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# Composite solution to the neutron lifetime anomaly

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Measurements of the lifetime of neutrons trapped in a bottle have been consistently shorter than the lifetime measured in neutron beam experiments. With trapping potentials as low as 50 neV and neutron detectors located only at the top of the bottle, this discrepancy could be the result of the soft scattering of dark matter with neutrons. However, it is challenging to obtain the observed loss rate in conventional models of dark matter scattering. We show that this phenomenology is possible in composite models of dark matter where the soft scattering is from dark matter that has been captured and accumulated in the Earth. This solution can be tested by placing more neutron detectors around the trap, providing better angular coverage. The phenomenology of soft scattering by trapped composite dark matter is generic and suggests new experimental directions that could be pursued to detect this large class of models.

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## I. INTRODUCTION

The lifetime of the neutron, a number of fundamental importance to big bang nucleosynthesis, has recently become a topic of contention. A persistent discrepancy at the level of  $3.9 \sigma$  has been reported between two different techniques used to measure this lifetime. The first technique measures the lifetime by looking at the decay of free neutrons in a beam. In this method, the decay is identified by the presence of charged particles produced as a result of the decaying neutron. Based on the rate of appearance of charged particles, this measurement yields a lifetime of  $887.2 \pm 2.2$  s [1]. In the second method, the lifetime is measured by counting the surviving number of trapped ultracold neutrons, yielding a lifetime of  $877.7 \pm 0.7$  s [2], shorter than the measured lifetime in the beam experiments by 9.2 s. These results suggest that neutrons are being lost from their trap without the production of charged particles.

An enticing avenue to explain this anomaly is to consider the possibility of new interactions between neutrons and the dark sector. A well-explored option is to consider the possibility of the neutron decaying invisibly into dark sector particles [3]. While possible, this option is heavily

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constrained by the stability of nuclei, requiring the existence of a dark particle that is nearly degenerate with the neutron. The existence of such states may also potentially destabilize neutron stars [4] and thus require more exotic nuclear equations of state. Stringent limits on such models also arise from the stability of hydrogen atoms [5]. Given these theoretical challenges, it is interesting to explore other phenomenological avenues to explain this anomaly.

In this paper, we explore the possibility that the loss of ultracold neutrons from the trap is due to scattering between neutrons and dark matter. This is a plausible direction, since these ultracold neutrons are trapped by a confining potential  $\lesssim 50 \text{ neV}$  [2], making it possible for even soft collisions to cause loss from the trap. The loss of neutrons through energy exchange between them and the environment is a significant systematic in the trapped neutron experiments, and there are thus experimental checks on this possibility [2]. However, these checks are aimed at constraining two loss mechanisms. The first involves collisions between neutrons and background gas. Experimentally, this possibility is constrained by ensuring that the quality of the vacuum in the trap is sufficiently good. The second involves the exchange of energy between the neutrons and the magnetic fields used to confine them. In this case, the neutron gains energy slowly and thus rises slowly up the trap. A neutron detector that is sensitive to soft neutrons is placed at the top of the trap, and the activity in this detector is used to constrain loss in this channel. But, if the neutron undergoes a scattering event that can give it a sudden kick ≥50 neV along any direction, this cross-check is inefficient due to the small solid angle subtended by this detector in the trap [6]. Since the experiments allow for the scattering of dark matter with the neutrons to explain this discrepancy, it is interesting to ask what class of dark matter models could accomplish this phenomenology while being otherwise unconstrained by other experiments.

It is challenging to explain this anomaly through the scattering of dark matter with neutrons. First, in order to efficiently kick the neutrons, the dark matter has to be reasonably massive. Second, there needs to be enough of this dark matter in the trap in order to account for the observed rate. It can be verified that these requirements cannot be satisfied with the Galactic dark matter population. This problem can be overcome if we instead consider the dark matter population that is captured and bound to the Earth. This captured dark matter can have significant overdensities [7]. While slower than the Galactic dark matter, this population is nevertheless hot enough to deposit the  $\approx$ 50 neV of energy necessary to kick the neutrons out of the trap. The captured dark matter needs to have a mass in the ≈GeV range to have a significant abundance on the surface of the Earth: lighter dark matter evaporates, while heavier dark matter might sink to the core. Furthermore, even in the GeV range, despite the large abundances, dark matter mediator couplings larger than unity are required to create a large enough neutron disappearance rate that would explain the bottle-beam discrepancy.

