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Los Angeles

Substrate Integrated Waveguide Based Metamaterial Components and Novel Miniaturized Planar Antennas

A dissertation submitted in partial satisfaction of the requirements for the degree Doctor of Philosophy in Electrical Engineering

by

Yuandan Dong

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ABSTRACT OF THE DISSERTATION

Substrate Integrated Waveguide Based Metamaterial

Components and Novel Miniaturized

Planar Antennas

by

Yuandan Dong

Doctor of Philosophy in Electrical Engineering University of California, Los Angeles, 2012 Professor Tatsuo Itoh, Chair

Miniaturized microwave components have drawn increased attention due to the size shrinking of the modern communication systems. This dissertation proposes two approaches to address this problem by reducing the size of the RF components and the antennas.

First, miniaturized substrate integrated waveguide components are introduced and developed by using the metamaterial concept. Traditional waveguide components

have excellent performance but with a bulky size due to the above-cutoff frequency operation. We demonstrate that by loading the metamaterial elements, the rectangular waveguide can be operated well below the cutoff frequency while maintaining good performance. Based on the substrate integrated waveguide technology, their wave propagation characteristics are studied and their practical applications for guided and radiated RF/microwave components, including transmission lines, filters, couplers, diplexers, oscillators, and leaky-wave antennas, are proposed and implemented. These devices are substantially miniaturized with superior performance achieved.

Second, various miniaturized planar antennas are developed to meet the industry application requirements. Different techniques, such as the metamaterial resonators, meta-surfaces, multi-layer folded structures, and the shared radiator approach, are adopted to design different antennas which are suitable to be applied in many wireless systems, including the WLAN links, cellular phone systems and ultra-wideband communication systems. Some special antennas, such as dually or circularly polarized antennas, diversity antennas, are also designed for specified applications. These antennas exhibit good radiation performance with a smaller size compared with the conventional planar antennas. Some of them are going to be used in commercial WLAN communication systems.

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The dissertation of Yuandan Dong is approved.

Jean L. Turner

Yuanxun Ethan Wang

Frank M.C. Chang

Tatsuo Itoh, Committee Chair

University of California, Los Angeles

To My Parents and Sister, for their unconditional and unparalleled Love and Support

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Chapter 1

Introduction

This dissertation will be mainly divided into two related topics. The first part is about miniaturizing the microwave substrate integrated waveguide components using metamaterial concept. Microwave/RF components such as transmission lines, filters, diplexer, couplers and oscillators are implemented based on our new proposal. The other part is about miniaturized planar antennas based on metamaterial resonators and some other techniques. These antennas have different features and can be applied in different systems. This introduction would also be separated into two sections giving some background information for the general readers.

1.1 Waveguide-based Metamaterial Structures and Their Applications

Metamaterials, which are broadly defined as artificially-engineered materials that exhibit unusual or difficult to obtain electromagnetic (EM) properties, have spurred a significant research interest over the past decade [1-6]. They are explained in the general context of periodical structures with a periodicity that is much smaller than the guided wavelength. Their exotic properties include negative or low values of permittivity (ε), permeability (μ) and refractive index (n) which are not readily available from conventional materials. These properties have enabled the development of new concepts, devices, and possible utilization in many novel applications [1-6]. For instance,



Figure 1.1 The permittivity-permeability $(\varepsilon - \mu)$ diagram which shows the material classifications. At the intersection (point A) it is the zero-index media.

metamaterials with simultaneously negative permittivity and permeability are referred to as left-handed (LH) materials [1]. By including the right-handed (RH) effects that occur naturally in traditional materials, a more general model has been proposed as composite right/left-handed (CRLH) structures [2], [7]. Strictly speaking, all the practical LH media actually falls under the designation of CRLH materials since their left handedness only hold in a small frequency band. In some scenarios the RH region is just too far away thus not in the region of interest. The classification of materials can be graphically illustrated with the ε - μ diagram shown in Figure 1.1. It should be pointed out that only the doublepositive medium and double-negative medium allow the wave propagation while the single negative materials prohibit the wave transmission. The double-negative medium (LH material) is characterized by anti-parallel phase and group velocities, negative refractive index (NRI), and backward-wave propagation which differs from the RH material. It is also noted that at the intersection of the various types of materials there is the zero-index media as indicated by Figure 1.1. The zero-index metamaterial, due to its infinite wavelength propagation, offers some interesting features and applications which have drawn some special attention in the community [2], [4], [7-9]. Metamaterials have provided the engineers with a means to manipulate the material intrinsic parameters so as to control and utilize the propagation of EM waves.

In this dissertation we mainly focus on the waveguide structures loaded with metamaterial elements, especially their wave propagation characteristics and the practical applications for guided and radiated microwave components. Based on their propagation characters, practical microwave applications based on these waveguide-based metamaterial structures are reviewed and presented. Here we mainly consider the waveguide with TE or TM propagation modes. This introduction mainly discusses their properties from the point of view of materials in terms of the permittivity and permeability. It is noted that they may also have other interpretations from different engineering angles. For instance, we can still analyze them using the equivalent circuits as we did later in the following chapters. We can also use the periodic structures or coupled resonator theory from filter synthesis point of view for analysis and design. These different approaches do not conflict and eventually should achieve the same design purpose and results.

1.1.1 Basic Types of Metamaterial Elements

The most original and well-known LH material was proposed by a group in University of California at San Diego (USCD) [1]. It consists of the split-ring resonators (SRRs) and



Figure 1.2 A summarize of the different metamaterial elements that have been used for metamaterial synthesis. (a) SRRs, which can be considered as equivalent magnetic dipoles, (b) Metal wire lines, which is regarded as electric dipoles, (c) CSRRs, which are considered as equivalent electric dipoles, and (d) slot lines, which can be viewed as magnetic dipoles.

thin copper wires, providing the negative permeability and negative permittivity, respectively. The SRRs behave similarly to the resonant magnetic dipoles which can be excited by an axial magnetic field [10], [11]. Later from a duality argument, complementary split-ring resonators (CSRRs) were introduced by Falcone *et al.* in 2004 as new metamaterial elements and have been proven to exhibit negative permittivity [12]. It is noted that the thin copper wire can be considered as an electric dipole. It also has a dual counterpart, which is the slot magnetic dipole. The slot has been used to synthesize transmission line (TL) metamaterials and provides the LH capacitance instead of the consideration of a magnetic dipole. Essentially they function in the same way and sometimes the slot is meandered in order to increase its effective length. Figure 1.2 summarizes all the above four metamaterial elements which can be considered as two



Figure 1.3 (a) Mushroom structure which consists of coupling slots and vias connected to the ground. It has been demonstrated to be a CRLH structure with a negative refractive index [20]. (b) Planar CRLH structure for composed by interdigital coupling slots and CSRRs on the ground. It has been used for wideband filter applications [21].

pairs of electric and magnetic dipoles.

It is important to bear in mind that both permittivity and permeability are tensors and only one of the tensor components could be thought to be negative for the artificial metamaterials synthesized by elements shown in Figure 1.2. Specifically, for the orientations shown in the figure they can be described as:

$$\overline{\varepsilon} = \begin{bmatrix} \varepsilon_{xx} & 0 & 0\\ 0 & \varepsilon_{yy} & 0\\ 0 & 0 & \varepsilon_{zz} \end{bmatrix} = \varepsilon_0 \begin{bmatrix} \varepsilon_{\rm lr} & 0 & 0\\ 0 & \varepsilon_{\rm lr} & 0\\ 0 & 0 & \varepsilon_{\rm tr} \end{bmatrix} = \varepsilon_0 \overline{\varepsilon}_{\rm r}$$
(1)

$$\overline{\mu} = \begin{bmatrix} \mu_{xx} & 0 & 0 \\ 0 & \mu_{yy} & 0 \\ 0 & 0 & \mu_{zz} \end{bmatrix} = \mu_0 \begin{bmatrix} \mu_{lr} & 0 & 0 \\ 0 & \mu_{tr} & 0 \\ 0 & 0 & \mu_{lr} \end{bmatrix} = \mu_0 \overline{\mu}_r$$
(2)

Here ε_0 and μ_0 are the free space permittivity and permeability whereas ε_{tr} (μ_{tr}) and ε_{tr} (μ_{tr}) stand for the relative permittivity (permeability) in the transversal and longitudinal directions. ε_{tr} and μ_{tr} could be negative for the displayed elements in Figure 1.2.

Most of the available metamaterial structures, except the lumped element type [13] and waveguide-based metamaterials [14-17], are synthesized based on these elements. On the other hand, arbitrarily selecting two of them (one electric dipole and one magnetic dipole) could usually result in a metamaterial realization once they are properly oriented. Specifically, there are four combination methods as shown below:

- A. SRR and Wire dipole: this case is the most original and widely used combination mode [1].
- B. SRR and CSRR: one realizing example using SRR and CSRR is shown in [18].Due to the difficulty in arrangement, this combination mode does not gain much popularity.
- C. Slot dipole and wire dipole: The mushroom structure as shown in Figure 1.3(a) falls into this configuration [19], [20]. The mushroom structure was first proposed in [19] for the realization of high-impedance surfaces. Many papers have investigated this structure using the CRLH TL theory [8], [9]. In essence, the coupling slots can be considered as slot dipoles providing the negative μ , while the vias can be viewed as wire dipoles which exhibit a negative ε .
- **D.** *Slot dipole and CSRR*: One example is shown in Figure 1.3(b) [21]. This combination mode is widely employed in microstrip technology [11].

Note that different configurations listed above could result in varied performances. Generally speaking, the TL metamaterials based on the CRLH theory are capable of providing a wider bandwidth compared with the resonator-type metamaterials. Nevertheless, those structures are considered lossy therefore inefficient. One way to increase the efficiency is to switch to the waveguide structures, which provide a much higher quality (Q) factor.

1.1.2 Waveguide Loaded with Metamaterials

A question arises: why do we choose waveguide structures to apply the metamaterials? One reason as stated above is that waveguide exhibits a high *Q*-factor which could be utilized to design low loss components with a good power handling capability. The second reason is that the waveguide is able to provide negative permittivity when operated below the cutoff frequency of the dominant TE mode [14]. It is well-known that rectangular waveguide can support TE and TM modes with the dispersion constant satisfying the following relation [22]:

$$k = \omega \sqrt{\mu_{\rm r} \varepsilon_{\rm eff}}, \quad \varepsilon_{\rm eff} = \varepsilon_{\rm r} \left(1 - \frac{\omega_0^2}{\omega^2} \right)$$
 (3)

where μ_r and ε_r are the permeability and permittivity of the substrate filling inside the waveguide, and ω_0 is the cutoff frequency for the considered mode. When the waveguide is operated below the cutoff frequency, ε_{eff} becomes negative and k becomes an imaginary number. The resulting mode is an evanescent one where the wave propagation is prohibited. It falls into the ε -negative material corresponding to second quadrant of the ε - μ diagram shown in Figure 1.1. This feature seems to be pointless to normal waveguide applications while it becomes an extremely attractive property under the scenario of metamaterial synthesis. We automatically obtain a uniform ε -negative material without introducing any resonant structures or any additional loss for the frequency range below the waveguide cutoff [14]. It should be pointed out the traditional wire arrays which also



Figure 1.4 SRR-loaded waveguide unit-cell and its features. (a) Configuration, (b) Simulated dispersion and attenuation constant, (c) Calculated effective permittivity and permeability (real part), and (d) Phase response and refractive index (real part). The unit-cell dimension is shown in [14].

follow the Drude model can also be used to achieve a non-resonant ε -negative medium [4] and the use of waveguides below the cutoff is just one of the options which we believe is superior in terms of simplicity and loss.

One perceptual intuition is that the negative permeability is missing and we only need to introduce a negative- μ material in order to simulate an LH metamaterial in waveguide format. Based on this idea, SRRs are inserted into the waveguide which are placed perpendicularly to the magnetic field in order to facilitate the excitation [14], [15]. The configuration of the unit-cell, which was originally proposed in [14], is displayed in Figure 1.4(a). We re-simulated the structure and found a good agreement with the conclusion made in [14]. The propagation curves indicate that there is an LH passband generated around 6.25 GHz where backward-wave propagation can be envisioned as suggested by the dispersion curve. Note that the waveguide cutoff frequency occurs at around 24 GHz. Then we retrieved all the parameters using the simulated S-parameters [22]. It is noted that all the simulation performed here is based on Ansoft's High Frequency Structure Simulator (HFSS) software package. The results are shown in Figure 1.4(b)-(d). The propagation curves shown in Figure 1.4(b) confirm that there is an LH passband generated around 6.25 GHz where backward-wave propagation can be envisioned as suggested by the dispersion curve. It is reminded that the waveguide cutoff frequency occurs at around 24 GHz. The calculated permittivity and permeability (real part) shown in Figure 1.4(c) verifies that it is a double negative material inside the interested frequency range. Figure 1.4(d) plots the phase response and the calculated refractive index (real part) which clearly indicates that it is an NRI material and phase advance (positive phase) occurs in this passband.

Since the CSRR also exhibit negative permittivity, it would be interesting to investigate the case of incorporating CSRRs into the waveguide. Would the combination of two ε negative materials give rise to a ε -positive material? We simulated the unit-cell of this structure which is shown in Figure 1.5(a) [23]. Two CSRRs are face-to-face oriented in terms of the split direction and incorporated on the waveguide surface. The retrieved material parameters are displayed in Figure 1.5(b)-(d). Figure 1.5(b) shows the dispersion curve and attenuation constant which demonstrates that a forward-wave passband below the cutoff is achieved around 4.8 GHz. For this configuration the waveguide cutoff frequency is at about 9.8 GHz. Figure 1.5(c) confirms our assumption that positive permittivity is obtained inside this passband. It is interesting to see that by loading an ε negative material into the waveguide we can manipulate the original material parameters resulting in a forward-wave passband far below the waveguide cutoff, which is very suitable to be utilized for real applications. We can explain this phenomenon in this way: First it is well known that a microstrip line or a parallel-plate waveguide loaded with CSRRs provides an equivalent ε -negative medium [12]. Then we create a waveguide environment and operate it below the cutoff frequency. According to (3), since the original ε_r is negative, the resulting ε_{eff} becomes positive for the frequency below ω_0 . It can also be interpreted in the way that CSRR is able to reverse the permittivity of the original material. Therefore initial ε -negative material below the waveguide cutoff becomes ε -positive after inserting the CSRRs. Figure 1.5(d) plots the phase response and refractive index which indicates that this passband has a negative phase (phase delay) and



Figure 1.5 CSRR-loaded waveguide unit-cell and its characters. (a) Configuration, (b) Simulated dispersion and attenuation constant, (c) Calculated effective permittivity and permeability (real part), and (d) Phase response and refractive index. (Unit-cell parameters: $w_1 = 0.26$ mm, $w_2 = 0.54$ mm, $w_3 = 11.7$ mm, p = 8 mm, l = 3.92 mm, dielectric constant is 2.2, thickness is 20-mil)

positive index. Outside the passband region below the cutoff, it is considered as singlenegative material (ε -negative and μ -positive) corresponding to the stopband. The obtained refractive index, as defined by Eq. (1.4) [2], becomes imaginary and meaningless. It is noted that we still consider this structure for metamaterial applications in such a way we employ a metamaterial structure to engineer the effective material parameters and facilitate the wave propagation which is not easily attainable with traditional technology like the evanescent wave propagation by inserting capacitive non-touching fins or post [25], [26].

$$n = \pm \sqrt{\varepsilon_{\rm r} \mu_{\rm r}} \tag{1.4}$$

Now we discuss the third case where the waveguide is loaded by slot dipoles etched on the top surface. The unit-cell configuration is shown in Figure 1.6(a). In order to increase the effective slot length, we modified the original slot to a meander type slot line. Based on the simulated *S*-parameters, we extracted the dispersion curve and material parameters as shown in Figure 1.6(b)-(d) [27]. Figure 1.6(b) shows that a balanced condition is achieved where the LH region and the RH region are seamlessly connected. Note that this is optimized results. Otherwise a bandgap would appear between the two regions. The attenuation characteristic indicates that a very broad passband is achieved starting from 8 GHz to 14 GHz. The transition frequency is designed to be 10 GHz. Figure 1.6(c) shows the calculated material parameters. The phase response and refractive index are plotted in Figure 1.6(d). It is seen that with the increase of the frequency, the material changes from double-negative medium, to zero-index medium, and finally to double-positive medium.



Figure 1.6 Interdigital slot-loaded waveguide unit-cell and its features. (a) Configuration and its equivalent circuit, (b) Simulated dispersion and attenuation constant, (c) Calculated effective permittivity and permeability (real part), and (d) Phase response and refractive index. (Unit-cell parameters: $w_1 = 0.33$ mm, $w_2 = 0.45$ mm, $w_3 = 8.84$ mm, p = 8.2 mm, l = 3.3 mm, substrate dielectric constant is 2.2, thickness is 20-mil)

In the LH region, phase advance occurs while phase delay happens in the RH region. At the transition frequency, the wavelength goes to infinity. Different from the above two cases, this design is able to offer a very wide operating bandwidth. We can also use the CRLH concept to analyze the structure and the related equivalent circuit is plotted on the right side of Figure 1.6(a) [27], [28]. Its dispersion relation can be determined as [2]:

$$\beta(\omega) = \frac{1}{p} \cos^{-1}(1 - \frac{1}{2}(\frac{\omega_{\rm L}^2}{\omega^2} + \frac{\omega^2}{\omega_{\rm R}^2} - \frac{\omega_{\rm L}^2}{\omega_{\rm se}^2} - \frac{\omega_{\rm L}^2}{\omega_{\rm sh}^2}))$$
(6.5)

where *p* is the length of the unit-cell and:

$$\omega_{\rm L} = \frac{1}{\sqrt{C_{\rm L}L_{\rm L}}}, \quad \omega_{\rm R} = \frac{1}{\sqrt{C_{\rm R}L_{\rm R}}}$$
$$\omega_{\rm se} = \frac{1}{\sqrt{C_{\rm L}L_{\rm R}}}, \quad \omega_{\rm sh} = \frac{1}{\sqrt{C_{\rm R}L_{\rm L}}} \tag{6.6}$$

There are two frequency points that are referred to as the infinite wavelength points $(\beta = 0)$ with a bandgap between them. In the balanced case ($\omega_{se} = \omega_{sh}$) they are equal to each other and the bandgap vanishes. Under this scenario choosing interdigital slot is for the purpose of increasing the LH capacitance.

For the last case of waveguide loaded with wire dipoles, we would just draw a conclusion here. Similarly to the case of waveguide loaded with CSRRs, a forward-wave passband can be generated below the cutoff frequency. The combination of two ε -negative materials leads to a ε -positive operation which enables the wave propagation below the cutoff frequency. The related verification has been presented in [17], [29], where the waveguide miniaturization using wire dipole arrays are proposed. It also gives

a relatively broad passband compared with the CSRR-loaded waveguide structures.

Note that there are also other interpretations for the unit-cells and their related transmission characteristics shown above.For instance, the image parameter method is used for periodic structures [22] and the resonance coupling-related wave propagation method is used for the design of evanescent mode waveguide filters [25], [26]. For the latter, backward or forward waves observed in waveguides below cutoff could be caused by interaction between resonators. As we stated before, these different explanations do not conflict as long as they are consistent and justified.

Finally we also would like to point out that there are still some other metamaterialbased waveguide structures which we did not mention above, for instance, the dielectric resonator based CRLH waveguide structures shown in [30]. Another interesting and important issue we should address is that all of the analysis is based on the TE_{10} mode. When the TM modes are introduced into the waveguide, everything would be reversed and it would provide a μ -negative environment when operated below the cutoff frequency [16]. Under this scenario the electric dipole (such as the CSRRs and wires) loaded waveguide are assumed to offer an LH passband below the cutoff frequency. This is also a potentially rewarding direction for metamaterial application in the waveguide environment.

The metamaterial-based waveguide structures have led to many novel microwave devices and applications. This Chapter 2 and Chapter 3 of this dissertation presents the guided and radiated applications that utilize their unique properties as discussed above. Since traditional rectangular waveguides are bulky, heavy and it is not very realistic to

etch slots on the surface, the substrate integrated waveguide (SIW), which is a new but similar guided wave structure synthesized on the planar substrate with linear periodic arrays of metalized vias, has been chosen in some of the applications discussed below. Exactly like the rectangular waveguide, the dominant mode of SIW is still TE₁₀ mode and it possesses a characteristic cutoff frequency [31], [32]. Half mode SIW (HMSIW), which keeps the half of the field distribution of the dominant TE₁₀ mode, reduces the size of conventional SIW structure nearly by half without deteriorating the performance [33], [34]. Both of them can be fabricated using the PCB process and have many advantageous features such as low cost and easy integration with other circuits.

1.2 Novel Miniaturized Planar Antennas

Here in the second part we will present our research advances on miniaturized planar antennas. Specifically, they can be divided into metamaterial-based small antennas and miniaturized diversity antennas. Due to the space limitation, we only selected some of the antennas shown here.

1.2.1 Metamaterial-Based Small Antennas

Antennas are used to launch energy into free space. Metamaterial-based antennas are a class of antennas inspired by metamaterials to enhance their capability or to achieve novel functions. They can be divided into two categories: leaky-wave antennas (LWAs) and the resonator-type small antennas. For LWAs, guided power leaks away gradually in the form of wave radiation. LWAs implemented by the composite right/left- handed (CRLH) transmission line (TL) metamaterials enable the backward to forward beam

scanning including the broadside radiation which is difficult to realize by conventional LWAs [35-38]. This report will focus on the second category: the metamaterial-based resonator-type small antennas.

A question may arise: what kind of benefits can the metamaterial-based small antennas bring to us? It is well known that small physical size, low cost, broad bandwidth, and good efficiency are desirable features for an integrated antenna. It is also well known that the quality factor (Q) and the radiation loss of the antennas are inversely related the antenna size [39]. Metamaterial-based small antennas are proposed to provide antennas with a means to manipulate the dispersion relation or the near-field boundary conditions, which could result in antenna size miniaturization while maintaining a good radiation performance. Metamaterial antennas open a way to overcome the restrictive efficiencybandwidth limitation for small antennas. Yet this approach is still far from being mature. Many challenges are still there waiting to be solved. This paper reviews the most recent progress in the development of metamaterial-based small antennas. Basically, they can be classified in the following four categories:

- A. CRLH-based or dispersion engineered resonant antennas. This includes the antennas with minus order modes and zeroth order resonators. There are a variety of antennas in this type that have been developed based on the engineered dispersion curves (k- β diagram) [40-50].
- **B.** Miniature antennas based on the metamaterial loadings, such as the Epsilon/Munegative materials [51-54], high permeability shells [55], and the magnetic

photonic crystals (MPC) [56], [57]. The metamaterial-inspired near-field resonant antennas proposed by Ziolkowski are also included here [58-61].

C. Meta-resonator antennas [62-68], particularly for the antennas based on the splitring resonators (SRRs) and complementary split-ring resonators (CSRRs).

Antennas loaded with meta-surfaces [69-78], such as the electromagnetic band gap (EBG) mushroom structures or patch-type reactive impedance surface (RIS). They are able to miniaturize the antenna size, reduce the surface wave as well as to improve the radiation characteristics.

These different techniques will be used for our antennas shown in the Chapters 3-5.

1.2.2 Miniaturized UWB Diversity Antennas

Due to the concept of "internet of everything" in this new information era, diversity antennas for wireless links are receiving more and more popularity. One example is the new smart phones produced by Samsung and Apple. Both of them are using diversity antennas for the receiving channel in order to enhance the signal quality. Diversity antennas are able to improve the reliability of the communication systems by introducing new channels and increasing the capacity of wireless links. They are very good candidates for the efficient use of the limited spectra and spatial resources.

Ultrawideband (UWB) techniques can be applied for diversity applications [79-83]. The combination of the UWB and diversity technologies could enable high data rate and good resolutions, which can be potentially used for imaging, data transfer, localization, and radar application. The initial UWB band authorized by the Federal Communication Commission (FCC) covers the frequency range of 3.1-10.6 GHz. A wide variety of

antennas have been developed to be operated in this range, including both the omnidirectional antennas, such as the monopole-type antennas [84-89], and the directional antennas, such as the Log-Periodic dipole antenna [90], Vivaldi antenna [91], horn antenna, planar quasi-Yagi antenna [92] and cavity backed antenna [93].

Here in this dissertation two planar diversity antennas operating in Ku- (12.4 -18 GHz) and K-band (18 -26.5 GHz) are proposed for ultrawideband (UWB) applications. Both of them consist of a monopole radiating element and two orthogonal feeding ports. Their ground planes are modified and optimized to improve the isolation as well as to control the radiation. The first one is a pattern diversity antenna with a disc monopole patch. The second one is a polarization diversity antenna based on a square patch which is able to provide both linear and circular polarizations. They share the same patch which leads to a big degree of miniaturization. Good radiation efficiency and isolation between the two ports are achieved. Consistent diversity performance is observed across the whole UWB bandwidth which is demonstrated by their radiation patterns.

1.3 Dissertation Outline

The key accomplishments of this dissertation are presented in Chapters 2-6.

In Chapter 2, CRLH SIW and HMSIW TLs and their applications are detailed. Many practical components such as filters, couplers, and leaky-wave antennas are proposed. This part of work has been published on IEEE transactions on AP, IET proceedings, and several top level conferences.

In Chapter 3, SIW loaded by CSRRs are investigated. Their applications to filters, multi-band filters, diplexers, and oscillators are presented. This part of work has been

published on IEEE transactions on MTT, IEEE MWCL, and IET proceedings.

In Chapter 4, CRLH resonator antennas are proposed and discussed. Many different antennas are investigated and presented with both simulated and measured results. This work appears on IEEE transaction on AP.

In Chapter 5, metamaterial resonator antennas based on SRR and CSRR elements are presented separately. This part of work also appears on IEEE transaction on AP.

In Chapter 6, UWB antennas with pattern or polarization diversity performance are proposed and discussed. They are operated in Ku- and K-band. This part of work has been accepted by IEEE transaction on AP.

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Chapter 2

Composite Right/Left-Handed SIW and HMSIW Components

This chapter presents the implementation of composite right/left-handed (CRLH) substrate integrated waveguide (SIW) and half mode substrate integrated waveguide (HMSIW) as well as their applications to various microwave components. They are realized by etching the interdigital slots on the metal surface of the waveguide. Figure 2.1 shows the model of SIW and HMSIW, together with the electric field distribution of the dominant modes, which are TE_{10} and $TE_{0.5, 0}$ modes, respectively. It is known that waveguide has an inherent shunt inductance. The slots etched on the surface act like a series capacitor, which, along with the shunt inductance, creates the necessary condition to support backward waves. Another explanation is that the interdigital slots are considered as magnetic dipoles placed along the H-field direction. By loading these magnetic dipoles a left-handed (LH) passband can be achieved below the waveguide cutoff [1]. Detailed transmission properties for the proposed structures are presented versus the conventional SIW and HMSIW transmission lines (TLs). Then their applications to couplers and filters are investigated. Finally leaky-wave antennas employing the proposed CRLH SIW and HMSIW TLs are designed and discussed, including a design with flexible polarization states. Using the standard PCB process they are fabricated and tested. Measured results are in good agreement with the simulation.



Figure 2.1 (a) The model and (b) the electric field distribution of the dominant modes in the SIW and HMSIW TLs.



Figure 2.2 Configuration of the proposed structures (a) CRLH SIW unit cell (b) CRLH HMSIW unit cell.

2.1 Theory and Implementation of CRLH SIW/HMSIW Unit Cells

Figure 2.2 shows the detailed configuration of the proposed CRLH SIW and HMSIW unit cells. Metallic vias are used to form the electric walls of the waveguide [2]. It is seen that the HMSIW structures keep almost half size compared with that of the full mode SIW. Interdigital capacitors are embedded in the surface of the waveguide. All the structures are synthesized on the substrate of Rogers 5880 with a thickness of 0.508 mm



Figure 2.3 Equivalent circuit models for (a) SIW and HMSIW TLs (b) CRLH SIW and CRLH HMSIW unit cells.



Figure 2.4 (a) Dispersion diagram of the CRLH SIW unit cells. (b) Unwrapped S_{21} phase for the corresponding one- and three-stage CRLH SIW unit cells obtained from HFSS simulation.

and a relative permittivity of 2.2. All the metallic via holes have a diameter of 0.8 mm and a center-to-center spacing of 1.45 mm.

Figure 2.3(a) presents the equivalent circuit model for the original SIW and HMSIW TLs without the slots, which is similar to the traditional rectangular waveguide [3]. The metal surface and the ground can be modeled as a two-wire TL with distributed series inductance and distributed shunt capacitance which are associated with the permeability

and permittivity of the substrate, respectively. It is important to bear in mind that the input impedance of a short circuited stub (via-walls) after a piece of TL appears as inductive. Figure 2.3(b) depicts the circuit model of the unit cells shown in Figure 2.2(a) and (b), which are symmetrical. The interdigital capacitor has been introduced into the model as $C_{\rm L}$. $L_{\rm L}$ represents the inductance generated by the via-walls. They correspond to the LH contribution. Right-handed (RH) contribution contains the distributed shunt capacitance C_R and L_R , which are made by the distributed series inductance from the waveguide and the parasitic inductance from the fingers. Flexible shunt inductance value $L_{\rm L}$ can be obtained by choosing different waveguide widths, which would also lead to the change of the waveguide cutoff frequency. By changing the slot width and length, the value of the series capacitor $C_{\rm L}$ can be adjusted conveniently, which will determine the position of LH region. When $C_{\rm L}$ is large, the LH band will move to a lower frequency thus a band gap will be generated between the LH and RH ranges. Figure 2.4 (a) presents the dispersion diagram for the CRLH SIW unit cell with parameter values shown below the figure. It is found that decreasing the slot width and increasing of its length, which mean the reduction of $C_{\rm L}$ value, will ultimately move down the LH propagation passband. However the RH region is not affected thus the band gap is created, which is called "unbalanced". The balanced case appears when the following relation is satisfied [4]:

$$L_{\rm R} \times C_{\rm L} = L_{\rm L} \times C_{\rm R} \tag{2.1}$$

Backward wave propagation phenomenon can be observed from Figure 2.4(b) in which the unwrapped phase variations of S_{21} for different number of balanced CRLH SIW cells



Figure 2.5 (a) Simulated S_{21} for the three-stage balanced and unbalanced CRLH SIW TLs compared with the SIW TL in the same dimension. (b) Simulated S_{21} for the three-stage balanced CRLH HMSIW TL compared with the HMSIW TL in the same dimension.

are depicted. It is clearly seen that positive phase (phase advance) exists in the LH region while negative phase (phase delay) corresponds to the RH characteristic. The figure also indicates that for the increase of stages, phase advance is also magnified in the LH region, confirming that the physically longer waveguide appears being electrically shorter.

2.2 CRLH SIW/HMSIW Transmission Lines

Figure 2.5 (a) shows the simulated results for the different three-stage CRLH SIW TLs, which are compared with the conventional SIW TL sharing the same waveguide parameter values but without the slots on surface. It is clearly seen that the transmission characteristics have been significantly changed due to the capacitive slots etched on the waveguide surface. The LH components provide an extra backward wave passband well below the cutoff frequency of the original SIW for the unbalanced case. For the balanced



Figure 2.6 Photograph of the fabricated CRLH TLs.

case, the LH and RH components contribute to a seamless transition and the passband has been substantially extended toward the low frequency along with a steeper cutoff transition. Figure 2.5 (b) presents the simulated results both for the three-stage balanced CRLH HMSIW TL and the corresponding HMSIW TL with the same waveguide dimension. It is seen that the starting frequency of passband has been reduced from 7 GHz to 4.3 GHz. Also, a positive phase response is observed in the LH region. However a narrow stopband at about 7.8 GHz in the RH region is also detected in the simulation. By investigating the field distribution we find it is mainly caused by the parasitic resonant behavior of the interdigital fingers.

To verify the simulated results of the proposed structures, the balanced three-stage CRLH SIW and HMSIW TLs are fabricated and tested. The corresponding SIW and HMSIW TLs are also fabricated and measured for comparison. Figure 2.6 shows the photograph of the fabricated CRLH SIW and HMSIW TLs which appear relatively compact. The design parameters are shown in [2]. Figure 2.7 presents the measured


Figure 2.7 Measured *S*-Parameters for the fabricated TLs (a) CRLH SIW and the corresponding SIW TLs, (b) CRLH HMSIW and the corresponding HMSIW TLs.

transmission results of the CRLH SIW and HMSIW TLs, compared with measured results of the SIW and HMSIW TLs. Basically the results are consistent with simulation, while the discrepancy is mainly caused by over-etching, which leads to the increase of the slot widths and the decrease of the interdigital capacitor values. It is seen the passband of the waveguide has been extended to a lower frequency without changing the waveguide size (for SIW from 7.4 GHz to 4.8 GHz and for HMSIW form 7.1 GHz to 4.7 GHz). However the transmission responses in high frequency are also affected to some degree. Three poles are observed below the cutoff frequency. Actually they are created by the three cells which indicate the three modes resonated at the LH region.

2.3 Backward Wave Directional Coupler Using CRLH HMSIW TLs

To further demonstrate their novel characteristics, a 3-dB backward wave directional



Figure 2.8 Backward-wave directional coupler based on CRLH half-mode SIW TL. (a) Photograph of the fabricated component, (b) electric field distribution, and (c) measured S-parameters.

coupler is investigated based on the CRLH HMSIW TLs. Its configuration and electric field distribution at the operating frequency is shown in Figure 2.8(a) and (b) [2]. It is organized by two pieces of CRLH HMSIW TL placed symmetrically along the open side with a small gap. Normally HMSIW TLs with similar configurations can only provide weak coupling. This coupler is operated in its LH region. The electric field distribution shown in Figure 2.8(b) gives us a better understanding on how it works. Clearly backward wave coupling is achieved. It is seen that the slots play an important role in the coupling. It is also important to note that only three stages are used to realize a 3-dB

coupler. By adopting more stages, arbitrary coupling is expected to be obtained. Figure 2.8(a) shows the photograph of this fabricated coupler. The measured results for the backward wave directional coupler are shown in Figure 2.8(c). The measured insertion loss is around -4.05 dB. The measured directivity is approximately 15 dB and it can be operated from 5.5 GHz to 5.9 GHz

2.4 Dual-Band Rat-Race Coupler Based on the CRLH HMSIW TLs

The proposed CRLH HMSIW TL can also be used to synthesize a dual-band rat-race coupler [5]. Figure 2.9(a) shows the original configuration of the CRLH HMSIW unit cell. Figure 2.9(b) shows the curved unit cell obtained from the CRLH HMSIW unit cell displayed in Figure 2.9 (a) by bending it towards the shorted boundary. Figure 2.9(c) shows the rat-race coupler with four ports composed of six unit cells. The transition shown in Figure 2.9(c) provides impedance conversion in order to improve the matching and facilitate the measurement. This coupler is built on the substrate of Rogers 5880 with a thickness of 0.508 mm and a relative permittivity of 2.2. All the metallic via holes have a diameter of 0.8 mm and a center-to-center spacing of 1.45 mm.

Figure 2.10(a) presents the dispersion diagram for the CRLH HMSIW unit cell. Apparently this is an unbalanced case. It is found that one particular phase shift corresponds to two different frequencies located in the LH and RH regions, respectively. Backward-wave propagation phenomenon can be observed from Figure 2.10(b) in which the unwrapped phase variations of S_{21} for different numbers of the CRLH HMSIW unit cells are depicted. It is clearly seen that positive phase (phase advance) exists in the LH



Figure 2.9 Configuration of the proposed CRLH structures (a) Original CRLH HMSIW unit cell, (b) Curved CRLH HMSIW unit cell, and (c) Rat-Race dual-band coupler [5].

region while negative phase (phase delay) corresponds to the RH characteristic. It should be noted the phase variation is not very smooth in the LH region for the three-stage case because of the resonance phenomenon created by the three cascaded unit cells instead of a periodic boundary condition.

