and normalize it to one. Notice that this filter only selects the multipole range for which the tSZ signal is large with respect to the noise, and thus, it does not modify significantly the non-Gaussianity properties of the y-maps. Furthermore, we have found that the filter used here behaves better than the more traditionally used Wiener filter, as it is less affected by point-source ringing. Following this procedure, the 1D PDF of the filtered Compton parameter maps, $P(y)$, is computed from the histogram of the pixels. As for the power spectrum, several Galactic masks have been considered in order to test the robustness of the results.

Figure 13 shows the 1D PDF for the NILC (left) and MILCA (right) Compton parameter map in red when masking 50% of the sky. Each of them corresponds to the convolution of the 1D PDF of the different components in the map: the tSZ effect; foregrounds; and the noise. The 1D PDF of the NILC and MILCA y-maps clearly show three distinct contributions: a Gaussian central part that is slightly wider than the noise contribution, as expected from the half-difference map 1D PDF (black curve); a small negative tail, corresponding most likely to residual radio

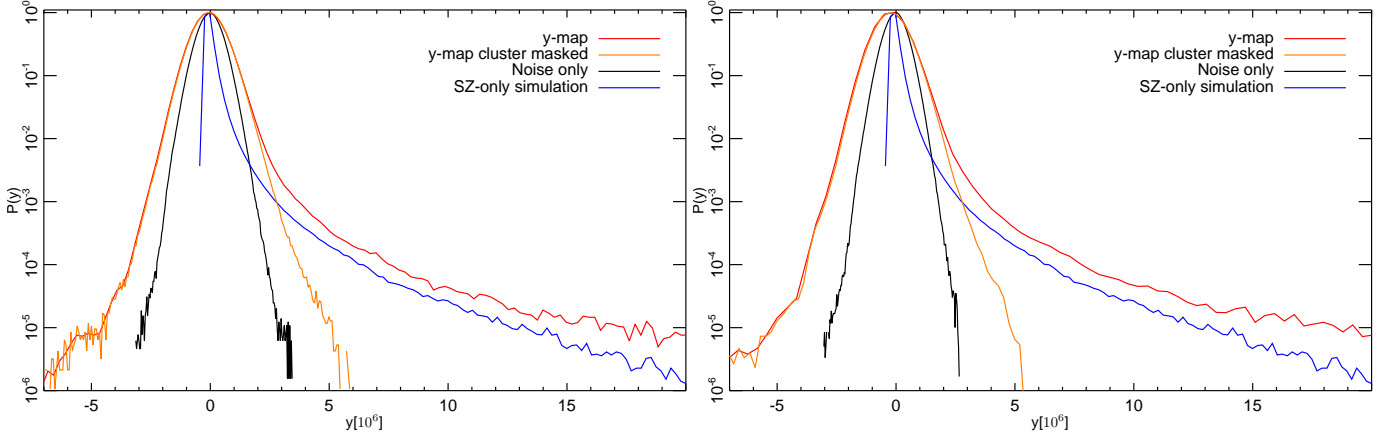


Fig. 13: 1D PDF of the *Planck* y -map before (red) and after (orange) masking the PSZ2 clusters, and of the half-difference map (black) for the NILC (left) and MILCA (right) methods. We also show for comparison the 1D PDF of the simulated PSZ2 cluster map (dark blue).

sources; and a positive tail corresponding mainly to the tSZ signal as observed for the PSZ2 cluster simulated map (dark blue). In comparison to the [Planck Collaboration XXI \(2014\)](#) we find now a better agreement between the NILC and MILCA results. This is mainly due to the improved masking of radio sources presented in Section 4.4.1. Finally we also show the 1D PDF of the reconstructed y -maps after masking the PSZ2 clusters (orange). We observe that most of the tSZ is removed, indicating that the 1D PDF of the y -map is dominated by detected clusters.

A simple analysis of the measured 1D PDF can be performed by considering the asymmetry of the distribution:

$$A \equiv \int_{y_p}^{+\infty} P(y) dy - \int_{-\infty}^{y_p} P(y) dy, \quad (7)$$

where y_p is the peak value of the normalized PDF $P(y)$. In addition, the non-Gaussianity of the positive tail can be quantified by

$$\Delta = \int_{y_p}^{+\infty} [P(y) - G(y)] dy, \quad (8)$$

with $G(y)$ the expected PDF if fluctuations were only due to noise. The latter can be obtained from the half-difference y -maps.

Masking 60 % of the sky, we find $A = 0.218$ and $\Delta = 0.10$ for the NILC Compton parameter map. Equivalently, for the MILCA Compton parameter map we find $A = 0.223$ and $\Delta = 0.11$. These results are in agreement and consistent with a positive tail in the 1D PDF, confirming the tSZ nature of the signal. The agreement between the NILC and MILCA results degrade when reducing the masked area as a consequence of a larger foreground contribution in the MILCA y -map. See [Hill et al. \(2014\)](#) for a similar analysis conducted on ACT data.

6.2. Bispectrum

Since the SZ signal is non-Gaussian, significant statistical information is contained in the bispectrum, complementary to the power spectrum ([Rubiño-Martín & Sunyaev, 2003](#); [Bhattacharya et al., 2012](#)). Results on SPT data have been obtained by [Crawford et al. \(2014\)](#) and [George et al. \(2014\)](#). The bispectrum also provides an additional statistic to assess the compatibility of the NILC and MILCA reconstructed Compton

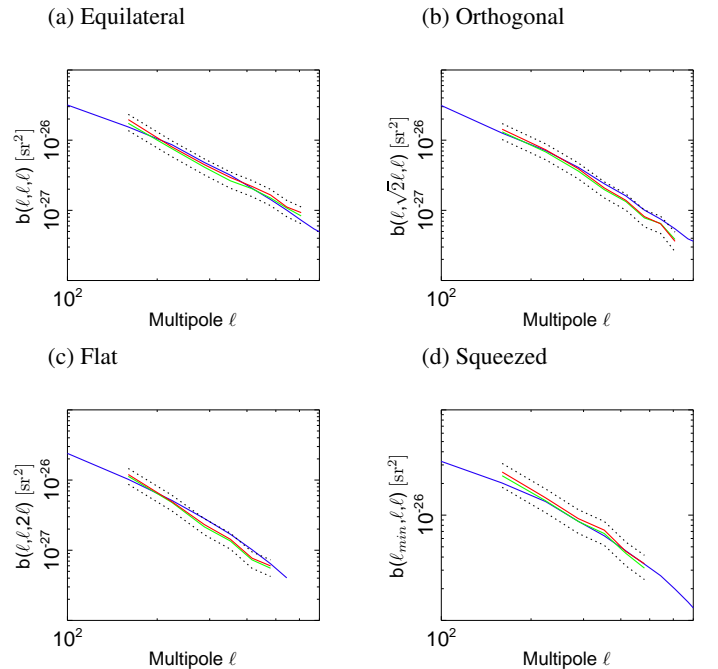


Fig. 14: Bispectra of the NILC (green) and MILCA (red) y -maps for four different configurations (equilateral, orthogonal, flat and squeezed), compared with the bispectrum of the projected map of the PSZ2 clusters (blue). $\pm 1\sigma$ uncertainties are indicated as black dotted lines.

parameter maps, as well as their reliability in terms of foreground contamination.

