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#### Cold N + NH Collisions in a Magnetic Trap

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We present an experimental and theoretical study of atom-molecule collisions in a mixture of cold, trapped N atoms and NH molecules at a temperature of  $\sim$  600 mK. We measure a small N + NH trap loss rate coefficient of  $k_{loss}^{\text{(N+NH)}} = 9(5)(3) \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}$ . Accurate quantum scattering calculations based on *ab initio* interaction potentials are in agreement with experiment and indicate the magnetic dipole interaction to be the dominant loss mechanism. Our theory further indicates the ratio of  $N + NH$  elasticto-inelastic collisions remains large  $(> 100)$  into the mK regime.

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The study of low temperature molecular collisions and interactions is a rapidly expanding area of research at the interface of chemistry and physics [\[1](#page-4-1)[,2](#page-4-2)]. Experimental and theoretical techniques have been developed for studying a wide variety of phenomena, ranging from quantum threshold scattering [[3](#page-4-3),[4\]](#page-4-4), inelastic atom—molecule collisions [\[5–](#page-4-5)[7](#page-4-6)], external field control of dipolar interactions in cold and ultracold molecules [[8](#page-4-7)[,9\]](#page-4-8), to chemistry at cold [\[10,](#page-4-9)[11\]](#page-4-10) and ultracold temperatures [\[2](#page-4-2),[12](#page-4-11)]. The immense diversity of molecular structure and interactions is the cornerstone of many applications of cold molecules in quantum information science [[13](#page-4-12)], condensed-matter physics [[14](#page-4-13)], precision measurement [\[15,](#page-4-14)[16\]](#page-4-15), cold controlled chemistry [[2\]](#page-4-2), and astrophysics [\[17\]](#page-4-16). Achievement of these applications relies on improved methods for cooling and further understanding of low temperature molecular collisions.

Recently, several experimental techniques were introduced to study molecular collisions at cold and ultracold temperatures. Ultracold ground state molecules with temperatures below 1  $\mu$ K can be created via coherent state transfer from magneto-associated ultracold atomic gases, producing KRb  $[9]$  $[9]$  $[9]$  and  $Cs<sub>2</sub>$  [\[18\]](#page-4-17). Alternatively, direct cooling techniques such as buffer-gas cooling [\[19](#page-4-18)] and Stark deceleration [[3\]](#page-4-3) enable the production of cold molecules from room-temperature sources, such as supersonic beams [[1](#page-4-1)[–3\]](#page-4-3). Since the maximum molecular trap densities for these direct cooling techniques are, so far,  $10^8$ – $10^9$  cm<sup>-3</sup>, the collision experiments with these molecular samples typically use a dense rare gas collision partner [[3](#page-4-3)[,5\]](#page-4-5) or perform collisions at energies  $>10$  cm<sup>-1</sup> [\[3,](#page-4-3)[4](#page-4-4)[,10\]](#page-4-9). Further cooling and compression of molecular samples produced via direct cooling techniques is key to study cold molecule-molecule interactions and their applications. One possible approach is to sympathetically cool a molecule via collisions with an atom [\[1](#page-4-1),[20](#page-4-19)–[24](#page-4-20)]. Thus, studies of cold atom-molecule collisions not only uncover the underlying collision physics, but also may lead to new methods for the production of a variety of ultracold molecules.

Theoretical searches for optimal collision partners for sympathetic cooling of molecules [\[20](#page-4-19)[–24\]](#page-4-20) have focused largely on alkali metals. However, accurate quantum scattering calculations have shown that collision-induced inelastic relaxation of molecules such as OH  $[20]$ , ND<sub>3</sub>  $[21]$  $[21]$ , and NH [[22\]](#page-4-22) with the alkali-metal atoms occurs rapidly, severely limiting the efficiency of sympathetic cooling. Sympathetic cooling of NH molecules with laser-cooled alkaline earth atoms such as Mg might be possible [\[23\]](#page-4-23), as might sympathetic cooling of large molecules with raregas atoms in an optical dipole trap [\[24\]](#page-4-20). We have recently suggested that cold atomic nitrogen (N) can be used for sympathetic cooling of open-shell molecules, and demonstrated cotrapping of N atoms with NH molecules [[19](#page-4-18)], but the presence of  ${}^{3}$ He buffer gas at 0.5 K precluded measurement of  $N + NH$  collisions in that experiment.

