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PARTIAL WAVE ANALYSIS OF THE  $\bar{K}N$  SYSTEM FROM 360 TO 1320 MeV/c\*

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ABSTRACT

In this paper we use new data from several recent  $\bar{K}N$  experiments in conjunction with older data to make an energy-dependent partial wave analysis of the  $\bar{K}N$  system. The important new additions never used before in a partial wave analysis, are: our precision measurements of the charge exchange total cross sections, our measurements of the charge exchange angular distributions, and the first measurements of the  $K^- p$  polarization at these low momenta. A new feature introduced in the analysis is the S wave cusp treatment at the  $\lambda\eta$  and  $\Sigma^0\eta$  thresholds, which we find necessary to describe the observed behavior in the charge exchange total cross sections near these thresholds. Other features include a single channel unitary formulation for resonances and backgrounds and a parametrization of these amplitudes incorporating centrifugal barrier effects. New values for masses, widths, and elasticities for resonances in this region are reported and better evidence is found for several of the less well established resonances. None of the new resonances suggested by recent  $I=0$  and  $I=1$  total cross section

measurements are required. Fits are displayed for all the data used and predictions of this partial wave analysis are compared with those of two other recent analyses for certain quantities yet to be measured. A table of the amplitudes, in steps of 20 MeV/c, is provided.

## I. INTRODUCTION

During the past several years, a number of experiments have been done with counters and with bubble chambers which have considerably improved the precision of measurements in the  $\bar{K}N$  system. For this reason we have undertaken a new partial wave analysis of the  $\bar{K}N$  channel in order to search for new structures and to re-evaluate the resonances derived from analyses of the older experiments.

We have chosen to study the  $\bar{K}N$  channel alone rather than perform a multichannel analysis since most of the new data are from the elastic and charge exchange reactions. The other two body channels ( $\Lambda\pi$ ,  $\Sigma\pi$ ,  $\Lambda\eta$ ,  $\Sigma\eta$ ) are exceedingly useful when the resonances have dominant branching fractions into these channels, hence a low elasticity. However, essentially all the information on resonant structure in these reactions can be obtained via single channel analyses because at the energies under consideration most of the beneficial constraints of a multichannel analysis are lost due to the complicating presence of several additional three and four body channels with substantial cross sections. Only at low energies where the three body cross sections become small has a multichannel analysis been found to be really useful.<sup>1</sup>

The momentum spanned by this analysis, 360 to 1320 MeV/c ( $1507 < E_{c.m.} < 1941$  MeV), was dictated by the available new data and by the existence of prominent resonances with well-established quantum numbers, at the lower and upper energies, with which to anchor the analysis. Experience has shown that an energy-dependent partial wave analysis in regions with such resonances leads to an unambiguous determination of the various amplitudes. In energy regions devoid of prominent

resonances the amplitudes become much less certain. The latter is the case for the  $\bar{K}N$  system from above 400 MeV/c to at least 700 MeV/c. Thus we found it essential to extend our analysis downward in momentum to 360 MeV/c in order to encompass the prominent  $\Lambda(1520)$  resonance and thereby stabilize the other partial wave amplitudes whose behaviors are uncertain. For this we also benefitted from the recently-published high-statistics bubble chamber coverage of the  $\Lambda(1520)$  region.<sup>2</sup> The upper limit was likewise determined by the co-existence of the very elastic  $\Lambda(1815)$  resonance and the new high-statistics bubble chamber experiment of the Rutherford Laboratory and Imperial College (RL-IC).<sup>3</sup>

Among the numerous  $\bar{K}N$  partial wave analyses<sup>4-10</sup> there has been general agreement concerning resonances in the higher angular momentum states. Only among the S and P wave amplitudes, where the non-resonant background is usually very large, have significantly different conclusions been drawn from the data. Often these differences are clearly apparent from inspection of the Argand diagrams. In other cases the Argand diagrams are similar and much of the difference in the resonances can be ascribed to differences in the parametrization of backgrounds and in the way in which resonances are combined with backgrounds.

In this paper we describe in detail a partial wave analysis reported earlier.<sup>9</sup> We also present the results from a new fit with an expanded data bank containing our recently measured charge exchange angular distributions<sup>11</sup> and having, in addition, constraints on the  $K^-p$  and  $K^-n$  forward scattering amplitudes derived from a new dispersion relation calculation.<sup>12</sup>

## II. DATA

Table I shows the various types of data used, their sources, and their contributions to  $\chi^2$  in the best fit we obtained. Of the many bubble chamber experiments in this region, we have included only those designed to study in a systematic way the energy dependence of structures arising from the formation of resonances. Thus we have left out a number of older experiments of low precision or of limited momentum coverage, but rely heavily, as do most previous analyses, on the extensive data of the CERN-Heidelberg-Saclay (CHS) collaboration.<sup>13</sup> As discussed in the introduction, new accurate bubble chamber data<sup>2,8,14</sup> have also contributed substantially to this analysis. Recent bubble chamber results<sup>15</sup> for the reaction  $K_L p \rightarrow K_S p$  have not been included since they involve assumptions concerning the positive strangeness KN interaction, thus introducing additional and unknown systematic uncertainties. Nor were the very sparse data currently available on  $K^- n$  elastic scattering from two older bubble chamber experiments<sup>16</sup> considered to be of sufficient statistical weight to be included.

