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# Guided Mode Evolution and Ionization Injection in Meter-Scale Multi-GeV Laser Wakefield Accelerators

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We show that multi-GeV laser wakefield electron accelerators in meter-scale, low density hydrodynamic plasma waveguides operate in a new nonlinear propagation regime dominated by sustained beating of lowest order modes of the ponderomotively modified channel; this occurs whether or not the injected pulse is linearly matched to the guide. For a continuously doped gas jet, this emergent mode beating effect leads to axially modulated enhancement of ionization injection and a multi-GeV energy spectrum of multiple quasimonoenergetic peaks; the same process in a locally doped jet produces single multi-GeV peaks with <10% energy spread. A three-stage model of drive laser pulse evolution and ionization injection characterizes the beating effect and explains our experimental results.

Laser-driven plasma wakefields [1,2] have accelerating gradients  $\sim 1000$  times larger than those in linear rf accelerators, enabling the production of multi-GeV electron bunches in centimeters [3–6]. In general, optical guiding is needed to keep the intensity of the driving laser high and extend the acceleration length. While relativistic self-guiding has resulted in  $\sim 2$  GeV electron bunches, it demands petawatt-scale laser powers [3,4]. More laser-energy-efficient and controllable acceleration of electrons can be achieved by using plasma waveguides [5–22].

Recently, we demonstrated laser wakefield acceleration (LWFA) of electrons to 5 GeV in a 20 cm plasma waveguide using <300 TW of laser power [6]. In our scheme, which employs hydrodynamic plasma waveguides [7,8] generated in Bessel-beam-heated meter-scale gas jets [6,22], the laser pulse undergoes “self-waveguiding” [20,21], while simultaneously driving the plasma wake responsible for electron acceleration. First, a zeroth order ultrashort pulse Bessel beam with a 50 cm long focus ionizes and heats (by optical-field ionization [12–22]) a 20 cm long hydrogen 95%/5%–H<sub>2</sub>/N<sub>2</sub> gas sheet. The explosive hydrodynamic response leaves a  $\sim 10\times$  reduced gas density on axis surrounded by an expanding cylindrical shock shell of enhanced density measured by two-color interferometry [20]. When end-injected by a high intensity laser pulse, the core and inside walls of this “prepared index structure” are ionized by the very early leading edge of the injected pulse, forming an on-the-fly plasma waveguide that confines most of the pulse.

The accelerated electrons are injected into the wake by ionization injection [23–26] of N<sup>5+</sup>.

In this Letter, we present experiments and simulations demonstrating that laser intensity oscillations from a general mode beating effect—*active whether or not the injected laser is linearly mode matched to the guide*—are responsible for periodically enhanced ionization injection, giving rise to characteristic multi-peaked electron spectra at multi-GeV energies. A three-stage model of intense laser propagation explains our results. Insight from this model then motivates an experiment showing that mode beating at an axially localized dopant region produces quasimonoenergetic multi-GeV electron bunches with energy spread <10% and mrad divergence. The mode-beating-induced injection effect described in this work is new and emerges from the use of narrow, low density meter-scale plasma waveguides.

Figure 1 presents results from a representative WarpX particle-in-cell (PIC) simulation [27] for the parameters of our experiments, using a 95%/5%–H<sub>2</sub>/N<sub>2</sub> gas mix. The figure shows pulse evolution and electron acceleration for a LWFA drive pulse (blue curve:  $a_{0i} = 2.0$ ,  $\tau_{\text{FWHM}} = 41$  fs,  $w_0 = 30$   $\mu\text{m}$  Gaussian pulse) injected into a 20 cm waveguide with on-axis plasma density  $N_{e0} = 2.0 \times 10^{17}$  cm<sup>-3</sup>, where  $w_{ch} = 20$   $\mu\text{m}$  is the  $e^{-2}$  intensity radius of the lowest order self-waveguided mode of the structure shown in Fig. 1(d) and computed using our leaky mode solver [9,20,28,29]. The injected pulse is therefore mode-mismatched. Figures 1(a) and 1(b) plot the peak normalized vector potential and

