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FISSION-EXCITATION FUNCTIONS IN INTERACTIONS OF  
 $^{11}\text{B}$ ,  $^{12}\text{C}$ ,  $^{14}\text{N}$  AND  $^{19}\text{F}$  WITH VARIOUS TARGETS†

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ABSTRACT

Fission cross sections for the systems  $^{169}\text{Tm} + ^{11}\text{B}$ ,  $^{175}\text{Lu} + ^{11}\text{B}$  and  $^{12}\text{C}$ ,  $^{174}\text{Y} + ^{12}\text{C}$ ,  $^{182}\text{W} + ^{12}\text{C}$ ,  $^{165}\text{Ho} + ^{14}\text{N}$  and  $^{159}\text{Tb} + ^{19}\text{F}$  have been measured for heavy-ion bombarding energies up to 10.4 Mev per nucleon. The experimental technique consisted of counting coincident fission-fragment pairs with two gold-surface-barrier silicon-diode detectors.

For the above systems fission takes place only for reactions in which a compound nucleus is formed between the incident projectile and the target nucleus. Values of the compound nucleus cross sections for these reactions are estimated from other data in order to account for surface reactions which occur in heavy ion bombardment. The difference between the cross-section for compound nucleus formation and that for fission is assumed to be equal to the cross-section for neutron evaporation products. The ratio of the fission cross-section to that for neutron evaporation is then taken to be equal to  $\langle \Gamma_f / \Gamma_n \rangle$ , the ratio of

the level widths for the two competing processes averaged over the various reaction channels. A theoretical fit to the  $\langle \Gamma_f / \Gamma_n \rangle$  values is obtained for the low-energy region of the excitation function where first chance fission is highly probable. We find the ratio of the level density parameter for fission to that for neutron emission to be  $1.2 \pm 0.1$  and values for the fission barrier to be in agreement with those predicted by Myers and Swiatecki.

## I. INTRODUCTION

Measurements of fission excitation functions constitute an important source of information concerning the probability of nuclear fission as a function of various nuclear parameters.<sup>1</sup> Analysis of fission-to-neutron-evaporation level width ratios,  $\Gamma_f / \Gamma_n$ , derived from such data are useful in determining nuclear level density parameters, fission barrier heights, the dependence of fissionability on angular momentum, etc.<sup>2</sup> Investigations of this type have been performed for several combinations of bombarding ions and heavy target nuclides ( $A > 200$ ), the results of which are summarized in Refs. 1 and 2.

The present work is primarily concerned with these aspects of the fission process when heavy-ions are used as incident particles on light target nuclides in the rare earth region and is a continuation of studies reported previously.<sup>3</sup> A broad understanding of fission probabilities for heavy-ion-induced nuclear reactions is of particular concern at the present time in view of current efforts to synthesize

super-heavy elements near  $Z = 114$  by means of such reactions. In addition a knowledge of trends in fission barrier energetics as a function of atomic number  $Z$  and mass number  $A$  are useful in estimating the stability of such elements against spontaneous fission. In this work we have measured fission excitation functions for a series of primarily even- $Z$  compound nuclei using the projectiles  $^{11}\text{B}$ ,  $^{12}\text{C}$ ,  $^{14}\text{N}$  and  $^{19}\text{F}$  and the targets  $^{174}\text{Yb}$  and  $^{182}\text{W}$  (separated isotopically) and  $^{159}\text{Tb}$ ,  $^{165}\text{Ho}$ ,  $^{169}\text{Tm}$  and  $^{175}\text{Lu}$  (naturally monoisotopic). In Ref. 3 these same targets were studied with  $^{12}\text{C}$ ,  $^{16}\text{O}$  and  $^{20}\text{Ne}$  ions.

For heavy-ions incident on targets heavier than tungsten ( $Z = 74$ ), fission cross-sections are nearly equal to the compound nucleus formation cross-section. For this reason it is not possible to obtain reliable  $\Gamma_f/\Gamma_n$  values without simultaneous measurement of both fission cross-sections and neutron evaporation cross-sections. However, for the systems examined here and in Ref. 3, the fission cross-section differs sufficiently from that for compound nucleus formation that the neutron evaporation cross-section can be determined reliably from the difference between the calculated compound nucleus formation cross-section and the measured fission cross-section (see below). The accuracy of this assumption is probably comparable to that for the experimental determination of total neutron evaporation cross-sections.

The experimental technique employed here is similar to that of Ref. 3. It consists of counting coincident fission-fragment pairs with two gold surface-barrier silicon-diode detectors. The advantage

of this method is that a fission event is not only identified by the energy of the fragments, but also by a coincidence requirement and by an angular correlation between the two fragments. The latter characteristic offers a convenient way of studying fission of targets lighter than lead and bismuth. In general such targets will have heavy-element impurities such as lead, bismuth and uranium that are difficult to eliminate. By proper positioning of the two detectors, one can minimize interference from fission of such impurities.

The theoretical analysis is somewhat different from that of Ref. 3. As will be described in Section IV, the average value for  $\Gamma_f/\Gamma_n$ , denoted  $\langle \Gamma_f/\Gamma_n \rangle$ , is obtained by averaging over  $\Gamma_f/\Gamma_n$  for individual  $\ell$ -waves of the incoming ions. In reference 3,  $\langle \Gamma_f/\Gamma_n \rangle$  was set equal to  $\Gamma_f/\Gamma_n$  for the average  $\ell$ -wave of the compound nucleus reactions that initiate fission. We shall also use a formula for  $\Gamma_f/\Gamma_n$  which contains angular momentum terms. The main purpose of the fitting process is to obtain values for the fission barrier height.

## II. EXPERIMENTAL PROCEDURE

We shall only give a brief account of the experimental arrangement since it has been described in earlier publications.<sup>3-5</sup> Heavy-ion beams were furnished by the Berkeley HILAC which accelerates ions to 10.4 Mev/nucleon. The beam was magnetically deflected through 30 degrees before reaching the fission chamber. Lower energies were obtained by inserting weighed aluminium foils into the beam path.

Northcliffe's range-energy curves for aluminium were used to estimate the resulting energy.<sup>6</sup> Additionally, the ranges of the ions in emulsion were measured and from this the average energy and the energy spread could be evaluated.<sup>7</sup> The average energies obtained with the two methods were generally in agreement at the highest energies, but differed by as much as 2 Mev at the lowest energies.

Before striking the target, the beam passed through two circular collimators 1.5 mm in diameter and 62 cm apart. The last collimator was 6 cm from the target. The beam current was collected in a Faraday cup arrangement, described previously<sup>3,4,5</sup> and was converted to the number of particles striking the target with the aid of values for the equilibrium charge distributions for heavy ions passing through matter.<sup>8</sup> Targets were made by vaporizing the metals onto 100- $\mu\text{g}/\text{cm}^2$  nickel films. Target thicknesses were about 200  $\mu\text{g}/\text{cm}^2$ .