We show that the required dark matter density and cross section that is consistent with all observational constraints can be realized in models of composite dark matter. Specifically, we consider dark matter blobs consisting of a large number of dark partons, which results in a large dark charge under a long-range force. Low-momentum scattering between this blob and the standard model via this longrange (~ micron) fifth force is coherently enhanced. This enhanced cross section permits the blobs to be captured in the Earth. Due to the large self-scattering between blobs, a small initial density of captured blobs can seed the capture of additional blobs, resulting in the rapid growth of blob density. In the range of parameters allowed by current experimental constraints, this growth is only possible when there is a distribution of blob masses; i.e., we will consider a small number of heavier blobs that stop and sink deeper into the Earth. Lighter blobs will scatter off these heavier blobs and get captured. Note that such a distribution in blob masses is to be expected in composite dark matter scenarios, since composite systems generically produce such a distribution during "blob nucleosynthesis." These blobs can then undergo the soft scattering needed to explain the lifetime of the trapped neutrons. Experiments that probe terrestrial dark matter at larger momentum transfer such as cryogenics [8], dilution refrigerators [9], and metastable isomers [10] are suppressed due to the momentumdependent form factor for long-range interactions or due to loss of coherence. With large cross sections, the thermalized dark matter or atmospheric overburden slows incoming dark matter down to energies undetectable at even surface experiments like SENSEI [11] or CRESST [12].

The rest of this paper is organized as follows: in Sec. II, we describe a simple model of the blob, and in Sec. III, we describe its captured population on the Earth. In Sec. IV, we evaluate the parameters necessary to explain the lifetime of the trapped neutrons, and in Sec. V, we discuss existing experimental limits on this parameter space. Finally, we conclude in Sec. VI, where we discuss future experimental prospects, both to constrain this particular explanation for the trapped neutron lifetime and to comment more generally on how these kinds of dark matter phenomenology can be probed.

## II. MODEL

We consider dark matter f with mass  $m_f$  that is part of a strongly coupled sector that confines at a scale  $\Lambda_f \approx m_f$ . The f particles are gauged under a vector A with mass  $m_A$  and gauge coupling  $g_f$ . The neutron (or proton) is assumed to have a "dark electric dipole moment" with this vector.

$$\mathcal{L} \supset \frac{1}{\Lambda} \bar{n} \sigma_{\mu\nu} \gamma_5 F_A^{\mu\nu} n + \bar{f} (m_f + D_A^{\mu} \gamma_{\mu}) f + m_A^2 A^2. \tag{1}$$

We assume  $\Lambda \sim 3 \times 10^8$  GeV to be consistent with supernova constraints [13,14].

At temperatures below  $\Lambda_f$ , we assume that the dark sector forms blobs with charge  $g_{\text{blob}} = N_f g_f$  and mass  $m_{\text{blob}} = N_f m_f$ . We make the simplifying assumption that all f-type dark matter is in blobs. We do not need all of the dark matter to be in these blobs—the fraction that is in blobs is denoted by  $f_{\text{blob}}$ .

For fermions, stability of these blobs requires [15]

$$N_f \lesssim \frac{1}{g_f^3} \Rightarrow N_f g_f = g_{\text{blob}} \lesssim \frac{1}{g_f^2}$$
  
 $\Rightarrow g_{\text{blob}}^3 \lesssim N_f^2 \Rightarrow N_f \gtrsim g_{\text{blob}}^{\frac{3}{2}}$  (2)

Let us assume  $N_f = \chi g_{\text{blob}}^{\frac{3}{2}}$ . When  $\chi \gtrsim 1$ , the blob satisfies the above constraint. But this is not a strict constraint, and it can be overcome by further model building—for instance, using a tuned long-range attractive force that cancels against the negative potential energy due to the vector A. For this reason, we take the above bound to be a tuning line rather than a strict bound and will consider situations where  $\chi \lesssim 1$ , where the model is tuned. Now,

$$\Lambda_f \approx m_f = \frac{m_{\text{blob}}}{N_f} \approx \frac{m_{\text{blob}}}{\chi g_{\text{blob}}^{\frac{3}{2}}}.$$
 (3)

The size of this blob is

$$R_{\text{blob}} = \frac{N_f^{\frac{1}{3}}}{\Lambda_f} = \frac{\chi^{\frac{4}{3}} g_{\text{blob}}^2}{m_{\text{blob}}}.$$
 (4)

This gives us a maximum momentum transfer,

$$q_{\text{max}} = \frac{m_{\text{blob}}}{\chi^{\frac{4}{3}} g_{\text{blob}}^2},\tag{5}$$

above which coherent enhancement over the whole blob is lost.