In this Letter, we report the observation of cold (570 mK) collisions between magnetically trapped, ground state open-shell atoms and ground-state polar molecules, N and NH—both species spin polarized. We carry out accurate *ab initio* quantum scattering calculations of  $N + NH$ collisions in a magnetic field. Our theoretical results agree with the observations and predict high elastic-to-inelastic ratios  $(\gamma)$  over a wide range of temperatures (from 1 K down to about 1 mK), suggesting the feasibility of sympathetic cooling of NH molecules by collisions with N atoms in a magnetic trap. Recent unpublished work by another group has made similar theoretical claims [\[25\]](#page-4-24).

The apparatus used to cotrap atomic nitrogen and NH is similar to that described in our previous work [\[19](#page-4-18)[,26\]](#page-4-25). A pair of superconducting solenoids produce a 4 T deep

spherical quadrupole magnetic trap. In the bore of the solenoids resides a cryogenic buffer gas cell held at 500 mK. N and NH are produced in a molecular beam using a dc glow discharge and enter the trapping region through a 1 cm diameter aperture in the buffer gas cell. N and NH thermalize with  ${}^{3}$ He buffer gas to 500 mK and fall into the trap. The initial buffer gas density at time of loading of  $10^{15}$  cm<sup>-3</sup> is produced using a cryogenic reservoir with fast actuating valve [\[26\]](#page-4-25) to inject buffer gas through a 3.8 cm diameter aperture in the cell. After trap loading, the valve is closed, and the buffer gas exits primarily back out through the larger aperture, yielding background helium densities of  $10^{12}$  cm<sup>-3</sup>, corresponding to NH trap lifetimes of several seconds.

Detection of trapped N is performed using twophoton absorption laser induced fluorescence from the ground  $(2p^3)^4S_{3/2}$  state to the excited  $(3p)^4S_{3/2}$  state at  $96750$  cm<sup>-1</sup>. NH is detected via laser induced fluorescence, as described in [\[19\]](#page-4-18). We initially load NH with densities on the order of  $10^8$  cm<sup>-3</sup>. Accurate knowledge of the absolute NH density is unnecessary as the NH density is much smaller than the N density in all our measurements. To determine the N density without relying on imprecise fluorescence collection measurements, the two-photon absorption laser induced fluorescence signal is calibrated using  $N + N$  collisional loss measurements [\[27\]](#page-4-26). We load  $5 \times 10^{11}$  N atoms into the trap with peak densities of  $10^{12}$  cm<sup>-3</sup>.

Figure [1](#page-2-0) shows a typical NH trapping decay. At time  $t = 0$  s, N and NH are coloaded into the magnetic trap. For the first 2 s, the NH trap loss is rapid due to the collisions with background helium gas during the pump out of buffer gas from the cell. By  $t = 5$  s the NH trap loss reaches a steady rate, with typical  $1/e$  lifetimes of about 3 s. Since the excitation laser for the N detection causes additional loss of the trapped NH, we measure the trapped N density at  $t = 15$  s.

To measure  $N + NH$  collisions, we observe the NH trap loss over a range of cotrapped N densities. The cotrapped N density is varied by changing the ratio of molecular

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<span id="page-2-2"></span>beam process gases  $N_2$  and  $H_2$  between (90%, 10%) and (3%, 97%). Figure [2](#page-2-1) shows the total NH loss rate,  $\Gamma_{\text{NH}}$ , versus cotrapped nitrogen density. The solid line in Fig. [2](#page-2-1) is a fit to the equation

$$
\Gamma_{\text{NH}} = \frac{k_{\text{loss}}^{\text{(N+NH)}}}{14} n_{\text{N}} + \Gamma_{\text{He}} \tag{1}
$$