The silicon detectors were of the gold surface-barrier type. They were mounted on movable arms with one of them in a permanent position at 90° to the beam. The angular position  $\psi$  of the second detector was varied to obtain the angular correlation of fission events. Circular collimators were used for both detectors, each with a geometry of  $1.4 \times 10^{-3}$  steradians. Measurement of the angular correlation functions is important in these experiments in order to obtain the following information:



- (a) The relative contribution of fission induced by surface reactions to the total fission cross-section; this is found to be a negligible effect for the targets used here.
- (b) The angular position  $\psi$  of the most probable angle of coincidence with the  $90^\circ$  detector.
- (c) The most probable value of the center-of-mass transformation parameter,  $\chi^2_{mp}$ .

The latter parameter is defined as  $\chi^2 = (V/v)^2$ , where  $V$  is the velocity of the center-of-mass and  $v$  is the velocity of the reaction product in the center-of-mass system.

The parameter  $\chi^2_{mp}$  is related to the most probable angle of coincidence  $\psi$  by the relationship:

$$\chi^2_{mp} = (1 + 4 \tan^2 \psi)^{-1}. \quad (1)$$

It is necessary to know this quantity in order to convert the laboratory angular distributions to the center-of-mass system for calculation of the total cross-sections, as discussed below.

Measurement of the fission cross-sections for the compound nuclei formed in these bombardments is complicated by the relatively low kinetic energies of the fragments. With semiconductor detectors it becomes difficult to obtain differential cross-sections from such fragments because the fission events are not easily differentiated from background noise. This problem can be eliminated by counting coincident

events between two detectors.<sup>3</sup> In order to determine the number of fragments emitted at a given angle using this technique, it is essential that the complementary detector have a large enough geometry to catch all coincident fragments; i.e. it must record the integrated angular correlation.

In this work a low geometry detector ( $1.4 \times 10^{-3}$  steradians) was used to measure the differential fission cross-section at  $90^\circ$  in the laboratory system at each bombarding energy. A large geometry detector (0.28 steradians) was then placed at the angle  $\bar{\psi}$ , determined in the angular correlation experiments. The counting efficiency of this arrangement was checked for the system  $^{197}\text{Au} + 124 \text{ Mev } ^{12}\text{C}$  ions, where distinct single fragment spectra could be obtained. We found the value for coincidence counting to be about 95% of the value obtained from counting with a single detector. Appropriate corrections for this loss in counting efficiency were then applied to the data.

The total cross-section for fission was then calculated from the equation:

$$\sigma_f = 2\pi \left[ \frac{d\sigma^\circ}{d\Omega} \left( \frac{\pi}{2} \right) \right]_{\text{abs}} \frac{\left[ \frac{d\sigma^\circ(\bar{\theta})}{d\sigma^\circ(\bar{\theta}^\circ)} \right] \frac{\sin \bar{\theta}}{\sin \bar{\theta}^\circ}}{\int_0^\pi \frac{d\sigma(\theta)}{d\sigma(\pi/2)} \sin \theta d\theta} \quad (2)$$

where  $(d\sigma/d\Omega)$  refers to the differential cross-section for fission at the angle  $\theta$ , which is the center-of-mass angle corresponding to the laboratory angle  $\psi$ . The angle  $\bar{\theta}$  corresponds to the angle  $\bar{\psi}$  determined in the angular correlation experiments.

The cross-sections were measured relative to those for  $^{16}\text{O}$  bombardment of the same target, and the superscript o refers to values obtained with  $^{16}\text{O}$  ions. The quantity  $[\text{d}\sigma(\pi/2)/\text{d}\Omega]_{\text{abs}}$  is the absolute differential cross-section value at the center-of-mass angle  $\pi/2$  for  $^{16}\text{O}$  incident on a given target. These values were taken from Ref. 3. The ratio of the relative differential cross-sections for the ion in question to that of  $^{16}\text{O}$ ,  $\text{d}\sigma(\bar{\theta})/\text{d}\sigma^{\circ\bar{\theta}^{\circ}}$ , was obtained by measuring the number of fragments per bombarding particle at the same detector geometry for each ion. In order to normalize this ratio to  $90^{\circ}$  in the center-of-mass system, this differential cross-section ratio must be multiplied by  $\sin\bar{\theta}/\sin\bar{\theta}^{\circ}$ . This accounts for the angular distribution of the fragments, as is discussed below.

The integral in Eq. (2) accounts for the angular distribution relative to  $90^{\circ}$  for the fission fragments. The actual fragment angular distributions could not be measured because of difficulties in obtaining good fragment spectra for angles near the beam axis. However, it is known that the angular distributions follow the  $1/\sin\theta$  law up to about  $15^{\circ}$  of the beam axis.<sup>3</sup> We have assumed the integral to be  $0.95\pi$  at 10.4-Mev/nucleon and that it decreases linearly with ion energy to  $0.85\pi$  at 6-Mev/nucleon bombarding energy. Errors introduced by this assumption are believed to be about 5%. (By errors we mean standard deviation).

### III. EXPERIMENTAL RESULTS

The fragment-fragment angular correlation functions of all the systems studied here showed only one peak. The positions of the peaks and the fact that they were symmetric clearly demonstrates that all fragments originate from compound nucleus formation between the target and projectile. Such correlation functions have been discussed and analyzed in detail in references 4 and 5.

Values for the fission cross section at various ion energies for the different systems are given in Tables I, II, and III. In the same tables are also listed the ratio  $\sigma_f/\sigma_R$ , where  $\sigma_R$  is the total reaction cross section, and  $\bar{\ell}_R$ , the average angular momentum generated in the reaction. Values for  $\sigma_R$  and  $\bar{\ell}_R$  were calculated as follows:

$$\sigma_R = \sum_{\ell=0}^{\infty} \sigma_{\ell} \quad \text{and} \quad \bar{\ell}_R = \left( \sum_{\ell=0}^{\infty} \ell \sigma_{\ell} \right) / \sigma_R \quad (3)$$

where  $\sigma_{\ell}$  is the cross-section for the  $\ell$ -th partial wave and is given by

$$\sigma_{\ell} = \pi \lambda^2 (2\ell + 1) T_{\ell} \quad (4)$$

Here  $\lambda$  is the de Broglie wave length of the projectile and  $T_{\ell}$  is the transmission coefficient. In the calculation of  $T_{\ell}$  we used the parabolic approximation to the real part of the optical-model potential suggested by Thomas.<sup>9</sup> Values for the parameters of this potential were taken from Viola and Sikkeland.<sup>10</sup>

Generally, the errors in the ratio  $\sigma_f/\sigma_R$  are about ten percent. The data have also been corrected for energy spread in the beam. This correction becomes significant only in regions where the fission cross-section changes rapidly with bombarding energy.

#### IV. DISCUSSION

##### A. Experimental $\langle \Gamma_f/\Gamma_n \rangle$ Values

As pointed out in the previous section, fission takes place only from reactions where a compound nucleus is formed between the bombarding ion and the targets studied in this work. In this case the initial compound nuclei in each reaction studied here all have the same nucleonic composition and excitation energy. The angular momentum distribution is a function of the incident heavy ion and hence varies from one compound nucleus to another. The value of  $\Gamma_f/\Gamma_n$  for a system with a particular angular momentum  $\ell$  is denoted here as  $(\Gamma_f/\Gamma_n)_\ell$  and that obtained by averaging over all  $\ell$ -waves in the reaction is the average level width ratio  $\langle \Gamma_f/\Gamma_n \rangle$ .