## III. CAPTURE

The dark matter blobs fall on Earth, and a fraction gets captured if it slows down to velocities below the escape velocity. At large charge  $g_{\text{blob}} \ge 10^9$ , this could be due to scattering with rock, and at smaller charge it needs to be aided by a secondary population of blobs with larger mass (and charge). Additional detail for capture is presented in the Appendix. For the remainder of this work, we assume that 100% of infalling dark matter is captured over the Earth's history. The average dark matter density on Earth is

$$\langle n_{\rm DM}^{\rm terr} \rangle = \frac{\pi r_E^2}{\frac{4}{3} \pi r_E^3} n_{\rm DM}^{\rm vir} v_{\rm vir} \approx \frac{10^{15}}{\rm cm^3} \frac{T_E}{10^{10} \text{ year}} f_{\rm blob} \frac{\rm GeV}{m_{\rm blob}}.$$
 (6)

Here  $r_E \approx 6400$  km is the radius of the Earth,  $n_{\rm DM}^{\rm vir} \approx \frac{0.3}{{\rm cm}^3} f_{\rm blob} \frac{{\rm GeV}}{m_{\rm blob}}$  is the number density of the virial population,  $v_{\rm vir} \approx 300$  km/s is the dark matter virial velocity, and  $T_E \approx 10^{10}$  year is the age of the Earth.

# A. Thermalized GeV DM population

For the cross sections we consider, capture initially occurs all over the Earth and is immediately followed by thermalization; this initial density is expected to be uniform over the volume of the Earth. Subsequently infalling dark matter gets stopped by the first few layers of terrestrial DM. This thermalized dark matter population has rms velocity  $v_{\rm th} \approx \sqrt{T_{\rm room}/m_{\rm blob}}$  with the temperature  $T_{\rm room} \approx 300$  K, the room temperature. There is, however, subsequent diffusion, with DM diffusing in time  $T_E$  a distance of

$$R_{\text{diff}} = \frac{1}{n_{\text{blob}}\sigma_T} (n_{\text{blob}}\sigma_T v_{\text{th}} T_E)^{\frac{1}{2}}$$

$$\approx 10^5 \text{ km} \frac{m_A}{10 \text{ eV}} \sqrt{\frac{10^{14}/\text{cm}^3}{n_{\text{blob}}}} \left(\frac{\text{GeV}}{m_{\text{blob}}}\right)^{\frac{1}{4}} \gtrsim R_E. \quad (7)$$

Thus, DM spreads all over the Earth.

Temperature and density variations, as well as gravity, can significantly modify the density profile on Earth. This Jeans density,  $n_{\rm jeans}$ , was calculated in Ref. [16], and it was shown that DM with masses around 1 GeV has a peaked distribution near the Earth's surface. While DM

lighter than 1 GeV evaporates, DM heavier than 1 GeV sinks towards the Earth's center. However, the presence of self-interactions can arrest sinking.

# B. Maximum packing

When the mediator is a vector, there are strong repulsive forces between blobs that set a limit on the local density. The minimum interblob distance  $r_{\text{int}}$  is given by solving

$$\frac{g_{\text{blob}}^2}{4\pi} \frac{e^{-m_A r_{\text{int}}}}{r_{\text{int}}} = T_{\text{room}}.$$
 (8)

To a very good approximation, this is given by

$$n_{\text{max}} \approx \frac{2 \times 10^{13}}{\text{cm}^3} \left(\frac{m_A}{10 \text{ eV}}\right)^3 \left(\frac{\log 10^4}{\log g_D}\right)^{3.4}.$$
 (9)

When  $m_{\rm blob} \geq 1$  GeV, evaporation is negligible [16]. In this limit, if  $n_{\rm max} \lesssim n_{\rm DM}^{\rm terr}$ , then the local density anywhere on Earth is set by  $n_{\rm max}$ . This effectively arrests sinking even for larger blob masses, since the inner regions of the Earth are saturated in blobs. If, instead,  $n_{\rm max} \gg n_{\rm DM}^{\rm terr}$ , then  $n_{\rm jeans}$  sets the local number density.

