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On Neural Architectures for Astronomical Time-series Classification with Application to Variable Stars

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ABSTRACT

Despite the utility of neural networks (NNs) for astronomical time-series classification, the proliferation of learning architectures applied to diverse datasets has thus far hampered a direct intercomparison of different approaches. Here we perform the first comprehensive study of variants of NN-based learning and inference for astronomical time-series, aiming to provide the community with an overview on relative performance and, hopefully, a set of best-in-class choices for practical implementations. In both supervised and self-supervised contexts, we study the effects of different time-series-compatible layer choices, namely the dilated temporal convolutional neural network (dTCNs), Long-Short Term Memory (LSTM) NNs, Gated Recurrent Units (GRUs) and temporal convolutional NNs (tCNNs). We also study the efficacy and performance of encoder-decoder (i.e., autoencoder) networks compared to direct classification networks, different pathways to include auxiliary (non-time-series) metadata, and different approaches to incorporate multi-passband data (i.e., multiple timeseries per source). Performance—applied to a sample of 17,604 variable stars from the MACHO survey across 10 imbalanced classes—is measured in training convergence time, classification accuracy, reconstruction error, and generated latent variables. We find that networks with Recurrent NN (RNNs) generally outperform dTCNs and, in many scenarios, yield to similar accuracy as tCNNs. In learning time and memory requirements, convolution-based layers are more performant. We conclude by discussing the advantages and limitations of deep architectures for variable star classification, with a particular eye towards next-generation surveys such as LSST, the Roman Space Telescope and ZTF2.

Keywords: Variable stars (1761), Periodic variable stars (1213), Light curves (918), Neural networks (1933), Light curve classification (1954)

1. INTRODUCTION

Time-domain imaging surveys continue to expand access to the photometric phase space of cadence and depth/volume. Despite many upcoming projects (e.g., the Rubin Observatory Legacy Survey of Space and Time – LSST¹, Ivezić et al. 2019; *Euclid*², Laureijs et al. 2011; and the Nancy Grace Roman Space Telescope – WFIRST³, Spergel et al. 2015) being optimized for transient (supernovae, microlensing) discovery and characterization, the data from these surveys create unprecedented opportunities to broaden our understanding of stellar variability and stellar evolution as well as expand the use of variable stars (VSs) as probes. Detached eclipsing binaries, for example, provide direct measurements of distance

³ https://wfirst.gsfc.nasa.gov/

(e.g., Paczyński 1997) and fundamental stellar parameters (Torres et al. 2010), while pulsating VSs such as RR Lyrae, Miras and Cepheids due to their accurate period-luminosity relations are considered useful tools to trace galactic structures (Kraft & Schmidt 1963; Majaess et al. 2009; Skowron et al. 2019), calibrate the cosmic distance ladder (Freedman et al. 2001; Huang et al. 2018; Riess et al. 2018, 2019) as well as standard candles to measure distances to their host-galaxies (Carretta et al. 2000; Clementini et al. 2003; Alves 2004).

Stellar variability, primarily manifest as changes in brightness and color, arises from various physical mechanisms. Intrinsic variations arise as flares, rotation, pulsations, and/or violent outbursts due to thermonuclear processes occurring in the surface layers or deeper within. Extrinsic factors that may add to the observed variability include eclipses, relativistic Doppler beaming, mutual interaction in binary systems, and/or gravitational lensing.

¹ https://www.lsst.org/

² https://www.euclid-ec.org/,https://sci.esa.int/web/euclid

The classification of VSs is based usually on brightness variations, typically, at visible wavelengths. While far from standard, the General Catalog of Variable Stars (GCVS; Samus' et al. 2017) maintains the taxonomy and nomenclature for VSs that distinguishes between subtypes of rotators, pulsators, eruptive variables, cataclysmic variables, eclipsing binaries in addition to other types such as microlensing sources. In general, stellar variability is not expected to fall into a unique type of dynamical behavior, as objects may display a multitude of physical behavior, such as rotational modulation superimposed to pulsation in RCB-type stars, rotational modulation interjected by abrupt episodes of deep minima or a steep increase in brightness in BY Dra-type stars, or symbiotic systems with a M-type pulsating Mira star with an accreting white dwarf companion as the R Agr star. A comprehensive survey of VS classification is provided by Eyer & Mowlavi (2008).

Large data volumes, the primary strength of massive surveys, also presents an acute challenge: how do we discover and characterize variable stars at scale in streaming, heterogeneous, and noisy time series? Human-free classification, part of a fully automated system to process and analyze survey data, requires the development and deployment of robust and reliable techniques from information-data technology to process large volumes of data and produce tractable and reproducible results.

Traditional machine-learning (ML) approaches for VS classification typically involve "featurization" to summarize and encode the raw observables into a set of informative descriptors exploited by a classifier to predict labels. Some popular features in the literature include frequency-domain metrics derived from Lomb-Scargle periodograms (Scargle 1998; Lomb 1976), statistical metrics (e.g., standard deviation, quantiles and skewness), variability indices (e.g., the Stetson indices K and L; Stetson 1996), best model fit parameters as well as additional "metadata" information from external catalogs (e.g., colors, redshifts and parallaxes measurements). VS classification using expert-engineered featurization and traditional ML algorithms have been extensively studied and used for decades (Debosscher et al. 2007; Blomme et al. 2011; Dubath et al. 2011; Richards et al. 2011, 2012; Rimoldini et al. 2012; Masci et al. 2014; Kim & Bailer-Jones 2016; D'Isanto et al. 2016). Specialized libraries for features extracting from astronomical light curves have been made available by the community in open-source software packages such as cesium (Naul et al. 2016), FATS (Nun et al. 2015), feets (Cabral et al. 2018), sncosmo (Barbary et al. 2016), gatspy (VanderPlas & Ivezić 2015; Vanderplas et al. 2016), and VARTOOLS (Hartman & Bakos 2016).

Ideally, featurization produces a uniform dimensionality reduced representation of the observations that adequately captures the intrinsic properties of the data needed for classification. However, a known issue in hand-coded feature-based classification lies in the fact that the generated low-dimensional representation may overlook subtleties in higher-order systems and restrict such complexity into a set of low-level descriptors tailored for specific use-case applications. Furthermore, developing domain-specific features can be time-consuming, computationally expensive, highly dependent of expert-knowledge, and may show a strong dependency on survey characteristics.

Representation learning (RL) techniques offer an alternatively possibility to process raw observables without traditional feature engineering. The benefit of fully-automating the classification task using RL lies in the ability to reach a higher level of abstraction and capture complex structures embedded in the data. Distinct approaches in RL to automate features extraction from astronomical time-series have already been introduced in a broad range of studies. Used techniques include unsupervised learning algorithms (Armstrong et al. 2016), dimensionality reduction techniques, data transformations (Johnston et al. 2020), autoencoders (Naul et al. 2018) or dictionary learning (Pieringer et al. 2019).

In the recent years, VS classification using deep learning (DL)/neural architectures has been explored in several works that achieved satisfactory classification performance and thus demonstrated the ability of DL systems to learn stellar variability types from light-curves measurements and auxiliary metadata. Among mostly-used DL architectures, recurrent neural networks (RNNs) proved to be highly-performant for periodic VS classification (Naul et al. 2018; Tsang & Schultz 2019), supernovae (SNe) classification (Charnock & Moss 2017) and online transient events detection (Muthukrishna et al. 2019a; Möller & de Boissière 2019). Convolutional neural networks (CNNs) have also proven comparably performant, with a better training convergence time and lower memory allocation requirements in comparison to RNNs in various applications such as exoplanet transit detection (Shallue & Vanderburg 2018; Schanche et al. 2019; Ansdell et al. 2018), SNe binary classification (Pasquet et al. 2019b) and Cepheid classification (Dékány et al. 2019). A review on the recent contributions of DL techniques in SNe classification is given by Ishida (2019).

To classify astronomical time-series, two main approaches have emerged, either (1) design an automated system to encode the photometric observables into a set of features (semior self-supervised learning) that constitute the entry point to traditional algorithms (e.g., support-vector machines, NNs or tree-based classifiers), or (2) develop a DL architecture to find an optimal mapping between the photometric observables and the labels through a supervised learning scheme.

The objective of this paper is twofold: first is to provide an overview of the current ML/DL techniques for variable stars classification, and second to discuss through a test example the applicability of a selected set of NNs architectures and the importance of data representation for classification of stellar variables. This paper also investigates approaches for variable stars classification using multiband photometric data. The paper is organized as follows. Section 2 first introduces the *state-of-the-art* of ML/DL techniques for VS classification then proceeds to present our proposed architectures for classification. In Section 3, we present variants of NNs architectures and discuss their performances through a test example using public data from the MACHO VS database. The networks performances are evaluated in term of training convergence time, classification accuracy, properties of the generated latent representations and light-curves reconstruction. Finally, we conclude in Section 4.

2. DEEP LEARNING ARCHITECTURES FOR VS CLASSIFICATION

2.1. State-of-the-art

Classification of variable stars can be performed in feature space or in data space. The first approach consists of finding an optimal mapping between the labels, a vector Y, and an (encoded) feature set, a matrix X_{enc} derived from the direct observables X; the second approach focuses on finding a direct mapping between the observables X and the labels Y.

In feature space classification, traditional approaches require hand-coded feature extraction to compute a set of informative descriptors using domain knowledge. For variable stars, the most discriminant features of stellar variability depends strongly on the specific class or subclass. For instance, the dominant modes of the pulsation mechanism can be well characterized in the frequency domain, found through Fourier decomposition or periodogram analysis. In eclipsing binaries, the shape, duration, and relative phase of the eclipses in their light-curves inform the type of the interaction (contact binaries, detached binaries or semi-detached binaries) and their properties such as the mass and radii ratios. Cataclysmic variables are described through the morphology of their light-curves at maximum light, the decline shape, the duration of the burst event, the event occurrence in time distinguishing between recurrent outbursts and final explosions, the quiescent state of the star post-event and observed spectral features during outburst. For eruptive variables, their light-curves and spectra show distinctive variations as sudden brightening or dimming episodes over extended periods of time due to flares and violent processes taking place in the corona or the chromosphere of these stars.

In traditional approaches, feature engineering relies on domain knowledge while feature learning automates the extraction procedure from the data using dimensionality reduction techniques, self-supervised networks (e.g., autoencoders), dictionary learning, or unsupervised algorithms. The extracted features constitute a discretized set of encoded information exploited by feature-based classifiers to predict labels. Among notable references, the work by Armstrong et al. (2016) exploits the unsupervised learning algorithm SOMs (*Self-Organizing Maps*) to encode photometric lightcurves into a set of features processed, along with additional descriptors, by the tree-based classifier, the random forest (RF, Breiman 2001), to predict labels for periodic VSs. The work of Naul et al. (2018) presents a bidirectional RNN autoencoder to discretize the photometric observables into a set of latent variables exploited, along with ancillary metadata, by a RF classifier to predict labels for periodic variables.

For classification in data space, common techniques exploit DL to identify embedded characteristics in the data and find a direct mapping between the input observables and the output labels. Applications using DL techniques for astronomical time-series classification include (1) SNe classification using RNN architectures to process multiband photometric data and auxiliary metadata (e.g., redshift measurements) (Charnock & Moss 2017; Muthukrishna et al. 2019a; Möller & de Boissière 2019), (2) online transient events detection using RNN architectures to compute timely class-predictions for early-observed light-curves in order to forecast potential pre-SN outbursts and prompt follow-up procedures before the event reaches its maximum light (Muthukrishna et al. 2019a; Möller & de Boissière 2019), and (3) exoplanetary transit detection using a composite convolutional networks that analyzes the full light curve and the eclipses to discern between planetary transits and stellar eclipsing binaries (Shallue & Vanderburg 2018; Ansdell et al. 2018; Schanche et al. 2019).

More recently, composite architectures has been introduced for astronomical time-series classification in the form of NNs composed of different submodules designed for specific tasks. Notable references include the work by Pasquet et al. (2019b) for SNe classification where the authors propose a DL architecture (PELICAN) with three modules: an autoencoder branch to generate the embeddings at the bottleneck level by optimal reconstruction, a classifier for label predictions and a contrastive module designed to reduce the discrepancy between the Test and Train sets. Binary classification of type Ia SNe is performed using multiband photometric data and ancillary metadata (redshift measurements of the host galaxies). The work by Tsang & Schultz (2019) proposes a similar approach for periodic VS classification, initially derived from the DAGMM (Deep Autoencoding Gaussian Mixture Model) network in Zong et al. (2018). The authors propose a network composed of two modules: an autoencoder branched out to a classifier module at the bottleneck level.

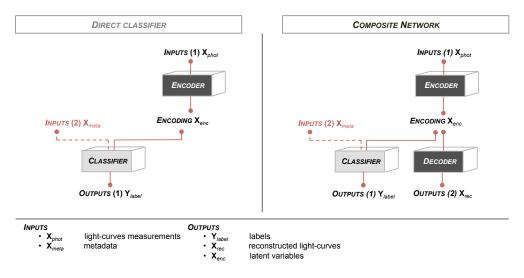


Figure 1. High-level architecture of the direct classifier (left) and composite (right) networks. In direct classifiers, the time-series data (\mathbf{X}_{phot}) and metadata (\mathbf{X}_{meta}) are combined through a series of neural layers and concatenations, leading to classification predictions (\mathbf{Y}_{label}) on which the loss function is optimized. Composite networks use \mathbf{X}_{phot} and a bottleneck/decoder to predict a reconstructed light curve (\mathbf{X}_{rec}). The bottleneck layer along with \mathbf{X}_{enc} is also used to predict \mathbf{Y}_{label} . Both \mathbf{X}_{rec} and \mathbf{Y}_{label} are used in the loss function of composite networks.

2.2. Architectures

This section presents selected architectures for VS classification. We distinguish between two types of architectures: direct classifiers and composite networks, as shown in Figure 1. Both architectures are composed of an encoder and classifier module. Composite networks are supplemented with a decoder connected at the bottleneck level. The encoderdecoder combination (i.e., autoencoder) aims to learn a latent representation \mathbf{X}_{enc} of the input photometric data \mathbf{X}_{phot} by optimal reconstruction, while the classifier maps the encodings to the labels Y_{label} . By connecting the autoencoder to the classifier module, the system ideally learns a latent representation (ie., compressed summary) that is closely correlated to different stellar variability types in the training data. The high-level design in Figure 1 is adaptable: modules can be adjusted to the application and data as needed. In the current work, the decoder module corresponds to a mirror-image of the encoder, which is a common choice for autoencoder architectures. We evaluate the encoder for different types of NNs such as recurrent neural networks, convolutional neural networks and their variants, while the classifier module is set to a 2-layer MLP (Multi-Layer Perceptron) for all networks to predict labels. A short description of the neural networks used in this work is provided in Appendix B.1.

The majority of applications for VS classification using DL exploit auxiliary features that complement the photometric observables such as redshift measurements, detectable frequencies for periodic variables, amplitudes and colors. The photometric information in the light-curves constitutes a fundamental description of the evolutionary state of the star over time but does not contain the entirely of the available information; unless the light curve of a certain class is demonstrably different than other classes, additional metadata can be expected to improve classification accuracy. Typically, classification tasks require an upstream phase of data preparation. However, preprocessing transformations applied to the photometric observables may inadvertently remove discriminating features linked to the stellar variability types, thus altering the quality of the information necessary for classification. For instance, light-curves of periodic variables are preprocessed through phase-folding and data normalization. The phase-folding procedure transforms the periodic data into a compact representation in phase of one to two cycles by stacking multiple observations, thus removing the periodicity information over time. On the other hand, data normalization via minmax normalization yields to rescaled magnitude measurements, amplitudes and errors. As a direct result, similarly shaped light-curves with different peak-topeak amplitudes cannot be distinguished from one another.

In the current work, we investigate the importance of the metadata in two scenarios in which the network classifies the data solely based on (preprocessed) light-curves without auxiliary metadata as opposed to supplementing metadata to the system as a secondary input for label predictions.

In VS classification, multiband photometry can be processed either by transforming the photometric passband measurements into a single entity fed to the network or by jointly processing individual encodings from each passband measurements for label predictions. A simplified representation of the aforementioned approaches, identified in this work as the *merged* and *hybrid* approaches, is provided in the Appendix Figure A1. In the *merged* approach, multipassband measurements are combined into a unique observable $\mathbf{X}_{phot.merged}$ processed by the encoder module to compute the latent representation \mathbf{X}_{enc} . The preprocessed light-curves per band can be combined through distinct representations as the variants presented in the Appendix A. Whereas, the *hybrid* approach independently encodes the multi-passband measurements into individual features combined at a latter time into a compact encoded representation \mathbf{X}_{enc} . In both scenarios, the classifier module exploits the generated encodings \mathbf{X}_{enc} , along with metadata \mathbf{X}_{meta} , for label predictions. Composite networks differ from the direct classifiers by the addition of a decoder module connected at the bottleneck level to the encoder to generate the embeddings by optimal reconstruction.

3. APPLICATION

This section presents a set of NN-based architectures for VS classification. We discuss through a test example the performance of these networks in terms of training convergence time, label predictions, reconstruction and generated latent representations.

3.1. Data

As an exemplar, for all architectures, we use public photometric data and labels from the MACHO survey (Alcock et al. 1996). The MACHO project carried-out a long-term photometric monitoring of stars in the Magellanic Clouds and the galactic bulge from 1992 to 1999 in search for rare microlensing events, observable in theory if the dark matter is composed of massive compact halo objects (MACHOs). The large collection of data from the survey has allowed over the years a rare insight into a variety of stellar populations such RR Lyrae, Cepheids, LPVs (Long-Period Variables) and eclipsing binaries (Cook et al. 1995). In MACHO, the LPVs are categorized into four subtypes - namely the four Wood sequences A, B, C and D – referring to the parallel sequences identified from the period-luminosity relation of these red variables (Wood et al. 1999). Photometric data in MACHO consists of magnitude measurements in two photometric filters (the MACHO red and blue filters), the associated 1- σ error measurements and the observation epochs expressed in MJD. We exploit the multiband photometric data of the public MACHO VS database⁴ to test our selected NNs architectures, and we perform further checks on the data. In particular, we retain the confirmed set of eclipsing binaries with corrected periods from Derekas et al. (2007). The full process yields 17604 periodic variables from the initial count of 24k periodic VS in the MACHO database to test our architectures: 1806 Cepheid variables, 9163 RR Lyrae, 2965 long-period variables (LPVs) and 3670 eclipsing binaries (cf. Table 1).

