Lawrence Berkeley National Laboratory

Recent Work

Title

TOPOLOGICAL THEORY OF ELEMENTARY-HADRON COUPLING CONSTANTS

Permalink

https://escholarship.org/uc/item/8vg795z8

Authors

Chew, G.F. Finkelstein, J. Levinson, M.

Publication Date

1981-05-01



Lawrence Berkeley Laboratory

UNIVERSITY OF CALIFORNIA

Physics, Computer Science & Mathematics Division

Submitted for publication

TOPOLOGICAL THEORY OF ELEMENTARY-HADRON JUL 2 1981 COUPLING CONSTANTS

HERIARI AND

RECEIVED

G.F. Chew, J. Finkelstein, and M. Levinson

May 1981



Prepared for the U.S. Department of Energy under Contract W-7405-ENG-48

DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.

TOPOLOGICAL THEORY OF ELEMENTARY-HADRON COUPLING CONSTANTS*

G. F. Chew

Lawrence Berkeley Laboratory and Department of Physics University of California Berkeley, California 94720

J. Finkelstein[†]

Department of Physics San Jose State University San Jose, California 95192

M. Levinson

Lawrence Berkeley Laboratory and Department of Physics University of California Berkeley, California 94720

ABSTRACT

Topological particle theory is applied to the computation of elementary-hadron coupling constants. All are determined through topological supersymmetry by a single dimensionless "zero-entropy" constant g_0 . The predicted coupling-constant ratios encompass and justify those of Mandelstam. The universality conjecture, $g_0 = e$, is supported (to 6%) by the accurately-measured value of the pionnucleon coupling constant. An explanation emerges for the experimental failure to find baryonium.

This work was supported in part by the Director, Office of Energy Research, Office of High Energy and Nuclear Physics, Division of High Energy Physics of the U.S. Department of Energy under Contract No. W-7405-ENG-48.

Participating guest at Lawrence Berkeley Laboratory.

Within the topological theory of particles there occurs a degenerate collection of "elementary hadrons",¹ all sharing a single mass m_0 , which are supposed to stand in one-to-one correspondence with certain physical mesons (spin 0, 1), baryons (spin 1/2, 3/2) and baryonium (spin 0, 1, 2).² A zeroth approximation to physical 3-hadron coupling constants is achieved by superposing corresponding "zero-entropy" amplitudes--which all are interrelated by topological supersymmetry.^{3,4} Precisely, if the dimensionless zero-entropy coupling constant is g_0 , then every zero-entropy 3-hadron M function is equal to g_0m_0 . Any <u>physical</u> hadronic coupling constant is approximated by counting how many different zero-entropy topologies associate to the physical 3-vertex and, with appropiate Clebsch-Gordan coefficients, multiplying by g_0 . This prescription turns out to encompass all the predictions of Mandelstam's model⁵-- which was already an extension of SU(6)_W symmetry--and adds a super-symmetry prediction for the ratios of baryon, meson and baryonium couplings.

Although the value of g_0 is in principle calculable from the nonlinear zero-entropy bootstrap equations, this computation has not yet been accomplished. On the other hand a conjecture has been made that physical S-matrix unitarity will require $g_0 = e^4$ We report in this paper that not only do our predicted ratios of elementary-hadron dimensionless coupling constants agree with measured ratios but, to 6%, the <u>magnitudes</u> of physical strong-interaction couplings agree with the $g_0 = e$ conjecture.

We begin by computing an elementary 3-meson coupling constant. A physical meson's identity is fixed by the spin and flavor attached to quark and antiquark quantum triangles which topologically "build" the

-2-

meson.¹ Given these spins and flavors, as well as the meson 4-momenta⁶ p_A , p_B , p_C with $p_A + p_B + p_C = 0$ and $p_A^2 = p_B^2 = p_C^2 = m_0^2$, the first task is to enumerate the compatible zero-entropy topologies--associating the M-function value g_0m_0 to any single topology, such as that depicted by the shorthand representation of Fig. 1. The solid arcs here carry quark spin and their direction distinguishes quark from antiquark. The direction rules for spin arcs are the same as those given originally for "quark lines" by Harari and Rosner,⁷ and it is possible to attach to each spin arc a flavor-generation index.⁸ The dashed lines in Fig. 1 are charge arcs as described in Ref. (9); each quark has two possible values of electric charge according to whether its charge-arc direction agrees or disagrees with its spin-arc direction. Specifying a set of quark spins and flavors fixes the directions of both spin and charge arcs and also fixes the generation index, but within the topology of Fig. 1 are certain "hidden parameters" not determined by physical-meson properties.