We therefore analyze the bispectra of the NILC and MILCA maps. The estimation method is essentially the same as for the 2013 results ([Planck Collaboration XX, 2014](#)), briefly re-capped here. We use the binned bispectrum estimator described in [Bucher et al. \(2010\)](#) and [Lacasa et al. \(2012\)](#), which is also used for the *Planck* primordial non-Gaussianity analysis ([Planck Collaboration XXIV, 2014](#); [Planck Collaboration XVII, 2015](#)). We use a multipole bin size $\Delta\ell = 64$ and a maximum multipole $\ell_{\max} = 2048$ for the analysis, working at a resolution $N_{\text{side}} = 1024$ to reduce computing time. The NILC and MILCA

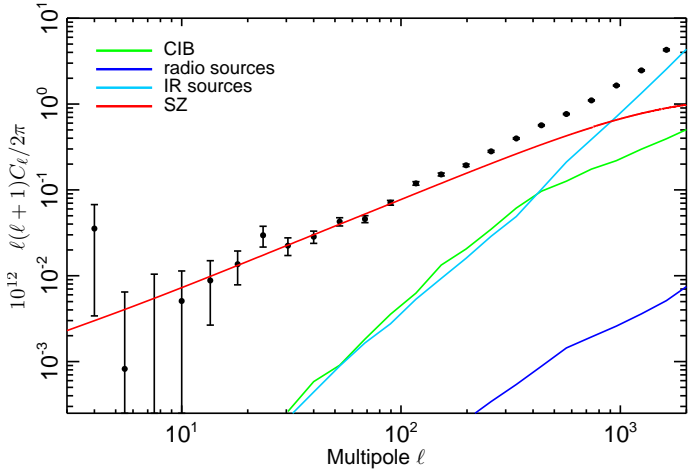


Fig. 15: NIILC - MILCA F/L cross-power spectrum (black) compared to the power spectra of the physically motivated foreground models. The considered foregrounds are: clustered CIB (green line); infrared sources (cyan line); and radio sources (blue line). Additionally, the best-fit tSZ power spectrum model presented in Sect. 7.1 is also plotted as a solid red line.

maps are masked with the combination of PSMASK, described in Sect. 4.4.1, and a Galactic mask at 50, 60 or 70%, described in Sect. 5.2.1 (in the rest of this section we will simply denote as X% mask the combination of PSMASK and the Galactic mask at X%). The best-fit monopole and dipole outside the mask are finally removed before estimation.

An important part of the pipeline is then to correct for the bias introduced by masking. To this end, we compute the ratio of the full-sky and masked sky bispectra, on highly non-Gaussian simulations with a tSZ-like bispectrum and a $10'$ resolution. This ratio is used to correct the measured bispectra and flag unreliable (ℓ_1, ℓ_2, ℓ_3) configurations. Specifically we flag configurations where the ratio is different by $> 25\%$ from the naive expectation $f_{\text{SKY}} B(\ell_1) B(\ell_2) B(\ell_3)$, where $B(\ell)$ is the Gaussian $10'$ beam.

For both NIILC and MILCA, we find that the bispectra computed on the 50, 60 and 70% masks are consistent. This indicates that there is no detectable residual galactic contamination in these bispectra. However we did find Galactic contamination on less aggressive Galactic masks, specifically positive Galactic dust. As Galactic dust is highly non-Gaussian, we warn the use against the measurement of higher order statistics using Galactic masks smaller than 50%. In the following we adopt the 50% mask as baseline, as it leaves the most sky available for estimation and minimizes masking effects in the measurement.

Figure 14 shows the obtained bispectra as a function of multipole for the NIILC (green) and MILCA (red) Compton parameter maps. We observe a good agreement between the bispectra of the two maps, and the bispectral behaviour is consistent with that expected from a tSZ signal (see e.g. Lacasa, 2014, chapter 5). We furthermore compare these measurements with the bispectrum of the simulated map for the PSZ2 clusters, which is presented in blue in Fig. 14. We observe a good agreement between the bispectra of the NIILC and MILCA and that of the PSZ2 clusters. We therefore conclude that the observed bispectrum in the y-map is dominated by detected clusters.

Finally, in Fig. 14 are shown the $\pm 1\sigma$ uncertainties of the measurements, in black dotted lines. The error bars were computed in a similar manner to that of the 2013 results (Planck

Table 2: Marginalized bandpowers of the angular power spectrum of the *Planck* tSZ Compton parameter map (in dimensionless $(\Delta T/T)^2$ units), statistical and foreground errors, and best-fit tSZ power spectrum and number counts models (also dimensionless).

ℓ_{\min}	ℓ_{\max}	ℓ_{eff}	$\ell(\ell+1)C_\ell/2\pi$ [10^{12}y^2]	σ_{stat} [10^{12}y^2]	σ_{fg} [10^{12}y^2]	Best-fit [10^{12}y^2]
9	12	10.0	0.00506	0.00629	0.00002	0.00726
12	16	13.5	0.00876	0.00615	0.00007	0.00984
16	21	18.0	0.01353	0.00579	0.00015	0.01320
21	27	23.5	0.02946	0.00805	0.00021	0.01737
27	35	30.5	0.02191	0.00522	0.00053	0.02274
35	46	40.0	0.02744	0.00464	0.00109	0.03008
46	60	52.5	0.04093	0.00468	0.00172	0.03981
60	78	68.5	0.04227	0.00429	0.00320	0.05236
78	102	89.5	0.06463	0.00454	0.00567	0.06901
102	133	117.0	0.10738	0.00562	0.00969	0.09102
133	173	152.5	0.12858	0.00594	0.01889	0.11956
173	224	198.0	0.15696	0.00611	0.02895	0.15598
224	292	257.5	0.21738	0.00687	0.04879	0.20306
292	380	335.5	0.28652	0.00824	0.08374	0.26347
380	494	436.5	0.36682	0.00958	0.13524	0.33848
494	642	567.5	0.42666	0.01242	0.19500	0.42930
642	835	738.0	0.53891	0.01645	0.27718	0.53577
835	1085	959.5	0.71103	0.02402	0.37576	0.65454
1085	1411	1247.5	0.82294	0.04172	0.55162	0.77885

Collaboration XX, 2014), see Appendix A.3 for a more detailed discussion.