The majority of ML/DL open-source software exploits input data in the form of a fixed-size input tensors and few DL architectures are able to process observables with different lengths, e.g., using generator functions on an iterable list of input data. In our approach, the architecture of the direct classifier can process fixed-size data in a batch mode as well as a list of observables with different lengths using generator functions. Composite networks, however, require fixed-size inputs to comply with the implementation specifications of the decoder module. To meet such requirements, we reduce the data into a fixed-size format. Typically, data reduction can be achieved using padding, rebinning, interpolation (e.g., splines or polynomials) or model fit and prediction. More recently, model prediction using Gaussian Processes (GPs) have been used used on astronomical time-series (Ambikasaran et al. 2016; Foreman-Mackey et al. 2017; Pruzhinskaya et al. 2019; Boone 2019). To describe the stellar variability in the MACHO periodic lightcurves, a GP model with a quasi-periodic covariance function is fitted to each object using the open source code Foreman-Mackey et al. (2019). The selected GP model is a mixture of stochastically-driven damped oscillators (SHOs), briefly discussed in the Appendix B.3. For each object, a GP model is fitted. Using a MAP (Maximum a posteriori) estimate, fixed-size light-curves are generated by model prediction on a reduced time-frame sampled within the range of the observed epochs. The GP predictions mean and error correspond to the reduced photometric data exploited in the rest of this work. At a latter stage, the reduced photometric lightcurves are normalized and phase-folded to span over 2 cycles. Phase-folding of periodic light-curves allows a better visualization of the cyclic behavior of the variables. For instance, short-period variables as RR Lyrae pulsate over timescales ranging from ~ 0.3 to 1 day. To fully observe the pulsation profile over a complete cycle, the observation cadence has to exceed the variability frequency to cover a full cycle. In practice, given realistic survey cadences, any one individual cycle will be sparsely observed if at all. By combining the observations through period-folding, however, even high-frequency variables such as RR Lyrae stars can have dense phase coverage. Still, properties of long-period variables that evolves over longer timescales, such as the Mira-type stars with pulsation periods ranging from ~80 to 1000 days, can be distinguishable in the initial time-frame without phase-folding. In the current application, we exploit a dataset of periodic VSs with light-curves from short-period pulsators, long-period pulsators and eclipsing binaries and apply the phase-folding procedure to all variables. Observed shortcoming from the preprocessing are discussed in the result section (cf. Section 3.3). In the majority of ML applications, normalization is applied to the data to improve the numerical stability and reduce the training time. In this work, the inputs \mathbf{X}_{phot} to the

⁴ http://macho.nci.org.au/

networks correspond to preprocessed light-curves, obtained after data reduction, phase-folding and normalization. The metadata X_{meta} consists of the amplitudes, averaged magnitudes and colors extracted from the raw data in addition to the primary periods.

Table 1. Selected dataset from the MACHO VS database.

CLASS LABELS	# IN CLASS
Cepheids FU	1143
Cepheids FO	663
RR Lyrae (type <i>ab</i>)	7147
RR Lyrae (type c)	1716
RR Lyrae (type e)	300
LPV (Wood seq. A)	310
LPV (Wood seq. B)	799
LPV (Wood seq. C)	1100
LPV (Wood seq. D)	756
Eclipsing binaries	3670 ^(a)

3.2. Design and implementation

(a)

We experiment with a variety of NN architectures and discuss the absolute and relative performances. Classification using multiband photometry is evaluated using the approaches introduced in Section 2.2, i.e. the merged and hy*brid* approaches. The *merged* approach exploits the second representation introduced in Appendix A combining the individual measurements of preprocessed light-curves into a 2-d tabular format. In the current application, normalization and phase-folding are applied to each band measurements independently, prior to generating the merged representation. Error measurements are used solely as weights in the autoencoder loss function. Incorporating error mesurements within the network can be part of further development of such networks. We investigate as well the use of auxiliary metadata as a secondary input on the classification accuracy for the direct classifier and composite networks via two scenarios, in which the network classifies the data using the information from preprocessed light-curves without metadata as opposed to supplementing auxiliary metadata as a secondary input for label predictions. Data entries for the different use case scenarios are summarized on the Appendix Table D1. The autoencoder is evaluated for different NN: RNN with LSTM cells, RNN with GRU cells, temporal CNN (tCNN) and dilated TCN (dTCN).

For VS classification, the objective of NNs is to empirically determine a mapping between the inputs, the photometric observables $\mathbf{X}_{phot} = [\mathbf{x}_1, \cdots, \mathbf{x}_{N_t}]^T$ and auxiliary metadata $\mathbf{X}_{meta} = [\mathbf{d}_1, \cdots, \mathbf{d}_{N_t}]^T$, and the output labels $\mathbf{Y}_{label} =$ $[y_1, \cdots, y_{N_t}]^T$, where N_t designates the total number of objects. In the current application, the datavectors $(\mathbf{x}_i)_{i:1 \to N_i}$ refer to the reduced photometric measurements - magnitudes, observation epochs and error measurements- spanning over N_p datapoints for the i^{th} object and the metadata $(d_i)_{i:1 \to N_r}$ is composed of N_f features such as the periods, the amplitudes, the averaged magnitudes and the colors. The elements $(y_i)_{i:1 \to N_i}$ refer to scalar values encoding the labels. For categorical classification, the labels are encoded into codewords transcribing the membership of the object to a variability class $\{j\}_{j:1 \to N_C}$ with N_C the total number of classes. A standard approach in categorical classification consists in transcribing class memberships into binary codewords {0, 1}. In online transient event detection applications, a similar methodology is used to map the observables into the output space. Class predictions are computed on the pixel level, which corresponds to a prediction vector $(\mathbf{y}_i)_{i:1 \to N_i}$ allowing to monitor the evolution over time of the label predictions and forecast potential pre-SN outbursts and trigger followup observations within a rapid decision time before the event reaches its maximum light. In contrast, the static-type prediction approach adopted for VS classification consists in associating the static label predictions to fully observed lightcurves. The approach is used in this study aiming to map the observables $\{X_{phot}, X_{meta}\}$ into scalar values Y_{labels} . Nonetheless, our architectures can be adapted to perform online predictions on the pixel level by adjusting the inputs-outputs format.

Detailed representations of the proposed architectures are shown in the Appendix Figures D1 to D3. After preprocessing (i.e., data reduction, phase-folding and data normalization of periodic light-curves), the networks proceed as follows. In the RNN architectures, the first part of the structure following the input layer is a stack of RNN layers that generates a sequence data of fixed length. The direct classifiers and composite networks differ in the last layer of the encoder module in which composite nets are supplemented with a fully-connected layer - a dense layer with a linear activation function - to transform the sequence data from the last RNN layer into an encoded representation \mathbf{X}_{enc} of a fixed size N_{enc} . If auxiliary metadata \mathbf{X}_{meta} is supplemented as a secondary input, the classifier exploits the augmented features to predict the labels \mathbf{Y}_{label} . The classifier module corresponds to a MLP of two dense layers with a rectified linear unit (ReLu) and softmax activation functions. In composite networks, the decoder transforms the encoded variables into reconstructed representations similar to Naul et al. (2018). The decoder proceeds by duplicating the embeddings in a number of times equivalent to the length of the input data, joins the epochs and passbands information and feeds the augmented embeddings into a stack of RNNs. The last component of the decoder module consists of a fully-connected layer that generates the final sequence data of the reconstructed light-curves. To prevent overfitting, regularization is added to the model through the dropout method (Srivastava et al. 2014) that randomly removes units during training.

Following the input layer, the tCNN architecture is composed of a series of convolutional layers with a number of filters and fixed kernel sizes for convolutions. The activation function for each convolutional layer is set to the hyperbolic tangent function and dropout is used for regularization. In the encoder module, the output of the last convolutional layer is flattened to generate a vector output. The latter corresponds to the final encodings for direct classifiers, while composite networks exploits an additional fully-connected layer to generate fixed-size embeddings. Similar to the RNN architectures, the encodings are fed to the classifier module, along with metadata when applicable. In the decoder, the data is processed through a reshaping substructure, stacks of transposed convolutional layers and a final fully-connected layer to generate the outputs. The reshaping substructure emulates the RNN decoder in order to reframe the encodings into a fixed-length format matching the input datapoints.

The dTCN architecture closely follows the TCN architecture (Lea et al. 2017) initially derived from the Wavenet architecture (Oord et al. 2016). Our design adds dropout functions after the causal convolutions to prevent overfitting. Following the input layer, the first component of the dTCN consists of a causal convolutional layer connected to interconnected stacks of residual blocks with dilated convolutions and gated activation units. Following the Wavenet design, a ReLu activation function and two convolutional layers are used after the stacks. The encoder outputs are transformed into a vector format and a fully-connected layer is supplemented in composite networks. The generated encodings are then fed into the classifier module and augmented with metadata when applicable. The decoder module is composed of a reshaping substructure, a TCN unit mirrored to the encoder module and a final fully-connected layer.

The NNs are tested with a different set of hyperparameters (cf. Appendix Table D2). The number of parameters per model are provided in the Appendix Table D3. All models are trained using the Adam optimization algorithm (Kingma & Ba 2017) with a learning rate of 5×10^{-4} , a fixed batch size per gradient-update in optimization, a dropout fraction and an early-stopping procedure to prevent the networks from overfitting. For all networks, a validation-based early-stopping procedure interrupts the training when an optimal solution is found (i.e., convergence) before reaching the maximum number of training epochs. The standard approach monitors the evolution of a scoring metric, typically the validation loss, over a period lag and terminates the training if the error estimated at the current time exceeds the last-verified value implying a large variance in the overfitting regime. An improved search for the hyperparameters space can be performed as an upstream stage of the final classification procedure. However, we choose in this study to empirically evaluate different sets of hyperparameter configurations, discuss the networks performances, and identify the best-performing models. In training, the autoencoder (i.e., encoder-decoder) aims to minimize the reconstruction loss, the weighted MAE (*Mean-Absolute Error*) function, and the classifier branch is set to minimize the categorical cross-entropy loss. Networks are trained to minimize the total loss L_{tot}.

direct classifier
$$L_{tot} = L_{ec}$$
,
composite network $L_{tot} = w_{ec} L_{ec} + w_{ed} L_{ed}$, (1)

where, $\{w_{ec}, w_{ed}\}$ respectively refer to the loss weights of the encoder-classifier and the encoder-decoder branches. In the current work, the individual losses L_{ec} and L_{ed} correspond to the following.

$$\mathcal{L}_{ec} = \frac{1}{N_t} \sum_{i=1}^{N_t} \left(-\sum_{j=1}^{N_c} y_{true,i}^{(j)} \log\left(y_{pred,i}^{(j)}\right) \right), \tag{2}$$

$$\mathcal{L}_{ed} = \frac{1}{N_t} \sum_{i=1}^{N_t} \left(\frac{1}{N_p} \sum_{k=1}^{N_p} w_i^{(k)} \Big| x_{phot,i}^{(k)} - x_{rec,i}^{(k)} \Big| \right), \tag{3}$$

where, of the i^{th} object, w_i corresponds to the sample weights of the autoencoder branch computed using the inverse of the error measurements σ_i . The losses, averaged across the sample of N_t objects, are computed by, on one hand, averaging the differences between the input photometric light-curves \mathbf{X}_{phot} and the decoder reconstructions \mathbf{X}_{rec} across the N_p datapoints, and, on the other hand, computing the crossentropy between the true labels Y_{true} and the classifier predictions \mathbf{Y}_{pred} over the N_C classes. Using the expression of the total loss in Eq 1, tested NNs are trained to minimize at each epoch the weighted sum of the individual losses with weights $\{w_{ec}, w_{ed}\}$ chosen equal to unity, as to depict a similar contribution from the individual branches into the total loss. The weighting scheme and cost functions can be revised for different applications and data types. Best-performing models are identified from minimum loss obtained on a Test set, i.e. the subset of data neither used in training nor validation. Our tests used up to 2-4 cores on a CPU model Intel Xeon E5-2643v3 on the UC Berkeley Savio Linux cluster. The NN architectures are implemented in the keras (Chollet et al. 2015) and Tensorflow (Abadi et al. 2015, 2016) programming frameworks, and the RNN autoencoder branch is partly adapted from the architecture in Naul et al. (2017). To facilitate reuse and reproducibility, our benchmarking codebase is provided in an open source repository⁵.

⁵ https://github.com/sarajamal57/deepnets_vs

3.3. Performance study

This section presents the results obtained on the public MACHO VS dataset. Computations are performed through a classical training-validation-test scheme with 80% of data for training-validation and 20% of unseen objects in the test prediction phase. Performance metrics are computed for all models, with a particular emphasis on the performances reached on the Test set. Metrics include the system total loss, the classification accuracy as well as averaged precision, recall and F1-score (cf. Appendix C). The total loss corresponds to the classification loss (categorical cross-entropy) evaluated on the encoder-classifier branch, supplemented in composite networks with the weighted MAE evaluated on the encoder-decoder branch. The classification accuracy is obtained through a direct comparison between the true labels \mathbf{Y}_{true} and the network predictions \mathbf{Y}_{pred} . We also discuss the classification performances within three main types of stellar variability: short-period pulsators including the RR Lyrae and Cepheids, long-period pulsators (LPVs) and eclipsing binaries. The autoencoder performances are assessed through the quality of the reconstructed light-curves \mathbf{X}_{rec} , and the embeddings \mathbf{X}_{enc} are projected onto a 3-d representation using a data reduction algorithm. The degree of separation (or lack thereof) in the reduced latent space is discussed.

3.3.1. Training convergence time

The training convergence time is reported for all networks in the Appendix Table E1. The network type, size and hyperparameters influence on the total time required to reach convergence, with an average training time for RNNs (LSTM and GRU cells) scaling higher in comparison with the convolutional networks (tCNNs and dTCNs) due to higher memory requirements for RNNs that entail a longer time in training. As expected, increasing the network size (i.e., number of parameters) correlates with a longer time in training. For instance, direct classifiers without metadata (c_F) corresponding to the hyperparameter set configuration (6) (the largest models for LSTM, GRU and dTCN) converges in training after approximately 4-5 hours for RNNs, 22 min for dTCNs and ~6 minutes for tCNNs using one photometric band on CPU. Networks processing multiband data converge at a slower rate due to larger data entries. After training, the prediction step is extremely fast: 0.5-3 ms per object for tCNNs, 1-10 ms per object for dTCNs and up to 3-20 ms per object for the RNNs on a CPU.

To track the evolution of the total loss and the accuracy during the training and validation stage, the Appendix Figures E1–E2 report the performances of the LSTM composite networks d_F and $d_{F,meta}$ using wMAE loss on the autoencoder branch and the categorical cross-entropy on the classifier branch. Over the training epochs, the loss function decreases and converges asymptotically to a constant value whereas the accuracy increases and stabilizes when the system reaches convergence. The system converges to reach at best ~73% for the best-performing LSTM d_F without metadata. By supplementing the metadata as secondary input, the accuracy increases up to $\sim 91\%$. During the validation step, the loss values decrease and moderately exceed the training losses which reinforces the ability of the networks to generalize the learned mapping from the training to the unseen validation data, as a lack of generalization would correspond to a larger gap between the training and validation losses. Generally, overfitting is detectable from a high variance in the model and a divergence in the validation loss function across training epochs despite the continuing decrease of the training loss. To prevent from such limitation, our models are trained using regularization through dropout functions in addition to a validation-based early-stopping procedure. Early-stopping monitors the validation loss values and interrupts the training before reaching the total number of training epochs if an optimal solution is found (i.e., convergence) or if the system oversees an high increase in the validation losses indicating a large variance.

We experimented with NNs classification using raw (i.e., without normalization) phase-folded light-curves. Models converge at a slower rate in an unstable pattern across the training epochs. In what follows, we focus our analysis on the results obtained using preprocessed (i.e., phase-folded and normalized) light-curves and associated metadata for MACHO periodic variables stars.

3.3.2. Labels predictions

Total loss and classification accuracy for all trained models are reported on the Appendix Tables E7-E8. We identify the best-performing models for each architecture type (LSTM, GRU, tCNN and dTCN) from minimum loss on the Test set, neither used in training nor validation. As previously mentioned, the total loss corresponds to the loss evaluated on the encoder-classifier branch (categorical cross-entropy) supplemented in composite networks to the loss the encoderdecoder branch (weighted MAE). For RNNs, the losses computed on the Validation set are close to the values obtained on the Train set across all datasets. However, a larger difference is seen in a few configurations of the tCNN direct classifier processing the multiband data in addition to the configurations of the dTCN direct classifiers. The gap between the validation and the training losses is significant for the dTCNs, which emphasizes the lack of generalization of these type of networks due to a higher complexity (large number of parameters) of the network inconsistent with the type of data in hand (1-d phase-folded light curves). Complex data would certainly benefit from higher-level network design as in dTCNs. Conversely, composite networks indicate a better stability, due to the addition of the autoencoder contribution

Table 2. Classification accuracy obtained on the Test set for the best-performing networks (see text for a description) across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]). Best performances among all nets are highlighted.

pu	Id net	LSTM	GRU	tCNN	dTCN
\boldsymbol{B}_{ba}	c_F	0.749	0.781	0.732	0.675
MACHO - B _{band}	$c_{F,meta}$	0.916	0.907	0.887	0.786
IACI	d_F	0.730	0.739	0.701	0.689
M	$d_{F,meta}$	0.905	0.886	0.900	0.802
rged	Id net	LSTM	GRU	tCNN	dTCN
MACHO - RBmerged	c_F	0.737	0.780	0.722	0.667
0-1	$c_{F,meta}$	0.890	0.910	0.815	0.747
CH	d_F	0.726	0.738	0.691	0.686
MA	$d_{F,meta}$	0.906	0.883	0.912	0.814
brid	Id net	LSTM	GRU	tCNN	dTCN
RBhy	c_F	0.776	0.789	0.744	0.696
MACHO - RBhybrid	C _{F,meta}	0.917	0.905	0.845	0.768
ACH	d_F	0.748	0.749	0.706	0.726
M	d _{F,meta}	0.905	0.880	0.904	0.818

to the total loss. We, also, notice an increase in the classification accuracy for the dTCN composite networks compared to their direct classifier counterparts. In the current application, best classification performances are achieved by RNNs and tCNNs. Appendix Table E2 reports the identifiers of the hyperparameters set configurations associated to the best-performing networks. The identifiers corresponds to the configurations set identifiers described in the Appendix Table D2 with varying number of layers or stacks $\{1,2,3\}$ and sizes {16,32}. Using this naming scheme, the identifiers of the best-performing models appear to not fall into a unique hyperparameters set configuration, as the architectures using LSTM layers performed well using 1 to 3 layers of different sizes. From Appendix Table E8, the classification results indicate about only a $\sim 1-6\%$ dispersion within the individual results per layer type in each of the architectures, which implies that the hyperparameters of the tested networks have a low-to-medium influence on the overall performances. Nonetheless, we notice for most LSTM architectures with 1 layer $(n_L = 1)$ underperform when processing multi-passband data. Deeper networks $(n_L > 1)$ appear necessary in processing larger datasets. In the current application, the qualification of best-performing models is solely based on an empirical search in the network hyperparameters space. Nonetheless, an improved search through the hyperparameters space can constitute a future work to investigate the effect of hyperparameters selection on the network performances and optimization landscape during training.

