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Moridis, George

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George Moridis, John Apps,  
Karsten Pruess, and Larry Myer

**Earth Sciences Division**

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**EOSHYDR: A TOUGH2 MODULE  
FOR CH<sub>4</sub>-HYDRATE RELEASE AND  
FLOW IN THE SUBSURFACE**

**George Moridis, John Apps,  
Karsten Pruess and Larry Myer**

*Earth Sciences Division  
Lawrence Berkeley National Laboratory  
Berkeley, CA 94720*

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# **EOSHYDR: A TOUGH2 Module for CH<sub>4</sub>-Hydrate Release and Flow In the Subsurface**

**George Moridis, John Apps, Karsten Pruess and Larry Myer**

Earth Sciences Division, Lawrence Berkeley National Laboratory, University of California, Berkeley, California

**Abstract.** EOSHYDR is a new module for the TOUGH2 general-purpose simulator for multi-component, multiphase fluid and heat flow and transport in the subsurface. EOSHYDR is designed to model the non-isothermal CH<sub>4</sub> release, phase behavior and flow under the conditions of the common methane hydrate deposits (i.e., in the permafrost and in deep ocean sediments) by solving the coupled equations of mass and heat balance. As with all other members of the TOUGH2 family of codes, EOSHYDR can handle multi-dimensional flow domains and cartesian, cylindrical or irregular grids, as well as porous and fractured media.

EOSHYDR extends the thermophysical description of water to temperatures as low as  $-30^{\circ}\text{C}$ . Both an equilibrium and a kinetic model of hydrate formation or dissociation are included. Two new solid phases are introduced, one for the CH<sub>4</sub>-hydrate and the other for ice. Under equilibrium conditions, water and methane, as well as heat, are the main components. In the kinetic model, the solid hydrate is introduced as the fourth component. The mass components are partitioned among the gas, liquid and the two solid phases. The thermodynamic phase equilibrium in EOSHYDR is described by the P-T-X diagram of the H<sub>2</sub>O - CH<sub>4</sub> system. Phase changes and the corresponding heat transfers are fully described. The effect of salt in pore waters on CH<sub>4</sub> solubility and on the growth and decomposition of gas hydrates is also taken into account.

Results are presented for three test problems designed to explore different mechanisms and strategies for production from CH<sub>4</sub>-hydrate reservoirs. These tests include thermal

stimulation and depressurization under both permafrost and suboceanic conditions. The results of the tests tend to indicate that CH<sub>4</sub> production from CH<sub>4</sub>-hydrates is technically feasible and has significant potential. Both depressurization and thermal stimulation seem to be capable of producing substantial amounts of CH<sub>4</sub> gas.

## 1. Introduction

Gas hydrates are solid compounds in which gas molecules are encaged inside the lattices of ice crystals. These gases are referred to as *guests*, whereas the ice crystals are called *hosts*. Of particular interest are hydrates in which the gas is a hydrocarbon. Under suitable conditions of low temperature and high pressure, hydrocarbon gases will react with water to form hydrates. The equation of formation or decomposition of hydrates from a hydrocarbon  $M$  and water is



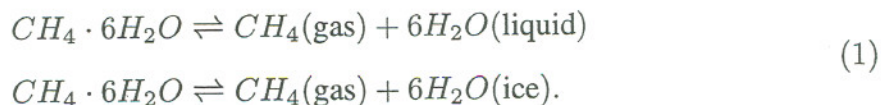
where  $n_h$  is the hydration number.

Vast amounts of hydrocarbons are trapped in hydrate deposits [Sloan, 1998]. Such deposits exist where the thermodynamic conditions allow hydrate formation, and are concentrated in two distinctly different types of geologic formations where the necessary low temperatures and high pressures exist: in the permafrost and in deep ocean sediments. The lower depth limit of hydrate deposits is controlled by the geothermal gradient.

Current estimates of the worldwide quantity of hydrocarbon gas hydrates range between  $10^{15}$  to  $10^{18}$  m<sup>3</sup>, and even the most conservative estimates of the total quantity of gas in hydrates may easily surpass by a factor of two the energy content of the total fuel fossil reserves recoverable by conventional methods [Sloan, 1998].

The majority of hydrocarbon gas hydrates are CH<sub>4</sub>-hydrates. Such hydrates concentrate methane volumetrically by a factor of 164, and require less than 15% of the recovered energy for dissociation. CH<sub>4</sub>-hydrates have a hydration number  $n_h = 6$ , and belong to the I crystalline structure [Sloan, 1991], which contains 46 H<sub>2</sub>O molecules per unit cell. Depending on the thermodynamic state of the system, the amount of hydrate created or

released is determined from the equilibrium reactions



The magnitude of this resource makes methane hydrate reservoirs a substantial future energy resource. While current economic realities do not favor  $CH_4$  production from hydrates, the potential of this resource clearly demands evaluation.

Three methods have been proposed for recovering  $CH_4$  from hydrate deposits. The first method is thermal stimulation [McGuire, 1981], in which fluids at an elevated temperature are injected into the hydrate formation and effect  $CH_4$  release by temperature. The second method is depressurization [Holder *et al.*, 1982], in which the  $CH_4$  release is achieved by lowering the pressure below that of the hydrate stability field at a given temperature. The third method is inhibitor injection [Kamath and Godbole, 1987], in which the  $CH_4$  is produced after the injection of substances (e.g., brines, methanol, glycol) which destabilize the hydrate. Combinations of these methods can also be used.

In this paper, we present the development of EOSHYDR, a TOUGH2 [Pruess, 1991] module for the simulation of the potential of recovering gas from hydrate reservoirs. EOSHYDR is designed to model the non-isothermal  $CH_4$  release, phase behavior and flow under the conditions of the common methane hydrate deposits (i.e., in the permafrost and in deep ocean sediments) by solving the coupled equations of mass and heat balance. Although  $CH_4$ -hydrates contain small amounts of other gaseous components, which are important for nucleation [Sloan, 1998], in this module we assume pure  $CH_4$ .

## 2. Governing Equations

A non-isothermal  $CH_4$ -hydrate system can be fully described by three mass balance equations and an energy balance equation. Following Pruess [1987; 1991], the components

$$\kappa \equiv \begin{cases} w & \text{for water} \\ m & \text{for } CH_4 \\ h & \text{for heat} \end{cases} \quad \text{and} \quad \kappa \equiv \begin{cases} w & \text{for water} \\ m & \text{for } CH_4 \text{ gas} \\ c & \text{for } CH_4\text{-hydrate} \\ h & \text{for heat} \end{cases}$$

under equilibrium and kinetic conditions, respectively, are considered. Mass balance in every subdomain (gridblock)  $n$  into which the flow domain is subdivided by the integral

finite difference method of TOUGH2 [Pruess, 1991] dictates that

$$\frac{d}{dt} \int_{V_n} M^\kappa dV = \int_{\Gamma_n} \mathbf{F}^\kappa \cdot \mathbf{n} d\Gamma + \int_{V_n} q^\kappa dV, \quad (2)$$

where

$V, V_n$	volume, volume of subdomain $n$ [ $\text{m}^3$ ];
$M^\kappa$	mass accumulation term of component $\kappa$ [ $\text{kg m}^{-3}$ ];
$M^h$	energy accumulation term [ $\text{J m}^{-3}$ ];
$\Gamma_n$	surface area of subdomain $n$ [ $\text{m}^2$ ];
$\mathbf{F}^\kappa$	Darcy flux vector of component $\kappa$ [ $\text{kg m}^{-2} \text{s}^{-1}$ or $\text{J m}^{-2} \text{s}^{-1}$ ];
$\mathbf{n}$	inward unit normal vector [ <i>dimensionless</i> ];
$q^\kappa$	source/sink term of component $\kappa$ [ $\text{kg m}^3 \text{s}^{-1}$ or $\text{J m}^3 \text{s}^{-1}$ ];
$t$	time [s].

Under the conditions of production from a natural  $\text{CH}_4$ -hydrate formation (i.e., in the permafrost or in deep marine sediments) there are four possible phases  $\beta$ : an aqueous phase ( $\beta \equiv w$ ), a gaseous phase consisting of water vapor and  $\text{CH}_4$  ( $\beta \equiv g$ ), a *solid* phase composed of  $\text{CH}_4$ -hydrates ( $\beta \equiv s$ ), and a *solid* ice phase ( $\beta \equiv i$ ).

## 2.1. Accumulation Terms

EOSHYDR allows both equilibrium and kinetic hydrate formation or dissociation. Under equilibrium conditions, the mass accumulation terms  $M^\kappa$  in equation (2) are given by

$$\begin{aligned} M^w &= \sum_{\beta \equiv w, g, i} \phi S_\beta \rho_\beta X_\beta^w + k_1 \phi \rho_c P_g^m \\ M^m &= \sum_{\beta \equiv w, g, i} \phi S_\beta \rho_\beta X_\beta^m + k_2 \phi \rho_c P_g^m, \end{aligned} \quad (3)$$

where

$\phi$	porosity [ <i>dimensionless</i> ];
$\rho_\beta$	density of phase $\beta$ [ $\text{kg m}^{-3}$ ];
$S_\beta$	saturation of phase $\beta$ [ <i>dimensionless</i> ];
$X_\beta^\kappa$	mass fraction of component $\kappa$ ( $\equiv w, m, c$ ) in phase $\beta$ [ $\text{kg/kg}$ ]
$P_g^m$	partial pressure of $\text{CH}_4$ in the gas phase [Pa].