With a detection per configuration at an average significance of 3.5σ , and a total significance of $\sim 60\sigma$, the *Planck* data thus provide a high quality measurement of the non-Gaussianity of the thermal Sunyaev-Zel'dovich signal, with undetectable contamination from foregrounds.

7. Cluster physics and cosmology

7.1. Power spectrum analysis

7.1.1. tSZ power spectrum modelling

As a measure of structure growth, the tSZ power spectrum can provide independent constraints on cosmological parameters. As shown by Komatsu & Seljak (2002), the power spectrum of the tSZ effect is highly sensitive to the normalization of the matter power spectrum, commonly parameterized by the rms of the $z = 0$ mass distribution on $8 h^{-1}$ Mpc scales, σ_8 , and to the total amount of matter Ω_m . We expect the tSZ power spectrum to also be sensitive to other cosmological parameters, e.g., the baryon density parameter Ω_b , the Hubble constant H_0 , and the primordial spectral index n_s . For reasonable external priors on those parameters, however, the variations are expected to be negligible with respect to those introduced by changes in Ω_m and σ_8 and so they are not considered here.

Following Planck Collaboration XXI (2014) we consider here a two-halo model for the tSZ power spectrum, which is fully described in Appendix A.1. This model accounts for both intra-halo (1-halo term) and inter-halo (2-halos) correlations.

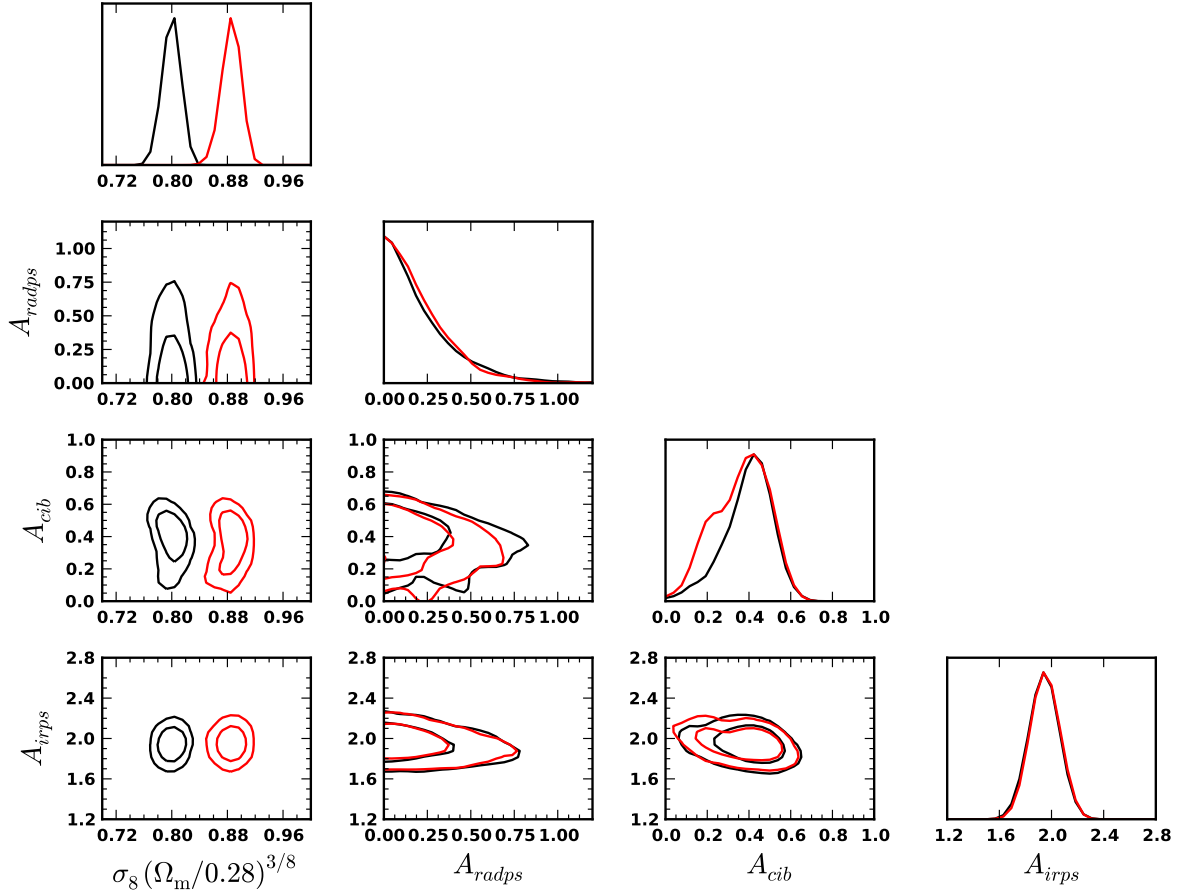


Fig. 16: 2D and 1D likelihood distributions for the combination of cosmological parameters $\sigma_8(\Omega_m/0.28)^{3/8}$, and for the foreground parameters $A_{\text{Rad,PS}}$, A_{CIB} and $A_{\text{IR,PS}}$. We show the 68.3% and 95.4% C.L. contours. The red and black contours correspond to a fixed mass bias of 0.2 and 0.4 respectively.

Following Eq. (A.6), the tSZ spectrum is computed using the 2-halo model, the Tinker et al. (2008) mass function, and the Arnaud et al. (2010) pressure profile. In particular, we use the numerical implementation presented in Taburet et al. (2009, 2010, 2011), and integrating in redshift from 0 to 3 and in mass from $10^{13} M_\odot$ to $5 \times 10^{15} M_\odot$. Our model allows us to compute the tSZ power spectrum at the largest angular scales. It is consistent with the tSZ spectrum presented in Efstathiou & Migliaccio 2012 (EM12), which was used as a template in the CMB cosmological analysis in Planck Collaboration XVI (2014) and Planck Collaboration XI (2015). We also include the mass bias parameter, b , which accounts for bias between the observationally deduced (M^{obs}) and true (M^{true}) mass of the cluster (see Planck Collaboration XX, 2014, for details) such that $M^{\text{obs}} = (1 - b)M^{\text{true}}$.