Table 2 summarizes the classification accuracy of the best-performing models reached on Test set. For the best-performing models, the overall accuracy ranges between 67% to 79% for models processing the light-curves information without metadata. In particular, without metadata , the dTCNs achieve a classification accuracy of 67-72% whereas the accuracy of RNNs and tCNNs jointly scales higher with 70–79% fraction of correct predictions. By incorporating the metadata –colors, amplitudes, averaged magnitudes and periods– in the models $c_{F,meta}$ and $d_{F,meta}$, the accuracy improves by 10–20% to reach at best ~88–92% for RNNs, ~82–92% for tCNNs and only ~75–82% for dTCNs.

The NN architectures learned on single band and multiband light-curves (the blue band B versus the multiband RB) show comparable classification accuracy. By comparing the individual results in Table 2 for each layer type, the addition of the MACHO red band data injects a moderate effect on the classification accuracy. In particular, the accuracy of the best-performing direct classifiers decreases by 0.1-3%for RNNs and 1-7% for tCNNs and dTCNs when using the multiband RB data in the merged approach in comparison with the B-band. Whereas, networks processing the multiband data via the *hybrid* approach mainly achieve a 1-4%increase in the classification accuracy compared to the Bband data. Moreover, the results on best-performing models do not indicate a significant difference in the individual performances reached by networks processing the multiband photometry RB via the merged and hybrid approaches, as individual results only indicate a 0.3-4% differences, due to the photometric bands (red and blue) in MACHO equally containing informative characteristics on the stellar variability types. The moderate disparity may indicate the need for a different strategy order when combining the data in the *merged* approach, as we combine in the current application the preprocessed (i.e., phase-folded and normalized) individual measurements per band. A different strategy can consist of combining the light-curves prior to normalization. In general, we would expect that classification using sparselyobserved multi-passband photometry would benefit from the availability of several sources of information on stellar variability. In such a case, the advantage of the *hybrid* approach would be more prevalent for systems sequentially processing the multi-passband photometry in an optimized scheme, whereas the merged approach may call for higher memory requirements in terms of CPU/GPU usage.

Classification performances are better summarized on a confusion matrix that reports the fraction of predicted labels compared to the true class labels. Optimal results correspond to a diagonal matrix with a fraction of true positives

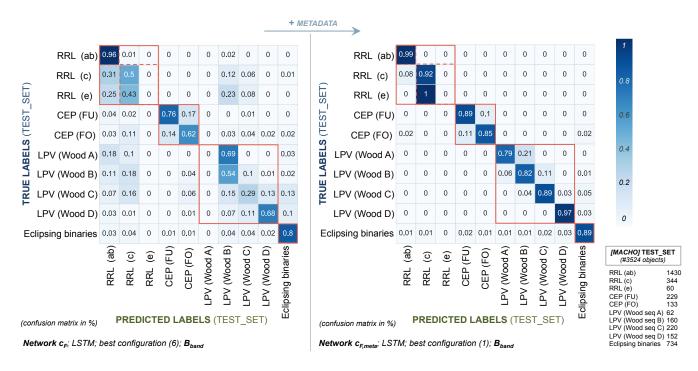


Figure 2. Confusion matrices obtained on the Test set predictions for the best-performing LSTM direct classifiers c_F and $c_{F,meta}$ on the B-band. The values in each box correspond to the number of predictions versus the initial count of true labels (indicated on the right). Main stellar variability groups are highlighted in red, respectively the RR Lyrae, the Cepheids, the LPVs and the eclipsing binaries.

per class (i.e., diagonal elements) close to unity. Figure 2 shows the performance obtained on the Test set for the bestperforming LSTM direct classifiers c_F and $c_{F,meta}$ that respectively reached an overall accuracy of 75% and 92%. Overall, the confusion matrices tell a similar story: the main stellar variability groups, highlighted in red, are recovered to a fair accuracy despite the overlap between subtypes and the misclassifications. The network c_F provides class predictions based on the information from preprocessed (i.e., normalized and phase-folded) light-curves without metadata. The observed degeneracy is to be expected between classes of objects sharing a similar shape of light-curves. By supplementing the metadata to the network, the accuracy-per-class for $c_{F,meta}$ increases and the number of false positives (i.e., off-diagonal elements in confusion matrices) is significantly diminished. Moreover, the observed porosity between adjacent classes in the confusion matrix appears to remain within the main stellar variability types.

From the confusion matrices, label predictions for the eclipsing binaries in our sample appear to overlap with other variability groups despite the use of the metadata. These misclassifications are possibly due to some degree of (true) label noise that impairs/affects the reliability of the mapping generated from training. In the current tests, class predictions of few subtypes remain erroneous despite the use of metadata. The second overtone RRL pulsators (type e) are inaccurately predicted as first-overtone RRL (type c). To avoid confusion within subtypes, a proposed solution would be to introduce

a weighting scheme on the feature contributions $\{\mathbf{X}_{enc}, \mathbf{X}_{meta}\}\$ injecting some prior knowledge regarding the features importance in VS classification.

To further investigate the classification performances, we compute additional metrics (cf. Appendix Table E4). The recall (i.e., the true positives rate or sensitivity) characterizes the ability of the network to properly retrieve the true labels and the precision depicts the level of agreement between the predictions per class and the true labels. The F1-score corresponds to a combination of both metrics. We report in Appendix Table E5 the averaged metrics for the best-performing LSTM direct classifiers c_F and $c_{F,meta}$ that respectively showcased a classification accuracy of 75% and 92%. The averaged precision, recall and F1-score are boosted respectively to 77%, 80% and 78% from an initial ~51% rate. Individual metrics per class highlight a better improvement. However, the inability of the network to predict a few subtypes such as the second-overtone RRL pulsators affect the recall and precision averaged across all observations in the Test set. Appendix Table E4 reports the averaged metrics for the bestperforming models for the GRU, tCNN and dTCN. Similar conclusions can be reached regarding the performances of the RNNs and tCNNs outperforming the dTCNs in the current tests.

We, also, investigate the accuracy within three main stellar variability groups – short-period pulsators (group 1), eclipsing binaries (group 2) and long-period variables (group 3), and report the classification accuracy achieved on the

Table 3. Selected subset of objects from the MACHO VS database for display.

	OBJECT ID (a)	Variability Type	α	δ	Period	$\langle R \rangle$	$\langle B \rangle$	$\langle K_V \rangle$	$\langle K_R \rangle$	$\langle K_V \rangle - \langle K_R \rangle$	AMPLITUDE	AMPLITUDE	SSR ^(b)
			(rad)	(rad)	(days)	(mag)	(mag)	(mag)	(mag)	(mag)	(in R)	(in B)	
n1	82.9138.798	RRL (type ab)	1.46723	-1.20004	0.539	-4.342	-4.198	20.096	19.692	0.403	0.729	1.053	0.416
n2	1.3449.1187	RRL (type c)	1.31759	-1.20170	0.337	-4.829	-4.906	19.427	19.244	0.183	0.258	0.399	0.652
n3	1.4052.2961	RRL (type e)	1.33093	-1.20398	0.264	-4.849	-4.848	19.471	19.21	0.261	0.226	0.396	1.005
n4	1.3441.45	CEP (FU)	1.31567	-1.21106	3.362	-8.420	-8.226	16.059	15.605	0.454	0.505	0.715	0.063
n5	81.9241.38	CEP (FO)	1.47038	-1.22092	1.973	-7.797	-7.420	16.832	16.195	0.637	0.217	0.320	0.208
n6	1.4046.1610	LPV (Wood seq. A)	1.33270	-1.21091	45.150	-9.351	-8.220	15.896	14.505	1.391	0.085	0.086	0.928
n7	5.4407.15	LPV (Wood seq. B)	1.34311	-1.21385	131.004	-9.397	-7.895	16.154	14.392	1.762	0.169	0.251	0.959
n8	82.9134.20	LPV (Wood seq. C)	1.46758	-1.20433	267.152	-7.578	-5.348	18.570	16.080	2.490	1.462	2.424	0.271
n9	1.3689.30	LPV (Wood seq. D)	1.32271	-1.20431	826.788	-8.949	-7.259	16.756	14.806	1.949	1.086	1.346	0.467
n10	1.3442.233	Eclipsing binary	1.31643	-1.21027	1.640	-6.332	-6.725	17.665	17.798	-0.132	0.930	1.090	0.208

(a) the standard three-integer identifier in the MACHO photometry database (field.tile.sequence).

(b) model fit residuals from Supersmoother applied to the reduced photometric B-band data.

Test set for the best-performing models per group in the Appendix Table E3. Examining the results of the bestperfoming RNNs and tCNN, the classification accuracy increases significantly after incorporating the metadata. For short-period pulsators, the accuracy of the best-performing networks reaches 78-85% without metadata solely based on the distinctive shape of these stars light-curves as the characteristic asymmetry and steep luminosity increase observed in fundamental mode pulsators. With metadata, the accuracy increases up to 92-94%. The classification of the eclipsing binaries in our sample shows a comparable improvement with a 91-92% correct predictions at best when using metadata. Similarly, the LPVs sample benefits from the use of metadata as a secondary input as best-performing networks achieve a 65-88% fraction of true positives at best from an initial 30-54% without metadata.

To characterize the need for metadata and photometric observables for classification, we performed a supplementary classification test using only the metadata as inputs to the classifier module. Results are reported on the Appendix Table E6. Using the metadata (i.e., the amplitudes, averaged magnitudes, periods and colors), the network achieves a 83% accuracy (i.e., fraction of true positives). However, the classification metrics per class indicate a high number of false predictions in addition to the inability to predict some subtypes, which corresponds to a lower precision, recall and F1score compared for instance to the performances of the bestperforming RNN direct classifier and composite network in Appendix Table E4. Overall, combining the information encoded in the light-curves and the metadata allows a better mapping characterizing the stellar variability types.

3.3.3. Reconstructed light-curves

In this section, the autoencoder performance is assessed through the quality of reconstructed light-curves X_{rec} . An ideal reconstruction would preserve the embedded (denoised) structure of the input data \mathbf{X}_{phot} . To visually assess the reconstruction quality, we select a sample of objects for display (cf. Table 3) and show the reconstructed light-curves for the best-performing composite network $d_{F,meta}$ in the Appendix Figures E3–E4. A subset for reconstructed light-curves for the best-performing LSTM composite network is also shown in Figure 3.

Overall, the reconstruction results indicates a smoothing effect on the magnitude measurements as well as a correlation between the decoder performance and the input data quality. In particular, low signal-to-noise levels in the data limits the ability of the network to recover real structures and the resulting \mathbf{X}_{rec} appears exaggeratedly smoothed out with no distinct features (such as the characteristic pulsation profile or peaks at maximum light). Furthermore, some pulsating variables can exhibit irregularity or low-frequency modulations that may evolve on timescales longer than the observed time-range, noticeably seen for Long-Secondary Periodic stars (LSP) in the Wood sequence D (Wood et al. 2004). In such cases, the folded light curves using the primary period appear as a mismatched superimposition of multiple cycles, as seen in the irregular LPV displayed in Figure 3. To prevent such limitations, detection of multiperiodicity, irregularity and low-frequency modulations should be considered to potentially isolate those objects that may require a different preprocessing strategy and classification approach.

To assess the global performances reached on the Test set, we evaluate the reconstruction error as a function of a dataquality indicator (SSR) corresponding to the model fit residuals computed from the SuperSmoother algorithm in Friedman (1984). The SuperSmoother performs a componentwise linear smoothing of the time-serie data using adaptive bandwidths. The residuals obtained from averaged differences between the time-series and the regression fits. In the current application, we use the SSR as a direct indicator of the data-quality in order to discuss the decoder reconstruc-

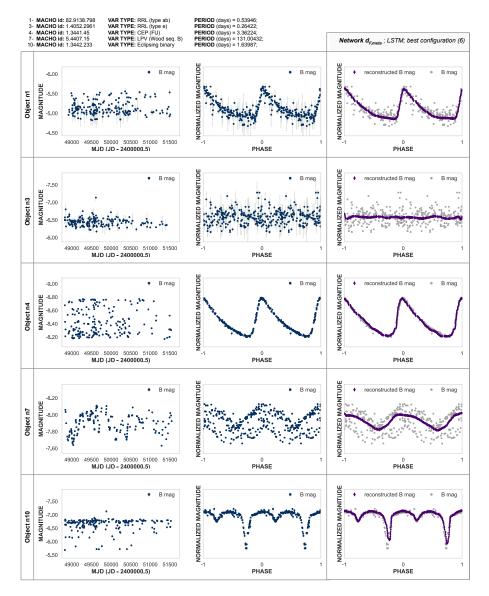


Figure 3. Reconstructed light-curves from the Test set for the best-performing LSTM composite network $d_{F.meta}$.

tions in the tested neural networks. We expect the lightcurve measurements with low signal-to-noise, irregular variations or extended low-frequency modulations in time to be associated with a high SSR. The distribution of the reconstruction error in Figure 4 suggests a distinct trend: the system is able to moderately recover the morphology of objects associated with low SSR (e.g., the Cepheids n4 and n5 and the Mira star n8) as opposed to noisier and irregular lightcurve profiles (e.g., objects n3, n6 and n7 which are RRL of type e and LPVs from the Wood sequences A and B).

A comparable analysis on the performances of the bestperforming GRU, tCNN and dTCN composite models $d_{F,meta}$ reaches a similar conclusion on the distribution of the reconstruction error (cf. Appendix Figure E5). From the reconstructed profiles of the selected objects (cf. Appendix Figures E3-E4), networks achieve overall comparable performances despite few noticeable differences, such as the reconstruction of the shockwave propagating before the maximum light in the fundamental model RR Lyrae (object n1) that is recovered by the convolutional networks but heavily smoothed out in the LSTM and GRUs. The RNNs also appear to overly smooth out the modulations of the LPV star (object n9, LPV Wood sequence D), while convolutional nets partially restore discontinuous plateaus. Furthermore, the composite LSTM model appears to preserve the shape of the primary and secondary eclipses in the detached eclipsing binary (object n10), while convolutional nets (dTCNs and tCNNs) partially recover the depth of the eclipses and the GRU disproportionately smoothing out these features. Based on the reconstructed profiles of selected objects, the moderate smooth-

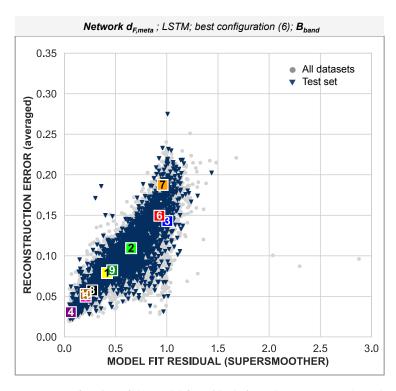


Figure 4. Reconstruction error (MAE) as a function of the model fit residuals from the SuperSmoother algorithm (Friedman 1984) for the best-performing LSTM $d_{F,meta}$ on the B-band. The highlighted numbers (1 to 10) refer to the subset of selected objects from the Test set used to showcase the reconstruction quality of the autoencoder branch.

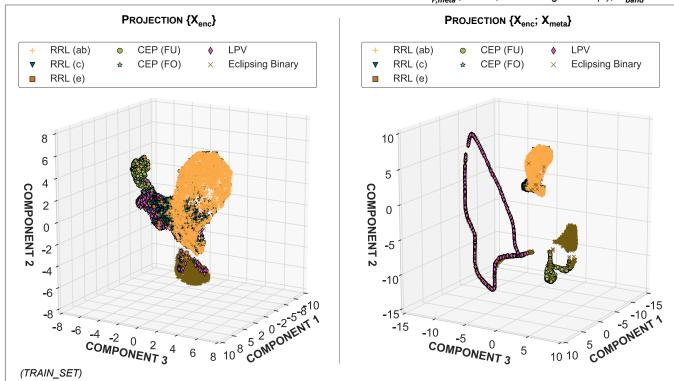
ing of small-scale features by the RNNs can be interpreted by these models focusing on an overall data structure propagated through the RNN cells. The signal-to-noise of these features plays a role as well in the reconstruction quality. Convolutional NN variants, given the choice of kernel sizes for convolutions, exhibit a similar behavior through a localized smoothing in the reconstructed profiles.

From the reconstruction error distributions, the reconstruction performances of best-performing LSTM, GRU, tCNN and dTCN show a comparable reconstruction ability. In our current designs, the decoder outputs reconstructed magnitudes. To further characterize the ability of the decoder modules to unfold the generated embeddings into reconstructed profiles close to the input data, the development of novel designs to output reconstructed profiles along with the associated prediction errors is left for future study.

