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A three-stage optimization methodology for envelope design of passive house considering energy demand, thermal comfort and cost

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Abstract
Due to reducing the reliance of buildings on fossil fuels, Passive House (PH) is receiving more and more attention. It is important that integrated optimization of passive performance by considering energy demand, cost and thermal comfort. This paper proposed a set three-stage multi-objective optimization method that combines redundancy analysis (RDA), Gradient Boosted Decision Trees (GBDT) and Non-dominated sorting genetic algorithm (NSGA-II) for PH design. The method has strong engineering applicability, by reducing the model complexity and improving efficiency. Among then, the GBDT algorithm was first applied to the passive performance optimization of buildings, which is used to build meta-models of building performance. Compared with the commonly used meta-model, the proposed models demonstrate superior robustness with the standard deviation at 0.048. The optimization results show that the energy-saving rate is about 88.2% and the improvement of thermal comfort is about 37.8% as compared to the base-case building. The economic analysis, the payback period were used to integrate initial investment and operating costs, the minimum payback period and uncomfortable level of Pareto frontier solution are 0.48 years and 13.1%, respectively. This study provides the architects rich and valuable information about the effects of the parameters on the different building performance.

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1. Introduction
Population growth, increased demand for indoor environment and global warming have led to a sharp increase in energy consumption for buildings heating and cooling, which accounts for 20% of global energy consumption [1]. Especially, the energy consumption by the residential building is increasing at approximately 30% annually worldwide [2]. Therefore, developing sustainable buildings has increasingly become a very important task, and Passive House (PH) has emerged as the preferred concept for architects and subject for researchers in most countries. PH are buildings that need 80%–90% less heating energy than conventional buildings to provide comfortable indoor conditions, while the incremental cost of their construction is only 5%–10% [3]. Many countries have introduced PH standards. For example, China has issued “Passive ultra-low energy green building technology guidelines” [4]. However, the standards merely set deterministic results to evaluate the design without pre-directing the design. Therefore, it is almost impossible to use standards to fully exploit large design spaces and to guide decision-makers. In addition, engineers and technicians put more focus on active equipment and facilities but ignore the idea that PH is based on improving passive performance [5]. The passive performance is the base of sustainable development, especially for residential buildings [6].

Current research on PH buildings mainly focuses on performance assessment such as energy consumption and thermal comfort. Many studies have shown the superior performance of PH buildings. Based on the performance simulation, the heating energy demand of the PH building is less than the requirement of the PH standard, and the annual cooling energy demand is also very low [7]. The measured data shows that the total energy consumption of PH buildings is reduced by about 50% compared with traditional buildings [8] and reduce heating energy consumption by about 65% and energy consumption by 35% compared with low-energy buildings. However, there are also studies that expose the negative side of PH buildings in the indoor thermal environment, especially during the transitional season. For example, based on in-use monitored data gathered in 21 months, a study evaluated the thermal comfort of a UK PH dwelling with vulnerable occupants [9].
This research indicated that indoor overheating risk (IOR) can occur if the dwelling is not managed correctly, energy and carbon savings should not be at the expense of thermal comfort. In Europe, IOR in PH buildings has been recorded as more widespread compared to traditional buildings [10,11]. Moreover, in Australia, the high-performance buildings do not directly encourage passive survivability and can even increase IOR compared to traditional buildings [12]. Even some studies have directly pointed out that improving building fabric (increased insulation and airtightness) increases IOR [13]. It should be mentioned that natural ventilation is very effective in reducing energy consumption and improving the indoor thermal environment [14]. Opening the window for ventilation during the night or uncomfortable daytime can maintain indoor thermal comfort [15]. In short, thermal comfort issues should be valued in high-performance buildings such as PH buildings.

Many recent scientific studies performed building performance optimization whether it is single or multi-objective. There are numerous metrics involved in assessing building performance: 1) energy metrics [16–20], including annual heating, cooling, lighting, and total building energy demand; 2) life cycle metrics [16], including life cycle costs, life cycle carbon emissions and life cycle energy consumption; 3) indoor thermal comfort metrics [17,18]. It should be mentioned that it is easy to transfer energy metrics into life cycle metrics with some simple additional information [21]. According to the research objects, these studies mainly focus on new residential buildings and renovated buildings. For example, a study developed a new methodology to optimize building life cycle cost, environmental impacts, and occupants satisfaction in the early design phase [17,22]. Another research proposed a set of optimization methods for energy-renovating buildings that focus on energy consumption, retrofit cost, and thermal discomfort hours [23]. However, the design priorities of PH and conventional buildings are different, in the related research of PH buildings, few studies involve integrated optimization of energy efficiency, thermal comfort, and economic benefit.

Computer-aided optimization is the earliest method used in building performance optimization (BPO). It is automatically optimized by coupling simulation software and optimization algorithms [24]. However, evolutionary algorithms usually still need a large number of cost function evaluations before a satisfying result can be obtained [25]. Moreover, higher time costs of dynamic building performance simulation reduce the effectiveness of BPO and especially its diffusion in professional practice [26]. A survey study based on architects, mechanical engineers, and green construction consultants demonstrated that slower optimization speed is the main reason for hindering the actual application of BPO [19]. More important, some optimization indicators cannot be directly obtained by running simulation software, generally, they need secondary processing. Therefore, traditional computer-aided algorithms are not suitable for multi-objective optimization problems. For this reason, an approximation of the optimization problem is required. Among existing approximation approaches, the functional approximation approach (a.k.a. meta-model or surrogate model approximation) is the most used in BPO [27]. The meta-model constructs a functional relationship between multiple inputs and multiple outputs, which improve efficiency by sacrificing precision [28]. It should be mentioned that the meta-model is not equal to the agent model. The former is generally used for building performance optimization problems, while the latter generally appears in research related to human behavior and perception [29]. Seeking appropriate algorithms to build a high-precision meta-model is getting more and more research attention [30–33]. Several studies have employed a variety of algorithms to establish meta-model, such as multiple linear regression [34–36], support vector machines (SVM) [33] and artificial neural networks (ANN) [17,23,37,38]. These meta-models are generally combined with optimization algorithms such as genetic algorithms (GA). For example, Asadi et al. present a multi-objective optimization model using GA and ANN to quantitatively assess technology choices in a building retrofit project [23]. Gou et al. established a model to optimize the thermal comfort and energy demand of new residential buildings, by using the Non-dominated Sorting Genetic Algorithm II (NSGA-II) coupled with the ANN [17]. Although the meta-model has been generally accepted and applied, proposing new algorithms to build a more robust and highly accurate meta-model is still the research focus. Especially for multi-objective optimization problems, the robustness of the meta-model is more important [39].

