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A Pliocene-Pleistocene stack of 57 globally distributed benthic $\delta^{18}$O records

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We present a 5.3-Myr stack (the “LR04” stack) of benthic $\delta^{18}$O records from 57 globally distributed sites aligned by an automated graphic correlation algorithm. This is the first benthic $\delta^{18}$O stack composed of more than three records to extend beyond 850 ka, and we use its improved signal quality to identify 24 new marine isotope stages in the early Pliocene. We also present a new LR04 age model for the Pliocene-Pleistocene derived from tuning the $\delta^{18}$O stack to a simple ice model based on 21 June insolation at 65$^\circ$N. Stacked sedimentation rates provide additional age model constraints to prevent overtuning. Despite a conservative tuning strategy, the LR04 benthic stack exhibits significant coherency with insolation in the obliquity band throughout the entire 5.3 Myr and in the precession band for more than half of the record. The LR04 stack contains significantly more variance in benthic $\delta^{18}$O than previously published stacks of the late Pleistocene as the result of higher-resolution records, a better alignment technique, and a greater percentage of records from the Atlantic. Finally, the relative phases of the stack’s 41- and 23-kyr components suggest that the precession component of $\delta^{18}$O from 2.7–1.6 Ma is primarily a deep-water temperature signal and that the phase of $\delta^{18}$O precession response changed suddenly at 1.6 Ma.

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1. Introduction

Alley [2003] recently called for a paleoceanographic “type section” to which all paleoceanographic measurements could be compared, in the same way that researchers have used data gathered by the Second Greenland Ice Sheet Project (GISP2) and Greenland Ice Core Project (GRIP) in studies of the last glacial cycle. A type section which provides a common timescale and reference of comparison for all paleoceanographic records would improve communication within the community and elucidate subtle differences among the ever-growing number of paleoceanographic records. Here we present a new 5.3-Myr benthic $\delta^{18}$O stack (the “LR04” stack), which we propose would make an excellent paleoceanographic type section for the Pliocene-Pleistocene.

Alley [2003] describes the ideal type section as high in resolution, multiply replicated by different laboratories, containing multiple paleoclimate proxies, and spanning as much time as possible. The LR04 stack contains over 38,000 individual $\delta^{18}$O measurements from 57 sites, sampled at many different laboratories. Because this stack incorporates information from so many sites, it has a higher signal-to-noise ratio than any previous $\delta^{18}$O record and more accurately reflects changes in global climate.

The stack’s resolution of orbital-scale (23-kyr) features in the Pleistocene is comparable to that of millennial-scale (1.5-kyr) features in the GISP2 $\delta^{18}$O record [Grootes et al., 1993], with 10–20 samples per cycle. The stack spans the entire Pliocene-Pleistocene with error bars averaging only 0.1%. We also use the LR04 stack to develop a conservatively tuned $\delta^{18}$O timescale, which minimizes deviations in globally averaged sedimentation rates. Although the LR04 stack contains only one paleoceanographic parameter, any paleoclimate proxy taken from a marine core with reliable $\delta^{18}$O data can easily be aligned to the LR04 stack through the use of automated graphic correlation software [e.g., Lisiecki and Lisiecki, 2002]. The LR04 stack and supplemental results are archived at the National Geophysical Data Center (http://www.ngdc.noaa.gov/paleo/paleocean.html).

In the following section we provide background information on $\delta^{18}$O and previously published stacks. Section 3 describes the $\delta^{18}$O data used in the LR04 stack. Section 4 contains a detailed description of the stack’s construction and demonstrates the effectiveness of our graphic correlation and stacking techniques in reducing the noise level of $\delta^{18}$O-like signals. Section 5 describes the creation of the orbitally tuned LR04 age model, which is additionally constrained by two measures of global sedimentation rate. In section 6 we present specific $\delta^{18}$O estimates with error bars and define 24 new marine isotope stages (MIS) in the early Pliocene. We also compare the LR04 stack to four previously published stacks.
Table 1. Notable δ18O Stacks

<table>
<thead>
<tr>
<th>Component</th>
<th>Approximate Length</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stack</td>
<td>δ18O Recordsa</td>
</tr>
<tr>
<td>SPECMAPb</td>
<td>5 p. 750 kyr</td>
</tr>
<tr>
<td>Pisias et al. [1984]</td>
<td>5 b. 300 kyr</td>
</tr>
<tr>
<td>Preq et al. [1986]</td>
<td>11 p., 2 b. 750 kyr</td>
</tr>
<tr>
<td>Williams et al. [1988]</td>
<td>3 p., 1 b. 1.9 Myr</td>
</tr>
<tr>
<td>Raymo et al. [1990]</td>
<td>3 b. 2.5 Myr</td>
</tr>
<tr>
<td>Bassinot et al. [1999]</td>
<td>2 p. 900 kyr</td>
</tr>
<tr>
<td>S95 Compositead</td>
<td>3 b. (in series) 6 Myr</td>
</tr>
<tr>
<td>Karner et al. [2002]</td>
<td>6–13 b. 860 kyr</td>
</tr>
<tr>
<td>HW04d</td>
<td>5 p., 5 b. (EOF) 780 kyr</td>
</tr>
<tr>
<td>LR04 (this study)</td>
<td>57 b. 5.3 Myr</td>
</tr>
</tbody>
</table>

aPlanktonic (p.) or benthic (b.).

[1984]. The included records vary widely in resolution and time span. The only benthic δ18O records purposefully excluded from the LR04 stack are those with sample spacings greater than 12 kyr, a resolution too low for accurate alignment. Our stacking technique, described below, is robust to the inclusion of records of varying quality because sites with higher resolution are more heavily weighted in the averaging process. The aligned δ18O records used in the stack are shown in Figure 2. The stack contains 47 records back to 0.4 Ma, ~25 records from 1–3 Ma, at least 12 records back to 4.9 Ma, and 5 records from 5–5.33 Ma. No one record represents more than 30% of the data in a 10-kyr interval except before 5 Ma, when Site 846 [Shackleton et al., 1995a] provides approximately 40% of the data. In total, the LR04 stack incorporates 38,229 individual δ18O measurements.