3.3.4. Latent space exploration

Using dimensionality reduction algorithms, encoded features of Train set can be projected into a reduced (2 or 3-d) representation. The results for the best-performing LSTM composite network $d_{F,meta}$ are shown in Figure 5. For better visualization, projections are separated for the three main variability groups in the Appendix Figures E6 to E8. We limit the analysis of the latent representation to the training dataset as it corresponds to the learned partitioning.

The encoded features generated from the best-performing composite network are projected onto a three-dimensional representation using the UMAP algorithm (McInnes et al. 2018) described in Appendix B.2. The degree of separation of the clusters in the reduced representation space characterizes the type of information fed to the classifier network. Without metadata, solely based on the encoded morphology of the light-curves, the projection outlines (cf. Figure 5 on the left) a large fraction of RR Lyrae, Cepheids, eclipsing binaries and LPVs isolated to some extend in the projected space. The level of separability of these clusters is limited by the overlap between classes of objects sharing a similar shape of (preprocessed) light-curves, as noticed for the majority of LPVs, overtone pulsating RR Lyrae, Cepheids and few eclipsing binaries in our sample. In the detailed representations (cf. Figures E6 to E8), the encoded features of eclipsing binaries are clustered into composition of a compact aggregate, a dispersed set and outliers, while short-period pulsators cluster into a compact aggregate of fundamental mode pulsators and an overlapping blend of overtone pulsators given their similar light-curves profiles. In the latent space, the LPVs sample clusters into a compact aggregate without a clear delineation between the different subtypes; this suggests a lack of discriminating features in \mathbf{X}_{enc} that would be necessary to distinguish the different subtypes.



Network d_{F,meta}; LSTM; best configuration (6); B_{band}

Figure 5. 3-d representation of encoded features from the best-performing LSTM composite network $d_{F,meta}$ on the B-band. Generated encodings are projected into a reduced 3-d representation using the UMAP algorithm.

When metadata is supplemented, the projection of the augmented features set $\{X_{enc}, X_{meta}\}$ shows a better separability in the reduced latent space (cf. Figure 5 on the right); this separability also coincides with the improvement in the classification accuracy for the networks utilizing metadata to complement the encoded photometry. In particular, the detailed representations for the main variability types highlight wellseparated clusters for the short-period pulsators, while the sample of eclipsing binaries clusters into a composition of a compact aggregate, a filamentary structure and dispersed outliers. The diversity in substructures in the eclipsing binaries sample can be explained by the different categories of binaries merged in the MACHO database (e.g., contact, detached and semi-detached stellar binaries) in addition to possible label contamination. Similarly, the LPVs sample is well-separated from others variability groups and is projected onto a filamentary structure with an enhanced separability between the different subtypes. The best-performing GRU, tCNN and dTCN composite networks give comparable projection results.

To investigate the properties of the embeddings obtained from composite networks versus direct classifiers, a projection of the generated encodings obtained by the bestperforming LSTM direct classifier is reported in Appendix Figure E9. Compared to the composite network, the direct classifier network generates an embedding layer X_{enc} by propagating the information between an encoder and a classifier module. In the latent representation, distinct clusters are noticeable along with the expected overlap of objects with a similar light-curves shape. From the 3-d representation, the main difference between the embeddings generated from the LSTM direct classifier (cf. Appendix Figure E9) and the LSTM composite network (cf. Figure 5) lies in the clusters (intraclass) dispersion. The encoder-decoder combination in the composite network appears to narrow the clusters in the latent representation; this effect would be useful for anomaly detection to locate potential outliers at the outskirts of identified compact aggregates or the intersection of adjacent clusters.

To summarize, composite NN architectures are able to encode the photometric observables into substructures associated with the stellar variability classes. Without metadata, the encodings generated from the photometric data cluster into distinct aggregates despite the overlap between classes of objects sharing a similar morphology of preprocessed lightcurves. By supplementing the metadata as a secondary input to complement the encoded photometry, the level of separation in the latent space is enhanced, which aligns with the overall increase in classification accuracy. An examination of the nature of the overlap regions of the latent space, as well as the properties of the different aggregates, are left for future study. We would expect similar studies using larger VS datasets will help test the potential universality of the latent space, and also reveal potential outliers that could constitute new subclasses.

4. CONCLUSIONS

In this work, we explored the use of NN architectures for VS classification through various use-case scenarios. These architectures allowed us to generate higher-abstraction encodings of the photometric data without the need for handcoded feature engineering.

Two types of architectures, identified as direct classifiers and composite networks, are tested. Both networks are composed of an encoder module to transform the data into a reduced representation and a classifier to predict labels. Composite networks include a decoder module to define an encoded representation of the input data by optimal reconstruction. In our analysis, VS classification using multi-passband photometric data can be performed in two approaches, either by encoding a merged representation of all passband measurements (*merged* approach) or jointly processing individual encodings (*hybrid* approach). Sparsely observed multipassband photometry would benefit from adopting the latter approach.

In this work, we also experimented with a variety of NN architectures and investigated the effect of ancillary metadata on classification performance. Through an empirical search on different hyperparameters set configurations, bestperforming models were identified. Models exploiting hyperparameters tuning through optimized ML approaches or bayesian optimization are left for future work. In our work, we found that systems solely exploiting the time-series data are able to reach a ~70% accuracy for the best-performing models. By supplementing the metadata as a secondary input, a net increase in the classification accuracy is observed across all network types, reaching at best a ~91% accuracy for the best-performing LSTMs and temporal CNNs models. Misclassifications for the best-performing networks are primarily restricted to the main stellar variability types, which provides a strong incentive for a multiple-stage architecture for label predictions, to first predict the main stellar variability type followed by subtypes prediction. On a computational level, the training convergence time for RNNs models was found to be longer, due in part to larger memory allocation costs.

For composite networks, the reconstruction quality of the decoder module appears highly contingent on the input data properties (ie., the signal-to-noise level and smoothness of the light-curves profiles). Variable stars exhibiting multiperiodicity, irregularity or modulations over time appear in their phase-folded representation as a mismatch of superimposed cycles that a network is unable to learn and overly smooths out in reconstruction.

The exploration of the learned encodings indicated a clear clustering linked to the stellar variability types. Without metadata, clusters of variables appear isolated despite the overlap noticed for objects sharing similar light-curves profiles. Supplementing the metadata to the encoded information predictably lessens such degeneracy and enhances the separation between the classes; this in turn, accounts for the increase in the fraction of correct predictions. We would expect the latent representations to highlight interesting properties in the data and pinpoint to potential outliers, unknown stellar variability types or new subtypes within known variability classes.

To conclude, various NN architectures are able to capture low-dimensional data representations and reach achieve excellent classification accuracy without the need for handcoded featurization. The best-performing networks in our tests are primarily LSTM- and tCNN-based models, with the latter benefiting from smaller training convergence time and smaller memory footprints.

As a future direction, developing a baseline for an automated system able to learn a wider range of stellar variability traits should be explored. The need for general architectures is strongly motivated from the fact that massive surveys are set to produce large datasets with a blend of different types of stellar variables such as aperiodic VSs (e.g., cataclysmic stars and microlensing events) as well as periodic and quasiperiodic variables (e.g., pulsators, rotators and eclipsing binaries). Automated classification for periodic VSs presented here exploits phase-folded representations as well as the information from the frequency domain, while classification of quasi-periodic variables require the use of a combination of multiple data representations - phase-folded light-curves, periodograms, O-C diagrams and the time-series - to produce reliable class predictions. To meet the need for a general framework, one proposed design would consist of a multistage architecture with different components specialized to distinguish distinct stellar variability traits, to first discriminate between the three categories of periodic, quasi-periodic and aperiodic VSs then follow with the classification into the stellar variability types and subtypes.

Despite our analysis being focused on applications for periodic variable stars classification, all arguments presented in the scope of this work extend to other types of astronomical time-series. NNs can be built with a comparable architecture for supernovae classification and transient detection, with adaptations in the of the input data representation, the preprocessing strategy and the necessary metadata (e.g., redshift measurements and spectral features). Similarly, our approaches in processing multi-passband photometric data for classification can be generalized to other variable objects. On the network design, the complexity of the networks should conform with the type of the data. In particular, higher-level multi-dimensional data would require deeper and complex architectures compared to a 1-d information such as phasefolded light-curves. Using the presented methodology on different datasets, we would expect, on one hand, an increase of the classification accuracy when supplementing the metadata, and on the other hand, a significant improvement in classification when combing sparse observations across multiple photometric bands. For sparsely observed light-curves, the networks processing multiband data would very likely exceed the classification results obtained with a single photometric band. We expect the landscape of the latent space representation to differ from current results. Further analysis of latent representations obtained from a larger scope of variability types is left for future study.

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Software: NumPy (Oliphant 2006; Walt et al. 2011), scikit-learn (Pedregosa et al. 2011), TensorFlow (Abadi et al. 2015, 2016), keras (Chollet et al. 2015), and exoplanet package (Foreman-Mackey et al. 2019) and its dependencies for GP model prediction: celerite (Foreman-Mackey et al. 2017; Foreman-Mackey 2018), pymc3 (Salvatier et al. 2016) and theano (Theano Development Team 2016).

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APPENDIX

A. CLASSIFICATION USING MULTIBAND PHOTOMETRIC DATA

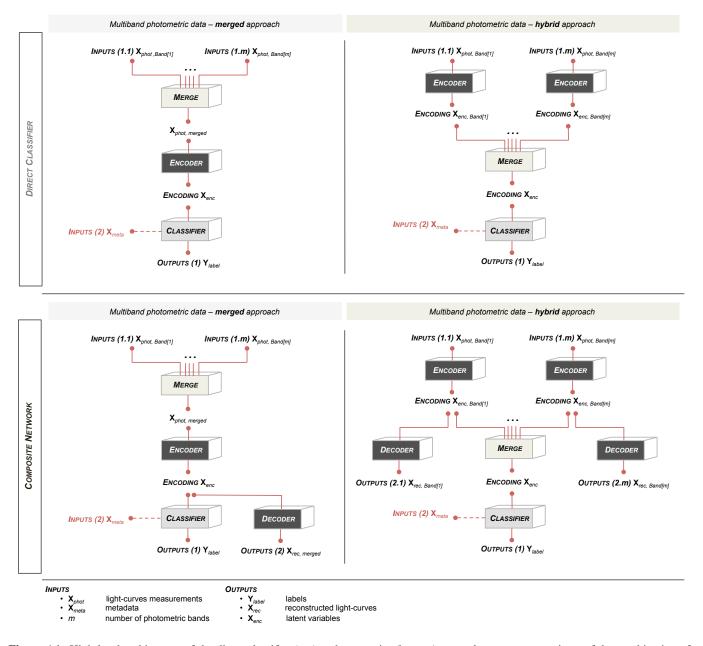


Figure A1. High-level architecture of the direct classifier (top) and composite (bottom) networks across two variants of the combination of multi-passbands photometric data, identified as *merged* and *composite* approaches [left and right]. In the *merged* approach, multi-passband measurements are merged into a unique observable $\mathbf{X}_{phot,merged}$ processed by the encoder module to compute the latent representation \mathbf{X}_{enc} . Whereas, the *hybrid* approach independently encodes the multi-passband measurements into individual features merged at a latter time into a compact encoded representation \mathbf{X}_{enc} . In both scenarios, the classifier module exploits the generated encodings \mathbf{X}_{enc} , along with metadata \mathbf{X}_{meta} , for label predictions. Composite networks differ from the direct classifiers by the addition of a decoder module connected at the bottleneck level to the encoder to generate the embeddings by optimal reconstruction.

In the *merged* approach, the multi-passband photometric data can be combined into a 2-d tabular data of dimension $(N_{p,merged}^* \times (2m+1))$, in which the *m* photometric band magnitude and associated error measurements are provided along with the observation epochs.

The i^{th} observation in $\mathbf{X}_{phot,merged}$ corresponds to the matrix representation:

$$\boldsymbol{x}_{i} = \begin{pmatrix} t_{i}^{(1)}, & \left[\max_{i}^{(1)}, \sigma_{i}^{(1)} \right]_{\text{band } 1}, & \cdots & \left[\max_{i}^{(1)}, \sigma_{i}^{(1)} \right]_{\text{band } m}, \\ \vdots & \vdots & \vdots \\ t_{i}^{(P^{*})}, & \left[\max_{i}^{(P^{*})}, \sigma_{i}^{(P^{*})} \right]_{\text{band } 1} & \cdots & \left[\max_{i}^{(P^{*})}, \sigma_{i}^{(P^{*})} \right]_{\text{band } m} \end{pmatrix},$$
(A1)

where, *m* refers to the number of photometric bands and P^* designates the total count of datapoints $N^*_{p,merged}$ for the *i*th observation. In this representation, the sparsity level of the matrix depends on the observation times across the different photometric bands.

Alternatively, multi-passband data can be combined into a 2-d tabular data of dimension $(N_{p,merged} \times 4)$, in which an auxiliary vector encoding the photometry band is provided along with the observation epochs and the *m* band magnitude and associated error measurements. The encoding vector associates each photometric band type to a dictionary item (numerical or qualitative variables).

$$\mathbf{x}_{i} = \begin{pmatrix} \operatorname{dict}_{\operatorname{band} 1}, & [\mathbf{t}_{i}, \operatorname{mag}_{i}, \sigma_{i}] \\ \vdots \\ \operatorname{dict}_{\operatorname{band} m}, & [\mathbf{t}_{i}, \operatorname{mag}_{i}, \sigma_{i}] \\ \end{bmatrix}_{\operatorname{band} m} \end{pmatrix},$$
(A2)

where, the enclosed measurements per band $\{b\}_{b:1 \to m}$ correspond to a matrix of $(P_b \times 4)$ dimension as follows.

$$\begin{bmatrix} \mathbf{t}_i, \mathbf{mag}_i, \boldsymbol{\sigma}_i \end{bmatrix}_{\text{band } b} = \begin{pmatrix} [t_i^{(1)}, \mathbf{mag}_i^{(1)}, \boldsymbol{\sigma}_i^{(1)}]_{\text{band } b} \\ \vdots \\ [t_i^{(P_b)}, \mathbf{mag}_i^{(P_b)}, \boldsymbol{\sigma}_i^{(P_b)}]_{\text{band } b} \end{pmatrix},$$
(A3)

where, $\{P_b\}_{b:1 \to m}$ refers to the number of datapoints per band.

B. DESCRIPTION OF NNS, UMAP AND GAUSSIAN PROCESS MODELING

B.1. RNN, CNN and TCN

Recurrent neural network (RNN) refers to a neural network architecture composed with interconnected nodes through a directed graph (cyclic or acyclic) along a temporal sequence. In the standard architecture, the fully-connected RNN layer is constructed such that each node is interlinked to the adjacent units. Each node in the standard architecture corresponds to a neural unit with an activation function and a weight. The LSTM (*Long-Short Term Memory*, Hochreiter & Schmidhuber 1997) and the GRU (*Gated Recurrent Network*, Cho et al. 2014) are variants of the RNN with a higher level node structure composed with multiple subunits acting as internal regulators to the propagated information within the network. Both the LSTM and GRU cells exploit a forget gate and an input gate, and the LSTM utilizes an additional output gate. RNNs applications on astronomical time-series include SNe classification (Charnock & Moss 2017) VS classification using autoencoders (Naul et al. 2018), gravitational-waves signal denoising (Shen et al. 2019), periodic VS classification (Tsang & Schultz 2019), and online transient events detection (Muthukrishna et al. 2019a; Möller & de Boissière 2019).

Convolutional neural network (CNN) refers to a NN architecture with convolutional layers that applies a series of convolutions through overlapping windows, allowing to capture spatial correlations in the data. The standard CNN architecture utilizes pooling layers after convolutions to downsize the data in addition to fully-connected layers. The performances of convolutional-based neural networks has been demonstrated in a broad range of astronomical data applications such as galaxy classification (Dieleman et al. 2015; Aniyan & Thorat 2017; Kim & Brunner 2017; Domínguez Sánchez et al. 2018), VS classification using asteroseismology (Hon et al. 2017), supernovae classification (Cabrera-Vives et al. 2016; Pasquet et al. 2019b; Brunel et al. 2019), photometric redshifts estimation (Hoyle 2016; DIsanto & Polsterer 2018; Pasquet et al. 2019a), cosmological parameters inference (Ntampaka et al. 2020), parameters estimation from 21-cm tomography (Gillet et al. 2019), strong lensing detection (Lanusse et al. 2018; Jacobs et al. 2019), gravitational-waves signal detection (Gebhard et al. 2017; Gabbard et al. 2018; George & Huerta 2018a; Fan et al. 2019; Gebhard et al. 2019) (George & Huerta 2018b), generator models for weak lensing convergence maps (Mustafa et al. 2019), cosmic rays modeling (Erdmann et al. 2018), and classification of supernovae spectra (Muthukrishna et al. 2018), fast radio bursts classification (Connor & Leeuwen 2018), and classification of supernovae spectra (Muthukrishna et al. 2019b).

Temporal convolutional neural network (TCN) refer to a NN architecture in Lea et al. (2017), initially derived from the Wavenet architecture (Oord et al. 2016). The network is a composition of a serie of dilated convolutions and residual blocks used to expand the filters receptive fields and reduce the training convergence time. A detailed description of deep learning techniques is available in specialized computer science publications, such as the overview on DL techniques by Schmidhuber (2015).

B.2. UMAP

The UMAP (*Uniform Manifold Approximation and Projection*) algorithm is a nonlinear dimensionality reduction algorithm introduced by McInnes et al. (2018). Assuming a uniform distribution of the data on a locally connected Riemannian manifold, the algorithm computes a low-dimensional representation by optimizing a fuzzy set cross-entropy between the simplicial set representations of the data and the target embeddings. The UMAP has gained interest and use recently for astronomical data applications such as the SDSS DR15 spectroscopic data classification in Clarke et al. (2019) and anomaly detection in SDSS galaxy samples in Reis et al. (2019).

