Lawrence Berkeley National Laboratory

Title
Correlating Humidity-Dependent Ionically Conductive Surface Area with Transport Phenomena in Proton-Exchange Membranes

Permalink
https://escholarship.org/uc/item/7rq9g09g

Author
He, Qinggang

Publication Date
2011-09-15

Peer reviewed
DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.
Correlating Humidity-Dependent Ionically Conductive Surface Area with Transport Phenomena in Proton-Exchange Membranes

Qinggang He, Ahmet Kusoglu, Ivan T. Lucas, Kyle Clark, Adam Z. Weber, and Robert Kostecki*

Environmental Energy Technologies Division, Lawrence Berkeley National Laboratory

1 Cyclotron Road, Berkeley, CA 94720, USA

Abstract

The objective of this effort was to correlate the local surface ionic conductance of a Nafion® 212 proton-exchange membrane with its bulk and interfacial transport properties as a function of water content. Both macroscopic and microscopic proton conductivities were investigated at different relative humidity levels, using electrochemical impedance spectroscopy and current-sensing atomic force microscopy (CSAFM). We were able to identify small ion-conducting domains that grew with humidity at the surface of the membrane. Numerical analysis of the surface ionic conductance images recorded at various relative humidity levels helped determine the fractional area of ion-conducting active sites. A simple square-root relationship between the fractional conducting area and observed interfacial mass-transport resistance was established. Furthermore, the relationship between the bulk ionic conductivity and surface ionic conductance pattern of the Nafion® membrane was examined.

Keywords: Nafion® 212 membrane, current sensing AFM, ionic conductivity, interfacial resistance, water content

* To whom all correspondence should be addressed. E-mail: R_Kostecki@lbl.gov
1. Introduction

Research in proton-exchange-membrane fuel cells (PEMFCs) has undergone exponential growth over the past decade. The PEM is a critical component for PEMFCs and it functions as a reactant separator while providing an ionic pathway for proton transport. Nafion®, developed by DuPont, is still the most prominent PEM material for PEMFC and other related technologies. Nafion® is a perfluorinated polymer with ether side chains terminated with sulfonic-acid groups. When in contact with water, in either liquid or vapor form, Nafion® swells and undergoes nanophase separation as the hydrophilic water-filled domains form via solvation of the sulfonic-acid groups. Once the protons dissociate from the sulfonic-acid groups, they move through the water-filled pathways. These phenomena are critical for high membrane proton conductivity and high PEMFC power density.

A wealth of analytical techniques has been used to obtain morphological and structural information about Nafion®, including X-ray and neutron scattering, electron microscopy, atomic force microscopy (AFM), numerical modeling, etc. Numerous studies of the ionic conductivity of Nafion® have been reported in the literature. Slade et al. determined that ionic conductivity is a function of different orientations of the ionic clusters formed in the cast membrane. Anantaraman et al. adopted a coaxial probe technique to show that the ionic conductivity of Nafion® 117 is nonlinear with regard to water content. Peckham et al. examined sulfonated PEMs and found that the differences in proton conductivity were mainly due to differences in effective proton mobility and acid concentration.

In addition to the bulk ionic conductivity, the surface properties of PEMs play a critical role in PEMFC performance. In fact, the electrode must be in direct contact with ionic channels on the solid-membrane electrolyte to reduce the interfacial contact resistances between cell
components, which together with electrical contact resistances contribute to the overall impedance of the cell. In addition, the surface structure can affect water absorption into the membrane and influence the rate of mass-transfer processes, and thereby limit PEMFC performance. Contact angle measurements and AFM imaging showed that the surface of the PFSA membrane is predominantly hydrophobic or non-wetting, especially at low relative humidity (RH) levels.

Electrochemical scanning probe techniques are very effective for simultaneous imaging of the surface structure and local distribution of active ion-conducting channels in ion-exchange membranes. A conductive STM or AFM probe that is polarized by a potentiostat or voltage bias controller allows simultaneous real-time imaging of both the surface morphology and electrochemical activity. O’Hayre et al., obtained impedance-modulus and phase images of Nafion® as a function of relative humidity. Proton conductance variation on the Nafion® surface was mapped by Zhu and coworkers, using current-sensing atomic force microscopy (CSAFM). The surface pattern of the hydrophilic paths and their dynamic behavior on the surface of Nafion® membrane were revealed and characterized from the time-resolved ionic conductivity mapping by CSAFM. Grazing-incidence small-angle X-ray scattering (GISAXS) studies of Nafion® confirmed the hydrophobic nature of the membrane surface vs. water vapor. In marked contrast, the surface of a liquid-equilibrated membrane was found to be completely hydrophilic or wetting.