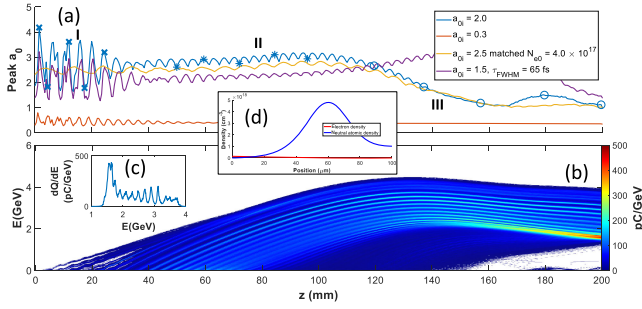


FIG. 1. WarpX [27] particle-in-cell simulations of drive pulse evolution in a waveguide formed from the prepared index structure [20] shown in the central inset, with  $w_{ch} = 20 \mu\text{m}$ . Gas composition is 95%/5%— $\text{H}_2/\text{N}_2$  and the simulation  $xyz$  grid is  $256 \times 256 \times 4096$  ( $256 \mu\text{m} \times 256 \mu\text{m} \times 204.8 \mu\text{m}$ ). (a) Peak laser field  $a_0$  vs propagation distance for (i) mismatched input field  $a_{0i} = 2.0$ ,  $w_0 = 30 \mu\text{m}$ ,  $\tau_{\text{FWHM}} = 41 \text{ fs}$ ,  $N_{e0} = 2.0 \times 10^{17} \text{ cm}^{-3}$  (blue curve); (ii) mismatched input field  $a_{0i} = 1.5$ ,  $w_0 = 30 \mu\text{m}$ ,  $\tau_{\text{FWHM}} = 65 \text{ fs}$ ,  $N_{e0} = 2.0 \times 10^{17} \text{ cm}^{-3}$  (purple curve); (iii) mismatched  $a_{0i} = 0.3$ ,  $w_0 = 30 \mu\text{m}$ ,  $\tau_{\text{FWHM}} = 41 \text{ fs}$ ,  $N_{e0} = 2.0 \times 10^{17} \text{ cm}^{-3}$  (orange curve); and (iv) matched  $a_{0i} = 2.5$ ,  $w_0 = 30 \mu\text{m}$ ,  $\tau_{\text{FWHM}} = 41 \text{ fs}$ ,  $w_{ch} = 30 \mu\text{m}$ ,  $N_{e0} = 4.0 \times 10^{17} \text{ cm}^{-3}$  (gold curve, Gaussian input pulse, parabolic channel). Labels I, II, and III denote the three characteristic propagation stages. Labels ( $\times$ ), ( $*$ ), and ( $o$ ) denote the locations of the frames displayed in Figs. 2(a)–2(c). (b) Electron spectrum vs propagation distance corresponding to the blue curve of (a). (c) Final integrated spectrum. (d) Prepared index structure measured by two-color interferometry [20] and fitted to even polynomial  $\times$  exponential.

electron energy spectrum vs  $z$ . The spectrum shows a striated energy structure caused by periodic ionization injection of electrons from  $\text{N}^{5+}$ ; comparing panels reveals that individual striations are correlated with  $a_0$  oscillations. With increasing  $z$ , the striations bend over as dephasing begins, and by  $z = 20 \text{ cm}$  the final spectrum of Fig. 1(c) shows that multiple quasimonoeenergetic peaks remain. The characteristic features of these plots are observed for a wide variety of conditions [28]. In pure  $\text{H}_2$ , pulse evolution is similar to that in Fig. 1(a), but with no electron injection and acceleration [28], in agreement with no experiments observing acceleration in pure  $\text{H}_2$  waveguides.

We identify three stages of pulse evolution as marked on the blue curve in Fig. 1(a): (I) large amplitude intensity oscillations during early propagation, which quickly transition to (II) sustained oscillations at lower amplitude, followed by (III) intensity decline and cessation of regular oscillations. Periodic ionization injection and the striated bunch energy structure occur during stages I and II; the degree of dephasing between the electron bunches and the plasma wake during stage III determines if this structure is preserved.