In the region where the probability for fission is increasing rapidly with excitation energy, the experimental value of  $\langle \Gamma_f/\Gamma_n \rangle$  can be approximated by the expression

$$\langle \Gamma_f/\Gamma_n \rangle = \sigma_f / (\sigma_{CN} - \sigma_f) \quad (5)$$

where  $\sigma_{CN}$  is the formation cross-section for compound nuclei.

Equation (5) is valid for a given compound nucleus in the case where all fission events occur before neutron evaporation from the compound nucleus. Because of the steepness of the excitation functions in the region of our data, we have assumed that only the first chance fission contributes to the fission cross section. This assumption is not expected to be rigorously true, but calculations by Plasil<sup>11</sup> also indicate that the contribution to the fission cross-section from latter chance fissions should be small. It has also been assumed that charged particle evaporation is a negligible mode of decay for the compound nucleus in regions where the excitation functions increase rapidly.

The total cross-section for compound nucleus formation  $\sigma_{\text{CN}}$  has been derived by correcting the calculated total reaction cross-section  $\sigma_{\text{R}}$  for the effects of surface reactions. The ratio  $\sigma_{\text{CN}}/\sigma_{\text{R}}$  is taken to be 0.82, 0.80, 0.76 and 0.66 for  $^{11}\text{B}$ ,  $^{12}\text{C}$ ,  $^{14}\text{N}$ , and  $^{19}\text{F}$  ions respectively.<sup>3,4</sup> The remainder of the cross-section is assumed to be taken up by surface reactions in which there is incomplete momentum transfer to the struck nucleus. This assumption is discussed in more detail in Ref. 3. The ratios  $\sigma_{\text{CN}}/\sigma_{\text{R}}$  are presumed to be independent of excitation energy and are based on the measurements of Ref. 5.

The ratio  $\sigma_{\text{f}}/(\sigma_{\text{CN}} - \sigma_{\text{f}})$  for the different systems studied here is plotted as a function of excitation energy in Figs. 1, 2, and 3. Fig. 1 also includes the curve for the system  $^{169}\text{Tm} + ^{12}\text{C}$  from Ref. 3. The excitation energies were computed from the bombarding energies and the masses of the nuclei involved in the reaction. Values for the masses were taken from Ref. 12.

The figures show qualitatively the effect of various quantities on the fission probability. Figure 1 shows the effect of target mass on  $\langle \Gamma_f / \langle n \rangle \rangle$  when the same projectile is used to bombard several targets. It is observed that as  $Z$  and  $A$  of the target decreases, the excitation functions are displaced towards higher excitation energies; i.e. the fissionability decreases. A similar shift is observed with  $^{16}\text{O}$  as the bombarding ion.<sup>3</sup> Of special interest is the similarity of the excitation functions for  $^{169}\text{Tm}$  and  $^{174}\text{Yb}$  bombardments. For the compound nuclei  $^{181}\text{Re}$  and  $^{186}\text{Os}$  formed in these reactions the values of the fissionability parameter  $Z^2/A$  and the neutron binding energies are very nearly the same. Hence, the expected dependence of fissionability on  $Z^2/A$  is confirmed.

From Fig. 2 it is apparent that the excitation functions for a particular compound nucleus are the same when  $^{11}\text{B}$  and  $^{12}\text{C}$  are used as bombarding ions. The masses of these ions are similar, resulting in approximately the same  $\ell$ -wave distribution for the compound nuclei formed with each of these ions. In Ref. 3 significant differences were observed between the excitation functions for the compound nucleus  $^{181}\text{Re}$  produced by  $^{12}\text{C}$ ,  $^{16}\text{O}$ , and  $^{22}\text{Ne}$  ions, which give distinctly different angular momentum distributions for bombardment with each ion.

In Fig. 3 are shown the excitation functions for fission of the consecutive isotopes  $^{178}\text{W}$ ,  $^{179}\text{W}$  and  $^{180}\text{W}$ . It is observed that the excitation functions for the two latter converge at low excitation energies, indicating the values of the fission barrier to be quite similar. For higher energies, the system formed with the heaviest

projectile, which involves the largest angular momentum transfer, is found to fission with the highest probability.

B. Theoretical Formula for  $\langle \Gamma_f / \Gamma_n \rangle$ .

In the following discussion we attempt to fit theoretical  $\langle \Gamma_f / \Gamma_n \rangle$  values to the experimental ones at the steep part of the curves where first chance fission dominates. Several formulas based on statistical models exist that relate the ratio  $\langle \Gamma_f / \Gamma_n \rangle$  to various nuclear quantities. A satisfactory fit to the experimental data at low energy has been obtained with one that is based on the level density expression<sup>1</sup>

$$\rho(E) \propto \exp[2(aE)^{1/2}] \quad (6)$$

where angular momentum effects are included in the calculation of the energy E. For the first chance fission we then have:<sup>2</sup>

$$(\Gamma_f / \Gamma_n)_\ell = \frac{K_o [2a_f^{1/2} (E - E'_f - E_R^f)^{1/2} - 1]}{4A^{2/3} (a_f/a_n) (E - B'_n - E_R^o)} \quad (7)$$

$$\exp\{2a_n^{1/2} [(a_f/a_n)^{1/2} (E - E'_f - E_R^f)^{1/2} - (E - B'_n - E_R^o)^{1/2}]\}$$

and the average value of  $\Gamma_f / \Gamma_n$  is:

$$\langle \Gamma_f / \Gamma_n \rangle = \frac{\sum_{\ell=0}^{\ell_{CN}} (\Gamma_f / \Gamma_n)_\ell \sigma_\ell}{\sum_{\ell=0}^{\ell_{CN}} \sigma_\ell} \quad (8)$$



The parameters of the above equations are as follows:

- $E$  - the excitation energy of the compound nucleus;
- $\sigma_{\ell}$  - the partial cross-section for the  $\ell$ -wave ion;
- $K_0$  -  $\approx 9.8$  Mev (Ref. 2);
- $A$  - the mass number of the compound nucleus;
- $a_n$  and  $a_f$  - the level density parameters for neutron evaporation and fission, respectively;
- $E'_f = E_f + \Delta_f$  - the effective neutron binding energy where  $B_n$  is the neutron binding energy and  $\Delta_n$  is the energy gap for the ground state of the nucleus following neutron evaporation;
- $E'_f = E_f + \Delta_f$  - the effective fission barrier, where  $E_f$  is the experimental fission barrier and  $\Delta_f$  is the energy gap for the fissioning nucleus at the transition state configuration;
- $E_R^o = \hbar^2 \ell(\ell + 1)/2 \mathcal{I}_o$  - the rotational energy of the nucleus following neutron evaporation which is characterized by a moment of inertia  $\mathcal{I}_o$ ;
- $E_R^f = \hbar^2 \ell(\ell + 1)/2 \mathcal{I}_f$  - the rotational energy of the fissioning nucleus at the transition state shape with moment of inertia  $\mathcal{I}_f$ , and
- $\ell_{CN}$  - a cut-off value above which compound nucleus formation does not take place. It can be estimated from the equation:

$$\frac{\sigma_{CN}}{\sigma_R} = \frac{\sum_{\ell=0}^{\ell_{CN}} \sigma_{\ell}}{\sum_{\ell=0}^{\infty} \sigma_{\ell}} \quad (9)$$

where  $\sigma_{CN}/\sigma_R$  values are given in Sec. IV A.