Figure 2.11 indicates the phase states under different operations of the rat-race coupler shown in Figure 2.9(c). The hybrid ring can be used for 180°-out-of-phase operation and in-phase operation. In the RH region, the working principle is the same with the conventional rat-race couplers where phase delay happens. Here we give an explanation on how the LH band works. In the case of 180°-out-of-phase operation, port 1 (the



Figure 2.10 (a) Dispersion diagram of the CRLH HMSIW unit cell as shown in Figure 2.9(a). (b) Unwrapped S_{21} phase for the corresponding one- and three-stage CRLH HMSIW TLs obtained form HFSS simulation.



Figure 2.11 Operating schemes of the dual-band rat-race coupler (a) 180°-Out-of-phase case and (b) In-phase case.

difference port) is applied with a signal which separates evenly into two parts. One part arrives at port 2 with 90° phase advance and the other part reaches port 4 with 270° phase advance. Port 3 receives signals from the two parts with the same amplitude but 180°



Figure 2.12 Photograph of the fabricated couplers based on the CRLH HMSIW (left) and HMSIW (right) TLs.

phase difference. Thus outputs with 180°-out-of-phase are obtained at port 2 and 4, while port 3 is isolated. In the case of in-phase operation, a signal applied to port 2 (the sum port) divides evenly into two parts. One part arrives at port 1 with 90° phase advance, and then reaches port 4 with 360° phase lead. The other part arrives at port 3 with 90° phase lead, and then reaches port 4 with 180° phase advance. Thus, in-phase outputs are obtained at ports 1, 3 while port 4 is isolated. Dual-band operation is automatically achieved by combining the RH and LH regions.

To verify our theoretical prediction, two couplers based on the HMSIW and CRLH HMSIW TLs are fabricated and tested for comparison. Rogers 5880 with a thickness of 0.508 mm is adopted as the substrate. Figure 2.12 shows the photograph of the fabricated components.

Figure 2.13 shows the simulated and measured results for the HMSIW rat-race coupler. Figure 2.13(a)-(d) are the simulated and measured S-parameters for the in-phase and outof-phase cases. The simulated and measured phase balances are plotted in Figure 2.13(e) and (f). It is found that good matching and isolation are obtained. The measured center



Figure 2.13 Coupler response base on the HMSIW TLs. (a) Simulated out-of-phase *S*-parameters, (b) Simulated in-phase *S*-parameters (c) Measured out-of-phase *S*-parameters, (d) Measured in-phase *S*-parameters, (e) Phase difference in the out-of-phase case, (f) Phase imbalance under the in-phase condition.

frequency for the out-of-phase case is 7.55 GHz with a fractional bandwidth around 7.8% with the amplitude imbalance in-between ± 0.5 dB. In this frequency range the phase differences between the outputs is $164^{\circ} \sim 194^{\circ}$ for the out-of-phase case and $-5.1^{\circ} \sim 4.6^{\circ}$ for the in-phase case.



Figure 2.14 The response of the coupler base on the CRLH HMSIW TLs for the 180°-out-ofphase case. (a) Simulated *S*-parameters, (b) Measured *S*-parameters, and (c) Phase difference.

Figure 2.14 shows the simulated and measured results of the proposed dual-band coupler for the case of 180°-out-of-phase power splitting. The measured results show that the center frequencies for the two bands are located at 4.425 GHz and 7.06 GHz,



Figure 2.15 The response of the coupler base on CRLH HMSIW TLs under in-phase condition. (a) Simulated *S*-parameters, (b) Measured *S*-parameters, and (c) Phase difference.

respectively. The bandwidth for the amplitude imbalance less than ± 0.5 dB is 3.65% and 7% for the two bands. In these two bands the ranges of the phase difference between the two outputs are $-194^{\circ} \sim -171^{\circ}$ and $168^{\circ} \sim 191^{\circ}$. The average magnitude at the two outputs

is 3.9 dB in the low band and 3.8 dB in the high band. Both the return loss and isolation are below -30 dB.

Figure 2.15 shows the dual-band coupler performance under the in-phase condition. The phase imbalance varies from -5.5° to 6.14° for the LH band and $-7.1^{\circ} \sim 7.3^{\circ}$ for the RH band. The average insertion loss at the two outputs is 3.88 dB in the low band and 3.70 dB in the high band. The measured return loss and isolation are better than 25 dB.

2.5 Miniaturized Filters based on SIW Negative Order Resonance

A family of waveguide filters base on the negative order resonances are investigated and presented in this section [6]. First the unit-cell is studied and then its application to second-, third-order filters is discussed and verified.

2.5.1 Characterisation of the Negative-Order Resonance

In order to reduce the size of the unit-cell shown in Figure 2.2(a) and eliminate the zeroth-order resonance, we propose a quarter-wavelength resonator obtained by closing one of the boundaries with vias placed behind the slot. Figure 2.16(a) shows the configuration of the quarter-wavelength resonator. Since the zeroth-order mode has uniform magnitude along the TL, the whole electric field is forced to be null after applying one shorted boundary. Thus the zeroth-order resonance is suppressed. Figure 2.16(b) shows a half-wavelength resonator operated by combining such two quarter-wavelength resonators. Figure 2.17(a) and (b) shows the equivalent circuits for the resonators displayed in Figure 2.16. It is noted that the circuit shown in Figure 2.17(b) is



Figure 2.16 (a) Quasi-quarter-wavelength resonator and (b) A half-wavelength resonator by combining two quasi-quarter-wavelength resonators.



Figure 2.17 Equivalent circuits for (a) the unit-cell shown in Figure 2.16(a); (b) The closed structure shown in Figure 2.16(b); and (c) the CRLH-SIW cavity with input/output shown in Figure 2.18(a).

similar to that of a normal CRLH resonator like the mushroom structure except with two shorted ends. And the field reaches maximum at the center instead of the two ends. It is similar to a capacitor-loaded evanescent-mode cavity [7]. The difference is that this mode has no relation with the dominant TE_{101} mode. For the evanescent-mode waveguide, the working mode is still TE_{10} -like mode and it seems rather that the passband is shifted down by the capacitive posts.

Figure 2.18(a) shows the cavity with the input/output on the two sides together with a normal SIW cavity plotted in Figure 2.18(b) for comparison. They have the same size. By



Figure 2.18 (a) Modified CRLH-SIW cavity with input/output along the *y*-direction, and (b) A normal SIW cavity with an identical size

placing the feed lines at the center along the *y*-direction only the even modes with symmetrical field distribution in respect of the feed line can be excited. The equivalent circuit for the CRLH-SIW cavity shown in Figure 2.18(a) can be roughly represented by the circuit depicted in Figure 2.17(c). It contains a CRLH unit-cell as shown in Figure 2.17(a) which has been demonstrated that the -1st and +1st order resonances would be excited and the 0th order mode will be suppressed [6]. Figure 2.19 shows the simulated transmission responses of equivalent circuit and the two cavities. Figure 2.20 plots the electric field distribution at each resonance frequency for the two cavities. Apparently the third resonance is the original TE_{101} mode of the cavity. The first resonance in the LH region is the expected half-wavelength resonator. The second resonance is a spurious mode of the first mode generated in the *y*-direction, which appears as a one-wavelength resonator. This mode doesn't exist in the lumped circuit as shown in Figure 2.19(a).

The proposed CRLH SIW cavity shown in Figure 2.18(a) exhibits several advantages. First, when operated on the negative half-wavelength resonator, the radiation created by the two slots has opposite directions which cancels each other in the broadside direction. Also the field reaches maximum at the cavity center and is weak along the interdigital



Figure 2.19 Simulated *S*-parameters for (a) The equivalent circuit shown in Figure 2.17(c); (b) Modified CRLH-SIW cavity shown in 2.18(a); and (c) The normal SIW cavity shown in 2.18(b).



Figure 2.20 Electric field distribution observed at the middle of the substrate in x-y plane at (a) 6.267 GHz, (b) 10.151 GHz, (c) 11.77 GHz for the response shown in Fig. 8a, and (d) 11.36 GHz for the response shown in Figure 19(b).

slots. Thus the wave leakage is small and it possesses a relatively high unloaded quality (Q) factor. Second, it is a cavity structure which has little wave leakage from the

boundaries. Third, this cavity is very compact when working on the negative order resonance. This frequency can still be pushed down by increasing the capacitance value of the interdigital slot. It is also noted that there are two transmission zeros which greatly improves the stopband rejection. The first one is obtained from the eliminated zeroth-order resonance. The second one is brought by the spurious mode. This first transmission zero can also be observed in the circuit-model simulation as shown in Figure 2.19(a). It can be controlled by changing the circuit parameters. Apparently this cavity is very suitable for filter design with a compact size and an improved stopband performance.

2.5.2 Filter Application

Two-order and three-order filters are designed and fabricated using the negative order resonance proposed above. Rogers 5880 with a thickness of 1.27 mm, a relative permittivity of 2.2 and a loss tangent of 0.0009 at 10 GHz is used as the dielectric substrate. Figure 2.21 shows a photograph of the fabricated filters. The detailed structure information is presented in Figure 2.22. The coupling between different cavities is inductive coupling which is widely used for waveguide filter synthesis [8]. The filter design starts from the circuit synthesis, which is based on the filter requirements. The detailed are coupling between the filter including the coupling coefficients and external Q-factor can be determined in terms of the circuit elements of a low-pass prototype filter [8]. After determining the required coupling coefficients and external Q-factor, the relationship between the coupling coefficients and physical structures of the filter. Here we use the similar approach as shown in [8] to get the coupling coefficients and external Q-factor.



Figure 2.21 (a) Modified CRLH-SIW cavity with input/output along the *y*-direction, and (b) A normal SIW cavity with an identical size [6].



Figure 2.22 Detailed structure information (a) Two-order filter and (b) Three-order filter. The dimensions are: (a) $c_1 = 7.15 \text{ mm}$, $c_2 = 6.1 \text{ mm}$, $t_1 = 1.3 \text{ mm}$, $t_2 = 0.79 \text{ mm}$, $w_s = 3.9 \text{ mm}$, $d_2 = 0.9 \text{ mm}$, $w_4 = 5.7 \text{ mm}$, l = 3.3 mm, $w_1 = 0.29 \text{ mm}$, $w_2 = 0.3 \text{ mm}$, $w_3 = 10 \text{ mm}$, n = 11, (b) $c_1 = 7.2 \text{ mm}$, $c_2 = 6.16 \text{ mm}$, $t_1 = 1.35 \text{ mm}$, $t_2 = 0.78 \text{ mm}$, $w_3 = 3.9 \text{ mm}$, $m_3 = 9.92 \text{ mm}$, for the outside cavities: $w_4 = 5.7 \text{ mm}$, l = 3.37 mm, $w_1 = 0.29 \text{ mm}$, $w_2 = 0.3 \text{ mm}$, for the inside cavity: $w_4 = 5.7 \text{ mm}$, l = 3.37 mm, $w_2 = 0.27 \text{ mm}$

However, in our case only the slot length and width are changed to adjust the resonance frequency. All the cavities here have the identical size.

Figure 2.23 shows simulated and measured transmission responses for the two-order filter. The measured group delay is also provided. Good agreement is achieved. The small



Figure 2.23 Simulated and measured transmission responses for the two-order filter (a) Narrowband response, (b) Measured wide-band response, and (c) Measured group delay.

discrepancy lies in that an obvious transmission is detected zero in the measurement. The measured minimum in-band insertion loss is approximately 1.59 dB. The measured center frequency and 3-dB bandwidth are 6.11 GHz and 0.4 GHz, respectively. The measured in-band return loss is better than -17.2 dB. The wide band response shown in Figure 2.23(b) indicates that the first spurious band happens around 10 GHz. Below this frequency excellent out-of-band rejection is achieved. The measured group delay shows that the in-band delay is about 1.2 ns which keeps relatively flat.

The simulated and measured transmission responses for the three-order filter are presented in Figure 2.24. Three poles in the passband are clearly observed. The stopband rejection is further improved, which quickly goes below -40 dB. The insertion loss is



Figure 2.24 Simulated and measured transmission responses for the three-order filter (a) Narrowband response, (b) Measured wide-band response, and (c) Measured group delay.

around 1.86 dB. The center frequency is 6.06 GHz and the 3-dB bandwidth is 0.39 GHz. The measured in-band return loss for this filter is better than -15.4 dB. The group delay is around 1.9 ns in the passband.

It is noted that these filters are quite compact. The three-order filter working in *C*-band only bears a size of 32 mm \times 15.7 mm. Since it is operated below the waveguide cutoff, the transverse size is much smaller than the normal SIW filters. We find that the longitudinal length of each cavity is also smaller than the conventional half-wavelength. The reason is that the working mode is totally different from the TE₁₀₁ mode. The improved out-of-band performance is due to the transmission zeros as well as a below-cutoff operation.

2.6 CRLH SIW/HMSIW Leaky-Wave Antennas

CRLH SIW and HMSIW leaky-wave structures for antenna applications are proposed and investigated in this section [9]. Their propagation properties and radiation characteristics are studied extensively. Their backfire-to-endfire beam-steering capabilities through frequency scanning are demonstrated and discussed.

2.6.1 Configurations

A leaky-wave antenna is a radiating TL structure, either in uniform or periodic configurations. In this part, the proposed leaky-wave TLs will be described. All the prototypes are built on the normally used substrate of Rogers 5880 with a permittivity of 2.2, a loss tangent of 0.001 and a thickness of 0.508 mm. The vias used in the models share a common diameter of 0.8 mm and a center-to-center spacing around 1.45 mm.

Figure 2.25(a) and (b) show the configurations of the one period CRLH SIW element, while the prototype of the whole TL with its orientation in the coordinate systems is illustrated in Figure 2.25(c). For the first resonator shown in Fig. 1(a), the slot is etched on the top surface and it is grounded by a solid metallic plane. For the second resonator shown in Fig. 1(b), both the top surface and the ground are incorporated with interdigital slots with a period distance of p. The slots also provide the radiation. As indicated in Figure 2.25(c) the radiation angle of the main beam is straightforwardly determined by:

$$\theta(\omega) = \sin^{-1} \left[\frac{\beta(\omega)}{k_0} \right]$$
(2.2)

which shows that a full space scanning (-90° to 90°) can be achieved if $\beta(\omega)$ varies



Figure 2.25 Configuration of the proposed CRLH SIW leaky-wave structures (a) Single-side radiating element, (b) Double-side radiating element, and (c) Overall antenna prototype.

throughout the range $(-k_0, k_0)$.

Figure 2.26(a) and (b) shows the configurations of the one period CRLH HMSIW element, while their overall transmission line structures with 15 unit cells are depicted in Figure 2.26(c). For the conventional HMSIW, because of the large width-to-height ratio and the metallic via array, only the quasi-TE_{*p*-0.5, 0} ($p = 1, 2 \dots$) modes can propagate in the waveguide [10]. Here the slots are embedded on the waveguide surface, leading to a CRLH HMSIW TL structure. Under this configuration wave can propagate and radiate both below and above the cutoff frequency of HMSIW while still keeping the half mode



Figure 2.26 Configuration of the proposed CRLH HMSIW leaky-wave structures (a) Initial unit cell, (b) Modified unit cell with a folded ground, and (c) Overall HMSIW antenna prototypes.

field distribution. For the second unit cell shown in Figure 2.26(b), another via-wall covered by a strip on the top is placed beside the open boundary of the HMSIW. This viawall is used to reduce the energy leakage from the open boundary. It can be viewed as a folded ground which can miniaturize the transverse size of the HMSIW, as well as restrict the radiation to go to the broadside. These leaky-wave TLs shown in Figure 2.26(c) can be easily mounted on the metal surface.

2.6.2 Model Analysis and Dispersion Relation

A CRLH TL is an artificial TL structure constituted by the repetition of series capacitance and shunt inductance into a host conventional TL medium exhibiting an LH band at low frequencies and an RH band at higher frequencies. Figure 2.3(b) presents the equivalent circuit model for the proposed CRLH unit cell shown in Figure 2.25(a), which



Figure 2.27 (a) Dispersion diagram calculated from driven mode and Eigen-mode simulations for the single-side CRLH SIW unit cell shown in Figure 2.25(a), the parameter values are: $w_1 = 0.33 \text{ mm}, w_2 = 0.45 \text{ mm}, w_3 = 9.2 \text{ mm}, n = 9, p = 8.2 \text{ mm}, l = 3.3 \text{ mm}$; (b) Dispersion curve and *Bloch* impedance obtained using driven mode simulation for the double-side CRLH SIW unit cell shown in Figure 2.25(b), the parameter values are: $w_1 = 0.32 \text{ mm}, w_2 = 0.33 \text{ mm},$ $w_3 = 8.6 \text{ mm}, n = 9, p = 7.45 \text{ mm}, l = 2.6 \text{ mm}$; (c) Dispersion curve using Eigen-mode simulation for the CRLH HMSIW unit cell and modified CRLH HMSIW unit cell shown in Figure 2.26, the parameter values are: $w_1 = 0.27 \text{ mm}, w_2 = 0.36 \text{ mm}, w_3 = 4.1 \text{ mm}, n = 5, p = 9.8 \text{ mm}, l = 3.3 \text{ mm},$ d = 4.4 mm c = 0.6 mm.

is symmetrical. The interdigital capacitor has been introduced into the model as C_L in the center to obtain a CRLH behavior. L_L represents the inductance generated by the viawall. Note that the series slot also plays the role of a radiating element for the leaky-wave antenna. Increasing the width and the length of the slots will make the radiation more efficient. Also bear in mind that increasing the slot width leads to a decrease of C_L while increasing the slot length results in an increase of C_L . Thus enhancing the radiation does not conflict with achieving a balanced case.

The dispersion diagrams for the proposed four unit cells are then investigated in detail by using Ansoft's High Frequency Structure Simulator (HFSS) software package. Usually two approaches are adopted to calculate the dispersion curve for a single unit cell. One is obtained based on the S-parameters from driven mode simulation [11], [12]. The other one is based on the eigen-mode simulation by applying periodic boundary conditions [12]. The Eigen-mode simulation method is more accurate but timeconsuming. To give a comparison, Figure 2.27(a) plots the dispersion curves of a balanced CRLH SIW unit cell using both of the two approaches. A good agreement is obtained. It is also observed from the Eigen-mode simulation that a very small bandgap (0.1 GHz) actually exists between the LH and RH regions. Fig. 2.27(b) presents the dispersion diagram and Bloch impedance obtained from driven mode simulation for a balanced CRLH SIW double-side radiating unit cell. The dispersion curves for an unbalanced CRLH HMSIW unit cell and an unbalanced modified CRLH HMSIW unit cell are shown in Fig. 2.27(c). The main parameter values for these unit cells are shown in the caption. In all of these cases the dispersion curve traverses four distinct regions as frequency increases, named LH-guidance, LH-radiation, RH-radiation and RH-guidance here, where the radiation regions are characterized by a phase velocity larger than the speed of light (airline). For the unbalanced case shown in Figure 27(c), a bandgap region

is generated between the LH and RH regions. By moving the LH region far below the waveguide cutoff, miniaturization can be obtained. In Figure 2.27(a) it is seen that a balanced case is almost achieved with the balancing point located at about 10 GHz, which ensures a seamless transition from the LH to the RH band. It happens when the series resonance frequency and shunt resonance frequency are equal as shown by Eq. (2.1). Under this condition the dispersion relation splits into additive positive linear RH and negative hyperbolic LH terms [4]:

$$\beta(\omega) = \beta_{\rm RH} + \beta_{\rm LH} = \frac{\omega}{p} \left(\sqrt{L_{\rm R}C_{\rm R}} - \frac{1}{\omega^2 \sqrt{L_{\rm L}C_{\rm L}}} \right)$$
(2.3)

where p is the length of the unit cell. This expression exhibits a null at the frequency:

$$f_0 \Big|_{\beta=0} = \frac{1}{2\pi\sqrt{L_{\rm R}C_{\rm L}}} = \frac{1}{2\pi\sqrt{L_{\rm L}C_{\rm R}}}$$
(2.4)

which is the transition frequency shown in Figure 2.27(a). It should be noted that at this frequency group velocity is nonzero despite the infinite phase velocity, which allows leaky-wave broadside radiation.

For a specified antenna design requirement, the width of the waveguide can be first chosen to approximately locate the RH region. Then we determine the size of the interdigital slot to roughly get the LH region. Due to the difficulty in extracting those lumped values (L_L , C_L , L_R and C_R), some numerical optimization is necessary to obtain a seamless transition for a balanced case or a required bandgap for an unbalanced case. It is also noted that the impedance matching should also be taken into account during the design process. However this matching can be designed in the last step using a taper line



Figure 2.28 Losses analysis for the single-side CRLH SIW unit-cell described in Figure 2.27(a).

at the two ends of a leaky-wave antenna [13]. As the *Bloch* impedance shown in Figure 2.27(b), the average value (real part) from 9.5 GHz to 13 GHz is around 36 Ohm, which can be easily matched to 50 Ohm using a taper line. However for the HMSIW type the average *Bloch* impedance is close to 50 Ohm therefore no taper line is used. The different losses for the unit cell are also an important issue. Figure 2.28 presents a loss analysis for the single-side CRLH SIW unit cell. It is seen that compared with the radiation, the other losses are not very significant. By a similar analysis it is found that both the dielectric loss and conductor loss for the HMSIW case are much smaller compared with the CRLH SIW unit cell, which is due to the weaker resonating field because of its one open boundary [14].

2.6.3 CRLH SIW Leaky-Wave Antennas

Here two CRLH SIW leaky-wave antennas are designed and fabricated using the substrate of Rogers 5880 with a thickness of 0.508 mm and a relative permittivity of 2.2. The first leaky-wave antenna is one-side radiating while the second one is a double-side



Figure 2.29 Photograph of the two fabricated CRLH SIW leaky-wave antennas.

radiating antenna which is realized by etching slots on both the top surface and the ground as indicated by Figure 2.25. Figure 2.29 shows the photograph of the fabricated antennas. The full-wave simulation is performed using the CST Microwave studio.

The first antenna has 15 identical elementary cells. The dispersion relation and parameter values for the unit cell have already been presented in Figure 2.27. Fig. 2.30 shows the measured and simulated *S*-parameters of this leaky-wave antenna, which are in good agreement. A satisfactory return loss above 10 dB in the band of interest (from 8.5 GHz to more than 12 GHz) is achieved. The insertion loss is almost below -10 dB, which indicates good leakage radiation. The curve also shows that in the LH region, the radiation is more effective compared with that in the RH region. The discrepancy of S_{21} between the simulation and measurement is due to the increase of reflection, the loss from the SMA connectors and probably the increased conductor loss.

Its CRLH behaviour is verified by the field distribution along the structure as shown in Figure 2.31. In the LH band, the phase and group velocities are anti-parallel, and the wave propagation is backward. At the transition frequency, infinite guided wavelength is observed and there are no field variations. However the group velocity is nonzero $(v_g = \partial \omega / \partial \beta \neq 0)$, thus the wave is still propagating and radiating. In the RH band, the



Figure 2.30 Measured and simulated *S*-Parameters for the one-side radiating CRLH SIW leaky-wave antenna.



Figure 2.31 Electric field distribution at different frequencies for the CRLH SIW leaky-wave antenna. (a) 9.8 GHz in LH region, (b) 10.0 GHz at the transition point, and (c) 12.8 GHz in the RH region.

phase and group velocities are parallel, and the wave propagation is forward. Also note that when the frequency is close to the balanced frequency as shown in Figure 2.31(a), the guided wavelength is larger corresponding to less field variations compared with the case shown in Figure 2.31(c).



Figure 2.32 Simulated 3-D radiation patterns at different frequencies for the CRLH SIW leakywave antenna. (a) 9.2 GHz in LH region, (b) 11.2 GHz in the RH region, and (c) 10.0 GHz at the transition point.

Figure 2.32 shows the simulated 3-D radiation patterns. It is seen that, when the frequency is increased, the main beam moves from the backfire towards the endfire direction. At the transition frequency, the radiation goes exactly to the broadside.

Figure 2.33 and Figure 2.34 show the normalized radiation patterns measured at different frequencies. The E-plane radiation patterns at 8.6 GHz and 9.3 GHz in the LH region are given by Figure 2.33(a). We find that at 8.6 GHz the beam angle θ is about - 70°, very close to backfire. Figure 2.33(b) presents the E-plane radiation patterns in the RH region. It is found that at 12.8 GHz the beam angle θ switches to approximately 60°. Figure 2.34 displays the measured broadside radiation patterns for both the co-polarization and cross-polarization in the E-plane and H-plane. We see that the cross-



Figure 2.33 Measured radiation patterns of the single-side SIW leaky-wave antenna (a) E-plane (x-z plane) in the LH region, (b) E-plane (x-z plane) in the RH region.



Figure 2.34. Measured radiation patterns at the balanced frequency for the single-side SIW leaky-wave antenna (a) In E-plane (x-z plane), (b) In H-plane (y-z plane).

polarization level is very low and is almost negligible.

Figure 2.35 shows the antenna gain response. The simulated radiation efficiency is also plotted in this figure. We find there is a discrepancy around 1.8 dB between the simulated and measured gains. The backfire-to-endfire beam-steering capability by the way of frequency scanning is confirmed with a maximum gain of approximately 10.8 dBi and an average efficiency of 82% for this antenna.

The double-side radiating leaky-wave antenna has a total number of 25 interdigital



Figure 2.35 Gain and the simulated radiation efficiency of the single-side CRLH SIW leaky-wave antenna.



Figure 2.0.36 Measured S-Parameters of the double-side CRLH SIW leaky-wave antenna.

slots etched on the top surface and the ground of the SIW. The simulated and measured transmission response is shown in Figure 2.36. Still a balanced case is realized in order to obtain a continuous beam-steering function. The observed S_{11} and S_{21} are quite low indicating a good matching and a good radiation performance. The connector loss, increased reflection and conductor loss are also responsible for the visible discrepancy of S_{21} .



Figure 2.37 Measured radiation patterns of the double-side radiating CRLH SIW leaky-wave antenna (a) E-plane (x-z plane) in the LH region, (b) E-plane (x-z plane) in the RH region.



Figure 2.38 Measured radiation patterns at the balanced frequency for the double-side SIW leaky-wave antenna (a) In E-plane (x-z plane), (b) In H-plane (y-z plane).

Figure 2.37 shows the measured E-plane radiation patterns in the LH and RH regions, respectively. Figure 2.38 gives the radiation patterns for the co-polarization and cross-polarization at the transition frequency in both the E-plane and H-plane. The E-plane patterns are similar to the inline element arrays while for the latter beam-steering is usually achieved by phase control which requires a complicated feeding network. This antenna has quasi-omnidirectional radiation in H-plane with a low cross-polarization



Figure 2.39 Antenna gain and the simulated radiation efficiency of the double-side radiating CRLH SIW leaky-wave antenna.

level. We also find that the main beam for this antenna is sharper compared with the first antenna. This is due to the reason that the distance between the unit cells on one side is increased for this second antenna, which results in the decrease of the beamwidth according to the array theory. This also explains that the beamwidth in the LH region (at low frequencies) is larger than that in the RH region (high frequencies correspond to a smaller wavelength). Figure 2.39 shows the measured and simulated antenna gains, as well as the simulated radiation efficiency. Its double-side radiating nature would decrease the antenna gain by 3 dB compared with the first antenna in theory. However, this antenna has a larger aperture size with respect to the single-side radiating antenna. Therefore, the observed gain difference between in simulation is only around 1 dB. The measured gain is 2-3 dB lower than that from the simulation.

In both of the above two cases, the measured gain and S_{21} are lower than those obtained from simulation using CST microwave studio. There are several reasons: 1) The conductor loss and dielectric loss in the measurement should be higher than that in the



Figure 2.40 Photograph of the two fabricated CRLH HMSIW leaky-wave antennas.

simulation, especially the conductor loss. The antennas were fabricated by us based on chemical etching and the observed conductor surface is not very smooth which would lead to an increase on the conductor loss; 2) The loss from the SMA connectors is not included in the simulation; 3) The measured gain takes the reflection (S_{11}) and terminated power (S_{21}) in to account; 4) We found that our chamber is not big enough. In the measurement our antennas are located close to the far field region but not exactly in the far field area, especially for the double-side antenna. This would lead to some inaccuracy for the gain measurement. These factors could all cause the decrease of the measured antenna gain.

2.6.4 CRLH HMSIW Leaky-Wave Antennas

Figure 2.40 shows the photograph of the two CRLH HMSIW leaky-wave antennas. They are fabricated using the same substrate at the High Frequency Center of the Electrical Engineering Department in UCLA. They have the same dimensions except that an extra via-wall is placed near the open side for the second antenna (see the modified unit-cell shown in Figure 2.26(b)), which can be viewed as a folded ground and leads to a miniaturization on the transverse size. This via-wall can also reduce the wave leakage from the open boundary, thus improving the gain.



Figure 2.41 Measured and simulated *S*-Parameters for the (a) CRLH HMSIW leaky-wave antenna and (b) Modified HMSIW leaky-wave antenna.

Figure 2.41 shows the simulated and measured transmission responses of the two leaky-wave antennas. They are unbalanced and the dispersion diagrams for the unit cells are shown in Figure 2.27(c). A bandgap region is observed in both the simulation and the measurement for these two antennas. It is important to bear in mind that by changing the slot size and the position of the vias we can easily control the position of the LH band.



Figure 2.42 Measured radiation patterns of the initial CRLH HMSIW leaky-wave antenna (a) Eplane (x-z plane) in the LH region, (b) E-plane (x-z plane) in the RH region, and (c) H-plane (y-z plane) at 10.6 GHz.



Figure 2.43 Measured E-plane (*x-z* plane) radiation patterns of the modified CRLH HMSIW leaky-wave antenna (a) In LH region and (b) In RH region.

Balanced condition can also be obtained by some optimization as shown in [2].

Figure 2.42 shows the measured radiation patterns for the first CRLH HMSIW antenna,



Figure 2.44 Measured and simulated antenna gains of the two CRLH HMSIW leaky-wave antennas.

while Figure 2.43 plots the measured E-plane patterns for the second CRLH HMSIW leaky-wave antenna. Beam scanning capability in E-plane for these two antennas is clearly observed. Since this is an unbalanced case and there is no balanced point which gives broadside radiation, it is difficult to obtain the H-plane radiation patterns which are observed in the *y*-*z* plane. We still give the H-plane pattern measured at 10.6 GHz for the first antenna. It is noted that this measured pattern does not corresponds to the maximum value as indicated by the E-plane pattern shown in Figure 2.42(b). The cross-polarization level is slightly higher compared with the CRLH SIW antennas, which is mainly due to the edge radiation caused by the open boundary.

Figure 2.44 shows the simulated and measured gains, as well as the radiation efficiencies for these two antennas. It is noted that the average radiation efficiency for HMSIW antennas is around 87%, which is higher than that of the CRLH SIW leaky-wave antennas. This is because the HMSIW antennas have less conductor and dielectric losses. Especially at low frequencies, they are less lossy than the SIW [14]. A gain



Figure 2.45 Simulated radiation patterns in terms of gain at 11 GHz for the CRLH HMSIW antennas with varied configurations. (a) Initial design with the ground extension d = 4.4 mm, (b) Initial design with the ground extension d = 1.0 mm, and (c) Modified design with c = 0.4 mm.

decrease around 2 dB is also observed in the measurement compared with the simulation. We also find that the gain for the second antenna with the modified structure is a little larger than the gain of the first one, although the second antenna has a smaller ground. To explain this difference, Figure 2.45 plots the simulated patterns in y-z plane viewed towards –x direction with varied ground conditions. It is found that when the ground extension from the open boundary of HMSIW is small (c is small), the antenna has a low gain as the case shown in Figure 2.45(b). However, when the extended ground is larger (c is large), the gain is increased as shown in Figure 45(c).

Fig. 2.46 shows a parametric study about the peak gain for the antennas with different ground configurations. It is observed that if the ground extension at the open side of the


Figure 2.46 Simulated antenna gains for the two CRLH HMSIW leaky-wave antennas with varied ground configurations.

HMSIW antenna is very small, the edge leakage is substantial resulting in a small gain. To reduce this undesired radiation a large ground is required. However, we can use the modified design to minimize the influence of the ground plane. And it is observed that the gain of the modified CRLH HMSIW antenna is not very sensitive to the distance between the via-wall and the open edge.

2.7 Substrate Integrated CRLH Leaky-Wave Antenna with Flexible Polarization

An effective development of a CRLH leaky-wave structure for polarization-flexible antenna application is presented in this section [15]. It consists of two symmetrical waveguide lines loaded with series interdigital capacitors which radiate orthogonal 45° linearly-polarized waves. Its backfire-to-endfire beam-steering capability through frequency scanning due to the CRLH nature is demonstrated and discussed. It is able to generate arbitrary different polarization states by changing the way of excitation



Figure 2.47 Configurations of the proposed structures (a) Single CRLH-SIW radiating element, (b) Two-element unit-cell of the whole structure, and (c) Overall leaky-wave antenna prototype.

including linear polarization (LP) and circular polarization (CP). Six different polarization states, including four LP cases and two CP ones, are experimentally verified. Measured results are consistent with the simulation. The proposed leaky-wave structure shows some desirable merits such as the simplicity in design, low-cost in fabrication, beam-steering and polarization-flexible capabilities.

2.7.1 Proposed Structure and Working Principle

The geometric configuration of the proposed leaky-wave structure is shown in Figure 2.47, in which the layout of the unit-cell elements and the prototype of the entire leakywave structure with its orientations in the coordinate system are displayed. As shown the unit-cell is surrounded by vias on the two sides which are connected to a solid metallic ground. The interdigital slots etched on the waveguide surface is 45° inclined compared to the propagation direction (X-directed). Two symmetrical leaky TLs are side-by-side arranged and separated with a small distance (w_4) to improve the isolation as depicted in Figure 2.47(b) and (c). Each of them carries 14 interdigital slots which are periodically etched on the broad wall. They can generate two orthogonal linearly-polarized waves. A piece of 50 Ω microstrip line along with a taper line for impedance matching is placed at the end of each waveguide to facilitate the outside connection. This leaky-wave structure is fabricated on a substrate of Rogers 5880 with a thickness of 50 mils and a relative permittivity of 2.2. Generally, a thick and low dielectric constant substrate can be used to reduce the loss. The metallic via holes are chosen to have a diameter of 0.8 mm and a center-to-center pitch around 1.5 mm.

The polarization of an electromagnetic wave is defined as the orientation of the electric field vector. The polarization-agile operation scheme for the proposed structure can be explained using Figure 2.47(b), (c) and Figure 2.48(a). The two leaky lines radiate two orthogonally-polarized waves. The total electric field is the vector addition of the two waves. When only *Port* 1 (left line) is excited, a guided wave will be transmitted along the left line which produces the linearly-polarized wave in the $\varphi = 45^{\circ}$ direction. It should



Figure 2.48 (a) Operation principle of the polarization-flexible antenna. (b) Circuit model of the CRLH-SIW element shown in Fig. 1(a).

Polarization State	Excitations	Electric Field Distribution	Working Scheme
$\varphi = \pm 45^{\circ}$ Linear- Polarization	$E_1 \neq 0, E_2 = 0$ Or $E_1 = 0, E_2 \neq 0$		E_t or E_t'
X-directed Linear- Polarization	$E_1 = E_2$ And $\alpha = 0^\circ$		
<i>Y</i> -directed Linear- Polarization	$E_1 = E_2$ And $\alpha = 180^\circ$	E REALINE ENTER	$E_t \overset{90^{\circ}}{\checkmark}$
Circular-Polarization (RHCP & LHCP)	$E_1 = E_2$ And $\alpha = \pm 90^{\circ}$	E E E E	

Table 2.1 A summary of six specific polarization states under different input excitations

be noted that the orthogonal wave will also be generated but in a very weak manner, which is called cross-polar component. When *Port* 4 (right line) is fed alone, only the linearly-polarized wave along the $\varphi = -45^{\circ}$ direction will be produced. When they are illuminated by two equal and in-phase signals simultaneously, X-polarized (horizontal direction) wave will be produced. Similarly, Y-polarized (vertical direction) wave can be obtained with two inputs of the same magnitude and 180°-out-of-phase. They form a pair of orthogonal linearly-polarized modes. When the two lines are equally excited with ±90° phase difference, a circularly-polarized mode can be generated. Depending on their phase relation (phase delay or advance), left-handed circular polarization (LHCP) or right-handed circular polarization (RHCP) can be implemented. As shown in Figure 2.48(a) the feeding control circuit is required in order to implement the desired polarization. And it is noted that arbitrary polarization, including linear, circular and elliptical types, can be achieved depending on the phase and magnitude relation of the two input excitations. To give a better explanation, Table 2.1 summarizes the operation principle of six specific polarization states. They can be generalized into three orthogonal pairs: $\pm 45^{\circ}$ linearly-polarized waves, X- and Y-directed linearly-polarized waves, RHCP and LHCP radiating waves.