Based on the above analysis, a summary of the existing problems and the corresponding innovations is as follows:

(1) From the optimization model:

   ● **The existing problems on PH buildings:** Most research related to PH buildings focuses on performance assessments, some of which only raised the phenomenon of the indoor overheating risk in PH buildings, but did not propose solutions to solve the problem. In addition, PH standards have only constrained the range of energy
consumption and certain design parameters, but it is difficult to guarantee an optimal solution. In summary, there is still a lack of systematic optimization methods to guide the passive design of PH buildings in engineering applications.

- **The corresponding innovation:** This paper establishes an optimization model for PH buildings. Different from previous research, the optimization model considers the effect of windowing for natural ventilation on the indoor thermal environment. The relationship between 20 passive design parameters and two building properties including energy demand and thermal comfort was constructed and the optimization scheme was explored under the constraints of PH standards. Finally, an economic analysis of the Pareto frontier solution was carried out. The optimization framework produces more practical and detailed design guidance.

2. Method

The optimization framework for PH buildings mainly includes three parts: constructing optimization model, establishing optimization method and post-Pareto analysis (Fig. 1). This section details the involved methods.

2.1. Optimization model

2.1.1. Optimization variables

The optimization variables involved are dominated by passive parameters, generally relate to design parameters of building components, such as the wall and roof (insulation, density, and specific heat), exterior windows (insulation and SHGC), building shape (shape coefficient and window-wall ratio), airtightness and building layout (orientation, etc.). The relationship between these parameters is more or less non-linear, so there will be interaction in the construction of variable space [40]. As shown in Table 1, 20 optimization variables are covered in this paper.

The boundaries and probability distribution of optimization variables will largely affect the optimization result. Considering that the research is oriented at the overall passivity of a building, it is assumed that the design variables are continuously and evenly distributed in order to fully cover the architectural feature space [41]. The determination of the boundaries of design variables can be divided into three cases. First, variables have been clearly defined in the PH standards [42], such as SHGC, the U-value of envelope components and airtightness. According to common practices, the insulation layer and the filling layer (usually concrete) of walls and roofs respectively affect the insulation level and thermal mass. The U-value is obtained by changing the insulation thickness,
and the density, as well as specific heat, are obtained by changing parameters of the filling layer [17,43]. Second, WWR for different orientations determined according to the JG series of standards [44]. Third, the boundary is determined according to the variables occurring in the related literature though they may not be clearly defined in norm or standards. For example, the overhang depth and the fin depth of shading are set equal to the height of the external window [17]; The specific heat changes within default limits as per EnergyPlus modeling guidelines [33]; the change in the density of the envelope is based on the characteristics of conventional concrete [45]. The solar absorptance of building coating was set according to the absorptive characteristic of surface materials of various colors. The building orientation is changed from 0° to 360°. The external windows are closed in the cooling season and the heating season. In the transition season, the indoor thermal environment can be regulated by natural ventilation. In this study, the “Wind and Stack with Open Area model” is used, which is a function of wind speed and thermal stack effect. The model is designed to simplify ventilation calculations rather than using a flow network model for more detailed ventilation investigations.

2.1.2. Optimization objectives

2.1.2.1. Energy-related performance indicators. Building energy demand was defined as the sum of the cooling and heating energy demand of all flats, calculated for the cooling (from Jun. 14 to Aug. 28) and heating periods (from Nov. 15 to Mar. 15) respectively. The energy demands for domestic hot water, electronic equipment, and artificial lighting were not considered as they were not expected to vary significantly throughout the periods of optimization [17]. Building energy demand, cooling and heating energy demand are represented by the annual energy use intensity (EUI), cooling energy use intensity (CEUI) and heating energy use intensity (HEUI), respectively. Similar to many previous related studies [16,17,19], the HVAC system used in this study was the ‘Ideal Loads Air System’, which means that the Coefficient of Performance (COP) of the system was assumed to be 1 and is used in situations where the intention is to study the building HVAC energy demand. Among then, the humidification/dehumidification consumptions were considered and the fresh air change rate of the HVAC system was set as 1 per hour for every simulation case. The building performance is based on the hourly simulation of the whole year, and the time step is 6 times/h.

2.1.2.2. Thermal comfort indicator. The adaptive model is used to evaluate the thermal comfort of free-running buildings, and the ASHRAE-55 adaptive model, which is based on field data collected from various climate zones, is the most commonly used [46]. The ASHRAE-55 model uses outdoor monthly average temperatures to represent outdoor weather conditions. The indoor environment of the transition season in this paper can be evaluated using this model.

The neutral temperature calculation based on the ASAHE-55 model is shown in equation (4):

\[ T_{c} = 0.31 \times T_{a} + 17.8 \]  

(4)

Considering 80% acceptability, thermal comfort fluctuates within 3.5 °C on either side of neutral temperature (7 °C bandwidth).

