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Presented at the XXIst Rencontre de Moriond on Strong Interactions and Gauge Theories, Les Arcs, France, March 16-22, 1986

DO THE CROSS SECTIONS FOR pp AND $p\bar{p}$ CONTINUE TO RISE AS $log^2(s/s_0)$?

M.M. Block and R.N. Cahn

March 1986

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I. INTRODUCTION

March 1986

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Do the Cross Sections for pp and $p\bar{p}$ Continue to Rise as $\log^2(s/s_0)$?

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The advent of pp collider physics at the CERN ISR and SppS during the last five years has extended the maximum pp center of mass energy from \sqrt{s} GeV to \sqrt{s} =900 GeV. At the SppS, experimental groups have measured σ_{tot} , the total cross section, and B, the nuclear slope parameter, at \sqrt{s} =540 GeV, as well as σ_{tot} at \sqrt{s} =900 GeV. In the energy range 30 GeV $\langle \sqrt{s} \rangle \langle 62$ GeV, groups at the ISR have made precision measurements of these quantities for both $p\bar{p}$ and pp, with the same apparatus used to compare the $p\bar{p}$ and the pp system. Moreover, new ISR measurements of elastic scattering in the Coulomb interference region have made possible accurate determinations of p, the ratio of the real to the imaginary portion of the forward nuclear scattering amplitude, for both $p\bar{p}$ and pp. These new data, taken together with earlier results, now enables us to make a critical comparison of the $p\bar{p}$ and pp elastic scattering parameters in the high energy domain from $\sqrt{s}=5$ GeV to $\sqrt{s}=900$ GeV, and allow theoretical extrapolation to much higher energies. We will deal exclusively with pp and pp collisions, and in particular, will concern ourselves with the analysis of elastic scattering in the low |t| region, $-t < 0.02 (GeV/c)^2$, where t is the four-momentum transfer squared. The treatment follows a recent Review of Modern Physics article by M.M. Block and R.N. Cahn. [1]

A model-free analysis will be made of the experimental quantities σ_{tot} , ρ and B. Traditionally, the requirements of analyticity have been compared with experimental data by means of dispersion relations. We will demonstrate how the same ends can be achieved more easily and transparently through direct use of simple analytic functions.

II. ANALYSIS OF t=0 AMPLITUDES

We define F as the analytic continuation of the forward scattering amplitude into the complex E plane, where E is the complex energy (E is the pp laboratory energy if E is real and $\geq m$, the nucleon mass). The F's are real analytic functions having cuts on the real axis from +m to ∞ and from -m to - ∞ . We choose the normalizations such, for fits with no odderons (unconventional odd amplitudes), the even continuation is,

$$4\pi F_{+} = -\sqrt{(m+E)(m-E)} \\ \left\{ \mathbf{A} + \beta \frac{\left[\log(2m(m+E)/s_{0}) + \log(2m(m-E)/s_{0}) \right]/2\right]^{2}}{1 + \operatorname{at}[\log(2m(m+E)/s_{0}) + \log(2m(m-E)/s_{0})]/2]^{2}} \\ + \frac{C}{2\sin(\pi\mu/2)} \left[\left[2m(m+E) \right]^{\mu-1} + \left[2m(m-E) \right]^{\mu-1} \right] \right\}, \qquad (2.1a)$$

and the odd continuation is

$$4\pi F_{=} - \sqrt{(m+E)(m-E)} \times \frac{D}{2\cos(\pi\alpha/2)} \left[[2m(m+E)]^{\alpha-1} - [2m(m-E)]^{\alpha-1} \right], \quad (2.1b)$$

where A, β , so, a, C, μ , D, and α are real constants to be fitted by the data. Clearly, $F_+(E) = F_+(-E)$ and $F_-(E) = -F_-(-E)$. To find the scattering amplitudes for pp scattering, f_+ and f_- , we evaluate $F_+(E+i\epsilon)$ and $F_-(E+i\epsilon)$, in the limit of real E and $\epsilon \rightarrow 0$ (for the $p\bar{p}$ amplitudes, we evaluate the F's at -E-i\epsilon). We obtain