The effect of mass transfer resistance at the membrane/vapor interface on the water-transport mechanism in Nafion® has been investigated using steady-state and transient diffusion measurements. The interfacial resistance was shown to be the limiting step for water transport in thinner membranes (less than 25 µm) at lower temperatures (25 °C) and at high
relative humidity. Interestingly, Zhao et al. reported RH-independent interfacial resistance whereas Kienitz et al. reported a decrease in mass-transport coefficient with increasing RH. However, the extent to which interfacial resistance controls the water transport is still under debate due to the variety of measurement techniques and data-analysis methods used.

In this work, we examine the Nafion® 212 membrane bulk ionic conductivity and local, surface ionic conductance as a function of relative humidity and membrane water content.

2. Experimental

2.1 Bulk conductivity measurements

The bulk ionic conductivity of the membrane was measured with an in-plane four-probe technique using a BekkTech BT-112 conductivity cell. The in-plane probe cell configuration consists of two Pt outer electrodes that supply the current to the sample, and two Pt inner electrodes that measure a voltage drop that is due only to ionic conduction. The membrane sample was cut to 1 cm wide by 3 cm long and loaded into the conductivity cell, which was then assembled into Fuel Cell Technologies hardware. Temperature, pressure, and relative humidity were controlled using a fuel-cell test system (model 850E, Scribner Associates Inc.). The sample was conditioned at room temperature for 2 hr at 25% RH followed by a series of steps in RH value (25%, 30%, 40%, 50%, 60%, 70%, 80%, 90%, and 95%), with each step of 30-minute duration (operating parameters: 100 kPa, 25°C, 1 L/min total N₂ gas flow). Humidity was controlled by mixing wet and dry N₂ gases. Prior to the membrane ionic conductivity measurements the cell was allowed to equilibrate for 30 min at each RH. DC cyclic voltammetry was performed to determine the membrane bulk resistance. The potential was swept from 0.1V
to -0.1V at 5mV/s using a Reference 600 Potentiostat/Galvanostat/ZRA, Gamry Instruments. The membrane resistance was determined from the slope of the resulting voltammogram using Gamry Analysis software.

2.2 Water Uptake

The water uptake of the membrane as a function of humidity was determined using a dynamic-vapor-sorption (DVS) analyzer (Surface Measurement Systems). The sample was first equilibrated at 0% RH at T = 120 °C for two hours in order to remove any residual water in the membrane and determine the initial weight of the sample. Then, the membrane was humidified via incremental RH steps of 10% up to 95%. The membrane was equilibrated at each RH step for 2 hours to determine its overall weight and water weight \( W \). Water content \( \lambda \), which represents the number of water molecules per sulfonic acid group, is determined by:

\[
\lambda(RH) = \frac{W(RH) - W_{dry}}{W_{dry}} \times \frac{EW}{18}
\]

where \( EW \) is the equivalent molar weight of the membrane, \( i.e., 1100 \text{ g/mol for Nafion® 212.} \)

2.3 CSAFM measurements

The CSAFM experimental setup is shown in Figure 1. A commercial AFM system (model 5500, Agilent) was equipped with a tip-sample voltage bias circuit capable of sensing currents as low as 1 pA. A conductive, PtIr-coated silicon tip (\( k = 1.2 - 29 \text{ N/m, Nanosensors} \)) was applied in contact mode and served as the AFM probe to image the morphology of the membrane sample, and as the nano-electrode to probe local surface ionic conductance. During the CSAFM measurements, a DC voltage bias was applied between the AFM tip and the Pt membrane sample holder. Upon DC polarization \( \text{H}_2 \) and \( \text{O}_2 \) evolution reactions took place on the Pt sample holder.
and the AFM Pt/Ir tip, respectively. The protons generated locally at the tip travel across the membrane and are reduced to form hydrogen at the Pt membrane sample holder. All AFM experiments were performed at room temperature in an environmental chamber filled with air at 30%, 51%, 65%, 77% and 84% RH levels, which were established using saturated salt solutions of calcium chloride, potassium nitrite, sodium nitrite, sodium nitrate and potassium chloride, respectively.

