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Publication Date

2008-11-18

Interface Structure and Transport of Complex Oxide Junctions

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ABSTRACT

The interface structure and magnetism of hybrid magnetic tunnel junction-spin filter devices have been investigated and correlated with the transport behavior exhibited. Magnetic tunnel junctions made of theoretically predicted half-metallic electrodes (perovskite $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ and spinel Fe_3O_4) sandwiching a spinel NiMn_2O_4 tunnel barrier exhibit very high crystalline quality as observed by transmission electron microscopy. Structurally abrupt interfaces allow for the distinct magnetic switching of the electrodes as well as large junction magnetoresistance. The change in the magnetic anisotropy observed at the spinel-spinel interface supports the presence of limited interdiffusion and the creation of a magnetically soft interfacial layer, whose strong exchange coupling to the Fe_3O_4 electrode likely accounts for the low background magnetoresistance observed in these junctions, and the successful spin filtering when the barrier layer is ferrimagnetic.

Interfaces play a crucial role in determining electrical transport across magnetic junction devices. Without considering the effects of the electrode-barrier interfaces, spin dependent transport behavior in magnetic junctions cannot be fully explained and understood. For example, the simple Julliere model^[Julliere] of a magnetic tunnel junction (MTJ) where the conductance depends on the relative bulk spin polarization of the electrodes does not adequately describe real MTJs. It is now largely acknowledged that the interfacial electronic structure needs to be taken into account to accurately describe magnetic tunnel junction experiments.^[Woods] Recently, magnon excitations at interfaces^[Moosera] and bonding effects at the electrode/barrier interface^[Butler] have also been identified as factors affecting junction transport.

Our recent work on magnetic junctions composed of perovskite structure $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ (LSMO) and spinel structure Fe_3O_4 electrodes with spinel structure NiMn_2O_4 (NMO) barrier layers have shown that even within one junction, the transport can be dominated by the electrode-barrier interfaces or the bulk properties of the barrier layer itself depending on whether NMO is paramagnetic or ferrimagnetic, respectively.^[NC07] These two different conduction mechanisms directly highlight the passive or active role of the barrier layer in comparison to electrode-barrier interfaces in the spin transport. More specifically, above the T_C of the NMO barrier, when the barrier layer is paramagnetic, the two different electrode-barrier interfaces dominate the spin transport behavior, resulting in an asymmetric bias dependence of the junction magnetoresistance (JMR) and inelastic tunneling spectra (IETS). Below the T_C of the NMO barrier, the properties of the barrier dominate the spin transport behavior over that of electrode-barrier effects, resulting in a transition to a symmetric bias dependence of the JMR and IETS.

Our discovery of the coexistence of magnetic tunneling behavior when the NMO is paramagnetic and spin filtering behavior when the NMO is ferrimagnetic suggests new routes in

the design of magnetic devices where the transport can be tuned by the barrier layer. Both tunneling and spin filtering behavior, in different temperature regimes, are possible because of the lack of magnetic coupling at the non-isostructural perovskite-spinel LSMO/NMO interface and strong magnetic coupling at the isostructural spinel-spinel NMO/Fe₃O₄ interface. This has been verified by element specific X-ray magnetic circular dichroism interface studies.^[NC07,NC08] However the atomic structure of the LSMO/NMO perovskite-spinel interface and NMO/Fe₃O₄ interfaces must be explored in an effort to explain the magnetic interactions at these interfaces. The structure and magnetism at each interface must then be correlated with the transport behavior in these half-metal-based junctions.

In this paper, we correlate the interface structure of these hybrid MTJ-spin filter devices with the magnetotransport. With our transmission electron microscopy (TEM) and scanning TEM (STEM) studies, we will show the successful deposition of highly crystalline abrupt perovskite-spinel heterointerfaces. In these crystalline LSMO/NMO/Fe₃O₄ heterostructures, the JMR is as high as -30% and the magnetic switching is sharp and distinct, indicating that the electrodes are not magnetically coupled. We will show that the change in the magnetic anisotropy at the NMO/Fe₃O₄ spinel interface supports the presence of a magnetically soft thin interdiffused interface layer of (Fe,Mn,Ni)₃O₄, whose exchange coupling to the Fe₃O₄ electrode likely accounts for the low background magnetoresistance seen in these junctions, and the successful spin filtering when the barrier layer is ferrimagnetic.