Based on the adaptive model, the annual cumulative comfort ratio (CTR) is used as a thermal comfort measure. The calculation formula is as follows:

\[ CTR = \frac{1}{m} \sum_{k=1}^{m} \left( \sum_{j=1}^{m} W_{fj} \cdot \frac{1}{N_{p}} \right)_{k} \in [0, 1] \]  

(5)

\[ W_{fj} = \begin{cases} 1, & \text{if } T_{lower} \leq T \leq T_{upper} \\ 0, & \text{if } T < T_{lower} \text{or } T > T_{upper} \end{cases} \]  

(6)

Where \( T \) is the comfort indicator, which here is the room temperature. \( T_{upper} \) and \( T_{lower} \) are the limits of the thermal comfort zone. \( N_{p} \) represents the total hours. The number of flats is \( m \), CTR is the
average of the thermal comfort of nine flats.

2.1.3. Objective functions

In this paper, the annual EUI and CTR were taken as optimization targets. In addition, according to the general requirements of the PH standard, the constraint condition is set as HEUI and CEUI. The fitness function is defined as Eq. (7):

\[
OF = \left[ f_1 = f(X, \text{EUI}_{\text{min}}) \right], \quad f_2 = f(X, \text{CTR}_{\text{max}})
\]

Subject to

\[
\begin{cases}
\bar{X} = \bar{X}_{\text{range}} \\
\text{HEUI} \leq 15 \\
\text{CEUI} \leq 3.5 + 2 \times \text{WDH}_{20} + 2.2 \times \text{DDH}_{28}
\end{cases}
\]

Where, the \( \bar{X}_{\text{range}} \) contains 20 variables, all variables meet the distribution form and value range requirements in Table 1. WDH\(_{20}\) (Wet-bulb degree hours 20) is the cumulative value of the differences between the wet-bulb temperature and the 20 °C when it is higher than 20 °C in one year (kkh). DDH\(_{28}\) (Dry bulb degree hours 28) is the cumulative value of the difference between the dry-bulb temperature and the 28 °C temperature when it is higher than 28 °C in one year (kkh).

2.2. Sensitivity analysis

Sensitivity analysis (SA) plays an important role in performance analysis such as building energy, which can specifically extract key factors that affect each building performance [41,47]. Regression methods are the most commonly used global SA method because they are easy to understand, and the minimum sample size required is relatively small [41]. Many sensitivity indicators are derived based on regression methods, such as Standardized Regression Coefficients (SRC), Partial Correlation Coefficients (PCC), standardized rank regression coefficient (SRCR) and partial rank correlation coefficient (PRRC). The first two apply to linear models, and their ranks apply to non-linear monotonic models. Compared to SRCR, PRRC suits the correlated input variables better because it can exclude the effects of correlations between input variables [48].

In the field of building performance, some passive variables are interactive, and the relationship between variables and optimized performance goals is non-linear. Therefore, PRRC is used as the SA index.

2.3. Optimization method

2.3.1. Redundancy analysis

PRRC can show the relative order of importance of a set of input variables on output variables. There are no clear assessment criteria to measure absolute importance, but mainly to present the relative importance of variables. Therefore, this paper used redundant analysis (RDA) to compensate for the deficiencies of the PRRC in this respect. While giving the level of influence of the input variable on the output variable, the redundancy analysis can also give the significance of the effect at the same time.

RDA is a multivariate technique that examines how a set of response variables (Y) is related to a set of explanatory variables (X) by measuring the portion of the variance in the response variables that is explained by explanatory variables. In this paper, design parameters and building performances are explanatory variables (X) and response variables (Y), respectively. Intuitively, RDA is a canonical version of principal component analysis (PCA), and in general consists in deriving a series of multiple linear regressions of the dependent variables Y on the independent variables X, followed by principal component analysis of the matrix of fitted values. The main steps in an RDA, which are described in Makarenkov and Legendre [49], are as follows:

Multiple linear regression is computed for each Y, one by one, on all X. This step yields the fitted values \( \tilde{Y} \) through the following formula:

\[
\tilde{Y} = XB = X\mathbf{X}'\mathbf{X}^{-1}\mathbf{Y}
\]

The covariance matrix \( S \) of the fitted values \( \tilde{Y} \) is computed using the following formula:

\[
S = \left[ 1 / (n - 1) \right] \tilde{Y}\tilde{Y}' = \left[ 1 / (n - 1) \right] \mathbf{Y}' \mathbf{X} (\mathbf{X}' \mathbf{X})^{-1} \mathbf{X}' \mathbf{Y}
\]

Eigenvalue and eigenvector decomposition of the covariance matrix \( S \) of \( \tilde{Y} \) is carried out by solving the following matrix equation:

\[
(S - \lambda_k \mathbf{I}) \mathbf{u}_k = 0
\]

Where \( \lambda_k \) is a canonical eigenvalue and \( \mathbf{u}_k \) is the related canonical eigenvector. The matrix containing the normalized canonical eigenvectors \( \mathbf{u}_k \) is called \( \mathbf{U} \).

The ordination of objects (Y rows) independent variable space is obtained directly from the centered matrix Y, using the standard equation for computing principal components:

\[
\text{Ord}_{\text{response variable Y space}}^k = Y_{uk}
\]

The ordination vectors defined by Eq. (4) are called “site scores”. Their variance is similar, although not necessarily equal to the corresponding eigenvalues.

Likewise, the ordination of objects in X space is obtained using the following equation:

\[
\text{Ord}_{\text{explanatory variable X space}}^k = \tilde{Y}_{uk}XBu_k
\]

The ordination vectors, called “fitted site scores”, are the linear combinations of the explanatory variables X. Their variance is equal to the corresponding eigenvalues.