3. Results and Discussion

3.1 Bulk ionic conductivity measurements

Measurements of the bulk ionic conductivity of Nafion® 212 were carried out at room temperature at RH levels ranging from 25% to 95%. Consequently, the bulk conductivity (κ) of Nafion® 212 can be calculated using the impedance fit data according to

$$\kappa = \frac{L}{R \cdot A} = \frac{L}{R \cdot W \cdot T}$$

(2)

where \( L, W, \) and \( T \) are the length (0.42 cm), width (1.0 cm), and thickness (50+0.1(RH) µm) of the Nafion® 212 sample, respectively. As noted, the thickness is a function of water uptake, and it varies from 53 to 59.5 µm for RH = 30 to 95%, respectively. The results of the ionic conductivity measurements for Nafion® 212 as a function of RH at room temperature are shown in Figure 2. Interestingly, Nafion® 212 shows ionic conductivity close to that of fully hydrated Nafion® 112 at 100% relative humidity at 25 °C (vapor equilibrated). The ionic conductivity of Nafion® 212 increases exponentially with humidity, similar to that reported for Nafion® 117. 
3.2 Surface ionic conductivity measurements

Figure 3 depicts the surface morphology, current-sensing images, surface-current distribution, and low-current and high-current contour maps obtained from the current-sensing images of Nafion® 212 for the RH range of 30 to 84% at room temperature. The topography images of Nafion® 212 show a very inhomogeneous surface although hydrophobic and hydrophilic domains composed of fluorocarbon matrix and sulfonates cannot be distinguished. Close examination of the topography and current-sensing images does not reveal a correlation between the surface morphology and current images. Since the capacitive current due to charging of the AFM tip is negligible, and only current signals associated with electrochemical reactions can be detected, the variation in surface ionic conductance is directly related to the distribution of ionic clusters on the membrane surface.15,49 Thus the current-sensing images shown in Figure 3 reflect the distribution of active ionic clusters on the surface and, to a certain extent, the percolated ion-conducting network in the membrane.

The CSAFM image of the membrane at RH = 30% (Figure 3B) shows large non-conductive regions responsible for the limited connectivity in the underlying hydrophilic network. As the RH increases to 51% and 65 %, more pronounced current pattern of more-conducting and larger active regions are observed in CSAFM images. The clustering of hydrophilic domains proceeds further at 77% and 84% RH resulting in much larger ionically conducting areas on the membrane surface. However, a few non-conducting spots, which are associated with the hydrophobic fluorocarbon phase still remain on the membrane surface.

The surface current distributions of Nafion® 212 derived from the current-sensing images at different RH are depicted in Figure 3C. The ionic-current signal is determined by the contact area between the tip and the ionic clusters on the membrane surface.48,60 Consequently, the
observed surface-current distribution reflects the average size of ionic clusters on the surface that are connected to the conductive network in the membrane bulk..

A plot of the weighted average current $I_{wa}$ versus RH that is shown in Figure 4 exhibits an exponential dependence on humidity. Although the water meniscus may also increase the contact area between the tip and the ionic clusters due to water condensation at high RH, the primary contribution to the increased current value arises from the increased proton conductance through the ionic network in the membrane\cite{44,61} and the increased surface ionic conductivity (i.e., more ionic groups are available to facilitate proton transport through the membrane) when the membrane becomes more hydrated.\cite{33,61,62}

To determine the fraction of conducting active area ($f_{aa}$), the current-sensing images must be deconvoluted into conductive and nonconductive regions. Using a Gaussian fit for the current distribution at 84% RH in Figure 3C the cutoff value ($I_c$) can be calculated from the first-standard-derivation value ($\sigma'$) according to

$$\sigma' = \sqrt{\frac{1}{N} \sum \left( x_i - \mu \right)^2} = 23.8 \text{ nA} \quad (3)$$

$$\mu = \frac{1}{N} \sum x_i$$

$$I_c = I_{wa} - \sigma = 11.2 \text{ nA} \quad (4)$$

Unfortunely, the current distributions at the other RH values do not follow a Gaussian distribution. Therefore the cutoff values are calculated using a cutoff ratio ($R$) obtained at 84% RH,

$$R = \frac{I_c}{I_m} = \frac{11.2 \text{ nA}}{35 \text{ nA}} = 0.319 \quad (5)$$
where $I_m$ is the maximum current value (35 nA) obtained from the CSAFM images.