2.7.2 Design Procedures

A. Single Unit-Cell Analysis

The proposed TL is basically a CRLH structure working in the fast-wave region with a small periodicity compared to the free-space wavelength. Similarly, the design can be started from analyzing the unit-cell. Figure 2.48(b) shows the equivalent circuit of the CRLH-SIW unit-cell as presented in Figure 2.47(a). To obtain a continuously beam-scanning performance, balanced condition is usually required. Note that the series interdigital slot, which is rotated by 45°, also plays the role of a radiating element. Here a radiation resistor can be introduced in parallel to the series capacitor. Increasing the width and length of the slot could make the radiation more efficient.

The dispersion diagram for the proposed unit-cell is then investigated carefully based on the HFSS simulation. Figure 2.49(a) plots the dispersion curves for the CRLH-SIW



Figure 2.49 (a) Dispersion diagram calculated from the driven-mode and Eigen-mode simulations for the CRLH-SIW unit-cell; (b) *Bloch* impedance obtained using the driven-mode simulation; (c) Calculated different losses and the normalized leakage constant for the unit-cell. The parameters of the unit-cell are: $w_1 = 0.545$ mm, $w_2 = 0.4$ mm, $w_3 = 12.4$ mm, p = 9.1 mm, l = 3.1 mm (The interdigital capacitor has 9 fingers).

unit-cell using both the *S*-parameter method and eigen-mode simulation. It should be pointed out that the eigen-mode simulation shows that actually a very small bandgap (from 8.085 to 8.2 GHz) exists between the LH and right-handed (RH) regions. Rich information can be obtained from this figure. The air line plotted in the figure gives rise to two distinct regions: the radiating region (fast-wave) below it and the guiding region (slow-wave) above the line. Figure 2.49(b) presents the simulated *Bloch* impedance of the unit-cell extracted from the *S*-parameters. For a symmetric CRLH unit-cell shown in Fig. 2.48(b) without considering the radiation resistor, the *Bloch* impedance takes the form [4]:

$$Z_{B} = Z_{L} \sqrt{\frac{(\omega / \omega_{se})^{2} - 1}{(\omega / \omega_{sh})^{2} - 1}} - \left\{ \frac{\omega_{L}}{2\omega} \left[\left(\frac{\omega}{\omega_{se}} \right)^{2} - 1 \right] \right\}^{2}$$
(2.5)

where:

$$Z_L = \sqrt{\frac{L_L}{C_L}}, \quad \omega_{se} = \frac{1}{\sqrt{L_R C_L}}, \quad \omega_{sh} = \frac{1}{\sqrt{L_L C_R}}, \quad \omega_L = \frac{1}{\sqrt{L_L C_L}}$$
(2.6)

It is seen that ω_{se} and ω_{sh} correspond to a zero and a pole of Z_B . The balanced condition satisfies when $\omega_{se} = \omega_{sh}$. Otherwise the zero and pole always exist on the *Bloch* impedance no matter how ω_{se} is close to ω_{sh} . This is consistent with what we observed in Figure 2.49(b) where a zero is close followed by a pole. Note that it is difficult to eliminate this rapid change near the transition frequency. The *Bloch* impedance value gives some useful information for the final impedance matching. Figure 2.49(c) shows a loss analysis for the unit-cell which is calculated using the equation shown in the inset. The normalized leakage constant is also included in the figure. Due to a waveguide propagation mode and a relatively thick (50 mils) and low-permittivity substrate, the dielectric and conductor losses are very small and almost negligible as indicated in the figure. Good radiation efficiency can be envisioned.

B. Investigation on Two-Element Unit-Cell

When symmetrically aligning two leaky TLs to form an antenna with specified



Figure 2.50 Simulated results for the two-element unit-cell with different w_4 . (a) Isolation between different ports; (b) The *y*-*z* plane radiation patterns for the in-phase excitation case (left) and 180°-out-of-phase excitation case (right) at the transition frequency; (c) AR observed in the *x*-*z* plane. The other unit-cell dimensions are the same as shown in the caption of Fig. 3.

polarization, the distance between them is an important factor which ultimately determines the isolation, cross-polarization level and the grating lobe performance. To this end here we did some analysis on the radiation characteristics in *y*-*z* plane to obtain an optimal value of the distance (w_4) between the two leaky TLs. And this information can be obtained at an early stage by investigating the two-element unit-cell as shown in

Figure 2.48(b). Here the structure is re-plotted in the inset of Figure 2.50(a) for convenience. Radiation boundary condition is applied on a big enough air box containing this two-element unit-cell. By changing the separation (w_4) varied isolation between the ports and different radiation characteristics can be observed. As shown by Figure 2.50(a), when w_4 is increased, the isolation between *Port* 1 and *Port* 3 is also enhanced. Also the isolation at upper frequencies is larger than that at lower frequencies because of the smaller wavelength at upper frequencies. The isolation between *port* 1 and *port* 4 is also shown for the $w_4 = 10.2$ mm case. It is interesting to note that due to the backward coupling in the LH region the isolation between *port* 1 and *port* 4 is weaker at lower frequencies and higher at the upper frequencies compared to that between port 1 and port 3. Figure 2.50(b) shows the simulated radiation patterns in y-z plane at the transition frequency for both the in-phase (left figure) and out-of-phase (right figure) excitation cases. It reveals that when w_4 is larger, the undesired cross-polarization level is increased and the grating lobe occurs. The mutual coupling as indicated by Figure 2.50(a) is not significant due to their traveling-wave nature for which the field is not resonating strongly. However it can still slightly deteriorate the axial ratio (AR) for the circular polarization when this separation w_4 is small. Figure 2.50(c) shows the simulated AR by exciting the two-element unit-cell with 90° phase difference. A larger w_4 allows a better AR at the main beam direction. The AR at different frequencies is also plotted for the $w_4 = 10.2$ mm case. Circular polarization scanning with the main beam is also observed. Bear in mind that the radiation characteristics for this two-element unit-cell is different from that of the whole leaky-wave antenna. The isolation could be decreased when the number of unit-cells is increased due to more slot couplings. Therefore the AR is also different for the whole leaky-wave antenna. Nevertheless it is still able to provide some useful information which can be used to predict the final performance and guide the design.

The above results tell that the choice of the separation should be a compromise between the isolation and cross-polarization. From the simulation we find that there is an optimal range for w_4 which could match the needs of both the isolation and cross-polarization. However, as shown in Figure 2.50(b) the desired polarization (co-polarization) only works in the region of -20° to 20° in *y*-*z* plane for both of the two cases. Outside this region the cross-polar component becomes dominant. This is an important feature of this proposed antenna.

C. Design of the Leaky-Wave Line

The whole line is a fast-wave radiating structure which can be built by simply cascading the unit-cell described in Figure 2.49 and viewed as a *uniform* LW structure essentially. However, to connect with the outside circuits matching network is necessary since the impedance of the unit-cell is not simply 50 Ω . From the *Bloch* impedance shown in Figure 2.49(b) the average real part considering the whole fast-wave region is around 40 Ω . The imaginary part appears as capacitive in the LH region and zero in the RH region. For the real part we use a simple taper line as shown in Figure 2.51 converting the impedance from 40 Ω to 50 Ω . For the imaginary part we can tune the waveguide length between the taper line and the first unit-cell (t_2 as indicated by Figure 2.51) to match the circuit. At the low frequency (LH region below the waveguide cutoff)



Figure 2.51 The detailed input matching structure for the leaky TL.

the vias provide a shunt inductance which can be used to compensate the initial capacitive value. However at the frequency above the cutoff (RH region) the vias form an electric wall which supports the propagation of TE_{10} mode. Thus by slightly extending the waveguide length before connecting the taper line, the matching in the LH region can be improved and in the RH region it almost remains the same.

D. Coupler Designs for Excitations

In order to realize the input excitations listed in Table 2.1, two broadband couplers are designed and fabricated covering the frequency range of interest. The first one is a two-section 3-dB rat-race hybrid providing in-phase and 180°-out-of-phase outputs [16]. The second one is a 90° 3-dB directional coupler designed on the half mode SIW scheme [17]. Their detailed design procedures are shown in [16] and [17].

The two-section rat-race hybrid is fabricated on the Rogers 5880 substrate with a thickness of 20 mils. A photo is shown in the inset of Figure 2.52(b). It consists of three vertical $\lambda_g/2$ and four horizontal $\lambda_g/4$ lines whose impedances are optimized to have a good wideband matching from 7 GHz to 11 GHz. Specifically, they are $Z_1 = 52.9 \Omega$, $Z_2 = 74.1 \Omega$, $Z_3 = 30.8 \Omega$, $Z_4 = 56.7 \Omega$, $Z_5 = 66.1 \Omega$, and $Z_0 = 50 \Omega$. Figure 2.52 shows the



Figure 2.52 Measured and simulated performance for the two-section rat-race coupler. (a) Measured *S*-parameters for the out-of-phase case; (b) Measured *S*-parameters for the in-phase case; (c) Measured and simulated phase performance. The structure is shown in the inset. *Port* 1 is excited for 180°-out-of-phase operation. *Port* 4 is the input port for the in-phase case.

experimental results for the coupler, including magnitude and phase responses for the out-of-phase and in-phase cases. Over the interested frequency band, small reflection (below -10 dB), good amplitude imbalance (less than 0.4 dB), small phase variation (less than $\pm 6^{\circ}$), and large isolation (better than 24 dB) are achieved.



Figure 2.53 Measured and simulated performances for the 3-dB HMSIW directional coupler. (a) Measured *S*-parameters, and (b) Measured and simulated phase performance. The structure is shown in the inset. *Port* 1 is the input port and *Port* 4 is isolated.

The fabricated prototype of the half-mode SIW directional coupler is shown in the inset of Figure 2.53(b). It is employed to realize the feedings with 90° phase difference and equal power division. The coupling area is an aperture on the via wall. This coupler is implemented on the Rogers 5880 substrate with a thickness of 50 mils. The measured results are shown in Figure 2.53. Good reflection and isolation (below 13.5 dB), balanced outputs and expected phase difference are achieved covering a frequency band from 7 GHz to 10 GHz.



Figure 2.54 Photograph of the fabricated LW antennas. Parameters are: $t_1 = 4$ mm, $t_2 = 5.2$ mm, $w_5 = 5.8$ mm, $w_{in} = 3.9$ mm, $w_4 = 10.2$ mm.



Figure 2.55 Measured *S*-parameters of the fabricated antennas shown in Fig. 11. Grey line shows the simulated results for comparison.

2.7.3 45°-Polarized Leaky-Wave Antenna

Based on the procedures shown above, a single traveling-wave antenna with 14 unitcells depicted in Figure 2.49 is designed and optimized. Figure 2.54 shows a photograph of the LW antennas with the parameters shown in the caption. Two identical LW lines are symmetrically aligned along the X-direction. We fabricated and measured these antennas in our laboratory. Figure 2.55 shows the measured *S*-parameters for each of the two antennas. Basically they are in agreement with the simulation (gray dash line). The LH and RH regions are separated by the transition frequency of 8.2 GHz. As observed the whole TL is not perfectly balanced which is in agreement with eigen-mode simulation on



Figure 2.56 Measured radiation patterns in x-z plane for co-polarization at different frequencies.



Figure 2.57 Comparison of the simulated and measured radiation patterns in x-z plane at 8.2 GHz. Measured patterns include the results obtained from the far field chamber and the near field chamber.



Figure 2.58 Simulated and Measured directivity, gain and the measured efficiency for the second linearly-polarized antenna.

the unit-cell. Small difference is due to that this is a finitely long leaky line which cannot guarantee a periodic boundary condition for the unit-cell. The matching in the RH region is better than the LH region which is consistent with the *Bloch* impedance analysis.

Figure 2.56 shows the normalized radiation patterns of the second antenna measured in a far-field chamber. It is important to bear in mind that its co-polar direction is 45° -rotated with respect to *x-z* plane (scanning plane or co-polarization plane). In the measurement the standard linearly-polarized horn antenna as the transmitter is rotated by 45° to match the co-polar direction of the LW antenna. Its full-space beam-steering performance by frequency scanning is verified experimentally. The beam-width is larger at the lower frequencies due to the larger leakage constant and decrease of the antenna equivalent aperture size.

To check the directivity and efficiency we also measured this antenna in a near-field chamber in our High-Frequency Center. Figure 2.57 compares the normalized broadside patterns at 8.2 GHz obtained from the simulation, the far-field measurement and the near-field measurement. The cross-polarization is also plotted. A reasonable agreement is observed. The cross-polar level is -15 dB in the measurement and -23.5 dB in the simulation. Figure 2.58 shows the simulated and measured directivity, realized gain, and the measured efficiency. The measured efficiency is low at 8.2 GHz and 10 GHz because of the large reflection and termination loss. When it radiates completely this antenna should be able to provide an average efficiency around 80% as that obtained at 7.8 GHz and 8.7 GHz. By improving the impedance matching and increasing the number of unit-cells better efficiency can be achieved.



Figure 2.59 Simulated patterns in terms of realized gain for the X-polarized antenna in x-z plane in (a) LH region, (b) Broadside, and (c) RH region.



Figure 2.60 Measured S-parameters of the X-polarized LW antenna.

2.7.4 X-Polarized Leaky-Wave Antenna

A. Simulation

The X-polarized wave is obtained by equally feeding the two leaky lines with in-phase excitations. In the simulation setup two identical signals are directly applied at *port* 1 and *port* 4 (Fig. 1(c)), respectively. To avoid handling large structures using HFSS the



Figure 2.61 Measured and normalized radiation patterns for the X-polarized antenna in x-z plane in (a) LH region, (b) Broadside, and (c) RH region.

coupler here is not included in the simulation. Figure 2.59 shows the simulated gain pattern in *x-z* plane (scanning plane) including both the co-polarization and cross-polarization. Low cross-polar level and beam-scanning are observed. The realized maximum gain in the *x-z* plane is 10 dB in the LH region and 12 dB in the RH region approximately.

B. Measurement

To measure the antenna performance under the X-polarized condition, we cascaded the fabricated rat-race hybrid and the two-element LW antenna as the prototype shown in the inset of Figure 2.60. The whole structure is fed at *port* 4 and Figure 2.60 presents the measured *S*-parameters. As predicted low reflection coefficient and good isolation are achieved. Figure 2.61 shows the normalized radiation patterns at five different frequencies obtained from the near-field measurement. The main-polarization is in the *x-z*



Figure 2.62 Simulated patterns in terms of realized gain for the Y-polarized antenna in x-z plane in (a) LH region, (b) Broadside, and (c) RH region.

plane and the cross polarization level is higher than that observed in the simulation which is due to the fact that the coupler performance is not ideal. Also the two fabricated radiating TLs are not identical. The measured gains at 7.5 GHz, 7.8 GHz, 8.2 GHz, 8.7 GHz, and 10 GHz are 9.72 dBi, 9.48 dBi, 7.76 dBi, 11.1 dBi, and 11.75 dBi, respectively. Overall the tested results are consistent with the simulation.

2.7.5 Y-Polarized Leaky-Wave Antenna

A. Simulation

Figure 2.62 shows the simulated gain patterns which are polarized in Y-direction. Two signals with 180° -out-of-phase are directly applied at *port* 1 and 4 without including the coupler. The *H*-plane coincides with the *x-z* plane (scanning plane) and full-space beam-scanning is also observed.



Figure 2.63 Measured S-parameters of the Y-polarized LW antenna.



Figure 2.64 Measured and normalized radiation patterns for the Y-polarized antenna in x-z plane in (a) LH region, (b) Broadside, and (c) RH region.

B. Measurement

Figure 2.63 shows the measured *S*-parameters. In this case the whole structure as indicated in the inset of Figure 2.63 is fed at *port* 1 and other ports are terminated with the 50 Ω load. Its radiation patterns are measured in the near-field chamber and Figure 2.64 shows the normalized results. The increase of cross-polarization level is also found



Figure 2.65 Measured and simulated radiation patterns in *y-z* plane at 8.2 GHz for (a) X-polarized LW antenna, and (b) Y-polarized LW antenna.

in the measurement after introducing the rat-race hybrid. The measured gains at 7.5 GHz, 7.8 GHz, 8.2 GHz, 8.7 GHz, and 10 GHz are 8.21 dBi, 10.8 dBi, 10.01 dBi, 11.78 dBi, and 11.13 dBi, respectively. It is interesting to find that at the broadside (8.2 GHz) the gain for Y-polarized wave is higher than that observed in the X-polarized case. To find the reason we checked the simulated and measured patterns in *y*-*z* plane at 8.2 GHz for both of the two cases. They are plotted in Figure 2.65 together with the 3D patterns in the inset. It is seen from the 3D radiation patterns that the beam in *y*-*z* plane for the X-polarized case is much wider than that in the Y-polarized case. The reason is that the cross-polar component is more significant for the X-polarized case. This result is in good agreement with the analysis on the two-element unit-cell shown in Figure 2.50(b).



Figure 2.66 Measured S-parameters of the entire circularly-polarized LW antenna.

2.7.6 Circularly-Polarized Leaky-Wave Antenna

The circular polarization is achieved by exciting two orthogonally-polarized radiating lines with 90° phase difference. For simplicity here only some measured results are provided. The detailed analysis and performance can be found in [18]. In the measurement the half-mode SIW 90° directional coupler is connected with the leaky lines to provide the required excitation. The whole structure, as displayed in the inset of Figure 2.66, is fed at *port* 1 resulting in a RHCP. It is worth noting that LHCP can also be obtained by feeding the whole structure at *port* 4. The measured *S*-parameters are shown in Figure 2.66. It is seen that the total reflection (*S*₁₁) is below -11 dB in the whole region. The isolation (*S*₄₁) experiences a peak around 8.2 GHz and deteriorates below 7.2 GHz. This is reasonable since the reflected waves from the two leaky lines arrive at *port* 1 with 180° phase difference thus they cancel each other. However, they are in-phase when arriving at *port* 4 thus it is the superposition of the two waves due to the 90° directional coupler. Therefore the *S*₄₁ behaves similarly to the reflection of the single radiating line.

Figure 2.67 shows the normalized radiation patterns measured in the near-field



Figure 2.67 Measured radiation patterns of the circularly-polarized antenna in x-z plane in (a) LH region, (b) Broadside at 8.2 GHz, and (c) RH region.



Figure 2.68 Measured AR of the circularly-polarized antenna in x-z plane in (a) LH region, (b) Broadside at 8.2 GHz for different w_4 , and (c) RH region.

chamber at five different frequencies. Both the co-polarization (RHCP) and crosspolarization (LHCP) are provided. Beam scanning is verified. The measured directivity is 10.45 dBi at 7.5 GHz, 10.71 dBi at 7.8 GHz, 11.52 dBi at 8.2 GHz, 13.22 dBi at 8.7 GHz, and 14.556 dBi at 10 GHz. The directivity in the RH region is higher than that in the LH region due to the lower leakage constant and the decrease of the wavelength, which lead to a more effective and larger aperture. The measured AR at the above frequencies is plotted in Figure 2.68. We also plotted the simulated AR for different separations (w_4) between the two TLs in Figure 2.68(b) in order to give a comparison with the AR obtained from the two-element unit-cell simulation shown in Figure 2.50(c). Overall the simulated AR for the whole LW antenna deteriorates a little compared to the unit-cell simulation because of the increased slot coupling. This adopted distance is an optimal value for the whole structure. It is seen that at the main beam direction the obtained AR is always below 3 dB. Discrepancy is observed between the simulated and measured AR which is predictable since the 3-dB coupler is not perfect and band-limited. Also the fabrication error could result in two different leaky lines which would affect the AR. In general, the antenna performance is satisfactory characterized by high directivity, low cross-polar level and good circular polarization.

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Chapter 3

SIW Loaded by CSRRs and Its Applications to Miniaturized Waveguide Components

Split-ring resonators (SSRs), originally proposed by Pendry *et al.* [1], have attracted great interest among researchers in electromagnetics and microwave engineers due to their potential applications to the synthesis of metamaterials with negative effective permeability. From duality argument, complementary split-ring resonators (CSRRs) were introduced by Falcone *et al.* in 2004 as new metamaterial resonators and have been proved to exhibit negative permittivity [2]. Later the characteristics for the SRRs and CSRRs including their equivalent circuit models have been studied and developed extensively [3]-[5], in which the SRRs are considered as resonant magnetic dipoles that can be excited by an axial magnetic field while the CSRRs are shown to behave as electric dipoles which need an axial electric field excitation. Their applications to planar miniaturized microwave devices such as filters, diplexers and couplers were then proposed and investigated [6-8]. These proposed components are usually achieved in microstrip and CPW technology by combining the metamaterial resonators with other planar elements such as shunt stubs or series gaps.

The CSRRs can be viewed as electric dipoles and are good candidates to behave as electric scatterers [9]. From the previous literature it is shown that for the SRRs-loaded waveguide the SRRs provide a stopband when they are resonant above the cutoff



Figure 3.1 (a) Topology and (b) Its equivalent circuit model of the square CSRR. Gray zone represents the metallization.

frequency [3]. This stopband switches to a passband when the SRRs are resonant below the cutoff frequency [10], [11]. The CSRRs exhibit similar abilities. It has already been demonstrated that they are capable of generating a stopband above the waveguide cutoff [3]. The applications of this property to the design of bandstop, bandpass and ultra-wide bandpass filters have been illustrated in [12], [13].

The present chapter discusses the characteristics of CSRRs resonant below the waveguide cutoff frequency, with a view to their working principles and possible applications. Considering the difficulties in combining the CSRRs with traditional metallic waveguide, we choose the SIW technology to implement these components. The SIW has provided a very attractive platform to the design of low-cost and highly integrated waveguide components, and more importantly, it is very convenient to etch the CSRRs on the waveguide surface. Without loss of generality, square or rectangular CSRRs are chosen who demonstrate better suitability for alignment purpose. The structure of the adopted CSRR and its equivalent circuit model are depicted in Figure 3.1. Wave transmissions below the cutoff frequency of the SIW, or so-called evanescent-wave

amplification, has also been discussed in [14], [15], both of which are realized by inserting some novel meta-structures into the waveguide and are characterized by backward-wave propagation.

In this study, forward-wave propagation below the waveguide cutoff is obtained based on the resonant behavior of the CSRRs. The passband generated in this way possesses controllable center frequency and bandwidth and is very suitable for miniaturized waveguide filter applications. By changing the orientations and structures of the CSRRs, three different kinds of filters are designed, fabricated and measured. We further extend their applications to diplexers and multi-band filters. Low insertion loss, high quality (Q) factor and excellent selectivity with compact size are achieved. The measured results are in good agreement with the simulation.

3.1 SIW-CSRR Resonators

Configurations of the proposed SIW – CSRR unit-cells are first presented in this section, followed by the investigation on the corresponding transmission behavior and working principles. A modified structure with improved transmission responses is proposed and analyzed. At the end of this section loss consideration for the resonators is presented in brief. Here more emphasis is placed upon the transmission behavior below the waveguide cutoff frequency, which distinguishes this study from the previous research [12], [13].

3.1.1 Configuration

Figure 3.2 shows the layout of the proposed unit-cells. The two linear arrays of



Figure 3.2 Configurations of the proposed SIW-CSRR unit cells, in which the CSRRs are (a) Face-to-face, (b) Back-to-back, (c) Side-by-side reversely oriented and (d) Side-by-side equally oriented.

metalized vias are used to form the electric sidewalls of the waveguide. A pair of identical CSRRs are adopted and etched on the metal cover of the waveguide. With respect to the direction of the split of the outer ring, they are aligned face-to-face, back-to-back and side-by-side. Also, the side-by-side type has been further divided into two cases with the CSRRs reversely or equally oriented as shown in Figure 3.2 (c) and (d). The ground remains as a solid ground in the design which is not depicted in Figure 3.2. Note that the CSRRs could also be etched on the ground. However, it is usually preferred to preserve the integrity of the ground in high-frequency system design in order to decrease the noise and reduce the radiation losses which may be introduced by the ring slots. The 50 Ohm microstrip feed line used here is for the purpose of measurement. The



Figure 3.3 Simulated transmission responses corresponding to the unit cells shown in Figure 3.2. (a) Face-to-face case, (b) Back-to-back case, (c) Side-by-side reversely oriented case and (d) Side-by-side equally oriented case. The geometrical parameters for the unit cells are: $a_1 = 0.32 \text{ mm}, a_2 = 0.32 \text{ mm}, d = 0.18 \text{ mm}, g = 0.26 \text{ mm}, b = 3.92 \text{ mm}, s = 1.53 \text{ mm}, t = 0.54 \text{ mm}, l = 2.04 \text{ mm}, w = 12.3 \text{ mm}.$ In the third case part of the parameters are revised as: $a_1 = a_2 = 0.34 \text{ mm}, d = 0.17 \text{ mm}, b = 3.93 \text{ mm}, t = 0.5 \text{ mm}, w = 12.1 \text{ mm}, \text{ others are the same}.$

substrate of Rogers RT/Duroid 5880 with a thickness of 0.508 mm and a relative permittivity of 2.2 is used in all of our designs. The metalized vias have a diameter of 0.8 mm and a center to center spacing of 1.48 mm. We choose the width of the waveguide w = 12.3 mm to fix the cutoff frequency of the initial SIW at about 8.7 GHz.

The adoption of such configurations is partially based on the field distribution inside the waveguide. The electric field for the dominant mode of the SIW is perpendicular to the surface and the ground. The direction of the magnetic field is parallel to the waveguide surface and perpendicular to the sidewalls. The CSRR, which essentially behaves as an electric dipole and requires an axial electric excitation, can only be effectively excited under this condition. This also explains that the SRR in a hollow waveguide has to be vertically placed in order to be properly excited.

3.1.2 Transmission Responses

Using Ansoft's High Frequency Structure Simulator (HFSS) software package, the transmission responses for the proposed unit-cells are simulated and investigated. Figure 3.3 presents the optimized results of the resonators shown in Figure 3.2, along with the circuit model simulated results in Figure 3.3 (a)-(c) which will be discussed in the following part of this section. Bear in mind that all the observed passbands are working below the cutoff of the waveguide. Also note that by modifying the orientations of the CSRRs, different characteristics of the passbands have been obtained.

The first and second unit cells with the CSRRs oriented face-to-face and back-to-back exhibit a similar passband with one pole and one transmission zero located above the passband. However, for the second case the transmission zero is closer to the pole which leads to a steep upper side transition which, on the other hand, is at the cost of increased insertion loss. This is mainly due to the weak coupling as shown later. For the third case, in which the two rings are side-by-side reversely arranged, two transmission poles along with two transmission zeros in the upper band are achieved. A good filtering response is obtained for this structure. With respect to the direction of wave propagation the two ring pairs are asymmetrically placed resulting in a two-pole transmission. This indicates that two different coupling modes are involved. A detailed explanation will be given later. A passband has been detected for the fourth resonator but the propagation is quite weak



Figure 3.4 Wideband responses of the face-to-face oriented unit cell compared with the corresponding simulated SIW response and the electric field distribution of the TE_{10} mode in these waveguides.

compared with the passbands in other cases. This indicates that the split of the ring slot plays an important role in transmission which essentially represents a magnetic connection.

To better clarify the principle of the passband which is defined as a forward-wave transmission below the waveguide cutoff, wide band response, including both the simulated and measured results for the unit cell shown in Figure 3.2 (a) is presented in Figure 3.4, which is compared with the simulated S_{21} of the initial SIW with the same dimensions. Figure 3.5 depicts the dispersion and attenuation diagram of this unit cell obtained from the *ABCD* matrix as illustrated in [16]. The measured results are consistent with the simulation. Figure 3.4 shows that the waveguide high-pass band for the unit cell is shifted up compared to the cutoff frequency of the initial waveguide, which can be calculated as shown in [17]. To explain this phenomenon, the electrical field at 11 GHz (in the high-pass band just above the cutoff frequency) for both of the structures has been



Figure 3.5 Dispersion diagram (including both computed and measured results) and attenuation diagram for the face-to-face oriented unit cell.

plotted in the inset of Figure 3.4. Generally the wave propagation at this frequency for the unit cell loaded by CSRRs still keeps the manner of TE_{10} mode. However, as observed the mode is squeezed by the pair of the CSRRs, although they are not resonant and do not affect the propagation. Thus, the cutoff frequency has been pushed up to a certain degree. Strictly speaking, this cutoff frequency is no longer the initial waveguide cutoff frequency. The normalized dispersion relation shown in Figure 3.5, which exhibits a positive slope at the frequencies of interest, confirms the forward-wave nature of the passband. The curve of the attenuation constant shows that there are two passbands existing in the observed frequency range, which are the forward-wave passband below the waveguide cutoff and the intrinsic waveguide high-pass band.

3.1.3 Equivalent Circuit Models

Here, the equivalent circuit models (see Figure 3.6) have been derived and verified for design purpose and, most importantly, to illuminate the essential differences between the



Figure 3.0.6 (a) Circuit model and (b) Simplified equivalent circuit for the first and second unit cells, and (c) Simplified equivalent circuit corresponding to the third unit cell.

unit cells which lead to the variations in transmission characteristics. Figure 3.6 (a) shows the initial circuit model corresponding to the first two unit cells shown in Figure 3.2 (a) and (b), while their simplified equivalent circuit is presented in Figure 3.6 (b). On the other hand, the structure of Figure 3.2 (c) can be roughly represented by the equivalent circuit shown in Figure 3.6 (c). Material losses are neglected in the models. As seen in Figure 3.6 (a), the SIW can be considered as an ordinary two-wire transmission line (formed by the metal surface and the ground) loaded with infinite number of short-circuited stubs (formed by via-walls). Viewed from the center of the waveguide, the

short-circuited stub (via-walls) appears as inductive after a piece of transmission line (see Figure 3.6 (a)) and it is modeled as L_d . This part makes a high-pass contribution. The CSRR is modeled by means of the shunt-connected resonant tank formed by the capacitance C_r and the inductance L_r as shown in Figure 3.1. L_c indicates the inductive connection mainly through the split of the outer ring between the waveguide transmission line and the ring resonators. The capacitive coupling which is realized by the slot coupling between the waveguide transmission line and the CSRRs is denoted by Cc. For the first two resonators a symmetrical plane can be used along the longitudinal direction thus the two parallel CSRRs are modeled by one resonator. For the third unit cell shown in Figure 3.2 (c), both of the two CSRRs are shunt-connected to the two-wire equivalent transmission line and the mutual interaction between the resonators needs to be taken into consideration. The coupling mechanisms for the SRRs were theoretically and experimentally studied in [18]. Here through similar analysis we consider the coupling between the CSRRs as a combination of magnetic and electric types. L_s , C_s are used here to describe the inductive and capacitive couplings between the CSRRs, respectively.

It is important to note that these circuit models are indeed simplified versions. Here at least three other simplifications are made. First the via-walls are just represented by an inductance L_d . In fact they should be modeled by infinite number of shunt inductances along the two-wire transmission line. Secondly as shown in Figure 3.6 (a) the CSRRs are coupled to the ground through both an equivalent inductance and a small capacitance C_2 in a parallel form. However, compared with the capacitive coupling which is mainly realized by the center patch of the resonator and the ground, the inductive connection
implemented directly by the via-walls is dominant. Thus C_2 is neglected. The impedance value Z_2 is much smaller compared with Z_1 . For convenience, we further regard the obtained impedance value Z_2 as zero which means the CSRR and the ground are directly connected. Third, the distributed series inductance and distributed shunt capacitance of the waveguide are all neglected. Also, the proposed circuit models are valid only for a limited frequency range. They cannot reflect the influence of the high-order modes of the resonators.

Although these circuit models are simplified they are basically correct and are fully capable of explaining the transmission characteristics of these structures. The first circuit model gives a zero-transmission frequency at:

$$f_{\rm z} = 1/2\pi \sqrt{L_{\rm C}C_{\rm C}}$$
 (3.1)

It is worth mentioning that the series part impedance undergoes an abrupt change (from inductance infinity to capacitance infinity) around this frequency which is a sudden change on the dispersion diagram shown in Figure 3.5. Similarly, it is clear that the second circuit model possesses two transmission poles and two transmission zeros. The second transmission zero located below the first transmission zero is created by the mutual coupling between the two CSRRs. The simulated results from these circuit models for the first three structures are depicted in Figure 3.3, compared with the results from full-wave simulation.

To better verify their working principles, the electric field and magnetic field distributions in the middle plane of the substrate at the center frequency of the passband for the four unit cells are simulated and presented in Figure 3.7. It is clearly seen that they



Figure 3.7 (a) Electric and (b) Magnetic field distribution at the resonance frequency of the four unit-cells.



Figure 3.8 Full-wave simulated S_{21} for the third unit cell with different *t*.

are totally different from the field distribution of TE_{10} mode shown in Figure 3.4. Compared with other resonators, the peak magnetic field of the second resonator is weaker as shown in Figure 3.7 (b). This suggests a lower energy capacity which ultimately indicates a smaller L_r . Apparently the current attains maximum intensity around the split of the outer rings. However the CSRRs when aligned back-to-back can only receive limited energy though this split. This accounts for the transmission difference between Figure 3.3 (a) and (b). The down-shift of the transmission zero in Figure 3.3 (b) is due to the increase of L_c . For the third unit cell it is to be noted the two CSRRs reach electric field maximum with a phase delay of 90 degree. The bandwidth of the passband for this unit cell can be adjusted by changing the mutual coupling. Figure 3.8 presents the results from full-wave simulation by changing the distance t between the two CSRRs. When t is smaller, which means the middle strip is thinner, the corresponding inductance denoted by L_s increases, and the bandwidth turns out to be smaller. In this case L_c decreases because the magnetic coupling becomes easier when the CSRRs are close to the center. Then the transmission zero described by (2) is shifted up. The passband transmission is weaker for the fourth unit cell shown in Figure 3.2 (d). It can be explained in the way that the magnetic coupling at one side nearly amounts to zero. However, this can be improved by increasing the capacitive coupling which can be achieved by decreasing the slot width a_1 of the outer rings. This is confirmed by the simulation shown in Figure 3.3 (d).

3.1.4 New Structure with Improved Performance

By investigating the differences of the electric field distribution between the TE_{10} mode shown in the inset of Figure 3.4 and the propagating mode shown in Figure 3.7 (a), we find that the propagation of the TE_{10} mode is heavily reliant upon the middle metal strip line between the two CSRRs. By removing the middle strip line the propagation of TE_{10} mode should be inhibited in theory. We find that this approach is feasible for the third type unit cell, where the strip line seems to be unimportant in the mutual coupling



Figure 3.9 (a) Proposed new structure and (b) Its transmission responses by circuit model and full wave simulation. The geometrical parameters are: $a_1 = 0.36$ mm, $a_2 = 0.36$ mm, d = 0.17 mm, g = 0.24 mm, b = 3.96 mm, $w_t = 0.62$ mm, l = 2.02 mm, w = 12.1 mm.

between the two CSRRs. To this end, a new structure is proposed as shown in Figure 3.9 (a). It is similar to the structure in Figure 3.2 (c) but without the connection line in the middle. The circuit model shown in Figure 3.6 (c) also applies to this structure. It is seen that the slot coupling is increased which means the increase of C_s . The series inductance is also increased due to the increased difficulty of inductive connection. Then the corresponding transmission zero should be moved down substantially. Figure 3.9 (b) presents the results obtained from circuit model and full-wave simulation, which verifies our prediction.