2.3.2. Meta-model

2.3.2.1. Gradient Boosted Decision Trees (GBDT). More advanced thinking called ensemble learning was introduced in the early 1990s [50]. The ensemble learning leverages the principle of model complementation to provide more accurate and stable results compared to base models [51]. Most review articles published in the recent past, suggest that ensemble algorithms are more effective than single prediction algorithms [52,53]. Choosing an effective machine learning algorithm is critical to achieving good performance with the resulting meta-model. GBDT also called multiple additive regression trees (MART) or gradient boosting machine (GBM), is an integrated machine learning algorithm [54]. Due to the high robustness, the GBDT algorithm has been increasingly popular in the field of building energy management. Numerous studies have shown that the GBDT model exhibits the highest performance in the prediction of energy consumption by appliances in a low-energy house [55], building baseline energy consumption predictions [56], and electricity load forecasting for utility energy management systems [57]. Therefore, this study builds meta-models for building performances based on GBDT algorithm. The detailed construction process of this algorithm is described in Ref. [58].

2.3.2.2. The evaluation index
Accuracy.

The error indicators specified in ASHRAE Guideline 14–2002 are introduced, that is, the basic requirements for meta-models. When the standard mean deviation (NMBe) and the coefficient of variation of root mean square error (CV-RMSE) is less than ±5% and ±15%, respectively, the model is accurate and reliable [59].

The calculation formula is as follows:

\[
NMBe = \frac{\sum_{i=1}^{n}(\hat{y}_i - \bar{y})}{n \times \bar{y}} \times 100%
\]

\[
CVRMSE = \sqrt{\frac{\sum_{i=1}^{n}(\hat{y}_i - \bar{y})^2}{\bar{y}}} \times 100%
\]

Where the \( \hat{y}_i \), \( \bar{y} \) represents the actual value, the predicted value and the average actual values.

Robustness.

The robustness of meta-model refers to the ability to provide acceptable accuracy for diverse problems with varying levels of complexity and dimensionality [60]. This paper covers a variety of building performance indicators include energy and thermal comfort. These performance indicators vary substantially in complexity and in the shape of the output distribution (see Section 2.4). Thus, the meta-model technique must be robust to each performance indicator. As an indicator of robustness, previous works have used the standard deviations of the accuracies obtained from multiple problems [61,62]. \( R^2 \) is generally used as an accuracy index to calculate the standard deviation [60].

2.3.3. Optimization algorithm

The multi-objective function is solved by a multi-objective optimization algorithm. Multiple optimization functions are generally involved in the performance optimization of building, and the dimensions between different properties may be different, such as energy demand kWh/(m²a) and thermal comfort level (%/a) in this article. It is difficult to integrate into one optimization function. Therefore, the Pareto method is usually used to solve such problems [63]. The Pareto method can provide a non-dominated optimization solution that allows for solution selection based on preferences during subsequent decision making [64]. These algorithms can handle efficiently non-linear problems with discontinuities and many local minima [65]. Among them, genetic algorithms (GA) are widely and effectively applied to building performance optimization problems, especially non-dominated sorting genetic algorithms (NSGA-II) [66]. For example, a study developed objective functions of energy consumption, retrofit cost, and thermal discomfort hours, and studied the interaction between these conflicting objectives and assess their trade-off using the NSGA-II algorithm [23]. Another study used the NSGA-II algorithm to solve the optimization function with the annual energy consumption and the summer comfort degree as the optimization goals [67]. Therefore, NSGA-II is used in this paper to optimize the passive performance of buildings.

2.4. Economic assessment

An economic analysis of the Pareto frontier solution is necessary. In this paper, the initial investment, operating costs and payback period are used to evaluate the economic benefits of the optimized solution. The design parameters that cause great economic differences due to various values are mainly the insulation thickness and the windows type. Therefore, they are the main parameters considered in the initial investment.

The main initial investment cost and the annual operating costs of HVAC are calculated as follows:

\[ C_i = c_{wall} + c_{roof} + c_{window} \]  \hspace{1cm} (17)

\[ C_o = c_{heating} + c_{cooling} \]  \hspace{1cm} (18)

\[ PBC = \left( C_{io} - C_{ib} \right) / \left( C_{io} - C_{oo} \right) \]  \hspace{1cm} (19)

Among them, \( C_i \) is the initial investment cost, CNY/m². The price of the insulation material and the exterior window can be obtained from Green building material selection technology [68] and the China Building Materials Network [69], respectively. \( C_o \) is the operating cost, including heating and cooling, CNY/m². The urban heating network is used in the winter, and the local heating cost is 0.13RMB/kWh. The household air conditioner is used in the summer, and the COP value is 2.8. The PBC is the payback period. The \( C_{io} \) and \( C_{ib} \) present the initial investment of optimized solution and the base building. \( C_{oo} \) and \( C_{ib} \) present the operating costs of optimized solution and the base building.

2.5. Construction of sample space

The input-output matrix is built by the coupling of Python programming language and EnergyPlus. As shown in Fig. 2, firstly, the input matrix is constructed using Latin hypercube sampling (LHS) in Python and stored in a CSV file. Then each set of the input variable is read from the CSV file and written to the EnergyPlus software in turn by means of Python. Then use Python to read the CSV file, and then write each set of the input variable to the IDF file of EnergyPlus in turn. Finally, EnergyPlus performs building performance simulation and enters the next loop. In general, the entire program consists of two loops: python writes the input variables to EnergyPlus in turn, and the EnergyPlus software performs a full-year simulation in time steps.

