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Accurate two-dimensional eye tracker using first and fourth Purkinje images

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Although a number of devices are currently in use for monitoring eye position, none is both accurate and convenient to use. Methods based on the use of contact lenses can provide high accuracy but have obvious inconveniences. Other techniques—e.g., skin-mounted electrodes, or eyeglass-mounted photoelectric pickups—are relatively convenient, but eye position can be measured to an accuracy of no better than about 0.5° to 1° . A novel eye-tracking instrument has been developed that makes use of two Purkinje images. The instrument operates in the infrared, so that it does not interfere with normal vision; it requires no attachments to the eye; it has a sensitivity and accuracy of about 1 min of arc, and operates over a two-dimensional visual field of 10° to 20° in diameter. The basic principle of the instrument is described, and operating records are shown.

Index Headings: Vision; Optical system; Infrared.

This paper describes a method of eye tracking that is based on the use of a pair of eye reflections that move similarly under translation but differentially under rotation. By monitoring the spatial separation of these two images, eye rotation can be measured accurately without confusion by translation. Similarly, eye translation can be measured accurately without confusion by eye rotation.

I. DOUBLE-PURKINJE-IMAGE METHOD OF EYE TRACKING

The virtual image formed by the light reflected from the front of the cornea is referred to as the first Purkinje image, as shown in Fig. 1. A second Purkinje image, formed by reflection from the rear surface of the cornea, is almost exactly coincident with the first Purkinje image.

The light that is not reflected from either of these surfaces passes through the cornea, passing in turn through the aqueous humor and then the lens of the eye. The third Purkinje image, a virtual image formed by light reflected from the front surface of the lens, is much larger and more diffuse than the others and is formed in a plane far removed from the plane of the other images. The fourth Purkinje image is formed by light reflected from the rear surface of the lens, at its interface with the vitreous humor that fills the bulk of the eyeball. This rear surface of the lens acts as a concave mirror, forming a real image of the source.

The fourth Purkinje image is almost the same size, and is formed in almost exactly the same plane, as the first Purkinje image. However, because the change of index of refraction at the back of the lens is much less than at the air–cornea interface, the intensity of the fourth Purkinje image is less than 1% of that of the first Purkinje image.

If the eye undergoes translation—e.g., due to a lateral head movement—the first and fourth Purkinje images move together through exactly the same distance. If the eye rotates, however, the two images move through different distances and thus change their separation. The physical separation of these two images, therefore, yields a measure of the angular orientation

FIG. 1. Schematic diagram of the eye: PR, Purkinje reflections; IL, incoming light; A, aqueous; C, cornea; S, sclera; V, vitreous; I, iris; L, lens; CR, center of rotation; EA, eye axis; $a \approx 6$ mm, $b \approx 12.5$ mm, $c \approx 13.5$ mm, $d \approx 24$ mm, $r \approx 7.8$ mm.

FIG. 2. Location of the first and fourth Purkinje images for (a) collimated light on the eye axis and (b) collimated light at angle Δ from optic axis of the eye: EA, eye axis; FT, first Purkinje image; FH, fourth Purkinje image; L, lens; C, cornea. The dark section of arc is the equivalent mirror for the fourth Purkinje reflection.

of the eye that is uncontaminated by translational movements.

The instrument described here provides a pair of continuous electrical signals whose magnitudes are proportional to the horizontal and vertical components of separation between the first and fourth Purkinje images of an input pattern of light. This, in effect, provides continuous monitoring of the angular position of the eye, or of the point in space at which the gaze is directed. Errors caused by translation are substantially eliminated; the accuracy is limited, in principle, by the quantum fluctuations in the very-low-intensity fourth Purkinje image.

II. MOVEMENT OF THE PURKINJE IMAGES

Let us consider the positions of the first and fourth Purkinje images in the eye. The first Purkinje image is formed by light reflected from the front surface of the cornea, which has about 7.8-mm radius of curvature. For a distant source, the (virtual) corneal image would be in the plane indicated by the solid dot in Fig. 2(a), i.e., at a distance $r/2 = 3.9$ mm from the front surface of the cornea. The fourth Purkinje image is formed by

light that is refracted by the cornea and the lens, reflected from the rear surface of the lens, and then refracted again by the lens and cornea. A single mirror that would form the identical real image is shown by the heavy line in Fig. 2(a). The radius of this mirror, for relaxed accommodation, is about 5.8 mm and its center C_4 is close to the corneal surface.¹ The position of the (real) fourth Purkinje image is shown by the open dot in Fig. 2(a), and we see that the planes of the first and fourth images are almost identical. (For about 9 diopters of accommodation, i.e., a normal eye focused on a target 11.1 cm from the eye, the equivalent mirror changes to about 5.3-mm radius, with its center shifted slightly farther from the corneal surface; the image plane, however, remains almost constant.)