B.3. Model prediction using Gaussian Processes

Part of preprocessing, data reduction is performed using Gaussian Processes (GPs) model to generate fixed-length representations of each source. Foreman-Mackey et al. (2017) provides GP kernels suitable for astronomical time-series, with various applications including radial velocity fitting and transit modeling. For periodic VSs, we select a GP kernel based on a composition of stochastically driven damped harmonic oscillators (SHOs) with a quasi-periodic covariance term. For each SHO model, the associated power spectral density $S(\omega)$ is defined as following:

$$S(\omega) = \sum_{i=1}^{N_{SHO}} S_j(\omega), \tag{B4}$$

$$S_{j}(\omega) = \sqrt{\frac{2}{\pi}} \frac{S_{0,j} \,\omega_{0,j}^{4}}{(\omega^{2} - \omega_{0,j}^{2})^{2} + \omega^{2} \omega_{0,j}^{2} / Q_{j}^{2}},\tag{B5}$$

where, $\omega_{0,j}$ and Q_j respectively refer to the frequency of the undamped oscillator and the associated quality factor of the j^{th} oscillator. The parameter $S_{0,j}$ is proportional to the resonance (i.e., $\omega = \omega_{0,j}$) power.

Our data reduction approach is a two-fold process: first, we fit a GP model on the observed data \mathbf{x}_{obs} and second, we use the model to predict a representation of the time-serie over a reduced time-frame \mathbf{T}_{red} along with the uncertainties from the GP fit. For periodic VSs, we use a GP model corresponding to a mixture of $N_{SHO} = 2$ SHOs. We based our selection on the applications of GP modeling to data showcasing periodicity patterns as transit light-curves or stellar variables in Foreman-Mackey et al. (2017). The GP model with 2 SHOs is chosen in order to take into consideration of multiperiodicity often encountered in variables stars. The current parametrization and kernel type is proper to the current work realized on a dataset of pulsating variables and eclipsing binaries.

In the model parameterization, the periodicity (due to pulsation or binarity) is captured by the resonance frequency, such that:

$$\omega_{0,j} = \frac{4\pi Q_j}{P_j + \sqrt{4Q_j^2 - 1}},\tag{B6}$$

$$S_{0,j} = \frac{A_j}{\omega_{0,j} Q_j}.$$
 (B7)

Here, P_j and A_j refer respectively to the period and amplitude of the variability per SHO model *j*. For each observed light-curve, an independent GP model is fitted. A full description of the GP modeling can be found in Foreman-Mackey et al. (2017) and the available open source Foreman-Mackey et al. (2019).

Using the MAP (*Maximum-a-posteriori*) solution, model prediction is performed on a time frame \mathbf{T}_{red} sampled within the range of observed epochs \mathbf{T}_{obs} . For unevenly sampled data, the GP predictions located in large time gaps are associated to a high uncertainty of the model. To prevent such limitation, we developed an approach to generate a random time range within the observed \mathbf{T}_{obs} outside significant time gaps. Using the unsupervised K-means algorithm applied to the time differences $\Delta \mathbf{T}_{obs}$, observations are clustered based on their proximity in time. Significant time gaps \mathbf{T}_{gaps} are identified within the group of large time differences, and an optional rejection criterion is supplemented to refine the detected time gaps to span, at least, higher than *n* cycles of the primary period of the light-curve. The reduced time frame \mathbf{T}_{red} is generated via random sampling of time values within the observed time range outside the identified time gaps $\mathbf{T}_{set} = {\mathbf{T}_{obs} \setminus \mathbf{T}_{gaps}}$. For each detected subset *j* of clustered observations, time values are obtained either by randomly generating values within the range of $\mathbf{T}_{set,j}$ or by randomly selecting of values in $\mathbf{T}_{set,j}$ shifted by a random $\delta_t > 0$. The second approach generates a time frame \mathbf{T}_{red} close to the observed \mathbf{T}_{set} .

The GP model fitted to the data is a mixture of 2 SHOs with the following parameters.

$$P_{1} = P, P_{2} = P/2, A_{1} = \exp^{\log A}, A_{2} = m_{A} \times \exp^{\log A}, Q_{1} = Q_{0} + \Delta Q, Q_{2} = Q_{0}, m_{A} \sim \mathcal{U}(0, 1), \log A \sim \mathcal{N}(\mu_{A}, \sigma_{A}^{2}), Q_{0} > \frac{1}{2}, \Delta Q \sim \mathcal{N}(\mu_{Q}, \sigma_{Q}^{2}),$$
(B8)

with, *P* is the primary period of the time-serie, (μ_A, σ_A^2) refer to the amplitude of the time series and associated error (or a fixed variance), and (μ_O, σ_O^2) are strictly positive values set to separate the two oscillation modes.

To illustrate the results of data reduction using the aforementioned GP model and prediction scheme, a display of MACHO light-curves is provided in Figure B1.

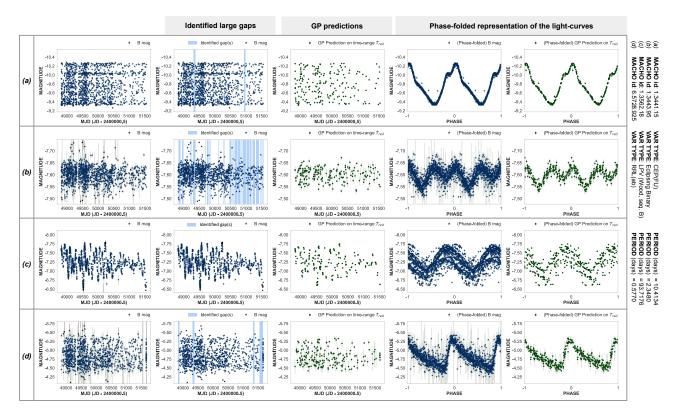


Figure B1. Displays of reduced MACHO light-curves using gaussian processes (GPs) model fit and prediction. A GP model is fitted to each observed light-curve and the best model is associated to the MAP (*Maximum-a-posteriori*) solution. The predictions –magnitudes and associated errors– are computed on a reduced time-range \mathbf{T}_{red} of 200 datapoints obtained by a random selection of time values within the observed time-range \mathbf{T}_{set} (outside the identified large gaps highlighted in light blue) and shifted with a random lag $\delta_t \in [0, \Delta T_{set}]$. Phase-folded representations of light-curves are given only as a reference. GP predictions are computed on the initial time-series.

C. METRICS FOR MULTICLASS CLASSIFICATION

To quantify the performances in multiclass classification, the following metrics are computed:

Table C1. Classification metrics

Metrics		Per class $\{j\}_{j:1 \to N_C}$		CRO-AVERAGING
Precision	Precision _(j)	$= \frac{\mathrm{TP}_{(j)}}{\mathrm{TP}_{(j)} + \mathrm{FP}_{(j)}}$	Precision _M	$= \frac{1}{N_C} \sum_{j=1}^{N_C} \operatorname{Precision}_{(j)}$
Recall (Sensitivity)	Recall _(j)	$= \frac{\mathrm{TP}_{(j)}}{\mathrm{TP}_{(j)} + \mathrm{FN}_{(j)}}$	Recall _M	$= \frac{1}{N_C} \sum_{j=1}^{N_C} \operatorname{Recall}_{(j)}$
F1-score	F1-score(j)	$= 2 \times \frac{\text{Recall}_{(j)} \times \text{Precision}_{(j)}}{\text{Recall}_{(j)} + \text{Precision}_{(j)}}$	F1-score _M	$= \frac{1}{N_C} \sum_{j=1}^{N_C} \text{F1-score}_{(j)}$
Accuracy	Accuracy	$= \frac{1}{N_s} \sum_{j=1}^{N_C} \mathrm{TP}_{(j)}$		

with N_C the total number of classes, N_s the number of true samples and $TP_{(j)}$, $TN_{(j)}$, $FP_{(j)}$ and $FN_{(j)}$ respectively referring to the true positives, the true negatives, the false positives and the false negatives computed from the predictions on objects from the true class *j*.

D. NETWORKS

Table D1. Networks configuration – Entries.

Network type	INPUTS	OUTPUTS
classifier c_F	\mathbf{X}_{phot}	Y _{label}
classifier $c_{F,meta}$	$\{\mathbf{X}_{phot},\mathbf{X}_{meta}\}$	\mathbf{Y}_{label}
composite d_F	\mathbf{X}_{phot}	$\{\mathbf{Y}_{label}, \mathbf{X}_{rec}\}$
composite $d_{F,meta}$	$\{\mathbf{X}_{phot},\mathbf{X}_{meta}\}$	$\{\mathbf{Y}_{label}, \mathbf{X}_{rec}\}$

Table D2. Networks configuration – Hyperparameters.

LAYER TYPE	CONFIGURATION ID	NB layers (n_L)	Size (n_S)	Common hyperparameters
	(1)	1		bidirectional network;
	(2)	2	16	categorical classification;
RNN {LSTM; GRU}	(3)	3	_	drop fraction=0.25;
KINI (LSTM, OKO)	(4)	1		batch size=128; maximum training epochs=200;
	(5)	2	32	Adam ^(a) optimizer; optimizer learning rate= 5×10^{-4} ;
	(6)	3	_	[composite nets: embedding dimension $n_E=8$; loss weights ^(b) ={1:1}
LAYER TYPE	CONFIGURATION ID	NB LAYERS (n_L)	Size (n_S)	Common hyperparameters
	(1)	1		convolution kernel size $n_K=5$;
	(2) -	2	16	categorical classification;
temporal CNN	(3)	3		drop fraction=0.25;
temporal CNN	(4)	1		batch size=128; maximum training epochs=200;
	(5)	2	32	Adam ^(a) optimizer; optimizer learning rate= 5×10^{-4} ;
	(6)	3		[composite nets: embedding dimension n_E =8; loss weights ^(b) ={1:1}
Layer type	Configuration id	NB STACKS (<i>n</i> _L)	Size (n_S)	Common hyperparameters
	(1)	1		dilation rate ^(c) $r=2$; convolution kernel size $n_K=3$;
	(2)	2	16	categorical classification;
dilated TCN	(3)	3		drop fraction=0.25;
unacu i civ	(4)	1		batch size=128; maximum training epochs=200;
	(5)	2	32	$Adam^{(a)}$ optimizer; optimizer learning rate=5×10 ⁻⁴ ;
	(6)	3		[composite nets: embedding dimension $n_E=8$; loss weights ^(b) ={1:1}

(a) Adam optimization algorithm (Kingma & Ba 2017).

(b) Loss weights report the contributions of individual branches {wee, wed} in the composite networks, respectively the encoder-classifier and encoder-decoder branches.

(c) Dilation factors in dTCN correspond to $\{2^{j-1}\}_{j:1 \to r}$, with r > 1 the dilation rate.

NEURAL ARCHITECTURES FOR VARIABLE STAR CLASSIFICATION

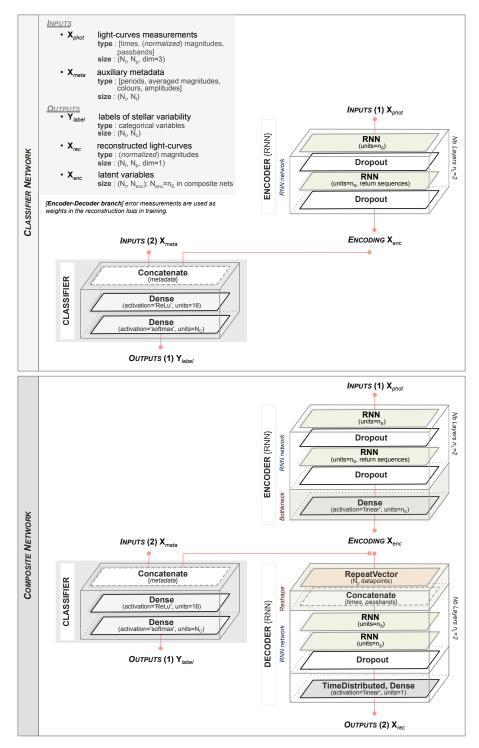


Figure D1. Architectures of the direct classifier and composite RNNs. Naming convention follows the implementation in keras.

JAMAL AND BLOOM

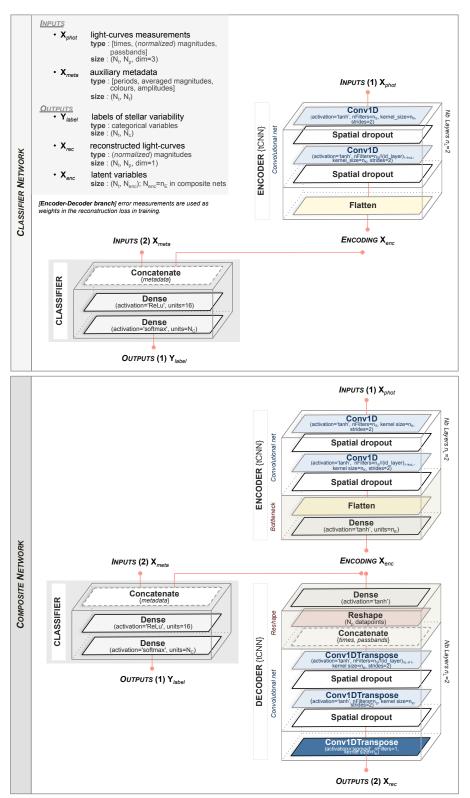


Figure D2. Architectures of the direct classifier and composite tCNNs. Naming convention follows the implementation in keras.

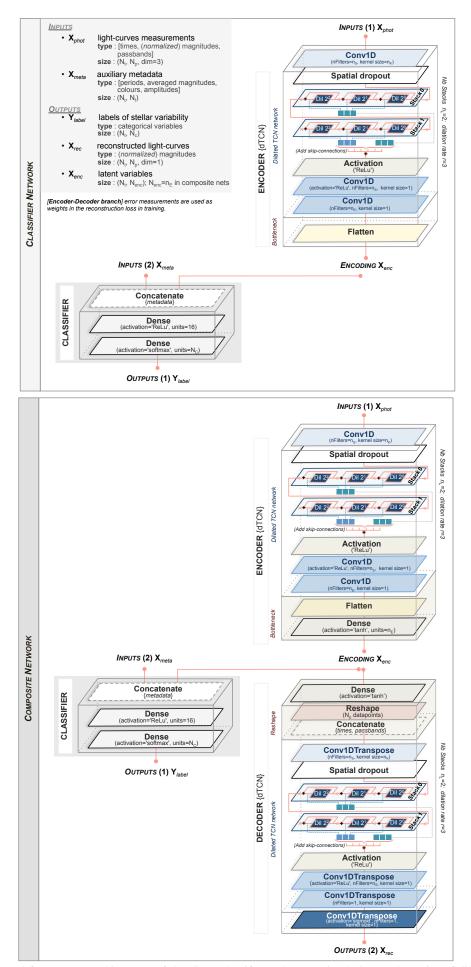


Figure D3. ** Corrected figures ** Architectures of the direct classifier and composite dTCNs. The series of dilated convolutions and residual stacks follow the Wavenet architecture (Oord et al. 2016) augmented with additional dropout functions to prevent overfitting. Naming convention follows the implementation in keras.

Table D3. Network sizes corresponding to the total number of parameters per model across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]). The identifiers of the hyperparameters set configurations (1) to (6) are ordered by increasing size. Largest networks for the RNNs, tCNNs and dTCNs correspond respectively to the identifiers (6), (4) and (6) and the smallest configurations to (1), (3) and (1). The metadata in the current application ($N_f = 6$) adds 96 parameters.

Network type	C _F	C _{F,meta}	d_F	$d_{F,meta}$
	3292; (1)	3388; (1)	6661;(1)	6757; (1)
	9564; (2)	9660; (2)	19205; (2)	19301; (2)
LSTM	10460; (4)	10556; (4)	21157; (4)	21253; (4)
LOIM	15836; <i>(3)</i>	15932; (3)	31749; <i>(3)</i>	31845; <i>(3)</i>
	35292; (5)	35388; (5)	70821; (5)	70917; (5)
	60124; (6)	60220; (6)	120485; (6)	120581; (6)
	2652; (1)	2748; (1)	5157; (1)	5253; (1)
	7356; (2)	7452; (2)	14565; (2)	14661; (2)
GRU	8156; (4)	8252; (4)	16101; (4)	16197; (4)
Gite	12060; (3)	12156; (3)	23973; <i>(3)</i>	24069; <i>(3)</i>
	26780; (5)	26876; (5)	53349; (5)	53445; (5)
	45404; (6)	45500; (6)	90597; (6)	90693; (6)
	5329; (3)	5425; (3)	8371; (<i>3</i>)	8467; (<i>3</i>)
	12118; (6)	12214; (6)	15925; (2)	16021; (2)
tCNN	13924; (2)	14020; (2)	16465; (6)	16561; (6)
icitit	28908; (5)	29004; (5)	26853; (5)	26949; (5)
	51676; (1)	51772; (1)	41349; <i>(1)</i>	41445; <i>(1)</i>
	103132; (4)	103228; (4)	67941; (4)	68037; (4)
	54100; (1)	54196; (1)	60335; (1)	60431; (1)
	56212; (2)	56308; (2)	64559; (2)	64655; (2)
dTCN	58324; (3)	58420; (3)	68783; <i>(3)</i>	68879; (<i>3</i>)
uten	61380; (4)	61476; (4)	75119; (4)	75215; (4)
	69700; (5)	69796; (5)	91759; (5)	91855; (5)
	78020; (6)	78116; (6)	108399; (6)	108495; (6)
		CF 3292; (1) 9564; (2) 10460; (4) 15836; (3) 35292; (5) 60124; (6) 7356; (2) 8156; (4) 12060; (3) 26780; (5) 45404; (6) 12118; (6) 13924; (2) 28908; (5) 51676; (1) 103132; (4) dTCN 54100; (1) 56212; (2) 58324; (3) 61380; (4) 69700; (5)	CF CF,meta TYPE 3388; (1) 9564; (2) 9660; (2) 10460; (4) 10556; (4) 15836; (3) 15932; (3) 35292; (5) 35388; (5) 60124; (6) 60220; (6) 60124; (6) 60220; (6) 7356; (2) 7452; (2) 8156; (4) 8252; (4) 12060; (3) 12156; (3) 26780; (5) 26876; (5) 26780; (5) 26876; (5) 45404; (6) 45500; (6) 12118; (6) 12214; (6) 13924; (2) 14020; (2) 28908; (5) 29004; (5) 51676; (1) 51772; (1) 103132; (4) 103228; (4) 103132; (2) 56308; (2) 58324; (3) 58420; (3) 61380; (4) 61476; (4) 69700; (5) 69796; (5)	c_F $c_{F,meta}$ d_F TYPE 3292; (1) 3388; (1) 6661; (1) 9564; (2) 9660; (2) 19205; (2) 10460; (4) 10556; (4) 21157; (4) 15836; (3) 15932; (3) 31749; (3) 35292; (5) 35388; (5) 70821; (5) 60124; (6) 60220; (6) 120485; (6) 2652; (1) 2748; (1) 5157; (1) 7356; (2) 7452; (2) 14565; (2) 8156; (4) 8252; (4) 16101; (4) 12060; (3) 12156; (3) 23973; (3) 26780; (5) 26876; (5) 53349; (5) 26780; (5) 26876; (5) 53349; (5) 26780; (5) 26876; (5) 90597; (6) 12118; (6) 12214; (6) 15925; (2) 13924; (2) 14020; (2) 16465; (6) 28908; (5) 29004; (5) 26853; (5) 51676; (1) 51772; (1) 41349; (1) 103132; (4) 103228; (4) 67941; (4) 103132; (4) 103228; (2) 64