The parameter  $k_2$  [ $\text{m}^3 \text{Pa}^{-1}$ ] is a *partition coefficient* distributing  $\text{CH}_4$  between the gas phase and the hydrate phase. In that respect,  $\text{CH}_4$  in the hydrate is considered sorbed  $\text{CH}_4$  gas in a manner akin to linear sorption, and the amount is a linear function of the partial pressure of  $\text{CH}_4$ . The value of  $k_1$  is determined from the equilibrium constant  $K = K(T)$  of Equation (1), which is given by

$$\ln K = -\frac{\Delta G^0}{RT} \quad \text{and/or} \quad \frac{d \ln K}{dT} = \frac{\Delta H^0}{RT^2} \quad (4)$$

where

$\Delta G^0$  standard Gibbs energy change of hydrate formation or dissociation [J/mole];

$\Delta H^0$  hydrate latent heat of formation or dissociation [J/mole];

$R$  universal gas constant [= 8.3145 J mol<sup>-1</sup> K<sup>-1</sup>].

The equilibrium in Equation (1) dictates that

$$K = \frac{\alpha_m (\alpha_w)^6}{\alpha_c} \quad (5)$$

In Equation (5),  $\alpha$  is the activity of the component denoted by the subscript, and the subscripts  $m$ ,  $w$  and  $c$  denote  $\text{CH}_4$ ,  $\text{H}_2\text{O}$  and  $\text{CH}_4$ -hydrate, respectively. For  $\text{CH}_4$ ,

$$\alpha_m = \frac{f}{f_0} = \frac{y \Phi P_g}{y \Phi_0 P_{g0}} \quad (6)$$

where

$f$  fugacity of  $\text{CH}_4$  in the gas phase [Pa];

$\Phi$  fugacity coefficient [dimensionless];

$y$  mol fraction of  $\text{CH}_4$  in the gas phase;

$0$  subscript denoting standard pressure [= 101300 Pa].

The fugacity coefficient  $\Phi$  is determined from

$$\ln \Phi = \frac{b}{b_M} (z - 1) - \ln \left( z - \frac{b_M P_g}{RT} \right) - \frac{a_M}{b_M RT} \left[ \frac{2 \sum_i y_i a_{ij}}{a_M} - \frac{b}{b_M} \right] \ln \left( 1 + \frac{b_M P}{z RT} \right), \quad (7)$$

in which the summation is over the components  $i$  in the gas phase. The compressibility  $z = PV/RT$  and the terms  $a$  and  $b$  are obtained from the Soave-Redlich-Kwong equation of state [Soave, 1972], i.e.,

$$P = \frac{RT}{V-b} - \frac{a}{V(V-b)}, \quad (8)$$

$$z^3 - z^2 + (A - B - B^2)z - aB = 0, \quad (9)$$

where

$$a(T) = a_c(T_c) \gamma(T_r, \omega), \quad (10)$$

$$a_c(T_c) = 0.42747 R^2 T_c^2 / P_c, \quad \gamma(T_r, \omega) = [1 + \eta(1 - T_r)^{0.5}]^2 \quad (11)$$

$$\eta = 0.48508 + 1.55171\omega - 0.15613\omega^2, \quad b = 0.08664 RT_c / P_c, \quad (12)$$

with

$$A = \frac{aP}{(RT)^2} \quad \text{and} \quad B = \frac{bP}{RT}. \quad (13)$$

The variables  $T_c$ ,  $P_c$  and  $\omega$  are the critical temperature, critical pressure, and the acentric factor of the gaseous component, respectively, while  $T_r$  is the reduced temperature defined as  $T_r = T/T_c$ . The subscript  $M$  in (7) denotes the mixing parameters, which are defined as

$$a_M = \sum_i \sum_j y_i y_j a_{ij}, \quad b_m = \sum_i y_i b_i, \quad a_{ij} = (a_i a_j)^{1/2} (1 - k_{ij}), \quad (14)$$

where  $a_{12} = a_{21}$ . The interaction parameters  $k_{ij}$  are close to zero for interactions between hydrocarbons, but are significantly different from zero for hydrocarbon-water interactions [Sloan, 1998].

The activity of the hydrate  $\alpha_c$  in Equation (5) is essentially constant at a given temperature regardless of whether the other phase is present. The activity  $\alpha_w$  is taken to be equal to one at relatively low pressures because of the low solubility of methane in water. In the presence of an inhibitor (such as salt in the water in ocean sediments of hydrates),  $\alpha_w$  is determined from Piroen's equation [Sloan, 1998]

$$\ln \alpha_w = \frac{\Delta H^0}{6R} \left[ \frac{1}{T_w} - \frac{1}{T_s} \right], \quad (15)$$

where  $T_w$  and  $T_s$  are the hydrate formation temperatures [K] in pure water and in the salt solution, respectively. The hydrate formation temperature in the presence of salt,  $T_s$ , is obtained from the equation [Sloan, 1998]

$$T_s = \left[ \frac{1}{T_w} - \frac{3.6046 \times 10^4}{\Delta H^0} \left( \frac{1}{273.15} - \frac{1}{T_{fs}} \right) \right]^{-1}, \quad (16)$$

where  $T_{fs}$  is the freezing point of the salt solution [K].

The parameter  $k_1$  in equation (3) is related to  $k_2$  through the stoichiometry of the hydrate. It is obvious that

$$\frac{k_1}{k_2} = \frac{6 W^w}{W^m} = 6.75, \quad (17)$$

where  $W^w$  and  $W^m$  are the molecular weights [ $\text{kg mol}^{-1}$ ] of water and  $\text{CH}_4$ , respectively. The amount of water released from the hydrates is added either to the aqueous or the ice phase, according to the prevailing thermodynamic conditions.

The heat of dissociation  $\Delta H^0$  in equation (4) under three-phase conditions ( $L_w$ -H-V or I-H-V) is determined from the Clausius-Clapeyron equation

$$\Delta H^0 = z R T^2 \frac{d \ln P}{dT}, \quad (18)$$

which is in excellent agreement with experimental data [Sloan, 1998]. The heat of hydrate formation under three-phase conditions is given by the equation

$$\Delta H^0 = C_1(T) + \frac{C_2(T)}{T}, \quad (19)$$

where  $C_1$  and  $C_2$  are experimental parameters (functions of  $T$ ) determined by Kamath [1984].

The values of some mass fractions can be determined *a priori*. Assuming that the solubility of the  $\text{CH}_4$  gas in ice is sufficiently small to be considered negligible,  $X_i^m = 0$  and  $X_i^w = 1$ . From the stoichiometry of hydrates,  $X_s^w = 0.87097$  and  $X_s^m = 0.12903$ .

Kinetic data on hydrate formation and dissociation under conditions characteristic of their presence in the subsurface are not available [Sloan, 1998]. Kinetic data from laboratory studies [Englezos *et al.*, 1987a,b; Skovborg and Rasmussen, 1994; Kamath, 1984; Selim and Sloan, 1985] appear to be specific to the apparatus used in the study, involve parameters

which are difficult to evaluate, and have limited applicability to reservoir-level studies. EOSHYDR allows consideration of kinetic hydrate formation or dissolution assuming a standard kinetic model, with parameters which may become available in the future from appropriate laboratory experiments.

Under kinetic conditions, the mass accumulation terms  $M^\kappa$  in Equation (2) are given by

$$M^\kappa = \sum_{\beta \equiv w, g, s, i} \phi S_\beta \rho_\beta X_\beta^\kappa, \quad \kappa \equiv w, m, c. \quad (20)$$

In the kinetic model,

$$\text{for } \beta \equiv w : X_w^c = 0,$$

$$\text{for } \beta \equiv g : X_g^c = 0,$$

$$\text{for } \beta \equiv s : X_s^w = X_s^m = 0, \quad X_s^c = 1, \quad \text{and}$$

$$\text{for } \beta \equiv i : X_i^m = X_i^c = 0, \quad X_i^w = 1.$$

The heat accumulation term includes contributions from the rock matrix and all the phases, and is given in both the equilibrium and the kinetic model by the equation

$$M^h = (1 - \phi) \rho_R C_R T + \sum_{\beta \equiv w, g, s, i} \phi S_\beta \rho_\beta u_\beta \quad (21)$$

where

$\rho_R$  rock density [ $\text{kg m}^{-3}$ ];

$C_R$  heat capacity of the dry rock [ $\text{J kg}^{-1} \text{K}^{-1}$ ];

$T$  temperature [K];

$u_\beta$  specific internal energy of phase  $\beta$ .

Due to the limited solubility of  $\text{CH}_4$  in the aqueous phase under the conditions of  $\text{CH}_4$ -hydrate occurrence in the subsurface, a good approximation to  $u_w$  is obtained by the aqueous phase to be pure water. The specific internal energy of the gaseous phase is a very strong function of composition, and is given by

$$u_g = \sum_{\kappa \equiv w, m} X_g^\kappa u_g^\kappa, \quad (22)$$

where  $u_g^\kappa$  is the specific internal energy of component  $\kappa$  in the gaseous phase.

## 2.2. Flux Terms

The mass fluxes of water and CH<sub>4</sub> gas include contributions from the aqueous and gaseous phases, i.e.,

$$\mathbf{F}^\kappa = \sum_{\beta \equiv w, g} \mathbf{F}_\beta^\kappa, \quad \kappa \equiv w, m. \quad (23)$$

The contributions of the two solid phases ( $\beta \equiv s, i$ ) to the fluid fluxes are zero. Therefore, in the kinetic model the mass flux of the hydrate component ( $\kappa \equiv c$ ) across all subdomain boundaries is

$$\mathbf{F}^c = 0. \quad (24)$$

For the aqueous phase,  $\mathbf{F}_w^w = X_w^w \mathbf{F}_w$ , and the phase flux  $\mathbf{F}_w$  is described by Darcy's law

$$\mathbf{F}_w = -k \frac{k_{rw} \rho_w}{\mu_w} (\nabla P_w - \rho_w \mathbf{g}), \quad (25)$$

where

- $k$  rock intrinsic permeability [m<sup>2</sup>];
- $k_{rw}$  relative permeability of the aqueous phase [*dimensionless*];
- $\mu_\beta$  viscosity of the aqueous phase [Pa s];
- $P_w$  pressure of the aqueous phase [Pa];
- $\mathbf{g}$  gravitational acceleration vector [ms<sup>-2</sup>].