For purposes of explanation, it is convenient to use the approximation that the equivalent mirror for the fourth Purkinje image has the same curvature as the cornea and that they are separated by exactly their radius of curvature. This configuration resembles a clam-shell arrangement, as shown in Fig. 2(b), C_1 being the center of curvature for the cornea (first Purkinje image) and C_4 the center of curvature for the fourth Purkinje image.

From Fig. 2(b), we see that the distance that each image moves as a consequence of eye rotation is directly proportional to the distance from the center of rotation to the center of curvature of the surface that forms it. These distances are approximately 6 and 13 mm for the first and fourth images, respectively. Thus, when the eye rotates through an angle Δ , with respect to the input axis, the two images, as viewed from the input axis, will move in the same direction and will separate by a distance

$$S \approx 7 \sin \Delta. \quad (1)$$

With respect to eye space, however, i.e., as viewed from the optic axis of the eye,² the images actually move in opposite directions. This is because one image is in front of its center of curvature and the other is behind its center of curvature.

If the eye undergoes translation, both images move through the same distance and direction as the eye. If the eye rotates, however, the two images change their separation. The change of separation between these two images yields a measure of the angular rotation of the eye, and the measure is uncontaminated by lateral movements. The basic action of the eye tracker is to monitor continuously the separation of these two images.

III. DESCRIPTION OF THE EYE-TRACKER SYSTEM

The basic optical system is shown in Fig. 3. Light source S is a GE DFW 500-W projection lamp. Its multiple filaments form a 7-mm square area and it contains a built-in reflector. (Although rated at 120 V,

it is operated at only 70 V in this application.) The light source is imaged by lens L_1 onto stop S_1 , which is a circular aperture 3.4 mm in diameter. Stop S_1 is in the focal plane of lens L_2 and is imaged in the plane of the pupil of the eye, which is located in the focal plane of lens L_3 . The image of S_1 at the eye is approximately 8.5 mm (magnified in the ratio of the focal lengths of lenses L_2 and L_3 , which are 60 and 150 mm, respectively). Stop S_2 , which contains a 2.2-cm round hole, is located in the focal plane of lens L_3 and therefore appears to the eye at optical infinity. All of the light that appears to emanate from stop S_2 passes through the image of S_1 formed at the eye. This input light also passes through a filter F with a pass band between 0.8 and 1.1 μm , and is chopped at 1200 Hz by a chopper wheel, CW, which contains alternating open and closed sectors.

FIG. 3. Schematic of the eye-tracker optical system: VT, visual target; R, allowed range of eye movements; IA, input axis; CA, collecting axis; CA', extension of collecting axis; S, light source; S₁, artificial pupil imaged at pupil of eye; CW, chopper wheel; S₂, source of Purkinje pattern, imaged at infinity; DC, dichroic mirror; M, front surface mirror; M_x and M_y, motors that drive M in *x* and *y* direction, respectively; BS, beam splitter; P₁ and P₄, quadrant phototubes; A₄, aperture in front of P₄. Focal lengths of lenses L₂, L₃, and L₄ are 60, 150, and 90 mm.

FIG. 4. Photocell connections: M_x and M_y , signals that drive the two-dimensional mirror in x and y , P_x and P_y , motors that drive P_4 in x and y directions.

First and fourth Purkinje images of stop S_2 are formed approximately in the plane of the eye pupil. These images are reduced in size by the ratio of the focal lengths of lens L_3 and the equivalent Purkinje mirrors and thus are about 0.57 and 0.43 mm in diameter, respectively. Light from these images is in turn reflected by a dichroic mirror, DC, reimaged by lens L_4 (a pair of back-to-back 180-mm focal length $f/3.1$ achromatic lenses), reflected by mirror M, and divided by a beam splitter, BS, to form two separate pairs of images. At A_4 is a diaphragm containing a small round hole positioned to pass the fourth image on two quadrant photocell P_4 . The diaphragm, which is attached to P_4 , blocks the light from the first Purkinje image. The beam splitter reflects about 10% of the incident light toward another quadrant photocell P_1 , where another pair of Purkinje images is formed.