For this study, MTJs of LSMO/NMO/Fe₃O₄ and NMO single layer films were synthesized. Fe₃O₄ and LSMO were chosen as electrode materials as they have theoretically and experimentally been shown to be half-metallic.^[Yanase84,Zhang91,Picket97] Since isostructural barrier layers have proven to greatly increase the JMR values for Fe₃O₄-based MTJs,^[Hu02] the

ferrimagnetic spinel, NiMn_2O_4 , was selected. The trilayers of LSMO/NMO/ Fe_3O_4 were grown on (110)-oriented single crystal SrTiO_3 (STO) substrates by pulsed laser deposition with a KrF excimer laser (248 nm) operating at 10 Hz with an energy density of approximately 1.5 J/cm^3 . Both (110)-oriented LSMO and Fe_3O_4 films have strong in-plane uniaxial anisotropy, which is optimal for magnetic switching, along the [100] easy direction. Recent work on the manganites also suggests that the magnetism of (110) planes is more robust than that of (001) planes.^[Infante08] The LSMO perovskite layer was deposited first at 700°C in 320 mtorr of O_2 . The NMO spinel layer was grown next at 550°C in 10mTorr of a 99% N_2 /1% O_2 gaseous mixture. Single NMO films prepared under these conditions exhibit a T_C of about 60 K, a large coercive field of 1.8 T at 30 K, and a magnetization of $0.8 \mu\text{B/formula unit}$. Finally, the Fe_3O_4 spinel layer was synthesized at 400°C in vacuum. The bulk lattice parameters of the STO and LSMO perovskites are 3.905 \AA and 3.873 \AA , respectively. The bulk lattice parameters of the NMO and Fe_3O_4 spinels are almost twice that of the perovskites and are 8.379 \AA and 8.397 \AA , respectively. This 2-to-1 perovskite-spinel unit cell stacking allows for near epitaxial growth of perovskite-spinel heterostructures, although a large lattice mismatch of almost 8% exists between the two structures. The junctions were composed of electrodes layers of 40-50 nm thick and NMO barrier thicknesses of 2.0, 3.0, and 4.5 nm.

The crystallinity and epitaxy of the individual electrode and barrier layers in the trilayer heterostructure were investigated by high resolution X-ray diffraction on an X'Pert Pro MRD and cross-sectional TEM and STEM using a FEI F20 UT Tecnai microscope at the National Center for Electron Microscopy, Lawrence Berkeley National Laboratory. Cross-sectional TEM was also used to study the interface structure in the trilayer heterostructure. Magnetization of the films was studied by a Quantum Design superconducting quantum interference device (SQUID)

magnetometer. The magnetism at the interfaces was also investigated by surface sensitive, element specific X-ray magnetic circular dichroism (XMCD) at the Advanced Light Source. As the mean probe depth of these techniques is approximately 5 nm, the bottom LSMO/NMO interface was investigated using a STO(110)/LSMO(40nm)/NMO(5nm) sample, while the top NMO/Fe₃O₄ interface was investigated using a STO(110)/LSMO(40nm)/NMO(5nm)/Fe₃O₄(5nm) sample. The Fe₃O₄ magnetism away from the NMO/Fe₃O₄ interface was also investigated with a STO(110)/LSMO(40nm)/NMO(5nm)/Fe₃O₄(8nm) sample, in which the top Fe₃O₄ layer was sufficiently thick so that the NMO/Fe₃O₄ interface was not accessed.

The MTJ structures were fabricated by conventional contact alignment photolithography and Ar ion milling. Magnetotransport measurements, including resistance versus applied magnetic field and current versus voltage, were taken between 5 K and 400 K and up to 8 kOe with a modified Quantum Design Physical Property Measurement System (PPMS). The magnetic field was applied along the [001]-in-plane magnetically easy direction of the two magnetic electrodes. The JMR were calculated in accordance with Julliere's model by the following equation: $[\Delta R/R_P]*100$ where $\Delta R=R_{AP}-R_P$. The reference (parallel magnetization) resistance was taken as the resistance at 8 kOe in the high junction resistance state.