Cosmological parameter results are very sensitive to the mass bias and in particular we expect σ_8 and Ω_m to be strongly degenerated with b (Planck Collaboration XXI, 2014). By contrast to Planck Collaboration XXIV (2015), for which external priors in the mass bias have been used, we consider here only two distinct values: $b = 0.2$ and $b = 0.4$. The former corresponds to the average value that numerical simulations seem to indicate

(Fig. A.2 in Planck Collaboration XX, 2014). The latter value for the bias alleviates the inconsistency with the constraints derived from the analysis based on primary CMB anisotropies (see Planck Collaboration XX, 2014).

This value is however larger than that obtained by mass comparison of clusters present in both the Planck cosmology sample (Planck Collaboration XX, 2014) and the *Weighing the Giants* (WtG von der Linden et al., 2014) project. Even if studies based on lensing mass measurements still provide different and inconsistent results for the cluster mass calibration, their number and their accuracy has incredibly improved in the very recent past (*i.e.* Mahdavi et al., 2013 for the CCCP project, Umetsu et al., 2014 for CLASH, Israel et al., 2014 for 400d WL, Ford et al. (2014) for CFHTLenS, Gruen et al., 2014 for WISCy) and they are expected to provide useful information.

7.1.2. Maximum likelihood analysis

As in Planck Collaboration XXI (2014), cosmological constraints are obtained from a fit of the tSZ power spectrum. As discussed in Section 5.2 we take the NILC-MILCA F/L cross-power spectrum (black dots in Figure 15) as a reference and limit

the analysis to 50% of the sky to minimize foreground residuals. In terms of astrophysical signal we consider a four-component model: tSZ, clustered CIB, radio point sources, and infrared point sources. We restrict the analysis to multipoles $\ell > 10$ so that we can neglect the residual thermal dust contamination (see Section 5.2.1). For $\ell > 2000$ the total signal in the tSZ map is dominated by correlated noise which is also accounted for in the fit. Because of this correlated noise and the expected high value of foreground contamination we limit the fit to multipoles $\ell < 1411$. Finally, the observed y -map power spectrum, C_ℓ^m , is modelled as:

$$C_\ell^m = C_\ell^{\text{tSZ}}(\Omega_m, \sigma_8) + A_{\text{CIB}} C_\ell^{\text{CIB}} + A_{\text{IR}} C_\ell^{\text{IR}} + A_{\text{Rad}} C_\ell^{\text{rad}} + A_{\text{CN}} C_\ell^{\text{CN}}. \quad (9)$$

Here $C_\ell^{\text{tSZ}}(\Omega_m, \sigma_8)$ is the tSZ power spectrum (in red in Fig. 15), C_ℓ^{CIB} is the clustered CIB power spectrum (in green), and C_ℓ^{IR} and C_ℓ^{rad} are the infrared and radio source power spectra, respectively (in cyan and in blue). C_ℓ^{CN} is an empirical model for the high multipole correlated noise.

Foreground contamination is modelled following Sect. 5.2.2. As discussed there, the main uncertainties in the residual power spectrum translate into up to 50% uncertainty in the amplitude of the clustered CIB. We have not considered in the analysis the CIB-tSZ cross-correlation that was proved to be negligible in terms of power spectrum. The amplitude of the IR and radio point-source contribution will depend very much on the exact Galactic mask used for the analysis. However, we expect the shape of their power spectra to remain the same. We thus allow for a variation of the normalization amplitudes for the clustered CIB, A_{CIB} , and for the point sources, A_{IR} and A_{rad} .

We assume a Gaussian approximation for the likelihood function. Best-fit values and uncertainties are obtained using an adapted version of the `CosmoMC` algorithm (Lewis & Bridle, 2002). Only σ_8 and Ω_m are allowed to vary. All other cosmological parameters are fixed to their best-fit values as obtained in Table 2 of Planck Collaboration XVI (2014). The normalization amplitudes, A_{CIB} , A_{rad} and A_{IR} , considered as nuisance parameters, are allowed to vary between 0 and 3. For the range of multipoles considered here, the tSZ angular power spectrum varies like $C_\ell \propto \sigma_8^8 \Omega_m^3$. The results are thus presented in terms of this parameter combination.

7.2. Best-fit parameters and tSZ power spectrum

Figure 16 presents the 2D and 1D likelihood distributions for the cosmological parameter combination $\sigma_8(\Omega_m/0.28)^{3/8}$ and for the foreground nuisance parameters. We present the results obtained assuming a mass bias of 0.2 (black) and 0.4 (red). We obtain very similar values for the nuisance parameters in both cases. In particular the best-fit values for a mass bias of 0.2 are $A_{\text{CIB}} = 0.29^{+0.34}_{-0.20}$, $A_{\text{rad}} = 0.01^{+0.70}_{-0.01}$ and $A_{\text{IR}} = 1.97^{+0.20}_{-0.30}$. However, there is a significant shift in the value of $\sigma_8(\Omega_m/0.28)^{3/8}$ as one would expect (Planck Collaboration XX, 2014). In the case of a mass bias of 0.2 we have $\sigma_8(\Omega_m/0.28)^{3/8} = 0.80^{+0.01}_{-0.03}$, while for a mass bias of 0.4 we have $\sigma_8(\Omega_m/0.28)^{3/8} = 0.90^{+0.01}_{-0.03}$. Notice that these values are obtained in a specific framework: all other cosmological parameters being fixed and a fiducial fixed model used for the signals. Relaxing this framework would likely weaken the constraints presented here as discussed below.

Figure 15 shows the NILC-MILCA F/L angular cross-power spectrum before correcting (black dots) for foreground contribution. We also show the best-fit foreground models: clustered

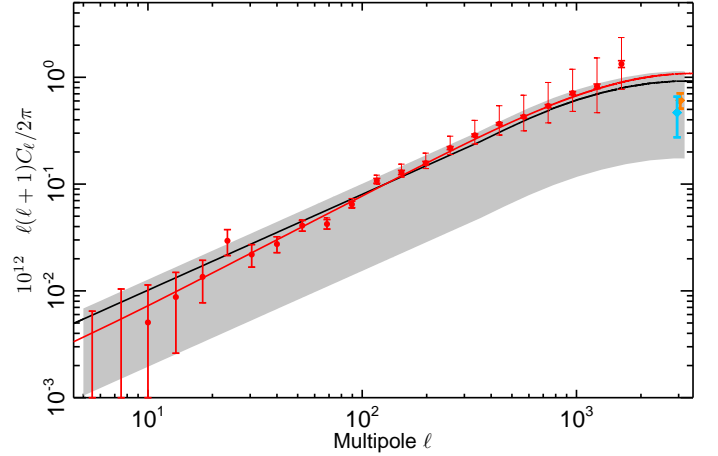


Fig. 17: NILC - MILCA F/L cross-power spectrum after foreground subtraction (red points), compared to the Atacama Cosmology Telescope (ACT; cyan dot) and the South Pole Telescope (SPT; orange, George et al., 2014) power spectrum estimates. The black line shows the tSZ power spectrum template (EM12 Efstathiou & Migliaccio, 2012) used in the *Planck* CMB cosmological analysis (Planck Collaboration XVI, 2014; Planck Collaboration XI, 2015) with its best fit amplitude A_{tSZ} (Planck Collaboration XI, 2015), the grey region allows comparison with the 2σ interval.