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Network type	c_F	$c_{F,meta}$	d_F	$d_{F,meta}$
	3292;(1)	3388;(1)	6661;(1)	6757;(1)
	9564 ; (2)	9660;(2)	19205 ; (2)	19301 ; (2)
ISTM	10460;(4)	10556;(4)	21157;(4)	21253 ; (4)
20101	15836 ; <i>(3)</i>	15932 ; <i>(3)</i>	31749 ; <i>(3)</i>	31845 ; <i>(3)</i>
	35292 ; (5)	35388;(5)	70821;(5)	70917;(5)
	60124 ; (6)	60220;(6)	120485;(6)	120581 ; (6)
	2652;(1)	2748;(1)	5157;(1)	5253;(1)
	7356 ; (2)	7452;(2)	14565 ; (2)	14661;(2)
GRU	8156 ; (4)	8252;(4)	23973 ; <i>(3)</i>	16197 ; (4)
GRU	12060 ; <i>(3)</i>	12156;(3)	16101;(4)	24069 ; <i>(3)</i>
	26780;(5)	26876;(5)	53349;(5)	53445 ; (5)
	45404 ; (6)	45500;(6)	90597 ; (6)	90693 ; (6)
	9329;(3)	9425 ; (3)	13971 ; <i>(3)</i>	14067;(3)
	20118 ; (6)	20214;(6)	24065 ; (6)	24161 ; (6)
tCNN	26724 ; (2)	26820;(2)	29525;(2)	29621;(2)
tertit	54508 ; (5)	54604;(5)	46853;(5)	46949;(5)
	102876;(1)	102972;(1)	81349;(1)	81445 ; (1)
	205532;(4)	205628;(4)	133541;(4)	133637;(4)
	105300;(1)	105396;(1)	114735;(1)	114831;(1)
	107412;(2)	107508;(2)	118959;(2)	119055 ; (2)
dTCN	109524;(3)	109620;(3)	123183 ; <i>(3)</i>	123279;(3)
uren	112580 ; (4)	112676;(4)	129519;(4)	129615 ; (4)
	120900;(5)	120996;(5)	146159;(5)	146255 ; (5)
	129220;(6)	129316;(6)	162799 ; (6)	162895 ; (6)
		TYPE CF 3292; (1) 9564; (2) 10460; (4) 15836; (3) 35292; (5) 60124; (6) 60124; (6) 2652; (1) 7356; (2) 8156; (4) 12060; (3) 26780; (5) 26780; (5) 26780; (5) 12060; (3) 20118; (6) 26724; (2) 54508; (5) 102876; (1) 205532; (4) dTCN 105300; (1) 107412; (2) 109524; (3) 112580; (4) 120900; (5)	C_F C_{Fmeta} 3292 ; (1) 3388 ; (1) 9564 ; (2) 9660 ; (2) 10460 ; (4) 10556 ; (4) 15836 ; (3) 15932 ; (3) 35292 ; (5) 35388 ; (5) 60124 ; (6) 60220 ; (6) 2652 ; (1) 2748 ; (1) 7356 ; (2) 7452 ; (2) 8156 ; (4) 8252 ; (4) 12060 ; (3) 12156 ; (3) 26780 ; (5) 26876 ; (5) 45404 ; (6) 45500 ; (6) 20118 ; (6) 20214 ; (6) 26724 ; (2) 26820 ; (2) 54508 ; (5) 54604 ; (5) 102876 ; (1) 102972 ; (1) 20532 ; (4) 20528 ; (4) 205532 ; (4) 205628 ; (4) 4TCN 105300 ; (1) 105306 ; (1) 107412 ; (2) 107508 ; (2) 10524 ; (3) 109620 ; (3) 112580 ; (4) 112676 ; (4)	TYPE c_F $c_{F,meta}$ d_F TYPE3292;(1)3388;(1)6661;(1)9564;(2)9660;(2)19205;(2)10460;(4)10556;(4)21157;(4)15836;(3)15932;(3)31749;(3)35292;(5)35388;(5)70821;(5)60124;(6)60220;(6)120485;(6)2652;(1)2748;(1)5157;(1)7356;(2)7452;(2)14565;(2)8156;(4)8252;(4)23973;(3)12060;(3)12156;(3)16101;(4)26780;(5)26876;(5)53349;(5)45404:(6)45500;(6)90597;(6)20118;(6)20214;(6)24065;(6)26724;(2)26820;(2)29525;(2)54508;(5)54604;(5)46853;(5)102876;(1)102972;(1)81349;(1)20532;(4)20528;(4)133541;(4)dTCN1105300;(1)105396;(1)114735;(1)107412;(2)107508;(2)118959;(2)10524;(3)109620;(3)123183;(3)112580;(4)112676;(4)129519;(4)120900;(5)120996;(5)146159;(5)

	Network	C _F	C _{F,meta}	d_F	$d_{F,meta}$
	TYPE	C _F	C F,meia	u _r	∝r,meia
		6364;(1)	6460;(1)	13110;(1)	13206;(1)
		18908;(2)	19004 ; (2)	38198;(2)	38294 ; (2)
	LSTM	20700;(4)	20796;(4)	42102;(4)	42198;(4)
	20111	31452;(3)	31548 ; <i>(3)</i>	63286 ; <i>(3)</i>	63382;(3)
		70364;(5)	70460;(5)	141430;(5)	141526;(5)
		120028;(6)	120124 ; (6)	240758;(6)	240854;(6)
		5084;(1)	5180;(1)	10102;(1)	10198;(1)
id		14492;(2)	14588;(2)	28918;(2)	29014;(2)
3 hybr	GRU	16092;(4)	16188 ; (4)	31990;(4)	32086;(4)
- RI	GRO	23900;(3)	23996;(3)	47734 ; <i>(3)</i>	47830;(3)
OH		53340;(5)	53436 ; (5)	106486 ; (5)	106582;(5)
MACHO - RBhybrid		90588;(6)	90684;(6)	180982 ; (6)	181078;(6)
1		10438;(3)	10534;(3)	16530 ; <i>(3)</i>	16626;(3)
		24016;(6)	24112;(6)	31638 ; (2)	31734 ; (2)
	tCNN	27628;(2)	27724;(2)	32718;(6)	32814;(6)
		57596;(5)	57692;(5)	53494 ; (5)	53590;(5)
		103132;(1)	103228;(1)	82486;(1)	82582;(1)
		206044;(4)	206140;(4)	135670;(4)	135766;(4)
		107980;(1)	108076;(1)	120458;(1)	120554 ; (1)
		112204 ; (2)	112300;(2)	128906 ; (2)	129002;(2)
	dTCN	116428;(3)	116524;(3)	137354 ; (3)	137450;(3)
	uicit	122540;(4)	122636 ; (4)	150026 ; (4)	150122;(4)
		139180 ; (5)	139276 ; (5)	183306 ; (5)	183402 ; (5)
		155820;(6)	155916 ; (6)	216586 ; (6)	216682;(6)

E. GLOBAL PERFORMANCES

				LS	ТМ					Gl	RU					tC	NN					dT	CN		
		(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)
hand	c _F	1.04	2.59	2.64	0.24	2.75	4.25	0.83	2.27	2.28	0.78	2.67	4.42	0.02	0.04	0.09	0.03	0.05	0.11	0.09	0.15	0.24	0.15	0.25	0.37
0 - B ₁	c _{F,meta}	0.78	2.08	3.45	1.00	3.12	5.19	0.62	1.84	2.42	0.83	2.75	4.02	0.06	0.08	0.09	0.04	0.06	0.14	0.17	0.16	0.27	0.17	0.31	0.48
MACHO	d _F	2.24	5.51	7.05	2.42	7.78	6.06	1.54	4.59	5.79	2.51	6.28	8.54	0.08	0.16	0.19	0.23	0.35	0.23	0.59	0.66	0.75	0.99	1.27	1.58
W	d _{F,meta}	1.80	5.56	8.60	2.91	7.94	12.76	1.50	3.72	7.78	1.99	4.79	8.55	0.10	0.13	0.22	0.23	0.32	0.45	0.42	0.86	0.90	0.83	2.91	4.61
erged	c _F	0.58	1.76		0.69	2.55	9.45	1.53	3.61	1.47	1.02	4.05	9.24	0.02	0.04	0.15	0.02	0.05	0.09	0.11	0.16	0.27	0.24	0.33	0.46
LRB "	c _{F,meta}	1.28	4.18		2.00	6.04	8.06	1.57	4.40	6.98	1.76	6.65	9.02	0.02	0.04	0.16	0.02	0.05	0.08	0.12	0.19	0.27	0.21	0.37	0.64
CHO	d _F	3.70	8.68	8.96	1.20	12.98	17.70	3.00	7.04	14.05	4.69	12.85	13.05	0.25	0.32	0.43	0.31	0.31	0.55	0.74	1.21	1.68	1.54	2.47	2.62
MA	d _{F,meta}	4.31	10.88	14.04	4.71	13.03	20.75	3.81	9.37	11.93	3.86	13.31	17.99	0.28	0.35	0.38	0.36	0.49	0.86	0.76	2.61	4.82	1.50	5.10	9.33
hybrid	c _F	0.36	1.92	2.09	0.58	4.53	6.31	0.98	2.82	4.70	1.46	3.29	6.01	0.03	0.04	0.11	0.04	0.07	0.12	0.15	0.24	0.26	0.26	0.38	0.52
- RB	c _{F,meta}	1.28	3.37	5.79	1.73	5.41	9.26	1.08	3.26	5.39	1.42	5.02	7.63	0.04	0.05	0.15	0.06	0.06	0.18	0.15	0.22	0.26	0.25	0.41	0.53
CHO	d _F	2.94	6.55	11.40	4.51	12.40	13.07	2.94	6.16	9.30	3.28	9.63	8.82	0.17	0.15	0.34	0.17	0.36	0.40	0.47	0.53	1.05	2.36	2.43	1.87
MA	d _{F,meta}	3.17	3.80	12.65	4.43	11.23	12.74	2.38	5.59	8.51	3.57	9.65	17.65	0.17	0.12	0.49	0.22	0.33	0.28	0.59	0.88	1.87	1.15	1.36	2.24

Table E1. Training convergence time (expressed in hours) of all models across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]). Runs are performed on a CPU model Intel Xeon E5-2643v3 using 4 cores per run at maximum capacity. The identifiers of the hyperparameters set configurations (1) to (6) are stated in the Appendix Table D2.

Table E2. Hyperparameters set configurations identified for the best-performing networks based on minimum loss obtained on the Test set across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]). The identifiers (1) to (6) are stated in the Appendix Table D2.

pu	Id net	LSTM	GRU	tCNN	dTCN
MACHO - B _{band}	c_F	(6)	(6)	(3)	(1)
- ОН	$c_{F,meta}$	(1)	(5)	(3)	(1)
IACI	d_F	(5)	(5)	(4)	(4)
W	$d_{F,meta}$	(6)	(4)	(5)	(1)
rged	Id net	LSTM	GRU	tCNN	dTCN
MACHO - RBmerged	CF	(6)	(6)	(3)	(3)
9-Y	CF,meta	(1)	(5)	(2)	(1)
CHI	d_F	(5)	(5)	(5)	(5)
MA	$d_{F,meta}$	(6)	(4)	(6)	(4)
brid	Id net	LSTM	GRU	tCNN	dTCN
Bhy	C_F	(5)	(3)	(3)	(1)
MACHO - RB _{hybrid}	CF,meta	(3)	(2)	(6)	(1)
NCH	d_F	(5)	(5)	(5)	(4)
MA	$d_{F,meta}$	(5)	(1)	(4)	(4)

Table E3. Classification accuracy evaluated on the Test set for the best-performing networks (see text for a description) across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]). The classification accuracy is evaluated for the three main variability groups: short-period pulsators (group 1), eclipsing binaries (group 2) and LPVs (group 3).

	Id net		LS	STM			G	RU			tC	CNN			ď	ГCN	
band	ID NET	Full	Group1	Group2	Group3												
) - B	c_F	0.749	0.819	0.802	0.428	0.781	0.834	0.831	0.520	0.732	0.811	0.797	0.359	0.675	0.765	0.752	0.247
CHC	$c_{F,meta}$	0.916	0.936	0.886	0.879	0.907	0.924	0.905	0.850	0.887	0.909	0.890	0.801	0.786	0.807	0.868	0.608
MA	d_F	0.730	0.798	0.787	0.407	0.739	0.811	0.772	0.431	0.701	0.781	0.760	0.337	0.689	0.782	0.777	0.239
	$d_{F,meta}$	0.905	0.930	0.887	0.833	0.886	0.943	0.907	0.652	0.900	0.929	0.838	0.870	0.802	0.848	0.819	0.611

p	Id net		LS	STM			G	RU			tC	CNN			dT	ſCN	
merge	ID NET	Full	Group1	Group2	Group3												
RB	c_F	0.737	0.808	0.755	0.455	0.780	0.834	0.819	0.532	0.722	0.794	0.785	0.379	0.667	0.729	0.768	0.315
ОН	$c_{F,meta}$	0.890	0.913	0.856	0.845	0.910	0.933	0.888	0.852	0.815	0.848	0.805	0.707	0.747	0.783	0.772	0.582
IAC	d_F	0.726	0.810	0.771	0.364	0.738	0.813	0.779	0.412	0.691	0.770	0.774	0.298	0.686	0.769	0.762	0.290
V	d _{F,meta}	0.906	0.924	0.896	0.854	0.883	0.938	0.907	0.653	0.912	0.935	0.894	0.848	0.814	0.856	0.864	0.594

P	Id net		LS	STM			G	RU			tC	CNN			ď	ΓCN	
hybrid	ID REI	Full	Group1	Group2	Group3												
- RB	c_F	0.776	0.841	0.809	0.495	0.789	0.852	0.808	0.535	0.744	0.821	0.779	0.412	0.696	0.768	0.755	0.359
ОН	$c_{F,meta}$	0.917	0.935	0.914	0.857	0.905	0.919	0.892	0.867	0.845	0.858	0.866	0.768	0.768	0.801	0.816	0.588
IAC	d_F	0.748	0.819	0.789	0.434	0.749	0.821	0.772	0.456	0.706	0.788	0.779	0.311	0.726	0.803	0.777	0.379
V	d _{F,meta}	0.905	0.921	0.894	0.859	0.880	0.939	0.890	0.648	0.904	0.933	0.881	0.825	0.818	0.873	0.872	0.545

Table E4. Classification metrics evaluated on the Test set for the best-performing networks (see text for a description) across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]).

Τ	Id net		LSTM			GRU			tCNN			dTCN	
L		$Precision_M$	Recall_M	F1-score _M	Precision _M	Recall_M	F1-score _M	Precision _M	Recall_M	F1-score _M	Precision _M	Recall_M	F1-score _M
	C_F	0.503	0.515	0.504	0.559	0.564	0.552	0.510	0.487	0.488	0.447	0.424	0.425
	C _{F,meta}	0.771	0.800	0.784	0.763	0.780	0.770	0.744	0.753	0.748	0.642	0.599	0.609
ſ	d_F	0.477	0.497	0.484	0.500	0.504	0.500	0.459	0.452	0.454	0.446	0.418	0.426
	$d_{F,meta}$	0.765	0.774	0.768	0.679	0.705	0.689	0.748	0.796	0.768	0.597	0.627	0.603

p	Id net		LSTM			GRU			tCNN			dTCN	
merged	ID NEI	Precision _M	Recall _M	F1-score _M	Precision _M	Recall_M	F1-score _M	Precision _M	Recall _M	F1-score _M	Precision _M	Recall _M	F1-score _M
- RB	CF	0.504	0.519	0.507	0.539	0.567	0.548	0.472	0.483	0.474	0.373	0.389	0.380
HO.	$C_{F,meta}$	0.744	0.757	0.749	0.759	0.794	0.775	0.667	0.673	0.668	0.565	0.566	0.562
IAC.	d_F	0.481	0.475	0.477	0.499	0.498	0.496	0.450	0.423	0.433	0.444	0.431	0.435
V	$d_{F,meta}$	0.773	0.778	0.774	0.677	0.702	0.687	0.765	0.788	0.776	0.614	0.627	0.619

id	Id net		LSTM			GRU			tCNN			dTCN	
tybr	ID NET	Precision _M	Recall_M	F1-score _M									
- RB	c_F	0.561	0.559	0.549	0.564	0.570	0.563	0.520	0.520	0.518	0.468	0.480	0.470
ЮН	$C_{F,meta}$	0.784	0.790	0.785	0.770	0.785	0.776	0.704	0.691	0.694	0.615	0.600	0.606
IAC	d_F	0.505	0.518	0.508	0.516	0.522	0.516	0.457	0.443	0.447	0.478	0.481	0.478
A.	$d_{F,meta}$	0.763	0.783	0.772	0.671	0.708	0.688	0.747	0.774	0.758	0.534	0.578	0.551

Table E5. Classification metrics computed on the Test set for the best-performing LSTM direct classifiers c_F and $c_{F,meta}$ on the B-band.