4. Stack Construction

4.1. Graphic Correlation

[1984]. The stack presented in this paper contains benthic δ18O records from 57 globally distributed sites. These sites are well distributed in latitude, longitude, and depth in the Atlantic and Pacific and include two sites in the Indian Ocean (Figure 1). Most of the δ18O measurements in these records are from Uvigerina peregrina or Cibicidoides wuellerstorfi, with appropriate species offset corrections [Shackleton and Hall, 1984]. The included records vary widely in resolution and time span. The only benthic δ18O records purposefully excluded from the LR04 stack are those with sample spacings greater than 12 kyr, a resolution too low for accurate alignment. Our stacking technique, described below, is robust to the inclusion of records of varying quality because sites with higher resolution are more heavily weighted in the averaging process. The aligned δ18O records used in the stack are shown in Figure 2. The stack contains 47 records back to 0.4 Ma, ~25 records from 1–3 Ma, at least 12 records back to 4.9 Ma, and 5 records from 5–5.33 Ma. No one record represents more than 30% of the data in a 10-kyr interval except before 5 Ma, when Site 846 [Shackleton et al., 1995a] provides approximately 40% of the data. In total, the LR04 stack incorporates 38,229 individual δ18O measurements.
peaks. Graphic correlation inherently requires some judgment to determine which features correspond to one another and to distinguish noise from isotopic features. Automated correlation algorithms provide the most objective correlation techniques because alignment criteria are explicit and applied consistently. However, each alignment must also be evaluated by eye because stratigraphic disturbances resulting from hiatuses, coring gaps, and duplicated sections can produce errors in the automated correlation.

We align 57 benthic δ¹⁸O records using an automated graphic correlation program [Lisiecki and Lisiecki, 2002], which considers all possible alignments to find the best global fit and penalizes alignments based on extreme sedimentation rates and sudden sedimentation rate changes. Alignments are performed using normalized δ¹⁸O records to maximize the algorithm’s accuracy. Each alignment is evaluated by eye and adjusted, if necessary, by changing the sedimentation rate penalties or adding tie points until a good alignment is achieved which agrees reasonably well with previously published age estimates (e.g., those derived from paleomagnetic reversals or biostratigraphic data). In general, we keep sedimentation rate penalties small because little is known about how linear sedimentation rates (LSR) vary with time. This allows the LSR at individual sites to vary a great deal and preserves as much coherent δ¹⁸O variation as possible. With our alignments and age model, the average standard deviation (σ) in a site’s LSR is 1.8 cm/kyr. As a percentage of each site’s mean LSR, σ averages 41% and ranges from 24% at Site GeoB1041 to 164% at ODP Site 927 from 5.0–2.6 Ma.

Graphic correlation allows the stack’s construction to be largely independent of its assigned timescale and, consequently, any specific forcing model for δ¹⁸O. However, stacking with graphic correlation does involve two assumptions: that each site records the same global δ¹⁸O signal with little phase difference and that the alignment procedure is not overly sensitive to noise. In support of the first assumption, each site does appear to record the same δ¹⁸O signal; the average correlation between the LR04 stack and individual records (after alignment) is 0.88. Also, phase differences in δ¹⁸O between sites should be minimal because the average mixing time of the deep ocean is only ~1 kyr. Glacial ventilation rates are uncertain, but benthic-planktonic age differences at the last glacial maximum yield deep-water age estimates of 1.1 kyr in the deep Atlantic [Keigwin and Schlegel, 2002] and 2 kyr in the deep Pacific [Broecker et al., 2004]. Graphic correlation actually corrects for any potential mixing lags between sites to produce an estimate of the δ¹⁸O signal as if it had been recorded with the same phase everywhere.

The assumption that alignments are insensitive to noise is a concern because sedimentation rates at individual sites are only loosely constrained in order to maximize the amplitude of isotopic features. Therefore we perform a series of simple experiments to test the ability of our alignment technique to reduce noise without artificially increasing signal amplitude. In the experiments, we construct test stacks from twenty noisy copies of a single isotope record. The noisy copies are created by the addition of white noise with standard deviations of 2 kyr and 0.2% to the ages and δ¹⁸O values of the initial signal. We also add white noise (σ = 0.15%) to the δ¹⁸O values of each alignment target before applying our graphic correlation and stacking algorithms. Figure 3 shows test...
Figure 2. Graphically aligned benthic δ¹⁸O data, plotted with their original variance but offset vertically. Data are from Sites 502 [deMenocal et al., 1992], 552 [Shackleton and Hall, 1984], 607 [Ruddiman et al., 1989; Raymo et al., 1989; Raymo et al., 1992; this study], 610 [Raymo et al., 1992], 658 [Tiedemann, 1991], 659 [Tiedemann et al., 1994], 662 (this study), 664 [Raymo et al., 1997], 665 [Curry and Miller, 1989], 677 [Shackleton et al., 1990], 704 [Hodell and Venz, 1992], 722 [Clemens et al., 1996], 758 [Chen et al., 1995], 806 [Berger et al., 1993], 846 [Mix et al., 1995a; Shackleton et al., 1995a], 849 [Mix et al., 1995b], 925 [Bickert et al., 1997; Billups et al., 1998; Franz, 1999], 927 [Bickert et al., 1997; Franz, 1999], 928 [Franz, 1999], 929 [Bickert et al., 1997; Billups et al., 1998; Franz, 1999], 980 [Oppo et al., 1998; McManus et al., 1999; Flower et al., 2000], 981 [McIntyre et al., 1999; Raymo et al., 2004], 982 [Venz et al., 1999; Venz and Hodell, 2002; this study], 983 [McIntyre et al., 1999; Raymo et al., 2004], 984 [Raymo et al., 2004], 999 [Haug and Tiedemann, 1998], 1012 and 1020 [Herbert et al., 2001; Z. Liu, personal communication, 2002], 1085 (D. Andreasen, personal communication, 2002), 1087 [Pierre et al., 2001], 1088 [Hodell et al., 2003], 1089 [Hodell et al., 2001], 1090 [Venz and Hodell, 2002], 1092 [Andersson et al., 2002], 1123 [Hall et al., 2001; Harris, 2002], 1143 [Tian et al., 2002], 1146 (S. Clemens, personal communication, 2002), 1148 [Jian et al., 2003], GeoB 1032, 1041, 1101 [Bickert and Wefer, 1996], GeoB 1113 [Sarnthein et al., 1994], GeoB 1117, 1211, 1214 [Bickert and Wefer, 1996], GeoB 1312 [Hale and Pflaumann, 1999], GeoB 1505 [Zabel et al., 1999], MD95-2042 [Shackleton et al., 2000], PC72 [Murray et al., 2000], RC13-110 [Mix et al., 1991; Imbrie et al., 1992], RC13-229 [Oppo et al., 1990], V19-28 [Ninkovitch and Shackleton, 1975], V19-30 [Shackleton and Pisias, 1985], V21-146 [Hovan et al., 1991].
stacks generated from initial signals of Pleistocene \((s = 0.43\%)\) and Pliocene \((s = 0.21\%)\) \(\delta^{18}O\) data. In 400 replications, the stacks’ error relative to the initial isotope signal (for either time period) has a standard deviation of \(0.09 \pm 0.01\%\), less than the noise in the alignment target and half that of the noisy records used to construct the stack. Experiments performed with red noise produce similar results. Stacking records of varying resolution (while holding the total number of data points constant) tends to reduce stack error by improving the alignment accuracy of high resolution records. In conclusion, the extraordinary similarity between the test stacks and the initial \(\delta^{18}O\) signal demonstrates the ability of our alignment and stacking technique to increase the signal-to-noise ratio of Pleistocene and Pliocene \(\delta^{18}O\) records.