In scenario A, we will assume that an appropriate mediator mass  $m_A$  can be chosen such that  $n_{\rm max} \approx n_{\rm DM}^{\rm terr}$ , hence the surface density is simply given by  $n_{\rm surf} = n_{\rm DM}^{\rm terr}$  at all masses above 1 GeV. Below 1 GeV, we account for evaporation effects as treated in Ref. [16].

In scenario B, we will assume that the mediator mass is large enough such that  $n_{\text{max}} \gg n_{\text{DM}}^{\text{terr}}$ , and assume  $n_{\text{surf}} = n_{\text{jeans}}$  taken from Ref. [16].

## IV. NEUTRON BOTTLE

The neutron bottle experiments are first summarized in Table I.

We will assume that a transfer of energy larger than half of the trapping potential—i.e.,  $E_{\rm trans} > 50~{\rm neV}$ —is sufficient to kick the neutrons. This sets the minimum momentum transfer at  $q_{\rm min} = \sqrt{2E_{\rm trap}m_n} \approx 9~{\rm eV}$ . The cross section to kick neutrons from the trap is given by

$$\sigma_{\text{neut}} = \int dq^2 \frac{d\sigma}{dq^2}.$$
 (10)

Hence,

$$\sigma_{\text{neut}} = \frac{4g_{\text{blob}}^2}{\pi \Lambda^2 v_{\text{th}}^2} \frac{\log (m_A^2 + q_{\text{max}}^2)}{\log (m_A^2 + q_{\text{min}}^2)}$$

$$\approx 10^{-34} \text{ cm}^2 g_{\text{blob}}^2 \frac{m_{\text{blob}}}{\text{GeV}} L_R(q_{\text{min}}), \qquad (11)$$

where the log ratio  $L_R(q_{\min}) = \frac{\log{(m_A^2 + q_{\max}^2)}}{\log{(m_A^2 + q_{\min}^2)}}$ , and  $v_{\text{th}} = \sqrt{\frac{2T_{\text{room}}}{m_{\text{blob}}}}$  is the thermal velocity at room temperature. Here  $q_{\max}$  is the maximum momentum transfer set by

Experiment	Description	Trap potential [neV]	Lifetime
Pattie, Jr. 18 [2]	grav + magnetic no extrapolation	50	$877.7 \pm 0.7 + 0.4 / -0.2$
P. Serebrov 18 [17] UCN	grav + oil	70	$881.5 \pm 0.7 \pm 0.6$
ARZUMANOV 15 [18]	Double bottle	100	$880.2 \pm 1.2$
STEYERL 12 [19]	Material bottle	106	$882.5 \pm 1.4 \pm 1.5$
PICHLMAIER 10 [20]	Material bottle	106	$880.7 \pm 1.3 \pm 1.2$
SEREBROV 05 [21]	grav + oil trap	106	$878.5 \pm 0.7 \pm 0.3$

TABLE I. Summary of the neutron bottle experiments.

$$q_{\text{max}} = \text{Min}(R_{\text{blob}}^{-1}, \mu v_{\text{th}}). \tag{12}$$

In order to explain the bottle-beam discrepancy,

$$\Gamma_{\rm DM} + \Gamma_{\rm beam} = \Gamma_{\rm bottle},$$

$$n_{\rm surf} \sigma_{\rm neut}^{\rm exp} v_{\rm th} + \frac{1}{\tau_{\rm beam}} = \frac{1}{\tau_{\rm bottle}}.$$
(13)

With  $\tau_{\text{beam}} = 888 \text{ s}$ ,  $\tau_{\text{bottle}} = 879 \text{ s}$ . For thermalized DM, we require

$$\sigma_{\rm neut}^{\rm exp} = 5.35 \times 10^{-25} \ {\rm cm^2} \sqrt{\frac{m_{\rm blob}}{\rm GeV}} \frac{10^{14}/{\rm cm^3}}{n_{\rm surf}}. \eqno(14)$$

Equating Eq. (14) with Eq. (11), we get

$$g_{\text{blob}} \approx \frac{7.1 \times 10^4}{\sqrt{L_R(9 \text{ eV})}} \left(\frac{\text{GeV}}{m_{\text{blob}}}\right)^{\frac{1}{4}} \sqrt{\frac{10^{14}/\text{cm}^3}{n_{\text{surf}}}}.$$
 (15)