The sample size taken by the LHS during the uncertainty analysis is generally at least ten times the number of input variables, but it is also related to the interaction complexity between input parameters. In order to ensure that the selected sample size is statistically representative, this paper compares the probability density function (PDF) of performance indicators for different sample sizes. It is generally believed that when the probability density function gradually becomes uniform as the sample size changes, the sample size can represent the overall building library. Independent sampling is performed to get the sample sets of variables in different sizes. According to Fig. 3, when the sample size is greater than 300, the PDF curve does not vary substantially as the sample size changes, especially CEUI. This verifies the effectiveness of the LHS method in this research question. In the subsequent analysis, we need to ensure that the sample size is greater than 300.

3. The base-case building model

3.1. Setting the building model

Since the optimization of passive parameters exists in the early stage of building design, as in most of the related existing studies, the simulation data is used to expand the research database [16]. The entire building performance is simulated using EnergyPlus (Ver.9.0.1), which is a highly validated simulation engine widely used in building energy analysis [70]. In order to represent the
Fig. 2. The framework used to perform automatic EnergyPlus simulations.

Fig. 3. The curve of the probability density function under different sample sizes.
characteristics of most Chinese residential buildings, this paper takes the popular slab-type building as an example, which has a rectangular footprint and there are about three flats on each storey [71]. According to the database of Lianjia [72], the most common area of flats is about 100 m² in most of the newly built buildings. The rectangular footprint of the total building is 31.2 m × 11.0 m (length × width) with three units on each story (Fig. 4). The building long axis is oriented East-West. The parameters of the envelope components are determined in accordance with JCJ residential building standards [44], which are shown in Table 2. It is assumed that three persons live in each unit, and their schedule of a workday is shown in Table 3. The internal thermal load from lighting, equipment, and people are assumed to be 4.3 W/m² on average.

Multi-story, especially the high-rise residential buildings, contain thousands of interior spaces, and it is not realistic to simulate a complete architectural model. In order to improve the computational efficiency, the common practice in the existing research is to select the bottom, standard and top stories to construct the building model according to the influence of the external meteorological environment [17]. Therefore, in order to reduce the number of thermal zones, this study uses a three-story building model in the subsequent process. In addition, since our research object is the average performance of the entire building, each flat is used as a thermal zone in order to simplify the calculation. This division method refers to some existing research [17] and the standard residential building model generated by the U.S. DOE Building Energy Codes Program [73].

### 3.2. Climate characteristics

China’s policy prescribes the design features of traditional buildings in the cold climate to be mainly for thermal insulation in winter [45]. However, with global warming and the improvement in living standards, the cooling demand during summertime is gradually increasing in the cold climate and the cooling energy consumption cannot be ignored. Therefore, it is necessary for the region to find the optimal passive design. This study selects the typical city of Tianjin as the case location. Tianjin is located in eastern China. HDD18 and CDD26 are 2743 and 92 respectively, and the annual average horizontal radiation intensity is 102 W/m². As shown in Fig. 5, the average daily temperature throughout the year is between –10 and 30 °C. The heating season in the area lasts from November 15 to March 15 of the following year, and the cooling season is from June 14 to August 28. The weather data for simulation are derived from the Chinese Standard Weather Data published by the EnergyPlus website [74].

**Table 2**

<table>
<thead>
<tr>
<th></th>
<th>Exterior wall</th>
<th>Roof</th>
<th>Exterior window</th>
<th>The floor</th>
<th>Interior wall</th>
</tr>
</thead>
<tbody>
<tr>
<td>U-value</td>
<td>0.7</td>
<td>0.45</td>
<td>2.5</td>
<td>0.65</td>
<td>1.5</td>
</tr>
<tr>
<td>WWR</td>
<td>North: 0.3; South: 0.5; West: 0.35; East: 0.35</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Form</td>
<td>Layer height:2.9; Shape coefficient:0.299</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Table 3**

<table>
<thead>
<tr>
<th>Time</th>
<th>1-7</th>
<th>8</th>
<th>9-18</th>
<th>18-19</th>
<th>19-23</th>
<th>23-24</th>
</tr>
</thead>
<tbody>
<tr>
<td>Accuracy</td>
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<td>Red</td>
<td>Yellow</td>
<td>Red</td>
<td>Red</td>
<td>Red</td>
</tr>
<tr>
<td>Lighting</td>
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<td>Green</td>
<td>Green</td>
<td>Green</td>
<td>Green</td>
<td>Green</td>
</tr>
<tr>
<td>Power</td>
<td>Green</td>
<td>Green</td>
<td>Green</td>
<td>Green</td>
<td>Green</td>
<td>Green</td>
</tr>
</tbody>
</table>

**Fig. 4.** Elevation and Isometric view of case building.

**Fig. 5.** The daily average temperature in Tianjin and the season division.
4. Results

4.1. Multivariate performance analysis

PRCC, the sensitivity index, derived from MLR is applied to analyze the main factors affecting building performance. The larger the sample size, the more stable the indicators will be. However, there is no a priori exact rule for determining the adequate sample size for LHS—PRCC index. A way to solve the problem is to systematically increase the sample size and check if the sensitivity index used can consistently capture and rank a similar set of most important effects [75]. Therefore, the sensitivity analysis results under different samples are compared in this section. The input variables involved include not only thermo-physical parameters but also parameters that have potential effects on EUI and thermal comfort such as WWR. SA has the complementary role of ordering by importance, the strength, and relevance of the inputs in determining the variation in the output. The SA results are determined and motivated by the thermo-physical characteristic, and also affected by the uncertainty of input variables [41]. For variables that are highly correlated in thermo-physical properties, it is also possible to have a relatively low order of influence when the parameter uncertainty (constrained by PH standards) is small.