4.2. Stacking

[13] The alignment process for the stack’s construction is iterative. Our initial alignment targets are high-resolution segments of seven \(\delta^{18}O\) records: GeoB1041 from 0–0.15 Ma, ODP Site 1012 from 0–0.6 Ma, ODP Site 927 from 0–1.4 Ma, ODP Site 677 from 0–2.0 Ma, ODP Site 849 from 1.7–3.6 Ma, ODP Site 846 from 2.7–5.3 Ma, and ODP Site 999 from 3.3–5.3 Ma. Each \(\delta^{18}O\) record is first aligned to these targets in the depth domain to create seven short stacks. In the intervals where these stacks overlap, we observe that the features of the stacks are largely independent of which site serves as the alignment target.

[14] The seven stacks are assigned timescales taken from the S95 composite and spliced together to form a transitional stack spanning the entire 5.3-Myr interval. In constructing the transitional stack, we select portions of the short stacks which are most representative of the component records and which best resolve substage features. These comparisons help prevent hiatuses, sediment disturbances, and splicing errors within an alignment target from affecting the final stack. Where possible, we also avoid using the first and last 5\% of each stack due to added uncertainty in the graphic correlation [Lisiecki and Lisiecki, 2002]. After creating the transitional stack, we make a few adjustments to its age model to eliminate large deviations in the sites’ sedimentation rates and perform a final set of alignments using the transitional stack as the alignment target.

[15] The LR04 stack (Figure 4) is the average of all \(\delta^{18}O\) records aligned to the transitional stack. This final step improves alignment accuracy because the transitional stack resembles the average \(\delta^{18}O\) curve more closely than any individual site does. Also, because the transitional stack spans the entire 5.3 Myr, most of our records could be aligned to it in one piece, reducing the potential for errors where the shorter stacks join together. The \(\delta^{18}O\) records from eleven sites are aligned to the stack in multiple pieces because they are greater than 3 Myr in length or contain large gaps. In Figure 4 we show the final LR04 stack assigned to the LR04 age model, described in section 5.

[16] Our stacking technique is similar to one used by Pisias et al. [1984]. The stack’s time domain is divided into small, equally spaced intervals (Table 2), and an average is taken of all \(\delta^{18}O\) measurements lying within each time interval. Therefore each point in the stack is the average of all of the data which fall in a particular time interval. Unlike the averaging of evenly interpolated records, this technique weights high-resolution records more heavily and prevents interpolation across gaps or hiatuses from affecting the stack. The final LR04 stack is composed of four sections of different resolution due to the decreasing number of records available in the more distant past. Table 2 provides the interval size (equivalent to stack resolution) and data statistics for each section. For any given time interval, the
concentration of data used in the LR04 stack is at least twice as high as in any previous stack or individual δ18O record spanning that interval. The stack’s resolution is comparable to previous stacks but is less than half that of the highest-resolution records.

[17] The LR04 stack is simply the average of the aligned benthic δ18O records. We do not adjust the mean or variance of the records, except to make species offset corrections. We choose not to adjust the isotope curves based on their modern bottom water temperatures because the temperature differences between sites may have changed dramatically over the last 5.3 Myr. We also do not weight the records based on their spatial distribution. The majority of records are from the Atlantic Ocean, and the number of sites in the stack varies with time, changing the relative weighting of different regions. However, we observe that regional differences in benthic δ18O are typically less than 0.3% (less than 0.15% after 0.6 Ma), and we are currently developing a detailed description of regional δ18O variability.

5. Age Model

[18] Because the LR04 stack is constructed by graphic correlation, its stratigraphic features are essentially independent of any timescale. Below we describe the construction of an age model which takes advantage of the high signal-to-noise ratio of the stack and analysis of the sedimentation rates at 57 sites. However, almost any age model could be applied to the LR04 stack. This flexibility allows the stack to be adapted to alternate models of δ18O response or to improvements in age estimates.

[19] We construct the LR04 age model by aligning our benthic δ18O stack to a simple model of ice volume while considering the average (stacked) sedimentation rate of
the stack’s 57 sediment cores. This age model is more reliable than one from a single δ^{18}O record because individual δ^{18}O records have more noise and fewer constraints on linear sedimentation rates (LSR) than a stack. We seek to minimize changes in the stack’s average LSR under the assumption that global sedimentation rates have been relatively stable. Constraining average LSR does not prevent individual sites from exhibiting highly variable sedimentation rates. Age-versus-depth plots and average sedimentation rates are often used to evaluate age models [e.g., Imbrie et al., 1984; Shackleton et al., 1990; Raymo, 1997] because timescale errors create LSR deviations at all sites while most sources of LSR variability are local or regional. Unlike Huybers and Wunsch [2004], we do not assume that average sedimentation rates are absolutely constant because the long-term climatic changes of the Pliocene-Pleistocene have likely had some effect on sedimentation rates. Therefore our tuning goals are to prevent rapid fluctuations in stacked LSR and to minimize its variance. By allowing sedimentation rates to vary slowly with time, we also eliminate the need to correct for sediment compaction except at the very top of the record.