It is worth noting that the novelty of this new structure consists in two aspects: First, we use a waveguide structure loaded by CSRRs to implement a passband below the waveguide cutoff frequency. The spurious modes of this passband which are located in



Figure 3.10 Calculated different transmission losses for the revised resonator.

the waveguide high-pass band are inhibited. Second, the modified CSRRs in return have suppressed the initial high-pass band of the waveguide to a certain extent. In this interesting way a filter with improved stopband rejection can be obtained.

3.1.5 Loss Consideration

Since the proposed resonators are not fully closed structures, the radiation loss appears as a practical issue for real application. To this end the radiation loss for all the resonators are calculated and it is found that this loss is not significant. Among them the modified resonator exhibits the largest radiation loss. The normalized radiation loss in the passband for this structure is smaller than 0.06. The radiation loss for both the first and third resonator is less than 0.042. Since the CSRR works as an electrical dipole we find that its radiation is quite similar to a dipole antenna. However the biggest radiation happens in a parallel plane to the ground inside the waveguide, which is confined by the via-walls thus the radiation leakage is very weak. The modified structure has additional slot coupling thus exhibits relatively larger radiation loss. Figure 3.10 presents a comparison by including all the losses for this resonator, which leads to a 1.2 dB insertion loss in total. Compared with the filters using metamaterial resonators shown in [7], this loss is smaller. But compared with normal SIW filters as shown in [19], this loss is slightly larger but this resonator shows advantage in terms of the selectivity and size.

3.2 Filter Design Methodology

Although periodic structures have the ability to generate a passband they are not very suitable for filter application for the lack of control on the bandwidth, return loss, etc. For design purpose it is important to follow the classic methodology as shown in [20] to synthesize a filter in order to meet the given specification. This section will briefly discuss the filter design procedure using the proposed resonators based on the traditional coupled resonator method. The design flow is outlined first and then a simple illustrative example is given in order to provide some useful guidelines.

The first step is circuit synthesis, which is based on the filter requirements. The design parameters of the filters including the coupling coefficients and external *Q*-factor can be determined in terms of the circuit elements of a low-pass prototype filter [20]. After determining the required coupling coefficients and external *Q*-factor, the relationship between coupling coefficients and physical structures of coupled resonators should be established in order to determine the physical configuration of the filter.

Generally the coupling coefficients of coupled resonators can be extracted from two split resonance frequencies resulting from electromagnetic coupling using [20]:

$$M = \frac{f_1^2 - f_2^2}{f_1^2 + f_2^2}$$
(3.2)

where f_1 and f_2 stand for the resonance frequencies of the low and high modes, respectively. The external *Q*-factor can be obtained by simulating a doubly loaded resonator and calculated by [20]:

$$Q_e = \frac{2f_0}{\Delta f_{3\,\mathrm{dB}}} \tag{3.3}$$

where f_0 is the frequency at which S_{21} reaches its maximum value and $\Delta f_{3 dB}$ is the 3 dB bandwidth for which S_{21} is reduced by 3 dB from its maximum value. Usually design curves of the coupling coefficients and external *Q*-factor versus physical dimensions of coupled resonators are established to facilitate the design. Finally a fine-tuning procedure is often used to optimize the entire filter.

As an illustrative example, a simple two-order filter using two face-to-face aligned SIW-CSRRs is designed following the above procedures. The passband of this filter is located around 5 GHz with a 3.2 % fractional bandwidth. By simple circuit synthesis a coupling matrix is generated in which $M_{12} = 0.0432$ and $Q_e = 24.55$. The dimensions of the resonator are first determined by simple eigen-mode simulation. To determine the internal coupling coefficient, the pair of cascaded resonators is required to be excited with a high external *Q*-factor in order to clearly observe the two resonance frequencies. Here we choose the eigen-mode simulation – a more accurate approach to obtain the resonance frequencies. The structure is shown in the inset of Figure 3.11 (c). Here it is surrounded with solid metallic walls instead of vias in order to expedite simulation. Two



Figure 3.11 (a) Vector magnetic field distribution for low mode, (b) Vector magnetic field distribution for high mode, and (c) Resonance frequencies and the coupling coefficient versus the distance l_{dis} between resonators (Other parameters are : $a_1 = 0.3 \text{ mm}$, $a_2 = 0.3 \text{ mm}$, d = 0.2 mm, g = 0.28 mm, b = 3.92 mm, t = 0.66 mm, w = 11.9 mm,).

eigen-modes around 5 GHz, also known as even and odd modes, are observed. Figure 3.11 (a) and (b) plot the vector magnetic field distribution of the low and high modes. The coupling coefficient, which is calculated by (3.2), can be adjusted by changing the distance l_{dis} between the two resonators. Figure 3.11 (c) presents the relationship between l_{dis} and the coupling coefficient as well as the eigen-mode frequencies.

To determine the external Q-factor, numerical analysis is carried out on the doubly loaded waveguide resonator shown in the inset of Figure 3.12. The coupling is controlled by the waveguide length between the CSRR and the input microstrip, which is denoted



Figure 3.12 External *Q*-factor of the input/output resonator. (Other parameters are : $a_1 = 0.3$ mm, $a_2 = 0.3$ mm, d = 0.2 mm, g = 0.28 mm, b = 3.92 mm, t = 0.66 mm, w = 12.3 mm, l = 2.64 mm)



Figure 3.13 Ideal response and the simulated response of the designed two order filter. $(a_1 = 0.3 \text{ mm}, a_2 = 0.3 \text{ mm}, d = 0.2 \text{ mm}, g = 0.28 \text{ mm}, b = 3.92 \text{ mm}, t = 0.66 \text{ mm}, w = 12.3 \text{ mm}, l_{dis} = 8.9 \text{ mm}, l = 1.22 \text{ mm})$

by *l* in the figure. Figure 3.12 shows the calculated Q_e versus *l* using (4).

By looking at the above design curves an optimal physical dimension is obtained. The final filter configuration after some simple tuning is indicated in the inset of Figure 3.13. The simulated response is also plotted in Figure 3.13, compared with ideal response from

matrix synthesis. Good agreement is achieved. The unsymmetrical response is attributed to the initial transmission zero of the resonator.

Other resonators can also be used for filter design following similar procedures. The coupling can be controlled in different ways as the example demonstrated in Figure 3.8 of the previous section. Meanwhile the equivalent circuits discussed before can be used to assist the design, such as the control of the transmission zeros.

3.3 Single-Band Filter Application

In this section three different types of single-band filters with varied arrangements are designed and fabricated. They are based on the resonators with CSRRs placed face-to-face, side-by-side reversely oriented (see Figure 3.2 (a) and (c)), and the proposed new resonators (see Figure 3.9), respectively. The Rogers RT/Duroid 5880 substrate with a relative permittivity of 2.2 and a thickness of 0.508 mm was used in all the experiments. All the metalized via arrays exhibit a diameter of 0.8 mm and a center to center spacing around 1.48 mm. These filters were fabricated with the standard PCB process in the High Frequency Center of our Lab., and they were measured using an Agilent 8510C vector network analyzer.

3.3.1 Filters with Face-to-Face Aligned CSRRs

Figure 3.14 (a) shows the photograph of the fabricated one-, two- and three-stage filters using the unit cell shown in Figure 3.2 (a). Although they are working in a waveguide format, they turn out to be pretty compact. The dimensions of two-stage filter are just



Figure 3.14 (a) Photograph of the fabricated first kind of filters, and (b) Detailed layout of the three-stage filter. The dimensions of the three-stage filter are: $a_1 = 0.3$ mm, $a_2 = 0.3$ mm, d = 0.2 mm, g = 0.265 mm, b = 3.9 mm, t = 0.54 mm, w = 12.3 mm, l = 1.13 mm, $l_1 = l_2 = 9$ mm.

shown in the above section. Figure 3.14 (b) presents the detailed structure and dimensions of the three-stage filter. Note that the *CSRR 2* as shown in Figure 3.14 (b) is scaled by a factor of k = 1.035 compared with the *CSRR 1* to adjust its resonance frequency. They are designed following the previously mentioned procedures.

Figure 3.15 shows the simulated (dashed line) and measured (solid line) frequency responses of the two-stage and three-stage filters. The transmission characteristics of the one-stage filter have already been presented in the previous section. As expected two-pole and three-pole filters with transmission zeros located in the upper band are obtained. The three-pole filter has a measured center frequency of 5.05 GHz and a 3-dB bandwidth of 0.33 GHz. Its minimum passband insertion loss is approximately 2.03 dB, which includes the extra loss caused by the SMA connectors. Its in-band return loss is better than -16.6 dB. Due to the existence of the transmission zeros, this filter exhibits a stopband rejection better than -52 dB as observed in the measurement. To illustrate the influence of the waveguide high-pass band, Figure 3.16 (a) presents the measured



Figure 3.15 Measured and simulated transmission responses of the (a) Two-stage filter and (b) Three-stage filters.

wideband response of the three-pole filter, compared with the simulated frequency response of the SIW which removes the CSRRs but shares the same waveguide dimensions. Figure 3.16 (b) presents the simulated transmission response of the three-pole filter with varied waveguide widths denoted by w. It can be easily seen that by decreasing the waveguide width, the cutoff frequency can be increased but the passband



Figure 3.16 (a) Measured wideband response of the three-stage filter compared with the simulated results of the corresponding SIW. (b) Simulated S_{21} for the three-stage filter with different waveguide widths denoted by w.

below the cutoff receives a much smaller influence. Only the coupling is affected.

Figure 3.17 (a) shows the simulated and measured unwrapped phase response for the one- and two-stage filters. The phase is negative (phase lag) and a decrease in the phase for an additional stage is observed in the passband from 4.75 to 5.2 GHz. This also confirms the forward-wave nature of the propagating passband. Figure 3.17 (b) shows the measured group delay of the two- and three-stage filters.



Figure 3.17 (a) Unwrapped S_{21} phase for one- and two-stage filter obtained from HFSS simulation and measurement, and (b) Measured group delay for the three-stage filter.

3.3.2 Filters with Side-by-Side Reversely Oriented CSRRs

Figure 3.18 (a) shows the photograph of the fabricated one-stage and five-stage filters based on the unit cell shown in Figure 3.2 (c). For the five-stage filter completely identical CSRRs are employed in order to simplify the optimization. Adjacent unit cells are longitudinally symmetrical. Only the distances between the resonators are tuned to adjust the coupling. The detailed information about the structure of the five-stage filter is



Figure 3.18 (a) Photograph of the fabricated second kind of filters, and (b) Detailed layout of the five-stage filter. The dimensions of the five-stage filter are: $a_1 = 0.25$ mm, $a_2 = 0.25$ mm, d = 0.18 mm, g = 0.22 mm, b = 3.8 mm, t = 0.9 mm, w = 12.6 mm, l = 1.55 mm, $l_1 = 7.5$ mm, $l_2 = 8.5$ mm, $w_y = 1.9$ mm, $l_x = 6$ mm.

presented in Figure 3.18 (b). In order to better match the 50 Ohm microstrip feed-line and the waveguide, a tapered-line transition is used in this particular design.

Figure 3.19 shows the simulated (dashed line) and measured (solid line) transmission responses of the filters, whereas the measured group delay for the five-stage filter is also plotted in the inset of Figure 3.19 (b). Good agreement is achieved. For the one-stage filter, we can clearly observe that it is a two-pole filter with two transmission zeros located above the passband. For the five-stage case, a highly selective passband with out-of-band rejection better than -45 dB is observed. The measured in-band return loss is below -19.5 dB, while the measured minimum in-band insertion loss is approximately 5.8 dB. The measured center frequency and 3-dB bandwidth are 5.45 GHz and



Figure 3.19 Measured and simulated transmission responses of the (a) One-stage filter and (b) Five-stage filter.



Figure 3.20 Measured wideband response of the five-stage filter compared with the simulated results of the corresponding SIW. The dispersion diagram of the unit cell is also depicted.

0.187 GHz, respectively. The small bandwidth, dielectric loss, conductor loss and the extra loss from the SMA connectors are all responsible for the high insertion loss. Also bear in mind that this filter actually is a five-stage ten-pole filter. Improved selectivity has been achieved but with increased insertion loss as tradeoff. Compared with the group delay of the previous filters shown in Figure 3.17 (b), the in-band variation of the group



Figure 3.21 (a) Photograph of the fabricated third kind of filters, and (b) Detailed layout of the two-stage filter. The dimensions of the two-stage filter are: $a_1 = 0.31$ mm, $a_2 = 0.31$ mm, d = 0.26 mm, g = 0.26 mm, b = 3.9 mm, t = 0.365 mm, w = 12.2 mm, l = 1.45 mm, $l_1 = 10.1$ mm. CSRR 2 is scaled by a factor of 1.052 on this basis.

delay for this five-stage filter is bigger, which is a result of the smaller bandwidth and the extra transmission zeros.

Figure 3.20 shows the wideband response of the five-stage filter. Also it is compared with the simulated results of the corresponding substrate integrated waveguide. The dispersion diagram for the unit cell of the filter is depicted in the inset of the Figure 3.20. A narrow forward passband is indicated by the dispersion curve.

3.3.3 Filters with Side-by-Side Reversely Oriented CSRRs

Figure 3.21 (a) shows the photograph of the fabricated filter with one or two unit cells depicted in Figure 3.9. The two-stage filter is essentially a four-pole filter and in order to synthesize its passband response, the unit-cell is revised as presented in Figure 3.18 (b). The *CSRR 2* is scaled by a factor of k = 1.052. The coupling between the *CSRR 1* and *CSRR 2* can be controlled by their distance denoted by w_t .

Figure 3.22 shows the simulated (dashed line) and measured (solid line) transmission responses of the one- and two-stage filters from 2-13.5 GHz. For the one-stage filter, two



Figure 3.22 Measured and simulated transmission responses of the (a) One-stage filter and (b) Two-stage filter.

poles with transmission zeros on both sides are obtained. Compared with other filters shown above, a steep transition and a measured stopband rejection better than -40 dB in the lower band are observed. In the upper band, stopband rejection better than -19 dB across a range from 6.5 GHz to > 13.5 GHz is achieved. The two-stage filter exhibits a passband with a center frequency at 5.36 GHz and a measured 3-dB bandwidth of

0.62 GHz. A closer look of the in-band transmission which is given in the inset of Figure 3.22 (b) shows that the measured minimum in-band insertion loss is approximately 2.63 dB, which includes the loss from the connectors, while the measured in-band return loss for this four-pole filter is below -10.2 dB. It is seen that the attenuation level in the stopband for this filter is further improved. The observed spur in the upper band corresponds to the resonance frequency of TE_{10} mode and its propagation is suppressed to a level below -30 dB.

3.3.4 Discussion on Filter Miniaturization

Previous research pointed out that besides the magnetic scatterers the waveguide miniaturization is also possible with the help of electric resonant scatterers. The filters presented here which are designed based on the platform of SIW loaded by CSRRs confirm this conclusion. The miniaturization of these filters can be summarized in two aspects: First, they are not restricted by the well known fact that the transversal dimension of the waveguide has to be at least half of a wavelength in the filling material, which applies to most rectangular metallic waveguide filters and SIW filters, through which the field distribution can satisfy the boundary conditions needed for the propagation of the electromagnetic waves along the waveguide. However in our cases the proposed waveguide filters are working below the characteristic cutoff frequency of TE_{10} mode. Their transversal dimension can be arbitrarily smaller, which is supported by the results indicated by Figure 3.16 (b). Secondly, the miniaturization obtained also refers to the longitudinal size of the SIW since the period of the resonator loads is significantly smaller than the wavelength in free space, unlike the normal inductive post SIW filters,



Figure 3.23 Working scheme of a coupled two-pole triple-band filter based on the triple-band resonators.

where the period of the posts is of the order of half-wavelength. This should be attributed to the peculiar behavior of the CSRRs, which is so called sub-wavelength resonators. This approach proposed here and verified by the experiments provides unique method for miniaturization of waveguide filters.

3.4 Multi-Band Filter Application

In this section multi-resonance CSRR-SIW resonators are proposed to achieve multipassband function below the waveguide cutoff [21], [22]. Two different types of dualband filters as well as the triple- and quadruple-band filters are presented. Filter design approach is illustrated in detail. These proposed filters are built by multi-band resonators sharing the common coupling channel which is provided by the SIW. A working scheme for the proposed two-pole triple-band coupling filter is shown in Figure 3.23. They exhibit the attractive features like high compactness, high selectivity, and low cost. It is shown that the two-pole triple-band filter can be realized with a size of $0.171 \lambda_0 \times 0.143 \lambda_0 \times 0.0056 \lambda_0$ only (λ_0 is the free- space wavelength at the center frequency of the first passband) but a stop-band rejection better that -50 dB. They are



Figure 3.24 Configuration of the proposed (a) one-pole and (b) two-pole dual-band filters based on the symmetric single-ring CSRRs.



Figure 3.25 The equivalent circuit model of the dual-resonance SIW-CSRR resonator or one-pole filter shown in Figure 3.23(a).

designed and fabricated using the standard PCB process. The measured results are consistent with the simulated data using Ansoft's HFSS software package and CST Microwave Studio.

3.4.1 Dual-Passband SIW Filter based on Symmetric Single-Ring CSRRs

A. Configuration

Figure 3.24 depicts the geometrical structures of the proposed dual-resonance unit-cell and the two-pole dual-band filter. As displayed in Figure 3.24(a), the unit-cell is realized by incorporating two integrated pairs of symmetric single-ring CSRRs on the metal surface of the waveguide. In terms of the direction of the split of the ring slot, they are face-to-face oriented. This alignment allows strong coupling between the waveguide and the CSRRs since the electric field reaches maximum in the waveguide center. The two single-ring CSRRs offer two relatively independent resonance frequencies where the inner slot ring corresponds to the higher frequency. In order to adjust the resonance frequency of the inner slot ring, a U-extension is introduced to increase its total slot length. The waveguide extent between the microstrip feed line and the CSRRs represents an inductive coupling since the wave is propagating below the waveguide cutoff as an evanescent wave. A two-pole filter can be constructed by arranging two resonators inline symmetrically as shown in Figure 3.24(b). The Rogers RT/Duroid 5880 substrate with a thickness of 0.508 mm and a dielectric constant of 2.2 is used in our designs. The metalized vias have a diameter of 0.8 mm and a center-to-center pitch around 1.45 mm.

B. Analysis of the Dual-band Resonator

Figure 3.25 presents an equivalent circuit for the resonator shown in Figure 3.24(a). The SIW is modeled as an ordinary two-wire transmission line (formed by the metal surface and the ground) loaded with infinite number of the short-circuited stubs (formed by the via-walls), which provide a shunt inductor (L_d). Wider slot width corresponds to a smaller capacitance and a higher resonance frequency. L_{ci} (i = 1 or 2) indicates the magnetic coupling mainly through the split of the slot ring between the waveguide transmission line and the ring resonators. The capacitive coupling realized by the slot coupling between the waveguide and the CSRRs is denoted by C_{ci} (i = 1 or 2). Two passbands from two resonance modes can be generated below the waveguide cutoff



Figure 3.26 The transmission responses by circuit model and full-wave simulations for the one-pole filter. The geometrical parameters are: t = 1.53 mm, l = 1.6 mm, $l_1 = 3.05$ mm, $w_1 = 1.8$ mm, s = 0.29 mm, w = 6.15 mm, g = 0.22 mm. For the outer CSRR: a = 4.6 mm, b = 4.8 mm, c = 0.15 mm, d = 0.45 mm. For the inner one: a = 3.86 mm, b = 4.06 mm, c = 0.15 mm, d = 0.2 mm. The electrical parameters are: $L_{c1} = 0.862$ nH, $C_{c1} = 0.27$ pF, $L_{r1} = 2.14$ nH, $C_{r1} = 0.755$ pF, $L_d = 0.6$ nH, $L_{c2} = 0.757$ nH, $C_{c2} = 0.621$ pF, $C_{r2} = 1.273$ pF, and $L_{r2} = 3.12$ nH.

frequency by the outer and inner CSRRs, respectively. Figure 3.26 shows the dual-band filtering response from the full-wave simulation for the resonator shown in Figure 3.24(a), compared with the results from the circuit model simulation. The field distribution at the two resonance frequencies is also plotted in the inset of Figure 3.26. It is pointed out that the waveguide cutoff frequency is above 9 GHz. The transmission zeros observed at 5.2 GHz and 8.9 GHz are due to the co-existence of the input and output magnetic and electric couplings.

The position of two bands can be independently controlled by changing their resonance frequencies. There are several factors that affect the self-resonance frequency of the CSRR, for instance, the length of split which can be used to adjust the frequency. The slot length and slot width are the two main parameters that determine the resonant mode.



Figure 3.27 Simulated $|S_{21}|$ in dB for the dual-band resonator shown in Figure 3.24(a) with varied inside CSRR size, which includes the slot width *c* and the length of U-extension l_1 . Other parameters are the same as indicated by Figure 3.26.

Increasing the length of the slot or decreasing the slot width is similar to increasing the capacitor value of C_{ri} (*i* = 1 or 2). On the other hand, increasing the length of slot will also lead to the increase of the inductor value. Both of them can be used to reduce the resonance frequency. Figure 3.27 shows the simulated *S*-parameters by changing the configuration of the inside CSRR while keeping the outer CSRR fixed. It clearly verifies our above conclusion based on the circuit model.

C. Filter Design Methodology

To meet the given specification, such as the bandwidth and selectivity, it usually requires the individual control on the external quality (Q) factor and the internal coupling coefficients. The detailed procedures are illustrated in the previous part.

The external *Q*-factors can be obtained by simulating a doubly-loaded resonator as shown in Figure 3.24(a) by Eq. (3.3). Figure 3.28(a) shows the simulated S_{21} response for different *l* (waveguide length between the CSRR and the input microstrip) while the



Figure 3.28 (a) Simulated $|S_{21}|$ for different *l* (waveguide length between the microstrip and CSRRs as shown in the inset), and (b) Calculated external *Q*-factor of the input/output resonator for both of the two bands.

relation between the calculated Q_e and the length *l* is plotted in Figure 3.28(b) for both of the two bands. Note that the vertical position (*s*) of the CSRRs could also affect Q_e .

The internal coupling coefficients between the resonators can be extracted from two split resonance frequencies by Eq. (3.2). The simulated structure is shown in the inset of Figure 3.29, which is surrounded with solid PEC walls instead of vias to expedite the simulation. The coupling coefficients can be adjusted by varying the distance (l_{dis}) between the CSRR resonators. Two pairs of eigen-modes, each of which consists of the odd and even modes, are observed. As an example, Figure 3.29 plots the vector electric



Figure 3.29 Vector electric field distribution of the even and odd modes for the lower band, resonance frequencies of the two pair modes and the calculated coupling coefficient versus the CSRR separation l_{dis} .

field for the lower pair modes. Figure 3.29 also shows the eigenmode frequencies and the calculated coupling coefficients dependent on the distance between the resonators. It is seen that the coupling is stronger when this distance is smaller. Other parameters, such as the waveguide width (w) and the position (s) of the CSRRs could also affect their coupling coefficient. These parameters can be adjusted together in order to obtain the desired coupling coefficient and finally, different bandwidth for the two passbands.

As an illustrative example, a simple dual-band two-order filter using the proposed structure is designed following the above procedures. The two passbands of this two-pole filter are located at 4.25 GHz and 5.97 GHz with a bandwidth of 161 MHz and 165 MHz, respectively. By simple circuit synthesis the coupling matrix can be obtained as:



Figure 3.30 Measured and simulated *S*-parameters of the one-pole filter. The photograph of the fabricated filters is shown in the inset.

Band I
$$\begin{cases} Q_e = 23.8 \\ M = \begin{bmatrix} 0 & 0.0454 \\ 0.0454 & 0 \end{bmatrix}$$
, Band II
$$\begin{cases} Q_e = 34.7 \\ M = \begin{bmatrix} 0 & 0.0315 \\ 0.0315 & 0 \end{bmatrix}$$

By looking at the above design curves an optimal physical dimension is obtained. After some small optimization the final filter configuration can be determined.

D. Fabrication and Measurement

The above two-pole dual-band filter is fabricated as well as a one-cell filter on the substrate of Rogers RT/Duroid 5880 with a thickness of 0.508 mm. A photograph of the fabricated filters is shown in the inset of Figure 3.30. Figure 3.30 also shows the measured and simulated transmission responses for the single-cell dual-band filter. Two measured resonances are found to be at 4.17 GHz and 6.08 GHz. It is noted that the stop-band rejection of this filter is relatively good which mainly attributes to the evanescent wave propagation below the waveguide cutoff frequency.

Figure 3.31 shows the measured and simulated results for the designed two-pole filter, where Figure 3.31(a) depicts the wideband response while Figure 3.31(b) presents a close



Figure 3.31 (a) Simulated and measured S-parameters for the two-pole dual-band filter. (b) A close look at the passband response including the circuit simulation, full-wave simulation and measured results. The parameters are: l = 0.9 mm, $l_1 = 3.05 \text{ mm}$, $w_1 = 1.8 \text{ mm}$, l_2 (l_{dis}) = 8.55 mm, s = 0.33 mm, w = 6.05 mm, g = 0.22 mm. For the outer CSRR: a = 4.6 mm, b = 4.8 mm, c = 0.15 mm, d = 0.45 mm. For the inner one: a = 3.86 mm, b = 4.06 mm, c = 0.15 mm, d = 0.2 mm.

look at the in-band performance compared with the circuit synthesized and full-wave simulated results. The two passbands are located at 4.22 GHz and 5.96 GHz in the measurement. The total filter size is $0.214 \lambda_0 \times 0.182 \lambda_0 \times 0.007 \lambda_0$, where λ_0 is the free space wavelength at the lower passband. The measured 3 dB bandwidths are 6.31% and 4.05%. The measured insertion loss is around 1.82 dB in the first band and 2.13 dB in the second band. The in-band return loss as observed is better than 12.2 dB. The insertion losses are attributed mainly to the conductor and dielectric losses because the leakage



Figure 3.32 Configuration of the dual-band filters based on the asymmetric double-ring CSRRs (a) One-pole filter, (b) Bilaterally symmetrical, and (c) Centro-symmetric two-pole filters.

from the CSRRs and apertures between via-holes are very small as calculated before. Good stopband rejection is achieved with multiple transmission zeros. Overall the measurement is in agreement with the simulation while the small discrepancy may due to the other factors such as the influence of SMA connectors and the fabrication errors.

3.4.2 Dual-Passband SIW Filter based on Asymmetric Double-Ring CSRRs

A. Configuration

Figure 3.32 shows the geometry of the proposed dual-band filters based on the asymmetric double-ring CSRRs. As displayed in Figure 3.32(a) the resonator is realized by incorporating two different double-ring CSRRs into the surface of the SIW. They have different sizes and slot widths which result in varied resonance frequencies. The two



Figure 3.33 The equivalent circuit model of the dual-resonance SIW-CSRR resonator or one-pole filter shown in Figure 3.32(a).



Figure 3.34 The transmission responses by circuit model and full-wave simulations. The geometrical parameters are: t = 1.53 mm, $l_1 = 1.75$ mm, $l_2 = 1.55$ mm, $s_1 = 2.65$ mm, $s_2 = 2.2$ mm, w = 6.15 mm. For the first CSRR: $c_1 = c_2 = 0.26$ mm, d = 0.2 mm, g = 0.26 mm, a = b = 4.5 mm. For the second one: $c_1 = c_2 = 0.38$ mm, d = 0.3 mm, g = 0.35 mm, a = 3.4 mm, b = 4.9 mm. The electrical parameters shown in Figure 3.12 are: $L_{c1} = 1.055$ nH, $C_{c1} = 0.43$ pF, $L_{r1} = 0.725$ nH, $C_{r1} = 1.52$ pF, $L_d = 0.62$ nH, $L_{c2} = 0.97$ nH, $C_{c2} = 0.773$ pF, $L_{r2} = 1.485$ nH, $C_{r2} = 2.32$ pF.

CSRRs are face-to-face oriented with respect to the outside ring split direction. In order to independently control the external coupling, the second CSRR is not square. Again the waveguide length between the microstrip feed line and the CSRRs represents an inductive coupling since the wave is propagating as an evanescent wave below the waveguide cutoff. Two-pole filters are built by arranging two resonators either in a bilaterally symmetrical form or a centro-symmetric way as shown in Figure 3.32(b) and (c). The Rogers RT/Duroid 5880 substrate with a thickness of 0.508 mm is used in our designs. The metalized vias have a diameter of 0.8 mm and a center-to-center pitch around 1.45 mm.

B. Analysis of the Dual-band Resonator

Figure 3.33 shows an equivalent circuit for the proposed resonator displayed in Figure 3.32(a). The operating principle is similar to the resonator shown in the above section. The CSRRs are modeled by means of the shunt-connected resonant tanks. Mixed electric and magnetic couplings are introduced by the slot and ring split, resulting in the transmission zeros. Again it is reminded that this circuit is a simplified version to illustrate the working principle. Two passbands from two resonance modes can be generated below the waveguide cutoff frequency by the CSRRs. Figure 3.34 shows the dual-band filtering response from the HFSS full-wave simulation for the resonator shown in Figure 3.32(a), which is compared with the results from the circuit model simulation. The field distribution at the two resonance frequencies is also plotted in the inset. The original waveguide cutoff frequency is above 9 GHz as indicated by the curve.

It is pointed out that the two resonance frequencies of the resonator, which are mainly determined by the CSRRs, can be arbitrarily controlled, making it possible to work at arbitrary passband locations. Figure 3.35 shows the different transmission responses by scaling the size of the CSRRs. The first one is obtained by scaling both of them



Figure 3.35 Simulated $|S_{21}|$ in dB for the dual-band resonator or one-pole filter shown in Figure 3.34(a) with varied CSRR size. The first (lower band) CSRR is scaled by k_1 and the second CSRR is scaled by k_2 . (a) The size of the two CSRRs is scaled simultaneously; (b) The size of the first CSRR is changed while the second one remains fixed.

simultaneously, while the second figure shows the results obtained by fixing the second CSRR and scaling the first one. Apparently it confirms that the resonance frequencies can be adjusted individually by the size or the slot width of the CSRRs.

C. Filter Design Methodology

The proposed dual-band filters here can be designed in the same manner using the procedure shown in the above section. The external quality-factors can be obtained by simulating the doubly-loaded resonator shown in Figure 3.32(a). Here the coupling is



Figure 3.36 Vector electric field distribution, resonance frequencies of the two pair modes and the calculated coupling coefficient versus the CSRR separation l_1 , where $l_2 = l_1$ -0.34 mm.



Figure 3.37 Measured and simulated *S*-parameters of the one-pole filter. The photograph of the fabricated filters is shown in the inset.

controlled by the waveguide length between the CSRR and the input microstrip. To realize individual control, the shape of the CSRRs can be adjusted instead of the square



Figure 3.0.38 Measured and simulated *S*-parameters of the bilaterally symmetrical two-pole filter shown in Figure 3.32(b). The parameters are: $l_1 = 9.5$ mm, $l_2 = 3.18$ mm, $l_3 = 3.36$ mm, $s_1 = 2.65$ mm, $s_2 = 2.3$ mm, w = 6.15 mm.

type as indicated by Figure 3.32(a). Also it is noted that the CSRRs can be shifted vertically to tune the external couplings.

The coupling coefficients between the resonators can be extracted from two split resonance frequencies and calculated using Eq. (3.3). Without loss of generality the centro-symmetric case is chosen here and the structure is shown in the inset of Figure 3.36. For simplicity it is surrounded with solid metallic walls instead of vias. The coupling coefficients can be individually adjusted by changing the distance (l_1 and l_2) between the resonators. Two pairs of eigen-modes, each of which consists of the odd and even modes, are observed. Figure 3.36 plots the electric field distribution of the lower band pair modes. Figure 3.36 also shows the eigenmode frequencies and the calculated coupling coefficients by changing the distance between the two resonators. It is seen that the coupling is stronger when this distance is smaller. It is also noted that here to increase the coupling for the upper band, the corresponding CSRRs are placed closer compared with the lower band pair. In this way their couplings can be adjusted separately. The coupling coefficients for the bilaterally symmetrical case can be similarly extracted. However, it is interesting to point out that to achieve the same coupling the required distance between the CSRRs is smaller for the centro-symmetric case than that for the bilaterally symmetrical case. Therefore the filter size can be further decreased by using the centro-symmetric type.

D. Fabrication and Measurement

Two two-pole dual band filters, together with the one-cell filter, are designed and implemented on the substrate of Rogers RT/Duroid 5880 with a thickness of 0.508 mm using the PCB process. A photograph of the fabricated devices is shown in the inset of Figure 3.37. The measured and simulated transmission responses for the single-cell dual-band filter are shown in Figure 3.37. Two resonances at measured to be at 4.03 GHz and 5.77 GHz, each of which is followed by one transmission zero.

Figure 3.38 shows the simulated and measured results for the designed two-pole bilaterally symmetrical filter. The two passbands are located at 4.06 GHz and 5.81 GHz. And the total size is $0.215 \lambda_0 \times 0.189 \lambda_0 \times 0.007 \lambda_0$, where λ_0 is the free space wavelength of the lower passband frequency. The measured 3 dB bandwidths are 3.83% and 3.36%. The measured insertion loss is around 2.72 dB in the first band and 1.98 dB in the second band. The in-band return loss as observed is better than 14 dB.

Figure 3.39 shows the simulated and measured transmission responses for the two-pole centro-symmetric filter. The passbands are measured to be at 4.05 GHz and 5.8 GHz, respectively. It exhibits an electrical size of $0.199 \lambda_0 \times 0.187 \lambda_0 \times 0.007 \lambda_0$. It has a measured 3 dB bandwidth of 4.59% in the lower band and 3.58% in the upper band. It



Figure 3.39 Measured and simulated transmission responses for the two-pole centro-symmetric filter shown in Figure 3.32(c). (a) *S*-parameters, and (b) In-band *S*-parameters the group delay. $(l_1 = 8.88 \text{ mm}, l_2 = 2.95 \text{ mm}, l_3 = 3.12 \text{ mm}, s_1 = 2.65 \text{ mm}, s_2 = 2.3 \text{ mm}, w = 5.9 \text{ mm})$



Figure 3.40 Configuration of the proposed (a) one-pole and (b) two-pole triple-band filters.
has less than 2.25 dB insertion loss and greater than 18 dB return loss in both of the two bands. It is also found in the simulation that each of the two passbands is followed by two transmission zeros which greatly improves the selectivity and stopband rejection. Figure 3.39(b) shows a close look at the *S*-parameters and the group delay in the two bands.

3.4.3 Design of Triple- and Quadruple-Passband Filters

Triple- and quad-band filters can be designed based on the proposed dual-passband filters shown in the above two sections. Here in this section we will show them separately with several design examples presented.

A. Triple-band Filters

The geometrical structure of the proposed triple-passband is depicted in Figure 3.40. Two single-ring CSRRs and a double-ring CSRR are adopted to achieve three different resonance frequencies. The double-ring CSRR is responsible for the lowest band, while the outer and inner single-ring CSRRs contribute to the second and third passbands, respectively. As demonstrated before these resonance frequencies can be arbitrary selected which are mainly determined by the configuration of the CSRRs. The external and internal couplings are also realized by the way of evanescent wave propagation through SIW. The two-pole filter can be designed in the same manner as in Section II. Note that there would be three pairs of modes. Besides the distance between CSRRs, both the vertical position (s_{i} , i = 1 or 2) and the split width (d) of the CSRRs can be used to control their coupling coefficients.

The triple-passband filters were also fabricated on the same substrate of Rogers 5880 with a height of 0.508 mm. Figure 3.41(a) shows a photograph of the fabrication. Figures



Figure 3.41 (a) A photograph of the fabricated triple-band filters, and (b) A photograph of the fabricated quad-band filters.