$$\frac{4\pi}{p}f_{+} = i\left\{A + \beta \frac{L\log(2mp/s_{0}) - \frac{1\pi}{2}]^{2}}{1 + allog(2mp/s_{0}) - \frac{1\pi}{2}]^{2}} + C\left[((2m)(E-m))^{\mu-1}e^{i\pi(1-\mu)/2} + \frac{((2m)(E+m))^{\mu-1} - ((2m)(E-m))^{\mu-1}}{2sin(\pi\mu/2)}\right]\right\}$$
(2.2a)

and

$$\left(\frac{4\pi}{p}\right) f_{-} = D\left\{ \left((2m)(E-m) \right)^{\alpha-1} e^{i\pi(1-\alpha)/2} + i \frac{\left((2m)(E+m) \right)^{\alpha-1} - \left((2m)(E-m) \right)^{\alpha-1}}{2\cos(\pi\alpha/2)} \right\}.$$

$$(2.2b)$$

The optical theorem relates the cross sections σ^+ and σ^- to the above by

$$\sigma^{\pm} = \left(\frac{4\pi}{p}\right) \operatorname{Imf}_{\pm}, \qquad (2.3)$$

where p is the laboratory momentum. Hence, the imaginary portions of (2.2a) and (2.2b) give the appropriate cross sections, from which we form

$$\sigma(\mathbf{p}\bar{\mathbf{p}}) = \sigma^+ + \sigma$$

and

$$\sigma(pp) = \sigma^+ - \sigma^- .$$

(2.4b)

(2.4a)

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The formulae (2.2a) and (2.2b) simplify greatly in the limit of $E \gg m$,

where s is given by s \sim 2mE \sim 2mp. Using the notation $\langle f \rangle$ for the limit of f as E- ∞ , we find

$$\frac{\left(\frac{4\pi}{p}\right) \langle f \rangle_{+} = i \left\{ A + \beta \frac{\text{Llog}(s/s_{0}) - i\pi/2]^{2}}{1 + a \text{Llog}(s/s_{0}) - i\pi/2]^{2}} + C s^{\mu - 1} e^{i\pi(1-\mu)/2} \right\}$$

$$(2.5a)$$

and

$$\left(\frac{4\pi}{p}\right)\langle f \rangle_{-} = -D\left(s^{\alpha-1}e^{i\pi(1-\alpha/2)}\right) . \qquad (2.5b)$$

If we put a=0 in (2.5a), we find by inspection of the real and imaginary parts of (2.5a) and (2.5b), the very useful and simple formulae,

$$\sigma(pp) = A + \beta \left[\log^2(s/so) - \frac{\pi^2}{4} \right] + C \sin\left(\frac{\pi u}{2}\right) s^{\mu-1} + D \cos\left(\frac{\pi u}{2}\right) s^{\alpha-1}, \qquad (2.6a)$$

$$\sigma(p\bar{p}) = A + \beta \left[\log^2(s/s_0) - \frac{\pi^2}{4} \right] + C \sin\left(\frac{\pi\mu}{2}\right) s^{\mu-1} - D \cos\left(\frac{\pi\alpha}{2}\right) s^{\alpha-1}, \qquad (2.6b)$$

 $\rho(pp) = \left[\beta\pi \log(s/s_0) - C\cos(\pi\mu/2)s^{\mu-1} + D\sin(\pi\alpha/2)s^{\alpha-1}\right]/\sigma(pp), \quad (2.6c)$

 $\rho(p\bar{p}) = \left[\beta\pi \log(s/s_0) - C\cos(\pi\mu/2)s^{\mu-1} - D\sin(\pi\alpha/2)s^{\alpha-1}\right]/\sigma(p\bar{p}). \quad (2.6d)$

We have essentially used the forms (2.6a-d) in our earlier work^[2], where we introduced only the coefficients A, β , so, D, α and a. We

interpret the even amplitude $Cs^{\mu-1}$ as an even Regge exchange term, and the odd amplitude $Ds^{\alpha-1}$ as an odd Regge exchange term. The term in β gives the $\log^2(s/so)$ rising cross section, and A corresponds to a constant cross section. It will turn out that the coefficients using (2.5a-b), i.e., using (2.6a-d), are nearly identical to those using the kinematically correct equations (2.2a-b). The only important difference is that (2.2a-b) give an improved χ^2 for the fit. This is because the low energy kinematics (the cut structure in E) is treated correctly in (2.2a-b) for $\sqrt{s} \sim 5$ GeV, where they are of importance. For $\sqrt{s} > 10$ GeV, the results using either (2.2a-b) or (2.5a-b) are numerically indistinguishable. The units are chosen such that σ is in mb, if E, m, p and \sqrt{s} are in GeV.