5.1. From 0 to 135 ka

While generally robust, our LSR tuning strategy is not effective for the most recent portion of the stack, where apparent sedimentation rates can be distorted by uncompacted sediments in the top few meters of a core [e.g., Skinner and McCave, 2003; Huybers and Wunsch, 2004]. Fortunately, reliable age estimates are available for this portion of the benthic δ^{18}O record. The top 22 kyr of the stack are dated by correlation to the 14C-dated benthic δ^{18}O record, NA87-22 [Waelbroeck et al., 2001]. From 22–120 ka the stack is aligned to the high-resolution benthic δ^{18}O record of Site MD95-2042 [Shackleton et al., 2000], which is dated by correlating millennial-scale features in its planktonic δ^{18}O to ice δ^{18}O from the GRIP ice core [Johnsen et al., 1992]. Finally, the age of Termination II is taken from the U-Th dating of coral terraces [Bard et al., 1990; Stein et al., 1993].

5.2. Tuning Target

Our tuning target is a simple nonlinear model of ice volume, y, which follows the equation

$$\frac{dy}{dt} = \frac{1 \pm b}{T_m} (x - y) \tag{1}$$

where the nonlinearity coefficient b is subtracted during ice growth and added during ice decay [Imbrie and Imbrie, 1980]. The model’s forcing function, x, is the 21 June insolation curve for 65°N from the La93(1,1) orbital solution, which uses modern values of dynamical ellipticity and tidal dissipation [Laskar et al., 1993]. We allow the nonlinearity b and mean time constant T_m of the ice model to increase with time due to the long-term increase in global ice volume. From 5.3–3.0 Ma, b is 0.3 and T_m is 5 kyr (M. Mudelsee, personal communication, 2004). Both increase linearly to 0.6 and 15 kyr, respectively, by 1.5 Ma and remain at those values to the present. The Pleistocene value of b is taken from Imbrie and Imbrie [1980] while the time constant of 15 kyr is selected to maximize agreement with the independent age estimates used for the last 135 kyr of the stack.

[22] Ice sheet response time and the lag between insolation forcing and δ^{18}O are poorly constrained before 0.8 Ma. We assume that small ice sheets respond more quickly than the massive ones of the late Pleistocene and choose early Pliocene values of b and T_m to reflect the absence of large northern hemisphere ice sheets. However, a study of the lag between δ^{18}O and other climate proxies at ODP Site 662 suggests that T_m may have been ~15 kyr since 3 Ma (P. deMenocal, manuscript in preparation, 2005). Using a response time of 5 kyr, instead of 15 kyr, makes the early Pliocene portion of the LR04 age model ~3 kyr older. At the other extreme, if T_m does not reach 15 kyr until the late Pleistocene, our age estimates would be reduced by less than 1 kyr from 3.0–0.8 Ma.

[23] The largest uncertainty in the Pliocene portion of the LR04 age model probably comes from the orbital calculations themselves. Different values of tidal dissipation in the orbital solution can shift the age model by 5 kyr at 5 Ma [Laskar et al., 1993]. Additionally, changes in global ice volume could alter the Earth’s dynamical ellipticity to produce age model errors of up to 20 kyr by 5 Ma [Laskar et al., 1993]. However, Lourens et al. [1996] do not find evidence for tidal dissipation or dynamical ellipticity changes in the Pliocene-Pleistocene climate record.

5.3. Sedimentation Rate Constraints

To prevent tuning errors we monitor the implied average sedimentation rate of the stack throughout the tuning process. We construct two different estimates of global sedimentation rates: an LSR stack, which averages the sites’ sedimentation rates, and a “normalized” LSR stack, which compensates for different mean sedimentation rates (MSR) across sites. The LSR of each site is calculated by placing its δ^{18}O record on the stack’s timescale and calculating its sedimentation rate. We calculate sedimentation rates as a function of meters composite depth (mdc) or revised mcd where possible (~75% of ODP records) and as meters below seafloor (mbsf) otherwise. The first LSR stack is an average of all site’s LSR estimates, interpolated to a
resolution of 2 kyr. The second, normalized LSR stack is constructed by dividing each site’s LSR by its MSR prior to stacking. For the eleven sites with $\delta^{18}O$ records aligned to the stack in multiple segments, the LSR of each segment is normalized separately. Normalization prevents sites with high MSRs from being unduly weighted and reduces the effect of records with different MSRs beginning and ending within the stack. For the idealized case in which each LSR is generated by an independent, stationary random process, the normalized LSR stack for the “true” age model would converge to a constant value of unity.

5.4. Tuning

[25] The LR04 stack is tuned to our simple ice model in a two-step process by the addition of age control points with an average spacing of 20 kyr. The goal of our first tuning is to find the correlation between $\delta^{18}O$ and ice model minima which produces the least variation in stacked LSR. Because this initial age model is derived primarily from globally averaged sedimentation rates with minimal orbital tuning, we avoid assumptions about the age or length of each glacial cycle. We also allow the instantaneous phase of $\delta^{18}O$ to lag insolation by 0–120°. This age model generates a normalized LSR stack with a standard deviation of only 0.06. In our second tuning we loosen the LSR constraint in order to keep the $\delta^{18}O$ signal approximately in phase with the obliquity component of the ice model. Figure 5 shows the early Pleistocene portion of the stack and illustrates the balance achieved between strictly tuning the stack and minimizing the variance of normalized LSR.

[26] We emphasize obliquity in our tuning because its effect on insolation is symmetric across hemispheres and because obliquity induces the strongest $\delta^{18}O$ response for most of the last 5.3 Myr. Our ice-model tuning target, which inherently accentuates the effects of obliquity relative to precession due to its long time constant, produces a fairly good match to the $\delta^{18}O$ stack. However, averaging normalized versions of the ice model and lagged orbital obliquity produces a curve which often has an even better correlation to $\delta^{18}O$ (e.g., in Figure 5). At the few points where correlation between the stack and the ice model is ambiguous within the constraints of average LSR, we choose the correlation which is most consistent with obliquity forcing. Section 7.1 provides uncertainty estimates for the LR04 age model.