In Eq. (7) the effect of quantum-mechanical barrier penetration has been neglected because the excitation energies spanned by the data are well above the fission barriers.<sup>14</sup> We have further ignored the angular momentum carried off by a neutron, which should be a good approximation if our assumption of first chance fission is valid. The quantities  $B'_n$ ,  $E'_f$ ,  $\mathcal{J}_0$ , and  $\mathcal{J}_f$  are all functions of angular momentum since rotation is expected to alter the shapes and masses of the states which decay via neutron evaporation and fission.<sup>11</sup> We have assumed that the inclusion of rotational energy terms in Eq. (7) accounts to first order for the changes in these quantities resulting from deformation due to angular momentum. Thus, these quantities take on the values of their non-rotating equivalents; i.e. the zero angular momentum case.

### C. Fitting Procedure

As expected, good fits were obtained with many sets of values for the parameters introduced in Eqs. (7) and (8). Since the main purpose of the analysis was to extract values for  $E'_f$ , it was necessary to choose values for some of the other parameters; specifically,  $B'_n$ ,  $a_n$ , and  $\mathcal{J}_0$ , the values of which were estimated in the following way:

$\underline{B'_n}$  : Values for  $B_n$  were taken from Ref. 12. The quantity  $\Delta_n$  was set equal to 0,  $\alpha$ , and  $2\alpha$  for an odd-odd, odd-A, and an even-even nucleus, respectively, where  $\alpha = 12/\sqrt{A}$  Mev.

$\underline{a_n}$  : Values were estimated from the formula  $a_n = A/10$  Mev<sup>-1</sup>.

$\mathcal{J}_0$  : For the nucleus after neutron evaporation the moment of inertia is expected to be very nearly equal to the moment of inertia of a rigid body. We have assumed the shape of this state to be spherical so that

$$\mathcal{J}_0 = (2/5)mr_0^2A^{5/3}$$

where  $m$  is one atomic mass unit and  $r_0 = 1.22 \times 10^{-13}$  cm is the nuclear radius parameter.

The uncertainty in  $B'_n$  is about 2 Mev which will introduce a similar error in  $E'_f$ . The parameters  $a_n$  and  $\mathcal{J}_0$  are weakly correlated with the other parameters, e.g.  $E'_f$ ,  $a_f/a_n$ , and  $\mathcal{J}_f/\mathcal{J}_0$  (see Refs. 3 and 13). Hence, the functional forms of  $a_n$  and  $\mathcal{J}_0$  are not critical. We shall in the evaluation of the errors in  $E'_f$ , assign an uncertainty of 1 unit in  $a_n$ . In the fitting process we found that the slope of  $\langle \Gamma_f/\Gamma_n \rangle$  increases strongly when the values of  $a_f/a_n$  and  $\mathcal{J}_f/\mathcal{J}_n$  were respectively, increased or decreased. Their values could both be chosen as constants independent of excitation energy, and of target and ion used. The result of such an analysis is presented below in Sec. IV E. Most importantly, if  $a_f/a_n$  indeed is a constant, the rotational energy terms in Eq. (7) cannot be left out if one is to obtain a fit to the data. When these terms are ignored one obtains, however, equally good fits if  $a_f/a_n$  is allowed to be a function of the target and ion. In this case the angular momentum effects are tied in with the value of  $a_f/a_n$ . The advantage of such a procedure is that one does not have to know the angular momentum distribution of the compound nucleus. The results of such an approach is presented in the following.

D. Level Density Formula Without Rotational Energy Terms.

In this case we have taken  $E'_f$  and  $a_f/a_n$  as the only adjustable parameters, both of which are assumed to be independent of bombarding energy. Their best fit values for the various systems are given in Table IV and the corresponding calculated  $\langle \Gamma_f/\Gamma_n \rangle$  values are presented as curves in Figs. 1 - 3. We see that the fit to experimental values is excellent for the onset of the excitation function. In Fig. 3 are also shown the curves which represent the limits of what we define as a reasonable fit. This introduced errors of only 0.05 and 1.0 Mev in  $a_f/a_n$  and  $E'_f$ , respectively. Their overall errors were 0.10 and 4.0 Mev, respectively, when the errors of 2 Mev in  $B'_n$  and  $10 \text{ Mev}^{-1}$  in  $a_n$  were taken into account.

The data in Table IV show that within the limits of our errors  $a_f/a_n$  is independent of the target used and increases with increasing mass of the ion. This is a direct result of angular momentum effects. That is, the average angular momentum and hence  $\langle \Gamma_f/\Gamma_n \rangle$  increase faster with excitation energy as the mass of the ion increases. Assuming a linear variation of  $a_f/a_n$  with the mass number  $A_i$ , of the ion, we obtain the following empirical relationship:

$$a_f/a_n = 1.11 + 0.075A_i \quad (10)$$

Hence, for a non-rotating system the value of  $a_f/a_n$  is 1.11 which should correspond to the one obtained using the formula containing rotational energy terms. It is difficult to attach physical significance to such an expression. However, such a semi-empirical expression has considerable utility for prediction purposes.

E. Level Density Formula With Rotational Energy Terms.

The best overall fit to the data was obtained with the values 1.20 and 2.0 for the ratios  $a_f/a_n$  and  $\mathcal{J}_f/\mathcal{J}_0$ , respectively. These values are in agreement with previous results.<sup>3</sup> The values for  $E_f'$  are listed in Table IV and the calculated curves for  $\langle \Gamma_f/\Gamma_n \rangle$  were similar to those given in Figs. 1 - 3. The overall error in  $a_f/a_n$  was estimated to be 0.05. This is correlated strongly with  $E_f'$  but rather weakly with  $a_n$ , the ratio  $\mathcal{J}_f/\mathcal{J}_0$ , and the angular momentum distribution, including its variation with excitation energy. The reason for the weak correlation in the latter two cases is that the average values for  $E_R^o$  and  $E_R^f$  are much smaller than those for  $E_f'$ . This introduces, however, a large error in  $\mathcal{J}_f/\mathcal{J}_0$ . For the assumed  $\ell$ -distribution we find this error to be about 0.5. The formula we have used to estimate the  $\ell$ -distribution is semi-empirical and contains several parameters whose values have been obtained by extrapolation. The reliability of this cannot be evaluated. The errors in the parameters  $a_f/a_n$ ,  $\mathcal{J}_f/\mathcal{J}_0$ ,  $B_n'$ , and  $a_n$  introduce in  $E_f'$  the errors 1.5 Mev, 1.2 Mev, 2.0 Mev, and 0.8 Mev respectively, to a combined uncertainty of about  $\pm 3.0$  Mev for  $E_f'$ .