For the EUI, PRCC and $R^2$ of the regression model for different sample sizes are exhibited in Fig. 6 and Table 4. For different sample sizes, the PRCCs are slightly different but the overall trend can be used as the basis for measuring important variables, and the fitting performance of the regression model is perfect with $R^2$ higher than 0.90. This indicates that the regression analysis model is robust. ACH ($x_9$) is recognized as the most important contributor. It accounts for over 95% of the explainable output variation. The U-value of the external wall ($x_1$) and roof ($x_4$), as well as the WWR of the south ($x_{14}$) are ranked after and contribute about 40%. The U-value of the external window ($x_7$), the SHGC ($x_8$) and WWR of the north ($x_{16}$) have some influence with PRCC about 30%. The solar absorptance of coating ($x_{10}$ and $x_{11}$) also has some influence on PRCC, about 10%. The remaining factors are considered relatively less important with individual contributions less than 10%. In addition, the impact of variables on the annual cooling load and the annual heating load also are shown in Fig. 6. The results of SA of EUI are different from both HEUI and CEUI, which indicates that the EUI is not only determined by the cooling or the heating energy demand.

Finally, obtaining the PRCC indices of CTR. The model achieved acceptable fitting performance with $R^2$ of 0.83. For CTR, the density ($x_5$) and heat capacity ($x_6$) of roof and SHGC ($x_8$) are the most important factors with PRCC around 0.6. Followed by WWR ($x_{13}$-$x_{16}$) and the length of overhang ($x_{19}$). The U-value of window ($x_7$), ACH ($x_9$), building orientation ($x_{12}$) and fin depth ($x_{20}$) have almost no impact on CTR.

For the cold climate zone, the rank and the magnitude of the influence of input variables are not consistent for EUI and CTR. Contrary to EUI, the effect of ACH ($x_9$) on CTR is largely negligible. This is because natural ventilation which is used during the transition season weakens the effect of airtightness on the indoor temperature. However, during the cooling and heating seasons, the external windows are closed, so the ACH will have a large impact on the load. EUI is more sensitive than CTR to the U-value of the wall,
roof, and windows. The density and heat capacity of the roof has little effect on EUI, but it is an important factor in CTR. But there are some commonalities, for example, the density and heat capacity of the external wall, the fin depth (x20) and orientation (x12), the U-value of the floor (x7) have little impact on EUI and CTR.

The sign of the PRCC indicates whether the relationship between input variables and output variables is positive or negative. WWR (x13-x16) is positively correlated with energy-related performance but negatively with CTR. This means that smaller WWR is required to improve indoor comfort. Nevertheless, the premise is that the requirements of indoor natural lighting must be met. The solar absorbances (x10 and x11), overhang height (x18), ACH (x9), U-value of roof (x4) and the SHGC (x8) are positively correlated with EUI, and the length of the overhang (x19) is negatively correlated with EUI. For CTR, the result is just the reverse.

4.2. Redundancy analysis

The RDA method can quantify the explanation and significances the explanatory variables to the overall response variables including EUI and CTR. Table 5 presents and explains and significance, other than x2, x20, x3, x12 and x20. The effect of the remaining explanatory variables on the response variables is significant with p less than 0.05. Taking two response variables as a whole, the explanatory variables of the top seven variables are, from high to low, x9, x8, x5, x6, x14, x16, and x19, each explaining more than 1% of the response. In subsequent optimization analysis, variables with insignificant effects were removed to reduce the complexity of the optimization model.

Table 5

<table>
<thead>
<tr>
<th>Name</th>
<th>Explains</th>
<th>% pseudo-F</th>
<th>P</th>
<th>P (adj)</th>
</tr>
</thead>
<tbody>
<tr>
<td>x0</td>
<td>42.1</td>
<td>799</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x3</td>
<td>10.8</td>
<td>252</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x4</td>
<td>10.1</td>
<td>301</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x6</td>
<td>6.8</td>
<td>248</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x14</td>
<td>7</td>
<td>330</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x16</td>
<td>3</td>
<td>162</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x19</td>
<td>2.8</td>
<td>173</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x4</td>
<td>0.9</td>
<td>61.4</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x1</td>
<td>0.8</td>
<td>54.4</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x15</td>
<td>0.7</td>
<td>47.2</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x13</td>
<td>0.5</td>
<td>33.9</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x7</td>
<td>0.3</td>
<td>22.1</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x11</td>
<td>0.3</td>
<td>19.9</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x18</td>
<td>0.2</td>
<td>18</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x10</td>
<td>0.2</td>
<td>17.2</td>
<td>0.002</td>
<td>0.04</td>
</tr>
<tr>
<td>x2</td>
<td>&lt;0.1</td>
<td>2.1</td>
<td>0.128</td>
<td>0.64</td>
</tr>
<tr>
<td>x20</td>
<td>&lt;0.1</td>
<td>1.6</td>
<td>0.188</td>
<td>0.752</td>
</tr>
<tr>
<td>x3</td>
<td>&lt;0.1</td>
<td>1.4</td>
<td>0.236</td>
<td>0.752</td>
</tr>
<tr>
<td>x12</td>
<td>&lt;0.1</td>
<td>0.8</td>
<td>0.432</td>
<td>0.864</td>
</tr>
<tr>
<td>x17</td>
<td>&lt;0.1</td>
<td>0.6</td>
<td>0.61</td>
<td>0.864</td>
</tr>
</tbody>
</table>

4.3. Meta models

Based on the GBDT algorithm, meta-models of building performance were established. Trading off the calculation time and reliability, the overall sample size is set to 1100 and randomly divided into two parts, of which 1000 cases are used as training sets and 100 cases are used as test sets. Two commonly used algorithms, SVM and ANN, were used to verify the reliability of the GBDT method.