X-ray diffraction taken of the trilayer heterostructures indicates excellent crystallinity and epitaxy. Scans taken in the $2\theta-\theta$ geometry show only {110}-oriented peaks for the Fe₃O₄, NMO and LSMO layers grown on (110) STO substrates, thus indicating out-of-plane epitaxy. Phi scans of the heterostructures also demonstrate in-plane registry with two-fold symmetry of the {001}-oriented peaks.

Cross sectional TEM elucidates both the microstructure of the perovskite and spinel as well as the coherence of the perovskite-spinel (LSMO/NMO) interface. The phase-contrast TEM lattice image in Figure 1(a) demonstrates that it is possible to obtain abrupt interfaces between the perovskite and spinel layers in the magnetic junctions. Figure 1(a) was taken of the trilayer structure along the [001] zone axis and shows highly crystalline LSMO, an abrupt and coherent spinel-perovskite interface, and spinel layers with high crystallinity. The spinel-spinel interface cannot be identified by TEM or STEM due to the similarities in both atomic number and crystal structure of NMO and Fe_3O_4 . The epitaxy of the trilayer is confirmed by the Fast Fourier Transform on the TEM image, shown in Figure 1(b), where the double spots are a signature of the lattice mismatch of LSMO and spinel layers, and demonstrate both in-plane and out-of-plane crystalline registry of the spinel with the perovskite template. Despite the relatively large lattice mismatch between the perovskite and spinel films, the spinel layers grow coherently on the LSMO with crystalline registry and good crystalline quality. However, even with the relatively high crystalline quality of the spinel films, the large lattice mismatch between the perovskite and spinel structures inevitably creates defects at the perovskite-spinel interface as well as the spinel layers themselves. The high-resolution STEM image of the Fe_3O_4 film in Figure 1(c) shows that we obtain very high-quality crystallinity of the Fe_3O_4 on a local atomic level, despite extended defects. Although the spinel films are not perfectly epitaxial, a combination of low-angle grain boundaries, anti-phase boundaries, and dislocations act as mechanisms for lattice relaxation that allow the spinel films to maintain good structural registry with the perovskite underlayer. While in general defects in heterostructures may be seen as undesirable, defects observed in the spinel Fe_3O_4 are crucial in the ability to grow relatively thick crystalline spinel films on highly mismatched perovskite underlayers. In addition, as seen from both SQUID magnetometry and

XMCD measurements, these defects do not significantly degrade the magnetic properties of the highly spin polarized Fe_3O_4 , and they prevent the coupling of the perovskite LSMO to the spinel NMO and Fe_3O_4 at the perovskite/spinel interface.^[N-C07]

Having established the structural integrity of the trilayer heterostructures, the magnetic order near each interface was probed by surface sensitive XMCD using total electron yield detection.^[NC07,NC08] Element specific hysteresis loops can be obtained by choosing specific X-ray energies corresponding to the Mn, Ni and Fe $L_{2,3}$ absorption edges. At the LSMO/NMO interface, the magnetism was probed via only the Mn ions because the Ni $L_{2,3}$ absorption edges overlap with the La $M_{4,5}$ absorption edges of the LSMO. While Mn is found in both NMO and LSMO, the differences in valence and site symmetry of the Mn ions in the spinel and perovskite structures allows for the differentiation and identification of the Mn in each layer. Furthermore, Mn XMCD hysteresis loops taken at two different energies (640.0 eV and 642.5 eV) in the Mn XMCD spectrum exhibit magnetically hard and magnetically soft behavior, respectively, at 55 K as shown in Figure 2. These two energies correspond to the magnetic behavior of the Mn in the NMO layer and the Mn in the LSMO layer, respectively.^[NC07] Thus, there appears to be no noticeable coupling of magnetic ions at the LSMO/NMO interface even when the NMO is ferrimagnetic. This magnetic decoupling of the adjacent magnetic layers is necessary to achieve the spin-filter effect observed in these junctions.^[NC07]