The introduction of an even Regge trajectory is a departure from our earlier treatment^[2]. We note that the $\log^2(s/s_0)$ term in the even amplitude, for $s < s_0$, simulates this term in the cross section. We have fixed the power μ to be 0.5, since we expect it to be about the same as α , which turns out to be $v_{0.5}$.

Clearly, setting a=0 in (2.2a) gives rise to a cross section which continues to rise indefinitely as $\log^2(s/s_0)$. The introduction of a small, positive value of <u>a</u> in (2.2a) gives us a functional form which will have the cross section rise <u>locally</u> as $\log^2(s/s_0)$ (in the energy region 5 GeV(\sqrt{s} < 62 GeV), However, as $s \rightarrow \infty$, i.e., at very high energies, the cross section will flatten out and go to the <u>constant</u> cross section, A + (β/a), for positive a. Thus, we model the case where the Froissart bound is not truly saturated (it rises as $\log^2 s$ only

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<u>locally</u>), and eventually the cross section rise stops, going to a constant cross section at ∞ . We consider this extreme case a measure of the deviation of the asymptotic behavior of the cross section from that of $\log^2(s/s_0)$.

Our original fits^[2], made several years ago for σ_{tot} and ρ for both the pp and pp systems, were for the energy domain 5 GeV $\langle \sqrt{s} \langle 62 \rangle$ GeV, and used about 80 pieces of data, including seven different types of experimental quantities, $\sigma(pp)$, $\sigma(p\bar{p})$, $\rho(p\bar{p})$, $\rho(p\bar{p})$, $\Delta\sigma =$ $\sigma(p\bar{p}) - \sigma(pp)$, $\Delta\rho = \rho(p\bar{p}) - \rho(pp)$, and $\rho_{av} = \Gamma\rho(p\bar{p}) + \rho(pp)J/2$. The χ^2 was minimized using the seven quantities and their quoted errors. No attempt was made to adjust any of the data systematically. The sources of the data are given in ref. [1]. The original fits were made before the earliest measurements of σ_{tot} at the SPS Collider. Those data were not included in our later work^[1] because they had large uncertainties and would not have had any statistical significance in our fits. These earlier studies showed:

1. The data were well fitted by simple functional forms using the proper analyticity. See Eqs (2.2a,b) or (2.5a,b).

2a. The data were consistent with a log²(s/so) growth of σ_{tot} at high energy. a=0 in Eq (2.2a) or Eq (2.5a).

2b. The data were also consistent with a form for which σ_{tot} grew as

 $\log^2(s/so)$ in the ISR energy region below $\sqrt{s} = 62$ GeV, but asymptotically became constant. This form introduced the extra parameter <u>a</u>, but did not give a significantly better χ^2 . $a \neq 0$ in Eq (2.2a) or Eq (2.5a).

3. The data were consistent with the hypothesis that $\sigma_{tot}(p\bar{p}) - \sigma_{tot}(pp) \propto s^{-\frac{1}{2}}$. We were able to place impressive limits on "odderons", odd amplitudes corresponding to Regge trajectories with intercept $\alpha_{odderon} = 1$.

4. The conclusions were independent of the choice of \sqrt{s}_{min} from 5 to 15 GeV.

The purpose of this communication is to discuss the results of fits that include the recently published results of UA-1^[3], UA-4^[4], and UA-5^[5], as well as the lower energy data. The input for UA-5 was $\sigma_{tot} = 66.5 \pm 2.4$ mb at $\sqrt{s} = 900$ GeV. For UA-1 and UA-5, the inputs for $\sqrt{s} = 540$ GeV were not the derived cross sections, but were the experimentally measured quantities: for UA-4, $\sigma_{tot}(1+\rho^2) = 63.3$ ± 1.5 mb, and for UA-1, $\sigma_{tot}(1+\rho^2)^{\frac{1}{2}} = 67.6 \pm 6.5$ mb. Although the two measurements are consistent, the much smaller error for UA-4 makes it dominate in the fitting procedure at $\sqrt{s} = 540$ GeV. The slope measurements at $\sqrt{s} = 540$ GeV were 15.2 ± 0.2 GeV⁻² for UA-4 and 17.1 ± 1.0 GeV⁻² for UA-1.