The oscillations in stages I and II suggest beating between different plasma waveguide modes. Although the modes of hydrodynamic plasma waveguides are strictly

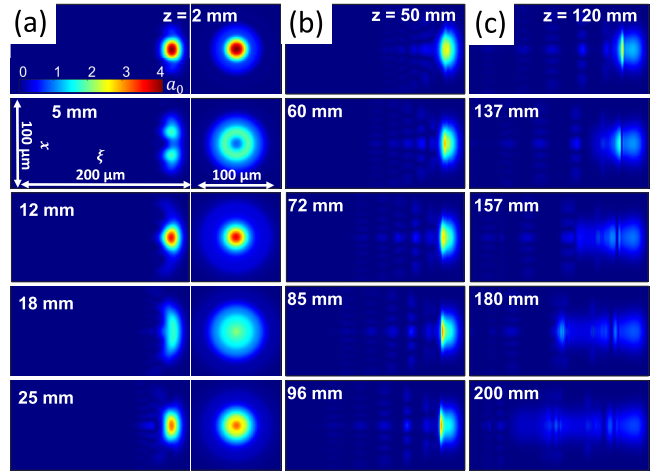


FIG. 2. Evolution of LWFA drive pulse corresponding to the blue curve in Fig. 1(a). Column (a) for stage I, plots  $x\xi$  slices of the field magnitude  $a_0$  on the left and the  $\xi$ -integrated mode on the right, where  $\xi = z - ct$  is the space coordinate in the moving computation frame. Longitudinal positions denoted on the frames are marked by the blue crosses in Fig. 1(a). Column (b), for stage II, plots  $x\xi$  slices of  $a_0$  for the longitudinal positions marked by the blue stars. Column (c), for stage III, plots  $x\xi$  slices of  $a_0$  for the longitudinal positions marked by the open circles in Fig. 1(a). All slices and profiles are normalized to the maximum at  $z = 2 \text{ mm}$ .

quasibound or “leaky” [9,29], an excellent approximation for low order modes of symmetric guides [9,28] is the spectrum of bound mode wave numbers of a parabolic plasma profile,  $\beta_{pm} = k_0[1 - N_{e0}/2N_{cr} - 2(2p + m + 1)/k_0^2 w_{ch}^2]$ , where  $(p, m)$  identifies the radial and azimuthal indices,  $N_{cr}$  is the plasma critical density,  $w_{ch} = (\pi r_e \Delta N_e)^{-1/2}$ ,  $\Delta N_e = N_e(w_{ch}) - N_e(0)$ ,  $r_e = e^2/mc^2$  is the classical electron radius, and  $k_0 = 2\pi/\lambda_0$  is the vacuum wave number [9,28]. The spatial beat period for two interfering modes is  $\Lambda = 2\pi/|\beta_{p'm'} - \beta_{pm}|$ . Mode beating between the (0,0) and (1,0) plasma waveguide modes, due to linear mismatch between the drive pulse and waveguide, has already been studied in Ref. [20]. Each mode has a characteristic  $1/e$  propagation decay length,  $L_{1/e}$ , which is longest for the (0,0) mode and decreases for higher order modes [9]. In the blue curve in Fig. 1(a), the oscillation period in stage I is  $\Lambda \sim 4.4 \text{ mm}$ , corresponding to beating dominantly between the (0,0) and (1,0) modes [28], with higher order modes contributing higher frequency interference. Despite the  $L_{1/e} \sim 7 \text{ m}$  and  $\sim 1 \text{ m}$  decay lengths of the (0,0) and (1,0) modes, the stage I beating quickly transitions to the lower amplitude oscillations of stage II.

To obtain further insight, we examine Fig. 2. Figures 2(a)–2(c) show the laser field magnitude  $a_0$  in the  $xz$  plane; the right column in 2(a) shows the field profile in the transverse ( $xy$ ) plane integrated over the pulse envelope. The panels are ordered vertically by the  $z$  locations marked on the blue curve in Fig. 1(a). The large

amplitude oscillations of stage I manifest in Fig. 2(a) as mode shape and size oscillations corresponding to the (0,0) and (1,0) modes. By  $z = 25$  mm, as stage I beating is fading, a small intensity tail has split off, lagging the main pulse. By  $z = 50$  mm, (stage II), a sequence of evenly spaced high order pulselets has increasingly separated from the main pulse, with the highest order modes the most delayed. This is understood as group velocity walk-off of higher order modes according to [9,20]  $v_{g,pm} = (\partial\beta_{pm}/\partial\omega)^{-1} = c[1 - N_{e0}/2N_{cr} - 2(2p + m + 1)/k_0^2 w_{ch}^2]^{-1}$ . However, as seen in the panels in Fig. 2(b) and the associated propagation movies in [28], the (1,0) structure remains tethered to the (0,0) structure by a long tail, sustaining the beating until  $z > \sim 110$  mm, whereupon the stage II oscillations decay as the wake weakens. Owing to the strong  $w_{ch}$  dependence of  $v_{g,pm}$ , this effect may be less observable in capillary waveguides, which typically have  $w_{ch} > 50$   $\mu\text{m}$ .