The aqueous pressure  $P_w$  is given by

$$P_w = P_g + P_{cgw}, \quad (26)$$

where  $P_g = P_g^m + P_g^w$  is the gas pressure [Pa],  $P_{cgw}$  is the gas-water capillary pressure [Pa], and  $P_g^m, P_g^w$  are the CH<sub>4</sub> gas and water vapor partial pressures [Pa], respectively. The solubility of CH<sub>4</sub> in the aqueous phase is related to  $P_g^m$  through Henry's law,

$$P_g^m = H^m X_w^m \frac{W^w}{W^m}, \quad (27)$$

where  $H^m = H^m(P_g, T)$  is a factor akin to Henry's constant.  $H^m$  values for both fresh water and seawater were obtained from Vargaftik [1975] and Handa [1990].

The mass flux of the gaseous phase ( $\beta \equiv g$ ) incorporates advection and diffusion contributions, and is given by

$$\mathbf{F}_g^\kappa = -k_0 \left( 1 + \frac{b}{P_g} \right) \frac{k_{rg} \rho_g}{\mu_g} X_g^\kappa (\nabla P_g - \rho_g \mathbf{g}) + \mathbf{J}_g^\kappa, \quad \kappa \equiv w, m, \quad (28)$$

where

- $k_0$  absolute permeability at large gas pressures ( $= k$ ) [ $\text{m}^2$ ];
- $b$  *Klinkenberg* [1941]  $b$ -factor accounting for gas slippage effects [Pa];
- $k_{rg}$  relative permeability of the gaseous phase [*dimensionless*];
- $\mu_\beta$  viscosity of the gaseous phase [Pa s].

The term  $\mathbf{J}_g^\kappa$  is the diffusive mass flux of component  $\kappa$  in the gas phase [ $\text{kg m}^{-2} \text{s}^{-1}$ ], and is described by

$$\mathbf{J}_g^\kappa = -\phi S_g \underbrace{(\phi^{1/3} S_g^{7/3})}_{\tau_g} D_g^\kappa \rho_g \nabla X_g^\kappa, \quad \kappa \equiv w, m, \quad (29)$$

where  $D_g^\kappa$  is the multicomponent molecular diffusion coefficient of component  $\kappa$  in the gas phase in the absence of a porous medium [ $\text{m}^2 \text{s}^{-1}$ ], and  $\tau_g$  is the gas tortuosity [*dimensionless*] computed from the *Millington and Quirk* [1961] model. The diffusive mass fluxes of the water vapor and  $\text{CH}_4$  gas are related through the relationship of *Bird et al.* [1960]

$$\mathbf{J}_g^w + \mathbf{J}_g^m = 0, \quad (30)$$

which ensures that the total diffusive mass flux of the gas phase is zero with respect to the mass average velocity when summed over the two components ( $\kappa \equiv w, m$ ). Then the total gas phase mass flux is the product of the gas phase Darcy velocity and the gas phase density.

The heat flux accounts for both conduction and convection, and is given by

$$\begin{aligned} \mathbf{F}^h = & - \{ (1 - \phi) K_R + \phi [S_s K_s + S_i K_i + S_w K_w + S_g K_g] \} \nabla T \\ & + \sum_{\beta \equiv w, m} h_\beta \mathbf{F}_\beta, \end{aligned} \quad (31)$$

where

- $K_R$  thermal conductivity of the rock [ $\text{W m}^{-1} \text{K}^{-1}$ ];

$K_\beta$  thermal conductivity of phase  $\beta \equiv w, g, s$  [ $\text{W m}^{-1} \text{K}^{-1}$ ];  
 $h_\beta$  specific enthalpy of phase  $\beta \equiv w, g, s$  [ $\text{J kg}^{-1}$ ].

For the reasons discussed in Section 2.1, the aqueous phase specific enthalpy is assumed to be that of pure water, and the gas phase specific enthalpy is computed as

$$h_g = \sum_{\kappa \equiv w, m} X_g^\kappa h_g^\kappa, \quad (32)$$

where  $h_g^\kappa, \kappa \equiv w, m$  is the specific enthalpy of the water vapor and  $\text{CH}_4$  gas, respectively. The relationship between enthalpy  $h$  and internal energy  $u$  is described by the thermodynamic equation

$$h = u + \frac{P}{\rho}, \quad (33)$$

where  $\rho$  is the density of the gas.

### 2.3. Source and Sink Terms

In the equilibrium model, injection of a fluid into the reservoir can occur at mass rates  $\hat{q}^\kappa, \kappa \equiv w, m$ , while removal of the compounds is described by

$$\hat{q}^\kappa = \sum_{\beta = w, g} X_\beta^\kappa q_\beta, \quad \kappa \equiv w, m, \quad (34)$$

where  $q_\beta$  is the production rate of the phase  $\beta$ .

In the kinetic model, the additional sink/source terms corresponding to hydrate dissociation and release of  $\text{CH}_4$  and  $\text{H}_2\text{O}$  must be accounted for. The source term for  $\text{CH}_4$  thus becomes  $\hat{q}^m + Q^m$ , where the production rate  $Q^m$  [ $\text{kg m}^{-3} \text{s}^{-1}$ ] of  $\text{CH}_4$  is taken from reaction kinetics as

$$Q^m = k^m W^m [\text{CH}_4]^\theta = k^m W^m \left( \frac{P_g^m}{RTz} \right)^\theta, \quad (35)$$

where

$k^m = k_m(T)$ , reaction constant [ $\text{m}^{3\theta} \text{mol}^{1-\theta} \text{s}^{-1}$ ];  
 $[\text{CH}_4]$  molar concentration of  $\text{CH}_4$  [ $\text{mol m}^{-3}$ ];  
 $\theta$  order of the reaction [dimensionless].

The fact that the dissociation of CH<sub>4</sub>-hydrates involves a CH<sub>4</sub> gas and, depending on the thermodynamic conditions, either two solid phases or a solid and a liquid phase (hydrate and ice), provides supporting evidence that Equation (35) describes representatively the rate of CH<sub>4</sub> release. Although currently there is no information on  $k_m$  and  $\theta$ , EOSHYDR includes this model because of the importance of kinetic behavior of CH<sub>4</sub>-hydrates.

The source term for water (aqueous or ice phase) is  $q^w + Q^w$ , where the hydrate-related release of water  $Q^w$  is determined from the stoichiometry of Equation (1) as

$$Q^w = \frac{6W^w}{W^m} Q^m. \quad (36)$$

Similarly, the sink term corresponding to the hydrate compound is

$$\hat{q}^c = Q^c = -\frac{W^c}{W^m} Q^m, \quad (37)$$

where  $W_c$  is the molecular weight of the CH<sub>4</sub>-hydrate.

Under equilibrium conditions, the rate of heat removal or addition includes contributions of (a) the heat associated with fluid removal or addition, as well as (b) direct heat inputs or withdrawals (e.g., microwave heating), and is described by

$$\hat{q}^h = q_d + \sum_{\beta = w, g} h_{\beta} q_{\beta}. \quad (38)$$

Under kinetic conditions, Equation (38) is extended to account for the heat of dissociation, thus becoming

$$\hat{q}^h = q_d + \sum_{\beta = w, g} h_{\beta} q_{\beta} + \hat{q}^c \Delta H^0. \quad (39)$$

## 2.4. Primary Variables

In order to describe the thermodynamic state of the three- or four-component system (two mass components and a heat component under equilibrium conditions, three mass components and a heat component under kinetic conditions) in EOSHYDR, a set of three or four appropriate *primary* variables must be selected. All other *secondary* parameters (which



include thermodynamic and transport properties of the system) needed for the solution of the four coupled equations in Equation (1) are computed from the primary variables.

Under equilibrium conditions, the three primary variables in EOSHYDR are (a) the gas pressure  $P_g$ , (b) the saturation of the gas phase  $S_g$ , and (c) the temperature  $T$ . Under kinetic conditions, the four primary variables in EOSHYDR are (a) the gas pressure  $P_g$ , (b) the saturation of the gas phase  $S_g$ , (c) the CH<sub>4</sub>-hydrate saturation  $S_s$ , and (d) the temperature  $T$ . This selection of variables allows simulations when the aqueous phase is absent.

The computation of the secondary variables (i.e., aqueous phase density, gas phase density and mass fractions, gas phase viscosity, capillary pressures, relative permeabilities, diffusivities for water and CH<sub>4</sub>) follows the approach in the TOUGH2 [Pruess, 1991] and T2VOC [Falta *et al.*, 1995]. In the computation of saturation-dependent properties (i.e., capillary pressure and relative permeabilities of the gas and aqueous phases), the properties of the porous medium free of hydrates are used.

## 2.5. Phase Equilibrium

The phases discussed in this section should not be confused with the phases considered in the formulation of the mass and heat balance equations, but are rather the thermodynamic phases in the P-T-X diagram of CH<sub>4</sub> and H<sub>2</sub>O. Thermophysical properties in EOSHYDR are obtained from the Pressure-Temperature-Composition (P-T-X) diagram of CH<sub>4</sub> [Kobayashi and Katz, 1949], as well as from CH<sub>4</sub> property tables [Vargaftik, 1975] and the water tables available in TOUGH2 [Pruess, 1991]. The water tables in TOUGH2 were extended to cover the -50 C to 500 C range.