Listed in Table I are the features of fifteen different types of fits for σ_{tot} and ρ values, made both with and without the SppS points.

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Since our previous studies showed that the odderon amplitudes were very small, we have not included them in this work. The even Regge trajectory (C≠0) with intercept μ =0.5 was included in some fits, and excluded in others. Fits with asymptotic behavior $\sigma \propto \log^2(s/s_0)$ were tried (a=0), as well as ones with asymptotically constant behavior (a≠0). The functional form $\sigma \propto \log^{\gamma}(s/s_0)$ with γ ≠2 was also investigated. Further, we investigated the sensitivity of our conclusions to our choice of $\sqrt{s_{min}}$.

In Table II are shown the results of the fits that were made excluding the SppS data, with γ set equal to 2 and a=0, so that $\sigma \propto \log^2(s/s\sigma)$ asymptotically. The fits are quite good and are insensitive to the inclusion of the lower energy data (5 GeV (\sqrt{s} (15 GeV). The presence of the even Regge trajectory with μ = 0.5 (fit #3, C≠0) has a rather minor effect on the other parameters, as well as on χ^2 .

Table III shows fits <u>including</u> the SppS with γ still set equal to 2. It is clear that good fits are only obtained when $a\neq 0$, i.e., <u>only</u> when the cross section does <u>not</u> grow asymptotically as $\log^2(s/s_0)$. We conclude that the $\log^2(s/s_0)$ form is <u>incapable</u> of fitting both the SppS data and the lower energy data simultaneously. This conclusion is unchanged either by by restricting the data to \sqrt{s} > 15 GeV (fit #5) or including the even Regge term (C≠0, fit #7). The consequences of both restricting ourselves to only higher energy data <u>and</u> including the even Regge term (C≠0) are discussed in detail later. The values of <u>a</u> obtained in the fits #6 and #8 are are consistent with our pre-SppS value, a = $0.0056 \pm 0.0030^{[1,2]}$, but now have much greater statistical significance, being almost 6 standard deviations away from zero. Further, the functional forms which give asymptotically constant cross sections yield good $\chi^{2'}$ s. The value of <u>a</u> and its uncertainty are nearly completely determined by values of the high energy UA-4 and UA-5 points.

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We illustrate fits #7 and #8 in Figs. la and lb, where we plot σ_{tot} and ρ , respectively, as a function of \sqrt{s} . At lower energies, the pp and $p\bar{p}$ data are clearly separated, with the pp data lower in value. In this region, fits #7 and #8 are indistinguishable. At higher energies, there is no distinction between pp and $p\bar{p}$, but fits #7 and #8 diverge. As seen in the figures, at high energies, fit #7 (a=0) gives higher values of σ_{tot} and ρ than does fit # 8. For fits #4, #5 and #7, where σ_{tot} grows asymptotically as $\log^2(s/s_0)$, we obtain unsatisfactory $\chi^{2's}$. In particular, the UA-4 and UA-5 points are consistently lower than the fit and contribute inordinately to χ^2 . The UA-1 point, which is statistically much less significant, is not in diagreement with the fit, as seen in Fig.la.

The failure of the fits using $\log^2(s/s_0)$ with a=0 led us to investigate a more general class, where the exponent of the term in $\log(s/s_0)$ was varied from the Froissart bound value of 2, i.e., we let the cross section vary asymptotically as $\sigma \propto \log^{\gamma}(s/s_0)$, with γ as a free

parameter to be fitted from the data. The results are given in Table IV. The fits which include the SppS points, #11 and #12, are unsatisfactory, again with UA-4 and UA-5 being the major contributors to the χ^2 . We note that <u>all</u> of the fits prefer a value of γ near the canonical value of 2. Thus, we clearly <u>can not</u> accommodate the SppS points simply by changing the value of γ .