Figure 3.42 Measured and simulated S-parameters of the one-pole triple-band filter.

3.42 and 3.43 illustrate the full-wave simulation and measurement responses for both the one-pole and two-pole triple-band filters. For the two pole filter, the total size excluding the microstrip transition is 15.6 mm × 13.1 mm, i.e., only approximately 0.171 $\lambda_0 \times 0.143$ λ_0 , where λ_0 is the free-space wavelength at the center frequency of the first passband. The three passbands are measured at 3.27 GHz, 4.75 GHz and 6.3GHz. The measured 3-dB fractional bandwidths are 3.0%, 2.5% and 2.6%. The measured passband return losses are all better than 14 dB, while the insertion losses are approximately 3.23, 3.69 and 1.67 dB at the first, second, and third passbands, respectively. The relatively large



Figure 3.43 Measured and simulated transmission responses for the two-pole triple-filter shown in Figure 3.40(b). (a) Wide band S-parameters, and (b) In-band response. The filter parameters are: $w_1 = 1.2 \text{ mm}$, $l_1 = 3.05 \text{ mm}$, $l_2 = 8.7 \text{ mm}$, $l_3 = 3.45 \text{ mm}$, $l_4 = 3.2 \text{ mm}$, $s_1 = 0.29 \text{ mm}$, $s_2 = 0.236 \text{ mm}$, w = 6.15 mm. For the upper outer ring: a = 4.7 mm, b = 4.9 mm, c = 0.15 mm, d = 0.2 mm. For the upper inner ring: a = 3.96 mm, b = 4.16 mm, c = 0.15 mm. For the doublering CSRR: a = 4.7 mm, b = 5.1 mm, c = 0.208 mm, d = 0.144 mm, and g = 0.208 mm.

insertion loss in the lower band is mainly due to the high conductor loss, where very strong current is observed around the CSRRs. There are two transmission zeros after each passband which is due to the mixed capacitive and magnetic couplings. As a result, good selectivity and stopband rejection are achieved.

B. Quadruple-band Filters

As a design example here a filter with a quad-passband response is realized with four different single-ring CSRRs incorporated on the surface which is shown in Figure 3.44.



Figure 3.44 Configuration of the proposed (a) one-pole and (b) two-pole quadruple-band filters.



Figure 3.45 Measured and simulated S-parameters of the one-pole quadruple- band filter.

The outer CSRR on the upper side is responsible for the first passband and inner CSRR on the upper side contributes to the second one. The third and fourth passbands are mainly generated by the outer and inner CSRRs on the lower side. This filter is built as a simple combination of two different types of dual-band filters shown in Section II and III. The CSRR size can be determined according to the passband locations. Then the filter can be designed using the same procedures discussed above. Four coupling channels are combined on the single SIW structure. The coupling coefficient can be adjusted by



Figure 3.46 Measured and simulated transmission responses for the two-pole quad-filter shown in Figure 3.44(b). (a) Wide band S-parameters, and (b) In-band response. The filter parameters are: $l_2 = 8.6$ mm, $l_3 = 3.4$ mm, $s_1 = 0.29$ mm, $s_2 = 0.25$ mm, w = 6.15 mm. For the upper outer ring: a = 4.6 mm, b = 5.75 mm, c = 0.15 mm, d = 0.45 mm. For the upper inner ring: a = 3.86 mm, b = 5.01 mm, c = 0.15 mm, d = 0.2 mm, $w_1 = 2$ mm, $l_1 = 3.05$ mm. For the lower outer ring: a = 3.3 mm, b = 6 mm, c = 0.15 mm, d = 0.45 mm. For the lower inner one: a = 2.58 mm, b = 5.28 mm, c = 0.15 mm, d = 0.2 mm, $w_1 = 1.55$ mm, and $l_1 = 3.4$ mm.

changing the separation between CSRRs. However, there is some limitation in controlling the bandwidth independently. Also it should be pointed out that when the split of the ring slot is narrow the unloaded *Q*-factor of the CSRR would be increased leading to a smaller bandwidth.

Figure 3.41(b) shows a photograph of the fabricated one-pole and two-pole quad-band filters. They are also designed on the Rogers 5880 substrate with a thickness of 0.508mm. Figures 3.45 and 3.46 present the simulated and measured results for the one-pole and



Figure 3.47 Configuration of the proposed SIW-CSRR diplexer ($t_1 = 0.85 \text{ mm}$, $t_2 = 3.42 \text{ mm}$, $l_1 = 5.50 \text{ mm}$, $l_2 = 1.643 \text{ mm}$, $l_3 = 2.985 \text{ mm}$, $l_4 = 0.518 \text{ mm}$, s = 1.53 mm, $w_1 = 12.21 \text{ mm}$, and $w_2 = 11.52 \text{ mm}$).

two-pole filters, respectively, where a close look at the in-band response for the two-pole filter is plotted in Figure 3.45(b). For the two-pole filter, the overall size is 15.4 mm × 13.1 mm, i.e., approximately $0.196 \lambda_0 \times 0.167 \lambda_0$, where λ_0 is the free-space wavelength of the first band center frequency. Other dimensions are shown in the caption of Figure 3.46. The measured center frequencies are 3.82GHz, 5.02GHz, 6.12GHz, and 9.07GHz. The insertion losses are 1.77, 3.61, 3.47 and 4.47dB, respectively. The measured 3-dB fractional bandwidths are 7.2%, 1.58%, 1.78% and 1.34% for the four passbands. Small discrepancy is mainly due to the manufacturing tolerances.

3.5 Miniaturized Diplexer Design

3.5.1 Configuration

A miniaturized and compact SIW diplexer implemented by CSRRs operated in a waveguide format is proposed and presented. Figure 3.47 shows the layout of the



Figure 3.48 Vector electric field distribution, resonance frequencies of the two excited modes and the calculated coupling coefficient versus the distance w_t .

diplexer. It is a three-port device with a transmitter filter and a receiver filter cascaded inline. A direct 50- Ω microstrip line inset-feeding is adopted on the top working as the T-junction in order to save the space. This technique, also known as the CPW-SIW transition, is commonly used for impedance matching in the SIW technology. The slot coupling and inset length of the feeding can be used to control the external quality factor. The channel filter is constructed by the CSRRs incorporated in an SIW as shown in Figure 3.9. The Rogers RT/Duroid 5880 substrate with a thickness of 0.508 mm and a relative permittivity of 2.2 is used in our design. The metalized vias have a diameter of 0.8 mm and a center-to-center pitch around 1.48 mm.

3.5.2 Diplexer Synthesis

The channel filter can be designed using the coupled resonator method as illustrated before. Figure 3.48 presents the curve of the coupling coefficient which is calculated



Figure 3.49 Simulated $|S_{21}|$ in dB for the two-pole filter with different w_t .

based on the two resonance frequencies. The bandwidth of the channels filters can be tuned by the coupling. Figure 3.49 shows the simulated S_{21} for the filter with different spacing (w_t) between the CSRRs. A stronger coupling is obtained when they are close to each other resulting in a larger bandwidth.

After obtaining two filters with desirable features, the T-junction as shown in Figure 3.47 is designed and optimized. By checking the input impedance we can purposefully and selectively tune the inset length t_2 , slot width t_1 and the distance between the feeding and resonators (l_4) in order to get a low in-band reflection. The two passbands can be very close to each other by changing to center frequency of the channel filters.

Here one diplexer working in *C*-band based on two different channel filters discussed above is designed and optimized using the Ansoft's HFSS package. The final diplexer response is shown in Figure 3.50. It is seen that high selectivity, high isolation and high stopband rejection with low loss are achieved.



Figure 3.50 Simulated transmission responses and isolation for the diplexer.



Figure 3.0.51 Measured and simulated channel filter return losses ($|S_{22}|$ and $|S_{33}|$).

3.5.3 Fabrication and Measurement

To verify the simulated results shown above, the diplexer is experimentally implemented on the substrate of Rogers RT/Duroid 5880 with a thickness of 0.508 mm using the PCB process. A photograph of the diplexer is shown in the inset of Figure 3.51 which appears very compact (about 17.5 mm \times 14 mm). It was measured using an Agilent 8510C network analyzer.



Figure 3.52 Measured diplexer transmission responses ($|S_{11}|$, $|S_{21}|$, $|S_{31}|$ and $|S_{32}|$).

 Table 3.2
 A Comparison between the Proposed Diplexer and the References

	3-D Size	$ S_{21} , S_{31} $ (Insertion Loss)		$ S_{21} , S_{31} $ (Suppression)	
		Channel 1	Channel 2	Channel 1	Channel 2
This Work	$0.27 \ \lambda_0 \!\!\times\!\! 0.217 \ \lambda_0 \!\!\times\!\! 0.008 \ \lambda_0$	1.6 dB	2.3 dB	43dB @ 4.66GHz	28dB @ 5.80GHz
Ref. 23 (part 1)	$0.17 \ \lambda_0 \! imes \! 0.272 \ \lambda_0 \! imes \! 0.003 \ \lambda_0$	2.7 dB	2.8 dB	40dB @ 1.50GHz	48dB @ 2.00GHz
Ref. 24 (part 2)	$0.187 \ \lambda_0 \! \times \! 0.30 \ \lambda_0 \! \times \! 0.003 \ \lambda_0$	2.8 dB	3.2 dB	38dB @ 1.50GHz	39dB @ 1.76GHz
Ref. 5	$2.71 \ \lambda_0 \! \times \! 3.35 \ \lambda_0 \! \times \! 0.009 \ \lambda_0$	2.6 dB	3.2 dB	55dB @ 5.42GHz	55dB @ 5.96GHz

Where, the " λ_0 " is regarding to the free-space wavelength of the first channel center frequency. The size compared here does not include the microstrip feeding. All the present results are the measured performance. And all the channels of the listed diplexers have a moderate fractional bandwidth (3% ~ 5%).

Figure 3.52 shows the measured reflection and transmission coefficients ($|S_{11}|$, $|S_{21}|$ and $|S_{31}|$), as well as the isolation ($|S_{32}|$) for the diplexer. The measured insertion losses at the two bands are approximately 1.60 dB and 2.30 dB, respectively, which include the extra loss from the SMA connectors. The measured return loss at the lower and higher bands is above 12.9 dB. The out-of-band rejection of each channel filter is better than 30 dB. To better characterize the performance of the diplexer, the simulated and measured channel return losses ($|S_{22}|$ and $|S_{33}|$ in dB) are plotted in Figure 3.51. As seen the measured return losses in both of the two channels are better than 13 dB, which agree well with the

simulation. Table 3.1 provides a performance comparison between the proposed diplexer and other designs in literatures, including two miniaturized designs using the microstrip [23] and one existing conventional SIW diplexer [24].

3.6 Dual-band Oscillator based on Cavity-Backed CSRR Resonator

In this section, a novel *C*-band low phase noise dual-band oscillator using a reconfigurable cavity-backed CSRR resonator is proposed and presented based on the SIW technology. The resonator consists of a PIN diode switch and a CSRR resonator embedded in an SIW cavity. It is able to provide two different resonance frequencies by selecting different diode modes. The design procedure and experimental verification are provided in the following part.

3.6.1 Design of SIW-CSRR Dual-Band Oscillator

The first stage for implementing this dual-band oscillator is to design a reconfigurable SIW-CSRR resonator. Figure 3.53(a) describes the physical layout of the proposed reflective cavity resonator. The circuit outside the resonator is for DC bias. The vias form a closed cavity structure. An inset CPW feeding is employed. A PIN diode, MADP-017015-1314 from MA-COM Solution Inc., across the inside ring slot of the CSRR is used to control the resonance frequency. When the diode is ON, it is a double-ring CSRR and it becomes a partially single-ring CSRR when the diode is OFF. Note that the outside microstrip line length does not affect the resonance frequency. However, it could change the phase of the reflected wave which is an important parameter for oscillator design. The



Figure 3.53 The proposed reconfigurable SIW-CSRR resonator. (a) Configuration, (b) Simulated reflection coefficient.

simulated reflection coefficient is shown in Figure 3.53(b). When the PIN diode is turned on, the CSRR becomes a double-ring resonator and the resonance frequency of the combined resonator drops down to 2.71 GHz from the original 3.82 GHz. It should be pointed out that these two resonance frequencies can be easily adjusted by changing the split length, as well as the length and width of the two ring slots of the CSRR.

Figure 3.54 depicts the geometrical layout of the proposed dual-band oscillator. It is designed on the Rogers5880 substrate with a thickness of 0.508 mm and a dielectric constant of 2.2. It is composed by a reconfigurable reflective SIW-CSRR resonator, transistor, DC biasing circuit, and the input and output feeding network. Stub A is for the matching of the reflective SIW-CSRR resonator which is switchable with a PIN diode. The PIN diode used here at Stub A position is MADP-008120-12790T surface mount diode from MA-COM Solution. Stub B is used for output matching. The active device used here is an Avgao ATF-34143 low noise pseudomorphic high electron-mobility



Figure 3.54 Geometrical layout of the proposed dual-band oscillator.

transistor (pHEMT). Its two source ports are connected to a shorted stub as shown in the figure. The length of the shorted stub is adjusted to make sure that the transistor is in an un-stable state at both of two frequencies. The drain port is connected to the output through a gap coupling. The gate port connects the resonator using a microstrip line and a switchable stub. The length of the microstrip line at the gate side is used for establishing the required negative conductance and meeting the oscillation conditions $|\Gamma r| \times |\Gamma in| > 1$ and Arg (Γr) = Arg (1/ Γin) at the two resonance frequencies. Since the cavity is essentially connected to the ground, the oscillator has the gate voltage of Vgs = 0 V.

3.6.2 Measured Results

Figure 3.55 shows a photograph of the fabricated dual-band oscillator. The oscillator was measured using a spectrum analyzer HP 8562A. Figure 3.56 shows the measured results. It is noted that small frequency shift is observed which would affect the matching and oscillating condition. Some mechanical tuning using small pieces of copper sheet is performed before achieving the best results. Both of the two stubs are tuned a little to



Figure 3.55 Photograph of the fabricated dual-band oscillator.



Figure 3.56 Measured spectrum response at (a) 2.675 GHz, and (b) 3.77 GHz.

obtain good oscillation at the two frequencies. The final resonance frequencies are 2.675 and 3.77 GHz, respectively. The output power at these two frequencies is 5.33 and 10.83



Figure 3.57 Measured phase noise at the two resonance frequencies of the oscillator.

dBm. Figure 3.57 plots the measured phase noise at these two different frequencies. It is seen that at a 100 KHz offset the phase noise is 105.5 and 99.3dBc/Hz, respectively. Table I shows a detailed performance summary for this oscillator, including the figure of merit (FOM) and the magnitude of the harmonics. The FOM is calculated as [5]:

$$FOM = -L(\Delta) + 20\log(\frac{f_0}{\Delta f}) - 10\log(P)$$
(3.4)

where *L* is the phase noise at the offset Δf , f_0 is the oscillation frequency, Δf is the offset, and *P*(mW) is the DC power consumption of the VCO. Note that the power consumption for this transistor is little higher than other transistors, which slightly brings down the FOM. Less power consumption can be obtained by choosing a better low noise transistor. Overall, good performance is achieved for this dual-band oscillator.

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Chapter 4

Composite Right/Left-Handed Metamaterial Resonator Antennas

Composite right/left-handed (CRLH) transmission line (TL) materials are understood to be artificially engineered materials that exhibit some unusual properties. They can be used to develop leaky-wave antennas with a full-space beam steering capability as shown before [1-4]. They can also be designed as resonant-type antennas which offer an alternative solution for antenna miniaturization or multi-band operation [5-8]. Much attention has been drawn towards the zeroth-order resonance antennas because of their infinite wavelength operation and omni-directional radiation patterns [6-8]. Most of these resonant-type CRLH antennas are developed based on the microstrip techniques and suffer from low radiation efficiency [6], [7]. A compact inductor-loaded TL antenna based on the zeroth-order resonance with extended bandwidth is proposed in [9] achieving a reasonable radiation efficiency. Many other compact antenna designs based on different technologies are also proposed due to the continuing demand to miniaturized communication systems [10-13]. However, there are not too many papers talking about antenna design using the negative order resonances. In [5] there are some small antennas designed based on the -1st order mode but the efficiency is too low.

In this chapter we will present two types of CRLH metamaterial resonator antennas based on the negative order modes with improved radiation efficiency. The first one is slot antennas designed using the SIW technology. The second one is low-profile patch antennas inspired by mushroom metamaterial resonators. Their working principle is illustrated. Experimental results are also provided to verify the simulation. This chapter will be divided into two sections introducing those two antennas, respectively.

4.1 Miniaturized SIW Slot Antennas with Negative Order Modes

The proposed antennas here are relatively simple and low-cost. They are operated on the negative order resonance, which distinguishes them from conventional waveguide transverse slot antennas [14], [15]. These proposed antennas can be classified into two categories: the open-ended type and the short-ended type. Because of an LH region operation, the open-ended antenna, which behaves as a quasi-half-wavelength resonator, shows a smaller size compared with the short-ended antenna, which acts like a quasiquarter-wavelength resonator. This property differs from that of the RH resonances. On the other hand, the short-ended antenna provides a higher gain owing to a completely cavity-backed configuration. Four antennas with one or two unit cells are designed and fabricated. Good agreement is observed between the simulation and measurement.

4.1.1 Antenna Configurations

Figure 4.1(a) shows the geometry of the fundamental CRLH-SIW unit cell. The unitcell is the same with the element shown in Chapter 2. The top layer and ground layer are connected by periodic via arrays forming an SIW structure. The slot is etched on the top surface of the waveguide. The slot serves as the radiator as well as a series capacitor. Figure 4.1(b) and (c) presents the one-element antenna configurations developed on the



Figure 4.1 Configurations of the proposed CRLH-SIW slot structures (a) fundamental unit cell, (b) the open-ended antenna with one element, and (c) the short-ended antenna with one element.

proposed unit cell. Both of them are synthesized on the substrate of Rogers 5880 with a thickness of 1.27 mm and a relative permittivity of 2.2. For fabrication convenience all the metallic via holes are chosen to have a diameter of 0.8 mm and a center-to-center spacing around 1.5 mm. The first antenna shown in Figure 4.1(b) is an open waveguide structure leaving both of the two ends unclosed. On the other hand, the second antenna displayed in Figure 4.1(c) is a closed waveguide model making it as a cavity-backed slot antenna. Both of them are excited by a piece of 50-Ohm microstrip line. Since they are operated below the cutoff, the waveguide length between the microstrip feeding and the slot is important for impedance matching. For the short-ended antenna an inset feeding is adopted to adjust the input impedance.



(a)



Figure 4.2 Structure of the two-stage CRLH SIW slot antenna with (a) open-ended boundaries, and (b) short-ended boundaries.

Figure 4.2 shows the antenna configurations consisting of two elements. The substrate of Rogers 5880 with a relative dielectric constant of 2.2 and a thickness of 1.27 mm is also used here. Similarly the first antenna shown in Figure 4.2(a) is open-ended and the second antenna is a short-ended structure. This small difference in the boundary condition results in a difference not only in the antenna performance but also in the working resonance which will be shown in the next section.

4.1.2 Antenna Operating Principles

Here a detailed investigation on the fundamental unit cell is carried out. The equivalent circuits are extracted and the dispersion diagram is presented. The working principles of the single-element antennas with open and shorted ends are discussed and compared. Following this, a complete comparison between the different resonances, including the



Figure 4.3 Equivalent circuits for the symmetrical CRLH unit cells (a) T-type model (b) π -type model.

negative order, zeroth-order and positive order modes, are presented by investigating a two-stage open-ended antenna.

A. Dispersion Relation and Equivalent Circuits

The equivalent circuit for a typical symmetrical CRLH unit cell, like the one used for a mushroom structure shown in [6], [7], is depicted in Figure 4.3(a) named T-type model here, in which the LH capacitor is located at both ends of the unit cell. For our unit cell shown in Figure 4.1(a), the LH capacitor is at the center thus it is characterized by an equivalent circuit described in Figure 4.3(b), named π -type model as discussed earlier. Flexible shunt inductance value $L_{\rm L}$ can be obtained by choosing different waveguide widths, which will also lead to the change of the waveguide cutoff frequency. By changing the slot width and length, the value of the series capacitor $C_{\rm L}$ can be adjusted conveniently, which determines the position of LH region. For instance, when the slot width is decreased or its length is increased $C_{\rm L}$ will become larger, and the LH band will move to a lower frequency thus a bandgap will be generated between the LH and RH ranges.

Figure 4.4 presents the dispersion diagrams obtained from the CRLH-SIW unit cell by



Figure 4.4 Dispersion diagrams for the unit cell shown in Figure 4.1(a) and the corresponding equivalent circuit shown in Figure 4.3(b). The dimensions for the unit cell are: $w_1 = 0.31$ mm, $w_2 = 0.46$ mm, $w_3 = 9.6$ mm, n = 9, p = 8.41 mm, l = 3.29 mm. The equivalent circuit parameters are: $L_L = 0.0595$ nH, $C_L = 0.459$ pF, $L_R = 0.8218$ nH, $C_R = 2.958$ pF.

full-wave simulation with Ansoft's HFSS package and the equivalent circuit shown in Figure 3.3(b) with all the parameter values shown in the caption. It is shown that the extracted circuit elements describe the dispersion relation of the unit cell very well. Rich information is contained in this dispersion diagram. There are two zeroth-order resonance frequencies which delimit the upper and lower edges of the bandgap, as given by the following equations [16]:

$$f_{\rm se} = \frac{1}{2\pi\sqrt{L_{\rm R}C_{\rm L}}}, \quad f_{\rm sh} = \frac{1}{2\pi\sqrt{L_{\rm L}C_{\rm R}}}$$
 (4.1)

These two points are referred to as infinite wavelength points ($\beta = 0$). In the balanced case they equal to each other and the bandgap vanishes. Usually only one particular zeroth-order resonance will be excited which depends on the circuit values and the

boundary conditions. In [16] it is shown that for the open-ended resonator, it is determined by f_{sh} . And for the short-ended case, it is represented by f_{se} while there is no resonance occurring at f_{sh} . Here for the unit cell shown in Figure 4.1(a) with the circuit model depicted by Figure 4.3(b) which terminates the unit cell with the LH inductor, the zeroth-order resonance occurs at f_{se} . The resonance frequencies of different order modes for an *M*-stage CRLH TL can be found on the dispersion curve when the following condition satisfies [16]:

$$\theta_{\rm M} = \beta p_{\rm M} = \beta M p = n\pi$$

$$\beta p = \frac{n\pi}{M} \begin{cases} n = 0, \pm 1, \dots, \pm (M-1) & \text{for } \mathbf{T} \text{ - type unit cell} \\ n = 0, \pm 1, \dots, \pm M & \text{for } \pi \text{ - type unit cell} \end{cases}$$
(4.2)

It should be noted that the difference in response between the T-type and π -type models lies in their circuit structures. The voltage difference between the two ports (from positive to negative) can be built with the help of a centered series capacitor so that the odd modes can be excited. Therefore for the π -type model the $\pm 1^{st}$ order resonances can be excited with only one unit cell. However it requires two unit cells for the T-type model in order to obtain the centered series capacitor and the $\pm 1^{st}$ order resonances.

Here we investigate a circuit by cascading two unit cells for both the T-type and π -type models as shown Figure 4.5. The resonators, which have the dispersion curve shown in Figure 4.4, are coupled to the input/output port by a small capacitor $C_{\rm C}$ (0.01 pF) in order to clearly observe all the resonances. The resulting transmission responses are presented in Figure 4.6. Since the input impedance varies with frequency only the +1st mode gets perfect matching. As predicted two extra resonances ($\pm 2^{nd}$ order modes) have been



Figure 4.5 Two-cell CRLH resonators (a) T-type model (b) π -type model.



Figure 4.6 Resonance peaks of the two-cell CRLH resonators shown in Fig. 5. The circuit parameters are the same with that shown in Figure 4.4: $L_{\rm L} = 0.0595$ nH, $C_{\rm L} = 0.459$ pF, $L_{\rm R} = 0.8218$ nH, $C_{\rm R} = 2.958$ pF, and $C_{\rm C} = 0.01$ pF.

excited for the π -type model. Here, the $\pm 2^{nd}$ order resonances are excited independently, instead of the spurious modes, of the $\pm 1^{st}$ order resonances in the lumped circuit. They appear as the even modes which are symmetrically distributed along the circuit. The zeroth-order resonance occurs at the upper edge of the bandgap which corresponds to a zero phase delay (infinite wavelength) as observed from the circuit response. Based on



Figure 4.7 Simulated reflection coefficient of the one-element open-ended slot antenna shown in Figure 4.1(b). The geometrical parameters are: $w_1 = 0.31$ mm, $w_2 = 0.46$ mm, $w_3 = 9.6$ mm, n = 9, $c_1 = 3.89$ mm, $c_2 = 2.35$ mm, l = 3.29 mm, $w_s = 3.9$ mm. (*n* is the number of fingers)

the above analysis we know that for a single unit cell shown in Figure 4.1(a), the zeroth and the $\pm 1^{st}$ order resonances can be excited. Now we are going to investigate their antenna applications with those negative order modes.

B. Single-Element Antennas

The configurations of the single-element antennas are shown in Figure 4.1(b) and (c). The first antenna is open-ended while the second antenna is short-ended, both of which are fed directly by a piece of microstrip line. Figure 4.7 shows the simulated reflection coefficient of the open-ended antenna with the design parameters listed in the caption. The -1^{st} order and the zeroth-order resonances are clearly observed at 7.26 GHz and 11.27 GHz, respectively. The $+1^{st}$ order resonance can also be determined by looking into the input impedance which is depicted in the inset of Figure 4.7. It is found that the resonance frequency for the $+1^{st}$ order mode is 16.19 GHz but the best matching point is at a slightly higher frequency. Basically this result agrees with the dispersion curve while



Figure 4.8 Simulated electric field distribution in *x-y* plane in the substrate and the extracted magnitude curve along the *x*-direction for the (a) -1^{st} mode at 7.26 GHz, (b) 0^{th} mode at 11.27 GHz, and (c) $+1^{st}$ mode at 16.19 GHz.

small discrepancy is expected since it is open-ended instead of having a periodic boundary condition and the size is not exactly the same. Figure 4.8 shows the simulated electric field distribution observed in x-y plane at the middle of dielectric and the extracted magnitude curves along the x-direction centered in the y-axis (middle of the structure) for these three modes. The x-axis value shows the position of the observing



Figure 4.9 Simulated reflection coefficient of the one-element short-ended slot antenna shown in Figure 4.1(b). The geometrical parameters are: $w_1 = 0.31$ mm, $w_2 = 0.46$ mm, $w_3 = 9.6$ mm, n = 9, $d_1 = 3.45$ mm, $d_2 = 2.7$ mm, l = 3.29 mm, $w_s = 3.9$ mm, $t_1 = 1.4$ mm, $t_2 = 0.5$ mm.



Figure 4.10 Simulated electric field distribution in the substrate and the extracted magnitude curve along the *x*-direction for the (a) -1^{st} mode at 7.75 GHz, and (b) the 0th mode at 11.86 GHz.

point as indicated in Figure 4.1, which is along the direction of the wave propagation. These magnitude curves are used to approximate the field intensity in order to better demonstrate the characters of the resonances. As seen the -1^{st} and $+1^{st}$ order resonances are very similar to a half-wavelength resonator. Strong electric field has been generated inside the slot because of the opposite field magnitude at the slot boundaries which helps to achieve a good radiation going to the broadside. The cutoff frequency of the corresponding SIW TL is at 11.3 GHz. A significant degree of miniaturization is achieved by an LH region operation.

By closing the boundary a cavity-backed slot antenna is created as shown in Figure 4.1(c). An inset feeding is used for impedance matching. Under this configuration the -1st order resonance switches to a quasi-quarter-wavelength resonator and the zeroth-order resonance is eliminated since the uniform field is forced to be zero by the boundary condition. Figure 4.9 shows the simulated reflection coefficient for this short-ended antenna. The -1st order is clearly observed and its resonance frequency is moved up to 7.75 GHz. This can be predicted by looking to the dispersion curve shown in Figure 4.4. Total refection happens at the zeroth-order resonance frequency and this can be confirmed by checking the input admittance (not the impedance) which is plotted in the inset of Figure 4.9. The +1st mode can be observed from Figure 4.9 but is very weak since it is not matched. It can also be found on the input impedance curve. Figure 4.10 shows the electric field distribution and the extracted magnitude curve along the x-direction for the -1^{st} order and the eliminated 0^{th} order modes. The -1^{st} order mode is very similar to an ideal quarter-wavelength resonator. By moving the right-side shorting vias closer to the slot, it approaches better to a quarter-wavelength resonator. This antenna has a relatively larger size in terms of wavelength compared to the first half-wavelength antenna, which



Figure 4.11 Simulated and measured reflection coefficient of the two-stage open-ended slot antenna shown in Figure 4.2(a). The unit cell dimensions are shown in Figure 4.4. Other parameter values are: $c_1 = 3.2$ mm, $c_2 = 3.1$ mm, $w_s = 3.9$ mm, p = 8.41 mm.

is the particularity of negative order resonances.

C. Two-Element Antennas

The configurations of the two-element antennas are shown in Figure 4.2. Figure 4.11 presents the simulated reflection coefficient for the open-ended two-stage antenna. Five resonances are excited between 5 GHz and 18 GHz. Here we will give a detailed comparison for these five observed modes. Table 4.1 lists the resonance frequency, field distribution, resonance type, radiation pattern and the simulated gain for the observed five modes. The magnitude curves of the resonances are in agreement with our prediction and the small discrepancy mainly comes from the influence of the input feeding. From these curves we can have a rough idea about their radiation patterns. For the -2^{nd} and $+2^{nd}$ order resonances, since the electric field inside the two slots has opposite direction, their radiation cancels each other in the broadside direction. For the other three modes, the peak radiation all goes to the broadside as shown in Table 4.1. From their radiation

	Frequency	Sim. Electric Field Distribution	Resonance Type	Radiation Pattern	Sim. Gain
-2 nd order	6.858 GHz		ideal Observed	Y - V - X	2.53 dBi
-1 st order	7.31 GHz		Ideal Observed	Y - X	5.29 dBi
0 th order	10.68 GHz		ideal Ideal Observed	× ×	5.48 dBi
+1 st order	12.83 GHz		Ideal Observed	x	5.93 dBi
+2 nd order	16.72 GHz		Ideal Observed	x x	7.86 dBi

Table 4.3 A Comparison for the Different Modes Excited by the Two-stage Open-ended Antenna

patterns and the simulated gain, we find that they are suitable for antenna applications. Electrically small antenna usually means low gain. However the -1st order resonance still gives an acceptable gain with a small size in wavelength.

The short-ended two-element antenna has similar characteristics. The -2^{nd} order resonance in this case consists of a quasi-half-wavelength resonator near the feeding and a quasi-quarter-wavelength resonator close to the other end. Also, the -1^{st} order modes is



Figure 4.12 Photograph of the fabricated CRLH-SIW slot antennas.

still similar to a quarter-wavelength resonator. The zeroth-order is suppressed by the shorted boundary. Because of its cavity-backed configuration this antenna working on the -1st order provides a higher gain compared with the open-ended case which will be shown later in Table 4.2.

4.1.3 Experimental Verification

This section provides the experimental results in order to validate our proposal. A performance comparison is then carried out to fully demonstrate their characteristics. Figure 4.12 shows the photograph of the fabricated four CRLH-SIW slot antennas. They are open-ended or short-ended antennas with one or two unit elements. They are all operated on the -1st order resonance. Rogers 5880 with a thickness of 1.27 mm, a relative permittivity of 2.2 and a loss tangent of 0.0009 at 10 GHz is used as the dielectric substrate. They are fabricated and measured in the UCLA Microwave Electronics Laboratory.

Figure 4.13 shows the measured reflection coefficient and radiation patterns in two orthogonal cutting planes for the one-stage open-ended antenna. This antenna has a



Figure 4.13 Measured (solid line) and simulated (dashed line) results for the one-stage openended antenna (the dimensions are shown in Figure 4.7). (a) reflection coefficient, (b) the normalized radiation patterns in *E*-plane (x-z plane), and (c) the normalized radiation patterns in *H*-plane (y-z plane).

center frequency of 7.25 GHz and a measured bandwidth (-10 dB) of 1.52%. Good impedance matching at the center frequency is achieved. A wideband response is also given in the inset of Figure 4.13 in order to observe the zeroth-order resonance. The radiation patterns in *E*-plane (*x*-*z* plane) and *H*-plane (*y*-*z* plane) are very similar to the patterns of conventional microstrip patch antennas or slot antennas. We can find that the *E*-plane pattern is not very symmetrical and the backward radiation is stronger than the



Figure 4.14 Measured (solid line) and simulated (dashed line) results for the two-stage openended antenna shown in Figure 4.11. (a) reflection coefficient, (b) the normalized radiation patterns in *E*-plane (x-z plane), and (c) the normalized radiation patterns in *H*-plane (y-z plane).

forward wave radiation. This can be attributed to the influence of the microstrip feeding and the fact that this antenna is operated on the -1^{st} order resonance. The observed crosspolarization level in the measurement is -12.5 dB in the *E*-plane and -13 dB in the *H*plane. The simulated cross-polarization in the *E*-plane is too low to detect in the figures due to the reason that the fields cancels each other in *x-z* plane for the cross-polarization. However in the measurement the cable, connector and noise all affect the radiation patterns which will substantially increase the cross-polarization level.



Figure 4.15 Measured (solid line) and simulated (dashed line) results for the one-stage shortended antenna (the dimensions are shown in Figure 4.9). (a) reflection coefficient, (b) the normalized radiation patterns in *E*-plane (x-z plane), and (c) the normalized radiation patterns in *H*-plane (y-z plane).

Figure 4.14 shows the measured and simulated reflection coefficient and radiation patterns for the two-stage open-ended antenna. A wideband measurement is made and the result is shown in Figure 4.11 for comparison. It is found that the reflection coefficient in the measurement is even better than that in the simulation. The center frequency is 7.65 GHz and the measured bandwidth (-10 dB) is 1.88%. The radiation as shown in the *E*-plane (*x-z* plane) pattern is a little backward shifted which is also due to the LH (-1st)


Figure 4.16 Measured (solid line) and simulated (dashed line) results for the two-stage shortended antenna. (a) reflection coefficient, (b) the normalized radiation patterns in *E*-plane (*x-z* plane), and (c) the normalized radiation patterns in *H*-plane (*y-z* plane). (The unit cell dimensions are shown in Figure 4.4. Other parameter values are: $d_1 = 2.7$ mm, $d_2 = 2.7$ mm, $t_1 = 1.9$ mm, $t_2 = 0.85$ mm, p = 8.41 mm).

order mode) region operation and the unsymmetrical microstrip excitation. A measured cross- polarization level of -12.5 dB in the *E*-plane and -7.5 dB in the *H*-plane (*y*-*z* plane) is observed. It is also noted that the cross polarization in the *H*-plane is mainly caused by the side leakage of the electric field inside the substrate which is perpendicular to the ground and surface, resulting in a cross polarization pattern as shown in the figure.

Figure 4.15 shows the measured reflection coefficient and radiation patterns for the one-stage short-ended antenna. It has a center frequency of 7.75 GHz and a bandwidth of 2.254% below -10 dB. As seen the radiation mainly goes to the broadside. The level of cross-polarization for this antenna is around -15 dB in the *E*-plane and -9 dB in the *H*-plane. It is noted that in the broadside direction, the level of cross-polarization is much lower than that of the co-polarization.

Figure 4.16 shows the measured results for the two-stage short-ended antenna with the dimensions listed in the caption. The center frequency is located at 7.86 GHz and its - 10 dB bandwidth is 2.51%. Its radiation patterns are also very similar to a microstrip patch antenna. As expected, the beamwidth is narrower compared to the one-stage short-ended antenna. The cross-polarization in both the *E*-plane and *H*-plane is less than - 12 dB.

