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# Single shot interferometric measurement of cavitation bubble dynamics

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### Abstract

We demonstrate an interferometric method to provide direct, single shot measurements of cavitation bubble dynamics with nanoscale spatial and temporal resolution with results that closely match theoretical predictions. Implementation of this method reduces the need for expensive and complex ultra-high speed camera systems for the measurement of single cavitation events. This method can capture dynamics over large time intervals with sub-nanosecond temporal resolution and spatial precision surpassing the optical diffraction limit. We expect this method to have broad utility for examination of cavitation bubble dynamics as well as for metrology applications such as optorheological materials characterization. This method provides an accurate approach for precise measurement of cavitation bubble dynamics suitable for metrology applications such as optorheological materials characterization.

Precise measurement of cavitation dynamics is relevant to phenomena as diverse as sonoluminescence, sonochemistry, molecular transport, fluidic mixing, and light-tissue interactions [1–4]. These phenomena have been exploited in numerous applications including ultrasonic cleaning [6], microfluidic mixing [7] and pumping [8], tissue ablation [5], drug delivery [9,10], ocular surgery [11], microrheology [12,13], screening of cellular mechanosignaling [14,15], and measurement of mechanical properties of soft materials [13,16,17].

Empirical studies providing detailed measurement of cavitation bubble dynamics most often utilize high-speed photographic methods [18,19]. Such measurements are critical

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to understand complex fluidic processes, assess computational fluid dynamics models, and optimize applications that utilize cavitation bubbles [20]. While the capabilities of high-speed photographic and holographic methods have advanced formidably in recent years, with systems capable of imaging rates as large as 1 trillion frames/second [21–23], significant limitations remain including the total number of frames available, diffraction-limited spatial resolution, and significant expense and complexity. These limitations place these high-speed photography and holography out of the reach of most researchers in terms of cost and/or needed expertise.

On the other hand, time-resolved photography, achieved through combining individual timegated images from independent cavitation events, has been used by a larger number of investigators [7,24–28]. This approach has enabled the reconstruction of complex bubble dynamics over long-time intervals with high temporal resolution. However, this approach provides an "average" view of the phenomena since the data acquisition utilizes images from different events. This effectively blinds the investigator to important factors that may cause shot-to-shot variability such as the stochastic nature of laser-induced plasma formation and the potential effects of medium heterogeneity and/or impurities [29,30].

As an alternative, investigators have developed optical techniques utilizing probe deflection or spatial transmittance modulation to determine cavitation bubble dynamics [31–34]. However, these techniques appear best suited to probe millimeter scale sized bubbles and generally lack the precision necessary to allow for detailed analysis. Moreover, to obtain quantitative bubble dynamics, these techniques require calibration and/or pairing with photography.

In this Letter, we present a new method for precise measurement of cavitation bubble dynamics with nanoscale temporal resolution and spatial precision. This method utilizes a heterodyne interferometer in a modified Mach-Zehnder configuration [35,36] as shown in Figure 1. To demonstrate its capabilities, we formed cavitation bubbles were formed via laser-induced plasma generation by irradiation using a single 500ps duration pulse emitted by a frequency-doubled Nd:YAG laser ( $\lambda$ =532 nm, Teem Photonics PNG-M03012) laser. The laser beam output was expanded and delivered to a water-filled cuvette using a  $40\times$ 0.8 numerical aperture water immersion microscope objective (OBJ, Leica HCX APO L 40x/0.80 W U-V-I). The interferometer was constructed utilizing a polarized continuous wave Helium-Neon laser (HeNe,  $\lambda$ =632.8 nm, 12mW, Newport Optics, R-30993). The separate arms of the interferometer are formed using a 110 MHz acousto-optic modulator (AOM, IntraAction Inc., ATM-1101A1) such that the first-order frequency-shifted beam from the AOM serves as the reference arm and the unshifted beam serves as the sample arm. The sample arm is directed through the cuvette perpendicular to and passing through the center of the bubble. The two beams are recombined using a non-polarizing 50/50 beam splitting cube (BSC, Thorlabs BS013). Dual balanced detection [37] is performed using two 1 GHz bandwidth Si PIN photodiodes (P1 & P2, S5973 Hamamatsu) with the detection circuit enclosed in a steel Faraday cage to reduce ambient electrical noise. The photodiode output signals are amplified using a broadband low-noise amplifier (AMP, Mini-Circuits, ZFL-500LN), digitized by a 2 GHz bandwidth oscilloscope (OSC, LeCroy WaveRunner

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6200A) at a sampling rate of 5GS/s, and processed using MATLAB's Hilbert transform function.

Prior to bubble formation the detected interferometer signal consists of a sinusoidal oscillation at the 110 MHz modulation frequency. Bubble formation changes the optical path length of the sample arm as it passes through the growing and collapsing cavity. This dynamic change in optical path length is detected by the photodiodes and prototypical waveforms of both the AOM reference and detected interferometer signals are shown in Figure 2.

The phase difference between the reference and sample arms is directly proportional to the cavitation bubble size. Figure 3 illustrates the results of the Hilbert transform in which both the phase of AOM signal, which is equivalent to the phase of the interferometer reference beam,  $\varphi$ *ref*, and phase of the detected interferometer signal,  $\varphi$ *sample*, are plotted vs time. The phase difference between these two signals is shown by  $\varphi$ *bub*. Prior to applying the Hibert transform, the raw interferometer signal is processed using notch filters to exclude 314MHz and 629 MHz frequency peaks that correspond to the mode hopping frequency of our HeNe laser. Additionally, a band pass filter between 2.9MHz to 220MHz is used to filter out electrical noise above and below relevant frequency range of the system.