CIB (green line), and radio (blue line) and IR (cyan line) point sources. The statistical (thick line) and total (statistical plus foreground, thin line) are also shown. The best-fit tSZ power spectrum is presented as a solid red line. We conclude that the NILC-MILCA F/L angular cross-power spectrum is dominated by tSZ for multipoles $\ell < 700$, and by foreground contribution for multipoles $\ell > 1200$. We also note that for the best-fit model the radio point-sources contribution seems to be negligible with respect to the IR one. This is not a physical result and it is most probably explained by the strong degeneracy observed between the radio and IR point-source amplitude (see Fig. 16).

Finally we present in Figure 17 the NILC-MILCA F/L angular cross-power spectrum after correcting for foreground contribution (red dots). Uncertainties account for statistical and systematic errors as well as for uncertainties in the foreground subtraction. The marginalized bandpowers and uncertainties are also presented in Table 2. We note that foreground induced uncertainties dominate at multipoles $\ell > 100$. Bandpowers for the best-fit model for the angular tSZ power spectrum are also given for comparison. We also show in the Figure 17 tSZ power spectrum estimates at high multipoles obtained in CMB oriented analyses by the Atacama Cosmology Telescope (ACT; cyan dot) and the South Pole Telescope (SPT; orange, George et al., 2014). The black line shows the tSZ power spectrum template (EM12 Efstathiou & Migliaccio, 2012) used in the *Planck* CMB cosmological analysis (Planck Collaboration XVI, 2014; Planck Collaboration XI, 2015) assuming the best-fit amplitude A_{tSZ} and the grey region 2σ uncertainties from Planck Collaboration XI (2015). We observe that the amplitude of the tSZ signal found in this paper is consistent with the high multipole based measurements.

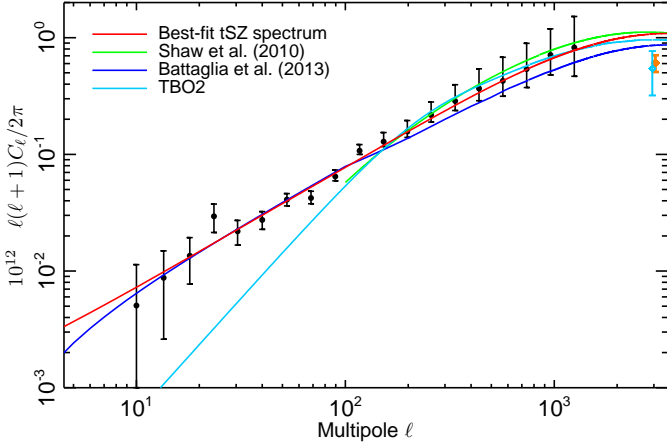


Fig. 18: tSZ power spectrum for existing models in the literature. N1LC-MILCA F/L cross-power spectrum after foreground correction (black dots) compared to the Atacama Cosmology Telescope (ACT; cyan dot) and the South Pole Telescope (SPT; orange, [George et al., 2014](#)) power spectrum estimates. We also show the tSZ power spectrum models from hydrodynamic simulations ([Battaglia et al., 2012](#), blue), from N -body simulations plus semi-analytical dust gas models ([Trac et al., 2011](#), cyan; TBO2), and from analytical calculations ([Shaw et al. 2010](#), green).

7.2.1. Cluster physics dependence

As discussed in [Planck Collaboration XXI \(2014\)](#), we also expect the tSZ power spectrum amplitude to be sensitive to the physics of clusters of galaxies. To explore this dependence we have considered a set of predicted tSZ spectra for various physical models. In [Fig. 18](#) we compare these models to the foreground cleaned *Planck* tSZ power spectrum derived above (grey dots), as well as to the Atacama Cosmology Telescope (ACT; cyan dot) and the South Pole Telescope (SPT; orange, [George et al., 2014](#)) power spectrum estimates. We consider the predictions derived from hydrodynamical simulations ([Battaglia et al., 2010](#); [Battaglia et al., 2012](#), blue), from N -body simulations plus semi-analytical models ([Trac et al., 2011](#), cyan; TBO2) and from analytical calculations ([Shaw et al. 2010](#), green). These models were originally computed for the set of cosmological parameters in [Hinshaw et al. \(2012\)](#) with $\sigma_8 = 0.8$ and have been rescaled in amplitude to our best-fit value for $\sigma_8^8 \Omega_m^3$. We note that there is some dispersion in the predicted amplitudes and shapes of the tSZ power spectrum. These differences reflect the range of methodologies and assumptions used both in the physical properties of clusters and in the technical details of the computation. The latter includes differences in the redshift ranges and also in the mass intervals probed by the limited sizes of the simulation boxes of the hydrodynamical simulations. Analytical predictions are also sensitive to the model ingredients, such as the mass function, mass bias and scaling relations adopted.

We see from [Fig. 18](#) that the models presented above (the tSZ template for CMB analyses, plus the [Battaglia et al. 2012](#), [Shaw et al. 2010](#) and TBO2 models) provide reasonable fits to the data for multipoles above 200. For lower multipoles the [Shaw et al. 2010](#) and TBO2 models are not consistent with the data.

We have also performed a simplified likelihood analysis to evaluate the uncertainties in cosmological parameters induced by the uncertainties in the modelling of the cluster physics. We

replace our own model of the tSZ power spectrum by the models discussed above and recompute $\sigma_8(\Omega_m/0.28)^{3/8}$, A_{CIB} , A_{Rad} and A_{IR} from a simple linear fit to the N1LC-MILCA F/L cross-power spectrum. In the case of mass bias of 0.2, we obtain values for $\sigma_8(\Omega_m/0.28)^{3/8}$ between 0.77 and 0.80, which lie within the 1σ uncertainties (0.03) presented above.

In the case of our fiducial model (see [Appendix A.1](#)) we can also consider uncertainties in the parameters describing the scaling relations allowing us to relate the observed tSZ flux to the mass of the cluster for a given redshift. Following [Eq. \(7\)](#) in [Planck Collaboration XXVIII \(2014\)](#) the main parameters to be considered are the mass bias b , the overall amplitude Y_* and the scaling slope β . As discussed above the mass bias is fully degenerate with σ_8 . Similar conclusions can be drawn for Y_* , which is expected to be known at the percent level (see [Table 1](#) in [Planck Collaboration XXVIII \(2014\)](#)) and therefore it is subdominant with respect to the uncertainties in the mass bias. Although the uncertainties in the slope of the scaling relation are relatively large, we have checked that they lead to negligible uncertainties on cosmological parameters.