where  $n_N$  is the peak nitrogen density,  $\Gamma_{\text{He}}$  is the NH loss rate attributable to collisions with background helium gas, and  $k_{\text{loss}}^{\text{(N+NH)}}$  is the N + NH loss rate coefficient. The factor of  $14(\pm 0.4)$  arises from averaging the N and NH densities over the volume of the magnetic trap [\[27\]](#page-4-26). We find from this fit that  $k_{\text{loss}}^{(N+NH)} = 9(5)(3) \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}$ . The uncertainties in  $k_{\text{loss}}^{(N+NH)}$  are statistical and systematic, respectively, where the systematic uncertainty is dominated by the N density calibration [\[27\]](#page-4-26). The  $N + NH$  loss rate coefficient has contributions from both elastic (evaporative) and inelastic  $N + NH$  collisions [[27](#page-4-26)], but their individual contributions cannot be determined by a single measurement. Therefore, our measurement of  $k_{\text{loss}}^{\text{(N+NH)}}$  is an upper limit on the inelastic  $N + NH$  rate coefficient. From the following theoretical analysis of  $N + NH$  elastic scattering and trap loss dynamics, we estimate elastic collisions contribute up to 60% to the total value of  $k_{\text{loss}}^{\text{(N+NH)}}$ .

To interpret the experimental observations and explore the possibility of sympathetic cooling of NH molecules by collisions with cotrapped N atoms, we performed rigorous quantum scattering calculations of  $N + NH$  collisions in an external magnetic field. The Hamiltonian of the atommolecule collision complex may be written  $(h = 1)$ 

$$
\hat{H} = -\frac{1}{2\mu R} \frac{\partial^2}{\partial R^2} R + \sum_{S=1/2}^{5/2} V_S(R, r, \theta) |SM_S\rangle\langle SM_S| + \frac{\hat{\ell}^2}{2\mu R^2} \n- \sqrt{\frac{24\pi}{5} \frac{\alpha^2}{R^3} \sum_q Y_{2q}^{\star}(\hat{R}) [\hat{S}_{\text{NH}} \otimes \hat{S}_{\text{N}}]_q^{(2)} + \hat{H}_{\text{NH}} + \hat{H}_{\text{N}},
$$

<span id="page-2-1"></span>

FIG. 1 (color online). NH trap decay taken at a trap depth of 3.9 T and cell temperature 570 mK. The solid line is a fit to the form  $n_{\text{NH}} = a \exp[-\Gamma_{\text{NH}} t]$ . The fit to the exponential decay was performed over the range of 5.5 to 10 s.

FIG. 2 (color online). NH loss rate vs cotrapped N density. The (red) line is a fit of the data to Eq. ([1\)](#page-2-2). The vertical error bars represent 1 standard deviation intervals from the fit for  $\Gamma_{\text{NH}}$  as shown in Fig. [1.](#page-2-0) The horizontal error bars represent the change in N density over the interrogation time of 5.5 to 10 s. The calibration of the peak N density (horizontal axis scale) contains an overall uncertainty of 30%.

where  $\mu$  is the reduced mass of the complex,  $R = |R|$  is the N + NH separation vector, r is the internuclear distance in NH,  $\theta$  is the angle between the vectors **R** and **r**,  $V_S(R, r, \theta)$  is the interaction potential of the N + NH collision complex,  $\hat{S}$  is the total spin of the complex, and  $M_S$  is its projection on the magnetic field axis. The last two terms in the Hamiltonian describe noninteracting collision partners in the presence of an external magnetic field of strength B [\[28\]](#page-4-27). The term proportional to  $R^{-3}$  represents the magnetic dipole interaction [\[27,](#page-4-26)[28\]](#page-4-27).

The interaction of NH(<sup>3</sup> $\Sigma$ ) molecules with N(<sup>4</sup>S<sub>3/2</sub>) atoms gives rise to three adiabatic potential energy surfaces (PESs) with  $S = 1/2$ ,  $3/2$ , and  $5/2$ . Since in our experiments both atoms and molecules are confined in a static magnetic trap, the incident collision channel is the maximally spin-stretched Zeeman state  $|M_{S_{\rm NH}} = 1 \rangle \otimes |M_{S_{\rm N}} =$  $3/2$  with  $S = 5/2$ . We neglect the weak couplings between the electronic states of different S arising from the fine-structure terms in  $\hat{H}_{\text{NH}}$  and off-diagonal matrix elements of the magnetic dipole interaction [[27](#page-4-26)[,28](#page-4-27)].