At the NMO/ Fe_3O_4 interface, both Ni and Mn exhibit long range magnetic order at room temperature and their hysteresis loops coincide with those of Fe.^[N-C08] Although the normalized Ni, Mn and Fe XMCD hysteresis loops from the trilayer sample are identical for all temperatures, the shape of the hysteresis loops changes distinctly below 60K, exhibiting magnetically harder hysteresis loops once the NMO layer becomes ferrimagnetic. These

coincident loops are strong evidence for magnetic coupling at the NMO/Fe₃O₄ interface, causing the NMO/Fe₃O₄ layers to act as a magnetic stack, rather than two independent layers, as one would expect in a normal MTJ. We have also recently found that at the NMO/Fe₃O₄ interface there is a thin interdiffused region of (Fe,Mn,Ni)₃O₄ leading to Mn and Ni magnetic properties similar to MnFe₂O₄ and NiFe₂O₄ by XMCD and X-ray absorption spectroscopy. ^[NC08]

A closer look at the magnetic properties of the sublayer region by XMCD indicates that the interdiffused (Fe,Mn,Ni)₃O₄ layer is magnetically softer than the NMO and Fe₃O₄ layers. Whereas the magnetically hard nature of the NMO layer was evidenced while investigating the LSMO/NMO interface and is shown in Figure 2, the bulk Fe₃O₄ layer also has a larger coercive field than the interdiffused sublayer region, as shown in Figure 3. Therefore, at the NiMn₂O₄/(Fe,Mn,Ni)₃O₄/Fe₃O₄ interface, the magnetically soft interdiffused sublayer couples to the Fe₃O₄ and NMO layers. When the NMO layer is paramagnetic, the sublayer magnetic moments magnetically switch with the interfacial Fe₃O₄ moments [Figure 4(a)]. When the NMO is ferrimagnetic, the sublayer and Fe₃O₄ moments switch with the interfacial NMO moments, resulting in an abrupt increase in coercive field below the NMO T_C [Figure 4(b)].

Hysteresis loops taken of the NMO/Fe₃O₄ interface in a trilayer sample also demonstrate that the in-plane [11-0] direction is in fact magnetically easier for the interfacial Fe, Mn and Ni than the in-plane [001] direction both above and below the Curie temperature of the NMO barrier layer. This anisotropy is in contrast with the in-plane [001] easy direction exhibited by both the LSMO and Fe₃O₄ electrodes grown on STO(110) substrates. This observation provides further evidence that a (Fe,Mn,Ni)₃O₄ interfacial sublayer is present which exhibits properties similar to MnFe₂O₄ and NiFe₂O₄. ^[Harrison58]

The transport of the fabricated MTJs with an abrupt LSMO/NMO interface and an

interdiffused NMO/Fe₃O₄ interface exhibit square junction magnetoresistance (JMR) loops with flat background magnetoresistance (MR) at high magnetic fields. As shown in Figure 5(a), transitions in the magnetization hysteresis loops coincide well with large and abrupt transitions in the JMR. The low resistance state occurs when the two magnetic electrodes are magnetized antiparallel to one another resulting in negative JMR values. This negative JMR is due to the opposite spin polarizations of the LSMO and Fe₃O₄ electrodes, which are majority and minority spin polarized, respectively.^[Hu02] The background magnetoresistance (MR) as a fraction of the maximum JMR for these junctions, as shown in Figure 5(b), is significantly lower than that previously seen in similar LSMO-Fe₃O₄ junctions with other spinel barrier layers. These junctions exhibited background MR values two to four times larger when barrier layers of CoCr₂O₄, MgTi₂O₄ and FeGa₂O₄ were used.^[Hu02, Alldredge06]

The interface structure and magnetic behavior of the NMO barrier layer can now be correlated to the junction transport. First, the abrupt switching of the JMR, even when the NMO is magnetic, indicates that the use of a magnetic barrier layer does not preclude the presence of distinct parallel and antiparallel spin polarized states at the electrode-barrier interfaces. The structurally distinct perovskite-spinel interface seen in the cross-sectional TEM likely contributes to the abrupt switching of the electrodes near the electrode-barrier interface by decreasing any electrode-electrode or electrode-barrier orange-peel coupling. Furthermore, the misfit dislocations present at the spinel-perovskite interface seem to eliminate exchange coupling between the magnetic layers across the non-isostructural interface, thereby decoupling the perovskite and spinel layers, allowing for the feasibility of a distinct antiparallel magnetization configuration between the electrodes.