This  $g_{\text{blob}}$ , which explains the neutron lifetime anomaly, is plotted as a function of  $m_{\text{blob}}$  for different values of  $f_{\text{blob}}$ , the fraction of Galactic dark matter in blobs, in Fig. 1, approximating  $L_R(9 \text{ eV}) \approx 2$ . Also shown for reference is

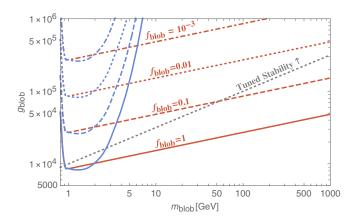


FIG. 1. The blob coupling  $g_{\text{blob}}$  that explains the observed neutron lifetime anomaly is shown as a function of mass of the blob  $m_{\text{blob}}$  for different  $f_{\text{blob}}$ , the fraction of dark matter in blobs. The red curves correspond to scenario A, while scenario B is shown in blue. The region above the gray dashed line is tuned due to stability considerations.

the stability line in gray for  $q_{\rm max} = R_{\rm blob}^{-1} = 10$  eV for  $\chi = 1$  from Eq. (5). Parameter space above this line is tuned. The red lines correspond to scenario A, while blue lines correspond to scenario B. In scenario B, blobs heavier than  $m_{\rm blob} \approx 1$  GeV sink with small number densities at the surface, resulting in astronomically large couplings required at higher masses. In scenario A, the sinking is arrested due to blob-blob repulsions. In both scenarios, there is no viable parameter space below 1 GeV, due to significant evaporation.

We will next deal with limits from current experiments and testability at future experiments.

#### V. DETECTION BY OTHER METHODS

Traditional direct-detection experiments that look for virialized DM will not be sensitive to blobs considered here. This is because the self-interactions rapidly thermalize incoming blobs, such that the blobs do not have enough kinetic energy by the time they reach even surface detectors like SENSEI [11] and CRESST [12]. We will start by considering the heating of cryogenic detectors by blobs.

#### A. Heating of cryogenics

Unlike single-event direct detection, cryogenic detectors work based on the amount of heat supplied onto the detector volume. As a result, sensitivity to smaller momentum transfers is possible. When thermalized blobs enter the detector volume, the energy-averaged cross section is given by

$$\langle \sigma E \rangle = \int \frac{d\sigma}{dq^2} \frac{q^2}{2m_T} dq^2$$

$$= \frac{2g_{\text{blob}}^2}{\pi m_T v_{\text{th}}^2 \Lambda^2} (q_{\text{max}}^2 - q_{\text{min}}^2 + m_A^2 L_R(0)). \quad (16)$$

Here  $m_T$  is the mass of the target atom. The energy deposition rate per target atom is

$$\frac{dH}{dt} = \langle \sigma E \rangle n_{\rm DM} v_{\rm th}. \tag{17}$$

Substituting for  $g_{\text{blob}}$  from Eq. (15), the heating rate caused by DM that can explain the neutron lifetime anomaly is

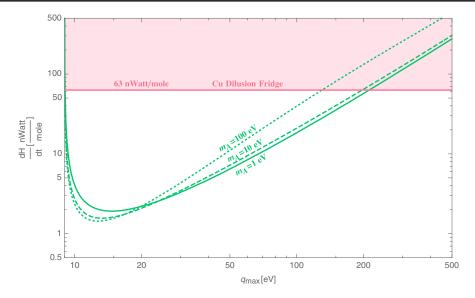


FIG. 2. Contours of the heat deposit rate,  $\frac{dH}{dt}$ , are plotted for different mediator masses  $m_A$  and maximum momentum transfer  $q_{\text{max}} = R_{\text{blob}}^{-1}$ .

$$\frac{dH}{dt}(\text{anomaly}) = \frac{56}{A_T} \frac{\text{nW}}{\text{mole}} \left( \frac{q_{\text{max}}^2 - q_{\text{min}}^2 + m_A^2 L_R(0)}{(10 \text{ eV})^2 L_R(9 \text{ eV})} \right). \tag{18}$$

This is  $m_A$  and  $q_{\rm max}$  dependent. The heat deposit rate  $\frac{dH}{dt}$  due to blobs that explain the neutron lifetime anomaly is plotted in Fig. 2 in green as a function of  $q_{\rm max}$  described in Eq. (12) for different  $m_A$ .  $A_T=63$  corresponds to copper. For this range,  $q_{\rm max}=R_{\rm blob}^{-1}$ .