The phases in the P-T-X diagram are: V (vapor),  $L_w$  (liquid water), I (ice), H (hydrate),  $M$  (solidified methane), and  $L_m$  (liquid methane). Of particular interest are the pressures and temperatures of the  $L_w$ -H-V and I-H-V three-phase lines, which delineate the limits to hydrate formation. The relationship between the three-phase  $P$  and  $T$  in EOSHYDR is obtained from a regression fit [Kamath, 1984] to a set of experimental data listed in Sloan [1998], which yielded the equation

$$P = \exp\left(e_1 + \frac{e_2}{T}\right), \quad (40)$$

where  $P$  is in Kpa,  $T$  is in K,

$$e_1 = \begin{cases} 38.980 \\ 14.717 \end{cases} \quad \text{and} \quad e_2 = \begin{cases} -8533.80 & \text{for } 0^\circ\text{C} \geq T \geq 25^\circ\text{C} \\ -1886.79 & \text{for } -25^\circ\text{C} \geq T \geq 0^\circ\text{C}. \end{cases} \quad (41)$$

Hydrates may also exist in equilibrium with  $\text{CH}_4$  when there is no aqueous phase present, in which case the two possible two-phase systems are H-V and H- $L_m$ . In the three-phase regions, only one intensive variable is needed to specify a binary system; however, two variables are needed to specify the two-phase binary system [Sloan, 1998]. Typically, the water concentration at a specified pressure and temperature is determined as the second variable using the algorithm of Sloan [1998].

### 3. Test Problems

#### 3.1. Test Problem 1

Test Problem 1 involves the depressurization-induced release of  $\text{CH}_4$  in a reservoir containing stratified layers of  $\text{CH}_4$  gas and hydrate deposits under permafrost conditions. Figure 1 and Table 1 show a schematic of the reservoir and the reservoir properties, respectively. Gas is produced in a single well completed throughout the gas zone. The well is located at the center of the reservoir, and its production rate is constant at  $0.81944 \text{ m}^3 \text{ s}^{-1}$  (2.5 MMFCD).

The problem was first studied by Holder *et al.* [1982], who solved the uncoupled pressure and temperature equations by using a 2-D grid for pressure calculations and a 3-D grid for temperature calculations. In their approach, the heat transferred to the interface (due to the temperature gradient) was used for the hydrate dissociation, and there was no energy balance based on the existing phases and their enthalpies.

Because of the radial symmetry of the problem and the need to have a higher definition in the vicinity of the well bore, we used a 2-D cylindrical system to simulate the reservoir. The reservoir radius was  $r = 567.5 \text{ m}$ , and its thickness was  $Z = 30.5 \text{ m}$  (100 ft) equally distributed between the hydrate layer and the free gas zone. These dimensions result in a reservoir with a volume identical to the cartesian system of Holder *et al.* [1982].

The system was discretized in  $(80 \times 40 = 3200)$  gridblocks in  $(r, z)$ . Using the equilibrium model, a total of 9600 coupled equations were solved simultaneously. The 40

$\Delta z$  dimensions were (moving from the reservoir top down) were 1.5 m, 12×1 m, 0.5 m, 0.3 m, 2×0.2 m, 6×0.1 m, 0.3 m, 2×0.2 m, 0.3 m, 0.5 m, 12×1 m and 1.5 m. The  $\Delta r$  dimensions were 0.1 m (the wellbore radius), 0.1 m, 0.2 m, 0.3 m, 0.5 m, and the remaining 75  $\Delta r$  were determined from a logarithmic distribution, in which the first  $\Delta r = 0.5$  m, and the multiplier is determined from the requirement that the outer radius be equal to 567.5 m. This discretization provided substantial detail near the wellbore. The wellbore itself was simulated by the first column of gridblocks at the origin of the system, in which the vertical permeability had been set to 1 m<sup>2</sup>, i.e., practically infinite compared to the reservoir permeability of  $4.3425 \times 10^{-14}$  m<sup>2</sup> (44 md). The horizontal permeability of the wellbore gridblocks was zero in the hydrate layer and equal to the reservoir permeability in the free gas zone. The production rate was assigned to the top wellbore gridblock.

Two cases were tested. In the Case 1, the initial hydrate saturation in the hydrate zone was  $S_s = 1$ , which results in zero initial fluid permeability in this region. However, after the beginning of dissociation, the permeability of gas and released water are no longer zero, and they are determined by the relative permeability curve and the gas and aqueous saturation ( $S_g$  and  $S_w$ ) in the hydrate zone. In Case 2,  $S_g = 0.7$  and  $S_w = 0.3$ .

For the relative permeability and capillary pressure curves, the *van Genuchten* [1980] model (available in TOUGH2) was used, according to which

$$\begin{aligned}
 k_{rw} &= \bar{S}_w^{1/2} \left[ 1 - \left( 1 - \bar{S}_w^{1/m} \right)^m \right]^2 \\
 k_{rg} &= \bar{S}_g^{1/2} \left( 1 - \bar{S}_w^{1/m} \right)^{2m} \\
 P_c &= -C_p \left[ \left( \bar{S}_w \right)^{-1/m} - 1 \right]^{1-m},
 \end{aligned} \tag{42}$$

where

$$\bar{S}_w = \frac{S_w - S_r}{1 - S_r}, \quad \bar{S}_g = \frac{S_g - S_r}{1 - S_r}, \tag{43}$$

and  $S_r$  is the irreducible water saturation. In hydrate reservoirs, the sum  $\bar{S}_w + \bar{S}_g \neq 1$  because of the presence of the hydrate and the ice phases. In this simulation,  $S_r = 0.1$ ,  $m = 0.45$  and  $C_p = 10^5$  Pa.

Figure 2 shows the cumulative contribution of hydrate dissociation to the total gas production as a function of production times. Compared to the *Holder et al.* [1982] results,

our simulation indicates a much higher contribution of dissociated gas in Case 1 (which corresponds to the *Holder et al.* [1982] conditions). The difference is attributed to the fact that in our model a gas phase emerges in the hydrate zone, which keeps expanding as the dissociation continues and the released water drains. Additionally, the water released through decomposition occupies a volume 13% smaller than the corresponding hydrate, thus further increasing  $S_g$ . In Case 2, the cumulative contribution of dissociated gas is higher due to the higher permeability to gas movement.

Figure 3 shows the vertical temperature profiles at a distance  $r = 0.15$  m from the wellbore. In Case 1, the maximum temperature decrease is 8.23 K, occurs at  $z = -14.6$  m, i.e., 0.4 m above the initial interface, and is significantly larger than the 1.2 K drop reported by *Holder et al.* [1982]. We believe that the differences are due to the reasons mentioned above, as well as to the much finer discretization in the vicinity of the well bore. In case 2, the maximum temperature decrease is 7.11 K and occurs 0.6 m above the initial interface. The differences between cases 1 and 2 are attributed to the higher gas permeability in Case 2.

Figure 4 shows the evolution over time of the pressure at the wellbore gridblock immediately below the initial interface (at  $r = 0.05$  m and  $z = -15.05$  m). The pressure in Case 1 is lower than the *Holder et al.* [1982] results, but the difference is rather small. It appears that the reason for the similarity of the answers is that the finer discretization and higher dissociation in our model produce roughly the same results as the coarser discretization and lower dissociation of the *Holder et al.* [1982] model. The pressures in Case 2 are larger than those in Case 1 due to the higher permeability (and, consequently, the higher hydrate dissociation) of the gas phase.

### 3.2. Test Problem 2

Test Problem 2 involves the depressurization-induced release of  $\text{CH}_4$  in a reservoir of  $\text{CH}_4$  hydrates and salt water (no free gas phase), i.e., under conditions of ocean sediments. The distribution of water and hydrate was uniform throughout the reservoir, with initial  $S_w = S_s = 0.5$  and  $S_g = 0$ . The reservoir dimensions, properties, and the initial conditions were the same as in Problem 1. The properties of fresh water were used in this simulation, but the effect of salt on the hydrate dissociation as accounted for. Fluids were produced by

setting the pressure at the wellbore gridblock at  $z = -14.95$  m, i.e., immediately above the interface, constant at  $1.7237 \times 10^7$  Pa (2500 psi), and were distributed in the production stream according to their mobilities.

The cumulative gas production over time (shown in Figure 6) is roughly proportional to the square root of time, and reaches the level of  $4.114 \times 10^7$  m<sup>3</sup> ( $1.453 \times 10^9$  ft<sup>3</sup>) after a year of production. The reason for this high level of production appears to be the very high compressibility of water. The temperature distribution along  $z$  at  $r = 0.15$  m (Figure 7) tends to support this thesis, as the temperature decrease is larger and more extended than in Problem 1. Although this is a simplified example, the results are encouraging for CH<sub>4</sub> production from hydrates in ocean sediments.

### 3.3. Test Problem 3

Test Problem 3 simulates the release of CH<sub>4</sub> through a thermal stimulation process in a reservoir of CH<sub>4</sub> hydrates and free CH<sub>4</sub> gas phase, i.e., under permafrost conditions. The problem simulated here is the frontal sweep production system discussed by *McGuire* [1981], which is similar to the steam flooding process in heavy-oil reservoirs. The frontal sweep method involves wells arranged in a *five-spot* pattern (Figure 8). The injected fluid was hot water because the parametric study of *McGuire* [1981] indicated that when steam is injected steam, the amount of produced gas was less than the estimated fuel consumption.

Because of symmetry, only 1/4 of the basic pattern needs to be modeled. The side of the basic square was 500 m, and the thickness of the reservoir was 30.5 m (100 ft). The domain was discretized in  $20 \times 20 \times 20 = 8000$  gridblocks in  $(x, y, z)$ , resulting in a uniform gridblock size of 25 m  $\times$  25 m  $\times$  1.525 m and a total of 24000 equations (equilibrium model). The injection well was completed in the bottom half of the reservoir, while the production well was completed in the top half. The reservoir porosity was 0.25, and initially  $S_g = 0.6$  and  $S_w = 0.4$ . All other reservoir properties and the initial pressure and temperature were the same as in the Test Problem 1. It was not possible to simulate the problem as described by *McGuire* [1981] because in his approach the porous medium and its effects on flow were neglected.