Moreover, the relatively low background magnetoresistance exhibited by these junctions

compared to other LSMO/Fe₃O₄-based junctions is likely associated with the properties of the thin interfacial (Fe,Mn,Ni)₃O₄ layer at the NMO/Fe₃O₄ interface and its interaction with the surrounding Fe₃O₄ and NMO. Since the parallel electrode magnetization configuration exhibits the highest resistance, we can hypothesize that the resistance rise with growing magnetic field is an indication of the increasingly parallel alignment of the interfacial electrode spins. In other words, larger (smaller) background magnetoresistance is an indication of greater (less) misalignment between the spin orientations of the two electrode-barrier interfaces. Since it has been shown that the perovskite and spinel layers in these heterostructures are magnetically uncoupled,^[NC07] it is likely that this background magnetoresistance arises from any spin misalignment present at the Fe₃O₄ electrode-barrier interface.

In junctions that exhibit such low background MR, it is surprising that the magnetically easy direction of the interfacial spinel sublayer detected at the NMO/Fe₃O₄ interface is not coincident with that of the Fe₃O₄ electrode above 60K, since such modulation of the interfacial magnetic anisotropy should contribute to misalignment of the spins at the electrode-barrier interface. However, the presence of this specific, predominately MnFe₂O₄-like spinel sublayer may in fact aid in the alignment of the Fe₃O₄ spins to the bulk of the Fe₃O₄ layer, resulting in lower background MR compared to other junctions, in the following way. When the field is applied in-plane along the [001]-direction, the magnetization of the Fe₃O₄ likely causes the magnetically soft interfacial sublayer spins to experience a large molecular field, resulting in strong exchange coupling across the interface. Such exchange coupling between magnetically soft and magnetically hard spinel ferrite thin films has been shown to be quite strong.^[Suzuki96] Furthermore, the strength of the interaction is inversely proportional to the thickness of the soft ferrite layer,^[Suzuki96] indicating that a magnetically soft ferrite sublayer on the order of 1-2 nm

thick should easily couple to a magnetically hard ferrite layer greater than 40 nm in thickness. Therefore, when the bulk of the Fe_3O_4 switches, so too does the interfacial sublayer. This would result in less background MR, as well as a greater JMR seen at each bulk electrode switching event. It is likely that any other spinel sublayer formed in the other LSMO- Fe_3O_4 heterostructures studied was magnetically harder than both the predominantly MnFe_2O_4 -like sublayer in this study and the Fe_3O_4 , and thus does not magnetically switch as easily with the Fe_3O_4 electrode. Unfortunately, verification of the exchange coupling of the sublayer region to the full 40 nm Fe_3O_4 top layer is difficult to verify in these heterostructures, as element-specific, surface-sensitive soft x-ray techniques cannot access a 40 nm-deep sublayer region, and the magnetization of the sublayer would be overwhelmed by the bulk Fe_3O_4 layer in bulk techniques.

In summary, we have investigated the structure and magnetic properties of hybrid MTJ-spin filter devices and how they affect the magnetotransport properties. The crystalline structure of the heterostructure facilitates the lack of magnetic coupling at the non-isostructural LSMO/NMO interface, and the strong magnetic coupling observed at the isostructural NMO/ Fe_3O_4 interface. In addition, the presence of a magnetically soft layer with a modified magnetic anisotropy at the isostructural NMO/ Fe_3O_4 interface strongly suggests the existence of a predominately MnFe_2O_4 -like interdiffused sublayer, whose exchange coupling to the Fe_3O_4 electrode likely accounts for the low background magnetoresistance seen in these junctions, and the successful spin filtering when the barrier layer is ferrimagnetic.. Nonlinear junction transport observed both above and below the T_C of NMO indicates that the insulating NMO is an effective potential barrier both in its paramagnetic and ferrimagnetic states. This work demonstrates that introducing a magnetic barrier layer can produce novel effects in MTJ-type structures, thereby creating a new paradigm for the design of spin-based devices.

This work was supported in full by the Office of Basic Energy Sciences, Division of Materials Sciences and Engineering, of the U.S. Department of Energy under Contract No. DE-AC02-05CH11231. The Advanced Light Source is supported by the Director, Office of Science, Office of Basic Energy Sciences, of the U.S. Department of Energy under Contract No. DE-AC02-05CH11231. Processing performed in the University of California-Berkeley Microlab.