The heating rates of several cryogenic compounds was investigated in Refs. [16] and [8]. In Ref. [16], the heating rates of helium, hydrogen, nitrogen, oxygen, and argon were reported as a fractional evaporation  $\mathcal{P}/\text{day}$ . This can be converted into heating rate per mole through

$$\frac{dH}{dt} = \frac{\mathcal{P}}{\text{day}} L \times A_T \approx 10 \frac{\mu \text{W}}{\text{mole}} \frac{\mathcal{P}}{0.01} \frac{L}{26 \text{ J/g}} \frac{A_T}{4}. \quad (19)$$

Here L is the latent heat of evaporation. The above equation is normalized to helium and is an order of magnitude larger than Eq. (18), and hence does not constrain. As seen in Table 1 of Ref. [16], the other elements—hydrogen, nitrogen, oxygen, and argon—have much larger latent heat and hence are less constraining. It is also important to remember that the above estimate was made in the transparent Dewar limit, and for large enough cross sections, blobs can thermalize with the outside of the flask and cool, thereby causing lesser heating of the cryogen. Table 1 of Ref. [8] also lists the heating rate in  $\mu$ W/mole. All their limits are larger than  $10~\mu$ W/mole. We find that these limits are subleading compared to those from dilution fridges.

The stability of dilution fridges could also set limits on the heating rate. Roughly, we take this to be  $100 \frac{\text{nW}}{\text{mole}}$  in a 100 g sample of copper [9]. This translates to  $\frac{dH}{dt} = 63 \frac{\text{nW}}{\text{mole}}$ , which is plotted in pink in Fig. 2. The region below this pink curve and above a green curve explains the anomaly and is not constrained yet. All of the parameter space could be tested with sensitivity to a heat deposit rate of about  $1 \frac{\text{nW}}{\text{mole}}$ .

## **B.** High-momentum probes

The orbital decay of Hubble Space Telescope (HST) was used to set limits on strongly interacting models in Ref. [16]. Roughly, the constraint corresponded to

$$\frac{dR}{dt} = 2n\sigma_T \frac{\mu}{m_{\rm HST}} R_{\rm orb} v_{\rm orb}.$$
 (20)

This primarily probes momentum transfers  $\mu v_{\rm orb} \sim 100~{\rm keV}$ , orders of magnitude larger than the inverse size of the blobs we consider. For this reason, blobs which explain the neutron lifetime anomaly predict  $\frac{dR}{dt} \sim 1~\frac{\rm m}{\rm year}$ , while the limit currently is a few orders of magnitude higher at 0.8  $\frac{\rm km}{\rm year}$ .

Metastable tantalum was proposed as a probe of dark matter accumulated on Earth in Refs. [7,10]. However, the momentum transfer required for the deexcitation of tantalum,  $q_0 \approx 1$  MeV, suppresses the long-range force tremendously:

$$\sigma_{\rm Ta} = \frac{\mu g_{\rm SM}^2 g_{\rm blob}^2}{2\pi q_0^3} S(q_0) \approx 10^{-49} \ {\rm cm}^2 \sqrt{\frac{{\rm GeV}}{m_{\rm blob}}} g_{\rm blob}^2 S(q_0), \tag{21}$$

where  $q_0 \approx 12.5$  keV. Note that  $S(q_0)$  is suppressed severely as well for  $q_0 \ll 1$  MeV. As a result, these limits are not relevant either.

The regime relevant to limits from the LHC beam lifetime are around 6.5 TeV [16]. Only inelastic collisions affect the beam as the multipoles correct for small changes in momentum. As a result, this is not expected to constrain these blobs either.

Lastly, anomalous heat transport on the Earth and in the Sun have been used to set limits on exotic matter that has collected over time [22]. However, the self-interaction cross section is so high that thermal conductivity is very low. As a result, these do not set appreciable limits on blobs with large coupling.

## C. Fifth-force experiments

Experiments looking for fifth forces typically operate by measuring the displacement of a test mass due to a force felt by another mass. With 1 s (3000 s) sensitivity, these experiments are sensitive to 0.2 nm displacements with interferometry techniques. We estimate here the displacement caused by the thermal distribution of dark matter blobs on a  $5 \times 10^{-5}$  g test mass.