7.3. Higher order statistics

7.3.1. Skewness measurements

The skewness of the 1D PDF distribution, $\int y^3 P(y) dy / (\int y^2 P(y) dy)^{3/2}$ can also be used to derive constraints on cosmological parameters. Following [Wilson et al. \(2012\)](#); [Planck Collaboration XXI \(2014\)](#) we have chosen a hybrid approach, by computing the skewness of the filtered Compton parameter maps outside the 50% sky mask. In particular, we have computed the skewness of the *Planck* data Compton parameter maps $\langle y^3 \rangle$, and of the half-difference maps $\langle y_N^3 \rangle$.

Using the models presented in [Sect. A](#) we can show that the unnormalized skewness of the tSZ fluctuation, $\langle T^3(\mathbf{n}) \rangle$ scales approximately as σ_8^{11} , whereas the amplitude of the bispectrum scales as σ_8^α with $\alpha = 11-12$, as shown by [Bhattacharya et al. \(2012\)](#). In the following we do not consider the dependency of the bispectrum and the unnormalized skewness on other cosmological parameters, since such dependencies are expected to be significantly lower than for σ_8 ([Bhattacharya et al., 2012](#)).

We derive constraints on σ_8 by comparing the measured unnormalized skewness and bispectrum amplitudes with those obtained from simulations of the tSZ effect. The tSZ contribution was obtained from a hybrid simulation including a hydrodynamic component for $z < 0.3$ plus extra individual clusters at $z > 0.3$, and with $\sigma_8 = 0.789$. This approach is strongly limited by systematic uncertainties and the details of the theoretical modelling (see [Hill & Sherwin, 2013](#)). Uncertainties due to foreground contamination are computed using the simulations and are accounted for in the final error bars.

We obtain $\sigma_8 = 0.77$ for N1LC and $\sigma_8 = 0.78$ for MILCA. Combining the two results and considering model and foreground uncertainties we obtain $\sigma_8 = 0.78 \pm 0.02$ (68% C.L.). Notice that the reported uncertainties are mainly dominated by foreground contamination. However the model uncertainties only account for the expected dependence of the unnormalized skewness upon σ_8 , as shown in [Appendix A](#). We have neglected, as was also the case in [Wilson et al. \(2012\)](#), the dependence on other cosmological parameters. We have also not considered any uncertainties coming from the combination of the hydrodynamical and individual cluster simulations. Because of these limitations, our error bars might be underestimated.

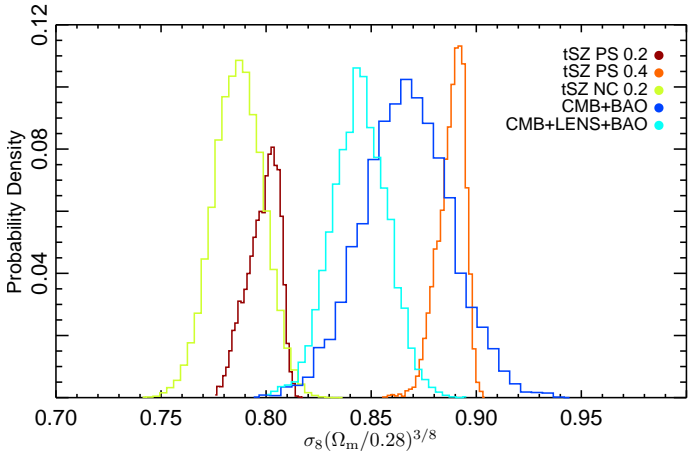


Fig. 19: Marginalised likelihood distribution for $\sigma_8(\Omega_m/0.28)^{3/8}$ for tSZ and CMB based analyses. We represent the tSZ power spectrum analysis results assuming a mass bias, b , of 0.2 (red) and 0.4 (orange), the cluster number count analysis results (green; [Planck Collaboration XXIV, 2015](#)), and the combined *Planck* CMB and BAO analysis ([Planck Collaboration XIII, 2015](#)) with (cyan) and without (blue) extra lensing constraints.

7.3.2. Fit of the 1D PDF distribution

We also derived constraints on σ_8 by fitting the 1D PDF obtained in Sect. 6.1. Here, we follow the formalism described in [Hill et al. \(2014\)](#) that evaluates the tSZ 1D PDF theoretically integrating across individual cluster contributions. We use the [Tinker et al. \(2008\)](#) mass function and the [Arnaud et al. \(2010\)](#) pressure profile. The later is normalised following the $Y-M$ scaling relations described in [Planck Collaboration XX \(2014\)](#), and considering a mass bias parameter of $b = 0.2$. All cosmological parameters are fixed to the *Planck* 2015 CMB analysis best-fit values, and we fit only for σ_8 .

We note that the [Hill et al. \(2014\)](#) formalism explicitly neglects any effects due to overlapping clusters along the line of sight. For this reason, and given the uncertainties in the modeling of the foreground residuals, the best-fit solution to the observed 1D PDF is fitted in the region which is dominated by non-overlapping cluster and where the noise and foregrounds contributions are minimal. In our case, we use $y > 4.5 \times 10^{-6}$.

The confidence limits on σ_8 are obtained from a maximum likelihood approach, in which the likelihood has a multivariate Gaussian shape with a covariance matrix which only depends on σ_8 . This covariance matrix is evaluated numerically, accounting only for Poisson terms (both for pixel to pixel and due to the correlations introduced by the cluster's y -profile). We obtain $\sigma_8 = 0.77 \pm 0.02$ (68 % C.L.) both for NILC and MILCA maps including statistical and systematic uncertainties.

7.4. Comparison to other *Planck* cosmological probes

We have shown in Figure 17 that the amplitude of the tSZ power spectrum measured in this paper and from the *Planck* CMB analysis are in good agreement. However, the *Planck* 2013 results ([Planck Collaboration XX, 2014](#)) have shown tension between CMB and tSZ derived constraints on σ_8 for wide range of experiments including *Planck*. Figure 19 shows the marginalised likelihood distribution for $\sigma_8(\Omega_m/0.28)^{3/8}$ as obtained from the combined *Planck* CMB and BAO analysis ([Planck Collaboration](#)

[XIII, 2015](#)) with (cyan) or without (blue) lensing constraints. We also presents the results obtained for the *Planck* 2015 cluster number count analysis assuming a mass bias of 0.2 (green; [Planck Collaboration XXIV, 2015](#)), and for the tSZ power spectrum analysis in this paper assuming a mass bias of 0.2 (red) and 0.4 (orange). We observe that assuming a mass bias of 0.2 the two tSZ analyses are in good agreement but the tension with the CMB measurements remains. This tension can be alleviated by assuming a larger mass bias that increases the value of $\sigma_8(\Omega_m/0.28)^{3/8}$. Furthermore, we find that including lensing constraints leads to smaller values of $\sigma_8(\Omega_m/0.28)^{3/8}$, which as a consequence are in better agreement with the tSZ results. From this we can conclude that the LSS data would have a marginal preference for small values of the mass bias.