Figure 1 - Structural characterization of the junction heterostructure taken along the [001] zone axis. (a) High resolution TEM image of the perovskite-spinel interface, (b) Fast Fourier Transform of the TEM image, (c) STEM image taken of the Fe_3O_4 . Schematics show atomic arrangement of tetrahedral (green) Fe, octahedral (blue) Fe and O atoms (red).

Figure 2 - XMCD of the LSMO/NMO interface. (a) Mn $L_{2,3}$ XMCD spectra taken at 55K of the LSMO/NMO bilayer with the mean XMCD probe depth demonstrated on the sample schematic. XMCD hysteresis loops taken at (b) 640.0 eV and (c) 642.5 eV.

Figure 3 – Room temperature in-plane Fe XMCD hysteresis loops taken along the [001] direction of the interdiffused $(\text{Fe,Mn,Ni})_3\text{O}_4$ sublayer at the NMO/ Fe_3O_4 interface (open circles) and of only the top Fe_3O_4 electrode in the trilayer heterostructure (closed circles). Sample schematics demonstrate the two samples used.

Figure 4– Fe hysteresis loops taken at 30 K and 80 K along the [001] and [11-0] in-plane crystallographic directions for the trilayer sample shown.

Figure 5 – Junction transport as a function of applied magnetic field at 75K. (a) JMR and moment at low magnetic fields, (b) JMR at high magnetic fields..