For a blob that traverses a distance b from the mass, the force is given by

$$F_{\text{blob}} = \sqrt{N_{\text{spin}}} \frac{g_{\text{blob}}}{\Lambda b^3}.$$
 (22)

And hence, the resultant displacement is given by

$$d(b) = \sqrt{N_{\text{spin}}} \frac{g_{\text{blob}}}{m_{\text{test}} \Lambda b^3} \left(\frac{b}{v}\right)^2. \tag{23}$$

The resultant net displacement due to several blobs traversing is obtained by an incoherent sum of these distances and hence given by

$$D^{2} = \int d^{2}(b)f(b)db = N_{\text{spin}} \frac{t}{v^{3}} \left(\frac{g_{\text{blob}}}{m_{\text{test}}\Lambda}\right)^{2} \log\left(\frac{b_{\text{max}}}{b_{\text{min}}}\right). \tag{24}$$

Here  $f(b) = bn_{\text{blob}}vt$ ,  $b_{\text{max}} = \frac{1}{m_A}$ ,  $b_{\text{min}} = R_{\text{blob}}$ , This is approximately

$$D = 10^{-23} \left( \frac{m_{\text{blob}}}{\text{GeV}} \right)^{\frac{3}{4}} \left( \frac{n_{\text{blob}}}{10^{14}/\text{cm}^3} \right)^{\frac{1}{2}} \text{meters.}$$
 (25)

This is orders of magnitude smaller than the sensitivity of interferometers.

# VI. CONCLUSIONS

We have shown that the anomalously small lifetime of the neutron in trapped neutron experiments can be explained by the soft scattering of a bound population of  $\approx$  GeV-scale dark matter with neutrons. This phenomenology is only possible with composite dark matter, where soft scattering can have a considerably larger cross section than hard scattering events, which are otherwise constrained by direct-detection experiments.

This phenomenology motivates two kinds of experimental strategies. First, trapped neutron experiments could check our proposed solution by placing more neutron detectors around the trap, covering a larger solid angle, thus observing the scattered neutrons. It would also be interesting to see if the measured lifetime changes by using a stronger magnetic field to confine the neutrons in the trap. The magnetic trap could potentially be made a factor of 10 times stronger. One might suspect that dark matter models could be constructed to deposit this larger amount of energy. While there is some freedom to do this, the parameter space is constrained by the analysis shown in Fig. 1.

Second, irrespective of the anomaly in the lifetime of the neutron, we have identified a new experimental opportunity in dark matter detection. Composite dark matter naturally gives rise to enhanced soft scattering while having a highly reduced hard scattering cross section. This can lead to a cold population of dark matter with a significantly enhanced number density that is bound to the Earth. This population cannot be detected using conventional dark matter detectors that are aimed at identifying the ionization and scintillation produced as a result of hard collisions. However, the total energy deposited by the dark matter in these soft collisions is quite significant, and it may be possible to detect it using a dedicated setup [23].

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# **APPENDIX: CAPTURE**

Dark matter blobs falling on Earth will get captured if they slow down to velocities below the escape velocity. To estimate the slowdown, we first present the momentum transfer cross section:

$$\sigma_T(v) = \frac{g_{\text{blob}}^2 q_{\text{max}}^2}{8\pi \mu^2 \Lambda^2 v^4}.$$
 (A1)

For initial capture, we require

$$\sigma_{\rm T}(v) \gtrsim \frac{m_{\rm blob}}{\mu n_{\rm rock} R_{\rm Earth}}$$
 (A2)

The coupling capturing all DM incoming with velocity below v corresponds to

$$g_{\rm blob}^{\rm cap}(v) \approx 10^{15} v^2 \frac{10~{\rm eV}}{q_{\rm max}} \frac{\sqrt{\mu \times m_{\rm blob}}}{{\rm GeV}}. \tag{A3} \label{eq:A3}$$

For  $g_{\rm blob} \geq g_{\rm blob}^{\rm cap}(10^{-3})$ ,  $\mathcal{O}(1)$  of incoming blobs is captured. For  $g_{\rm blob} < g_{\rm blob}^{\rm cap}(10^{-3})$ , only a slow-moving fraction  $f_{\rm cap} \propto v^3$  is captured. This leads to a buildup of dark matter on Earth, which is given by

$$\langle R_{\rm DM}^{\rm terr} \rangle = f_{\rm cap}(g_{\rm blob}) \frac{\pi r_E^2}{\frac{4}{3}\pi r_E^3} n_{\rm DM}^{\rm vir} v_{\rm vir}$$

$$\approx \frac{10^5}{\rm cm^3} \frac{1}{\rm year} f_{\rm cap}(g_{\rm blob}) f_{\rm blob} \frac{\rm GeV}{m_{\rm blob}}. \tag{A4}$$