Water at 333.15 K was injected at a rate of  $0.055$  kg  $s^{-1}$  at the injection well. This injection rate is the same with the one used in the *McGuire* [1981] study. Figure 9 shows

the cumulative CH<sub>4</sub> production over a year of injection and gas production. At the end of the year, the amount of produced CH<sub>4</sub> ( $2.36 \times 10^7 \text{ m}^3$ ) is substantially smaller than the *McGuire* [1981] estimate ( $4.96 \times 10^7 \text{ m}^3$ ) for the same injection temperature. This was expected because the *McGuire* [1981] model was not a porous medium model and did not take into account the resistance to flow that the hydrates present [*Holder et al.*, 1984]. Thus, the *McGuire* [1981] predictions were highly optimistic. The produced gas, however, is well above the ( $1.41 \times 10^7 \text{ m}^3$ ) level necessary to cover the fuel consumption for heating the injected water

Figure 10 shows the temperature distribution along the line connecting the producing and injection well at  $z = -16 \text{ m}$  from the reservoir top at  $t = 1 \text{ year}$ . The curve exhibits a regions of temperature decline associated with the advancing hot water front. A second region with declining temperatures below the initial temperature level is evident in the vicinity of the production well, and is attributed to the inevitable depressurization process as fluids are withdrawn.

#### 4. Summary and Discussion

We developed EOSHYDR, a new module for the TOUGH2 general-purpose simulator for three-dimensional, multi-component, multiphase fluid and heat flow and transport in the subsurface. EOSHYDR is designed to model the non-isothermal CH<sub>4</sub> release, phase behavior and flow under the conditions of the common methane hydrate deposits (i.e., in the permafrost and in deep ocean sediments) by solving the coupled equations of mass and heat balance. As with all other members of the TOUGH2 family of codes, EOSHYDR can handle multi-dimensional flow domains and cartesian, cylindrical or irregular grids, as well as porous and fractured media.

In EOSHYDR both an equilibrium and a kinetic model of hydrate formation or dissociation are included. Two new solid phases are introduced, one for the CH<sub>4</sub>-hydrate and the other for ice. Under equilibrium conditions, water and methane, as well as heat, are the main components. In the kinetic model, the solid hydrate is introduced as the fourth component. The mass components are partitioned among the gas, liquid and the two solid phases. The thermodynamic phase equilibrium in EOSHYDR is described by the P-T-X

diagram of the H<sub>2</sub>O - CH<sub>4</sub> system. Phase changes and the corresponding heat transfers are fully described. The effect of salt in pore waters on CH<sub>4</sub> solubility and on the growth and decomposition of gas hydrates is also taken into account. The current model does not account for the effects of dilution of the salty water on hydrate inhibition and dissociation (a potentially important issue in the injection of hot brines for inhibitor-induced dissociation), but this could be accomplished rather easily by the addition the salt mass balance equation.

Although EOSHYDR has the ability to model kinetically-controlled hydrate dissociation, only the equilibrium model was used in the three tests conducted in this study because of lack of the necessary parameters. The first test involved CH<sub>4</sub> production from a stratified reservoir of CH<sub>4</sub>-hydrate and free CH<sub>4</sub> gas through a depressurization process under permafrost conditions with zero and non-zero initial gas saturation in the hydrate zone. The second test modeled depressurization-induced CH<sub>4</sub> production from a reservoir of CH<sub>4</sub>-hydrate and salt water (uniformly distributed) under oceanic conditions. The third test modeled the thermal stimulation process of the frontal sweep system, which involved injection of hot water to dissociate CH<sub>4</sub> in a CH<sub>4</sub>-hydrate and water reservoir.

The results of the tests tend to indicate that CH<sub>4</sub> production from CH<sub>4</sub>-hydrates is technically feasible and has significant potential. Both depressurization and thermal stimulation seem to be capable of producing substantial amounts of CH<sub>4</sub> gas. Although the depressurization method appears to have an advantage over the thermal stimulation process, it is not possible to render a definitive judgement because of the dearth of information on the properties of hydrate reservoirs and their thermodynamic behavior. There are practically no reliable measurements of the permeability, porosity and saturation of natural hydrate deposits, while the understanding of the kinetic behavior of hydrates is at a very early stage of advancement [Sloan, 1998]. The enormity and potential of this resource clearly demands evaluation, and numerical studies are a powerful and efficient way to accomplish this. While the current data on hydrates allow the determination of the model sensitivity to inputs and the relative importance of the various reservoir and production parameters, data representative of reservoir conditions must be obtained to render models sufficiently robust for practical applications.

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<b>Table 1. Reservoir characteristics and properties</b>	
<b>Parameter</b>	<b>Value</b>
Gas zone thickness	50 m
Hydrate zone thickness	50 m
Initial pressure $P_0$	$2.07 \times 10^7$ Pa
Initial temperature $T_0$	293.43 K
Gas composition	100% CH <sub>4</sub>
Permeability $k$	$4.3425 \times 10^{-14}$ m <sup>2</sup>
Gas production rate $\hat{q}_m$	$0.82$ m <sup>3</sup> s <sup>-1</sup>
Thermal conductivity	$1.5$ W m <sup>-1</sup> K <sup>-1</sup>
Thermal diffusivity	$7 \times 10^{-7}$ m <sup>2</sup> s <sup>-1</sup>

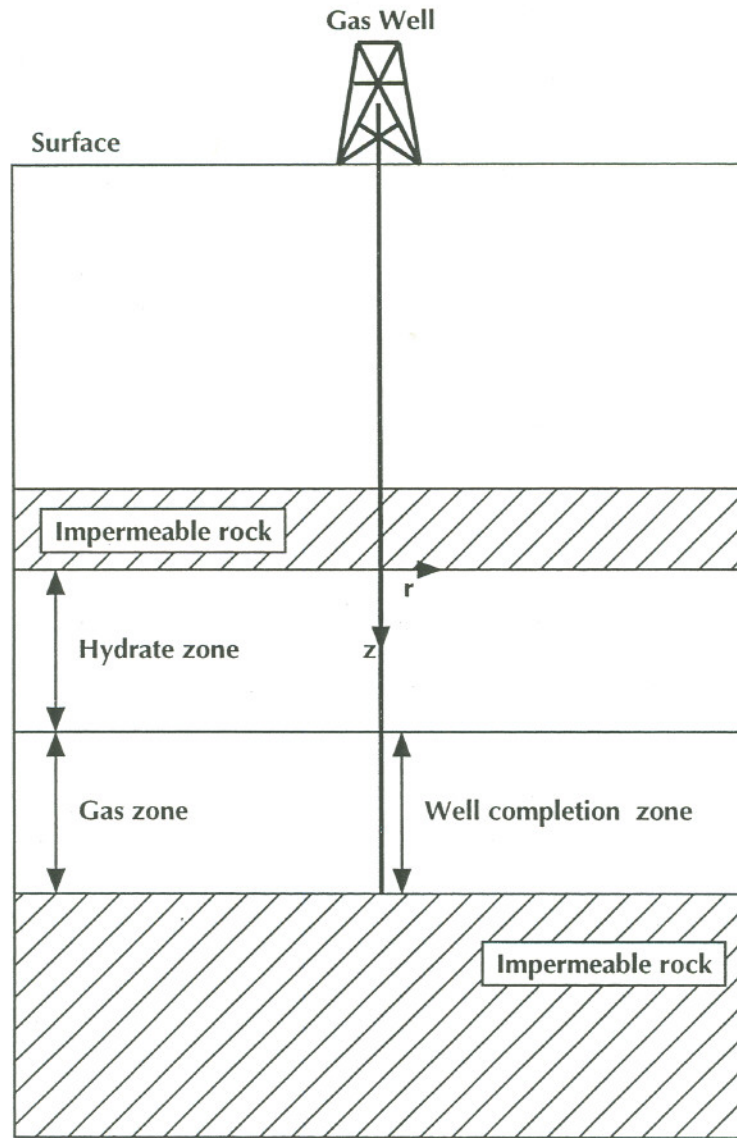
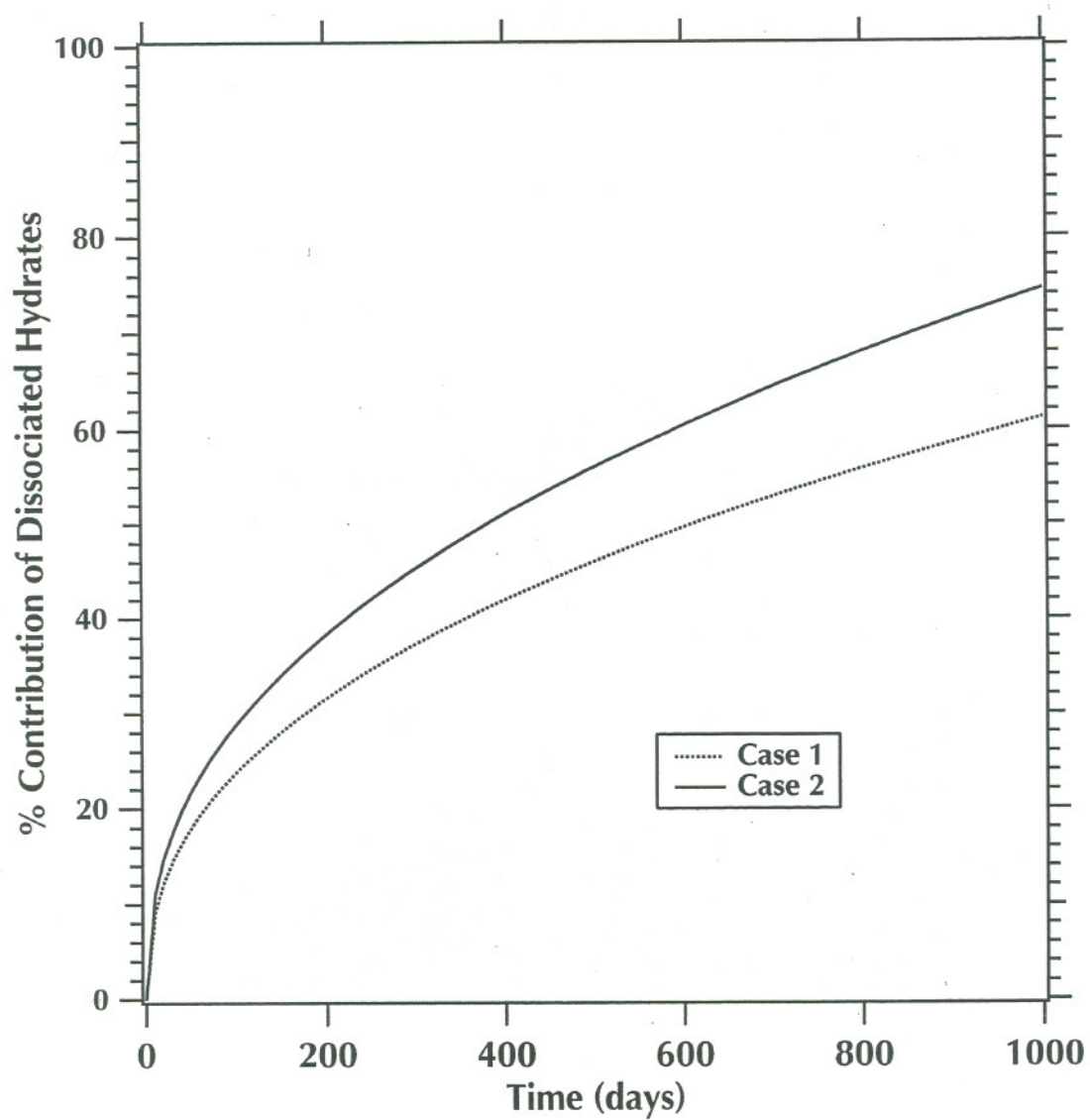