The cut-off current ($I_c$) values were calculated for RH = 30%, 51%, 65% and 77% and listed in Table 1. The resulting contour maps of the current-sensing images that consist of low-current regions (green) and high-current regions (blue) are shown in Figure 3D. In addition, the influence of RH on the fraction of ionically conductive area is plotted in Figure 4. An increase in the fraction of the membrane active area with humidity is consistent with earlier observations. However, the fraction of conductive area of Nafion® 212 increases exponentially as a function of RH, which is contrary to Aleksandrova’s finding that the surface proton conductivity area of Nafion® 112 is proportional to RH. The difference between extruded Nafion® 112 and dispersion-cast Nafion® 212 can be attributed to differences in morphology and anisotropy of ionic channel networks.

There still remains an open question that it might be arbitrary to assign the R value as 0.319. Choosing the right R value to calculate the fraction of conducting area is important for an accurate, quantitative characterization of the membrane surface. To examine this, we used alternative R values of 0.2 and 0.4 to calculate the fraction of conductive area for Nafion® 212. From Figure 5, the exponential trend of the fraction of conductive area curve can be seen for all different R values (R = 0.2, 0.319, and 0.4). However, the results of fraction of conductive area using R values of 0.2 or 0.4 are inconsistent with the current-sensing images in Figure 3. For instance, the $f_{\text{aa}}$ value for 77% RH has already reached 99%, whereas Figure 3, row 2, column IV shows a large area of low-current domain.

To characterize accurately the effect of humidity on the ionic conductivity, RH values are converted to water content using the measured sorption isotherm from DVS analysis (Figure 6). The initial water content at 0% RH ($\lambda_0$) is around 2, indicating that a small amount of residual
water exists in the membrane even under dry conditions. Figure 7 shows the fraction of active area, \( f_{aa} \), as a function of water content, \( \lambda \). The best fit to this data is obtained by a power-law scaling relationship, i.e.

\[
f_{aa} \propto (\lambda - \lambda_0)^n \tag{6}
\]

where the scaling exponent \( n = 2.5 \) and \( \lambda_0 \) is the initial water content. Our analysis suggests that actual water content in the membrane is a much better quantity than RH for correlating the membrane surface and bulk properties.

3.3 Correlating fraction of ionically conductive area to mass transport properties

The ionically conductive areas on the membrane surface can be interpreted as the hydrophilic active sites comprising ion-rich water pools. Thus, ionic conductivity and water transport can be explored together to study the mechanisms of water and proton transport in the membrane. To understand better the role of the fraction of conducting area i.e., concentration of hydrophilic sites on the surface, we use the water-vapor mass-transport coefficient, \( k_{\text{int}} \), expressed as the reciprocal of the interfacial mass-transfer resistance\(^{64} \) (Figure 7a).

\[
N = k_{\text{int}} (a_{\text{in}} - a_{\text{out}}) \tag{7}
\]

where \( N \) is the water flux through interface, and \( a_{\text{in}} \) and \( a_{\text{out}} \) refer to the water activities directly inside and outside of the membrane interface, respectively. The interfacial mass-transfer resistance can be seen as a reciprocal resistance that is in series along with the transport resistance through the bulk membrane.

The resulting mass-transport coefficient increases (interfacial resistance decreases) with increasing water content, similar to the fraction of conducting area. Thus, the mass-transport
coefficient can be correlated with the fraction of active area; the plot of which suggests a relationship of the form \( k \propto f_a^{1/2} \) (Figure 7b). Even though the findings here correlate and support the role of hydrophilic active sites in water transport, the definitive theoretical origins of this relationship require additional information on the surface morphology and membrane nanostructure, which is beyond the scope of this work.