Further examination of Fig. 1(a) explains the propagation physics. A low intensity, *mode-mismatched* injected pulse with  $a_{0i} = 0.3$  and  $w_0 = 30$   $\mu\text{m}$  (orange curve), reproduces the stage I mode beating of the blue curve; here the beating terminates with complete walk-off of the (1,0) mode. For a higher intensity *mode-matched* Gaussian pulse in a parabolic channel [ $a_{0i} = 2.5$ ,  $\tau_{\text{FWHM}} = 35$  fs,  $w_0 = 30$   $\mu\text{m}$ ,  $w_{ch} = 30$   $\mu\text{m}$ , and  $N_{e0} = 4.0 \times 10^{17}$   $\text{cm}^{-3}$  (gold curve)], the stage I oscillations of the blue curve are absent, replaced by regular low amplitude oscillations (seen in [30–33]) extending through  $z > 110$  mm (the mode-matched case of  $a_0 = 2.0$  and  $N_{e0} = 2.0 \times 10^{17}$   $\text{cm}^{-3}$  yields little injection and acceleration). These oscillations are similar to the blue curve stage II oscillations, and both can be understood as beating of the (0,0) and (1,0) modes of a *ponderomotively modified channel*, where  $w_{ch}^{\text{blue}} = 18$   $\mu\text{m}$  (in stage II) and  $w_{ch}^{\text{gold}} = 24$   $\mu\text{m}$  are determined from the simulations [28]. Each is less than its corresponding unperturbed channel mode radius  $w_{ch,0}$  (20  $\mu\text{m}$  and 30  $\mu\text{m}$ , respectively).

The sustained beating of (0,0) and (1,0) modes appears to be a general feature of  $a_0 > 1$  laser pulse propagation in a plasma waveguide, *whether or not the injected pulse is linearly mode-matched to the guide*. As simulation movies show [28], pulse front erosion and red shifting from wake excitation, along with self-steepening at the back of the pulse, continuously feed energy from the front of the pulse, where  $w_{ch} = w_{ch,0}$ , to the cavitated region of the pulse centroid, where  $w_{ch} < w_{ch,0}$ . This effective mismatch couples to the (0,0) and (1,0) modes, generating a beat period  $\Lambda = 2\pi/|\beta_{10} - \beta_{00}| = \pi^2 \lambda_0 (w_{ch}/\lambda_0)^2$ . For the specific cases of Fig. 1(a),  $w_{ch} = w_{ch}^{\text{blue}}$  (in stage II) gives  $\Lambda_{\text{blue}} = 4.0$  mm and  $w_{ch} = w_{ch}^{\text{gold}}$  gives  $\Lambda_{\text{gold}} = 7.1$  mm. These are in good agreement with the oscillation periods from the simulations in Fig. 1(a).

This beating results in periodic axial modulations of the pulse envelope, with the peak  $a_0$  moving back and forth in