Figure 1. The reservoir configuration in Test Problem 1.



**Figure 2.** Cumulative contribution of  $\text{CH}_4$  dissociated from hydrates to the total gas production in Test Problem 1.

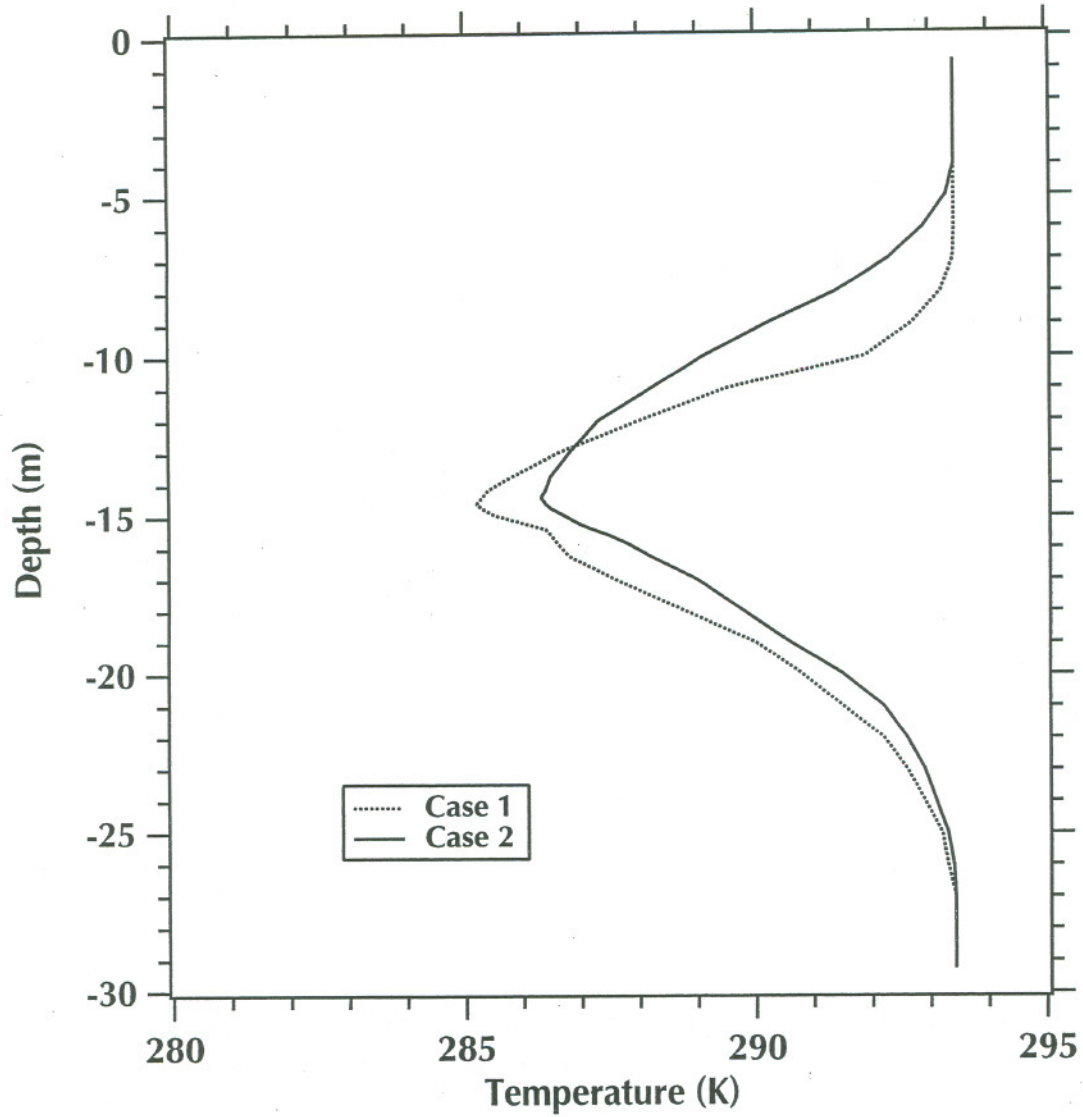
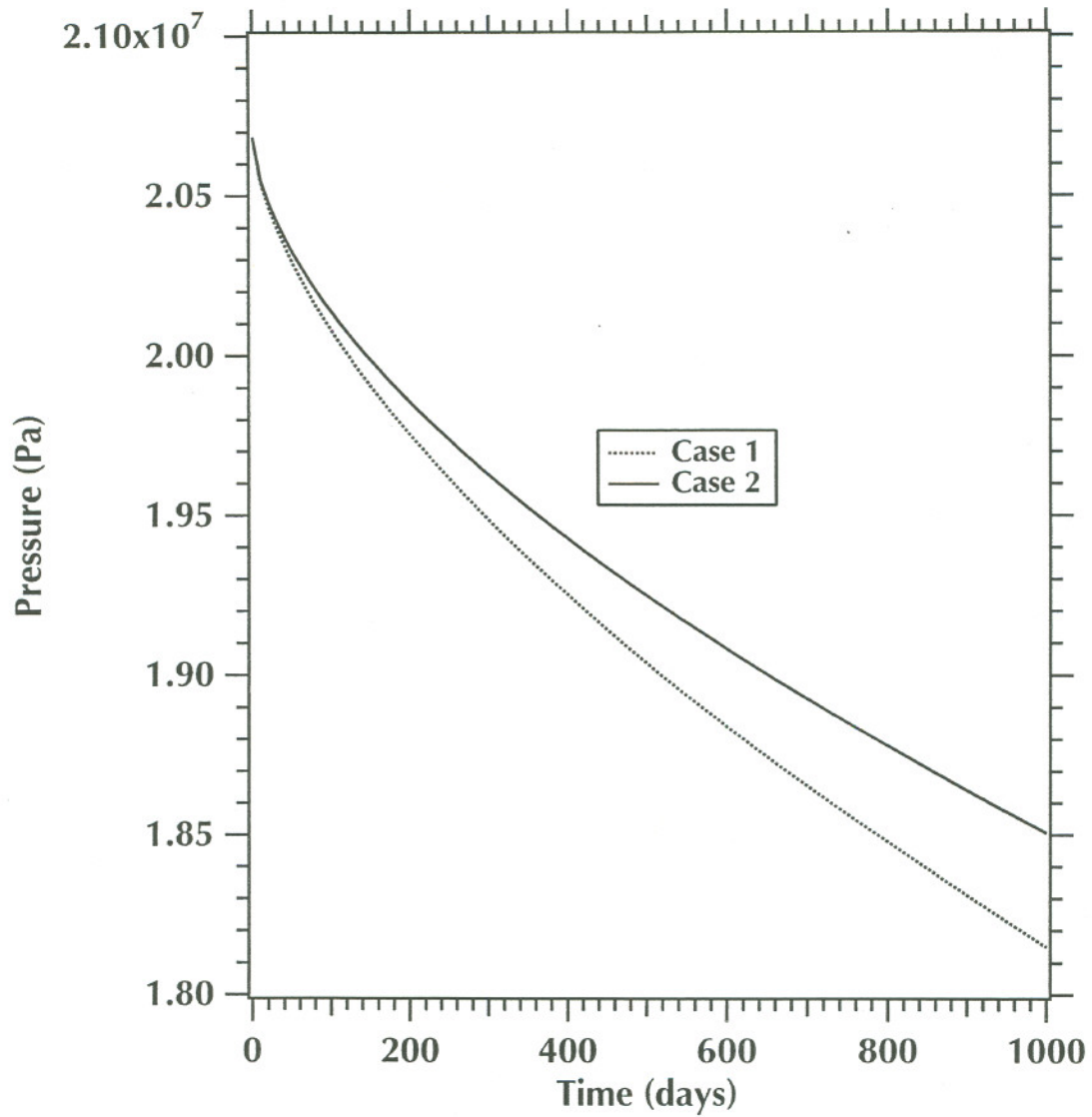


Figure 3. Vertical temperature distribution at  $r = 0.15m$  in Test Problem 1.