							Netw	ork c _F ; LSTM	best configur	cation (6); B _{ban}
	Classes $\{i\}_{i=1 \to N_C}$	NB OF \mathbf{Y}_{true} (in counts)	Nв оF Y _{pred} (in counts)	TP(i)	FN(i)	FP(i)	TN(i)	Precision(i)	Recall(<i>i</i>)	F1-score(i)
Í	RRL (type ab)	1430	1574	1370	60	204	1890	0.870	0.958	0.912
4	RRL (type c)	344	333	172	172	161	3019	0.517	0.500	0.508
\boldsymbol{B}_{band}	RRL (type e)	60	0	0	60	0	3464	_	-	-
	CEP (FU)	229	202	174	55	28	3267	0.861	0.760	0.807
MACHO	CEP (FO)	133	153	82	51	71	3320	0.536	0.617	0.573
MAG	LPV (Wood seq. A)	62	0	0	62	0	3462	_	-	-
~	LPV (Wood seq. B)	160	289	87	73	202	3162	0.301	0.544	0.388
	LPV (Wood seq. C)	220	164	64	156	100	3204	0.390	0.291	0.333
	LPV (Wood seq. D)	152	158	103	49	55	3317	0.652	0.678	0.665
	Eclipsing binaries	734	651	589	145	62	2728	0.905	0.802	0.851
	$N_{C} = 10$	$N_s = 3524$					Accuracy	PRECISION _M	RECALL _M	F1-score _M
							0.749	0.503	0.515	0.504

Network cF,meta; LSTM; best configuration (1); Bband

	Classes $\{i\}_{i=1 \to N_C}$	NB OF \mathbf{Y}_{true} (in counts)	Nв оf Y _{pred} (in counts)	TP(i)	FN(i)	FP(i)	TN(i)	Precision(i)	Recall(i)	F1-score(i)
	RRL (type ab)	1430	1460	1422	8	38	2056	0.974	0.994	0.984
p	RRL (type c)	344	388	316	28	72	3108	0.814	0.919	0.863
B_{band}	RRL (type e)	60	0	0	60	0	3464	-	-	-
	CEP (FU)	229	232	204	25	28	3267	0.879	0.891	0.885
МАСНО	CEP (FO)	133	141	113	20	28	3363	0.801	0.850	0.825
NAG	LPV (Wood seq.A)	62	65	49	13	16	3446	0.754	0.790	0.772
	LPV (Wood seq. B)	160	157	131	29	26	3338	0.834	0.819	0.826
	LPV (Wood seq. C)	220	230	195	25	35	3269	0.848	0.886	0.867
	LPV (Wood seq. D)	152	175	147	5	28	3344	0.840	0.967	0.899
	Eclipsing binaries	734	676	650	84	26	2764	0.962	0.886	0.922
	$N_{C} = 10$	$N_s = 3524$					Accuracy	PRECISION _M	RECALLM	F1-score _M
							0.916	0.771	0.800	0.784

Table E6. Classification metrics computed on the Test set using the metadata via the classifier module.

								Network classi	fier module (1	MLP); metadata
	Classes $\{i\}_{i=1 \to N_C}$	NB OF \mathbf{Y}_{true} (in counts)	NB OF \mathbf{Y}_{pred} (in counts)	TP(i)	FN(i)	FP(i)	TN(i)	Precision(i)	Recall(i)	F1-score(i)
	RRL (type <i>ab</i>)	1430	1457	1414	16	43	2051	0.970	0.989	0.980
ata	RRL (type c)	344	397	323	21	74	3106	0.814	0.939	0.872
metadata	RRL (type <i>e</i>)	60	0	0	60	0	3464	_	-	_
- <i>m</i> e	CEP (FU)	229	254	213	16	41	3254	0.839	0.930	0.882
OF	CEP (FO)	133	114	95	38	19	3372	0.833	0.714	0.769
MACHO	LPV (Wood seq. A)	62	50	42	20	8	3454	0.840	0.677	0.750
M	LPV (Wood seq. B)	160	265	158	2	107	3257	0.596	0.988	0.744
	LPV (Wood seq. C)	220	0	0	220	0	3304	_	-	_
	LPV (Wood seq. D)	152	0	0	152	0	3372	-	-	-
	Eclipsing binaries	734	987	686	48	301	2489	0.695	0.935	0.797
	$N_{C} = 10$	$N_s = 3524$					Accuracy	PRECISION _M	RECALLM	F1-score _M
							0.832	0.559	0.617	0.579

Table E7. Total loss (weighted MAE for reconstruction and categorical cross-entropy for classification) computed for all trained models across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]). Solid underlines highlight to the best-performing models associated to minimum loss obtained on the Test set. The identifiers (1) to (6) refer to the hyperparameters set configurations.

					LS	ГМ					Gl	RU					tC	NN					dT	CN		
			(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)
		c _F	0.76	0.73	0.74	0.90	0.68	0.67	0.98	0.66	0.71	0.74	0.58	0.53	0.79	0.71	0.72	0.80	0.67	0.70	0.74	0.52	0.66	0.53	0.60	0.44
		F,meta	0.22	2.57	1.86	0.89	0.89	0.89	0.89	0.90	0.31	0.27	0.23	0.24	0.24	0.20	0.25	0.32	0.29	0.87	0.40	0.21	0.29	0.27	0.19	0.20
		d _F	8.08	7.83	7.85	7.62	7.55	7.60	8.17	8.16	7.96	7.69	7.55	7.52	7.72	7.65	8.03	7.54	7.69	7.97	7.29	7.31	7.49	7.15	7.91	7.36
	d _{F,}	F,meta	8.99	7.87	7.91	9.01	7.64	6.88	8.82	8.19	9.47	7.77	7.78	7.84	8.87	7.12	7.32	8.72	7.02	7.12	7.64	8.00	7.94	7.67	15.50	10.50
band	130	c _F	0.77	0.76	0.75	0.92	0.72	0.71	0.98	0.68	0.72	0.75	0.62	0.63	0.92	0.83	0.80	0.94	0.81	0.81	1.00	1.04	0.99	1.03	1.09	1.14
		F,meta	0.24	2.59	1.88	0.91	0.91	0.91	0.90	0.92	0.34	0.29	0.27	0.30	0.42	0.35	0.32	0.51	0.45	1.00	0.60	0.71	0.64	0.61	0.83	0.90
MACHU-E		d _F	7.89	7.75	7.79	7.54	7.50	7.58	7.98	8.06	7.80	7.54	7.48	7.49	7.80	7.67	7.92	7.61	7.73	7.90	7.59	7.45	7.63	7.44	8.10	7.59
W	d _F	F,meta	8.87	7.79	7.85	8.89	7.60	6.86	8.67	8.06	9.33	7.69	7.71	7.81	8.92	7.12	7.26	8.82	7.04	7.07	7.77	8.18	8.09	7.80	15.13	10.37
		c _F	0.80	0.78	0.78	0.95	0.76	0.74	1.02	0.73	0.79	0.79	0.68	0.65	0.93	0.85	0.82	0.96	0.86	0.83	1.03	1.07	1.06	1.10	1.12	1.21
	c _{F,}	F,meta	0.25	2.60	1.90	0.93	0.94	0.94	0.92	0.95	0.36	0.30	0.28	0.33	0.43	0.39	0.35	0.51	0.46	1.00	0.60	0.70	0.65	0.62	0.89	0.92
Tree	3	d _F	8.07	7.85	7.86	7.67	7.60	7.67	8.14	8.17	7.98	7.75	7.60	7.61	7.88	7.74	8.06	7.72	7.84	7.98	7.64	7.58	7.74	7.53	8.21	7.65
	d _F	F,meta	8.99	7.91	7.98	9.05	7.70	6.97	8.82	8.18	9.43	7.81	7.86	7.91	9.06	7.22	7.33	8.91	7.15	7.19	7.86	8.26	8.18	7.89	15.31	10.56

					LS	ГМ					GI	RU					tC	NN					dT	CN		
			(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)
	,	c _F	1.20	1.01	0.75	1.22	0.72	0.68	0.76	0.66	1.10	0.77	0.60	0.56	0.59	0.56	0.64	0.72	0.57	0.61	0.44	0.43	0.43	0.42	0.32	0.13
	N SET	c _{F,meta}	0.32	2.58	1.88	0.91	0.89	0.94	0.90	0.89	0.26	0.33	0.22	0.23	0.22	0.26	0.85	0.29	0.22	0.35	0.20	0.17	0.12	0.15	0.10	0.04
	TRAIN	d _F	10.98	10.66	11.04	12.34	10.23	10.48	11.02	11.04	11.85	10.45	10.32	10.80	10.08	10.27	10.77	9.99	10.14	10.54	9.61	9.68	10.17	9.37	9.34	9.77
		d _{F,meta}	12.06	10.96	11.00	11.94	10.50	9.75	11.80	10.93	12.79	10.53	10.55	10.69	11.20	9.65	10.16	11.26	9.51	9.73	9.91	18.73	18.72	9.77	18.66	18.59
merged	SET	c _F	1.19	1.01	0.75	1.23	0.74	0.71	0.76	0.68	1.09	0.76	0.64	0.62	1.16	0.92	0.82	1.15	0.94	0.81	1.27	1.39	1.21	1.34	1.53	2.18
RB		c _{F,meta}	0.32	2.59	1.91	0.93	0.91	0.94	0.91	0.91	0.30	0.34	0.25	0.29	0.81	0.51	1.01	0.78	0.62	0.52	0.95	1.02	1.17	1.05	1.13	1.54
CHO	LIDATION	d _F	10.44	10.14	10.51	11.62	9.91	10.13	10.44	10.48	11.27	9.97	9.88	10.32	10.47	10.24	10.45	10.37	10.24	10.36	10.16	10.12	10.41	10.03	10.02	10.13
MAC	VA	d _{F,meta}	11.48	10.42	10.50	11.46	10.18	9.43	11.26	10.45	12.26	10.04	10.18	10.27	11.52	9.65	9.84	11.59	9.61	9.61	10.30	17.91	17.91	10.16	17.89	17.86
		c _F	1.21	1.04	0.80	1.24	0.77	0.75	0.79	0.73	1.15	0.79	0.69	0.67	1.23	0.97	0.87	1.21	1.00	0.87	1.38	1.46	1.26	1.44	1.60	2.36
	TSET	c _{F,meta}	0.34	2.61	1.92	0.94	0.94	0.96	0.93	0.94	0.31	0.37	0.27	0.31	0.81	0.55	1.05	0.80	0.65	0.55	0.99	1.10	1.24	1.10	1.19	1.58
	TEST	d _F	10.86	10.57	11.06	12.21	10.29	10.54	10.90	10.94	11.73	10.39	10.27	10.74	10.80	10.59	10.78	10.71	10.55	10.71	10.41	10.41	10.75	10.35	10.28	10.45
		d _{F,meta}	11.96	10.90	11.00	11.89	10.53	9.79	11.69	10.86	12.69	10.48	10.55	10.64	11.85	10.00	10.10	11.93	9.92	9.92	10.57	18.14	18.15	10.46	18.10	18.11

					LS	ТМ					GI	RU					tC	NN					dT	CN		
			(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)
	,	$c_{\rm F}$	1.15	0.70	0.78	0.88	0.55	0.60	0.69	0.63	0.57	0.60	0.54	0.48	0.69	0.61	0.62	0.87	0.63	0.56	0.53	0.48	0.34	0.47	0.27	0.37
	N SET	c _{F,meta}	0.90	0.92	0.23	1.17	0.27	0.90	0.94	0.24	0.90	0.29	0.87	0.90	0.29	0.26	0.92	0.37	0.33	0.26	0.17	0.11	0.15	0.13	0.06	0.07
	TRAIN	d _F	19.88	19.79	19.09	18.57	18.41	18.60	19.79	19.85	19.96	18.69	18.21	19.16	18.32	18.90	19.66	18.69	18.43	18.85	18.08	18.41	18.34	16.86		18.39
		d _{F,meta}	20.10	22.06	20.15	20.34	17.95	19.69	19.72	21.92	21.18	19.76	20.12	19.77	17.99	19.25	19.01		18.61	19.23	18.45	19.92	26.67	17.99	18.79	29.38
hybrid	SET	$c_{\rm F}$	1.17	0.70	0.79	0.89	0.62	0.63	0.70	0.65	0.61	0.63	0.61	0.59	0.91	0.77	0.74	1.00	0.85	0.76	1.00	0.98	1.16	1.11	1.32	1.22
- RB _{III}		c _{F,meta}	0.92	0.93	0.26	1.20	0.30	0.93	0.95	0.27	0.94	0.30	0.92	1.00	0.52	0.48	1.05	0.60	0.53	0.45	0.79	0.82	0.92	0.94	1.14	1.20
CHO	NOLLEVI	d _F	18.72	18.65	18.15	17.61	17.59	17.82	18.66	18.84	18.97	17.68	17.41	18.19	17.92	18.13	18.68	18.21	17.91	17.96	17.85	17.93	17.96	17.11	17.35	18.08
MAG	VA	d _{F,meta}	18.94	20.71	19.26	19.41	17.17	18.89	18.59	20.89	20.13	18.79	19.30	18.91	17.58	18.49	18.12	17.38	18.05	18.38	18.20	19.60	25.99	17.93	18.64	28.26
		$c_{\rm F}$	1.20	0.75	0.83	0.94	0.68	0.69	0.73	0.70	0.65	0.67	0.67	0.66	0.94	0.82	0.79	1.01	0.89	0.80	1.04	1.04	1.26	1.11	1.40	1.25
	SET	c _{F,meta}	0.93	0.97	0.27	1.21	0.31	0.95	0.98	0.29	0.97	0.32	0.94	1.04	0.56	0.48	1.07	0.62	0.54	0.48	0.81	0.87	0.98	0.91	1.07	1.21
	TEST	d _F	19.49	19.60	18.89	18.36	18.30	18.51	19.45	19.55	19.72	18.52	18.12	18.99	18.65	18.86	19.34	18.98	18.53	18.70	18.47	18.65	18.66	17.78	18.03	18.75
		d _{F,meta}	19.74	21.72	19.98	20.11	17.83	19.59	19.36	21.62	20.92	19.59	20.00	19.72	18.32	19.22	18.85	18.06	18.74	19.00	18.95	20.36	26.67	18.56	19.19	28.71

Table E8. Classification accuracy, defined as the fraction of true positives within the sample, computed for all trained models across three different datasets (B-band only [top], and two variants of the combination of R- and B-bands [middle and bottom]). Solid underlines highlight the best-performing models associated to minimum loss obtained on the Test set. The identifiers (1) to (6) refer to the hyperparameters set configurations.

				L	STM					G	RU					tC	NN					dT	CN		
		(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)
	c _F	0.746	0.753	0.750	0.694	0.766	0.772	0.703	0.776	0.754	0.749	0.806	0.819	0.741	0.762	0.756	0.728	0.777	0.766	0.756	0.834	0.775	0.832	0.806	0.849
Let Let	c _{F,meta}	0.928	0.803	0.843	0.894	0.892	0.888	0.890	0.891	0.899	0.913	0.925	0.919	0.923	0.936	0.923	0.896	0.903	0.900	0.854	0.937	0.904	0.914	0.946	0.934
D AIN	d _F	0.726	0.726	0.723	0.733	0.743	0.732	0.722	0.722	0.738	0.744	0.747	0.745	0.701	0.712	0.710	0.718	0.719	0.685	0.719	0.708	0.687	0.721	0.707	0.693
	d _{F,meta}	0.845	0.884	0.885		0.874	0.914	0.855	0.878	0.811	0.895	0.865	0.875	0.836	0.896	0.916	0.847	0.907	0.915	0.816	0.852	0.824	0.821	0.872	0.862
band	c _F	0.74	0.747	0.750	0.697	0.761	0.766	0.703	0.780	0.760	0.758	0.788	0.795	0.712	0.728	0.734	0.688	0.742	0.739	0.683	0.689	0.687	0.703	0.679	0.694
		0.919	0.794	0.835	0.888	0.885	0.879	0.888	0.879	0.893	0.906	0.913	0.892	0.860	0.884	0.896	0.838	0.848	0.854	0.791	0.783	0.799	0.801	0.767	0.755
MACHO-B Validation	d _F	0.727	0.733	0.728	0.732	0.741	0.731	0.718	0.725	0.737	0.747	0.749	0.753	0.691	0.709	0.707	0.708	0.711	0.691	0.690	0.694	0.678	0.693	0.687	0.670
	d _{F,meta}	0.834	0.881	0.877		0.874	0.908	0.848	0.876	0.802	0.887	0.865	0.870	0.827	0.896	0.912	0.841	0.900	0.914	0.813	0.846			0.867	0.857
	c _F	0.736	0.741	0.738	0.686	0.745	0.749	0.687	0.757	0.727	0.737	0.779	0.781	0.699	0.723	0.732	0.691	0.723	0.726	0.675	0.683	0.679	0.687	0.673	0.690
Las.	c _{F,meta}	0.916	0.796		0.881	0.881	0.873	0.881	0.875	0.882	0.907	0.907	0.889	0.865	0.871	0.887	0.833	0.846	0.856	0.786	0.780	0.789	0.800	0.757	0.745
Treat	d _F	0.716	0.717	0.719	0.724	0.730	0.716	0.710	0.717	0.730	0.737	0.739	0.734	0.684	0.698	0.700	0.701	0.710	0.680	0.691	0.685	0.678	0.689	0.686	0.674
	d _{F,meta}	0.835	0.874	0.877	0.831	0.867	0.905	0.844	0.871	0.806	0.886	0.852	0.867	0.825	0.886	0.911	0.838	0.900	0.912	0.802	0.840	0.812	0.808	0.871	0.853