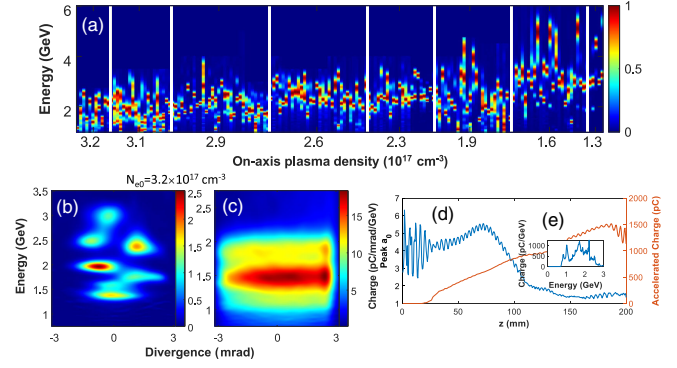


FIG. 3. (a) Angularly integrated electron spectra varying plasma density (P1 was 11 J,  $\tau_{\text{FWHM}} = 65$  fs,  $w_0 = 30$   $\mu\text{m}$  and  $a_0 \sim 2.0$ ), showing multipeak spectra ranging from  $>1$  GeV to  $<6$  GeV. Here, a 95%/5%– $\text{H}_2/\text{N}_2$  gas mix was injected by all six valves along the gas jet. Multiple shots were taken in each density bin, with an increase in accelerated electron energy as density drops. Each spectrum is normalized to its peak. (b) Example of multipeak spectrum with  $a_{0i} = 2$  and  $N_{e0} = 3.2 \times 10^{17}$   $\text{cm}^{-3}$ . (c) Example of “washed out” spectrum for higher intensity and waveguide density:  $a_{0i} = 2.5$  and  $N_{e0} = 3.2 \times 10^{17}$   $\text{cm}^{-3}$ . (d),(e) Results of PIC simulation for conditions of (c) showing early onset of depletion. Charge is for  $>1$  GeV.

the pulse frame [28]. High-resolution PIC simulations (see Appendix B) show that injection is enhanced during the phase of beating when the local peak in  $a_0$  is closest to the minimum of the wake potential. While some injection occurs during stage I, the large amplitude beating induces significant distortion of the wake and loss of trapped electrons. By  $z > 80$  mm, ionization injection in stage II ceases owing to pulse self-steepening and etching [28]. By stage III [Fig. 2(c)], the pulse has dispersed and broken up from red shifting and pulse stretching. Here, depletion-induced dephasing [6,34] results in a reduction of maximum accelerated electron energy for  $z > 140$  mm, but the striated energy structure is preserved because the pulse is too weak to disrupt the wakefield structure. For higher laser intensity and/or plasma density, we observe pulse breakup earlier in propagation, leading to wakefield distortion and loss of the striated energy structure [28]. A decrease in drive pulse energy (due, for example, to mismatched coupling) may also cause an earlier onset of depletion and loss of striations in the energy spectrum [28].

The three-stage picture is well-matched to our self-waveguided LWFA experiments at the ALEPH laser system [35] at Colorado State University. Details of the experimental setup are presented in Appendix A. We used three gas flow configurations: pure  $\text{H}_2$ , a dopant gas mix (95%/5%  $\text{H}_2/\text{N}_2$ ), or pure  $\text{H}_2$  with added localized injection of the dopant gas mix.

Figure 3(a) is a plot of angle-integrated electron bunch spectra vs plasma waveguide central density  $N_{e0}$  for the case of the dopant gas mix supplied to all six jet valves.

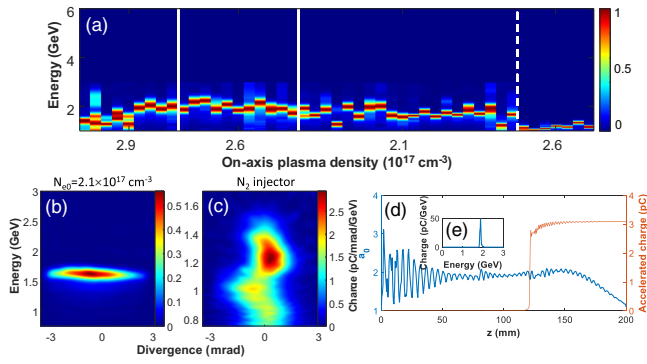


FIG. 4. (a) Angularly integrated electron spectra from multiple shots in each density bin, showing mostly single quasimonoenergetic peaks  $<2.5$  GeV. Here,  $a_{0i} = 2.0$ , and pure  $H_2$  was injected by all six valves along the gas jet, with a 95%/5%– $H_2/N_2$  dopant gas injector either at  $z = 10$  cm (spectra to the left of the dashed white line) or  $z = 14$  cm (spectra to the right of the dashed white line, where the waveguide central plasma density was fixed at  $N_{e0} = 2.6 \times 10^{17} \text{ cm}^{-3}$ ). Each spectrum is normalized to its peak. (b) Example of quasimonoenergetic spectrum with  $a_{0i} = 2.0$  and  $N_{e0} = 2.1 \times 10^{17} \text{ cm}^{-3}$  (localized dopant at  $z = 10$  cm). (c) Example of spectrum resulting from pure  $N_2$  injector at  $z = 14$  cm, showing continuous injection. (d),(e) Results of WarpX simulation for  $a_{0i} = 1.5$  and  $N_{e0} = 2.1 \times 10^{17} \text{ cm}^{-3}$  with localized dopant at  $z = 10$  cm. Charge is for  $>1$  GeV.