To evaluate the PES for the  $S = 5/2$  electronic state of N-NH, we use the partially spin-restricted coupled cluster method with single, double, and noniterative triple excitations [[29](#page-4-28)] using quadruple-zeta basis set (aug-cc-pvqz) [\[30\]](#page-4-29) augmented with  $3s3p2d2f1g$  bond functions placed in the middle of the intermolecular distance. A contour plot of the calculated PES is shown in Fig. [3.](#page-3-0) The PES has a global minimum 87.83 cm<sup>-1</sup> deep in the linear N-HN configuration ( $R = 7.02a_0$ ,  $\theta = 0$ ) and a secondary minimum of  $77.52 \text{ cm}^{-1}$  in the HN-N configuration  $(R = 6.61a_0, \quad \theta = 180^\circ)$  separated by a barrier 39.6 cm<sup>-1</sup> high located at  $\theta = 92^{\circ}$ .

To solve the scattering problem, we expand the wave function of the collision complex in a direct-product basis set  $|NM_N\rangle|S_{NH}M_{S_{NH}}\rangle|S_{NH}M_{S_N}\rangle|\ell m_\ell\rangle$ , where N is the rotational angular momentum of NH, and  $M_N$ ,  $M_{S_{\rm NH}}$ ,  $M_{S_{\rm N}}$ , and  $m_{\ell}$  are the projections of  $\hat{N}$ ,  $\hat{S}_{NH}$ ,  $\hat{S}_{N}$ , and  $\hat{\ell}$  on the magnetic field axis. We solve the resulting close-coupled equations

<span id="page-3-0"></span>

FIG. 3 (color online). Contour plot of the ab initio interaction PES for the fully spin-polarized  $S = 5/2$  state of N + NH calculated in this work. The NH bond distance is fixed at its equilibrium value  $r = 1.958 a_0$ . Energies are in units of cm<sup>-1</sup>.

numerically for each value of the total angular momentum projection  $M = M_N + M_{S_{\text{NH}}} + M_{S_N} + m_\ell$  for collision energies between  $10^{-4}$  and 1 cm<sup>-1</sup> and extract the S-matrix elements and scattering cross sections. Large basis sets with  $N = 0$ -5 and  $\ell = 0$ -8 are used to ensure that the results are converged to <5%.

Figure [4\(a\)](#page-3-1) shows the cross sections for elastic energy transfer and inelastic relaxation in  $N + NH$  collisions. The cross sections increase with decreasing collision energy before reaching a maximum at  $E_C \sim 2$  mK, which we identify as a shape resonance supported by the centrifugal barrier with  $\ell = 1$  in the incident collision channel. At  $E_C$  < 0.1 mK the inelastic cross sections assume the characteristic  $E_C^{-1/2}$  dependence on collision energy, and the elastic cross sections become constant, according to the Wigner threshold law. By thermally averaging the cross sections in Fig. [4\(a\)](#page-3-1), we obtain elastic and inelastic rate constants at the experimental temperature of 570 mK of  $k_{\text{el}} = 2.2 \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}, \quad k_{\text{in}} = 4.1 \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}.$ The fraction of elastic  $N + NH$  collisions that lead to trap loss is less than  $3 \times 10^{-3}$  [[27](#page-4-26)], leading to a total trap loss rate coefficient  $\frac{\text{(N+NH)}}{\text{loss-theory}} = (4-11) \times$  $10^{-13}$  cm<sup>3</sup> s<sup>-1</sup>, in good agreement with the experimental value of  $k_{\text{loss-experiment}}^{(N+NH)} = 9(5)(3) \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}$ . The ratio  $\gamma = k_{el}/k_{in}$  is shown in Fig. [4\(b\)](#page-3-1) as a function of temperature. The ratio remains large ( $\gamma > 100$ ) over the temperature range  $\sim$ 10 mK–1 K, which indicates that



<span id="page-3-1"></span>FIG. 4 (color online). (a) Cross sections for elastic scattering (black line) and inelastic relaxation (red line) in  $NH + N$  collisions calculated as functions of collision energy at an average magnetic field of 0.1 T experienced by trapped species at a temperature of 600 mK in the 4 T deep trap. Also shown is the cross section calculated with the magnetic dipole interaction omitted (dashed line). (b) Thermally averaged ratios of the rate constants for elastic scattering and inelastic relaxation as functions of temperature.