Table 4.2 draws a performance comparison for the fabricated four antennas with the antenna size in terms of wavelength, simulated and measured peak gain, measured directivity, measured -10 dB bandwidth as well as the simulated and measured antenna efficiency. The measured radiation efficiency is obtained using the directivity/gain (D/G) method. And the antenna directivity is measured in the near-field chamber in UCLA. From this table we find that the open-ended antennas have a smaller size than the short-ended antennas with the same number of unit cells. However the short-ended antennas provide a higher gain and a higher efficiency, which is due to the cavity-backed configuration, resulting in little leakage from the boundaries.

Compared with the conventional waveguide slot antenna as shown in [17-19], the

	One-stage Open-ended Ant.	Two-stage open-ended Ant.	One-stage Short-ended Ant.	Two-stage Short-ended Ant.
Antenna Size	$\begin{array}{c} 0.265\lambda_0 \\ \times 0.318\lambda_0 \end{array}$	$\begin{array}{c} 0.48 \ \lambda_0 \\ \times \ 0.33 \ \lambda_0 \end{array}$	$\begin{array}{c} 0.296 \ \lambda_0 \\ \times \ 0.335 \ \lambda_0 \end{array}$	$\begin{array}{c} 0.506 \ \lambda_0 \\ \times \ 0.343 \ \lambda_0 \end{array}$
Meas. Bandwidth (-10 dB)	1.52 %	1.88 %	2.254 %	2.51 %
Sim. Peak Gain	2.93 dBi	5.29 dBi	4.504 dBi	6.184 dBi
Sim. Efficiency	0.818	0.922	0.913	0.939
Meas. Directivity	4.323 dBi	5.49 dBi	4.92 dBi	7.254 dBi
Meas. Peak Gain	3.16 dBi	4.95 dBi	4.31 dBi	6.83 dBi
Meas. Efficiency	0.765	0.883	0.869	0.907

Table 4.4 A Performance Comparison For the Fabricated CRLH-SIW Slot Antennas

miniaturization of our proposed antennas which are based on the negative modes can be summarized in two aspects: First, the antennas are working below the characteristic cutoff frequency of the TE_{10} mode of the SIW. Their transversal dimension can be arbitrarily smaller by simply moving down the LH region. Secondly, the miniaturization obtained also refers to the longitudinal size of the SIW since the period of the unit cells is significantly smaller than the wavelength in free space. They are similar to the waveguide transverse slot antennas. Compared with the conventional half-wavelength microstrip patch antennas, which have an average gain of 6-7 dBi with a radiation efficiency around 80%-90% [20], the proposed two-stage antennas give a similar gain level but they still exhibit a smaller size. The microstrip patch antenna needs a big ground while this is unnecessary for our CRLH waveguide slot antennas. Bandwidth enhancement for the proposed antennas can be achieved by cascading non-uniform unit cells. Multi-band operation is also feasible by using the zeroth-order and $+1^{st}$ resonances simultaneously.

4.2 Miniaturized Patch Antennas Loaded with Mushroom-like Metamaterial Structures

In this section, two miniaturized single-feed circularly polarized (CP) patch antennas loaded with the mushroom-like CRLH structures and a reactive impedance surface (RIS) are proposed. The characterization of the meta-surface and the CRLH resonator is first described. The detailed antenna configuration, CP working principle and radiation performance are then presented. Based on this CP antennas, a dual-band dually-polarized patch antenna and an antenna with increased bandwidth working on the negative order resonances have also been developed. The measured results are in agreement with the predicted data obtained from the HFSS simulation.

4.2.1 CRLH Mushroom-Like Structure

The mushroom-like structure, as shown in the inset of Figure 4.17, was first proposed for the realization of the high-impedance surface [21]. Later it has been demonstrated that essentially it is a CRLH structure. The left-handed (LH) capacitance C_L is provided by the coupling of adjacent top patches, while the LH inductance is provided by the via connected to the ground plane. Figure 4.17 shows the dispersion diagram of the mushroom unit-cell obtained from full-wave simulation. It is clearly seen that the LH and right-handed (RH) regions are generated and separated by a small bandgap. Zeroth order antennas based on this mushroom-type resonator have already been proposed [6]. Multiband antennas by employing both the negative and positive order resonators were developed in [22]. The negative order resonance, which is located in the LH region, has a lower resonance frequency therefore is able to provide a degree of size miniaturization.



Figure 4.17 Dispersion diagram of a typical mushroom-type unit-cell based on HFSS eigenmode simulation.



Figure 4.18 Simulated reflection phase of the RIS unit-cell with different a_1 ($a_2 = 6.2$ mm is fixed here). Unit-cell of the RIS as shown is bounded with PEC and PMC walls and illuminated by a normal incident plane wave. The material setup is the same as the antenna shown later in Figure 4.19.

4.2.2 Reactive Impedance Surface

The unit-cell of the RIS employed here is shown in the inset of Figure 4.18. It is composed by two dimensional periodic metallic patches printed on a grounded substrate.

The detailed design procedures and the analysis can be found in [10]. Here a brief investigation on the basic features of the RIS is presented. Usually the periodicity of the metallic patches is much smaller than the wavelength. Considering a single cell illuminated by a TEM plane wave, PEC and PMC boundaries can be established around the cell as shown in Figure 4.18. The resulting structure can be modeled as a parallel LCcircuit. The edge coupling from the patches provides a shunt capacitor and the shortcircuited dielectric-loaded transmission line can be modeled as a shunt inductor. Figure 4.18 shows the simulated phase reflection response under an incident plane wave model for the RIS unit-cell. In the simulation the periodicity (a_2) is fixed while the patch size is varied, which corresponds to a change of the shunt capacitance value. The 180° reflection phase corresponds to a PEC surface while the 0° reflection phase means a PMC surface. Depending on the operation frequency, either an inductive RIS (below the PMC surface frequency) or a capacitive RIS (above the PMC surface frequency) can be obtained. As demonstrated in [10] and [23], due to the matching difficulty and loss problem, PMC surface is not an optimum choice. An inductive RIS is able to store the magnetic energy and increase the total inductance of the patch, which can be used to compensate for the electric energy stored in the near-field of the antennas. This results in the antenna miniaturization. In the meantime the inductive RIS is also able to provide a wider matching bandwidth so that it is more suitable for antenna application. It should be pointed out that since the near field generated by the patch antenna is not a uniform plane wave and the meta-surface is size-limited far from being periodic, the thinking or design of a radiating patch over the meta-surface (RIS) using the equivalent circuit and unit-cell



Figure 4.19 Configurations of the proposed CP patch antenna loaded with the mushroom-like structure and the RIS. (a) Perspective view, (b) Top view, and (c) Side View.

analysis shown in Figure 4.18 is just an approximation to qualitatively explain its working principle. To better explain the role played by RIS, an analysis on the near field interaction would be very meaningful and essential.

4.2.3 Antennas with Diagonal Feeding

A. Configuration

Figure 4.19 shows the geometry of the proposed CP patch antenna. A coaxial probe feeding is adopted. The RIS, which is composed of a 5 by 5 periodic array of metallic square patches printed on a grounded dielectric substrate, is introduced below the top surface. It is a three-layer structure where the upper and lower dielectric substrates are "MEGTRON 6" with a dielectric constant of 4.02 and a measured loss tangent of 0.009 at 2.4 GHz. A 2 by 2 mushroom-like structure is inserted into the microstrip patch to inspire the patch antenna. It is noted that several holes are etched on the RIS to let the vias and the feeding probe drill through so that they are not connected. The mushroom structure is shifted from the patch center by x_1 and y_1 . The probe is located on the 45° diagonal line. Both the mushroom structure and the microstrip patch can be adjusted to obtain a good CP radiation.

The equivalent circuit model of the proposed antenna can be roughly described by Figure 4.20. It is noted that this circuit only represents a one-dimensional case. The real structure is two dimensionally distributed in both X and Y directions. The microstrip patch is modeled as an *RLC* parallel resonator which is inductively connected to the probe. The mushroom-like structure is modeled as a two unit-cell circuit. It is capacitively coupled to the outside patch by a small gap. It provides a lower resonance frequency compared with the microstrip patch. The wave can be coupled from the mushroom to the patch and be radiated away with the radiation resistance (R_p) of the patch.



Figure 4.20 Equivalent circuit model for the proposed patch antenna loaded with CRLH structures.



Figure 4.21 Simulated reflection coefficient for the proposed antenna and two reference antennas: one without the RIS middle layer and the other one without loading anything. They have the same patch size as shown in Figure 4.19.

B. CP Antenna Design

As indicated by Figure 4.20, the final structure is actually a combination of the RH and CRLH sections. Although the first resonance frequency (-1st mode) is excited by the mushroom-like structure in the LH region, it is coupled to the patch and both the mushroom structure and patch size would affect the resonance frequency. However, for this -1st mode, a complete 180° phase change can be observed locally along the 2 by 2 mushroom-type structure. Apparently here the antenna miniaturization has been achieved



Figure 4.22 Simulated $|S_{11}|$ for the proposed CP patch antenna with different mushroom sizes. (w_1 is the width of the mushroom unit-cell and $l_1 = w_1$).

by two approaches: by loading the mushroom-like structure and by loading the RIS. Two orthogonal modes can be excited along the *x*-direction and *y*-direction. A 90° phase shift is provided by the feeding which is located on the 45° diagonal line, leading to a pure CP mode.

Figure 4.21 shows the simulated $|S_{11}|$ response for three different cases but with the same patch size. It is shown that by loading the CRLH structure and the meta-surface, the first operating frequency has been successfully pushed down from 3.3 GHz to 2.58 GHz. It should be pointed out that the size of the mushroom structure can be further increased to reduce the resonance frequency. This is confirmed by Figure 4.22. However, this miniaturization is usually obtained at the sacrifice of the radiation efficiency and bandwidth. The size reduction of this proposed antenna, compared to the un-loaded patch, is 39%. The achieved miniaturization factor shows some advantages even compared with other conventional miniaturization techniques, such as the peripheral slits method shown in [24].



Figure 4.23 Simulated AR with different mushroom positions (y_1) at the broadside direction and the measured AR versus frequency for the fabricated prototype.



Figure 4.24 Electric field distribution inside the top-layer substrate in time-domain.

The perturbation to generate the CP mode can be realized by either changing the configuration of the mushroom-like structure or the microstrip patch, mainly the width-to-length ratio. Here it is interesting to note that the position of the mushroom-like structure can also be used to improve the axial ratio (AR). Figure 4.23 shows the simulated AR performance with different *y*-positions of the mushroom structure. It should be pointed out that here the matching will also be slightly affected. Nevertheless it



Figure 4.25 Measured and simulated $|S_{11}|$ for the proposed CP patch antenna. A photograph of the fabricated CP patch antenna is also displayed in the inset.

still appears as an effective way to optimize the CP radiation. Figure 4.24 shows the field distribution inside the top layer substrate in the time domain. It is clearly seen that a local 180° phase change is observed along the mushroom structure, which confirms -1st mode operation. A left-hand (clockwise) rotated field moving along the patch edge is detected which reveals its left-handed circular polarization nature.

C. Experimental Results

A photograph of the fabricated CP antenna is shown in the inset of Figure 4.25. The overall antenna size is around $0.177 \lambda_0 \times 0.181 \lambda_0 \times 0.025 \lambda_0$ at 2.58 GHz. It was tested using an Agilent 8510C network analyzer and a near-field spherical chamber. Figure 4.25 shows the simulated and measured $|S_{11}|$ response. A small frequency shift is detected which is due to the change of the permittivity of the substrate. The measured dielectric constant is around 3.85 instead of 4.02 assumed in the simulation. The measured and simulated -10 dB bandwidth are 4.6% and 4.62%, respectively. The simulated and



Figure 4.26 Measured and simulated far-field patterns at the center frequency in x-z plane and y-z plane. The patterns are normalized and the display scale is 5 dB per division.



Figure 4.27 Three-dimensional (a) AR and (b) Radiation pattern measured in a spherical near field at the center frequency.

measured AR at the boresight direction is included in Figure 4.23. The measured 3-dB AR bandwidth is 1.46%. It is worth noting that from the simulation it is shown that the designed antenna is adequately tolerant to fabrication errors. For instance, the $\pm 2\%$ tolerance of the RIS unit-cell patch size would lead to a resonance frequency change of $\pm 0.54\%$ only.

Figure 4.26 shows the measured and simulated radiation patterns in x-z and y-z



Figure 4.28 Measured and simulated $|S_{11}|$ for the dual-band dually-polarized antenna shown in the inset of the figure. The geometrical parameters shown in Fig. 3 are: $a_1 = 5.4$ mm, $a_2 = 6$ mm, $h_1 = 0.4$ mm, $h_2 = 2.6$ mm, $s_1 = 3.26$ mm, $s_1 = 2.2$ mm, $l_2 = 16.5$ mm, $w_2 = 23.3$ mm, $l_1 = 3.45$ mm, $w_1 = 3$ mm, $t_1 = 0.1$ mm, $t_2 = 0.32$ mm, $x_1 = 2.3$ mm and $y_1 = 1.3$ mm.

principal planes, which are in good agreement. As seen the antenna is left-handed circularly polarized. The backside radiation, which mainly is the cross polarization wave, is probably affected by the test support and appears much weaker. The measured gain is 2.98 dBi, corresponding to a radiation efficiency around 72%. Figure 4.27 shows the measured three-dimensional AR and radiation pattern. It is seen that a CP radiation is retained in a very wide region and the pattern is very similar to a traditional patch antenna.

D. Application to a Dual-band Dually-polarized Antenna

By increasing the width-to-length ratio of the mushroom unit-cell or the microstrip patch, the resonance frequency of the two orthogonal modes, both of which are excited by the -1st mode, can be separated far away and a dual-frequency dual linearly-polarized antenna can be easily obtained. To validate this conclusion, we designed and fabricated such an antenna which is operated at 2.4 GHz and 2.9 GHz. Figure 4.28 shows the



Figure 4.29 Measured and simulated radiation patterns of the dual-band antenna at the center frequency for (a) The first band and (b) The second band.



Figure 4.30 Spherical radiation patterns measured in the near-field chamber at (a) The first operating frequency, (b) The second operating frequency. It shows the pattern in x-y plane viewed form +z to -z direction.

measured reflection coefficient with an antenna photograph displayed in the inset. A small frequency shift is also detected. Figure 4.29 shows the measured and simulated



Figure 4.31 The photograph of the fabricated circularly polarized antenna with corner cut.



Figure 4.32 The simulated and measured reflection coefficient.

radiation patterns in both *E*-plane and *H*-plane tested in a far-field chamber. Note that their polarization states are linear and orthogonal to each other. The first resonance is polarized in *y*-*z* plane while the second one is polarized in *x*-*z* plane. For verification a near- field measurement was also performed and Figure 4.30 shows the measured radiation data in a spherical view, which clearly indicates the polarization directions. The measured gain at the two bands is 2.25 dBi and 3.11 dBi, respectively. The overall size of this antenna is only 0.133 $\lambda_0 \times 0.187 \lambda_0 \times 0.025 \lambda_0$ at 2.4 GHz.



Figure 4.33 Simulated and measured radiation patterns.



Figure 4.34 Measured and simulated AR versus (a) frequency at the broadside direction, and (b) theta angle at the center frequency.



Figure 4.35 Three-dimensional (a) AR and (b) radiation pattern measured in a spherical near field.



Figure 4.36 The photograph of the fabricated wideband antenna.

4.2.4 Antennas with Corner Cut

A. CP Antenna

In the above part, a circularly polarized antenna with diagonal feeding is analyzed in detail. Here we briefly show that circular polarization can also be obtained with corner cut. Figure 4.31 shows the photograph of the antenna. Its simulated and measured reflection coefficient is shown in Figure 4.32. The radiation patterns and AR are shown in Figure 4.33 and Figure 4.34, respectively. Similarly, we measured this antenna in the near field chamber. The measured 3D pattern and AR is shown in Figure 4.35.

B. Application to a Wideband Antenna

The above antenna possesses two resonances leading to a circular polarization by applying 90° phase difference. By separate the two resonance frequencies to certain degree we can easily get a wide band antenna. We designed and fabricated this antenna with a large bandwidth. The coaxial feeding is at the center of the y-axis. Two corners are chamfered to provide the perturbation. Two resonance frequencies are generated. The two resonances do not overlap therefore it is not circularly polarized. A frequency shift is



Figure 4.37 The simulated and measured reflection coefficient.



Figure 4.38 Simulated and measured radiation patterns in *E*-plane and *H*-plane at the two peak frequencies: (a) 2.5GHz and (b) 2.62GHz. The E-plane and H-plane correspond to the phi=45 deg and 135 deg planes. (Solid line is for the simulation and dotted line is the measured results)

also detected. The polarization of the two modes are along phi=45° and 135° direction. This can be called as a dual-mode antenna. Figure 4.36 shows a photograph of the antenna. The simulated and measured reflection coefficient is displayed in Figure 4.37. One disadvantage of this antenna is that the radiation pattern across this wide frequency range is not uniform due to the orthogonal polarization of the two resonances. The radiation patterns are shown in Figure 4.38.

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Chapter 5

Metamaterial Resonator Antennas Based on SRR and CSRR Structures

Split-ring resonator (SRR) can be considered as a resonant magnetic dipole while complementary split-ring resonator (CSRR) behaves like a resonant electric dipole [1-3]. They have been widely used to synthesize metamaterials [1-7]. In this chapter an investigation into the planar electrically small antennas designed based on the SRR and CSRR structures is presented. A small reactive impedance surface (RIS) composed by two metallic patches is employed to further reduce the antenna size [8]. Their working principles are illustrated in detail. A loss analysis is carried out showing that the proposed antennas are able to provide relatively good radiation efficiency. They have a planar structure and can be fabricated by the standard PCB process at a low cost. They are proposed and designed specifically for practical 2.4 GHz wireless Local Area Network (LAN) application. Nevertheless, they can be easily scaled up or down and applied in other communication systems.

5.1 Vertical Split-Ring Resonator (VSRR) Antennas

In this section, we present a detailed investigation into the electrically small vertical SRR (VSRR) antennas. It is demonstrated that the proposed VSRR antenna behaves essentially similarly to a magnetic dipole antenna placed above a PEC plane. By



Figure 5.1 Configurations of the proposed inductively-fed VSRR antennas. (a) Perspective view of the RIS-loaded antenna, (b) Perspective view of the un-loaded antenna, (c) Top view of the RIS-loaded antenna, and (d) Side view of the RIS-loaded antenna. These two antennas have the same parameters as shown in Table I. There are seven vias on each of the two ends with a radius of 0.15 mm and a spacing of 0.75 mm.

appropriately changing the ground configuration, the antenna could be switched to a miniaturized electric dipole-type antenna. These proposed antennas can be directly fed with a 50 Ω coaxial probe without introducing any matching network. Their working principles are illustrated in detail. Different feeding techniques are adopted and compared. Six antennas are designed and fabricated based on the standard PCB process.

5.1.1 Inductively-Fed VSRR Antennas

In this section, the characteristics of the inductively-fed VSRR antennas with or without the RIS are investigated and compared. First the antenna working principle is discussed. The features and influence of the RIS are also illustrated. Then the influence of the ground is discussed and a loss analysis is provided to the readers. The detailed simulation and experimental results are presented in the final part.

A. Configuration and Working Principle

Figure 5.1 shows the geometrical layout of the proposed inductively-fed VSRR antennas with (a) or without (b) the RIS. A coaxial feeding probe is directly connected to the top surface of the SRR which can be represented by a series inductor. The interdigital capacitor, which is the split of the VSRR, is the main radiator of this structure. The top surface and the metalized via-holes on the two ends, together with the ground, constitute a capacitor-loaded half-wavelength loop resonator forming an SRR configuration. The RIS, which is composed of two metallic square patches printed on a PEC-backed dielectric substrate, is introduced below the top surface as shown in Figure 5.1(a). Note that two rectangular holes and a circular hole have been cut away on the RIS in order to let the vias and the feeding probe drill through. It should be remarked that it is a little farfetched to consider a two-unit-cell structure as a "surface". However, since the wave only interacts intensively with the particular surface area below the radiating slot, we still find that this small surface is able to offer characteristics similarly to that of a two dimensional periodic surface. It is a three-layer structure (two-layer for the case without RIS) where the top and bottom dielectric substrate is "MEGTRON 6" with a relative



Figure 5.2 Equivalent circuit model for the proposed inductively-fed VSRR antennas shown in Figure 5.1.



Figure 5.3 Simulated complex input impedance for the inductively-fed VSRR antennas shown in Figure 5.1 with or without the RIS.

permittivity of 4.02 and a loss tangent of 0.009 at 2.4 GHz. It is pointed out that this substrate is considered to be a little lossy compared with other low-loss material like the Rogers substrate which exhibits a loss tangent around 0.0009-0.002. The copper metal, which is assumed to have a 5.8×10^7 Siemens/m conductivity, is used in all of the designs.

These proposed antennas can be roughly represented by the circuit model shown in Figure 5.2. The VSRR is modeled as a high-Q LC resonator with a parallel radiation resistance (R_{rad}) associated with the capacitor C_r . The series inductor L_{in} indicates the direct connection or coupling between the probe and VSRR. This circuit is excited by

simply applying a voltage difference across capacitor which generates current along the loop and induces axial magnetic field inside the loop. In this manner it can be equivalent to a magnetic dipole placed along the *y*-direction above a PEC surface. Apparently by increasing the value of L_r or C_r we are able to reduce the resonance frequency. By loading an inductive RIS the overall L_r value can be enhanced which leads to a miniaturization of the antenna size. Figure 5.3 shows the simulated input impedance for the designed antennas with or without loading the RIS. The antenna dimensions are shown in Table I next to Figure 5.1(c). Note that the antenna without the RIS has exactly the same parameter values. It is seen that by loading the RIS, the initial resonance frequency has been moved down from 2.83 GHz to 2.4 GHz. Due to an inductive feeding, the observed reactance is almost positive. It is interesting to note that the matching can be optimized by changing the *x*-position of the feeding probe as well as the number and spacing of the vias.

B. RIS

The RIS was discussed earlier in Chapter 4. Here a brief investigation about its characteristics is provided. Considering a single cell illuminated with a TEM plane wave, PEC and PMC boundaries can be established around the cell as shown in Figure 5.4(a). The resulting structure can be modeled as a parallel *LC* circuit [8]. Figures 5.4(b) to (d) show the simulated reflection phase with varied parameter values under an incident plane wave model for the RIS unit-cell displayed in Figure 5.4(a). Note that the 180° reflection phase corresponds to a PEC surface while the 0° reflection phase means a PMC surface.

However, since our proposed antenna is very small (11.94 mm×5.38 mm only), two



Figure 5.4 (a) Unit-cell of the RIS bounded with the PEC and PMC walls and illuminated by a normal incident plane wave; (b) Simulated reflection phase of the RIS unit-cell for different patch size; (c) Simulated reflection phase of the RIS unit-cell for different slot width; and (d) Simulated reflection phase of the RIS unit-cell for different substrate thickness h_2 ($h_1 = 0.4$ mm is fixed here), The parameters are: $a_1 = 8.0$ mm, $a_2 = 8.15$ mm, $h_1 = 0.4$ mm, and $h_2 = 2.6$ mm. The substrate information is shown in Figure 5.1(c).

unit-cells are enough to cover the top plane circuit and this two-cell surface is far from being periodic therefore it is far-fetched to be called a "surface". We have to mention that the thinking or design of a radiating element over this meta-surface (RIS) using the equivalent circuit and unit-cell analysis is just an approximation to qualitatively explain its working principle. Nevertheless, since the near field interaction mainly happens around the radiating aperture which is the interdigital slot here, this two-unit-cell surface is still capable of achieving the main function of a periodic RIS. To verify its impact, we changed the RIS configuration in accordance to Figures 5.4(b)-(d) and simulated the



Figure 5.5 A parameter study on reflection coefficient by changing the RIS configuration for the antenna shown in Figure 5.1(a). (a) Changing the patch size of the RIS; (b) Changing the slot width; and (c) Changing the bottom layer substrate thickness h_2 .

whole antenna displayed in Figure 5.1(a). The obtained different reflection coefficient responses are presented in Figure 5.5. They are in good agreement with the information provided by Figure 5.4. We also remind the readers that using a cap below the interdigital slot could also enhance the capacitor value leading to the decrease of the resonance frequency. Yet this two-cell surface has totally different characteristics which confirms us that it works much more close to a two dimensional RIS. Figure 5.5(a) illustrates how the resonance frequency varies when the patch size is adjusted. When the size of the square patch is small, the corresponding capacitor is reduced which increases the antenna resonance frequency. Note that when a_1 is equal to 5 the RIS is completely covered by the top metal as indicated by the figure shown in the inset. Under this condition still considerable frequency reduction is achieved compared with the un-loaded case. Figure 5.5(b) shows that by decreasing the width of the gap between the patches, the resonance frequency can also be pushed down. Figure 5.5(c) shows that by increasing the thickness of the bottom substrate, which would increases the equivalent inductor of the RIS, the resonance frequency is shifted down dramatically. This is consistent with the results shown in Figure 5.4(d).

C. Impact of Ground Size

Usually antennas in the communication systems only have a finite ground size. And when this finite ground size is large enough, the antenna performance is believed to be independent of the ground size. However, for our antennas the required size including the ground is specified and restricted instead of being large enough. It would be useful and interesting to investigate the influence of the ground size.



Figure 5.6 A parameter study on the ground size for the un-loaded antenna shown in Figure 5.1(b). (a) Changing the length of the ground, l_1 , while w_1 is fixed at 20 mm, (b) Changing the width of the ground, w_1 , while l_1 is fixed at 28.6 mm Here the "infinite" ground is just a rough approximation which actually has a finite size of 150 mm × 150 mm.

We performed a parameter study for the ground size on the un-loaded antenna displayed in Figure 5.1(b). The results are shown in Figure 5.6. It is noted that the "infinite ground" referred here actually has a finite size of $1.2\lambda_0 \times 1.2\lambda_0$ (150 mm × 150 mm) where λ_0 is the free space wavelength at the resonance frequency. Compared with the antenna size which is $0.112\lambda_0 \times 0.051\lambda_0$ (11.94 mm × 5.38 mm) only, it is large enough to be considered as an infinite ground. It is found that the length of the ground (l_1 as shown in Figure 5.1) does not affect resonance frequency very much.



Figure 5.7 Simulated normalized H-plane patterns for the un-loaded antennas with different ground width.

Table 5.5 A Performance Comparison For the Un-loaded VSRR Antennas with different Ground Width

Ground Width	<i>f</i> ₀ (GHZ)	D (dBi)	Effi.	Front-to-Back Ratio (dB)
6 mm	2.612	2.257	71.3 %	0.875
16 mm	2.808	3.175	69.6 %	2.321
20 mm	2.827	3.559	67.3 %	2.928
26 mm	2.840	3.969	63.2 %	3.29
$\rightarrow +\infty$	2.857	6.232	50.5 %	13.54

The length of the ground is fixed here for the first four cases: l_1 =28.6mm. Also the infinite ground case is just an approximation. The ground size is actually 150 mm × 150 mm, which is very large compared with other cases. It behaves very close to the true infinite ground. To eliminate the influence of matching, the gain calculated here is the antenna gain itself instead of the realized gain.

However, the width of the ground (w_1) has a more perceptible influence on the resonance frequency as shown in Figure 5.6(b). The basic reason is that the width affects the inductance value of the circuit indicated by Figure 5.2 since the ground is also one part of the loop. Narrow ground means larger inductance. Particularly, when w_1 is reduced to 6 mm, the resonance frequency is moved to a much lower frequency. We simulated their



 Table 5.6 A Electric Field and Pattern Comparison for the Antennas with large Ground (left) and Narrow Ground (Right)

z value represents the distance of the observation plane to the ground. z = 2.8 mm indicates the plane is inside the substrate. z = 3.2 mm means the plane is slightly above the top plane. z = 5.0 mm shows that the plane is 2 mm above the top surface.

H-plane (*y-z* plane) pattern and plotted it in Figure 5.7. For convenience, we also extracted their directivity, radiation efficiency and front-to- back ratio as displayed in Table 5.1. It is seen that the smaller the ground width is, the more omni-directional the pattern becomes. For the $w_1 = 6$ mm case, the pattern is almost omni- directional. Also the directivity is 2.257 dBi which is very close to the directivity of a half-wavelength



Figure 5.8 (a) Magnetic field distribution inside the substrate in x-y plane for the antenna shown large ground. The field is very similar to that generated by a magnetic dipole antenna placed on a PEC plane. (b) Electric field distribution inside the substrate for the antenna with narrow ground. The field is very similar to that generated by an electric dipole antenna in free space.

dipole (2.15 dBi). We then checked their electric field distribution at the resonance frequency as plotted in Table 5.2. For the sake of convenience, we also plotted their structure and 3-D radiation pattern in the Table. It is shown that for the $w_1 = 6$ mm case, the VSRR antenna evolves exactly to a miniaturized electric dipole-type antenna. For the $w_1 = 20$ mm case the field shows that it is still an SRR-type resonance. It is very interesting to point out that by simply changing the ground width a magnetic dipole-like antenna has been switched to an electric dipole-like antenna. For convincing purpose, we simulated the magnetic field for the former and electric field for the latter at a plane inside the substrate and they are plotted in Figure 5.8. It is clearly seen that the former behaves as a magnetic dipole antenna over a PEC surface while the latter can be



Figure 5.9 Simulated $|S_{11}|$ for the miniaturized electric dipole-like antenna with different ground length l_1 .



Figure 5.10 Simulated $|S_{11}|$ for the miniaturized electric dipole-like antenna with different finger length l_3 of the interdigital capacitor.

considered as a miniaturized electric dipole antenna in free space. We claim it is miniaturized since its overall length (l_1) is only 0.249 λ_0 at the resonance frequency while the conventional electric dipole antenna has a length around half wavelength. It is also reminded that when it is evolved to an electric dipole-like antenna, the length of the ground becomes important since it becomes one part of the current path and participates

in the radiation. Similarly to Figure 5.6(a), we changed the ground length (l_1) for the $w_1 = 6$ mm case and the simulated reflection coefficient is shown in Figure 5.9. It is intuitively observed that now the resonance frequency is dependent on l_1 . Compared with the conventional electrical dipole antennas, this miniaturized dipole-like antenna shows some advantageous features. First, it is automatically matched to a coaxial feeding probe without the need of a matching network. Second, this antenna could be miniaturized very conveniently by changing the capacitor value. For instance, we varied the finger length of the interdigital capacitor and the resulting reflection coefficient is shown in Figure 5.10. Potentially it could be a very useful replacement of the traditional dipole antenna for some special compact systems.

C. Loss Budget

The ESAs usually suffer from low efficiency. Of course, the loss is dependent on the used material and lossless materials would not impose any loss. From this point of view, air and silver are preferred since they have less loss. But for integrated circuit usually the circuit is printed on a substrate therefore air is difficult to apply. The silver is expensive and usually the copper is widely used. Besides the material issue, the operating principle of the antenna is the most important factor determining the radiation efficiency. For instance, strong current should be avoided in order to reduce the conductor loss. It is helpful for the engineers to know the overall loss and its constitution. For this purpose we present a loss analysis as shown in Table 5.3 for both of two antennas with or without the RIS. The efficiency for loaded case is smaller mainly due to a decreased resonance frequency. Taking the unloaded antenna as an example, it is seen that overall radiation
	Without RIS (at 2.83 GHz)			With RIS (at 2.4 GHz)		
	Directivity	Gain	Efficiency	Directivity	Gain	Efficiency
Lossy: ε _r =0.009	3.559	1.84	67.3%	3.0152	-0.512	44.4%
Lossy: <i>ɛ</i> _r =0.001	3.608	3.194	90.9%	3.073	1.946	77.14%
Cond. Loss Only	3.603	3.394	95.3%	3.106	2.456	86.1%
Lossless	3.582	3.582	100%	3.131	3.131	100%

Table 5.7 A loss Analysis on the Proposed two Inductively-Fed Antennas based on HFSS Full-wave Simulation

efficiency is 67.3% based on the material we used. If we use a substrate with a low loss, such as the Rogers substrate, the efficiency could be improved substantially up to more than 90%. It is also seen that the conductor loss is not very critical compared with the dielectric loss. Overall, as an integrated ESA, this antenna provides us with quite good radiation efficiency.

C. Simulated and Measured Results

The above two antennas shown in Figure 5.1 with or without the RIS are designed and fabricated. Their dimensions are also listed in the figure. Figure 5.11 shows a photograph of the two antennas. They appear quite compact with an electrical size of $0.096\lambda_0 \times 0.043\lambda_0 \times 0.024\lambda_0$ and $0.112\lambda_0 \times 0.051\lambda_0 \times 0.028\lambda_0$ (λ_0 is the free space wavelength at the simulated resonance frequency), respectively, which as seen are much smaller than a coin. Figure 5.12 shows their simulated and measured reflection coefficients. A small frequency shift is observed. To find the reason for this discrepancy we tested the substrate characteristics and found that the measured dielectric constant is reduced a little (around 3.8~3.9). And the measured loss tangent of the substrate is around 0.005~0.008 (in the simulation we set it as 0.009). Therefore the measured resonance frequency is

[&]quot;Lossy" means with both conductor and dielectric loss. The gain is the radiation gain not taking the mismatching into account.



Figure 5.11 A photograph of the fabricated inductively-fed VSRR antennas with (left) or without (right) the RIS.



Figure 5.12 The measured and simulated reflection coefficients for the inductively-fed VSRR antennas (a) without the RIS, and (b) with RIS.



Figure 5.13 Measured and simulated far-field gain patterns for the inductively-fed VSRR antennas (a) without the RIS, and (b) with the RIS loading.

	Without RIS	With RIS	
Sim. f_0 / ka	2.83 GHz / 0.427	2.4 GHz / 0.362	
Sim. FBW (-10 dB)	1.75 %	1.38 %	
Meas. FBW (-10 dB)	2.1 %	1.58 %	
Sim. Peak Gain	1.823 dBi	-0.671 dBi	
Sim. Directivity	3.559 dBi	3.015 dBi	
Sim. Efficiency	67.1%	42.8%	
Meas. Gain	2.05 dBi	0.47 dBi	
Meas. Efficiency	68.1%	48.9%	

Table 5.8 A Performance Comparison For the Inductively-Fed Antennas

ka indicates the electrical antenna size. Note that for the antenna with RIS, ka is calculated without considering the size increase due to the RIS, since it is not the radiating element and it can be miniaturized as shown by Figure 5.5(a). (If the RIS is included, ka = 0.47). The simulated and measured gain is the realized gain which has taken the mis-matching into account.

moved up a little. The simulated and measured gain patterns in both E-plane and H-plane for the two antennas are shown in Figure 5.13. Due to the up-shift of the resonance frequency and decrease of the dielectric loss tangent, the measured gain is slightly higher for both of two antennas and the front-to-back ratio is increased. It is also seen that the cross polarization level is very low. We summarized the antenna performance including the electrical size, bandwidth and radiation efficiency in Table 5.4. And here *ka* indicates the electrical antenna size where *k* is the wave number and *a* is the radius of the smallest sphere enclosing the antenna. The proposed antennas are electrically small according to the criterion ka < 1 [9]. Basically the measured results are in agreement with the simulation and the antennas are showing promising performance.

5.1.2 Capactively-Fed VSRR Antennas

In this section, the characteristics of the capactively-fed VSRR antennas with or without the RIS are investigated and compared. The detailed simulation and experimental results are provided and discussed.