Here, P1 (11 J,  $\tau_{FWHM} = 65$  fs,  $w_0 = 30 \mu\text{m}$  and  $a_{0i} \sim 2.0$ ) was injected at 2.5 ns delay into the prepared index structure generated by P2 (0.5 J,  $\tau_{FWHM} = 75$  fs). The spectra vary shot to shot, under nominally similar conditions, due to injected laser pointing and energy fluctuations [6,28], but the majority of the spectra [such as Fig. 3(b)] are multi-peaked spectra consistent with the simulations of Fig. 1 for the case of dopant gas all along the waveguide. The distribution of the peaks shifts to higher energies with decreasing plasma density, as expected [6]. For higher P1 intensity (15 J,  $\tau_{FWHM} = 45$  fs,  $w_0 = 30 \mu\text{m}$ , and  $a_0 \sim 2.6$ ), the multipeak spectrum gives way to a broad, high charge and lower energy peak as illustrated by Fig. 3(c). The simulation of Fig. 3(d) for these conditions shows that higher laser intensity causes earlier onset of depletion-induced dephasing (stage III of pulse propagation), resulting in earlier rollover of the spectrum [compared to Fig. 1(b)], suppressing the lower energy striations and washing out the higher energy striations into a broad peak.

To generate a quasimonoenergetic spectrum, these results suggest employing the intensity oscillations as an injector over a localized region of dopant gas, an approach also used in capillary discharge waveguides [36,37]. Our gas jet design ([22], Appendix A) provides this capability via axially localized dopant gas inlets. Figure 4(a) is a plot of angle-integrated electron bunch spectra vs plasma waveguide central density  $N_{e0}$  for the case of pure  $H_2$  supplied to all six jet valves, and the dopant gas mix supplied through

an injector either at  $z = 10$  cm (left side of white dashed line) or at  $z = 14$  cm (right side)—well beyond the stage I mode-beating oscillations. The resulting spectra are dominantly single quasimonoenergetic peaks. By restricting the dopant gas region, we have limited the number of electron injection events from longitudinal oscillations in pulse intensity. This is reproduced in the simulation [Figs. 4(d) and 4(e)]. The narrowest peaks in Fig. 4 show energy spreads of  $<10\%$ .

To summarize, we have presented experiments and simulations showing that a universal mode-beating effect in meter-scale low density plasma waveguides—*occurring whether or not the injected laser is linearly mode-matched*—enhances ionization injection to produce multipeak, multi-GeV electron spectra or single quasimonoenergetic peaks. Enhancement occurs mainly due to mode-beating-driven back-and-forth oscillations in peak  $a_0$ . Additional spectrum control may be possible using waveguide sections with much higher dopant concentration. For example, Fig. 4(c) shows a spectrum where the dopant gas mix, at  $z = 14$  cm, was replaced with pure  $N_2$  gas, producing a continuous spectrum with a peak at  $\sim 1.3$  GeV in a narrow,  $\sim$ milliradian angular beam profile. Because the Bessel-beam-induced shock expansion in nitrogen is significantly slower than for hydrogen, the index structure in the injector section is narrowed. The guided pulse is then squeezed into a smaller channel at the injection section, increasing the pulse intensity above the ionization injection threshold and promoting continuous ionization injection. Across all of our experimental conditions, such continuous spectra were generated only with the use of a pure  $N_2$  injector, which suggests the possibility of electron spectrum control by guided mode shaping.