Figure 1

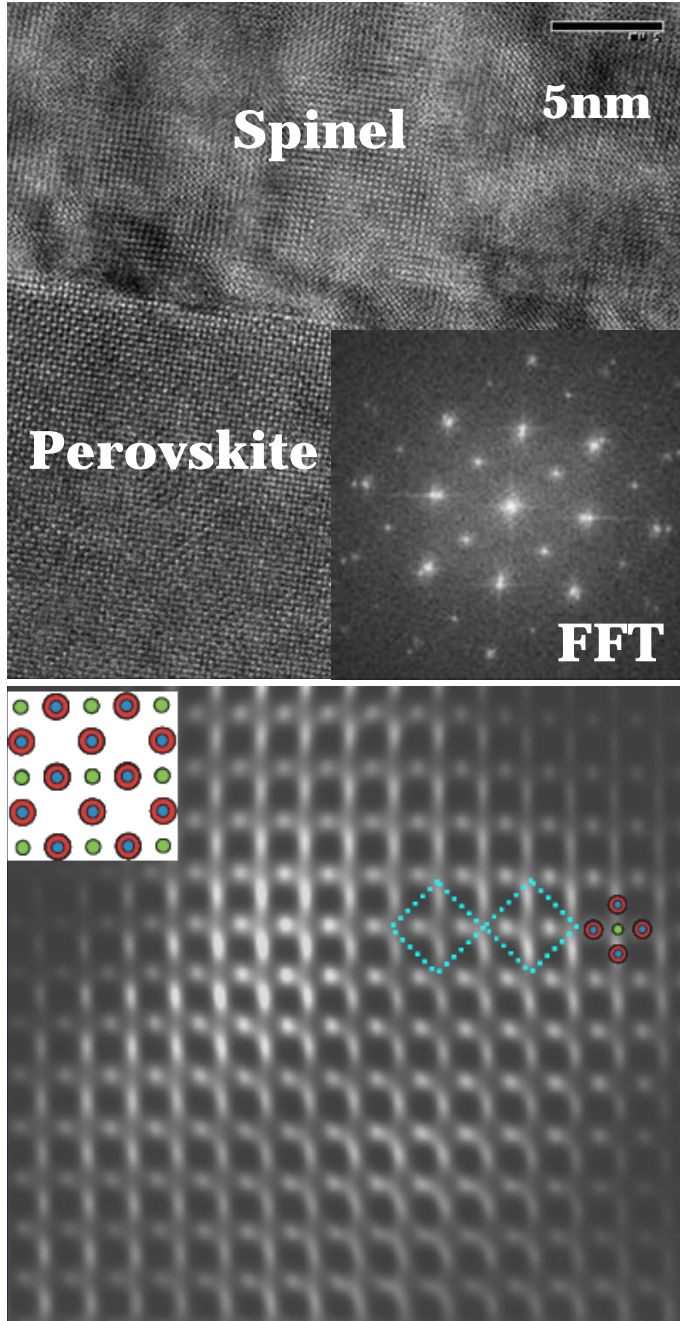


Figure 2

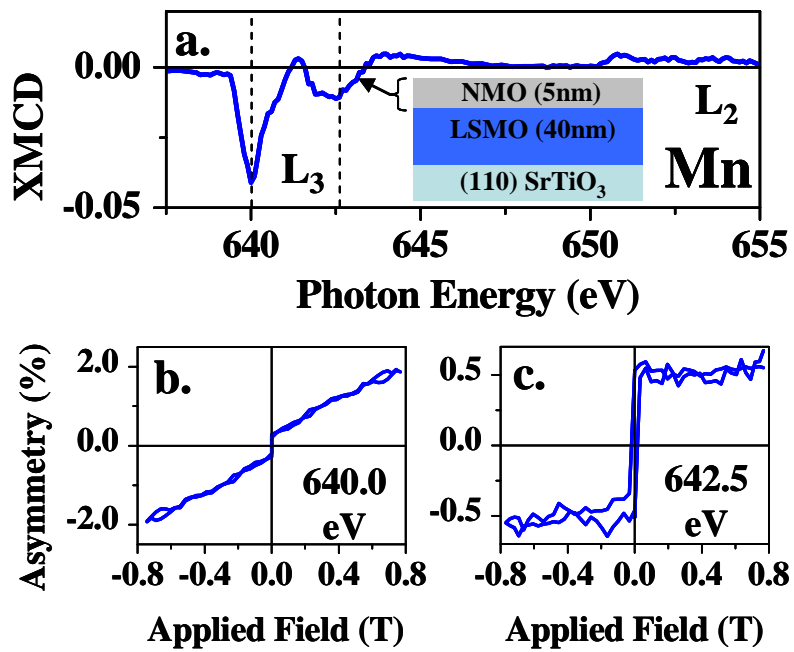


Figure 3

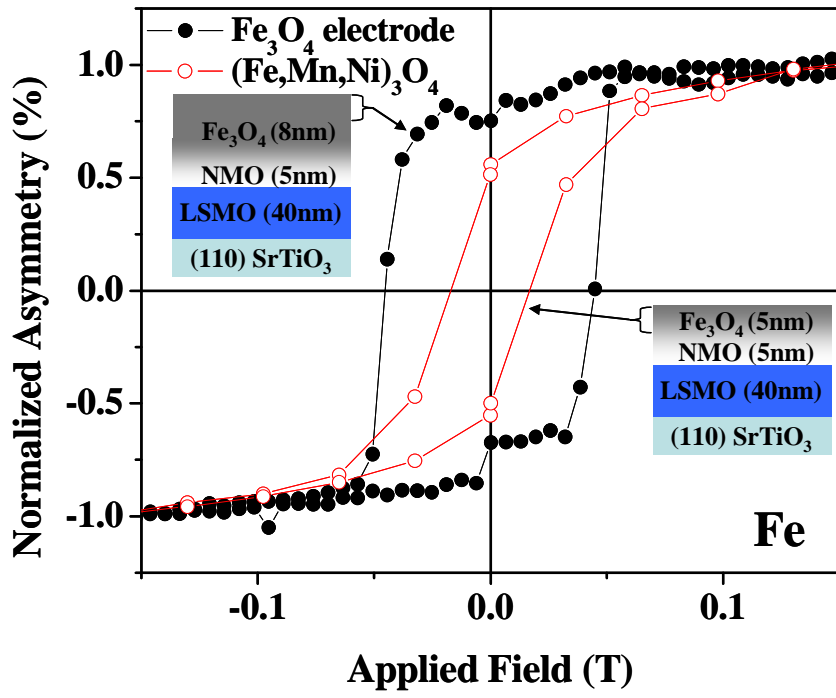