V. CONCLUSION

The data in Table IV suggest that the average values for  $E_f'$  and  $a_f/a_n$  are respectively, only about 1.5 Mev lower and 0.02 higher when the formula without rotational energy terms is used. In Table IV we

have also listed the values for  $E_f$  as estimated by Myers and Swiatecki using a semi-empirical formula.<sup>15</sup> The agreement is quite consistent with the predictions of Ref. 15. It is interesting to note that the average difference between the values of  $E_f$  and  $E'_f$  corresponds to a value of 0.7 Mev and 1.4 Mev for the energy gap at saddle of an odd-A and an even-even nucleus, respectively. However, the uncertainty in the data is too large to take these values for the energy gap seriously. A linear extrapolation of the values for  $a_f/a_n$  given in Table IV yields a value of 1.11 for  $a_f/a_n$  for a non-rotating system. This is substantially lower than the value of 1.20 obtained with the formula which contains rotational energy terms. Since we do not know if such a linear extrapolation is justified we suggest rather conservatively that in this region of the periodic table the value of  $a_f/a_n$  is  $1.20 \pm 0.10$ .

Our conclusion is that when  $E'_f$  is large the inclusion or exclusion of rotational energy terms in the formula for  $\langle \Gamma_f/\Gamma_n \rangle$  yields similar values for  $E'_f$  and  $a_f/a_n$ . The latter analysis is rather easy to perform. We should finally reemphasize that the fits have been made only at the lowest energies of the excitation functions. As the energy increases the deviation between calculated and experimental  $\langle \Gamma_f/\Gamma_n \rangle$  values increases. Possible reasons for this discrepancy have been discussed in Ref. 3.

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Table I. Values for  $\sigma_f$ ,  $\sigma_f/\sigma_R$  and  $\bar{l}_R$  at various laboratory ion energies,  $E_L$ , for the systems ( $^{159}\text{Tb} + ^{19}\text{F}$ ) and ( $^{165}\text{Ho} + ^{14}\text{N}$ ) where  $\sigma_f$  is the total experimental fission cross-section and  $\sigma_R$  and  $\bar{l}_R$  are respectively, the estimated total cross-section and average angular momentum in the interaction.

<u><math>^{159}\text{Tb} + ^{19}\text{F}</math></u>				<u><math>^{165}\text{Ho} + ^{14}\text{N}</math></u>			
<u><math>E_L</math> (Mev)</u>	<u><math>\bar{l}_R</math> (<math>\hbar</math>)</u>	<u><math>\sigma_f</math> (mb)</u>	<u><math>\sigma_f/\sigma_R</math></u>	<u><math>E_L</math> (Mev)</u>	<u><math>\bar{l}_R</math> (<math>\hbar</math>)</u>	<u><math>\sigma_f</math> (mb)</u>	<u><math>\sigma_f/\sigma_R</math></u>
193.8	68.0	530	$2.30 \cdot 10^{-1}$	145.3	50.5	241	$1.10 \cdot 10^{-1}$
170.2	60.0	516	$2.46 \cdot 10^{-1}$	140.0	48.7	192	$8.97 \cdot 10^{-2}$
155.0	55.5	421	$2.16 \cdot 10^{-1}$	134.5	47.0	183	$8.88 \cdot 10^{-2}$
143.5	51.0	329	$1.81 \cdot 10^{-1}$	122.5	43.0	109	$5.71 \cdot 10^{-2}$
132.2	46.4	219	$1.32 \cdot 10^{-1}$	115.7	40.7	68.9	$3.81 \cdot 10^{-2}$
120.6	42.0	166	$1.15 \cdot 10^{-1}$	109.5	38.4	37.0	$2.18 \cdot 10^{-2}$
113.8	35.0	120	$9.40 \cdot 10^{-2}$	105.9	37.0	30.0	$1.83 \cdot 10^{-2}$
107.9	30.5	62.0	$5.48 \cdot 10^{-2}$	102.7	35.6	19.7	$1.26 \cdot 10^{-2}$
101.1	28.0	28.8	$3.10 \cdot 10^{-2}$	102.2	35.4	17.7	$1.13 \cdot 10^{-2}$
94.2	26.0	8.0	$1.13 \cdot 10^{-2}$	98.7	34.0	11.2	$7.57 \cdot 10^{-3}$
87.0	19.1	1.4	$3.4 \cdot 10^{-3}$	96.0	32.7	6.9	$4.9 \cdot 10^{-3}$
				95.2	32.2	7.9	$5.6 \cdot 10^{-3}$
				91.4	30.4	4.1	$3.2 \cdot 10^{-3}$
				91.1	30.2	4.2	$3.3 \cdot 10^{-3}$
				88.0	28.6	3.1	$2.6 \cdot 10^{-3}$
				87.4	28.2	1.5	$1.3 \cdot 10^{-3}$
				83.2	25.8	0.4	$3.9 \cdot 10^{-4}$

Table II. Values for  $\sigma_f$ ,  $\sigma_f/\sigma_R$  and  $\bar{l}_R$  at various laboratory ion energies,  $E_L$ , for the systems ( $^{169}\text{Tm} + ^{11}\text{B}$ ) and ( $^{175}\text{Lu} + ^{11}\text{B}$ ) where  $\sigma_f$  is the total experimental fission cross-section, and  $\sigma_R$  and  $\bar{l}_R$  are respectively, the estimated total cross-section and average angular momentum in the interaction.

<u><math>^{169}\text{Tm} + ^{11}\text{B}</math></u>				<u><math>^{175}\text{Lu} + ^{11}\text{B}</math></u>			
<u><math>E_L</math> (Mev)</u>	<u><math>\bar{l}_R</math> (<math>\hbar</math>)</u>	<u><math>\sigma_f</math> (mb)</u>	<u><math>\sigma_f/\sigma_R</math></u>	<u><math>E_L</math> (Mev)</u>	<u><math>\bar{l}_R</math> (<math>\hbar</math>)</u>	<u><math>\sigma_f</math> (mb)</u>	<u><math>\sigma_f/\sigma_R</math></u>
114.4	41.0	74.8	$3.28 \cdot 10^{-2}$	114.4	41.2	134	$5.80 \cdot 10^{-2}$
108.6	39.5	60.0	$2.70 \cdot 10^{-2}$	110.0	39.7	101	$4.51 \cdot 10^{-2}$
105.8	38.5	50.9	$2.31 \cdot 10^{-2}$	105.7	38.5	71.9	$3.34 \cdot 10^{-2}$
102.6	37.5	47.3	$2.19 \cdot 10^{-2}$	101.2	37.0	58.6	$2.79 \cdot 10^{-2}$
96.5	35.5	26.2	$1.28 \cdot 10^{-2}$	96.6	35.5	31.4	$1.53 \cdot 10^{-2}$
89.8	33.0	12.5	$6.47 \cdot 10^{-3}$	93.5	34.5	26.4	$1.32 \cdot 10^{-2}$
86.4	32.0	9.9	$5.27 \cdot 10^{-3}$	88.4	32.6	15.3	$8.05 \cdot 10^{-3}$
82.9	30.5	5.5	$3.0 \cdot 10^{-3}$	83.3	30.7	6.6	$3.7 \cdot 10^{-3}$
81.0	30.0	4.5	$2.6 \cdot 10^{-3}$	79.6	29.3	4.7	$2.8 \cdot 10^{-3}$
77.8	28.5	4.3	$2.6 \cdot 10^{-3}$	71.6	25.7	1.7	$1.2 \cdot 10^{-3}$
73.4	27.0	1.5	$9.5 \cdot 10^{-4}$	69.6	24.8	0.9	$7.0 \cdot 10^{-4}$
71.3	26.0	1.2	$8.1 \cdot 10^{-4}$				