			LSTM						GRU						tCNN							dTCN					
			(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	
		$c_{\rm F}$	0.618	0.636	0.749	0.629	0.758	0.766	0.743	0.772	0.619	0.738	0.796	0.810	0.814	0.818	0.789	0.768	0.811	0.797	0.856	0.850	0.850	0.871	0.902	0.958	
	N SET	c _{F,meta}	0.901	0.801	0.839	0.888	0.891	0.876	0.885	0.888	0.910	0.894	0.928	0.920	0.938	0.921	0.905	0.918	0.935	0.887	0.936	0.948	0.963	0.950	0.974	0.991	
	FRAIN	d _F	0.718	0.719	0.696	0.638	0.740	0.746	0.705	0.694	0.704	0.742	0.747	0.726	0.757	0.735	0.697	0.765	0.714	0.711	0.754	0.736	0.723	0.798	0.785	0.748	
		d _{F,meta}	0.846	0.885	0.886		0.877	0.915	0.854	0.885	0.809	0.892	0.872	0.874	0.844	0.918	0.911	0.845	0.910	0.922	0.835	0.871	0.863	0.841	0.876	0.864	
nerged	ATION SET	c _F	0.615	0.642	0.750	0.628	0.757	0.762	0.748	0.773	0.630	0.748	0.784	0.797	0.656	0.719	0.736	0.641	0.708	0.743	0.667	0.653	0.681	0.628	0.644	0.648	
RB		c _{F,meta}	0.898	0.797		0.882	0.889	0.872	0.879	0.878	0.903	0.890	0.920	0.897	0.759		0.853	0.745	0.805	0.827	0.764	0.741	0.749	0.735	0.725	0.737	
OH	LIDAT	d _F	0.728	0.725	0.696	0.646	0.744	0.748	0.710	0.707	0.712	0.749	0.753	0.737	0.717	0.719	0.708	0.717	0.709	0.715	0.703	0.690	0.700	0.715	0.697	0.709	
MAG	VA	d _{F,meta}	0.835	0.876	0.880		0.874	0.910	0.853	0.876	0.802	0.886	0.865	0.866	0.838	0.907	0.903		0.902	0.917	0.824	0.864	0.862		0.873	0.865	
	SET	$c_{\rm F}$	0.612	0.625	0.733	0.620	0.738	0.737	0.729	0.754	0.612	0.732	0.772	0.780	0.639	0.696	0.722	0.642	0.698	0.724	0.651	0.636	0.667	0.615	0.642	0.633	
		c _{F,meta}	0.890	0.791		0.879	0.876	0.868	0.877	0.875	0.892	0.881	0.910	0.889	0.752	0.815	0.848	0.732	0.785	0.821	0.747	0.733	0.728	0.719	0.731	0.717	
	TEST	d _F	0.708	0.708	0.691	0.631	0.726	0.730	0.696	0.684	0.685	0.733	0.738	0.709	0.700	0.709	0.690	0.706	0.691	0.698	0.688	0.683	0.685	0.693	0.686	0.691	
		d _{F,meta}	0.837	0.873	0.874	0.827	0.868	0.906	0.848	0.876	0.801	0.883	0.860	0.867	0.835	0.906	0.905	0.829	0.901	0.912	0.819	0.866	0.858	0.814	0.874	0.856	

			LSTM						GRU						tCNN							dTCN					
			(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	(1)	(2)	(3)	(4)	(5)	(6)	
		$c_{\rm F}$	0.606	0.762	0.734	0.685	0.809	0.793	0.770	0.783	0.807	0.799	0.812	0.837	0.771	0.799	0.796	0.709	0.796	0.815	0.835	0.841	0.891	0.845	0.902	0.872	
	N SET	c _{F,meta}	0.888	0.879	0.926	0.881	0.908	0.888	0.878	0.919	0.883	0.911	0.897	0.880	0.909	0.921	0.883	0.879	0.888	0.913	0.952	0.972	0.955	0.964	0.987	0.981	
	IRAIN	d _F	0.729	0.720	0.750	0.738	0.762	0.758	0.735	0.750	0.748	0.753	0.759	0.748	0.715	0.711	0.711	0.709	0.713	0.734	0.716	0.717	0.713	0.762	0.739	0.710	
		d _{F,meta}	0.885	0.820		0.805	0.919	0.844	0.888	0.801		0.846	0.807	0.844	0.921	0.823	0.858	0.915	0.850	0.829	0.835	0.810	0.831		0.787	0.800	
hybrid	SET	$c_{\rm F}$	0.603	0.765	0.734	0.686	0.791	0.786	0.767	0.778	0.793	0.788	0.790	0.808	0.725	0.758	0.761	0.675	0.737	0.753	0.708	0.702	0.693	0.684	0.694	0.686	
- RB	VALIDATION	c _{F,meta}	0.879	0.876	0.914	0.871	0.900	0.879	0.871	0.907	0.871	0.908	0.875	0.849	0.821	0.852	0.844	0.802	0.817	0.854	0.780	0.791	0.768	0.778	0.759	0.763	
OH		d _F	0.733	0.722	0.753	0.739	0.760	0.760	0.737	0.753	0.756	0.759	0.760	0.756	0.713	0.709	0.712	0.707	0.716	0.737	0.711	0.715	0.708	0.733	0.722	0.707	
MAG		d _{F,meta}	0.879	0.823	0.828	0.799	0.916	0.833	0.879	0.796	0.824		0.802	0.837	0.916	0.829	0.856	0.912	0.849	0.832	0.839	0.810	0.826	0.838	0.780	0.792	
		$c_{\rm F}$	0.591	0.750	0.721	0.673	0.776	0.763	0.755	0.760	0.789	0.774	0.778	0.786	0.706	0.740	0.744	0.673	0.712	0.744	0.696	0.690	0.682	0.686	0.682	0.678	
	SET	c _{F,meta}	0.881	0.865	0.917	0.872	0.893	0.875	0.867	0.905	0.862	0.902	0.879	0.839	0.813	0.847		0.790	0.814	0.845	0.768	0.777	0.745	0.758	0.764	0.759	
	TEST	d _F	0.719	0.713	0.741	0.733	0.748	0.749	0.729	0.743	0.740	0.743	0.749	0.738	0.708	0.694	0.704	0.694	0.706	0.720	0.703	0.707	0.698	0.726	0.717	0.700	
		d _{F,meta}	0.877	0.815	0.824	0.796	0.905	0.833	0.880	0.790	0.827		0.799	0.831	0.911	0.810	0.845	0.904		0.815	0.821	0.799	0.819	0.818	0.773	0.781	

Network d_F; LSTM; best configuration (5); **B**_{band}

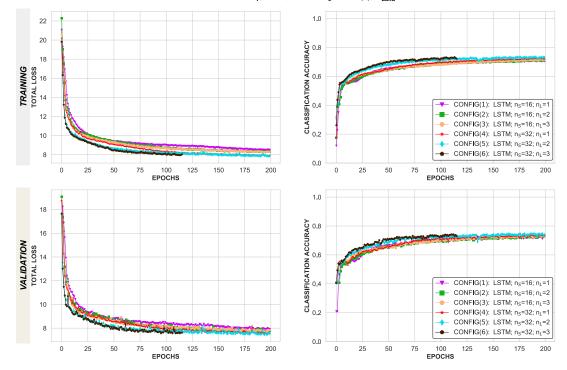
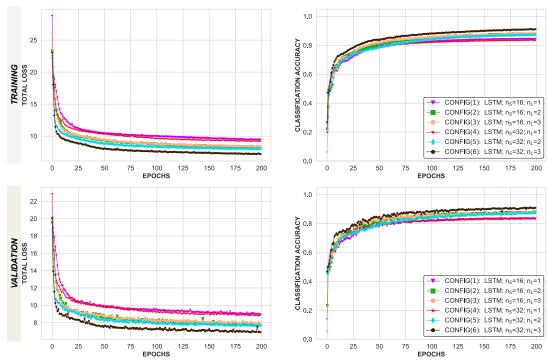
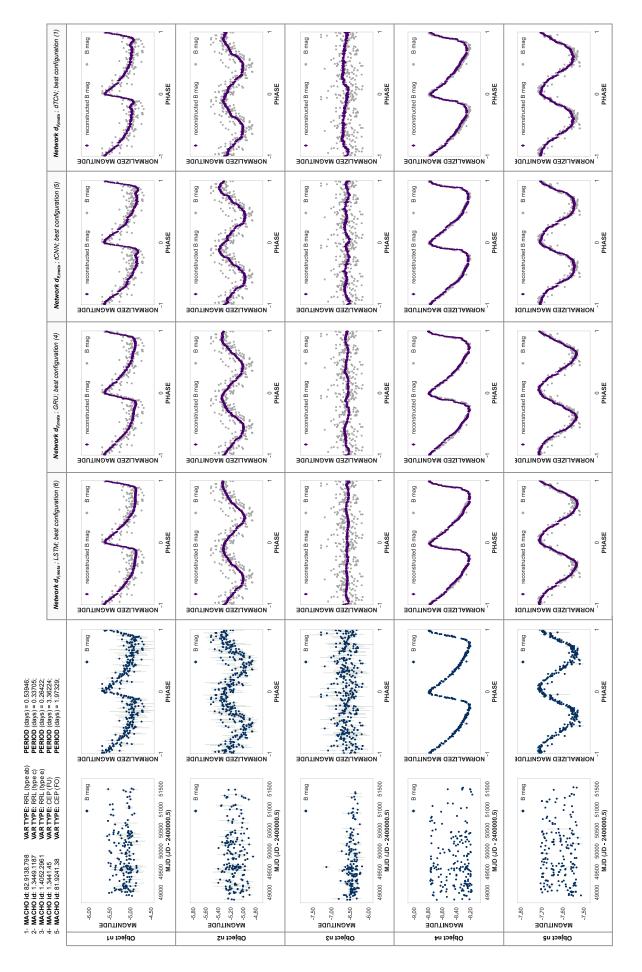


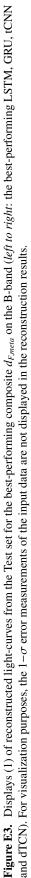
Figure E1. Total loss and classification accuracy for the LSTM composite d_F on the B-band.

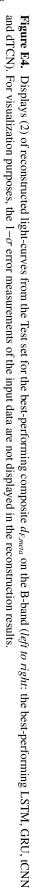


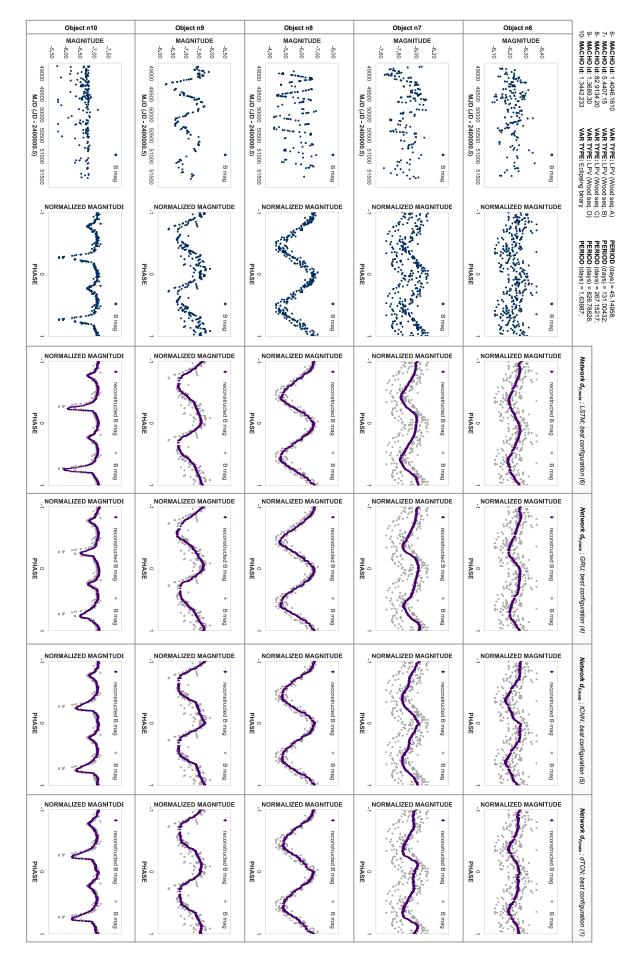
Network d_{F,meta}; LSTM; best configuration (6); B_{band}

Figure E2. Total loss and classification accuracy for the LSTM composite $d_{F,meta}$ using metadata as a secondary input on the B-band.









3.0 All datasets
 Test set 0.5 1.0 1.5 2.0 2.5 MODEL FIT RESIDUAL (SUPERSMOOTHER) Network d_{F,meta}; tCNN; best configuration (5); B_{band} All datasets
 Test set Network d_{F,meta}; dTCN; best configuration (1); B_{band} 0.0 RECONSTRUCTION ЕRROR (аveraged) 00.00 0.35 0.30 0.05 3.0 All datasets Test set 0.5 1.0 1.5 2.0 2.5 MODEL FIT RESIDUAL (SUPERSMOOTHER) Network d_{Fmeta}; GRU; best configuration (4); **B**_{band} RECONSTRUCTION ERROR (averaged) 0.35 0.05 00.00 0.30 0.0 0.10 0.15 00.00 0.35 0.05 0.30 0.25 0.20

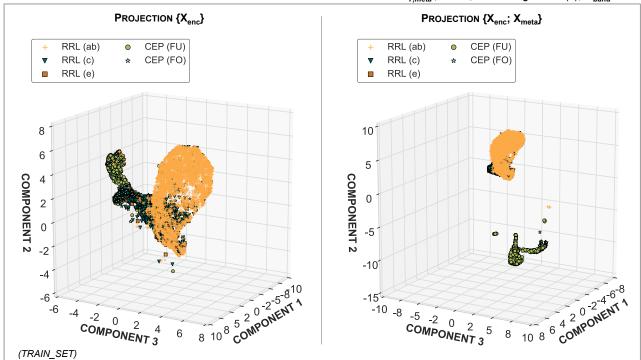
RECONSTRUCTION ERROR (averaged)

Figure E5. Reconstruction error (MAE) as a function of the model fit residuals from the SuperSmoother algorithm (Friedman 1984) for the best-performing GRU, tCNN [top, left to right] and dTCN [bottom] d_{F,meta} on the B-band. The highlighted numbers (1 to 10) refer to the subset of selected objects from the Test set used to showcase the reconstruction quality of the autoencoder branch.

3.0

0.5 1.0 1.5 2.0 2.5 MODEL FIT RESIDUAL (SUPERSMOOTHER)

0.0



Network d_{F,meta} ; LSTM; best configuration (6); B_{band}

Figure E6. 3-d representation of encoded features for the short-period pulsators in MACHO. The generated features from the best-performing LSTM composite network $d_{F,meta}$ on the B-band are projected into a reduced 3-d representation using the UMAP algorithm.

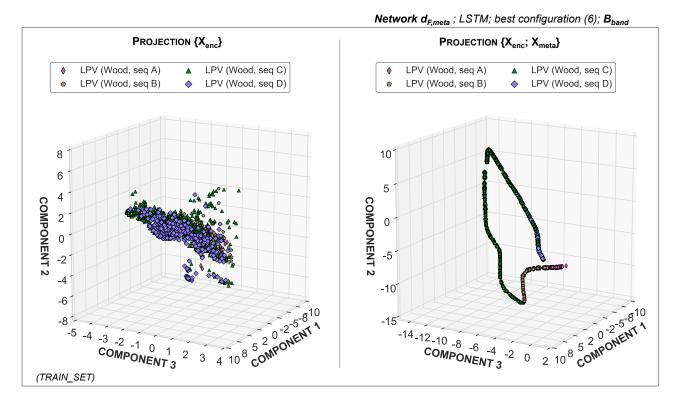


Figure E7. 3-d representation of encoded features for the LPVs in MACHO. The generated features from the best-performing LSTM composite network $d_{F,meta}$ on the B-band are projected into a reduced 3-d representation using the UMAP algorithm.

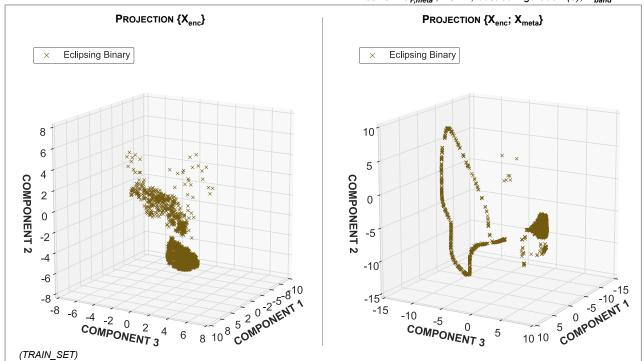


Figure E8. 3-d representation of encoded features for the eclipsing binaries in MACHO. The generated features from the best-performing LSTM composite network $d_{F,meta}$ on the B-band are projected into a reduced 3-d representation using the UMAP algorithm.

Network d_{F,meta}; LSTM; best configuration (6); B_{band}

Network c_{F,meta}; LSTM; best configuration (1); B_{band}

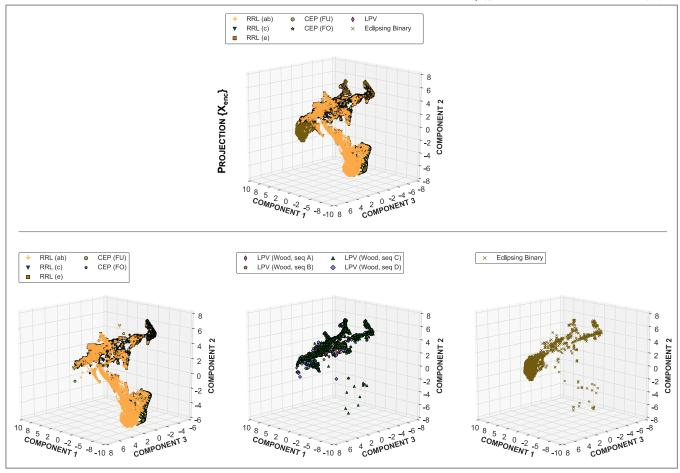


Figure E9. 3-d representation of encoded features for the best-performing LSTM direct classifier $c_{F,meta}$ on the B-band. Generated encodings are projected into a reduced 3-d representation using the UMAP algorithm.