[27] Figure 6 shows the stacks of true and normalized LSR produced by the final LR04 age model. Some features of the two stacks differ slightly because they weight the LSR of each site differently. For example, the LSR stack is more sensitive to variability at sites with high mean sedimentation rates while the normalized LSR stack is more sensitive to sites with low sedimentation rates. The normalized stack, in which each LSR record is divided by its mean sedimentation rate, has a standard deviation of 0.09 in the final LR04 age model. The normalized LSR stack generally varies by less than 10% from 4.3–0.1 Ma, demonstrating that little tuning is necessary to achieve a high coherence with obliquity. Prior to 4.3 Ma normalized LSR must vary by up to ~20% in order to achieve coherence with obliquity. These larger deviations may occur because fewer records contribute to the stack before 4 Ma, because the average LSR of these sites is smaller, or because sedimentation rates experienced greater variability in the early Pliocene. The age models of Shackleton et al. [1995b] (hereinafter referred

Figure 5. The tuning process. (a) The $\delta^{18}O$ stack shown with 21 June insolation at 65°N, the ice-model tuning target, and an equally weighted average of ice and obliquity. (b) The normalized LSR stack for the same time period with circles denoting age control points.
The coherence and phase of the stack relative to the obliquity and precession components of 21 June insolation are calculated using Blackman-Tukey cross-spectral analysis [Jenkins and Watts, 1968] with a moving window of 500 kyr and a 300-kyr lag (Figure 7). The stack is generally incoherent with respect to the eccentricity component of insolation, but coherence with the obliquity component is at the 95% confidence level for most of its length and is always above the 80% confidence level. At least one precession frequency is coherent for all of the last 1.7 Myr and most of the interval from 4.1–2.8 Ma.

Because we emphasize obliquity in our tuning process, its phase relative to insolation is primarily determined by the lag generated by our ice model. The plot of obliquity phase in Figure 7 clearly shows the increase in model response time from 3.0–1.5 Ma. The lag in obliquity is relatively constant at 30°/C176 (3.4 kyr) before 3 Ma, then increases steadily, and finally levels off at 60°/C176 (6.8 kyr) in the Pleistocene. At 4.4 Ma the obliquity phase shows a small deviation, which may be related to the particularly low 41-kyr variance of δ18O at that time. The lag relative to precession is more variable. The average precession lag is 52° (3.3 kyr) from 4.1–2.7 Ma, decreases to 21° (1.3 kyr) from 2.7–1.6 Ma, and then jumps to 75° (4.8 kyr) for the rest of the Pleistocene. The average error in coherent phase estimates is 8° for 41 kyr and 15° for 23 kyr.

6. Results
6.1. The δ18O Values

The LR04 benthic stack reconstructs the average δ18O signal of each marine isotope stage and substage within the Pliocene and Pleistocene. The features of these stages are largely independent of the assigned age model because the stack is constructed by graphic correlation. Overall, the mean standard error of the stack is 0.06‰, and only 2% of the data points have errors greater than 0.1‰. This paper presents all isotopic error bars as plus or minus two standard errors. The maximum δ18O value of the benthic stack is 5.08 ± 0.11‰ at 433 and 630 ka (MIS 12 and 16), and the minimum is 2.65 ± 0.15‰ at 5.135 Ma (MIS T7). The magnitudes and ages of the last seven glacial terminations are provided in Table 3. We define termination magnitude as the difference between the maximum δ18O value of the preceding glacial and the minimum of the following interglacial. Each termination is dated by the temporal midpoint between the start and end of rapid change in δ18O. Terminations III and VI are shown to be significantly smaller than the others, in agreement with Raymo [1997].

Recent research has focused on MIS 11 as a possible analog for the present interglacial [e.g., Loutre and Berger, 2003; EPICA Community Members, 2004] because both occur during times of low eccentricity. The LR04 age model establishes that MIS 11 spans two precession cycles, with δ18O values below 3.6‰ for 20 kyr, from 398–418 ka. In comparison, stages 9 and 5 remained below 3.6‰ for 13 and 12 kyr, respectively, and the Holocene interglacial has lasted 11 kyr so far. In the LR04 age model, the average LSR of 29 sites is the same from 398–418 ka as from 250–650 ka; consequently, stage 11 is unlikely to be artificially stretched. However, the 21 June insolation minimum at 65°N during MIS 11 is only 489 W/m², much less pronounced than the present minimum of 474 W/m². In addition, current insolation values are not predicted to return to the high values of late MIS 11 for another 65 kyr. We propose that this effectively precludes a “double precession
cycle” interglacial [e.g., Raymo, 1997] in the Holocene without human influence.

### 6.2. MIS Identification

In Figure 4 we use the MIS taxonomy of SPECMAP, Ruddiman et al. [1989], and Raymo et al. [1989] from the present to MIS 104 in the Pliocene. Below MIS 104 we adopt the stage identification scheme of Shackleton et al. [1995a] (hereinafter referred to as SHP95). In this scheme, isotope events are identified based on the magnetic subchron within which they are found. For example, Co2 is the uppermost glacial excursion within the Cochiti subchron. Shackleton et al. [1995a] developed this methodology to prevent uncertainty in stage identifications from accumulating down core. While they suggest that further subdivisions of the stages be designated by lettered substages analogous to 5a–5e in the late Pleistocene, we feel that renumbering is less cumbersome and is justified by the large number of records examined in this study. Therefore we propose modifications to the early Pliocene MIS taxonomy as described below. Recognizing the potential for confusion when isotope stages are renamed, we do not remove any previously defined stages and only add a new one if it is clearly identifiable in most δ¹⁸O records and has an amplitude comparable to other nearby stages. Additionally, the flexibility of the SHP95 numbering scheme minimizes the number of renamed stages because new stages in one magnetic subchron will not alter MIS names in other subchrons.

Above the Mammoth subchron, the stages in the LR04 stack are easily correlated to previous δ¹⁸O records (e.g., Sites 607 and 846) although many are better resolved by the stack. In the Pleistocene, the signal-to-noise ratio of δ¹⁸O is sufficiently high that most isotopic stages and substages are accurately recorded in individual sediment cores. One exception is the warm substage of MIS 28, which is quite clear in the LR04 stack but absent in the S95 composite and somewhat distorted in DSDP Site 607. The lower signal-to-noise ratio of the Pliocene makes the definition of MIS stages from a single core more difficult. Some of the smaller Pliocene stages from Sites 607 and 846 become better defined in the stack (e.g., MIS 77 and 83) while others almost disappear because they are small or absent in most δ¹⁸O records. The stages which are unusually small or poorly defined in the LR04 stack are MIS 68, 69, 79, 80, 94, 102, G5, G8, G9, K2, and KM6.