One such hidden parameter is the patchwise orientation of the "classical" surface that houses the spin and charge arcs. This orientation--denoted by the central arrow in Fig. 1--relates to parity¹ and may either agree (ortho) or disagree (para) with the Harari-Rosner (HR) orientation. (The topology of Fig. 1 is para.) Physical amplitudes are always sums over pairs of topological amplitudes belonging to opposite patchwise orientations.

Another hidden parameter in Fig. 1 is the relative order within each quark of its charge and spin arcs. Either arc may be "on the outside". We assume (see Appendix B of Ref. (9) and Appendix D of Ref. (1)) that these two possibilities correspond to using either $1 + \gamma_5$ or $1 - \gamma_5$ quark (4-component) M functions. Thus, for example, the particular para amplitude associated with Fig. 1 has the value

-4--

$$g_{0}^{m} [\bar{v}^{\alpha}(B)(1 + \gamma_{5})v^{\alpha}(A)][\bar{v}^{\gamma}(A)(1 + \gamma_{5})v^{\gamma}(C)][\bar{v}^{\beta}(C)(1 - \gamma_{5})v^{\beta}(B),$$
(1)

where U is a conventional u or v spinor--depending on whether the attached particle is outgoing or ingoing. The U and $\bar{\text{U}}$ contain the boosts that convert M functions to S-matrix elements; the normalization is such that $\overline{U}(p)$ U(p) = 1. We are here expressing through 4-component Dirac spinors the same two forms proposed by Mandelstam, ⁵ who described the two alternatives (corresponding to (0, 1/2) and (1/2, 0) representations of the Lorentz group) through a 2-valued "hidden" index added to each quark helicity. Stapp has discussed these alternatives with 2-component M functions.¹⁰ A natural notation employs M functions with dotted and undotted spinor indices so that zero-entropy guark-spin propagators take the form of Kronecker delta functions. Spin at zero entropy then behaves exactly like flavor, with each index taking 4 possible values even though physical spin is 2-valued. For computational convenience we nevertheless prefer Formula (1)--associating (for a specified classical-patch orientation) $1 + \gamma_5$ with one order of charge and spin arcs and 1 - γ_5 with the other.

Stapp¹⁰ has shown from S-matrix unitarity that physical amplitudes are sums of topological amplitudes where <u>each zero-entropy component</u> <u>occurs with coefficient + 1</u>. This fact is the key to the results of the present Letter. Summing over the two charge-spin orders for each quark line leads to $(1 + \gamma_5) + (1 - \gamma_5) = 2$, so together with

-3-

classical-patch orientation doubling, the physical 3-meson amplitude is approximated by

(2)

-5-

$$2^{4} g_{0}^{m} [\overline{v}^{\alpha}(B) v^{\alpha}(A)] [\overline{v}^{\gamma}(A) v^{\gamma}(C)] [\overline{v}^{\beta}(C) v^{\beta}(B)],$$

This formula is compatible with that of Mandelstam⁵ when he employed quark wave functions symmetrized in the"hidden" index. Unitarity gives the reason for such symmetrization and also provides a definite overall normalization.¹¹

The normalized spin and flavor superposition corresponding to a particular physical meson is straightforward. Attaching such a "wave function" to each meson location in Fig. 1, and summing over the two different cyclic orders (another hidden parameter) for the 3 mesons leads to a physical coupling constant. For example we find for the $\rho^+\pi^-\pi^0$ amplitude F⁰ the value

$$F_{\rho^{+}\pi^{-}\pi^{0}}^{0} = 12 \sqrt{2} g_{0}S_{\rho^{+}} \cdot (p_{\pi^{-}} - p_{\pi^{0}}), \qquad (3)$$

where S $_{\rho^+}$ is the ρ^+ polarization 4-vector. The corresponding resonance width is

$$\Gamma_{\rho \to 2\pi} = \frac{4}{3} (12)^2 \left(\frac{g_0^2}{4\pi}\right) \frac{k_{cm}^3}{\frac{m_{\rho}^2}{m_{\rho}^2}} .$$
 (3')