8. Summary and conclusions

Because of its wide frequency coverage from 30 to 857 GHz, the *Planck* satellite mission is particularly well suited for the measurement of the thermal Sunyaev-Zeldovich effect. Working with the *Planck* frequency channel maps from 30 to 857 GHz, we have reconstructed the tSZ signal over the full sky using tailored component separation methods.

We tested and validated the *Planck* y -maps extensively and characterized them in terms of noise and foreground contamination. As expected the noise in the y -map is inhomogeneous and can be characterized by pixel dependent variance and a homogeneous correlated Gaussian noise. Foreground contamination by thermal dust emission is found to be important at large angular scales. Additional foreground contamination is due to radio and IR point sources for which a mask is provided. In terms of tSZ signal we find good agreement between the flux of blindly detected clusters in the y -map and that measured for clusters in the *Planck* cluster sample. Furthermore, we find that the sensitivity of the y -map is sufficient to detect faint and diffuse structures such as bridges between merging clusters. Moreover, we have proved via a stacking analysis that the very low signal-to-noise regions in the y -map preserve the tSZ signal even for small galaxy groups (tens of galaxies).

After accounting for foreground contribution, mainly thermal dust emission at large angular scales, and clustered CIB and point sources at small angular scales, we have derived from the y -map the tSZ angular power spectrum in the multipole range from $9 < \ell < 1411$. This extends significantly the range with respect to previous measurements ([Planck Collaboration XXI, 2014](#)) giving for the first time access to the 2-halo term contribution. The cosmological analysis of the tSZ power spectrum allows us to set constraints on cosmological parameters representing matter content in the Universe, mainly σ_8 and Ω_m . These constraints are consistent with those obtained from cluster number counts ([Planck Collaboration XXIV, 2015](#)) and in soft tension with those derived from CMB analysis ([Planck Collaboration XIII, 2015](#)).

The analysis of the non-Gaussian properties of the y -map using the 1D PDF, the unnormalized skewness and the bispectrum of the map have confirmed the tSZ nature of the signal.

The *Planck* y -maps and additional ancillary data (noise variance maps, foreground masks and ILC weights) are made available to the public for the *Planck* 2015 release (see Appendix C for details). These y -maps are expected to be useful in a wide range of astrophysical and cosmological analyses with clusters. For any of these analyses, and depending on the scientific goals,

the inhomogeneous properties of the noise, and the systematics and foreground contamination should be taken into account in different ways as described in this paper. Regions masked by the point source mask should never be used. In the case of pixel based analyses quality flags can be defined by combining the information from the variance map and the various foreground masks. For power spectrum, cross correlation and higher order statistic analyses we remind the fact that the y -maps present significant foreground contamination that needs to be taken into account both by masking highly contaminated regions (namely the Galactic plane region) and by using adequate foreground models to which the ILC weights are applied. Taking these necessary precautions, the *Planck* y -maps will prove a very useful tool for the community.

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Appendix A: Modelling the expected tSZ signal

A.1. tSZ power spectrum

The representation of the y -map in spherical harmonics, $Y_{\ell m}$, reads

$$y(\mathbf{n}) = \sum_{\ell m} y_{\ell m} Y_{\ell m}(\mathbf{n}). \quad (\text{A.1})$$

Thus, its angular power spectrum is given by

$$C_{\ell}^{\text{tSZ}} = \frac{1}{2\ell + 1} \sum_m y_{\ell m} y_{\ell m}^*. \quad (\text{A.2})$$

Note that C_{ℓ}^{tSZ} is a dimensionless quantity here, like y .

As in (Planck Collaboration XX, 2014) the tSZ power spectrum is modelled using a 2-halo model to account both for intra-halo and inter-halo correlations:

$$xC_{\ell}^{\text{SZ}} = C_{\ell}^{\text{1halo}} + C_{\ell}^{\text{2halos}}. \quad (\text{A.3})$$

Following (Komatsu & Seljak, 2002) the 1-halo term reads:

$$C_{\ell}^{\text{1halo}} = \int_0^{\bar{z}_{\max}} dz \frac{dV_c}{dz d\Omega} \int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} |\tilde{y}_{\ell}(M, z)|^2, \quad (\text{A.4})$$

where $dV_c/(dz d\Omega)$ is the comoving volume per unit redshift and solid angle and $n(M, z)dM dV_c/(dz d\Omega)$ is the probability of having a galaxy cluster of mass M at a redshift z in the direction $d\Omega$. The quantity $\tilde{y}_{\ell} = \tilde{y}_{\ell}(M, z)$ is the 2D Fourier transform on the sphere of the 3D radial profile of the Compton y -parameter of individual clusters,

$$\tilde{y}_{\ell}(M, z) = \frac{4\pi r_s}{l_s^2} \left(\frac{\sigma_T}{m_e c^2} \right) \int_0^{\infty} dx x^2 P_e(M, z, x) \frac{\sin(\ell_x/l_s)}{\ell_x/l_s} \quad (\text{A.5})$$

where $x = r/r_s$, $\ell_s = D_A(z)/r_s$, r_s is the scale radius of the 3D pressure profile, $D_A(z)$ is the angular diameter distance to redshift z and P_e is the electron pressure profile.

The 2-halos term (Komatsu & Kitayama, 1999; Diego & Majumdar, 2004; Taburet et al., 2011) is given by:

$$C_{\ell}^{\text{2halos}} = \int_0^{\bar{z}_{\max}} dz \frac{dV_c}{dz d\Omega} \times \left[\int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} |\tilde{y}_{\ell}(M, z)| B(M, z) \right]^2 P(k, z), \quad (\text{A.6})$$

where $P(k, z)$ is the 3D matter power spectrum at redshift z . $B(M, z)$ is the time-dependent linear bias factor that relates the matter power spectrum, $P(k, z)$, to the power spectrum of the cluster correlation function. Following Komatsu & Kitayama (1999, see also Mo & White 1996) we adopt $B(M, z) = 1 + (v^2(M, z) - 1)/\delta_c(z)$, where $v(M, z) = \delta_c(M)/D(z)\sigma(M)$, $\sigma(M)$ is the present-day rms mass fluctuation, $D(z)$ is the linear growth factor, and $\delta_c(z)$ is the threshold over-density of spherical collapse.