To obtain an approximate measure of local ionic conductivity at the active sites, the average current is normalized with the fraction of active area, \( i.e. \frac{I_{aw}}{f_{aa}} \), and plotted as a function of water content in Figure 8a. For comparison, measured bulk conductivity is also included along with an empirical fit. The scaling of bulk conductivity with water content can be written in the following empirical form based on percolation theory,\(^{14,65}\)

\[
\kappa \propto (\lambda - \lambda_0)^m
\]  

(8)

where \( \lambda_0 \) corresponds to the percolation threshold and the best-fit scaling exponent is \( m = 1.57 \), which is in accord with earlier studies on the conductivity of PFSA membranes.\(^{14,59,65,66}\) The above equation and percolation theory assume that at the percolation threshold a continuous water-filled transport network is formed across the membrane, and additional water makes the network less tortuous. Such an analysis is in concert with more complicated networks and transport derived from \textit{ab-initio} molecular dynamics for Nafion\(^\text{®}\).\(^{56}\) The normalized surface current and bulk ionic conductivity both exhibit a similar dependence on water content. By exploiting this similarity, the normalized surface current is plotted as a function of bulk conductivity (Figure 8b). Despite the limited data points, a very good linear correlation is observed, providing clear evidence for the relationship between the local and bulk conductivity.
3.4 Discussion

The accurate calculation of local ionic conductivity requires the contact area between the tip and the membrane, which is often challenging due to meniscus formation and a lack of knowledge about the meniscus shape and ionic conductivity. One can envision that a smaller meniscus may exhibit a higher ionic conductivity than a larger one due to its proximity to the sulfonic acid sites and their dissociation (i.e., Debye length), whereas the larger one has more bulk-like water. Because of the above ambiguities, we refrain from making quantitative comparisons between the local and bulk ionic conductivity. However, the linear relationship observed in Figure 8 can be used to investigate, at least qualitatively, how the ionically conducting sites on membrane surface contribute to the bulk ionic conductivity. As humidity increases additional hydrophilic sites form on the membrane surface, thereby facilitating the transport of water from the surface through the bulk membrane. In terms of proton conduction, this manifests itself as a contact resistance, where there are both highly conducting and non-conducting surfaces. Such a contact resistance has been shown to exist during ionic conductivity measurements, and it is reported to decrease with increasing humidity in a nonlinear manner\(^6\), similar to the interfacial resistance for the water transport. The contact and water-mass-transfer resistances are very likely to be of the same origin that is controlled by the humidity-dependent surface structure of the membrane. Thus, increasing the fraction of hydrophilic phase at the membrane surface enhances the water transport and associated proton transport. However, it should also be noted that the strong correlation between the mass transport properties and fraction of surface ionically conducting area is relative in that the magnitudes of the mass-transfer coefficient and/or conductivity cannot be obtained unambiguously without a reference experimental measurement.
While the underlying mechanisms between water diffusion and proton conductivity may be different, they both require transport across the surface ionic sites. Thus, it is reasonable to focus on the morphology of the membrane surface to understand the local ionic conductivity. Bass and co-workers showed that the surface morphology of Nafion is strongly related to the humidity and interfacial effects. When the membrane faces a vapor phase below saturation, the surface ionic groups orient internal to the membrane/vapor interface in order to minimize interfacial energy, thereby reducing the surface fraction of the less-favored hydrophilic sites. The degree of this effect depends on humidity, with an inversion occurring in liquid water where the minimum interfacial energy is the case of the ionic groups oriented external to the membrane/vapor interface. This model is in accord with the observations of a higher fraction of conducting active area and improved surface current at higher humidities (Figure 7). Lastly, as the bulk conductivity requires the presence of active sites (e.g., SO$_3$ ionic groups) on the membrane surface, which have a direct role in local ionic conductivity, bulk conductivity is expected to increase linearly with the surface current as confirmed in Figure 8. Therefore, the slope of the line in that figure reflects the geometric features of the membrane nanostructure responsible for the proton movement, the understanding of which requires information on the three-dimensional morphology of the membrane from surface to inner regions.

4. Conclusions

We have studied the bulk and local ionic conductivities of a Nafion® 212 membrane using electrochemical impedance spectroscopy and current-sensing atomic force microscopy. CSAFM images of surface ionic conductivity and topography of Nafion® 212 reveal that the surface-conductance variation is primarily correlated with the surface distribution of ionic clusters. The surface-current distributions of the membrane at different relative humidities
reveal a nonlinear increase of the fraction of ionically conductive area with water content. The fact that the mass-transfer coefficient of the membrane, reflecting the resistance to water transport at the membrane-vapor interface, exhibits a similar dependence on humidity suggests that this resistance is controlled by the accessibility of the hydrophilic surface domains. Indeed, the mass-transfer resistance and fraction of conductive area can be simply correlated. Moreover, the increase in the bulk conductivity and surface current with water content are also correlated, where the bulk ionic conductivity is found to be directly proportional to the local ionic conductivity, suggesting that the limiting mechanisms of proton transport are similar in both cases. The reported information is of importance for understanding transport properties at the membrane surface and in its bulk, and therefore allows for the optimization of water management and performance in fuel cells.