All our 3-meson coupling ratios are in agreement with Mandelstam.⁵

The first stage in computing a meson-baryon-antibaryon coupling constant is similar to the foregoing. Corresponding to Fig. 2, after summing over classical-patch orientation and charge-spin order for each of the 4 quark lines, we have

$$2^{5}g_{0}^{m}[\overline{v}^{\alpha}(A)v^{\alpha}(B)][\overline{v}^{\beta}(A)v^{\beta}(B)][\overline{v}^{\gamma}(C)v^{\gamma}(B)][\overline{v}^{\delta}(A)v^{\delta}(C)].$$
(4)

Physical baryons, however, are not distinguished by the <u>order</u> of their 3 quark lines--a hidden parameter which in Ref. (1) has been characterized as "topological color". For each physical baryon there are 6 possible quark permutations, each distinct at zero entropy. A convenient procedure is to attach to each baryon location (A and B) in Fig. 2 an ordinary 3-quark spin-flavor baryon wave function, each quark carrying a (1, 2, 3) color label as described in Ref. (1), but to assign the wave function a norm $<\psi|\psi>$ equal to 6.¹³ One thereby finds for the accurately-measured $np\pi^+$ amplitude the value

$$F_{np\pi^{-}}^{0} = 60 g_{0}(\bar{u}_{p} \gamma_{5}\gamma \cdot p_{\pi^{-}n}^{u}).$$
 (5)

The well-known constant $\frac{g_{\pi NN}^2}{4\pi}$ (\approx 15) has a corresponding value of

$$\frac{g_{\pi NN}^2}{4\pi} = \frac{(60)^2}{2} \frac{g_0^2}{4\pi} .$$
 (5')

Again, all our baryon-antibaryon-meson couplings agree with Mandelstam.⁵ We now additionally predict through supersymmetry (not via vector dominance) the ratios to 3-meson couplings. These latter ratios agree with experiment. In particular, the measured $\frac{g_{\pi NN}^2}{4\pi} = 14.8$ predicts, through comparison of Formulas (3') and (5'),

$$\Gamma_{\rho \to 2\pi} = \frac{8}{75} \frac{g_{\pi NN}^2}{4\pi} \frac{k_{cm}^3}{m_{\rho}^2}, \qquad (6)$$

a ρ width of 124 MeV.¹⁵

A next question is how well the conjecture $g_0 = e$ is borne out. Formula (5') with $g_0 = e$ gives a result only 12% smaller than the above experimental value of $g_{\pi NN}^2/4\pi$. The conjectured universality of electroweak and strong couplings is thus given encouraging support. It remains to confirm that coupling-constant corrections from higher-order terms of the topological expansion are no more than a few percent even though mass shifts are large.

Topological hidden parameters systematically make BBM coupling constants larger than MMM coupling constants by a factor 4(16 in the square of coupling constants).² One factor of 2 arises from the extra quark line and one factor of 2 from the always-allowed permutation of the two quark lines that do not touch the meson. The attachment of baryon wave functions obscures but does not remove the systematic factor of 4. Some readers may be puzzled by remembering that vector dominance of electromagnetic structure functions requires that <u>Dirac</u>type coupling of vector mesons to baryons should have the same magnitude as the $\rho\pi\pi$ coupling in Formula (3) above. This fact is compatible with our theory; the additional enhancement is in <u>Pauli-type</u> coupling between baryons and vector mesons.