Below the Mammoth subchron, the LR04 stack reduces noise in some portions of the record to the extent that new isotopic stages can be resolved. Therefore we introduce a new set of MIS names for these subchrons based on the identification of each stage in at least 80% of

### Table 3. Recent Glacial Terminations

<table>
<thead>
<tr>
<th>Termination</th>
<th>Magnitude, %</th>
<th>Age, ka</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>1.78 ± 0.10</td>
<td>14</td>
</tr>
<tr>
<td>II</td>
<td>1.86 ± 0.13</td>
<td>130</td>
</tr>
<tr>
<td>III</td>
<td>1.18 ± 0.16</td>
<td>243</td>
</tr>
<tr>
<td>IV</td>
<td>1.64 ± 0.13</td>
<td>337</td>
</tr>
<tr>
<td>V</td>
<td>1.97 ± 0.12</td>
<td>424</td>
</tr>
<tr>
<td>VI</td>
<td>1.15 ± 0.14</td>
<td>533</td>
</tr>
<tr>
<td>VII</td>
<td>1.57 ± 0.15</td>
<td>621</td>
</tr>
</tbody>
</table>
the high-resolution records which span it. These new stages, which fall between MG5 and ST4, are shown in Figure 8 along with the SHP95 stage identifications of Site 846 and six other high-resolution benthic records. Each proposed change to the SHP95 stage names is described below. First, SHP95 stages MG5 and MG6 at the bottom of the Mammoth-Gauss interval are subdivided into stages MG5–MG12, as shown in Figure 8. Next, SHP95 stage Gi15 is subdivided into stages Gi15–Gi19, causing SHP95 stages Gi16–Gi22 to be renamed Gi20–Gi26. SHP95 stage N1 is split into stages N1–N3, and SHP95 stages N2–N8 are renamed N4–N10. Finally, we insert stages Gi27–Gi28, Co3–Co4, CN3–CN8, and ST3–ST4 at the bottoms of their respective subchrons, where they have no effect on subsequent stage names. From the Thvera subchron down, we again adopt the stage names of SHP95.

6.3. Paleomagnetic Polarity Reversals

[35] In Table 4 we compare the age estimates of paleomagnetic polarity reversals from Shackleton et al. [1990] (hereinafter referred to as SBP90), SCHPS95, CK95, Lourens et al. [1996], and the LR04 age model. Errors in these estimates can arise from both age model construction and reversal identification within sediment cores. Therefore we estimate the ages of magnetic reversals down to the Matuyama/Gauss boundary according to their average ages in Sites 607, 659, 677, 982, 983, 1090, 1146, and 1148, with outliers more than 2% away from the mean removed. The standard deviation in reversal ages from these sites ranges from 5 to 22 kyr. Because fewer records are available, below the Matuyama we also use reversal identifications from Leg 138, correlated to Site 846 [Shackleton et al., 1995b]. Ages for the Kaena and Mammoth subchrons are averages from Sites 607 and 846 while the Gauss/Gilbert boundary and the top of the Cochiti subchron are dated from Sites 659 and 846. All other polarity reversals are based solely on Site 846. Given the error involved in reversal identification, we observe that all four age models are quite similar.

6.4. Comparison to S95 Composite

[36] With a few exceptions, the LR04 global Pliocene-Pleistocene stack is similar to the S95 composite, which contains unstacked, high-resolution benthic records from sites V19-30, ODP 677, and ODP 846. One difference between the two records is that the S95 composite is ~0.14% heavier than the LR04 stack after 1.8 Ma, where
Table 4. Magnetic Polarity Reversal Ages, Ma

<table>
<thead>
<tr>
<th>Reversal</th>
<th>SBP90/</th>
<th>MIS</th>
<th>SCHPS95</th>
<th>CK95</th>
<th>Lourens et al. [1996] (This Study)</th>
<th>LR04</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brunhes/Matuyama</td>
<td>19</td>
<td>0.780</td>
<td>0.780</td>
<td>0.780</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jaramillo (t)</td>
<td>28</td>
<td>0.990</td>
<td>0.990</td>
<td>0.991</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jaramillo (b)</td>
<td>31</td>
<td>1.070</td>
<td>1.070</td>
<td>1.075</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Olduvai (t)</td>
<td>63</td>
<td>1.770</td>
<td>1.770</td>
<td>1.785</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Olduvai (b)</td>
<td>74</td>
<td>1.950</td>
<td>1.950</td>
<td>1.942</td>
<td></td>
<td>1.968</td>
</tr>
<tr>
<td>Matuyama/Gauss</td>
<td>G2</td>
<td>2.600</td>
<td>2.581</td>
<td>2.582</td>
<td></td>
<td>2.608</td>
</tr>
<tr>
<td>Kena (t)</td>
<td>G22</td>
<td>3.046</td>
<td>3.040</td>
<td>3.032</td>
<td></td>
<td>3.045</td>
</tr>
<tr>
<td>Kena (b)</td>
<td>KM2</td>
<td>3.131</td>
<td>3.110</td>
<td>3.116</td>
<td></td>
<td>3.127</td>
</tr>
<tr>
<td>Mammoth (t)</td>
<td>KM6</td>
<td>3.233</td>
<td>3.220</td>
<td>3.207</td>
<td></td>
<td>3.210</td>
</tr>
<tr>
<td>Mammoth (b)</td>
<td>MG1</td>
<td>3.331</td>
<td>3.330</td>
<td>3.330</td>
<td></td>
<td>3.319</td>
</tr>
<tr>
<td>Gauss/Gilbert</td>
<td>MG12</td>
<td>3.594</td>
<td>3.580</td>
<td>3.596</td>
<td></td>
<td>3.588</td>
</tr>
<tr>
<td>Cochiti (t)</td>
<td>G27</td>
<td>4.199</td>
<td>4.180</td>
<td>4.188</td>
<td></td>
<td>4.184</td>
</tr>
<tr>
<td>Cochiti (b)</td>
<td>Co4</td>
<td>4.316</td>
<td>4.290</td>
<td>4.300</td>
<td></td>
<td>4.306</td>
</tr>
<tr>
<td>Nunivak (t)</td>
<td>N1</td>
<td>4.479</td>
<td>4.480</td>
<td>4.493</td>
<td></td>
<td>4.478</td>
</tr>
<tr>
<td>Nunivak (b)</td>
<td>N9</td>
<td>4.623</td>
<td>4.620</td>
<td>4.632</td>
<td></td>
<td>4.642</td>
</tr>
<tr>
<td>Sidufjall (t)</td>
<td>SI2</td>
<td>4.781</td>
<td>4.800</td>
<td>4.799</td>
<td></td>
<td>4.807</td>
</tr>
<tr>
<td>Sidufjall (b)</td>
<td>Si6</td>
<td>4.878</td>
<td>4.890</td>
<td>4.896</td>
<td></td>
<td>4.898</td>
</tr>
<tr>
<td>Thvera (t)</td>
<td>T1</td>
<td>4.977</td>
<td>4.980</td>
<td>4.998</td>
<td></td>
<td>4.989</td>
</tr>
<tr>
<td>Thvera (b)</td>
<td>TG2</td>
<td>5.232</td>
<td>5.230</td>
<td>5.236</td>
<td></td>
<td>5.254</td>
</tr>
</tbody>
</table>