Finally, we use the Tinker et al. (2008) mass function, $dn(M, z)/dM$, including an observed-to-true mass bias b , as discussed in detail in Planck Collaboration XX (2014), and we model the SZ Compton parameter using the pressure profile of Arnaud et al. (2010).

A.2. Nth moment of the tSZ field

Assuming a Poisson distribution (1-halo term) of the clusters on the sky and neglecting clustering between clusters the N th moment of the tSZ signal (Komatsu & Kitayama, 1999; Wilson et al., 2012; Planck Collaboration XX, 2014) reads

$$\int_0^{\bar{z}_{\max}} dz \frac{dV_c}{dz d\Omega} \int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} \int d^2\theta y(\theta, M, z)^N, \quad (\text{A.7})$$

where $y(\theta, M, z)$ is the integrated Compton parameter along the line of sight for a cluster of mass M at redshift z .

A.3. Bispectrum

The angular bispectrum is given by

$$B_{\ell_1 \ell_2 \ell_3}^{m_1 m_2 m_3} = \langle y_{\ell_1 m_1} y_{\ell_2 m_2} y_{\ell_3 m_3} \rangle, \quad (\text{A.8})$$

where the angle-averaged quantity in the full-sky limit can be written as

$$b(\ell_1, \ell_2, \ell_3) = \sum_{m_1 m_2 m_3} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ m_1 & m_2 & m_3 \end{pmatrix} B_{\ell_1 \ell_2 \ell_3}^{m_1 m_2 m_3}, \quad (\text{A.9})$$

and satisfies the conditions $m_1 + m_2 + m_3 = 0$, $\ell_1 + \ell_2 + \ell_3 = \text{even}$, and $|\ell_i - \ell_j| \leq \ell_k \leq \ell_i + \ell_j$, for the Wigner $3j$ function in brackets. Assuming a Poissonian spatial distribution of the clusters as above, the bispectrum reads (Bhattacharya et al., 2012)

$$b(\ell_1, \ell_2, \ell_3) \approx \sqrt{\frac{(2\ell_1 + 1)(2\ell_2 + 1)(2\ell_3 + 1)}{4\pi}} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ 0 & 0 & 0 \end{pmatrix} \times \int_0^{\bar{z}_{\max}} dz \frac{dV_c}{dz d\Omega} \int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} \tilde{y}_{\ell_1}(M, z) \tilde{y}_{\ell_2}(M, z) \tilde{y}_{\ell_3}(M, z).$$

Appendix B: Bispectrum cosmic variance

Following (Lacasa, 2014, chapter 2), the bispectrum cosmic variance is composed of a Gaussian term, a bispectrum \times bispectrum term, a spectrum \times trispectrum term

and a connected 6-point term. Due to the lack of model or measurement of the trispectrum and 6-point function, we neglected the last two terms. Note that they are however expected to yield a subdominant contribution. Thus we have in full-sky :

- Gaussian cosmic variance :

$$\text{Var}_G(b_{\ell_1\ell_2\ell_3}) = \frac{C_{\ell_1} C_{\ell_2} C_{\ell_3}}{N_{\ell_1\ell_2\ell_3}} \times \begin{cases} 6 & \text{equilateral} \\ 2 & \text{isosceles} \\ 1 & \text{general} \end{cases} \quad (\text{B.1})$$

where

$$N_{\ell_1\ell_2\ell_3} = \frac{(2\ell_1 + 1)(2\ell_2 + 1)(2\ell_3 + 1)}{4\pi} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ 0 & 0 & 0 \end{pmatrix}^2 \quad (\text{B.2})$$

and where C_ℓ is the auto power spectrum of the Compton parameter map, thus containing the noise contribution.

- Bispectrum×bispectrum cosmic variance

$$\begin{aligned} & \text{Cov}_{3 \times 3}(b_{\ell_1\ell_2\ell_3}, b_{\ell'_1\ell'_2\ell'_3}) = \\ & b_{\ell_1\ell_2\ell_3} b_{\ell'_1\ell'_2\ell'_3} \times \left(\frac{\delta_{\ell_1\ell'_1}}{2\ell_1 + 1} + \frac{\delta_{\ell_1\ell'_2}}{2\ell_1 + 1} + \frac{\delta_{\ell_1\ell'_3}}{2\ell_1 + 1} \right. \\ & \quad + \frac{\delta_{\ell_2\ell'_1}}{2\ell_2 + 1} + \frac{\delta_{\ell_2\ell'_2}}{2\ell_2 + 1} + \frac{\delta_{\ell_2\ell'_3}}{2\ell_2 + 1} \\ & \quad \left. + \frac{\delta_{\ell_3\ell'_1}}{2\ell_3 + 1} + \frac{\delta_{\ell_3\ell'_2}}{2\ell_3 + 1} + \frac{\delta_{\ell_3\ell'_3}}{2\ell_3 + 1} \right) \quad (\text{B.3}) \end{aligned}$$

This is the only term which gives off-diagonal contributions to the covariance matrix.

For our purpose, this cosmic variance is multiplied by f_{SKY} and binned to the appropriate binning scheme.

We also consider systematic errors induced by foreground residuals or masking effects. We estimate systematic errors due to component separation uncertainties from the half difference of the NILC and MILCA bispectra. Masking effects are normally corrected for using simulations, which may under- or overestimate leakage from large to small scales. We thus take a conservative $\pm 25\%$ error on the debiasing ratio, consistently with the fact that the selected configurations have a ratio within $\pm 25\%$ of $f_{\text{SKY}} B(\ell_1) B(\ell_2) B(\ell_3)$. This error is most likely a conservative overestimate.

Appendix C: Products

In the following we list the y-map related products delivered in the *Planck* 2015 data release⁴:

- Full-sky MILCA and NILC y-maps for the full mission and for the first (F) and second (L) halves of *Planck* stable pointing period in Compton parameter units (see Section 3.2).
- ILC weights per filter and per frequency used for the reconstruction of the MILCA and NILC full mission y-maps, as described in Section 3.2.
- Variance map accounting for the non homogeneous coverage and power spectrum of the correlated homogeneous counterpart, C_ℓ^N , for the MILCA and NILC full mission y-maps in Compton parameter units (see Sect. 4.2).
- Point source masks including known radio and IR sources as described in Section 4.4.1.
- Galactic masks used in the analyses presented and in Sections 5 and 6.

⁴ A more detailed description is given in the *Planck* explanatory supplement.

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