The setting of hyperparameters has important influences on model accuracy. The main parameters affecting the GBDT model include the maximum depth of trees (MD), the number of trees (NT), the maximum of features (MF) and the learning rate (LR). The SVR model has two crucial parameters: c and γ. The c is the penalty factor, which is the tolerance for error. The γ is the coefficient of the kernel function, which implicitly determines the distribution of the data after mapping to the new feature space [76]. For ANN, the activation and training functions are “tansig” and “trainld”, respectively. The number of hidden layer nodes and learning rates are their main parameters. The parameter settings of three algorithms after optimization are shown in Table 6.

The linear fit between predicted and simulation results and their R² are shown in Fig. 7 and Table 7, respectively. The comparison shows that the fitting performance of the GBDT model is superior to other models as a whole with the R² of EUI and CTR being 0.996 and 0.935, respectively. Table 7 presents the accuracy evaluation indices for the two objectives. Besides SVM, GBDT and ANN also meet the requirements of ASHRAE Guideline 14—2002 with NMSE and CVRMS less than 5% and 15%, respectively. In particular, the GBDT model, NMSE of EUI and CTR are 2.45% and 1.78%, and CVRMS of EUI and CTR are 3.36% and 2.36%.

In addition, the model robustness is also important, which represents the versatility for all building performance indicators. The standard deviation of R² for EUI and CTR is used as the robustness indicator (shown in Fig. 8). It can be seen that the robustness of GBDT is the best with the standard deviation at 0.048, followed by ANN and SVM.

In summary, the GBDT model is superior in terms of robustness and fit and was chosen to construct the fitness function of the optimized model.

4.4. Multiply optimization and evaluation

The building performance model established by GBDT can participate in multi-objective optimization as adaptive functions in the genetic algorithm. The optimization objectives are to minimize the EUI and maximize CTR in this paper. In order to cope with the two opposite optimization goals of minimizing and maximizing, the minimization convention is generally followed. Therefore, the minimization of discomfort (DCTR = 1-CTR) is used instead of CTR. In terms of the NSGA-II algorithm, the roulette selection method and two-point cross are selected. Several other important optimization settings, including the population size, number of maximum generations, generation gap, crossover and mutation probability are summarized in Table 9, according to a statistical summary of existing literature and an adaptive variation of optimization configurations [77].

Table 6

<table>
<thead>
<tr>
<th>Model</th>
<th>Parameter</th>
<th>DCTR</th>
<th>EUI</th>
</tr>
</thead>
<tbody>
<tr>
<td>GBDT</td>
<td>subsample</td>
<td>0.8</td>
<td>0.8</td>
</tr>
<tr>
<td>SVM</td>
<td>c</td>
<td>0.1</td>
<td>0.1</td>
</tr>
<tr>
<td>ANN</td>
<td>Iterations</td>
<td>10000</td>
<td>10000</td>
</tr>
<tr>
<td></td>
<td>Convergence error</td>
<td>0.00001</td>
<td>0.00001</td>
</tr>
<tr>
<td></td>
<td>LR</td>
<td>0.01</td>
<td>0.01</td>
</tr>
<tr>
<td></td>
<td>The number of hidden layer nodes</td>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>
optimized EUI and DCTR both fluctuate within a small range with a variation of 13.1–14.1 kWh/(m²a) and 13.1–13.3%, respectively. The CEUI and HEUI constraints of the PH standard are less than 16.73 kWh/(m²a) and 15 kWh/(m²a), respectively. The corresponding CEUI of the Pareto frontier solution is approximately 13.4–14.6 kWh/(m²a), while the HEUI is substantially lower than 1 kWh/(m²a), which is obviously meeting constraints. In addition, the EUI and CTR of the base-case building are known to be 111.2 kWh/(m²a) and 63.0%, respectively. Therefore, the energy-saving rate of EUI is about 88.2% and the improvement rate of CTR is about 37.8%. In short, in the case of reasonable design and operation, the overall performance of PH buildings can be greatly improved.

In order to more intuitively display the distribution of design variables corresponding to the Pareto frontier solution, it is normalized as shown in Fig. 10. Some variables such as x5, x6, and x19 are concentrated in the upper limit of the constraint range, and its correlation with all optimization targets is negative. The larger the value, the better the optimization goal. Therefore, the value of these variables should be as large as permitted under the circumstances. Some variables are all distributed at the lower boundary of the constraint range, and these variables are positively correlated with all variables (x7, x8, x9, x13, x14, x15, and x16). Therefore, the design should be as small as possible. There are also some variables that are distributed almost throughout the constraints, such as x1, x7, x10, x11, and x18. These variables have

Table 7
The R² between the predicted and simulated results.

<table>
<thead>
<tr>
<th>Objective</th>
<th>GBDT</th>
<th>SVM</th>
<th>ANN</th>
</tr>
</thead>
<tbody>
<tr>
<td>EUI</td>
<td>0.996</td>
<td>0.910</td>
<td>0.938</td>
</tr>
<tr>
<td>CTR</td>
<td>0.935</td>
<td>0.842</td>
<td>0.820</td>
</tr>
</tbody>
</table>

Table 8
Accuracy metrics.

<table>
<thead>
<tr>
<th>Objectives</th>
<th>CVRMSE</th>
<th>NMSE</th>
<th>GBDT</th>
<th>SVM</th>
<th>ANN</th>
</tr>
</thead>
<tbody>
<tr>
<td>EUI</td>
<td>3.36</td>
<td>5.96</td>
<td>4.53</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CTR</td>
<td>2.36</td>
<td>4.06</td>
<td>2.59</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NMSE</td>
<td>1.78</td>
<td>3.3</td>
<td>2.00</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 9
The setting of the NSGA-II algorithm.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Population size</td>
<td>100</td>
</tr>
<tr>
<td>The number of maximum generation</td>
<td>500</td>
</tr>
<tr>
<td>Generation gap</td>
<td>0.5</td>
</tr>
<tr>
<td>Crossover probability</td>
<td>0.8</td>
</tr>
<tr>
<td>Mutation probability</td>
<td>0.6</td>
</tr>
</tbody>
</table>

Fig. 7. The fitting curve between predicted and simulated results.