An early fit to the ISR data that has been widely used was presented in 1977 by Amaldi et al.^[6] The form used was

$$\sigma_{\text{tot}} = B_1 + B_2 (\log s)^{\gamma} + C_1 E^{-\nu_1} \pm C_2 E^{-\nu_2}, \qquad (2.7)$$

where the upper sign is for pp and the lower is for $p\bar{p}$. It is important to note that in the second term of the Amaldi expression, s is measured in GeV², i.e., that so, (the scale of s) is <u>arbitrarily</u> set to 1 GeV². Since the fit was made in 1977, there were no $p\bar{p}$ data available in the ISR energy region to be used. Moreover, no values of $\rho(p\bar{p})$ were used in their fit at any energy. They calculated the values of $\rho(pp)$ by numerical means, using a singly subtracted dispersion relation, with the cross sections for pp and $p\bar{p}$ parametrized by (2.7).

We have investigated fits of the type \log^{γ} , à la Amaldi, using our analytic technique, by setting a=0, so=1 GeV² and replacing the exponent 2 by the parameter γ in Eq (2.2a) or (2.5a), and by letting C≠0. Two fits were made, one in which μ was fixed at 0.5 and the other with μ as a free parameter. The results are shown in Table V. We have included all of our usual data in the fit, including the Spps points. The even Regge intercept μ is expected to be near 0.5, consistent with the value of the odd intercept α . If we fix μ to be 0.5, we get for fit #14 a χ^2 per degree of freedom, $\chi^2/df = 3.92$, which is obviously completely unsatisfactory. In fit #15, we allow μ to vary, and we obtain the best fit values $\mu = 0.78 \pm 0.03$ and $\gamma = 1.999$ ± 0.002 , with a $\chi^2/df = 1.24$. Although the χ^2/df is not unreasonable, the fit is highly suspect, since the value of μ is very far from the canonical value of 0.5, expected from a Regge analysis which justifies the inclusion of such an amplitude. We thus conclude that the Amaldi type of analysis cannot be reconciled with the full data set, even when varying γ .

The conclusions drawn from the fifteen fits described above are simple and quite straightforward. The fits that <u>exclude</u> the SppS points are all satisfactory. The fits that <u>include</u> the SppS points are satisfactory <u>only</u> if $a \neq 0$, i.e., unless the asymptotic growth of the total cross section is <u>much</u> slower than $\log^2(s/s_0)$. In particular, we get a satisfactory χ^2 if the cross section asymptotically approachs a <u>constant</u>. Since this is a most unexpected result, in our opinion, we have tried to investigate under what circumstances a $\log^2(s/s_0)$ growth of σ_{tot} is possible using the SppS data points.

In fit #5, only data above \sqrt{s} = 15 GeV were used, with C=0. The fit was a failure. In fit #7, the full data set (\sqrt{s} > 5 GeV) was used,

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but the even Regge trajectory (C≠0) with intercept $\mu = 0.5$ was included. This too was inadequate, yielding $\chi^2/df = 1.54$ (120/78). By combining the options of #5 and #7-restricting the data set to \sqrt{s} > 15 GeV <u>and</u> introducing the parameter C≠0-we increase the chance of finding a reasonable fit. Such a fit-fit #16, which is described in Table VI-is subject however to serious objections. The even Regge term which is proportional to C describes a piece of the total cross section that vanishes as s goes to infinity. The restricted data set of fit #16 however covers almost exclusively the region of <u>rising</u> cross section, even for pp̄. Without the many high precision datum points at the lower energies, the parameter C might well be taking on a new and anomolous role: it could now decouple the fit in the region 5 GeV < \sqrt{s} < 62 GeV from the fit to the Spp̄S data.

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Not suprisingly, this fit with $\sqrt{s} > 15$ GeV and C#0 is successful, with $\chi^2/df = 1.14$ (35.2/31). Of course, we can not altogether dismiss this fit because of the inherent difficulties in fitting C #0 at high energies. However, there are many features of fit #16 which set it apart from the other fifteen fits. All other 15 fits have β , the coefficient of the log²(s/so) term, near the value 0.6, whereas here β = 0.32. Also, all other fits have so near 300 GeV², while for fit #16, so = 30 GeV². Further, those previous fits where C#0 and so were fitted gave C < 25, whereas here C = 69.