Mirror M is pivoted at its center and is driven in altitude and azimuth by two separate motors, so as to maintain the first Purkinje image centered on the stationary photocell P₁. The control signals M_x and M_y that drive these two motors are derived from signals from the four sectors of P₁, arranged so that P₁ functions simultaneously both as a horizontally oriented split-field cell and as a vertically oriented split-field cell, as shown in Fig. 4. The position of photocell P₄ is controlled by two separate motors, P_x and P_y, so as to keep the photocell centered on the fourth Purkinje image. The control signals that drive these two motors are derived from the four quadrants of P₄ in a similar manner to that of photocell P₁, shown also in Fig. 4. In sum, mirror M is servo-controlled to maintain the first Purkinje image stationary on photocell P₁, which is spatially fixed, and photocell P₄ is servo-controlled in two dimensions to track any movement of the fourth Purkinje image that remains after mirror M has removed the movement

FIG. 5. Feedback circuit around each motor: D.S., drive signal; M.D., motor driver; M, motor; MM, mechanical motion; M.S., motion sensor, Hewlett-Packard DCDT displacement transducer; O, output signal.

component that is shared with the first Purkinje image. The position of P_4 thus indicates the distance between the first and fourth Purkinje images, which is a measure of the angular position of the eye.

If the eye is translated, mirror M is automatically repositioned so as to maintain the first Purkinje image centered on P_1 . This same movement properly repositions the fourth Purkinje image as well, and no movement of P_4 is required. In other words, there is no change of output. However, if the eye rotates, the images move differentially and the output signal changes accordingly. (A direct measure of eye translation can be obtained by subtracting the two-dimensional movement of P_4 from the movement of the two-dimensional mirror.)

The four servo motors used in the current instrument are Pye-Ling type V-47 vibration generators; two of the motors drive mirror M and two drive photocell P_4 . In order to obtain good high-frequency response, each motor control loop incorporates an accurate motion sensor, MS, shown in Fig. 5, which has a position accuracy better than $1\text{ }\mu\text{m}$. Signals from these motion sensors (Hewlett-Packard DCDT displacement transducers) are fed back to form high-gain internal loops within each major drive loop. All four drive circuits are flat to about 100 Hz (corner frequency).

The subject is positioned by means of a standard chin-rest, forehead-rest combination, or a dental-impression plate. He views the visual target through the dichroic mirror, DC, which transmits visible light and reflects the infrared. The angle between the eye axis and input axis is labeled Δ in Fig. 3. The angle between the light-collecting axis and the input axis is labeled θ . In the current version of the instrument, the collecting axis is displaced horizontally from the input axis by about 30° , i.e., $\theta = 30^\circ$ in Fig. 3.

The instrument has a tracking range of the form sketched in Fig. 3. As the eye rotates toward the input axis (i.e., toward A), the angular separation Δ decreases and the first and fourth Purkinje images move closer together. (At $\Delta = 0$, the two images would be superimposed and therefore inseparable.) Tracking in this direction is eventually limited when light from the very-much-brighter first Purkinje image enters photocell P_4 (through the aperture A_4), and also when light

from the third Purkinje image falls on P_4 . (The effects of the third Purkinje image are discussed in Appendix A.) As the eye moves away from the input axis (i.e., increasing Δ), the horizontal separation of the images increases. Tracking in this direction is eventually limited when the fourth Purkinje image is cut off by the pupil of the eye.

Vertical rotation of the eye, i.e., in the direction C-D in Fig. 3, results in corresponding vertical separation of the first and fourth images and is again limited by occultation by the pupil. In other words, the range of the instrument is primarily limited by the eye pupil on the boundaries away from the input axis, and by confusion from the first and third Purkinje images with the fourth Purkinje image in the direction of the input axis. We have not yet had extensive experience with adjustment of the instrument for maximum range, although it is quite easy to obtain an operating field greater than 10° in diameter.