Table III. Values for  $\sigma_f$ ,  $\sigma_R$  and  $\bar{l}_R$  at various laboratory ion energies,  $E_L$ , for  $^{12}\text{C}$  ions incident on  $^{174}\text{Yb}$ ,  $^{175}\text{Lu}$  and  $^{182}\text{W}$  where  $\sigma_f$  is the total experimental fission cross-section, and  $\sigma_R$  and  $\bar{l}_R$  are respectively, the estimated total cross-section and average angular momentum in the interaction.

$E_L$ (Mev)	$^{174}\text{Yb} + ^{12}\text{C}$			$^{175}\text{Lu} + ^{12}\text{C}$			$^{182}\text{W} + ^{12}\text{C}$		
	$\bar{l}_R$ ( $\hbar$ )	$\sigma_f$ (mb)	$\sigma_f/\sigma_R$	$\bar{l}_R$ ( $\hbar$ )	$\sigma_f$ (mb)	$\sigma_f/\sigma_R$	$\bar{l}_R$ ( $\hbar$ )	$\sigma_f$ (mb)	$\sigma_f/\sigma_R$
124.6	43.1	106	$4.91 \cdot 10^{-2}$	43.0	241	$1.12 \cdot 10^{-1}$	43.0	752	$3.58 \cdot 10^{-1}$
120.2	42.0	93.1	$4.43 \cdot 10^{-2}$	41.9	220	$1.05 \cdot 10^{-1}$	41.8	745	$3.61 \cdot 10^{-1}$
116.3	40.8	69.8	$3.39 \cdot 10^{-2}$	40.5	178	$8.77 \cdot 10^{-2}$	40.2	612	$3.06 \cdot 10^{-1}$
111.8	39.4	48.6	$2.45 \cdot 10^{-2}$	39.1	147	$7.56 \cdot 10^{-2}$	38.5	551	$2.87 \cdot 10^{-1}$
109.7	--	--	--	37.8	103	$5.37 \cdot 10^{-2}$	38.0	519	$2.73 \cdot 10^{-1}$
107.8	38.9	34.9	$1.81 \cdot 10^{-2}$	--	--	--	37.1	493	$2.66 \cdot 10^{-1}$
102.8	36.2	22.9	$1.24 \cdot 10^{-2}$	35.9	72.9	$4.02 \cdot 10^{-2}$	35.6	382	$2.18 \cdot 10^{-1}$
98.2	34.5	11.0	$6.3 \cdot 10^{-3}$	--	--	--	35.3	322	$1.94 \cdot 10^{-1}$
95.8	--	--	--	33.5	36.3	$2.17 \cdot 10^{-2}$	--	--	--
93.2	--	--	--	--	--	--	31.6	223	$1.44 \cdot 10^{-1}$
90.6	31.4	4.5	$2.9 \cdot 10^{-3}$	31.2	24.4	$1.58 \cdot 10^{-2}$	30.8	153	$1.03 \cdot 10^{-1}$
88.1	30.1	3.1	$2.1 \cdot 10^{-3}$	29.9	17.2	$1.18 \cdot 10^{-2}$	29.2	140	$9.86 \cdot 10^{-2}$
85.6	29.1	1.9	$1.3 \cdot 10^{-3}$	28.8	10.8	$7.7 \cdot 10^{-3}$	--	--	--
82.7	--	--	--	27.2	6.2	$4.7 \cdot 10^{-3}$	26.8	54.9	$4.39 \cdot 10^{-2}$
79.8	26.3	0.6	$4.5 \cdot 10^{-4}$	26.0	4.0	$3.3 \cdot 10^{-3}$	--	--	--
77.9	25.3	0.4	$3.4 \cdot 10^{-4}$	24.8	1.9	$1.5 \cdot 10^{-3}$	24.2	30.8	$2.63 \cdot 10^{-2}$
74.3	--	--	--	22.8	1.2	$1.1 \cdot 10^{-3}$	22.2	11.4	$1.19 \cdot 10^{-2}$
70.8	--	--	--	--	--	--	20.0	9.2	$1.15 \cdot 10^{-2}$

Table IV. Various quantities used in the fit of calculated  $\langle \Gamma_f / \Gamma_n \rangle$  values to experimental ones, and a comparison of experimental and calculated fission barrier values.

System	Compound Nucleus	$Z^2/A$	$B'_n$ (Mev)	$a_f/a_n^a$	$E_f^a$ (Mev)	$E_f^b$ (Mev)	$E_f^d$ (Mev)
$^{159}\text{Tb} + ^{19}\text{F}$	$^{178}\text{W}$	30.76	10.7	1.25	21.5	23.0	25.3 <sup>e</sup>
$^{165}\text{Ho} + ^{14}\text{N}$	$^{179}\text{W}$	30.59	7.5	1.24	23.2	25.2	25.6 <sup>e</sup>
$^{169}\text{Tm} + ^{11}\text{B}$	$^{180}\text{W}$	30.42	10.3	1.19	25.0	28.7	25.0
$^{169}\text{Tm} + ^{12}\text{C}$	$^{181}\text{Re}$	31.08	9.7	1.21	24.0	25.0 <sup>c</sup>	23.9 <sup>e</sup>
$^{174}\text{Yb} + ^{12}\text{C}$	$^{186}\text{Os}$	31.05	10.0	1.20	24.7	25.7	23.2
$^{175}\text{Lu} + ^{11}\text{B}$	$^{186}\text{Os}$	31.05	10.0	1.20	24.9	26.0	23.2
$^{175}\text{Lu} + ^{12}\text{C}$	$^{187}\text{Ir}$	31.71	9.4	1.20	21.6	21.8	21.1
$^{182}\text{W} + ^{12}\text{C}$	$^{194}\text{Hg}$	32.99	10.2	1.20	19.8	19.4	18.3

a Best fit values when  $a_n = A/10 \text{ Mev}^{-1}$  and rotational energy terms are ignored.

b Best fit values when  $a_n = A/10 \text{ Mev}^{-1}$ ,  $a_f/a_n = 1.20$ , and  $\frac{J_f}{J_0} = 2.0$ .

c Data taken from Ref. 3.

d Values taken from Ref. 15.

e This value is equal to that of the saddle mass, as taken from Ref. 15, reduced by 1.0 Mev.