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## End Matter

*Appendix A: Experimental setup*—Figure 5(a) is a sketch of the experimental configuration. Plasma waveguides were generated by initial Bessel beam heating, via optical-field ionization, of a 20 cm long multi-valve-fed gas jet followed by self-waveguiding of the main end-injected pulse [20], which also drives LWFA. We used three gas flow configurations in our experiments: pure  $H_2$  in all valves, a dopant gas mix (95%/5%– $H_2/N_2$ ) in all valves, or pure  $H_2$  in all valves with added localized injection of the dopant gas mix. Figure 5(b) plots longitudinal atomic hydrogen gas density profiles [22] used in the experiments. The axial nonuniformity originates from the six discrete gas supply valves and slight machining variations in the jet throat. Further details on diagnostics of the gas jet and plasma waveguide and on phase front correction of Bessel beams are found in [6,22,39]. The ability of the injector to axially localize the dopant gas is demonstrated in Fig. 5(c). The jet was first run with  $H_2$  in the six valves and pure  $N_2$  in the injector valve, with the fluorescence image collected through an interference filter passing only the  $H-\alpha$  emission. The blue curve is the extracted axial density profile of atomic hydrogen, showing a notch at the location of the injector. Then the gases were switched, with  $H_2$  in the injector and  $N_2$  in the six valves, yielding the orange curve showing the axial specificity of injection. As in Refs. [6,22], the permanent magnet spectrometer is located outside the vacuum chamber, requiring propagation of the electron beam through an aluminum flange prior to dispersion in the

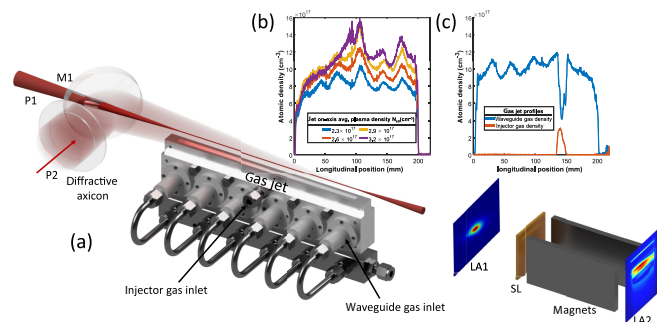


FIG. 5. (a) Sketch of experiment. A 10–15 J 45–65 fs,  $w_0 = 30 \mu\text{m}$  drive pulse (P1) is focused into the prepared index structure formed 2.5 ns after an initial plasma column has been generated by a synchronized 0.5 J, 75 fs zeroth-order Bessel beam ( $J_0$ ) pulse (P2) with a  $\sim 40$  cm long central focal line 3 mm above a 20 cm supersonic (Mach 4)  $H_2$  gas jet. The  $J_0$  pulse is produced by splitting a portion of the main beam, compressing it in a separate compressor, and focusing it with a diffractive axicon. The jet is supplied by six gas valves and has localized inlets for dopant gas to seed ionization injection. Accelerated electron bunches exit the end of the waveguide and pass through an 0.85 mm thick aluminum exit flange and LANEX screen (LA1) [41,42] before entering a 0.93 T permanent magnet spectrometer with an adjustable 0.25–1 mm collimating slit (SL). The dispersed electron spectrum is recorded on LANEX (LA2), and imaged with an Andor Zyla 4.2 camera. (b) Atomic hydrogen density profiles and associated on-axis waveguide plasma densities. (c) Example of gas distributions with use of a localized  $N_2$  injector at  $z = 14$  cm from the waveguide entrance.

magnetic field. Ray tracing simulations [40] suggest that this increases the apparent energy spread and divergence of dispersed electron beams.

*Appendix B: Correlation of ionization injection and mode beating*—To investigate the effect of mode beating on electron injection, we performed a quasi-3D simulation with FBPIC (Fourier-Bessel particle-in-cell code) [43], employing particle tracking, for the same parameters as for the blue curve in Fig. 1(a). Here, particles  $>50$  MeV in the bunch at  $z = 10$  cm are tracked back to their  $z$  location of birth. The simulation was performed in a boosted frame with  $\gamma = 2$ , with four azimuthal modes and eight tracked particles per cell (eight per azimuthal, one per radial, and one per longitudinal grid segment). The field and tracked particle data were saved every  $20 \mu\text{m}$  from  $z = 0$  to  $z = 10$  cm. Electrons born slightly after a save location may evolve over several simulation steps before being recorded as “new” particles at the next save location.