In order not to lose tracking during an eye blink, the gain of each motor driver is substantially reduced during the blink period. As a result, each servo-control tends to return slowly to some central position. If the eye has not wandered to a completely different gaze position during closure then, when the eye is reopened, the servo controls quickly recapture their respective Purkinje images and tracking is resumed. Blinks are detected by monitoring the sum of all quadrants of P_1 , i.e., signal $(a' + b' + c' + d')$. This sum signal is nominally independent of eye position and therefore remains constant throughout operation except during an eye blink, when it might become larger or smaller than normal, depending on the condition of light reflection from the eyelid. A blink is signaled whenever this sum signal becomes greater or less than the limiting values, S_{min} and S_{max} .

IV. PERFORMANCE

The primary goal of this project was to build an instrument that would monitor eye rotation without error caused by translations of the eye. Figure 6 shows the horizontal motion of the eye during steady fixation, and during two horizontal rotations of 3° each. The top record is the horizontal motion of the two-dimensional mirror (driven from the first-Purkinje-image cell) and the bottom record is the horizontal movement of the fourth-Purkinje-image photocell. The first record is identical with that obtained from a typical corneal image tracker (i.e., it contains the usual wandering baseline that results from translation-induced errors), whereas the signal from the fourth cell is translation insensitive, as explained earlier.

While the record in Fig. 6 was being taken, the head was held rigidly by a tight-fitting dental-impression plate with the extra support of a forehead rest. (Translation-induced effects may be attributable to movements of the eye within its socket.) To test for sensitivity to

translation of the eye, the dental plate and headrest were translated horizontally by 0.5 mm at the point marked T in the record and returned at point T' . As can be seen, the upper record deflected strongly, whereas the lower record is almost completely insensitive to even such a large movement. We see then that the fourth-Purkinje output provides a measure of eye rotation that is uncontaminated by translation.

Conversely, by subtracting this fourth-Purkinje output from the first-Purkinje output (which contains rotation plus translation signals), we can obtain a measure of eye translation, undisturbed by rotations. (That the instrument can provide translation signals independently is especially important in image stabilization when the image being viewed is close to the eye; in this case even eye translation can result in image movement on the retina.)

A. Range and Linearity

Figure 7 is an x, y recording of eye movements over a square array of points. For this purpose the subject viewed a back-lighted board containing an 11×11 array of tiny holes on 25-mm centers. The board was placed 80 cm from the subject, so that movement from one spot to another corresponded to an eye movement of about 1.8° . The subject traced out the pattern, starting at the center point, and then moved successively around each larger square. The random-looking motion about each point is the small motion that typically occurs

FIG. 7. An x, y recording of eye movements (movements of P_4) over an 11×11 array of illuminated points. Adjacent points were separated by 1.8° . The ragged traces on the horizontal axis, left of center, are due to eye blinks.

during steady fixation—the subject fixed each spot for approximately 2–3 s. The ragged traces on the horizontal axis, left of center, are due to eye blinks, which the subject was instructed to make at this location as he traced out each successive square. The usable range of the present instrument is better than 10° in diameter. Determining the ultimate range will require a great deal more detailed design study. Design for improved linearity over the field will also require more detailed design study.

B. Over-All Accuracy

Appendix B contains a description of a set of measurements showing that an earlier version of the double-Purkinje-image tracker tracked the eye with an error of no more than one minute of arc over the range of movements that occur during attempted fixation. We have not yet measured the accuracy of this version of the instrument but, because the system described here contains significant improvements over the one already tested, it is reasonable to suppose that its accuracy will be at least as good.

C. Response to Saccades

Figure 8(a) shows horizontal and vertical eye-movement components during steady fixation. Note that the peak-to-peak noise level is on the order of one minute of arc. Figure 8(b) is an eye-movement record with the subject tracing out the corners of a 0.5° square. Figure 8(c) shows a diagonal eye movement with 3° horizontal and vertical components, respectively.

The accuracy with which rapid saccades can be tracked depends on the frequency response of the servo

FIG. 6. Upper, horizontal eye movements recorded from first-Purkinje-image tracker; lower, horizontal eye movements recorded from fourth-Purkinje-image tracker. The upper trace shows the wandering baseline, typical of corneal image trackers. Both traces record two 3° horizontal eye movements. During the interval $T-T'$, the subject's head was translated 0.5 mm horizontally, which shows in the upper trace but not the lower. Arrows at the bottom indicate eye blinks.