The time-resolved bubble radius  $R_{\rm B}(t)$  is obtained from the optical phase  $\varphi_{\rm bub}(t)$  corresponding to the dynamic optical path length difference between the reference and sample arms introduced by the bubble. This leads to the following relationship between the time-resolved bubble radius  $R_{\rm B}(t)$  and the optical phase introduced by the bubble  $\varphi_{\rm bub}(t)$ 

$$R_B(t) = \frac{\lambda \varphi_{bub}(t)}{4\pi (n_G - n_W)} \tag{1}$$

where  $\lambda$  is the wavelength of the probe beam and  $n_{\rm G}$  and  $n_{\rm W}$  are the refractive index of the gas within the bubble and surrounding water, respectively.

Once the bubble is initiated and growing in size, the instantaneous frequency of the interferometer signal  $I_{int}$  falls below the 110 MHz heterodyne frequency since the optical Pathlength in the sample arm is decreasing with time. Conversely, once the bubble reaches its maximum size and begins to collapse the instantaneous frequency of the interferometer signal  $I_{int}$  rises above 110 MHz heterodyne signal. The detection limit of our bubble measurement is dependent on the phase noise associated with the baseline signal which is 0.1 radians corresponding to 15nm.

To assess the measurement accuracy of the interferometer, we compare the bubble dynamics measurements with predictions provided by the Rayleigh-Plesset model [38] which has been demonstrated to provide accurate predictions for the cavitation bubbl dynamics in this case [13,26]:

$$\rho \left[ R_B \frac{d^2 R_B}{dt^2} + \frac{3}{2} \left( \frac{d R_B}{dt} \right)^2 \right] = p_b - p_\infty - \frac{2\sigma}{R_B} - \frac{4\mu}{R_B} \frac{d R_B}{dt},$$
(2)

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where  $R_{\rm B}(t)$  represents the time-resolved bubble radius,  $\mu$  the viscosity of water,  $\rho$  the density of water, and  $\sigma$  the surface tension at water/vapor interface, with  $p_{\rm B}$  and  $p_{\infty}$  representing the pressure inside the bubble and surrounding liquid, respectively. Figure 4 shows excellent agreement between the predictions made by the Rayleigh-Plesset model and the interferometric measurement. As a point of comparison, we also provide bubble dynamics data obtained under similar conditions obtained by taking a single bubble image at different time points using time-resolved photography.

Comparison of the two data sets clearly illustrates the increased measurement uncertainty that is incurred when determining the bubble dynamics using time-resolved images obtained using multiple independent trials. However, we do find that our current interferometric method has difficulty unwrapping the phase during the final stages of bubble collapse once the velocity of the bubble wall exceeds approximately 84–94 m/s. This collapse velocity corresponds to a heterodyne detection frequency in excess of 154–159MHz. Interestingly, we have an unidentified source of ambient electronic noise located at 156 MHz. This leads us to believe that our difficulty in resolving the bubble collapse is not intrinsic to our overall approach but may instead be resolved through better electrical isolation or by using an AOM operating at a lower modulation frequency.

In summary, we have demonstrated an accurate interferometric method for obtaining the complete cavitation bubble dynamics from a single cavitation event with 15nm radial precision and sub-nanosecond temporal resolution. This approach is more accurate, less costly and simpler to operate as compared to fast-frame photographic and holographic methods. Moreover, unlike probe beam methods, our method requires no calibration to obtain quantitative measurements. This approach allows for capturing of the full cavitation bubble dynamics extending over 10's of microseconds while retaining (sub-)nanosecond temporal resolution. We anticipate these capabilities will be of broad utility for examination of cavitation bubble dynamics as well as for metrology applications such as optorheological materials characterization.

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#### Fig. 1:

Diagram of the Mach-Zehnder interferometric system. M1-M5 are 1 inch silver mirrors used to direct both the pump (Nd:YAG) and interferometer probe (HeNe) beams. 50mm convex lenses L1 & L2 are used to direct the interferometer probe beam through the bubble. 10mm convex lenses L3 & L4 are used to focus the combined interferometer beams onto the Si-PIN diodes P1 and P2. 50mm concave (L5) and 125 mm convex (L6) lenses are used to expand and recollimate the Nd:YAG pump beam.



#### Fig. 2:

Recovered Photodiode signal and AOM driving signal from oscilloscope following initiation of a cavitation bubble using a 20 $\mu$ J.  $I_{int}$  (blue) and  $I_{aom}$  (orange) are shown in segments corresponding to (a) the beginning, (b) middle and (c) end of bubble a 175 $\mu$ m diameter bubble created by a 20 $\mu$ J laser pulse.



#### Fig. 3:

Measured  $\varphi$ ref and  $\varphi$ int corresponding to the formation of a 141.3  $\mu$ m diameter cavitation bubble using a 10 $\mu$ J laser pulse.  $\varphi$ bub is the phase difference between the reference and interferometer signals.



#### Fig. 4:

Time resolved bubble dynamics for bubbles formed using pulse energies of 2.5, 10, and 20  $\mu$ J resulting in maximum bubble radii of 77, 136, and 172  $\mu$ m, respectively, is shown with theoretical bubble radius predicted by the Rayleigh-Plesset model. In the case of the 10 $\mu$ J pulse energy, we also show data acquired using images from captured from separate events using an intensified CCD camera.