Fig. 8. Robustness evaluation of meta-models.

Fig. 9. Pareto optimization solution.
different correlation directions for the two optimization goals, and the difference in the degree of relevance is not very large. Taking \( x_1 \) as an example, the conventional approach is to make the U-value as small as possible, but in the multi-objective trade-off design, the optimization value is in the middle of the recommended value of PH standards. This shows that the integrated design of the building ontology is necessary.

4.5. Economic analysis

An economic analysis is performed in order to investigate the cost-effectiveness of the optimal solutions. Through the investigation of 20 high-performance buildings in the climate, the common insulation materials are summarized in Fig. 11. Rock wool and XPS are the most commonly used materials for walls and roofs, respectively. The market price of rock wool and XPS per square meter is 0.3 and 0.5 CNY/(mm thickness). According to Table 2, the U-value of the wall and roof of the base building are 0.45 and 0.7 W/(m²K), and the cost of corresponding insulation materials is 7.2 and 23.7 CNY/m² respectively. The external window of the basic building has a U-value of 2.5 W/(m²K) and the corresponding type of external window is plastic steel (5 mm + 12 mm Air + 5 mm) with the market price being 310 CNY/m². In addition, since the U-value and SHGC of windows corresponding to Pareto frontier solution are concentrated around 1 W/(m²K) and 0.18, it can be realized by adjusting the air layer thickness, so the window price can be considered the same with a market price of 483 CNY/m² [plastic steel window (5 mm low-e + 13 mm Air + 5 mm + 13 mm Air + 5 mm)].

Calculated according to Eqs. (17) and (18), \( C_i \) and \( C_o \) of the base building are 96.6 and 107.8 RMB/m², respectively, and the corresponding cost of the Pareto frontier solution is shown in Fig. 12. There is an exponential relationship between \( C_i \) and \( C_o \) (R² = 0.73), and with the increase of \( C_i \), \( C_o \) tends to be stable. Further, the payback period is used to integrate \( C_i \) and \( C_o \). The shorter the payback period, the better the economic benefit, so it is used to the final decision making on the Pareto frontier solution. As can be seen from Fig. 13, there is generally a positive correlation between the payback period and the DCTR. The optimal solution is present, with the payback period and DCTR of 0.48 years and 13.1%, respectively.

5. Conclusion

This paper proposes a multi-objective optimization method for PH design, and the cold climate zone is chosen as an example to construct the multi-objective optimization model. Annual energy demand and comfort level are used as optimization objectives, and the boundaries of design parameters, annual cooling, and annual heating energy demand are used as constraints. The proposed three-stage optimization design method can reduce the complexity of the model and improve optimization accuracy and efficiency.

The main conclusions are as follows:

1) Linear regression-based PRCC sensitivity indicators were used to analyze the correlation between design variables and building performance indicators. To increase reliability, repeated tests...
were performed on the SA and results show that the PRCC at different tests is slightly different, but the overall trend can be used as a basis for measuring important variables. The fitted MLR model achieved higher robustness with the CEUI, HEUI, EUI, and CTR, R² being 0.92, 0.85, 0.92 and 0.84, respectively. 

2) The pre-RDA method is used for dimensionality reduction, which can provide the importance ranking and significance of design parameters to the overall optimization objectives. Compared to SA, this method reduces the influence of subjective judgment and is more suitable for multi-objective optimization problems. RDA shows that the impact of five variables (the density of wall, the fin depth, the specific heat of wall, the orientation, and the U-value of the floor) is not significant with
p<0.05. Therefore, these variables were excluded from the problem space for further optimization.

3) This study is the first one in which the GBDT algorithm has been implemented to study a PH building. It outperformed other commonly seen big data algorithms such as SVM and ANN in our experiment. Meta-model based on GBDT algorithm meets the requirements of ASHRAE with NMBE and CVMRE of EU and CTR are 2.45%, 3.36%, 1.78%, and 2.36%, respectively. An indicator is proposed to evaluate the robustness of the model. The meta-model based on GBDT with the standard deviation at 0.048, is more robust than several existing advanced models.

4) By using the GBDT-based NSGA method, the optimized solutions of EU and CTR are 13.1 kWh/(m²a) — 14.1 kWh/(m²a) and 86.7 — 86.9%, respectively. The energy-saving rate of EU is about 82.2% and the improvement rate of CTR is about 63.0% compared with the base-case building.

5) Implement an economic analysis of the Pareto frontier solution. There is an exponential relationship between $C_i$ and $C_e$ ($R^2 = 0.73$), and with the increase of $C_i$, $C_e$ tends to be stable. The $C_i$ and $C_e$ of the base building are 96.6 and 107.8 CVN$/m^2$, respectively. Further, the payback period is used to integrate $C_i$ and $C_e$. The shorter the payback period, the better the economic benefit; so it is used to the final decision making on the Pareto frontier solution. There is generally a positive correlation between the payback period and the DCTR. The optimal solution is present, with the payback period and DCTR of 0.48 years and 13.1%, respectively.

This study can provide a reference for the integrated design of Passive house buildings. It can be further extended to other fields, such as building energy-saving renovation, early performance design of buildings of different types or located in different regions.

Declaration of competing interest

The authors declared that they have no conflicts of interest to this work.

We declare that we do not have any commercial or associative interest that represents a conflict of interest in connection with the work submitted.

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