Figure Captions

Fig. 1. Experimental  $\langle \Gamma_f / \Gamma_n \rangle$  values as function of the excitation energy,  $E$ , of the compound nucleus with  $^{12}\text{C}$  incident on  $^{182}\text{W}$  ( $\square$ );  $^{175}\text{Lu}$  ( $\blacktriangle$ );  $^{174}\text{Yb}$  ( $\circ$ ); and  $^{169}\text{Tm}$  ( $\triangle$ ).

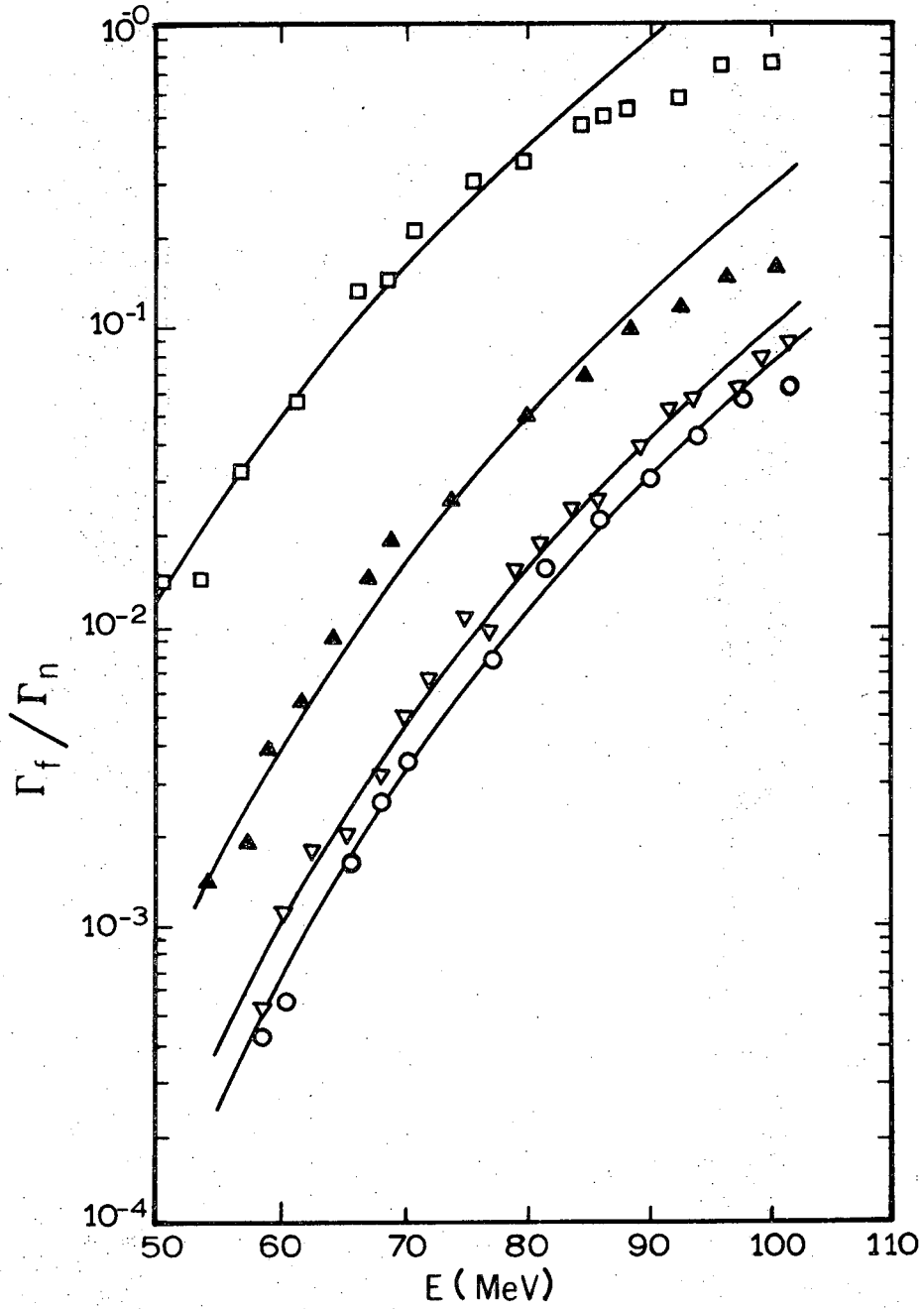
The curves are calculated using the formula without rotational energy terms with  $a_n = A/10 \text{ MeV}^{-1}$  and with the values for  $B'_n$ ,  $a_f/a_n$ , and  $E'_f$  as given in Table IV.

Fig. 2. Experimental  $\langle \Gamma_f / \Gamma_n \rangle$  values as function of the excitation energy,  $E$ , of the compound nucleus for the reactions  $^{174}\text{Yb} + ^{12}\text{C} = ^{186}\text{Os}$  ( $\circ$ ) and  $^{175}\text{Lu} + ^{11}\text{B} = ^{186}\text{Os}$  ( $\triangle$ ).

The curve is calculated using the formula without rotational terms with  $a_n = A/10 \text{ MeV}^{-1}$ ,  $B'_n = 10.0 \text{ MeV}$ ,  $a_f/a_n = 1.20$ , and  $E'_f = 24.7 \text{ MeV}$ .