Acknowledgement

This work was supported by the Assistant Secretary for Energy Efficiency and Renewable Energy, Office of Fuel Cell Technologies of the U.S. Department of Energy under Contract No. DE-AC02-05CH11231. We would like to thank Dr. Frank McLamon for helpful comments and suggestions during preparation of this manuscript.
References


(37) Shevchenko, V. V.; Gumennaya, M. A. Theoretical and Experimental Chemistry 2010, 46, 139.


(40) Aleksandrova, E.; Hiesgen, R.; Friedrich, K. A.; Roduner, E. Physical Chemistry Chemical Physics 2007, 9, 2735.


(50) Bass, M.; Freger, V. *Polymer* **2008**, *49*, 497.


Captions

Table 1  
Current-sensing AFM results for Nafion® 212 at different relative humidities

Figure 1  
Illustration of the setup for CSAFM measurement with Nafion® 212

Figure 2  
Influence of RH on the bulk conductivity of Nafion® 212

Figure 3  
Synchronized AFM topography (row 1), current-sensing image (row 2), current distribution (row 3) and low-current (green) and high-current (blue) contour maps for current-sensing images (row 4) of Nafion® 212 (bias voltage: -1.5V, scan size: 5 x 5 µm², scan rate: 1 Hz), Column I: RH=30%; Column II: RH=51%; Column III: RH=65%; Column IV: RH=77%; Column V: RH=84%. The red curves in the current distribution graph for RH=84% indicate a Gaussian fit.

Figure 4  
Influence of RH on the weighted-average current values of the conduction distributions and fraction of conducting active area from current-sensing images of Nafion® 212

Figure 5  
Influence of RH on the fraction of conducting active area values of a Nafion® 212 sample with three cutoff ratio values.

Figure 6  
Sorption isotherm of Nafion® 212 measured at 25°C.

Figure 7  
(a) Fraction of active area, f_{aa}, and mass-transport coefficient, k_{int},^{64} as a function of water content for Nafion® 212. (b) Correlation of the mass-transport coefficient with the fraction of active area for Nafion® 212. Water-content values are determined from the relative humidities using the measured sorption isotherm (Fig. 7).
Figure 8  Comparison (a) and correlation (b) of normalized average current (with respect to the fraction of active area) and bulk conductivity of Naﬁon® 212 at 25°C.
Table 1

<table>
<thead>
<tr>
<th>RH</th>
<th>30%</th>
<th>51%</th>
<th>65%</th>
<th>77%</th>
<th>84%</th>
</tr>
</thead>
<tbody>
<tr>
<td>$I_{wa}$ (nA)</td>
<td>0.025</td>
<td>0.29</td>
<td>1.87</td>
<td>6.49</td>
<td>14.8</td>
</tr>
<tr>
<td>$I_{c}$ (nA)</td>
<td>0.038</td>
<td>0.35</td>
<td>2.23</td>
<td>7.02</td>
<td>11.2</td>
</tr>
<tr>
<td>Conducting active area %</td>
<td>4.1</td>
<td>13.7</td>
<td>30.9</td>
<td>65.2</td>
<td>94.8</td>
</tr>
</tbody>
</table>

* $I_{wa}$: the weighted average of current distribution derived from topography and current-sensing images of a Nafion® 212 membrane; $I_{c}$: the cutoff value for calculation of fraction of conductive area ($f_{wa}$)
Figure 1

\[ 2H_2O \rightarrow O_2 + 4H^+ + 4e^- \]

\[ 4H^+ + 4e^- \rightarrow 2H_2 \]
Figure 2
Figure 4
Figure 5
Figure 6

\[ f_{aa} \propto (\lambda - \lambda_0)^{2.5} \]

Figure 7a

\[ k_{int} \propto (\lambda - \lambda_0)^{1.25} \]
Figure 7b
Figure 8a
Figure 8b