-8-

In the coupling of a baryonium to BB there is an <u>additional</u> factor of 4 coming from one more quark line and one more pair of permutable quark lines.¹⁶ The experimental failure to find baryonium thereby becomes understandable. Even if a baryonium lies below the BB threshold so that decay must lead to mesons via an OZI-ruleviolating higher component of the topological expansion, the OZI suppression mechanism has to fight a factor of 16 in rate as well as the large phase space available to the final mesons. Although the OZI mechanism for baryonium decay has not yet been understood in detail, the extremely large baryonium coupling constants make it difficult for baryonium to have widths sufficiently narrow as to be detectable by a straightforward experiment.

-7-

ACKNOWLEDGEMENTS

-9-

·. ' ``

Discussions with S. Mandelstam, H. Stapp and M. Suzuki have been of great help to this paper. This work was supported in part by the Director, Office of Energy Research, Office of High Energy and Nuclear Physics, Division of High Energy Physics of the U. S. Department of Energy under Contract No. W-7405-ENG-48.

REFERENCES AND FOOTNOTES

- G. F. Chew and V. Poénaru, Phys. Rev. Letters <u>45</u>, 229 (1980); Lawrence Berkeley Lab. preprint LBL-11433, submitted to Nuclear Physics B.
- 2. The quantum numbers of elementary hadrons are those of ground ($\ell = 0$) states in constituent-quark models.
- P. Gauron, B. Nicolescu and S. Ouvry, Orsay preprint IPNO/TH 80-58, Dec. 1980.
- G. F. Chew, Lawrence Berkeley Lab. preprint 12436, submitted to Phys. Rev. Letters.
- 5. S. Mandelstam, Phys. Rev. 184, 1625 (1969); Phys. Rev. D1, 1745 (1970).
- 6. Topological quarks do not carry momentum, as explained in Ref. (1).
- 7. H. Harari, Phys. Rev. Letters 22, 562 (1969).
 - J. Rosner, Phys. Rev. Letters 22, 689 (1969).
- The theory of Ref. (1) predicts 4 flavor generations, but this number is not needed for the computations described here.
- 9. G. F. Chew, J. Finkelstein, Robert E. McMurray Jr., and V. Poénaru, Physics Letters <u>100B</u>, 53 (1981) and Lawrence Berkeley Lab. preprint LBL-11435, submitted to Phys. Rev.
- 10. H. P. Stapp, Lawrence Berkeley Lab. preprint LBL-10774.
- 11. As explained in Ref: (10), unitarity also generates higher terms in the topological expansion that eliminate the wrong-parity "ghost poles" which occur in zero-entropy M functions for more than 3 particles.

20

- See, for example, B. Sakita and K. C. Wali, Phys. Rev. 139B, 1355 (1965).
- 13. The usual baryon wave functions include a sum over the six quark permutations with a corresponding normalizing factor of $\frac{1}{\sqrt{6}}$. If each permutation is to be given a weight +1, this latter factor must be omitted.
- 14. All our 3-particle amplitudes have the dimension of mass.
- 15. The Breit-Wigner ρ width listed in the Particle Data Group Tables is 158 MeV, but it is known for the $\Delta(1238)$ that the imaginary part of the mass of such broad P-wave resonances is significantly smaller than half the Breit-Wigner width.
- 16. In calculating a physical baryonium coupling to BB, ordinary 2-quark 2-antiquark spin-flavor wave functions are employed, the two quarks being distinguished by a color label and similarly for the two antiquarks. The norm of the wave function is 4--corresponding to the four topologically-distinct color permutations belonging to a single physical baryonium. See Sec. IX of Ref. (1).

X

1. The 3-meson vertex.

2. The baryon-antibaryon-meson vertex.



Figure 1

----- spin (HR) arc ----- charge arc

3

؟ ۲

13





Figure 2

ø

XBL 815-905

14

This report was done with support from the Department of Energy. Any conclusions or opinions expressed in this report represent solely those of the author(s) and not necessarily those of The Regents of the University of California, the Lawrence Berkeley Laboratory or the Department of Energy.

ł

Reference to a company or product name does not imply approval or recommendation of the product by the University of California or the U.S. Department of Energy to the exclusion of others that may be suitable. .

,

TECHNICAL INFORMATION DEPARTMENT LAWRENCE BERKELEY LABORATORY UNIVERSITY OF CALIFORNIA BERKELEY, CALIFORNIA 94720

-

1.5