This new fit differs dramatically from the others. If it is accepted,

then the others must be rejected. In its starkest form, we must choose between, say, fit #1, which utilizes 81 data points in the energy interval 5 GeV $\langle \sqrt{s} \rangle \langle 62$ GeV, and fit #16, which uses 37 data points for 15 GeV $\langle \sqrt{s} \rangle \langle 900$ GeV. We see that a good fit can be had either by dropping the UA-4 point at 540 GeV and the UA-5 point at 900 GeV, or, conversely, by ignoring the 47 data points below 15 GeV. We must make a subjective choice, since we have no <u>a priori</u> knowledge that our parametrizations of the amplitudes are adequate for the full energy region 5 GeV $\langle \sqrt{s} \rangle 900$ GeV. Nonetheless, one should be extremely cautious in embracing fit #16.

III. SLOPE ANALYSIS OF NEARLY-FORWARD ELASTIC SCATTERING DATA

The near-forward hadronic amplitude for $p\bar{p}$ and pp elastic scattering is reflected in three experimentally accessible paramaters, the total cross section σ_{tot} , the ρ value, and the nuclear slope parameter B(s), defined as

$$B(s) = \frac{d}{dt} \left[\log\left(\frac{d\sigma}{dt}\right) \right]_{t=0}$$
(3.1)

In Section II, we analyzed t=0 data for σ_{tot} and ρ , in order to extract the forward hadronic amplitudes f_+ and f_- . In this Section, we will use the results of Fit #2 to obtain the s dependence of the slopes B for pp and pp elastic scattering, using experimental data in the near-forward direction (defined as the small |t| region, -t < 0.02

 $(\text{GeV}/\text{c})^2$). We write the invariant hadronic differential scattering cross section as

$$\frac{d\sigma}{dt} = \frac{\pi}{D^2} |f_+g_+(t,s) \pm f_-g_-(t,s)|^2 , \qquad (3.2)$$

where p is the laboratory momentum. We have assumed real, exponential "form factors" in Eq. (3.2), with $g_{\pm}(t,s) = \exp(B^{\pm}t/2)$. Since we are only concerned with very small |t|, the assumption of an exponential is the practical equivalent of replacing $e^{Bt/2}$ with 1+Bt/2. We rewrite Eq. (3.2) as

$$\frac{d\sigma}{dt} = \frac{\pi}{p^2} \left\{ \operatorname{[Ref}_{+} \exp(B^{\dagger}t/2) \pm \operatorname{Ref}_{-} \exp(B^{\dagger}t/2)]^2 + \operatorname{[Imf}_{+} \exp(B^{\dagger}t/2) \pm \operatorname{Imf}_{-} \exp(B^{\dagger}t/2)]^2 \right\}, \quad (3.3)$$

with the + sign for $p\bar{p}$ and the - sign for pp.

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In our analysis, we will include slope data in the energy region 5 GeV(\sqrt{s} < 62 GeV, and only those data measured in the low |t| region, -t v 0.02 (GeV/c)², in order to reasonably approximate the definition of B made in Eq. (3.1). The data do <u>not</u> form a smooth set, unlike the situation for σ_{tot} and p. In an earlier paper^[6], we discussed the choice of experimental data that have we employed. Since the total cross section is assumed to rise as log²s/so, it is important to parameterize the B⁺ term, the even slope, with a corresponding log²s term.^[6] We choose

$$B^+(s) = C^+ + D^+\log s + E^+\log^2 s$$
 (3.4a)

and

$$B^{-}(s) = C^{-} + D^{-}\log s , \qquad (3.4b)$$

where s is measured in $(GeV)^2$. No attempt is made to adjust the data for systematic errors. The slope results with fits #3 and #7 used for t=0 amplitudes are given in Table VII.

Fig. 2 is a plot of our predicted values of B vs. \sqrt{s} , where the data used in the fit were in the energy interval 5 GeV $\langle \sqrt{s} \rangle \langle 540$ GeV, and the results of fit #7 were used for the t=0 amplitudes.