NH can be sympathetically cooled by elastic collisions with spin-polarized N down to the millidegrees Kelvin regime. As shown in Fig. [4\(b\)](#page-3-1), an increasing magnetic field suppresses inelastic relaxation, so that  $\gamma$  remains high ( $\sim$  50) even at T = 1 mK. The suppression occurs due to an increase of the energy gap between the initial and final collision channels with increasing magnetic field [\[27](#page-4-26)[,31\]](#page-4-30). Although the current experiment, at a temperature of 600 mK, is not sensitive to this suppression, applying a strong uniform magnetic field of order 1 T may be used to stabilize spin-polarized atom-molecule mixtures against collisional losses at temperatures below 100 mK, thereby enhancing the efficiency of sympathetic cooling.

Inelastic collisions of  ${}^{3}\Sigma$  molecules with open-shell atoms like N can occur due to (i) spin-dependent couplings arising from an interplay between the anisotropy of the atom-molecule interaction potential and the intramolecular spin-spin interaction [[5,](#page-4-5)[28\]](#page-4-27), and (ii) direct couplings between atomic and molecular Zeeman levels induced by the long-range magnetic dipole interaction. The magnetic dipole interaction [\[27\]](#page-4-26) can thus be more efficient in inducing inelastic relaxation than other spin-dependent couplings. Figure [4\(a\)](#page-3-1) shows that omitting the magnetic dipole interaction from scattering calculations reduces the inelastic cross sections by a factor of  $\sim$ 10, confirming that Zeeman transitions in  $N + NH$  collisions are indeed driven by the magnetic dipole interaction. In our experiments, both N and NH collision partners are fully spin-polarized, so the chemical reaction  $N + NH \rightarrow N_2 + H$  is spinforbidden and can only proceed via nonadiabatic transitions between different electronic states of the N-NH complex in the entrance reaction channel mediated by the fine-structure and magnetic dipole coupling terms of the Hamiltonian. Our observed value for  $k_{\text{loss-experiment}}^{(N+NH)}$  is much smaller than the calculated reaction rate for spinunpolarized reactants  $(k_{\text{reaction}} \sim 3 \times 10^{-11} \text{ cm}^3/\text{s}$  at  $T = 1$  K) [[32](#page-4-31)]. Since our measurements are consistent with theoretical predictions that ignore the reaction channel, we conclude that chemical exchange processes in spinpolarized  $N + NH$  mixtures occur at a slow rate, and do not contribute to the trap loss dynamics. This finding shows that inelastic relaxation in  $N + NH$  collisions occurs via the same mechanism as dipolar relaxation in spin-polarized atomic gases [[27](#page-4-26)].

In conclusion, we have measured a small  $N + NH$  trap loss rate coefficient of  $9(5)(3) \times 10^{-13}$  cm<sup>3</sup> s<sup>-1</sup> at a temperature of  $\sim 600$  mK. To interpret experimental observations, we have carried out accurate ab initio quantum scattering calculations of Zeeman relaxation in  $N + NH$ collisions in a magnetic field and find theory and experiment to agree. Our calculations show that the ratio of  $N + NH$  elastic-to-inelastic collisions remains large ( $> 100$ ) over the temperature range  $\sim 10$  mK–1 K, which indicates that it may be possible to sympathetically cool NH down to the millidegrees Kelvin regime via elastic

collisions with (evaporatively cooled [\[27\]](#page-4-26)) spin-polarized N. If this conclusion holds for other paramagnetic molecules such as the highly polar CaH and SrF in their electronic ground states of  ${}^{2}\Sigma$  symmetry, it may be possible to create large samples of these molecules via collisional cooling with N in a magnetic trap.

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