Figure 4

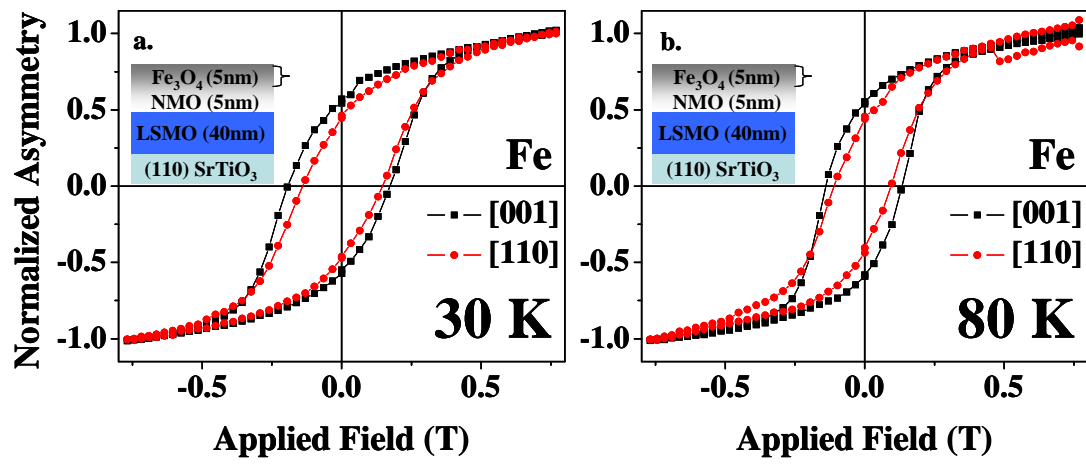
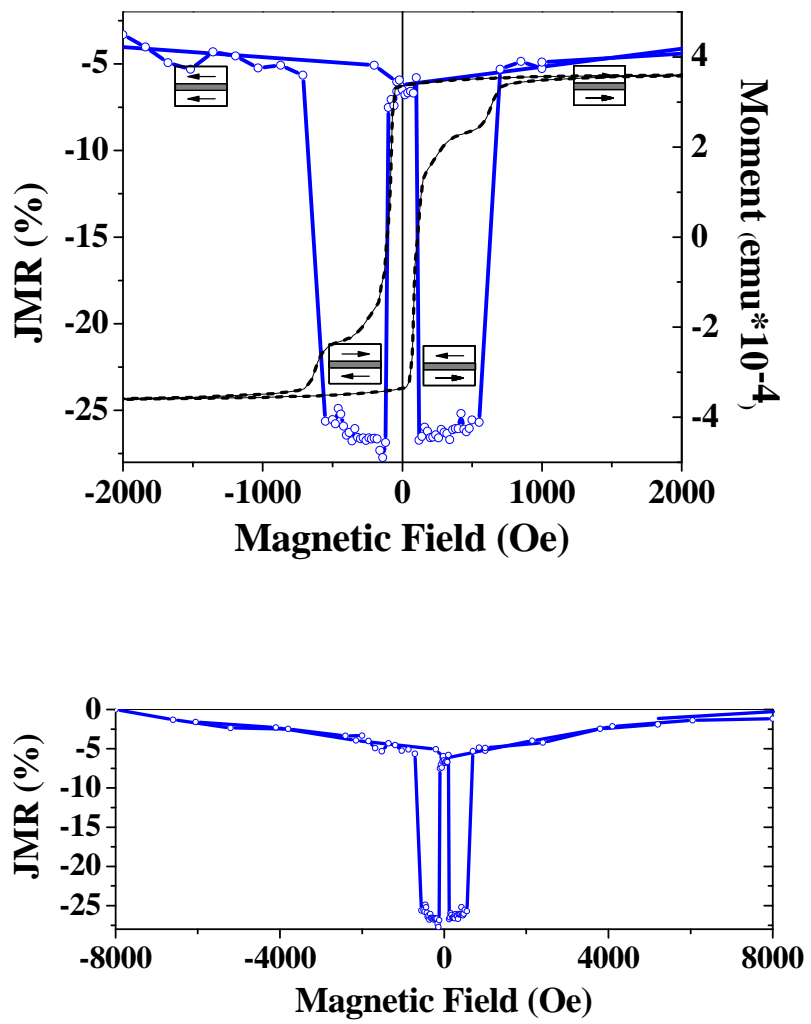


Figure 5



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