IV. PREDICTIONS

Table VIII gives a summary of our high energy predictions for σ_{tot} and ρ , using fits #7 and #8. Table IX summarizes the predictions for the nuclear slope parameter B, using fit #7 for the t=0 amplitude.

V. CONCLUSIONS

It is most likely that the total cross section <u>does not</u> rise as $\log^2(s/s_0)$ if the UA-4 point at 540 GeV and the UA-5 point at 900 GeV

are correct. These experimental results are indeed compatible with the hypothesis that the total cross section asymptotically goes to a <u>constant</u> value. This completely unexpected and provocative result will have to be confirmed by measurements of either ρ at SppS energies or σ and/or ρ at the Tevatron Collider (\sqrt{s} = 2000 GeV), an energy where measurements become definitive. It is clear that measurements of elastic pp and pp scattering at ultra-high energies may still hold surprises for elementary particle physics.

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1a. The total pp and $p\bar{p}$ cross section data and fits #7 and #8. At low energies, the pp data is lower than the $p\bar{p}$ data and the two fits coincide. At higher energies, the data coalesce but the predictions diverge. Fit #7 (a=0) lies higher than fit #8 (#0).

2a. The pp and $p\bar{p} \rho$ data and fits #7 and #8. At low energies, the pp data is lower than the $p\bar{p}$ data and the two fits coincide. At higher energies, the data coalesce but the predictions diverge. Fit #7 (a=0) lies higher than fit #8 (#0).

3. The slope data B and the fit. At lower energies, the pp slope is smaller than the $p\bar{p}$ slope. Fit #7 was used for the t=0 amplitude.

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<u>Table I</u>

Characteristics of the fits to the cross sections and ρ data. When the even Regge trajectory is included (C≠0), μ is set equal to 0.5, except in fit #15.

Fit	Cha	<u>racteristics</u>	· · · · · · · · · · · · · · · · · · ·
	Parameters	√s _{min} (GeV)	Features
#1	5	5	No SppS
#2	5	15	No SppS
#3	6	5	No Spp̃S, C≠O
#4	5	5	SppS
# 5	5	15	SppS
#6	6	5	SppS, a≠0
#7	6	5	SppS, C≠0
#8	7	5	Spp̃S, C≠O, a≠O
#9	6	5	No $SppS$, $\gamma \neq 2$
#10	6	15	No SppS, y≠2
#11	6	5	SppS, γ≠2
#12	7	5	Spp̃S, γ≠2, C≠0
#13	7	5	No SppS, $\gamma \neq 2$, C $\neq 0$
#14	6	5	SppS, γ≠2, so=l GeV ² , C≠0
#15	7	5	Spp̄S, γ≠2, μ≠0.5, so=1 GeV², C≠0

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Fits to the data including SppS points

<u>Fit</u>	#4	1	‡ 5	#6		#7	#8
A	41.66 ±	0.04 41.34	± 0.12	41.68 ±	0.04	40.42 ± 0.27	41.13 ± 0.22
β	0.62 ±	0.01 0.48	± 0.03	0.63 ±	0.01	0.52 ± 0.02	0.59 ± 0.02
50	349 ± 3	8.4 242	± 26	330 ±	7.6	217 ± 25	278 ± 21
D	-37.7 ±	1.5 -33.6	± 6.2	-39.0 ±	1.5	-41.1 ± 1.9	-41.2 ± 1.9
о.	0.49 ±	0.01 0.52	± 0.04	0.48 ±	0.01	0.46 ± 0.02	0.46 ± 0.01
С	0		0	0		22.6 ± 4.5	10.5 ± 4.0
a	0		0	0.0083 ±	0.0013	0	0.0074 ± 0.0014

χ²/df 146/79=1.85 51.9/32=1.62 86.1/78=1.10 120.4/78=1.54 78.9/77=1.02

<u>Table II</u>

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Fits to the data excluding SppS points

<u>Fit</u>	#1	#2	#3
Α.	41.74 ± 0.37	41.66 ± 0.12	41.36 + 0.25
β	0.66 ± 0.01	0.60 ± 0.04	0.63 ± 0.03
50	337 ± 8	306 ± 27	299 ± 25
D	-39.3 ± 1.6	-34.6 ± 6.8	-40.4 ± 1.8
α	0.48 ± 0.01	0.51 ± 0.04	0.47 ± 0.01
С	0	0	7.3 ± 4.6
χ²/df	91.6/76=1.20	32.5/29=1.12	89.0/75=1.19

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Table IV

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Fits with the variable γ in $\log^{\gamma}(s/s_0)$. Only fits #11 and #12 include the SppS data.