**Figure 4.** Test Problem 1: Pressure vs. time at the wellbore gridblock located at  $r = 0.05$  m,  $z = -15.05$  m.

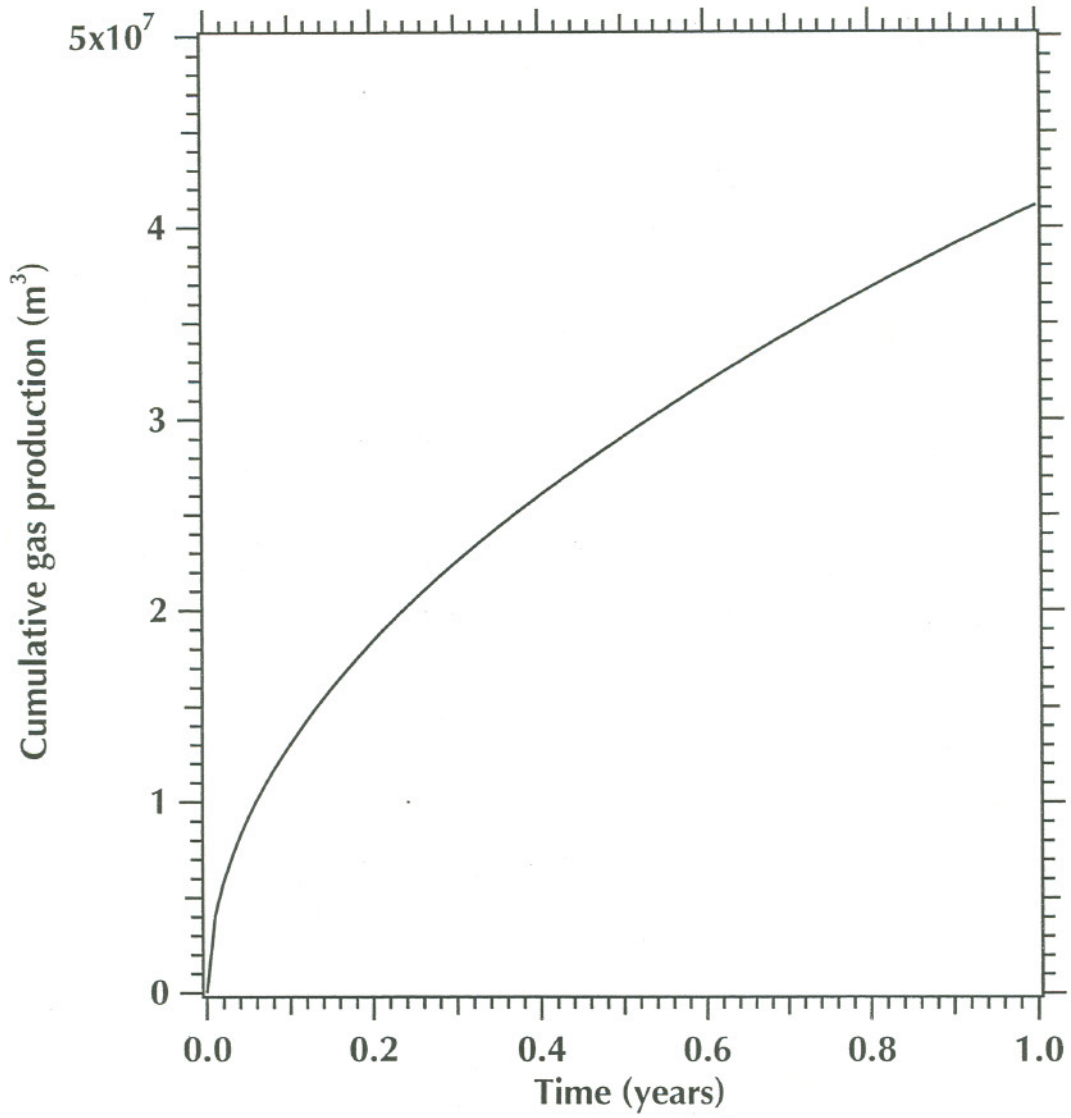


Figure 5. Cumulative CH<sub>4</sub> production at  $t = 1$  year in Test Problem 2.