#### 1. Self-interactions

After initial accumulation of DM, self-interactions start becoming important. For blob-blob scattering, the Born approximation is not valid for the large couplings we consider, and we work in the classical regime. The selfinteraction cross section is given by

$$\sigma_{\text{self}} \approx \frac{\pi}{m_A^2} \approx 10^{-9} \text{ cm}^2 \left(\frac{\text{eV}}{m_A}\right)^2.$$
 (A5)

Thus, the self-interactions dominate capture dynamics when

$$n_{\text{blob}}\sigma_{\text{self}} \ge n_{\text{rock}}\sigma_{\text{T}}.$$
 (A6)

We will assume that all self-interactions result in an incoming blob with velocity  $v_{\rm vir}$  transferring half its momentum into thermalized blobs. Hence, incoming and thermalized blobs both leave with velocity  $\frac{v_{\text{vir}}}{2}$  due to a single collision. There is subsequent capture only if the penetration depth of these blob particles is smaller than the depth of the remaining rock or terrestrial dark matter population. Otherwise, this results in a net loss of dark matter on Earth. For large enough coupling, this is a runaway process, and there is 100% capture of virial blobs due to subsequent self-interactions. The exact calculation of this coupling involves multiple levels of blob-blob collisions and will require a Monte Carlo simulation, which we leave for future work. However, considering up to two collisions, we have checked that  $g_{\text{blob}} \gtrsim \frac{1}{4} g_{\text{blob}}^{\text{cap}} (10^{-3})$  is enough to capture close to 100% of all blobs falling in.

By contrast, for a smaller coupling, this leads to negligible buildup due to incoming blobs kicking thermalized blobs out. Number densities are expected to saturate the equality in Eq. (A6)—i.e.,

$$n_{\rm eq}^{\rm kick} \sim n_{\rm rock} \frac{\sigma_{\rm T}}{\sigma_{\rm self}} \approx \frac{1}{{\rm cm}^3}$$
 (A7)

Blobs with small couplings can be captured if there is a secondary population of more massive blobs thermalized on Earth.

## 2. Secondary blobs

We assume that there is a secondary blob population of type B with mass  $m_{\text{blob}}^B$  and charge  $g_{\text{blob}}^B$ , with  $\frac{m_{\text{blob}}^A}{g_{\text{blob}}^A} = \frac{m_{\text{blob}}^B}{g_{\text{blob}}^B}$ Here A-type blobs are the ones populating the Earth's surface and are responsible for the neutron lifetime anomaly. We further assume that B-type blobs have larger mass (and charge)—i.e.,  $m_{\rm blob}^B\gg m_{\rm blob}^A$ —but make up a much smaller fraction of DM,  $f_{\text{blob}}^B \ll f_{\text{blob}}^A$ . This is a natural consequence of dark nucleosynthesis. We will assume that the secondary population satisfies  $g_{\text{blob}}^B >$  $g_{\text{blob}}^{\text{cap}}(10^{-3})$ , such that all of its infalling virial population gets captured. While the incoming A blobs with virial velocity continue to kick the thermalized population of A blobs, they do not carry enough momentum to kick out blobs of type B. Since the self-interaction cross sections are identical for both species, kickout due to A-A selfinteractions become important only when  $n_A \ge n_B$ . However, if

$$n_B \sigma_{\text{self}} R_E \gg 1,$$

$$n_B \gg \frac{1.5}{\text{cm}^3} \left(\frac{m_A}{\text{eV}}\right)^2, \tag{A8}$$

then by the time the A blobs build up to  $n_B$  density, there are enough terrestrial A blobs to absorb all of the momentum from incoming A blobs and prevent subsequent kickout. Then, subsequent self-interactions rapidly build up A blobs, a runaway process which can soon outnumber B blobs due to their superior virial density. Due to their large mass, heavy B blobs subsequently sink to the Earth's core and are a nonfactor in experiments today. Thus, an extremely small number density of a heavier population of blobs can help achieve a near 100% capture of A blobs on Earth.

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