FIG. 8. (a) Fixation record; (b) repetitive traverse of the corners of a $\frac{3}{4}^\circ$ square; (c) diagonal saccadic movement with 3° horizontal and vertical components. Upper, horizontal movements; lower, vertical movements.

systems. The servo systems in the present instrument, as noted earlier, have corner frequencies of about 100 Hz. With this response and a ramp input signal (corresponding to a constant angular velocity of the eye, as in the central portion of a large saccade), the driven mechanical elements have a time lag of approximately 4 ms. For an eye velocity of $300^\circ/\text{s}$ (as in a 5° saccade, see Robinson⁹), 4-ms lag corresponds approximately to 1.2° . The lag is correspondingly smaller for smaller saccades.

There are two basic ways to improve tracking accuracy. First, and most desirable, is to improve the basic response of the servo systems. Experience gained with the instrument thus far has shown how the basic servo response can be substantially improved in subsequent designs. A second method, used here, is to add a portion of the error signal from each fourth-Purkinje-image servo control into the corresponding final output signal. These fed-forward error signals can be adjusted with a model eye that is connected to an accurate motion sensor. The amplitudes of the fed-forward signals are adjusted to make the final signal match the eye motion as closely as possible.

V. SUMMARY

A two-dimensional eye tracker is described that requires no contact with the eye. The resulting accuracy is nevertheless in the same range as that achieved with the most tightly fitting contact lenses. The instrument operates by tracking simultaneously the first and fourth Purkinje images, which are formed in the plane of the eye pupil by the optical elements of the eye. The first Purkinje image derives from light that is reflected from the front surface of the cornea; this is the

familiar corneal image. The fourth Purkinje image is formed by light reflected at the rear surface of the eye lens. A high degree of accuracy is achieved because these two images move together when the eye is merely translated but move differently when the eye rotates. Therefore, the spatial separation of these images gives an accurate measure of eye rotation undisturbed by eye translations. (An instrument that monitors only the first Purkinje image—i.e., a corneal tracker—is limited in absolute accuracy to about 0.5 – 1° , at best.) The light used to form these Purkinje images is in the near infrared and is invisible to the subject. The instrument is very easy to use and align. A standard chin-rest and forehead-rest combination is adequate for alignment of the subject. It takes only a few minutes to align the instrument to a new subject.

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APPENDIX A: INTERFERENCE BY THE THIRD PURKINJE IMAGE

This eye-tracker system operates by measuring the difference of position between the first and fourth Purkinje images. However, a third Purkinje image is also present, and disturbing light from this image could fall onto the first and fourth photocells. It is important, therefore, to understand how the third Purkinje image moves with respect to the other two images.

Figure 9(a) shows the configuration of all of these images, if we assume that the eye is rotated so that the eye axis is aligned with the collecting axis. This angle of the eye axis corresponds to position *b* in the range sketch of Fig. 3. To simplify the drawing, we have assumed that the source is simply a point at infinity, resulting in the pattern of point images labeled 1, 3, and 4 in Fig. 9(a). The centers of curvature and equivalent mirror surfaces are labeled C_1 , C_3 , and C_4 and 1st, 3rd, and 4th, respectively. Figure 9(b) shows the condition when the eye is rotated so that its axis is halfway between the input and collecting axes, corresponding to intercept position *a* in Fig. 3.

In Fig. 9(a), the third Purkinje image is behind the first Purkinje image and slightly to the side away from

FIG. 9. Location of the third Purkinje image with respect to the first and fourth images: IA, input axis; EA, eye axis; CA, collecting axis.

the fourth image, as seen from the collecting axis. (This configuration can be observed by sighting along the collecting axis.) In Fig. 9(b), however, the third Purkinje image is almost exactly centered between the first and fourth images, again as seen from the collecting axis. If the eye axis moved still closer to the input axis, the third Purkinje image would eventually cross directly behind the fourth image. However, tracking is affected even before the third image crosses behind the fourth image. This is because the third Purkinje image, which is approximately 5 mm behind the first and fourth images in eye space, is blurred in the plane of the quadrant photodetectors. Therefore, the third Purkinje image limits the range in the direction of the input axis. With even a small vertical eye rotation, however, the third image is again displaced from the fourth image and tracking is restored.

Although the third Purkinje image is very dim, we have been able to locate it with an ir viewer and in this way verify that the geometric relationships shown in Fig. 9 are basically correct.