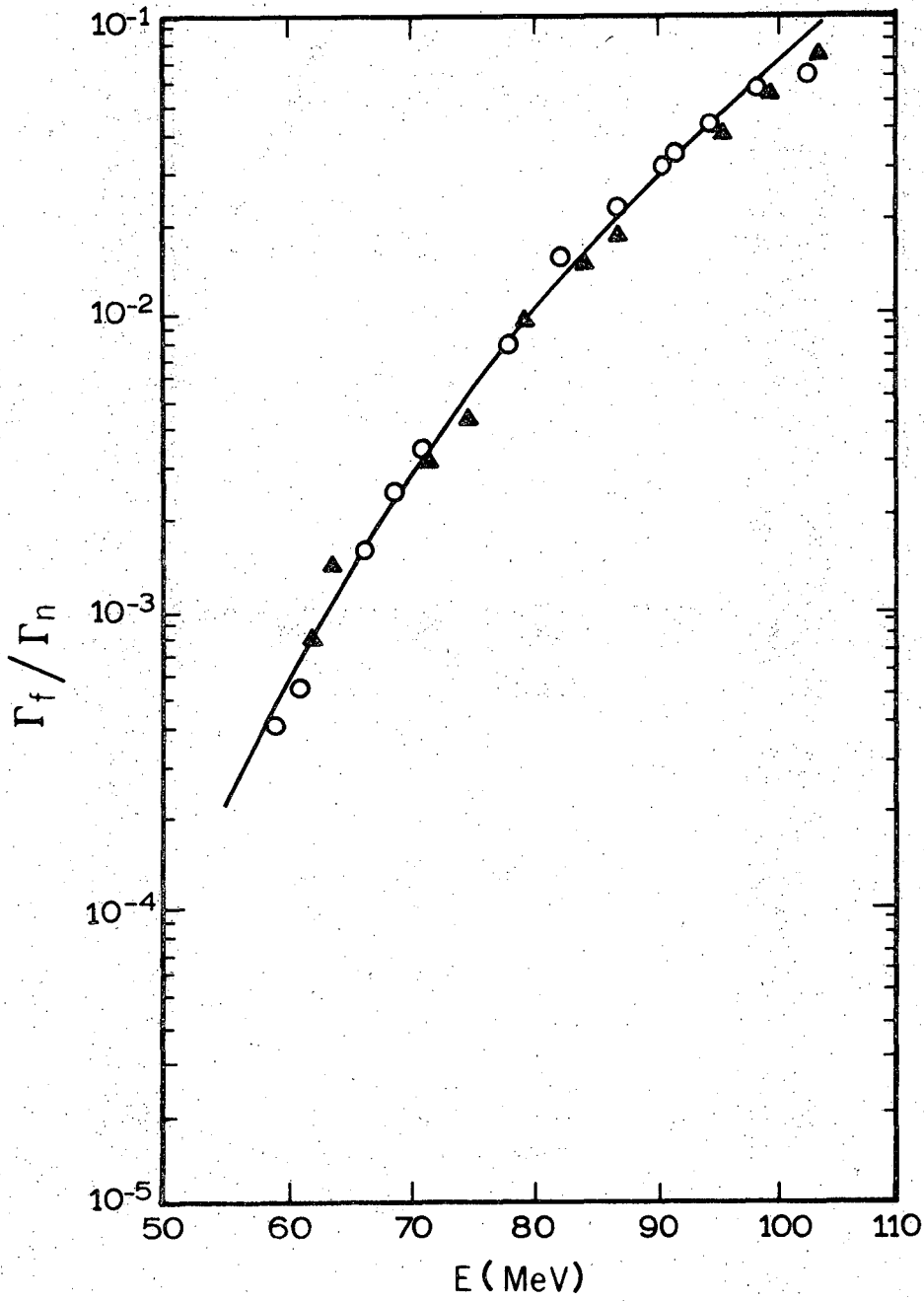
Fig. 3. Experimental  $\langle \Gamma_f / \Gamma_n \rangle$  values as function of the excitation energy,  $E$ , of the compound nucleus for the reactions  $^{159}\text{Tb} + ^{19}\text{F} = ^{178}\text{W}$  ( $\blacktriangle$ ),  $^{165}\text{Ho} + ^{14}\text{N} = ^{179}\text{W}$  ( $\triangle$ ), and  $^{169}\text{Tm} + ^{11}\text{B} = ^{180}\text{W}$  ( $\circ$ ).

The curves are calculated using the formula without rotational energy terms with  $a_n = A/10 \text{ MeV}^{-1}$  and with values for  $B'_n$  as given in Table IV. For the solid lines we used the best fit values for  $a_f/a_n$  and  $E'_f$  as listed in Table IV. For the dashed lines labeled a and b, we used  $a_f/a_n = 1.20$  and  $E'_f = 22.4 \text{ MeV}$ , and  $a_f/a_n = 1.30$  and  $E'_f = 24.8 \text{ MeV}$ , respectively.



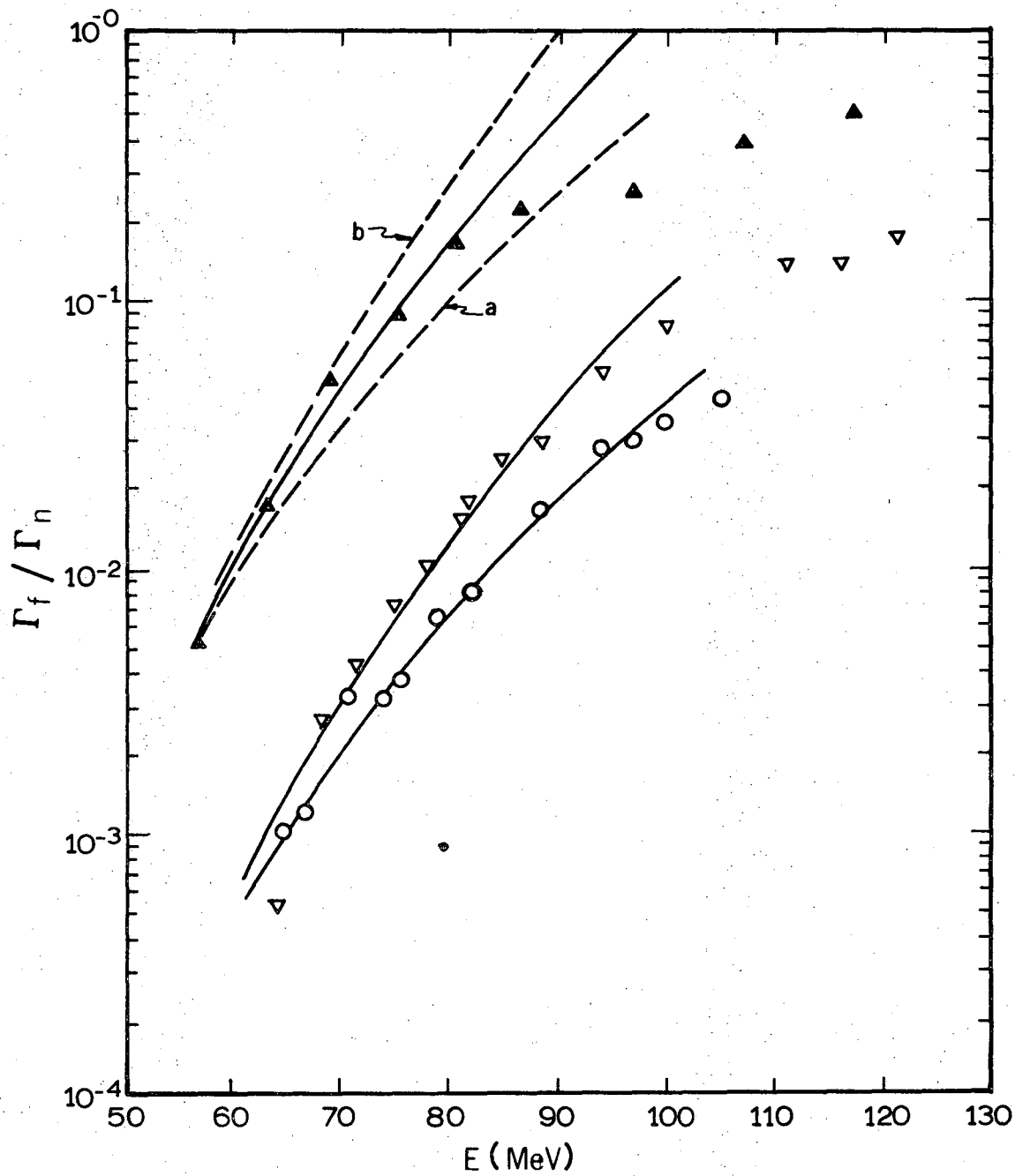
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Fig. 1



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Fig. 2



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Fig. 3



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