A. Configuration and Working Principle

Figure 5.14 shows the structures of the proposed VSRR antennas with a capacitive feeding. Compared with the previous antennas, the coaxial feeding probe is capacitively coupled to the VSRR which is achieved by cutting a circular ring slot the between probe position and the top surface. Similarly, two antennas loaded with or without the RIS are designed and optimized. Their dimensions are listed in the caption of Figure 5.14. To improve the matching, we use only three metallic vias to connect the ground and top



Figure 5.14 Configurations of the proposed capactively-fed VSRR antennas. (a) Perspective view of the RIS-loaded antenna, (b) Perspective view of the un-loaded antenna, and (c) Top view of the RIS-loaded antenna. The geometrical parameters are for the unloaded case: $a_1 = 9.0$ mm, $a_2 = 9.15$ mm, $R_1 = 1.63$ mm, $R_2 = 1.5$ mm, $s_1 = 0.23$ mm, $l_1 = 27.8$ mm, $w_1 = 20$ mm, $l_2 = 13.43$ mm, $w_2 = 5.77$ mm $l_3 = 2.83$ mm, $w_3 = 0.52$ mm, $d_1 = 5.47$ mm, $d_3 = 1.95$ mm, and $d_4 = 5.5$ mm. There are three vias on each of the two ends with a radius of 0.15 mm and a spacing of 2 mm. For the loaded case: $l_2 = 16.03$ mm, $w_2 = 5.77$ mm, $l_1 = 26.5$ mm, $w_1 = 20$ mm, $a_1 = 9.0$ mm, and $a_2 = 9.15$ mm.

surface. It is reminded that here three parameters can be used to optimize the matching: the probe positing along x axis, the size and width of the ring slot, and the vias. The substrate material used here is the same as the previous antennas.

The equivalent circuit for these two antennas is shown in Figure 5.15. This circuit is similar to the circuit model shown in Figure 5.2 except for the coupling capacitor C_{in} . The VSRR is still modeled as a parallel *LC* resonator associated with a radiation resistor. The antenna is excited by applying a voltage difference on the capacitor C_r . Figure 5.16 shows the full-wave simulated input impedance for the two antennas. Due to a capacitive input



Figure 5.15 Equivalent circuit model for the proposed capacitively-fed VSRR antennas shown in Figure 5.14.



Figure 5.16 Simulated complex input impedance for the capacitively -fed VSRR antennas shown in Figure 5.14 with or without the RIS.

coupling, the reactance is mainly negative and close to zero at their resonance frequency. By loading the RIS, it is seen that the resonance frequency has been pushed down considerably.

B. Simulated and Measured Results

The above antennas are fabricated and tested with the standard PCB process. A photograph of the fabricated components is shown in Figure 5.17. They look very simple and compact. The simulated and measured reflection coefficients are shown in Figure



Figure 5.17 A photograph of the fabricated capacitively-fed VSRR antennas with (right) or without (left) the RIS.



Figure 5.18 The measured and simulated reflection coefficients for the capacitively-fed VSRR antennas (a) without the RIS, and (b) with RIS.



Figure 5.19 Measured and simulated far-field gain patterns for the capacitively- fed VSRR antennas without the RIS.

	Without RIS	With RIS
Sim. <i>f</i> ₀ / <i>ka</i>	2.396 GHz / 0.397	1.833 GHz / 0.347
Sim. FBW (-10 dB)	1.21 %	0.98 %
Meas. FBW (-10 dB)	1.22 %	1.10 %
Sim. Peak Gain	-0.535 dBi	-4.93 dBi
Sim. Directivity	3.027 dBi	2.508 dBi
Sim. Efficiency	44.04%	18.04%
Meas. Gain	-0.4 dBi	-3.86 dBi
Meas. Efficiency	45.0%	22.5%

Table 5.9 A Performance Comparison for the Capacitively-Fed Antennas

Note that the simulated and measured gain is the realized gain which has taken the mis-matching into account. For the antenna with RIS, *ka* is calculated without considering the size increase introduced by the RIS.

5.18. Due to the shift of dielectric constant the resonance frequency for these antennas also moves up which is similar to the antennas shown in the above section. We measured the radiation patterns for them and plotted the gain pattern for the un-loaded case in Figure 5.19. Good agreement is observed. Low cross polarization is achieved. Table 5.4 shows the summarized the antenna characteristics including the fractional bandwidth, gain and radiation efficiency. The measured gain is higher than the simulated data, which

is also due to the decrease of the material loss tangent and the rise of resonance frequency. By loading the RIS, *ka* is changed from 0.397 to 0.347 while the measured radiation efficiency is also reduced from 45.0% to 22.5%. It is seen that for these ESAs, size reduction could substantially deteriorate the radiation efficiency. Compared with Table 5.3 and 5.4, it is found that the inductively-fed antennas provide a relatively better radiation performance than the capactively-fed antennas.

5.1.3 Capactively-Fed Asymmetric VSRR Antennas

The performance and characteristics of the capacitively-fed asymmetric VSRR antennas are presented and discussed in this section.

A. Configuration and Working Principle

Figure 5.20 shows the geometrical layout of the proposed capacitively-fed asymmetric VSRR antennas. The substrate is the same as shown in Figure 5.1(c). The vias on one side is removed and the coaxial feeding probe becomes part of the current loop. We immediately provide an equivalent circuit model of the antennas as shown in Figure 5.21. Since one side is open the wave may radiate away from this open boundary. Note this circuit is just a simplified approximation which is used to roughly explain the working principle. In fact a small radiation resistor should also be applied parallel to the capacitor $C_{\rm g}$. The capacitor $C_{\rm in}$ represents the capacitive coupling between the probe and the top surface. It should be pointed out that since the total capacitance of the VSRR is reduced due to the series connection of $C_{\rm r}$ and $C_{\rm g}$, the resonance frequency is higher compared with the previous two cases. In other words, their electrical size is larger. Another influence is that due to the edge radiation, the main beam direction may be shifted from



Figure 5.20 Configurations of the proposed asymmetric capaciticely-fed VSRR antennas. (a) Perspective view of the RIS-loaded antenna, (b) Perspective view of the un-loaded antenna, and (c) Top view of the RIS-loaded antenna. The geometrical parameters for the are: $a_1 = 9.0$ mm, $a_2 = 9.15$ mm, $R_1 = 1.1$ mm, $R_2 = 0.7$ mm, $s_1 = 0.23$ mm, $l_1 = 26.5$ mm, $w_1 = 20$ mm, $l_2 = 16.33$ mm, $w_2 = 6.89$ mm, $w_3 = 0.66$ mm, $l_3 = 3.73$ mm, $d_1 = 3.22$ mm, $d_2 = 2.35$ mm, $d_3 = 3.4$ mm, and $d_4 = 5.5$ mm. There are three vias on each of the two ends with a radius of 0.15 mm and a spacing of 1.5 mm. The two antennas have the same size.

the Z-direction leading to an asymmetric beam pattern in E-plane. We also designed two antennas with or without the RIS as shown in Figure 5.20(a) and (b). The input impedance for two optimized designs is provided and compared in Figure 5.22. It is clearly seen that the resonance frequency is pushed down from 2.764 GHz to 2.44 GHz due to the RIS loading. The reactance is mainly negative because of the capacitive coupling. It approaches zero at the two matching points. Note that the matching can also be easily obtained by changing the probe position and the ring slot size or width.



Figure 5.21 Equivalent circuit model for the proposed asymmetric capaciticely-fed VSRR antennas shown in Figure 5.20.



Figure 5.22 Simulated complex input impedance for the asymmetric capacitively-fed VSRR antennas shown in Figure 5.20 with or without the RIS.

B. Simulated and Measured Results

The two antennas are fabricated and tested. Figure 5.23 shows a photograph of the fabricated antenna prototype. They still look compact even though that they are larger compared with the previous antennas. Figure 5.24 shows the simulated and measured reflection coefficients. They are well matched and the small frequency shift is due to the change of the dielectric constant. Figure 5.25 shows the simulated and measured gain patterns in two principle cuts. As predicted we found that the main beam direction in E-plane is shifted away from the broadside due to the open boundary or the unsymmetrical



Figure 5.23 A photograph of the fabricated asymmetric capaciticely-fed VSRR antennas with (right) or without (left) the RIS.



Figure 5.24 The measured and simulated $|S_{11}|$ for the asymmetric capaciticely-fed VSRR antennas (a) without the RIS, and (b) with RIS.



Figure 5.25 Measured and simulated far-field gain patterns for the asymmetric capaciticely-fed VSRR antennas (a) without the RIS, and (b) with RIS.

	Without RIS	With RIS	
Sim. <i>f</i> ₀ / <i>ka</i>	2.764 GHz / 0.541	2.44 GHz / 0.478	
Sim. FBW (-10 dB)	1.52 %	1.44 %	
Meas. FBW (-10 dB)	1.72 %	1.74 %	
Sim. Peak Gain	0.246 dBi	-2.066 dBi	
Sim. Directivity	3.15 dBi	2.355 dBi	
Sim. Efficiency	51.2%	36.13%	
Meas. Gain	0.49 dBi	-1.66 dBi	
Meas. Efficiency	52.0%	38.9%	

Table 5.10 A Performance Comparison For the asymmetric Capacitively-Fed Antennas

Note that the simulated and measured gain is the realized gain which has taken the mis-matching into account. For the antenna with RIS, ka is calculated without considering the size increase introduced by the RIS.

configuration. This may be useful for some special pattern diversity antenna systems. We also summarized the radiation performance for these two antennas in Table 5.5. The measured radiation efficiency is 52% for the un-loaded case and 38.9% for the loaded case. Small discrepancy between simulation and measurement also come from the change of the loss tangent of the material. Comparing Table 5.3, 5.4 and 5.5, we found that the inductively-fed antennas have the best performance in terms of both the radiation efficiency and bandwidth.

5.2 Miniaturized Patch Antennas Loaded with CSRRs

This section presents a comprehensive study into the patch antennas loaded by CSRRs over an RIS. The CSRR is embedded on the top surface as a high-Q resonator which can couple the field to the antenna patch and make it radiate. The structure of the adopted CSRR and its equivalent-circuit model are depicted in Figure 3.1. The CSRR is modeled as a shunt *LC* resonator tank which can be excited by the orthogonal electric field. It can be equivalent to an electric dipole placed along the ring axis [1]. As a dipole it essentially generates wave propagating along the plane of ring surface and relies on the edges of patch for radiation. The coupling between the CSRR and patch mainly comes from the capacitive coupling through the ring slot and the magnetic coupling through the split of the outer ring. By properly feeding the antenna, the inherent half-wavelength patch resonant mode can still be well excited. It is interesting to note that the interaction between the CSRR-inspired resonance and the patch resonance is very weak when they are orthogonally polarized. Under this condition circular polarization (CP) is attainable when they share the same operating frequency with a 90° phase delay in excitation. In

addition the interaction is strong when they are polarized in the same plane, which gives rise to two mixed modes. The RIS is employed to further decrease the resonance frequency and improve the antenna radiation performance. When it works as an inductive surface it is able to store the magnetic energy and increases the inductance value of the patch type resonance. The resonance frequency of the patch, which is inherently a parallel *RLC* resonator, is shifted down in this way resulting in the miniaturization. It is shown that the antenna polarization state can be easily changed by altering the configuration of the CSRRs. Dual-and triple-band operations can also be achieved by appropriately exciting the CSRRs and the microstrip patch. A circularly-polarized antenna has also been developed by exciting two orthogonally-polarized modes with a 90° phase difference. Six different antennas are fabricated and measured to verify the simulation based on the multi-layer PCB process. The proposed antennas show advantages in terms of the compact size, low-fabrication cost, low-cross polarization level and the multi-band operation with flexible polarization states. In the following parts the six antennas will be studied and presented in each different section with a detailed analysis provided to the first antenna. Here the simulation is performed using Ansoft's High Frequency Structure Simulator (HFSS) software package.

5.2.1 Patch Antenna Loaded with CSRRs and RIS

Here the characters of the CSRR-loaded patch antenna over an RIS will be investigated and discussed in detail using an antenna model loaded with two CSRRs which are faceto-back oriented. An equivalent circuit for the proposed structure is derived to gain an



Figure 5.26 Configurations of the proposed CSRR-loaded patch antenna over an RIS. The CSRRs are face-to-back oriented and the feeding probe is in the center. (a) Perspective view, (b) Top view, and (c) Side View.

insight into the working principle. The design of CSRRs is summarized. The features and influence of the RIS is also presented.

A. Configuration

Figure 5.26 shows the geometrical layout of the proposed antenna with two CSRRs face-to-back oriented with respect to the direction of the ring split. This configuration is chosen here since it is simpler than the side-by-side configuration which will be discussed later. A coaxial probe-feeding is utilized and placed in the center of the microstrip patch. Due to this center feeding no patch resonances can be excited. Also the alternative cases with two CSRRs either face-to-face or back-to-back oriented could not radiate well due to a symmetrical structure which cancels all the radiation from the patch edges. Under those conditions the main radiation should come from the ring slot of the CSRR. However, as explained later the CSRR is a high-Q resonator instead of a good radiator. To verify this conclusion we also simulated these two cases and found that the resonance could still be excited at a little higher frequency but the radiation efficiency for both of the two cases is below 0.7%. Face-to-back case is a good option since the patch can radiates well. The RIS, which is composed of a periodic array of metallic square patches printed on a metal-backed dielectric substrate, is introduced below the top surface. It is a three-layer structure where the top and bottom dielectric substrate is "MEGTRON 6" with a relative permittivity of 4.02 and a measured loss tangent of 0.009 at 2.4 GHz.

B. Equivalent Circuit Model

Figure 5.27(a) shows the circuit model of a conventional probe-fed microstrip patch antenna. The input impedance of the patch antenna is modeled as an RLC resonator near its resonance frequency. The series inductor represents an inductive probe feeding. The



Figure 5.27 Equivalent circuit model for (a) Conventional probe-fed patch antenna, and (b) Proposed patch antenna loaded with CSRRs.

structure of Figure 5.26(a) can be roughly represented by the circuit model shown in Figure 5.27(b). The CSRR is modeled as a high-Q shunt-connected RLC resonator tank $(R_L, L_r \text{ and } C_r)$ which has been designed to exhibit a lower resonance frequency compared with microstrip patch. R_L denotes the losses including both the conductor and dielectric losses. The probe inductance is represented by L_{in} . Due to the equivalence to an electric dipole, the wave generated by the CSRR is mainly propagating along the *x-y* plane inside the substrate and radiates when it arrives at the edges of the patch. The CSRR itself has little radiation since the radiation from the ring slot would cancel itself. To verify this viewpoint we have created a model with the CSRR etched on a rectangular cavity. Unlike other cavity-backed slot antennas, little radiation through the ring slot is detected and most of power is dissipated by the loss, which demonstrates that the CSRR itself is not a good radiator. The field can be coupled from the CSRR to the patch and radiates away

using the radiation resistance (R_p) of the microstrip patch. It is noted that this coupling is a combination of the inductive and the capacitive couplings, where the former comes from the connection through the split of the outer ring and the latter comes from slot coupling. The same situation applies to the coupling between the feeding probe and the CSRR. Here it is also pointed out that this circuit model is just a simplified approximation where we have neglected the direct coupling between the two CSRRs on the two sides. Since the structure is not symmetrical, the coupling for the two CSRRs is different. The series inductance is relatively larger when the ring split is far away from the feeding probe on the other side. Since the value of the coupling elements is different, the resonance frequency looking into circuit also varies. Therefore two resonances could be observed on the input impedance which will be shown later in Figure 5.35(a).

C. CSRR

It would be helpful to know the characters and design methodology for the CSRRs while designing the proposed CSRR-loaded patch antennas. Here we adopted an approach based on the eigen-mode simulation to quickly obtain the resonance frequencies. In this setup, the CSRR is etched on the surface of a dielectric-filled rectangular cavity. Note that cavity itself is resonating at a much higher frequency. First we simulated an example given in [1] and found a good agreement. Then based on this method we extracted the resonance frequency for the rectangular CSRRs used in our antennas. Figure 5.28(a) shows the field distribution from eigen-mode simulation for the CSRR used in this design. A series of simulations has been carried out by changing the parameters to investigate the properties of the CSRR. The results are displayed in Figures



Figure 5.28 An investigation into the features of the CSRR inherent resonance frequency based on HFSS eigen-mode simulation. The initial CSRR is etched on the surface of a rectangular cavity and resonates at 3.075 GHz. (a) Field distribution at the CSRR resonance frequency; (b) The resonance frequency versus the substrate thickness h; (c) The change of the resonance frequency with different CSRR geometries (l_1+w_1 is fixed here); (d) The variation of resonance frequency for different slot width c. (e) Simulated resonance frequency versus the strip width g. The parameters are: $l_1 = 6.3$ mm, $w_1 = 7.8$ mm, $c = c_1 = c_2 = 0.45$ mm, g = 0.5 mm and d = 0.5 mm.

5.28(b) to (e).

Figure 5.28(b) shows the influence of the substrate thickness to the resonance frequency. The decrease of thickness corresponds to an enhancement of the capacitance

 C_r which leads to a decrease of the resonance frequency. Figure 5.28(c) shows how the variation of the geometry affects the resonance frequency. The perimeter (l_1+w_1) is set to be fixed. It is seen that the CSRR resonance frequency has a very small variation when the geometry changes. It has a minimum value for a square shape. This is predictable since this shape gives the maximum area resulting in a maximum C_r and finally a minimum resonance frequency. It is worth noting that for the CSRR-loaded patch, the coupling can be adjusted by the change of the CSRR geometry since the CSRR frequency is almost not affected. When slot width *c* is reduced, the capacitance C_r is increased and the resonance frequency is decreased. Figure 5.28(d) verifies this conclusion. Figure 5.28(e) shows the increase of inductance L_r , achieved by reducing the strip width *g*, could also decrease the resonance frequency. Other parameters, such as the dielectric constant and CSRR size, may be used to control the frequency as well. Note the above results are obtained without the consideration of RIS.

D. RIS

The RIS is first proposed and studied in [8]. Here a brief investigation about the features is presented. As shown in Figure 5.26 it is composed by two dimensional periodic metallic patches printed on a grounded substrate. The periodicity of the metallic patches is much smaller than the wavelength. Considering a single cell illuminated with a TEM plane wave, PEC and PMC boundaries can be established around the cell as shown in Figure 5.29. The resulting structure can be modeled as a parallel LC circuit displayed in Figure 5.29. The edge coupling of the square patch provides a shunt capacitor and the short-circuited dielectric loaded transmission line can be modeled as a shunt inductor.



Figure 5.29 Unit-cell and its equivalent circuit of the RIS bounded with PEC and PMC walls and illuminated by a normal incident plane wave.

The impedance then can be obtained as:

$$Z_{\rm ris} = \frac{X_{\rm L} X_{\rm C}}{X_{\rm L} - X_{\rm C}} \tag{5.1}$$

where

$$X_{\rm L} = jZ_{\rm d} \tan kh_2 = jZ_{\rm d} \tan k_0 \sqrt{\varepsilon_{\rm r}} h_2, \quad X_{\rm C} = \frac{1}{j\omega C_{\rm ris}}$$
(5.2)

The calculation of X_L and X_C has been detailed in [8]. The variation of the patch size and slot width mainly changes the capacitor value while the substrate thickness and dielectric constant mainly affects the inductance value, all of which can be used to control the resonance frequency. To better explain the role played by RIS an analysis into the near field interaction would be more meaningful and essential. Due to the matching difficulty and loss problem, PMC surface is not a proper choice. An inductive RIS is able to store the magnetic energy which thus increases the inductance of the circuit. Therefore it can be used to miniaturize the size of a patch type antenna which is essentially an RLC parallel resonator. At the same time it is shown in [8] the inductive RIS is also able to provide a wider matching bandwidth therefore it is more suitable for antenna application.



Figure 5.30 A parameter study on the RIS for the proposed antenna shown in Figure 5.26. It shows the different simulated reflection coefficients by (a) Varying h_2 while keeping h_1+h_2 fixed (3mm). (b) Varying a_1 while keeping $a_2 = 5.68$ mm. All the other parameters are the same as shown later in Figure 5.34.

E. Simulated and Measured Results

Based on HFSS commercial software package, this antenna loaded by CSRR and RIS as shown in Figure 5.26 is designed and optimized at a working frequency of 2.4 GHz. To have more design information about the RIS, a parametric study is first performed by changing the slot width between the RIS patches and the RIS thickness. The result is shown in Figure 5.30. Note that here in all these simulations the ground size is assumed



Figure 5.31 A comparison of $|S_{11}|$ for the proposed antenna with different RIS unit-cell numbers. All other parameters remain unchanged in the simulation.

to be 34 mm × 34 mm and the patch size is $12.4 \text{ mm} \times 19.2 \text{ mm}$. It is seen that the resonance frequency can be pushed down by either increasing the equivalent capacitance of the RIS or increasing the equivalent inductance. To provide a better understanding about the function of the RIS, Figure 5.31 shows the variation of antenna resonance frequency by changing of the RIS unit-cell numbers. It is seen that for the case without the RIS, the resonance frequency is 2.75 GHz shown by both the simulation and measurement. By adding the RIS, the resonance frequency has been moved down to 2.4 GHz. It is important to note that as long as the RIS covers the mircostrip patch size (minimum 3×5 unit-cells in this case), the increase of the unit-cell number only poses a very weak influence on the resonance frequency. The reason is that outside the microstrip patch region the field is weak. It is also observed that further reducing the unit-cell number could change the resonance frequency distinctly. Figure 5.32 shows a parameter analysis on the size of the CSRR and the microstrip patch. It is seen that the resonance frequency is mainly determined by the CSRR while the patch size also affects it but in a



Figure 5.32 Simulated reflection coefficients by (a) Varying l_1 while keeping the other parameters unchanged, and (b) Varying w_2 (the size of patch).



Figure 5.33 Photograph of the fabricated patch antenna loaded with face-to-back CSRRs and the RIS.



Figure 5.34 The measured reflection coefficient compared with the results from circuit simulation and full-wave simulation using HFSS and CST. The equivalent circuit parameter values are: $L_1 = 0.5$ nH, $C_1 = 4.33$ pF, $L_2 = 1.34$ nH, $C_2 = 3.08$ pF, $L_3 = 1.06$ nH, $C_3 = 1.9$ pF, $L_4 = 3.06$ nH, $C_4 = 3.13$ pF, $L_r = 1.89$ nH, $C_r = 2.16$ pF, $L_{in} = 3.07$ nH, $L_p = 0.25$ nH, $C_p = 1.46$ pF, $R_p = 48$ Ohm, $R_L = 960$ Ohm The geometrical parameters are: $a_1 = 5.0$ mm, $a_2 = 5.68$ mm, $h_1 = 0.4$ mm, $h_2 = 2.6$ mm, $s_1 = 4.9$ mm, $l_2 = 12.4$ mm, $w_2 = 19.2$ mm, $l_1 = 6.3$ mm, $w_1 = 7.8$ mm, $c_1 = c_2 = 0.45$ mm, g = 0.5 mm and d = 0.5 mm.



Figure 5.35 (a) Input impedance from HFSS full-wave simulation and equivalent circuit model shown in Figure 5.27, and (b) Electric field distribution at the two resonance frequencies. The two resonances are polarized in *y*-*z* plane which is indicated by their radiation patterns.

weaker manner.

Figure 5.33 shows a photograph of the fabricated antenna. The patch size is around $0.099 \lambda_0 \times 0.153 \lambda_0$, which is very compact. The sizes of the RIS and ground are $0.22 \lambda_0 \times 0.22 \lambda_0$ and $0.272 \lambda_0 \times 0.272 \lambda_0$, respectively. The reflection coefficient of the antenna is measured and plotted in Figure 5.34, compared with the results from the circuit simulation and full-wave simulation using both HFSS and CST. A good agreement between them is observed. It is also important to bear in mind that since the circuit simulation cannot include the radiation for an antenna and it is simplified for the couplings and the losses, this is just a rough approximation used to explain its working principle. The values for those lumped elements are listed in the caption. Two resonance frequencies are observed which are exactly from the two circuit branches shown in Figure 5.27(b). The designed resonance is found to be at 2.406 GHz in the measurement and it exhibits an impedance match better than -20 dB. The measured relative bandwidth is 1.04%. The second resonance at 2.84 GHz is not matched as predicted by the input impedance shown in Figure 5.35(a). The simulated radiation pattern at this frequency indicates that this second resonance is also polarized in y-z plane. The field distribution at the two resonance frequencies is plotted in Figure 5.35(b). It is clearly seen that the field is coupled to the microstrip patch and radiated from the two patch edges. The CSRRs are resonating separately at each of the resonance frequencies. Due to the poor matching for the second resonance the field is only strong along the lower part of the patch and it is not well radiating. It should be pointed out that the two CSRRs have the same inherent resonance frequency. However, the appeared resonance frequencies here are not from the



Figure 5.36 Measured and simulated far-field patterns in *E*-plane (*y-z* plane) and *H*-plane (*x-z* plane) at the resonance frequency. The scale is 5 dB per division.

CSRR only but from the whole circuit. Because of the different orientation, the couplings are also different which leads to different resonance frequencies shown in Figure 5.34. The equivalent circuit shown in Figure 5.27(b) is developed in order to provide a clear picture about this working mechanism.

The radiation patterns are measured in a far-field anechoic chamber and are plotted in Figure 5.36. It is noted that the antenna is polarized in *y*-*z* plane as shown in Figure 5.35(b). The measured gain and front-to-back ratio at 2.406 GHz are -2.02 dBi and 6.5 dB, respectively, which agree with the simulation. Since the antenna is electrically small a relatively low gain is expected. The measured and simulated radiation efficiency is 22.54% and 25.5%, respectively. Here all the measured radiation efficiency is obtained using the gain/directivity (G/D) method. And the antenna directivity is measured in the near-field chamber in our department. The relatively low radiation efficiency is also due to the high dielectric loss of the substrate. Finally, it is interesting to give a comparison for the proposed CSRR-loaded antennas with the antenna without the RIS, the patch

	Patch with CSRR and RIS	Patch with CSRR only	Patch with RIS only	Simple Patch
Resonance Frequency	2.4 GHz	2.75 GHz	3.03 GHz	3.642 GHz
Sim. Gain	-2.0 dBi	0.267 dBi	4.076 dBi	5.11 dBi
Sim. Efficiency	25.5 %	36 %	76.7 %	84.6 %

Table 5.11 A Comparison for the antennas with the Same Size but with Different Loadings

antenna with RIS but without the CSRR, and the simple patch antenna without the RIS or CSRR. For the patch antennas without the CSRR we excited the *y*-*z* direction resonance by changing probe position, which means that they have the same polarization and patch size. Table 5.7 shows the comparison on the resonance frequency, simulated gain and radiation efficiency.

5.2.2 Dual-Band Dually-Polarized Antenna

The antenna shown in the previous section is excited by a probe fed in the center and is polarized in *y*-*z* plane. By moving the probe off the center along *x*-direction, the original 2.4 GHz resonance still exists only with the matching a little affected, while a conventional microstrip patch resonance can be excited simultaneously, which is polarized in *x*-*z* plane. Note that when the antenna is fed in the center no half-wavelength patch resonance can be excited due to a symmetrical structure requiring a symmetrical field distribution. Also since this patch resonance is orthogonally polarized compared with the CSRR-inspired resonance, their interaction is relatively small. Figure 5.37 presents the detailed structure and a photograph of the fabricated antenna. It is noted that this antenna has exactly the same dimensions as the first antenna except the difference in the probe feeding position.



Figure 5.37 (a) Perspective view and (b) A photograph of the proposed dual-band duallypolarized antenna with face-to-back CSRRs. Parameter value are the same as the first one, $s_2 = 2.8$ mm.



Figure 5.38 Measured and simulated reflection coefficient for the dual-band antenna loaded with face-to-back CSRRs.

Figure 5.38 shows the simulated and measured reflection coefficient of the antenna. The two bands are measured at 2.41 GHz and 3.82 GHz. Figure 5.39 shows the electric field distribution at the two resonance frequencies. The simulated and measured radiation patterns are plotted in Figure 5.40. As expected the two resonances have orthogonal polarizations. The first resonance is polarized in *y*-*z* plane while the second one is polarized in *x*-*z* plane. The measured gain at the two resonance frequencies is -2.13 dBi and 5.04 dBi, respectively. The measured bandwidth for the two bands is 0.91% and



Figure 5.39 Electric field distribution at the two operating frequencies: 2.4 GHz and 3.79 GHz.



Figure 5.40 Measured and Simulated far-field patterns at (a) 2.4 GHz, and (b) 3.79 GHz. The *E*-plane is *y*-*z* plane for the first band and *x*-*z* plane for the second band. The display scale is 5 dB per division.

1.76%. The front-to-back ratio is 5.17 dB at the first frequency and 12.87 dB at the second frequency. The corresponding radiation efficiencies are 25.3% and 80.2% in the simulation, and 22.8% and 74.5% in the measurement. The low efficiency at the first band is due to the high conductor and dielectric losses. The CSRR is essentially a high-Q



Figure 5.41 (a) Perspective view, (b) A photograph, and (c) Top view of the proposed dual-band equally-polarized antenna with side-by-side CSRRs. The geometrical parameters are: $a_1 = 5.2 \text{ mm}, a_2 = 6 \text{ mm}, h_1 = 0.4 \text{ mm}, h_2 = 2.6 \text{ mm}, s_1 = 5.3 \text{ mm}, s_2 = 3.6 \text{ mm}, l_2 = w_2 = 20 \text{ mm}, l_1 = w_1 = 7.7 \text{ mm}, c_1 = c_2 = 0.41 \text{ mm}, g = 0.7 \text{ mm} \text{ and } d = 0.6 \text{ mm}.$

resonator which induces strong current and field along the ring position. This strong current would take away considerable power resulting in a reduced efficiency. By employing low-loss material the efficiency can be substantially increased.

5.2.3 Dual-Band Equally-Polarized Antenna

From the antenna discussed in the previous part, it is seen that the polarization of the antenna resonance excited by the CSRRs is mainly determined by their orientations. In this section a dual-band antenna with the same polarization is designed by utilizing this feature. Two CSRRs are side-by-side equally placed on the patch as shown in Figure



Figure 5.42 Measured and simulated reflection coefficient for the dual-band equally-polarized antenna loaded with side-by-side CSRRs.

5.41. It is worth noting that all the antennas designed here use the same substrate as the first antenna indicated by Figure 5.26(c). The CSRRs are embedded in the middle of the patch along the *y*-direction. A photograph of the fabricated antenna is displayed in Figure 5.41. In terms of the wavelength of the first resonance frequency, the patch size is around 0.158 $\lambda_0 \times 0.158 \lambda_0$, and the sizes of the RIS and ground are $0.23 \lambda_0 \times 0.23 \lambda_0$ and $0.277 \lambda_0 \times 0.277 \lambda_0$, respectively. Figure 5.42 shows the measured and simulated reflection coefficient. It is seen that two resonances are excited with a good impedance matching. The resonance frequencies are simulated at 2.37 GHz and 2.93 GHz, and are measured to be 2.386 GHz and 2.958 GHz. The measured -10 dB bandwidth is 1.32% for the first band and 2.68% for the second band. It is also noted that the patch resonance by removing the CSRR occurs at 2.88 GHz. The initial patch and the CSRRs couple to each other generating two mixed modes polarized in the same direction. The coupling is through both the electric and magnetic couplings. Since the orientation of the CSRR coincides with the patch antenna polarization plane, which facilitates the interaction



Figure 5.43 Electric field distribution at the two operating frequencies: 2.37 GHz and 2.93 GHz.



Figure 5.44 Simulated $|S_{11}|$ by (a) Varying w_1 where $l_1 = w_1$, and (b) Varying l_2 (the length of the patch). Other parameters remain the same.

between them, the coupling is substantially enhanced. Figure 5.43 shows the field distribution for the two resonances. It is observed that the field is strong along the left edge of the patch for the first resonance, meaning a strong slot coupling and a large



Figure 5.45 Measured and Simulated far-field patterns at (a) The first resonance frequency, and (b) The second resonance frequency. The *E*-plane is x-z plane for both of the two resonances. The display scale is 5 dB per division.

coupling inductor (weak inductive coupling due to a large distance). While for the second resonance the field is strong along the right edge, meaning a smaller coupling inductor due to a small distance. Figure 5.44 gives a parametric study on the size of the CSRR and the patch. It is seen that both of them can be used to control the antenna resonance frequencies, which indicates that the patch and the CSRR are mixed giving rise to two resonating modes.

Figure 5.45 shows the measured and simulated radiation patterns for the antenna. The cross polarization level is too low to be observed in the plot. The gain at the two resonance frequencies is simulated to be -0.1 dBi and 2.99 dBi, which correspond to



Figure 5.46 (a) Perspective view, (b) A photograph, and (c) Top view of the proposed dual-band, orthogonally-polarized antenna with side-by-side CSRRs. The geometrical parameters are: $a_1 = 5 \text{ mm}, a_2 = 6 \text{ mm}, h_1 = 0.4 \text{ mm}, h_2 = 2.6 \text{ mm}, s_1 = 4.6 \text{ mm}, s_2 = 3.8 \text{ mm}, l_2 = w_2 = 19.9 \text{ mm}, l_1 = w_1 = 7.3 \text{ mm}, c_1 = c_2 = 0.38 \text{ mm}, g = 0.7 \text{ mm} \text{ and } d = 0.6 \text{ mm}.$

40.7% and 63.8% simulated radiation efficiencies. The measured gain is 0.21 dBi and 3.13 dBi, corresponding 38.5% and 59.3% measured radiation efficiencies. The measured front-to-back ratio is 8.16 dB and 14 dB, respectively.

5.2.4 Dual-Band Dually-Polarized Antenna with Side-by-Side CSRRs

In this section we show that dual-band antenna with orthogonal polarizations can also be obtained by side-by-side reversing the orientation of the CSRRs. The structure and photograph of the fabricated antenna is shown in Figure 5.46. In terms of the wavelength of the first resonance frequency, the patch size is around $0.15 \lambda_0 \times 0.15 \lambda_0$, and the sizes


Figure 5.47 Electric field distribution at the two operating frequencies: 2.27 GHz and 2.78 GHz.



Figure 5.48 Simulated reflection coefficients by (a) Varying w_1 (the CSRR size) where $l_1 = w_1$, and (b) Varying w_2 (the patch size) where $l_2 = w_2$.

of the RIS and ground are $0.219 \lambda_0 \times 0.219 \lambda_0$ and $0.265 \lambda_0 \times 0.265 \lambda_0$, respectively. The CSRRs are side-by-side reversely placed in the center of the patch. It is to be noted that



Figure 5.49 The measured and simulated reflection coefficients for the dual-band, orthogonally-polarized antenna loaded with side-by-side CSRRs.

due to the configuration the two CSRRs reach the electric field maximum with a phase difference of 180°, which means that the positive maximum for one CSRR corresponds to the negative maximum for the other one. This is also indicated by the field distribution shown in Figure 5.47. Unlike the symmetrical configuration of the previous antenna, for this case the field can be coupled from one CSRR to the other one directly. The coupling between two CSRRs has also been studied in [5]. The resonance generated here by the CSRRs is polarized in $\varphi = 135^{\circ}$ which is along the diagonal line of the square patch. Another resonance, which is the inherent patch resonance, is excited along the perpendicular direction as shown in Figure 5.47, which is similar to the corner-truncated or corner-fed dually polarized patch antennas [10]. This pair of resonances is generated independently with little interference. Figure 5.48 shows a parametric study by changing the patch and the CSRR. It is obviously seen that the first resonance is mainly determined by the CSRRs while the second one is mainly controlled by the microstrip patch. Figure 5.49 shows measured and simulated reflection coefficient, where the two resonances are



Figure 5.50 Measured and simulated far-field patterns at (a) the first resonance frequency, and (b) the second resonance frequency. The *E*-plane is at $\varphi = 135^{\circ}$ for the first band and $\varphi = 45^{\circ}$ for the second band.

observed at 2.27 GHz and 2.78 GHz in the simulation, and 2.31 GHz and 2.83 GHz in the measurement. A little frequency shift is observed which is probably due to the change of the dielectric constant and the fabrication error. The measured -10 dB bandwidth for the two bands is 1.38% and 3.29%. It should be pointed out that there is another resonance around 2.97 GHz which is brought by the CSRRs. However it is not matched and appears to be very weak.