APPENDIX B: ACCURACY CALIBRATION

The principles underlying the operation of the eye tracker described in the body of the paper were first tested in a simpler one-dimensional version, which was used by Dr. Michael Katcher, in his dissertation research, to stabilize images on the retina.⁴ As part of that study, he measured how well the composite system stabilized the image, using a modification of a technique developed by Barlow.⁵ Because the eye tracker must be at least as accurate as the complete system, the accuracy of stabilization may be taken as a conservative estimate of the accuracy of the eye tracker itself.

The essence of this technique is to compare the position of an afterimage (which is caused by events occurring within the retina and therefore is perfectly stabilized with respect to the retina⁶) with the position of an image that is stabilized by means of the optical system. If the stabilizing system does not fully compensate for eye movements, the separation between the afterimage and the stabilized image will vary as a function of time; the change of separation from one moment to the next may be taken as a direct measurement of the system's ability to compensate for eye movements.

The auxiliary optical system used in these experiments is shown schematically in Fig. 10. All of the optics above mirror M_R constitute a standard two-

FIG. 10. Auxiliary optical system used in stabilization experiments.

channel maxwellian-view stimulating system. Mirror M_R , which occupies the position normally occupied by the eye of the observer, is mounted on a high-quality galvanometer and imaged by means of lenses L_1 and L_2 in the plane of the subject's pupil. Rotation of mirror M_R causes the image to shift laterally with respect to the eye axis. Lenses L_1 and L_2 are separated by the sum of their focal lengths so that the target plane of the maxwellian-view stimulating system is imaged in the focal plane of lens L_2 . This optical system, then, images the light source in the plane of the subject's pupil and presents the target to him at optical infinity.

The output signal from the eye tracker is amplified and used to drive the mirror galvanometer. Whenever the subject's eye moves, the voltage at the output of the eye tracker changes by an amount proportional to the magnitude of that eye movement. This voltage change causes the mirror to rotate by the amount necessary to stabilize the image on the retina. Because the eye movements being tracked in the study were small (no more than 30' of arc), the front of the eye never moved by more than about 0.1 mm and the image of the rotating mirror remained well centered in the subject's pupil.

With this composite optical-electronic system, the following procedure was used to measure stabilization accuracy. With the subject carefully fixating a point source, a bright vertical slit (4'×12' of arc) was flashed just below his fixation point. Seven seconds later a pair of parallel vertical slits (both 4'×12' and separated by 4') was flashed. If there were no errors of tracking or stabilization, the afterimages of the three slits would form the pattern shown in the upper portion of the inset in Fig. 10. If there were a tracking or stabilization error, the afterimages would be misaligned, as shown in the lower portion of the inset.

To evaluate the disparity within the afterimage pattern, the subject was provided with a device containing a pair of fixed lines and an adjustable line identical in retinal-image size with those presented in the display flashes. After each pair of flashes, the subject moved off the bite bar and observed the afterimage against a blank field that was illuminated by a flickering light. After examining the afterimage in this manner, he adjusted the position of the single line until the relationship between the single and double lines in the device matched the afterimage. [The subject's ability to make this type of adjustment was

measured independently by offsetting the single and double lines in the stimulating system by a fixed amount (e.g., 1' of arc) and flashing the single and double lines simultaneously. The subject then adjusted his device to match the afterimage; the adjustment was accurate to within 0.15'.]

Stabilization measurements were made under two different conditions. In one, the subject remained on the bite bar and maintained fixation during the 7-s interval between the two flashes; in the other condition, he got off and then back on the bite bar between the two flashes. The stabilization errors were approximately normally distributed in both conditions. The standard deviations were 1.1' of arc for the first condition and 1.2' for the second.

The results compare favorably with those obtained using other types of stabilization. Barlow⁵ reported that the standard deviation of stabilization errors for a "tightly fitting" scleral contact lens, with optics mounted directly on the contact lens, was from about 3' to 5'. The standard deviation for a small cup applied to the cornea by suction and similarly carrying the optics for stabilization was 0.6' to 0.7'. Riggs and Schick⁷ determined that the standard deviation for a tightly fitting contact lens with a small plane mirror mounted directly on it was 0.4'. Thus, the Purkinje-image tracker is probably more accurate than most of the contact-lens eye-tracking and stabilization devices that have been used in the past, and only slightly less accurate than the best ones.

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