*Here t, top; b, bottom.

6.5. Comparison to Other Stacks

[19] The LR04 benthic stack is generally similar to previously published stacks with respect to MIS features and timescale but differs somewhat in its variance and spectral density. Table 5 gives a summary of total and orbital-band variances for the late Pleistocene from the five $\delta^{18}O$ stacks discussed in this paper. We perform Blackman-Tukey spectral analysis for 0–780 ka with a lag of 400 kyr. (SPECMAP is analyzed over only the last 625 kyr with a 350-kyr lag.) The LR04 stack has more total variance than any of the other stacks but also contains proportionally more sites from the Atlantic, which may increase the amplitude of its deep-water temperature signal. When only deep Pacific sites are stacked, the variance decreases to 0.16%. This is comparable to the variance of the S95 composite, which represents one Pacific site, but still larger than the stacks of SPECMAP and Karner et al. [2002], suggesting that their

![Figure 9](image-url)
stacking techniques fail to preserve the full amplitude of late Pleistocene δ18O change.

[40] The MIS features of the LR04 and SPECMAP stacks are quite similar back to 625 ka, but the planktonic SPECMAP stack has relatively more variance in the eccentricity and precession bands and less in obliquity, possibly due to precessional responses in sea-surface conditions. The variance of the SPECMAP stack is only 60% that of the LR04 stack from 0–625 ka. The low resolution of SPECMAP records and the smoothing performed on the final stack probably played a large role in reducing SPECMAP variance. The SPECMAP and LR04 age models typically differ by less than 6 kyr since 625 ka (Figure 11). The SPECMAP age model is distorted before 625 ka due to an error in the accepted age of the Brunhes/Matuyama reversal, later corrected by Shackleton et al. [1990].

[41] Karner et al. [2002] present a “minimally tuned” stack of six tropical benthic δ18O records extending to 860 ka. Before stacking they tune the obliquity component of each record and apply a phase offset to produce a core-top age of 0 kyr. Unlike the development of our age model, their tuning requires initial age estimates to calculate the 41-kyr component of each record. This step produces alignment errors which cause the authors to create a second stack that excludes records with highly variable sedimentation rates. This second, tropical stack has consistently less amplitude than ours and a mean standard error of 0.09% (compared to 0.05% for the LR04 stack over the same interval). The reduced amplitude of their stack is probably due to the introduction of phase shifts between its component δ18O records. Phase differences of up to 11 kyr between their δ18O records can be expected to reduce their stack’s precession component in particular. Indeed, the tropical stack has only 25% as much precessional variance as the LR04 stack (Table 5). The Karner et al. [2002] and LR04 age models generally differ by 3–13 kyr, converging only at 0 and

![Figure 10.](image-url)

(a) Late Pleistocene age models of the LR04 stack, the S95 composite, and the EDC Antarctic ice core (rescaled ice δD, EDC2 age model) [EPICA Community Members, 2004]. Circles mark age control points used to parameterize the EDC2 ice-flow model. (b) The average normalized sedimentation rates (defined in section 5.3) produced by each age model.

<table>
<thead>
<tr>
<th>Table 5. Orbital Variance in δ18O, 0–780 ka</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
</tr>
<tr>
<td>Total Variance, %²</td>
</tr>
<tr>
<td>Eccentricity (88–120 kyr), %</td>
</tr>
<tr>
<td>Obliquity (38–48 kyr), %</td>
</tr>
<tr>
<td>Precession (17–25 kyr), %</td>
</tr>
</tbody>
</table>

²This study.
³From 0 to 625 ka.
⁴From Karner et al. [2002].
⁵From Huybers and Wunsch [2004] (EOF1, normalized).
860 ka. However, the lower precession power of the tropical stack (Figure 12) is not caused by age model differences because using the LR04 age model only increases the tropical stack’s precession power to 2.8% of total variance.

The depth-derived age model of Huybers and Wunsch [2004] ranges from 5 kyr older to 8 kyr younger than the LR04 age model and averages 6.5 kyr younger from 150–500 ka. These age differences all fall within the uncertainty estimates published for the HW04 age model. The leading EOF of their best benthic and planktonic records contains proportionally more variance than the LR04 stack in the 100-kyr band but less in the 41- and 23-kyr bands. Huybers and Wunsch [2004] predict this drop off in orbital variance at higher frequencies due to the effects of jitter in their age model. The spectral power and substage features of their EOF are also affected by the use of only 17 age control points to align the records. Interestingly, even their benthic EOF with no orbital tuning has more variance in the precession band (3.6%) than the minimally tuned stack of Karner et al. [2002].