Figure 5.50 shows the measured and simulated radiation patterns. The measured frontto-back ratio for the two bands is 8.33 dB and 14.4 dB, respectively. The gain is



Figure 5.51 (a) The perspective view and (b) a photograph of the proposed and fabricated circularly-polarized antenna with side-by-side CSRRs. The geometrical parameters are: $a_1 = 5 \text{ mm}, a_2 = 6 \text{ mm}, h_1 = 0.4 \text{ mm}, h_2 = 2.6 \text{ mm}, s_1 = 5.2 \text{ mm}, s_2 = 4.5 \text{ mm}, l_2 = w_2 = 19.9 \text{ mm}, l_1 = 6.15 \text{ mm}, w_1 = 5.95 \text{ mm}, c_1 = c_2 = 0.48 \text{ mm}, g = 0.7 \text{ mm} \text{ and } d = 0.6 \text{ mm}.$

simulated to be -3.14 dBi and measured as -2.09 dBi for the lower resonance. For the second one it is simulated as 3.13 dBi and measured to be 3.85dBi. Considering the patch size is $0.15 \lambda_0 \times 0.15 \lambda_0$ only, the antenna efficiency is relatively low, which is simulated to be 22% for the first resonance and 69.2% for the second resonance. The measured antenna radiation efficiency for the two bands is 24.45% and 71.8%, respectively. The discrepancy is mainly caused by the shift of the resonance frequency and probably a smaller loss tangent for the real material.

5.2.5 Circularly-Polarized Antenna

Based on the dual-frequency, orthogonally-polarized antenna proposed in the above part, a circularly-polarized antenna is designed here. The principle is to overlap the two working frequencies and excite these two resonances with a 90° phase difference. Since the probe feed is in the center and the wave goes to the two diagonal lines oppositely with 45° phase delay, the 90° phase difference can be automatically introduced. The reason is that at the resonance frequency, the wave travels from one edge to the opposite edge with



Figure 5.52 The measured and simulated reflection coefficients for the circularly-polarized antenna loaded with side-by-side CSRRs.



Figure 5.53 Measured and simulated far-field patterns at the center frequency in x-z plane and y-z plane. The display scale is 5 dB per division.



Figure 5.54 Measured and simulated AR and the realized gain for the CP antenna.



Figure 5.55 Simulated AR at the center frequency in two different planes.

180° phase delay. Now the wave propagates from the probe to the diagonal plane covering an angle of only 45°, which give rise to 45° phase delay. Here only the impedance matching needs to be improved, which is the *x*-position of the probe feed. The size of the CSRRs is scaled down in order to push up its resonance frequency. The final structure, as well as a photograph of the fabricated antenna, is shown in Figure 5.51. This antenna has a patch size of $0.186 \lambda_0 \times 0.186 \lambda_0$, an RIS size of $0.271 \lambda_0 \times 0.271 \lambda_0$, and a ground size of $0.327 \lambda_0 \times 0.327 \lambda_0$. The measured and simulated reflection coefficient is shown in Figure 5.52. The center frequency is 2.8 GHz and the -10 dB bandwidth is 5.03% in the simulation. And in the measurement they are 2.824 GHz and 4.9%.

The radiation characters of the CP antenna are tested in the UCLA spherical chamber. The measured and simulated radiation patterns in x-z and y-z plane are shown in Figure 5.53. The discrepancy is mainly due to the interference of the testing equipment. The measured and simulated gain and axial ratio (AR) are shown in Figure 5.54. The measured and simulated AR at center frequency in x-z plane and y-z plane is also



Figure 5.56 Three-dimensional (a) radiation pattern and (b) AR measured in a spherical near field chamber at the center frequency.

provided in Figure 5.55. The bandwidth for AR less than 3 dB is observed as 1.60% in the simulation and 1.68% in the measurement. Figure 5.56 shows the measured threedimensional AR and radiation patterns. It is seen that a CP radiation is retained in a very wide region and the pattern is very similar to a traditional patch antenna. This antenna radiation efficiency is observed to be 80% in the simulation and 74.1% in the measurement.

5.2.6 Triple-band Antenna with Varied Polarizations

In this part a triple-band antenna with different polarization states is developed. The structure, as shown in Figure 5.57, is similar to the previous two antennas. Two CSRRs are side-by-side reversely embedded on the top surface. They are shifted from the patch center by S_3 . Also the patch itself is not a square patch. This structure is able to generate three resonances at same time with a proper feeding. Two of them, the first and the third one, come from the CSRRs and the second one is mainly excited by the microstrip patch. This is justified by comparing it with the inherent patch resonance frequency and



Figure 5.57 (a) Perspective view, (b) A photograph, and (c) Top view of the proposed tripleband antenna with different polarizations. The geometrical parameters are: $a_1 = 5$ mm, $a_2 = 6$ mm, $h_1 = 0.4$ mm, $h_2 = 2.6$ mm, $s_1 = 6.2$ mm, $s_2 = 4.85$ mm, $s_3 = -1.4$ mm, $l_2 = 18.75$ mm, $w_2 = 21.6$ mm, $l_1 = 7.4$ mm, $w_1 = 7$ mm, $c_1 = c_2 = 0.5$ mm, g = 0.7 mm and d = 0.6 mm.

checking the field distribution. We also found that compared with the other two resonances the CSRR size is not very influential to the second resonance frequency. Figure 5.57(b) shows a photograph of the fabricated antenna. "MEGTRON 6" with a relative permittivity of 4.02 is also used here as the substrate. In terms of the wavelength of the first resonance frequency, this antenna exhibits a patch size of $0.15 \lambda_0 \times 0.17 \lambda_0$, an RIS size of $0.23\lambda_0 \times 0.23 \lambda_0$, and a ground size of $0.28 \lambda_0 \times 0.28 \lambda_0$.

Figure 5.58 shows the simulated and measured reflection coefficient. As seen the three bands are well matched to be below -22 dB. The measured -10 dB bandwidth for the three bands is 1.61%, 3.27%, and 3.08%, respectively. Figure 5.59 shows the field



Figure 5.58 Measured and simulated reflection coefficient for the triple-band antenna loaded with side-by-side CSRRs.



Figure 5.59 Electric field distribution at the three operating frequencies: 2.4 GHz, 2.8 GHz and 3.4 GHz.

distribution at the three resonance frequencies. Clearly they have different polarization angles. The CSRRs are strongly resonating in the first and third resonances. The second resonance should mainly come from the patch itself. To verify this we calculated and found that the inherent patch resonance (without CSRRs) in *y*-direction occurs at 2.78 GHz, which is very close to the resonance frequency of this second mode. Their *E*planes are located at $\varphi = 110^{\circ}$, 54°, and 160°, respectively. To confirm this, a near field measurement was performed in the spherical near field chamber which directly verifies the polarization angles from simulation. Figure 5.60 shows the measured pattern from a



Figure 5.60 Measured and simulated far-field patterns in their principle *E*-plane and *H*-plane at (a) 2.426 GHz, (b) 2.845 GHz, and (c) 3.373 GHz. The display scale is 5 dB per division.

far-field measurement, compared with the simulated data. It is noted that they are measured in their own *E*-plane and *H*-planes independently. The measured front-to-back ratio for the three bands is 6.5 dBi, 8.3 dBi and 13.0 dBi. The gain measured at these



Figure 5.61 The variation of the principle *E*-plane angles by changing S_3 (*x*-position of the CSRRs). Other parameters remain unchanged.

 Table 5.12 Polarization Influencing Factors for a CSRR-Loaded Patch Antenna with fixed CSRR and Patch Configuration

	Polarization of the CSRR- inspired Resonance	Polarization of the Patch Resonance	Examples
Symmetric Structure	CSRR orientation	Not affecting	Antennas in Section IV
Un-Symmetric Structure	CSRR orientation, CSRR position	CSRR orientation, CSRR position	Antennas in Section II, V, VII

Note that besides the above factors, the patch geometry and feeding position are also capable of changing the polarization of the resonances.

three resonance frequencies is 0.27 dBi, 3.31dBi, and 4.45 dBi, respectively. Their corresponding measured efficiencies are 43.7%, 69.8% and 75.5%, which are very close to the simulated efficiencies: 41.9%, 68.5% and 77.62%.

Finally, it is interesting to note that their principle polarization angles can be steered simply by changing the position of the CSRRs (S_3 : the x-distance between the patch center and the CSRR center). Figure 5.61 shows the simulated *E*-plane angle variations for all the three modes. It is seen they are rotated together as the CSRRs move along the *x*-direction. The reason for this variation is that the split of the CSRRs plays an important

role in the wave coupling which affects the polarization angle. The position of the CSRRs also affects the patch resonance since they block the original wave propagation and lead to the modification of the field pathway. Table 5.8 summarizes the influencing factors on polarization for the different CSRR-loaded antennas.

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Chapter 6

Miniaturized Planar UWB Antennas for Diversity Applications

It is well known that strong reliability, high data-rate and robustness are favorable features for wireless communication systems. However, the radio channels are usually situated in dense, complex and rapidly time-varying environments which make it very challenging to achieve efficient and robust wireless links. Diversity antennas at the transmitter and the receiver can effectively increase the capacity of wireless links by introducing new channels, and therefore provide more reliability for the communication systems [1], [2]. They appear as good candidates for the efficient use of the limited spectra and spatial resources. Basically these diversity antennas can be classified into four categories: pattern diversity [3], polarization diversity [4-7], frequency diversity [8] and spatial diversity [9] antennas.

Many progresses on diversity antennas have already been achieved [3-9]. Due to the advantages such as compactness, low cost, and high integration ability, planar microstrip patch antennas have received substantial attention for practical implementation. However, these antennas usually suffer from small bandwidth [5]. Much effort has been dedicated by engineers to the design of broadband and compact diversity antennas. Ultrawideband (UWB) techniques can be applied for diversity applications [10-14]. The combination of the UWB and diversity technologies could enable high data rate and good



Figure 6.1 Working scheme of the proposed dual-fed UWB diversity antennas.

resolutions, which can be potentially used for imaging, data transfer, localization, and radar application. The initial UWB band authorized by the Federal Communication Commission (FCC) covers the frequency range of 3.1-10.6 GHz. A wide variety of antennas have been developed to be operated in this range, including both the omnidirectional antennas, such as the monopole-type antennas [15-20], and the directional antennas, such as the Log-Periodic dipole antenna [21], Vivaldi antenna [22], horn antenna, planar quasi-Yagi antenna [23] and cavity backed antenna [24].

In this chapter, two UWB diversity antennas are proposed and presented which are specially designed to cover the entire Ku- and K-band (12.4-26.5 GHz). Recently this frequency range receives some particular research interest due to the development of high frequency communication systems. They are developed based on the initial UWB monopole antenna concept with a two-orthogonal-port configuration. The basic idea is to arrange two UWB antennas together perpendicularly to share the same monopole element in order to reduce the antenna size as described by Figure 6.1. By changing the feeding signals applied at the two ports, different radiation characteristics can be obtained. The first antenna developed here is a pattern diversity antenna utilizing a disc patch, while the second antenna is a polarization diversity antenna based on a square patch. Their ground,

which is printed on the reverse side of the PCB substrate, is modified and optimized in order to increase the isolation and achieve different radiation functions. Detailed simulation results are presented. To experimentally evaluate their performance two broadband couplers, including a two-stage rat-race coupler and a three-stage branch-line coupler, are designed and integrated with the antenna for excitation purpose. The measured radiation performance is demonstrated, which shows good agreement with the simulated data.

6.1 Pattern Diversity UWB Antenna

6.1.1 Antenna Configuration

Figure 6.2 shows the geometry of the proposed pattern diversity antenna. The antenna is printed on a Rogers RT/Duroid 5880 substrate with a thickness of 0.254-mm and a dielectric constant of 2.2. Basically the design idea comes from the UWB disc monopole antennas [16], [20]. The ground is composed by a rectangular metal and a half-oval structure with its major and minor axis depicted by r_2 and r_3 . This choice (half oval structure) is made mainly to get a smooth tapering between the disk patch and the ground. It also enables us to tune the length of the major and minor axis independently to obtain better matching. Here note that the ground of the initial monopole antenna also participates in the radiation and the slot between the disc patch and the ground acts as a tapered slot line converting the original impedance to the characteristic impedance of air. The overall antenna is built by such two antennas which are orthogonally placed and sharing the same monopole element. The antenna is excited via 50- Ω microstrip lines. A



Figure 6.2 Geometry of the proposed pattern diversity antenna. (a) Top view, and (b) Side view. The parameters are: $r_1 = 3 \text{ mm}$, $r_2 = 5.28 \text{ mm}$, $r_3 = 3.78 \text{ mm}$, $w_1 = 13.62 \text{ mm}$, $w_3 = 0.2 \text{ mm}$, $w_4 = 0.78 \text{ mm}$, $l_1 = 2.29 \text{ mm}$, $l_2 = 4.5 \text{ mm}$, $l_3 = 0.23 \text{ mm}$, $l_4 = 11.4 \text{ mm}$, tw = 0.78 mm, gw = 25.73 mm, h = 0.254 mm.



Figure 6.3 Operating principle of the pattern diversity antenna. (a) In-phase case, and (b) 180°-out-of-phase case.

microstrip taper line is employed between the monopole and the microstrip feeding line providing the impedance conversion. There is a small gap (l_3) between the monopole patch and the ground on the reverse side. To increase the isolation between the two ports we added a strip intentionally in the center which extends out from the ground plane [10], [11]. This strip is also used to suppress the radiation of the inside tapered slot line towards the inner region. Therefore the radiation is mainly contributed by the outside slot lines. The coupling through the patch itself is low since the other feeding is located at the center of the patch edge corresponding to the lowest electric field, which is similar to the conventional half-wavelength patch antenna [6].

6.1.2 Working Principle

Figure 6.3 shows the operating principle of this pattern diversity antenna where k_i (i = 1 or 2) represents the wave propagation direction. When fed at Port 1 (or 2) only, the antenna mainly radiates waves going to the $\varphi = 45^{\circ}$ (or -45°) direction. This angle may increase at lower frequencies since the ground which has a long current path generates most of the radiation under this scenario. When the antenna is excited simultaneously at Port 1 and 2 with in-phase and equal-magnitude signals, the E_y component of the electric field would be cancelled out and only the E_x component remains. The radiation consequently goes to the two sides ($\pm y$ -direction) as illustrated by Figure 6.3(a). On the other hand, when the antenna is excited with equal magnitude and 180°-out-of-phase signals, the E_x component of the electric field would be cancelled out the electric field would be cancelled and the resulting radiation goes to the +x-direction with the field polarized in y-direction. The related working scheme is illuminated by Figure 6.3(b). It is seen that by changing the input signals applied at the two ports, the radiation pattern could be easily controlled.

6.1.3 Simulated Results

Figure 6.4 shows the simulated reflection coefficient ($|S_{11}|$) and the isolation ($|S_{21}|$) between the two ports. Overall good matching (better than -10 dB) and isolation (larger



Figure 6.4 The simulated *S*-parameters and envelope correlation of the pattern diversity antenna shown in Figure 6.2.



Figure 6.5 Simulated gain patterns in x-y plane when the antenna is fed at Port 1 only. (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz. (Note that cross-polarization component is too low to be observed in (a) and (b) cases)



Figure 6.6 Simulated electric field distribution at 20 GHz for the in-phase excitation case and out-of-phase excitation case. The electrical field is plotted along the metal where only the vertical component exists.

than 15 dB) is observed in the entire K*u*- and K-band. Note that large isolation between the ports is preferred. The envelope correlation, which can be calculated using the *S*parameters as shown by (6.1) and is plotted in the inset of Figure 6.4, provides a good estimation of the diversity performance of the antenna. It is seen from the figure that the simulated envelope correlation coefficient is lower than -32 dB across the whole band.

$$\rho_{e} = \frac{\left|S_{11}^{*}S_{12} + S_{21}^{*}S_{22}\right|^{2}}{\left(1 - \left(\left|S_{11}\right|^{2} + \left|S_{21}\right|^{2}\right)\right)\left(1 - \left(\left|S_{22}\right|^{2} + \left|S_{12}\right|^{2}\right)\right)}$$
(6.1)

Figure 6.5 shows the simulated radiation pattern in *x*-*y* plane for the antenna when only Port 1 is excited (Port 2 is terminated with a 50- Ω load). It agrees with our assumption that the main radiation comes from the outside slot taper line and goes to the $\varphi = 45^{\circ}$ direction. At a lower frequency which corresponds to a larger wavelength this beam angle increases as indicated by the 16 GHz case. This is due to the fact that for a small resonance frequency or a large wavelength the radiation mainly comes from the ground



Figure 6.7 Simulated gain patterns in x-y plane when the antenna is excited with in-phase signals at (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.



Figure 6.8 Simulated 3D radiation patterns when the antenna is excited with in-phase signals at the two ports. (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.



Figure 6.9 Simulated gain patterns in x-y plane when the antenna is excited with out-of-phase signals at (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.



Figure 6.10 Simulated 3D radiation patterns when the antenna is excited with out-of-phase signals at the two ports. (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.

which is able to provide a long current path.

Figure 6.6 shows a plot of the field distribution at 20 GHz for this pattern diversity antenna to help the readers better understand its operating principle. The field distribution for both the in-phase and out-of-phase cases clearly demonstrates that the antenna works as a tapered slot line travelling-wave radiator. Figure 6.7 shows the simulated radiation patterns in x-y plane (E-plane) for the in-phase excitation case while its 3-D radiation patterns are provided in Figure 6.8. It is seen that the radiation is mainly going to the two sides ($\pm y$ -direction) and the patterns are stable across the frequency range. The simulated peak gains at 16, 20, and 24 GHz are 3.0, 3.2, and 3.5 dBi, respectively. The simulated xy plane gain patterns and 3-D radiation patterns for the 180°-out-of-phase excitation case are presented in Figures 6.9 and 6.10. Apparently the antenna radiates waves towards the +x-direction and it turns into a directive antenna in this case. The patterns are stable while the gain increases along the rise of the frequency. The simulated maximum gains at 16, 20, and 24 GHz are 2.6, 4.4, and 5.8 dBi, respectively. In both of two cases there is a small portion of waves leaking to the z-direction as shown by the 3-D patterns which is due to its UWB monopole antenna nature. Nonetheless, they are insignificant and the main beam goes to the desired direction. The average simulated radiation efficiency for the above two cases is around 94%-96%.

6.1.4 Feeding Circuit Design

In order to realize the input excitations with in-phase and 180°-out-of-phase signals, a broadband two-stage rat-race coupler is designed in the interested frequency range [25]. The coupler configuration is shown in the inset of Figure 6.11(a). It is synthesized on the



Figure 6.11 Simulated performance for the two-section rat-race coupler. (a) *S*-parameters for the in-phase case; (b) *S*-parameters for the out-of-phase case; (c) Phase performance. The structure is shown in the inset. Port 3 is the input port for in-phase operation. Port 1 is excited for 180°-out-of-phase operation.



Figure 6.12 Photograph of the fabricated pattern diversity antenna integrated with rat-race coupler.



Figure 6.13 Measured S-parameters of the antenna shown in Figure 6.12.

same Rogers 5880 substrate with a thickness of 0.254 mm. It is able to provide in-phase (fed at Port 3) and 180°-out-of-phase (fed at Port 1) output signals at Ports 2 and 4. It consists of three vertical $\lambda_g/2$ and four horizontal $\lambda_g/4$ lines whose impedances are optimized to have a good wideband matching from 17 GHz to 25 GHz. Specifically, they are $Z_1 = 52.9 \Omega$, $Z_2 = 74.1 \Omega$, $Z_3 = 30.8 \Omega$, $Z_4 = 56.7 \Omega$, $Z_5 = 66.1 \Omega$, and $Z_0 = 50 \Omega$. The detailed design procedure is discussed in [25]. The overall size of this coupler is 18 mm × 25.73 mm. Note that the ground width (25.73 mm) of the coupler is actually



Figure 6.14 Measured (solid line) and simulated (dotted line) normalized antenna radiation patterns in *x*-*y* plane for the in-phase case at (a) 17 GHz, (b) 20 GHz, and (c) 22 GHz.

determined by the antenna ground size. Figure 6.11 shows the simulated results including magnitude and phase responses for both the in-phase and out-of-phase cases. Over the interested frequency band, small reflection (below -10 dB), good amplitude imbalance (less than 0.4 dB), small phase variation (less than $\pm 6^{\circ}$), and large isolation (better than 26 dB) are achieved.

6.1.5 Experimental Results

The above antenna and coupler are integrated together and fabricated on the 0.254-mm Rogers RT/duroid 5880 substrate. A photograph is shown in Figure 6.12. Two super SMA connectors which can work up to 26 GHz are mounted on the coupler to test the



Figure 6.15 Measured (solid line) and simulated (dotted line) normalized radiation patterns in *x-y* plane for the out-of-phase case at (a) 17 GHz, (b) 20 GHz, and (c) 22 GHz.

antenna. The measured *S*-parameters from 16 GHz to 25 GHz are shown in Figure 6.13, compared with the simulated results. Port 1 corresponds to the out-of-phase excitation case while Port 3 corresponds to the in-phase case. The reflection coefficients deteriorate a little which are basically less than -10 dB. The isolation is greater than 33 dB.

The radiation patterns were measured in a far-field chamber and an HP 8340A Synthesized Sweeper which works up to 26.5 GHz is used to provide the source signals. A power amplifier is used before the transmitting horn antenna in order to clearly distinguish the signal and noise. Considering the bandwidth of the rat-race hybrid and the stability of the generated source signals we only tested patterns at a minimum frequency of 17 GHz and a maximum frequency of 22 GHz. The measured normalized radiation

patterns, compared with the simulation data, at three tested frequencies (17, 20 and 22 GHz) for the in-phase and out-of-phase cases are plotted in Figures 6.14 and 15, respectively. They are in good agreement. For the in-phase case the radiation goes to the two sides while for the out-of-phase case the main beam points to the +x-direction. The measured peak gains are 2.5, 2.88, 3.4 dBi at the tested frequencies for the in-phase cases and 3.1, 4.1, 5.5 dBi for the out-of-phase cases, respectively. The gain reduction compared with the simulation is partially due to the loss in the coupler. Small discrepancy may come from the fabrication and testing error. The measured results confirm that good pattern diversity performance has been achieved for the proposed antenna.

6.2 Polarization Diversity UWB Antenna

6.2.1 Antenna Configuration

Figure 6.16 shows the geometry of the proposed polarization diversity antenna. It is also printed on the Rogers 5880 substrate with a thickness of 0.254 mm. It consists of a modified ground, a corner-chamfered square patch, and two feeding lines. The idea is to combine two square patch UWB antennas orthogonally by sharing the same monopole element. It is noted that the previous monopole disk antenna shown in the above section works mainly as a travelling-wave tapered slot antenna for which the radiation is the strongest along the endfire direction. This square-patch antenna shown in Figure 6.15 works more like a UWB wide-strip dipole antenna. The radiation is stronger along the top and bottom ($\pm z$) directions. Therefore it is more suitable for this polarization diversity



Figure 6.16 Geometry of the proposed polarization diversity antenna. The parameters are: $t_1 = 0.5 \text{ mm}$, $w_1 = 1.55 \text{ mm}$, $w_2 = 3.68 \text{ mm}$, $w_3 = 0.3 \text{ mm}$, $w_4 = 6.43 \text{ mm}$, $w_5 = 3.42 \text{ mm}$, $w_6 = 1.9 \text{ mm}$, $l_1 = 1.1 \text{ mm}$, $l_2 = 3.27 \text{ mm}$, $l_3 = 2.13 \text{ mm}$, $l_4 = 0.98 \text{ mm}$, a = 3.95 mm, tw = 0.78 mm, gw = 22 mm.

application. The feeding lines are composed of a 50- Ω microstrip line, a linear tapered impedance transformer, and a trident-shaped strip. As investigated in [15], [19], the trident-shaped strip is able to provide wideband impedance matching compared to the single-feeding strip mechanism. It should be pointed out that we extended the microstrip line and the ground towards the -x direction in order to connect the antenna with the outside circuits or the testing connectors, as well as to reduce the interference of the connectors in the measurement since the antenna itself is quite small. From simulation it is seen that there is no big difference in performance after extending the microstrip lines. From the current distribution it is found that the top corner of the square patch is not critical to the radiation therefore it is chamfered and the corners are slightly rounded to



Figure 6.17 Operating principle of the polarization diversity antenna. (a) In-phase case, (b) 180°-Out-of-phase case, and (c) Circularly polarized case.

improve the matching. In this way the antenna is further miniaturized. To increase the isolation between the two ports the ground is also modified but in a different manner compared with the pattern-diversity antenna shown in the previous section. We etched a slot in the center of the ground to increase the isolation as well as to avoid disturbing the radiation generated from the ground plane. The slot increases the actual electrical length between the two antenna elements. Another reason is that the slot actually diverts the wave to the ground direction (-*x* direction) instead of the original side direction ($\pm y$ direction). Therefore the slot also works to increase the isolation. Similarly those corners on the ground are chamfered and filleted slightly to increase the matching by creating a smooth current path.

6.2.2 Working Principle

Figure 6.17 shows the working principle of the polarization diversity antenna. As a single UWB square patch antenna essentially it can be equivalent to a UWB wide-strip electric dipole antenna which is polarized along the feeding line direction and radiates omni-directionally but a little focused towards the $\pm z$ -direction. Similarly to the pattern



Figure 6.18 The simulated *S*-parameters and the envelope correlation of the polarization diversity antenna shown in Figure 6.16.

diversity antenna, it is polarized along the $\varphi = -45^{\circ}$ (or 45°) direction when only Port 1 (or 2) is excited. For the case shown in Figure 6.17(a) when both of the two ports are excited with equal- magnitude and in-phase signals, the resulting electric field is along the *x*-direction which is the polarization angle. For the out-of-phase case indicated by Figure 6.17(b), the overall *E*-vector after summation is along *y*-direction. Therefore the antenna is polarized along *y*-direction. When 90° phase difference is applied which results in two perpendicular *E*-vectors with a 90° phase difference, circular polarization (CP) is expected as the case shown in Figure 6.17(c). Note that the polarization also depends on the wave travelling angle so that the wave going to -z direction has opposite polarization compared to the wave radiating to +z direction.

6.2.3 Simulated Results

Figure 6.18 shows the simulated *S*-parameters with the calculated envelope correlation coefficient ρ using Eq. (6.1) displayed in the inset. The reflection coefficient is less than -



Figure 6.19 Simulated gain patterns in x-z and y-z planes when the antenna is excited with inphase signals at (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.

10 dB across the whole frequency range from 12 GHz to 30 GHz. The isolation between the two ports is larger than 15 dB for the frequency above 15GHz. The envelope correlation coefficient is lower than -40 dB for the frequency range above 14 GHz. It is noted that low correlation implies that there is little overlapping between the two beam patterns which is desired for polarization diversity applications.

Figures 6.19 and 20 show the radiated gain patterns at 16, 20, and 24 GHz for the inphase and 180° -out-of-phase cases, respectively. Note that the *E*-plane is *x*-*z* plane for the in-phase case and *y*-*z* plane for the out-of-phase case. Mainly the radiation goes to the *z* direction for these two cases while for the in-phase case at low frequencies the antenna



Figure 6.20 Simulated gain patterns in x-z and y-z planes when the antenna is excited with out-ofphase signals at (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.

acts like a UWB monopole antenna which has an omni-directional H-plane pattern (*y-z* plane). The cross polarization level is relatively low in both of the two cases. Figures 6.21 and 22 show the simulated 2D and 3D radiation patterns for the circularly polarized case excited by a pair of signals with 90° phase difference. As predicted the antenna radiates left-handed CP waves towards +z direction and right-handed CP waves to the opposite direction which is due to the different propagation directions. The simulated peak gains at 16, 20 and 24GHz are 3.0, 3.5 and 4.4 dBi, respectively, which correspond to an average radiation efficiency of 97%. To provide the readers with a clear understanding about its CP radiation nature, Figure 6.23 displays the electric field distribution in time domain at



Figure 6.21 Simulated gain patterns in *x-z* and *y-z* planes for the circularly polarized case at (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.



Figure 6.22 Simulated 3D radiation patterns for the circularly polarized case at (a) 16 GHz, (b) 20 GHz, and (c) 24 GHz.



Figure 6.23 Simulated electric field distribution at 20 GHz for the CP case at different stages in time domain. The electrical field is plotted along the metal where only the vertical component exists.



Figure 6.24 Simulated AR in y-z plane at four different frequencies.



Figure 6.25 Simulated AR versus frequency at $\theta = 0^{\circ}$ and 180° point (Z-axis).



Figure 6.26 Simulated performance for the three-section branch-line 90° coupler. (a) *S*-parameters; (b) Phase performance. The structure is shown in the inset.

20 GHz. It is seen that the ground also participates in the radiation. A left-hand (clockwise) rotated field is detected which reveals its left-handed circular polarization nature. Figure 6.24 shows the simulated axial ratio (AR) in *y*-*z* plane at four different frequencies. Good CP mode is observed in $\pm z$ directions with an average 3-dB AR beam width around 80°. Figure 6.25 shows the simulated AR versus frequency at $\pm z$ axis points. CP radiation is achieved with a 3-dB bandwidth of 53.7%.
6.2.4 Feeding Circuit Design

To obtain the feedings with 90° phase difference and equal power division, a broadband three-stage branch-line coupler is designed and optimized covering the frequency range from 17 GHz to 26 GHz [26]. The configuration of the coupler is presented in the inset of Figure 6.26(b). It is synthesized on the Rogers 5880 substrate with a thickness of 0.254 mm. It consists of four vertical and six horizontal $\lambda g / 4$ lines whose impedances are optimized to exhibit a good wideband matching over the interested band [26]. The corresponding line impedances shown in the figure are $Z_1 = 152.1 \Omega$, $Z_2 = 43.7 \Omega$, $Z_3 = 91.2 \Omega$, $Z_4 = 40.2 \Omega$, and $Z_0 = 50 \Omega$. The overall coupler size is around 25 mm×22 mm. The simulated *S*-parameters and phase response are displayed in Figure 6.26. Small reflection (below -15 dB), good amplitude imbalance (less than 0.5 dB), small phase variation (less than $\pm 2^\circ$), and large isolation (better than 14 dB) are realized across the designed frequency range.

6.2.5 Experimental Results

Here we only experimentally verified the circularly polarized case which has the most complicated scenario. Generally speaking, the linearly polarized cases would work as long as the feasibility of the circularly polarized case is proved. The broadband branch-line coupler and the antenna are integrated together and fabricated on the 0.254-mm Rogers 5880 substrate. Figure 6.27 shows a photograph of the fabricated device. The *S*-parameters measured using a network analyzer are presented in Figure 6.28 compared with the simulated results. Good matching and isolation are observed. The antenna was then measured in a near-field chamber in our department to obtain its radiation



Figure 6.27 Photograph of the fabricated polarization diversity antenna.



Figure 6.28 Measured (dotted line) and simulated (solid line) *S*-parameters of the antenna shown in Figure 6.27.



Figure 6.29 Measured (solid line) and simulated (dotted line) AR versus frequency at $\theta = 0^{\circ}$ and 180° point (*z*-axis).



Figure 6.30 Measured (right) and simulated (left) normalized radiation patterns in x-z and y-z planes at (a) 20 GHz, and (b) 24 GHz.

performance. Figure 6.29 shows the measured AR in $\pm z$ directions at different frequencies. Good CP performance is detected from 19 GHz to 25 GHz. The discrepancy compared with the simulation may come from several aspects such as the influence of the fabrication error and the connectors. Figure 6.30 shows the measured normalized radiation patterns at 20 and 24 GHz. The measured antenna peak gain is approximately 3.0 dBi at 20 GHz and 4.2 dBi at 24 GHz. Figure 6.31 shows the measured and simulated AR at 24 GHz in *x-z* and *y-z* planes for the antenna. CP radiation is observed but the measured 3-dB AR beam width decreases compared with the simulated data which are



Figure 6.31 Measured and simulated AR in *x-z* and *y-z* planes at 24 GHz. (a) Front side, and (b) Back side.

probably due to the fabrication error and the influence of the branch-line coupler. Overall the measured results verify that this proposed antenna is able to provide polarization diversity performance in Ku- and K-band.

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Chapter 7

Conclusion and Future Work

7.1 Conclusion

The development of wireless communications, internet of things has brought many great challenges to the RF component and antenna areas such as broad band, size reduction, and multiple functionalities. Metamaterials demonstrate good potential for these challenges. The main objectives of this dissertation were to design high performance microwave/RF components and antennas based on metamaterial conception. The key contribution of the research can be summarized as following:

1). We, for the first time, summarized the four elements to be used for synthesis of metamaterials, including the wire and slot dipoles, the SRR and CSRR resonators. Then we discussed and characterized the propagation features of waveguide loaded by these metamaterial particles. Waveguide miniaturization is obtained by below-cutoff operation.

2). We proposed using the interdigital slot to load the SIW to obtain a high performance CRLH transmission line. Various applications were proposed, implemented and verified, such as filters, couplers, and resonator-type, leaky-wave-type antennas.

3). We, for the first time, proposed using the CSRR resonators to load the SIW to obtain wave propagation below the waveguide cutoff frequency. High performance miniaturized filters and diplexers were proposed based on this configuration.

4). We designed many novel CRLH resonator type antennas based on the zeroth-order

or negative order resonances with good performance. Different techniques were employed to improve the antenna radiation efficiency.

5). We made significant progress on the topic of electrically small antennas based on the SRR and CSRR resonators. By adopting different configurations, such as planar or vertical type, different orientations, we realized a variety of small antennas with different functions, such as dual-band operation, wide bandwidth, circular polarization, and pattern diversity applications.

6). We made some original contribution on UWB antennas with diversity performance. We proposed realizing the diversity performance by sharing the same monopole element for the UWB antenna in order to miniaturize the antenna size. Bothe polarization and pattern diversity function across the Ku- and K-band were implemented

To sum up, we have made our original contribution in two related areas: 1) the waveguide-based metamaterial structures and their applications; 2) Miniaturized antennas based on the metamaterial conception. In related to my major above research focus, I have also made contribution on the UWB antenna technologies.

7.2 Future Work

Some innovative ideas were comprehensively explored in the research. Representative results from both simulations and experiments were presented. However, research is just like a circle. The more you get to know, the more unknown you will be facing. Some suggestions for future work are listed below:

1). New metamaterial synthesize method. We have already summarized the four basic

elements used to metamaterial application. Any combination of an electric dipole and a magnetic dipole type element would guarantee the success of a metamaterial realization. We can do more research on this topic to obtain high performance metamaterials which is a quite promising topic.

2). CSRR combined with TM modes. The TM modes when operated below the cutoff are able to provide a uniform μ -negative environment. By loading the CSRR, which is essentially a ε -negative material, we can easily obtain a double-negative material in the below-cutoff region.

3). Electrically small antennas based on SRR resonator. So far we have carried out some interesting research on this topic. But far more can be done since it is a truly useful design. For instance, multi-band antennas, wideband antennas, circularly polarized antennas can all be implemented. The SRR can either be horizontally or vertically placed. The radiation pattern may also be tailored for specified applications.

4). Planar small folded antennas with multi-layer configurations. Multi-layer fabrication is a very mature technique right now. We can fold the antennas to miniaturize the size. Multiple modes can be combined to broaden the bandwidth. Actually we have already kicked off this project and obtained some satisfactory results. This could be a potentially rewarding topic for WIFI and mobile phone antenna applications.

5). UWB diversity antennas at lower frequency. There is a demand for UWB antennas covering from 800 MHz to 2.5 GHz. Designing miniaturized UWB antennas with diversity performance would be very meaningful. This would be a continued topic from the research shown in Chapter 6. Short distance UWB communication, due to their great

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merits, would be widely used in the future. Therefore research along this direction would be very useful.

6). Active small antennas. Traditional small antennas suffer from small bandwidth and low efficiency. Using active circuits could be helpful in this regard. For instance, the concept of active non-Foster metamaterial used in matching network to broaden the bandwidth of electrically small antenas has also drawn considerable attention. It is usually built via a combination of active devices (transistors) as well as lumped capacitors and inductors.