<u>Fit</u>	#	9			10)		1	1		12	2	#	1:	3
A	41.72	±	0.04	41.70	±	0.12	41.65	±	0.04	40.33	±	0.29	41.72	±	0.40
β	0.66	±	0.01	0.62	±	0.04	0.61	±	0.01	0.51	±	0.02	0.66	±	0.04
50	375	±	20	335	±	49	371	±	21	195	±	30	375	±	72
D	-41.0	±	1.9	-37.0	±	8.4	-38.4	±	1.7	-40.6	±	1.9	-41.1	±	1.9
or	0.46	±	0.02	0.50	`±	0.05	0.48	±	0.01	0.47	±	0.02	0.46	±	0.02
С .		0			0			0		24.3	±	4.6	0.1	±,	7.9
Y	2.015	±	0.017	2.008	±	0.011	2.009	±	0.007	1.992	±	0.007	2.015	±	0.011

χ²/df 86/75=1.15 32.0/28=1.14 145/78=1.86 118.8/77=1.54 86.4/74=1.17

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Table V

Amaldi-type fits: so = 1 GeV². Fit #14 fixes μ =0.5 corresponding to v1=0.5 in Eq (2.7), whereas fit #15 allows μ to vary.

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<u>F1t</u>	#14	#15				
A	32.57 ± 0.22	16.61 ± 3.26				
β	0.16 ± 0.003	0.28 ± 0.02				
50	1	1				
D	-39.8 ± 2.0	-41.9 ± 2.1				
a.	0.47 ± 0.02	0.46 ± 0.02				
С	80.9 ± 1.9	56.3 ± 1.7				
Y	, 1.981 ± 0.003	1.999 ± 0.002				
μ	0.5	0.779 ± 0.025				
χ²/df	305.4/78=3.92	95.3/77=1.24				

Table VI

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A fit to the data for \sqrt{s} > 15 GeV using the even Regge term (C#0).

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Fit	#16	
A	36.37 ± 1.78	
β	0.32 ± 0.046	
50	30.1 ± 24.8	
D	-41.0 ± 10.2	
a.	0.47 ± 0.05	
С	69.2 ± 17.0	
χ²/df	35.2/31=1.13	

Fits for the slope parameters. See Eqs (3.4a), (3.4b).

Table VII

<u>Fit</u>	No Sp <u>ē</u> s	With Sp <u>ē</u> S				
c+	10.79 ± 0.59	9.92 ± 0.31				
ם + מ	-0.049 ± 0.202	0.27 ± 0.09				
E+	0.040 ± 0.017	0.013 ± 0.006				
c -	21.5 ± 5.1	18.9 ± 5.1				
ם_	1.23 ± 1.08	1.93 ± 1.07				
χ²/df	78.8/52=1.52	85.6/54=1.59				

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Table IX

Predictions for the nuclear slope parameter B, using fit #7 for the t=0 amplitudes

JS (TeV)	B (GeV/c) ⁻²
.540	16.6 ± 0.5
2.0	19.4 ± 1.0
40.0	28.1 ± 2.6

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Table VIII

Predictions of fit #7 (a=0) and fit #8 ($a\neq 0$).

√s (TeV)	.540	.540	2.0	2.0	40.0	40.0
	σ _{tot} (mb)	ρ	σ _{tot} (mb)	ρ	$\sigma_{tot}(mb)$	ρ

a=0 66.0±0.67 0.18±0.003 88.9±1.41 0.18±0.003 168.1±4.3 0.15±0.002 a=0.0074 62.2±0.94 0.11±0.009 73.7±2.26 0.09±0.010 92.5±5.7 0.04±0.007

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