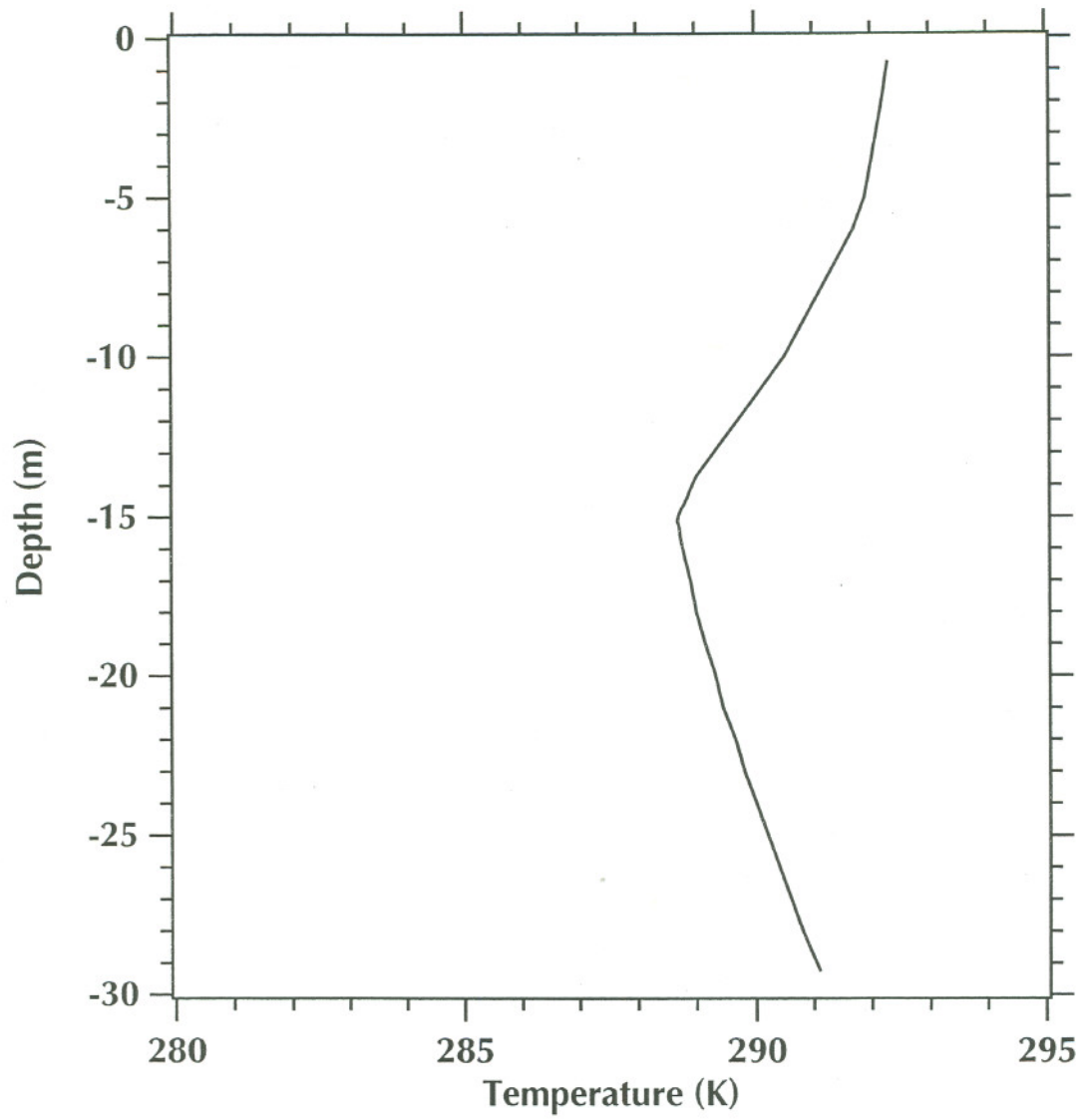
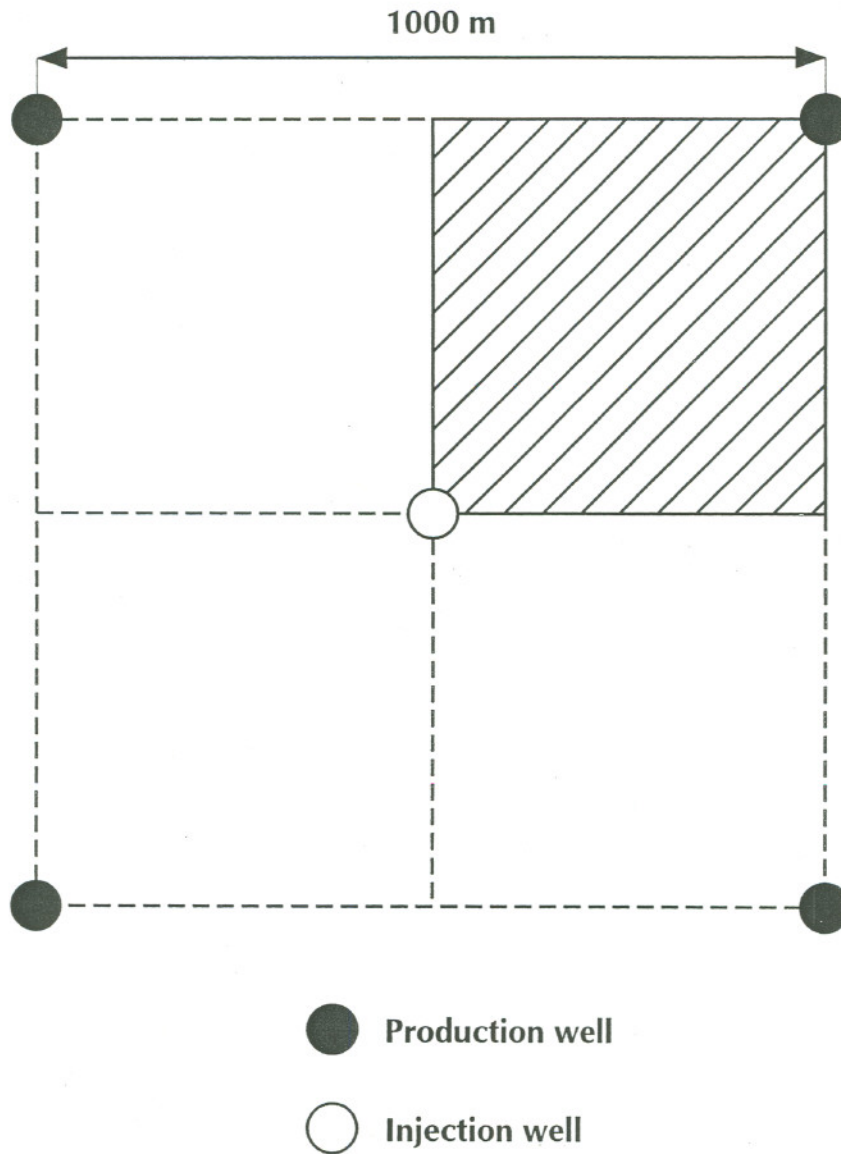
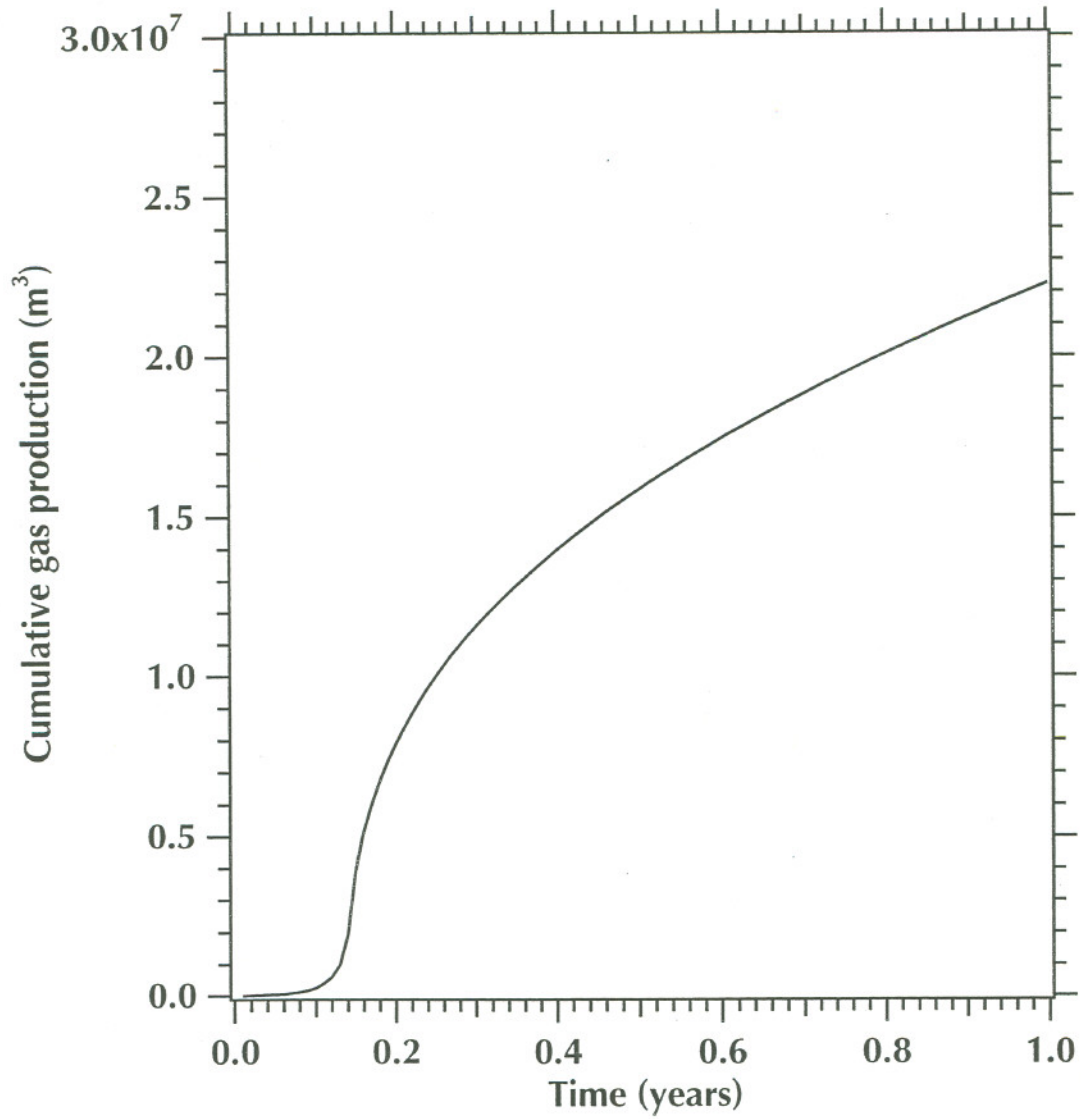


Figure 6. Vertical temperature distribution at  $r = 0.15m$  in Test Problem 2.

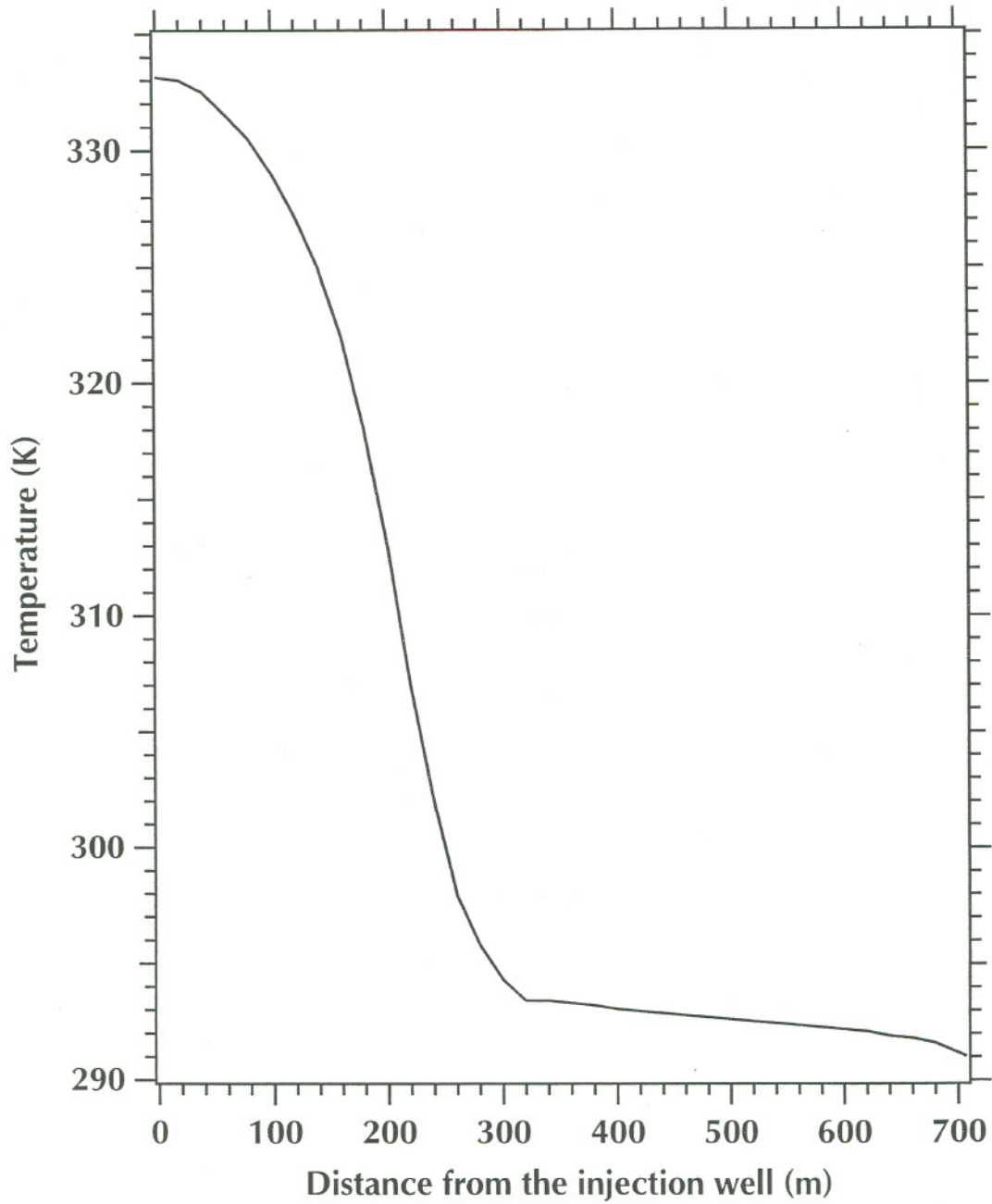




**Figure 7.** Five-spot well pattern for modeling a 1/4 symmetry subdomain in the frontal sweep problem.



**Figure 8.** Cumulative CH<sub>4</sub> production at  $t = 1$  year in Test Problem 3.



**Figure 9.** Temperature distribution at  $t = 1$  year and at  $z = -16.03$  m along the axis connecting the injection and the production wells.