Figure 6(a) plots the on-axis laser envelope in  $(\xi, z)$  space along with the charge per unit length  $dQ/dz$  injected vs  $z$  (white curve). The overall rise of the white curve (apart from its modulations) occurs as the laser peak intensity retreats in the light frame, leading to slower wake velocity and enhanced charge injection. The evident correlation between envelope oscillation and injection in Fig. 6(a) is explained by Fig. 6(b), which replots  $dQ/dz$  (blue curve) along with the relative wake position  $\Delta\xi_{\text{wake}} = \xi_{\text{wake}} - \langle \xi_{\text{wake}} \rangle_{1 \text{ cm}}$  (purple curve), relative position of  $a_0$  peak  $\Delta\xi_{a_0, \text{peak}} = \xi_{a_0, \text{peak}} - \langle \xi_{a_0, \text{peak}} \rangle_{1 \text{ cm}}$  (red curve), and peak  $a_0$  vs  $z$  (green curve). The wake position  $\xi_{\text{wake}}$  is the location where  $E_z = 0$ , the potential minimum or trapping center near the back of the wake bubble, and  $\langle \rangle_{1 \text{ cm}}$  denotes an average over 1 cm of propagation. Note that few electrons injected in the early part of the waveguide ( $z < \sim 25$  mm) survive to  $z = 100$  mm; the injected electrons are dominantly from stage II of propagation. Figure 6(c) plots the laser field envelope (top half of frame) and plasma density (bottom half) overlaid with injected electron initial locations (white dots and circles) during a full cycle of beating. Given the  $20 \mu\text{m}$  save interval for the simulation, electrons born slightly after a save location may evolve over several simulation steps before being recorded as “new” particles at the next save location. This is why the

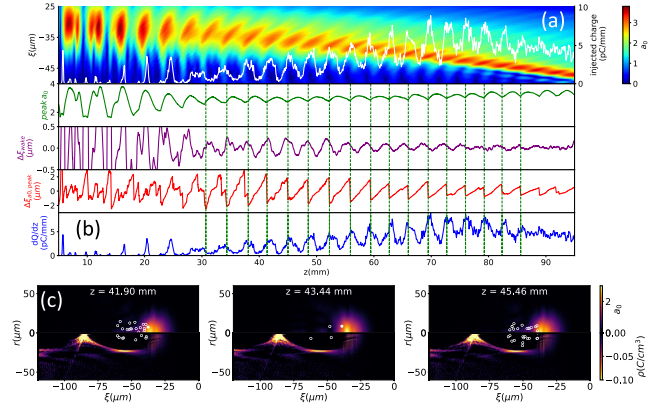


FIG. 6. FBPIC simulation with particle tracking, for the same parameters as the blue curve of Fig. 1(a). (a) On-axis evolution of the laser envelope ( $a_0$ ) in the light frame (computation window,  $\xi = z - v_g t$ ), showing the periodic motion of the laser pulse peak and pulse retreat in the light frame. The white curve is a histogram of electron injection locations contributing to the bunch at  $z = 10$  cm with electrons  $>50$  MeV. (b) Lineouts of pulse and wake parameters vs propagation distance (see text). Green curve: peak  $a_0$  in moving window. Purple curve: relative position of the back of the wake,  $\Delta\xi_{\text{wake}} = \xi_{\text{wake}} - \langle \xi_{\text{wake}} \rangle_{1 \text{ cm}}$ . Red curve: relative position of peak  $a_0$ ,  $\Delta\xi_{a_0, \text{peak}} = \xi_{a_0, \text{peak}} - \langle \xi_{a_0, \text{peak}} \rangle_{1 \text{ cm}}$ . Blue curve: replot of white curve from panel (a). (c) Laser field envelope (top half of frame) and plasma density (bottom half) overlaid with injected electron initial locations (white dots and circles) over a full cycle of beating, showing two injection maxima and a minimum. The dots mark likely birth locations of trapped electrons in a given frame.

axial extent of the white circles in Fig. 6(c) is approximately  $20 \mu\text{m}$ , with those on the left closest to trapping. The white dots to the right mark likely birth locations of trapped electrons in a given frame.

Figure 6 makes clear that injection is enhanced when mode beating shifts the location of maximum  $a_0$  closest to the wake trapping center; for this phase of the beating, peak  $a_0$  in the moving frame is a minimum. During stage II, the oscillations of  $\Delta\xi_{a_0, \text{peak}}$  are an order of magnitude larger than  $\Delta\xi_{\text{wake}}$ , showing that periodically enhanced injection is mainly due to the mode-beating-driven back-and-forth oscillations in peak  $a_0$ , and not oscillations in wake velocity as may occur under other conditions [33,44].