7. Discussion

7.1. Age Model Uncertainty

The greatest potential source of error in the LR04 age model is uncertainty in the orbital solution, which may be as high as 25 kyr in the early Pliocene. Relative to the orbital solution, our tuning errors should be no more than a few thousand years because we tune a low-noise signal and avoid spikes in the stack’s average sedimentation rate. The only portion of the timescale for which we consider tuning errors greater than 10 kyr possible is prior to 4.3 Ma, where the stack contains less 41-kyr variance and larger deviations in average LSR are required to achieve coherence with obliquity. Before 5 Ma the LR04 age model is also subject to increased uncertainty because the stack contains fewer records and inherently has fewer tuning and alignment constraints.

In the more recent part of the age model, most of the uncertainty derives from our sedimentation rate constraint and the assumed response times of the ice sheets. The LSR tuning technique may neglect some real but high-frequency changes in global LSR, such as those resulting from global climate reorganizations over glacial-interglacial cycles. However, such changes would produce age model errors of no more than several thousand years, and alignment to the tuning target prevents these errors from accumulating over multiple cycles. Deviations from the tuning target due to our sedimentation rate constraints are typically no more than 4 kyr. Uncertainty in ice sheet response time could produce errors of 1 kyr in the Pleistocene and 3.5 kyr in the Pliocene. Including all sources of error, we estimate the uncertainty in the LR04 age model to be 40 kyr from 5.3–5 Ma, 30 kyr from 5–4 Ma, 15 kyr from 4–3 Ma, 6 kyr from 3–1 Ma, and 4 kyr from 1–0 Ma.

7.2. Precession Phase and Deep-Water Temperature

As explained in section 5.4, the time constant of our ice model is the primary factor controlling the stack’s phase relative to obliquity. Because we emphasize obliquity in our tuning procedure, the stack’s phase relative to precession is allowed to deviate from that of the ice model. Indeed, Figure 7 shows that the stack’s lag in precession actually decreases at 2.7 Ma while the ice-sheet response time and obliquity lag begin to increase. From 2.7–1.6 Ma the average precession lag is only 21° or 1.3 kyr, about 2 ± 1 kyr smaller than that of our ice model tuning target. This small lag suggests that a
significant portion of the precession component of late Pliocene δ18O is a deep-water temperature signal which leads ice volume. An increase in the magnitude of temperature response at 2.7 Ma would account for the observed decline in precession lag during the onset of northern hemisphere glaciation. The temperature response may have continued to increase from 2.7–1.6 Ma, compensating for the gradually increasing lag of the ice model. At 1.6 Ma the precession lag suddenly jumps by 45° relative to that of obliquity, putting it in close agreement with our ice model for the rest of the Pleistocene.

[46] Phase measurements are fairly sensitive to age model uncertainty, but this is not a likely explanation for this sudden phase shift. First, the stack’s obliquity phase is approximately constant at 1.6 Ma. Changing the age model to eliminate the jump in precession lag would therefore produce a counterintuitive decline in obliquity lag. If the ice model’s mean time constant $T_m$ is held constant at 15 kyr for the last 3 Myr, a 30° change in precession lag still occurs at 1.6 Ma. Finally, the use of an ice model forced by insolation on a day other than 21 June shifts the precession lag of the entire stack but does not affect the sudden change at 1.6 Ma.

[47] The observed increase in δ18O lag at 1.6 Ma could be due to a decline in precession-driven temperature change, an increase in the precession response of ice volume, or an increase in the lag of temperature. We propose that either a climate feedback sensitive to precession enhanced ice sheet response or the deep-water temperature signal became phase-locked with ice volume due to the increased climatic influence of large northern hemisphere ice sheets. Additionally, a pronounced expansion of polar (cold water) fauna occurs in the North Atlantic at about this time [Raymo et al., 1986; Mc Intyre et al., 2001].

[48] Finally, the stack’s coherence with precession from 4.1–2.8 Ma provides clues to the climate’s response before the growth of major northern hemisphere ice. The stack’s phase relative to precession in this interval demonstrates that northern hemisphere insolation was the major driver of benthic δ18O change by at least 4.1 Ma, perhaps through northern deep-water formation or the growth of small northern glaciers. Precission response is not significantly coherent prior to 4.1 Ma, presumably due to weaker δ18O response, but our phase estimates are still indicative of northern hemisphere forcing. We also note that the stack’s precession lag prior to 3.6 Ma is sensitive to the value of tidal dissipation in the orbital solution, producing an uncertainty of about 30°.

8. Conclusions
[49] The global Pliocene-Pleistocene stack presented in this paper contains benthic δ18O data from 57 globally distributed sites and has an average standard error of only 0.06‰. The LR04 age model takes advantage of the stack’s low noise content and conservatively tunes the stack within the constraints provided by global sedimentation rates. The LR04 stack and the LR04 age model provide the paleoclimate community with two stratigraphic tools, which can be applied to a wide variety of Pliocene-Pleistocene studies. We hope that they will serve as a much-needed common timescale and reference of comparison (correlation target) for the large number of paleoceanographic records collected recently.

[50] The LR04 stack agrees well with previously published stacks for the late Pleistocene but exhibits significantly more variance as the result of higher-resolution records, a better alignment technique, and a greater percentage of records from the Atlantic. The LR04 stack is also the first stack to extend before 2.5 Ma and therefore offers an invaluable improvement in signal quality for the early to mid-Pliocene. We define 24 new isotopic stages from 5.0–3.4 Ma and identify several likely errors in the S95 composite. The LR04 age model, designed to minimize changes in global sedimentation rates, generally supports the SPECMAP timescale back to 625 ka and the S95 age model, except from 0.6–0.4 Ma and before 4.5 Ma. Finally, the LR04 stack’s phase relative to precession suggests the presence of a large deep-water temperature signal from 2.7–1.6 Ma and reveals a sudden change in the phase of precession response at 1.6 Ma.

Notation

$x$ 21 June insolation at 65°N, W/m²;
$y$ modeled ice volume;
$b$ nonlinearity coefficient of ice;
$T_m$ mean time constant of ice, kyr;
$\sigma$ standard deviation.

[51] Acknowledgments. We thank all of the researchers who have made their data available; without their work, these results would not be possible. L. Lisiecki also thanks T. Herbert, W. Prell, and S. Clemens for their guidance throughout this project. We thank R. Tiedemann and L. Skinner for their thoughtful reviews. N. Shackleton, W. Ruddiman, P. deMenocal, Z. Liu, K. Lawrence, L. Cleaveland, P. Huybers, and M. Mudelsee also contributed many helpful comments regarding this manuscript.

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