For reasons of economy the computer program was limited to 100 discrete momenta. Since the various experiments were done at many more momenta, it was necessary to interpolate some of the data points; in the case of experiments of low statistical accuracy we simply displaced the published momentum, typically by a few MeV/c.

### A. $K^- p$ elastic scattering

The bulk of the  $K^- p$  differential cross section data comes from bubble chambers, with improved statistical accuracy from a recent



Birmingham-Rutherford electronic experiment<sup>17</sup> over the central third of our momentum region. Instead of fitting the differential cross sections directly we have, for economy of computation, fit both the shape-dependent ratios  $A_n/A_0$  of the Legendre polynomial coefficients through  $n = 6$  and the integrated cross section ( $\sigma = 4\pi \chi^2 A_0$ ). Correlations between the various orders of polynomial coefficients have not been included. The uncertainty on the integrated cross section depends mostly on the accuracy of the  $K^-$  flux determination, hence it is essentially independent of the measurement of the shape. We have also explicitly fitted the  $K^-p$  differential cross section at  $180^\circ$ . Most of the points were obtained by extrapolation of bubble chamber data, there having been but one ad hoc counter experiment<sup>21</sup> to measure this quantity. Although this was a redundant use of the data described by the polynomial coefficients, it served to better constrain the fit in the backward direction which, for certain momenta, was particularly difficult to fit.

Only a few measurements<sup>18</sup> of the  $K^-p$  and  $K^-n$  forward scattering amplitudes have been made in the resonance region. However, they can be calculated with some reliability at all energies by means of a dispersion relation using all the available  $K^+N$  forward scattering measurements and the total cross sections. For this we have used a new dispersion relation determination of the real parts of the  $K^-p$  and  $K^-n$  forward scattering amplitudes<sup>12</sup> which incorporates all of the very low energy  $K^-p$  data, the recently measured real parts at higher energies<sup>18</sup> and, in contrast to previous determinations,<sup>19</sup> is constrained to yield the observed dip in the charge exchange differential cross section at 300 MeV/c.<sup>2,20</sup> These results have been used in our partial wave analysis by introducing as

data points the real parts of the  $K^-p$  and  $K^-n$  forward scattering amplitudes at approximately 100 MeV/c intervals with uncertainties of  $\pm 0.05$  fermi.

Polarization in  $K^-p$  elastic scattering had previously been measured only above 860 MeV/c.<sup>22</sup> This has now been extended down to 650 MeV/c by recent measurements at BNL.<sup>23</sup> The polarization has been fitted directly at all angles and energies for which it has been measured. This was preferable to fitting the polarization coefficients because these coefficients involve an expansion of the product of the differential cross section times the polarization and therefore contains two independent measurements.

#### B. Charge exchange scattering

For this reaction, polarization measurements have not yet been made; only the angular distributions and total cross sections have been measured. We again fit the shape-dependent angular distribution coefficients  $A_n/A_0$  and the total charge exchange cross section. Our precision measurements<sup>24</sup> of the latter dominate the much less accurate bubble chamber data over most of the momentum region covered by the analysis, while our recent measurements of the angular distributions for charge exchange scattering<sup>10</sup> are also of substantially higher statistical accuracy than the bubble chamber data.

### C. Total cross sections

The other precision data used in this analysis are the total  $K^-p$  cross sections. Below 1 GeV/c these have been measured by three counter experiments.<sup>25-27</sup> We have preferentially used the most recent and accurate measurements of BNL,<sup>27</sup> interpolated to momenta where other types of data exist. Between 360 and 430 MeV/c we have relied on bubble chamber measurements<sup>12</sup> of these cross sections, while above 1 GeV/c other counter experiments were used.<sup>25,28</sup>

The individual  $I=0$  and  $I=1$  total cross sections were also fitted. Below 1 GeV/c these were obtained from the analysis of Carroll et al.<sup>27</sup> Because there is considerable disagreement between the various determinations of the isospin-decomposed cross sections and because of the uncertainties associated with the deuterium corrections, we have enlarged the errors on these derived cross sections to approximately  $\pm 5\%$ . A partial wave analysis of bubble chamber data in the vicinity of 400 MeV/c<sup>20</sup> suggests an  $I=1$  total cross section some 10 mb larger than that of Carroll et al. Due to this discrepancy we have restricted the isospin-decomposed cross sections to those above 430 MeV/c.

### III. METHOD OF ANALYSIS

The basic partial wave analysis program is an outgrowth of that used by CHS<sup>4</sup> into which we have incorporated a number of sophistications deemed necessary for the elastic amplitudes in this energy region. Each

partial wave amplitude through  $J=7/2$  was given an energy-dependent parametrization, consisting of a non-resonant background upon which, if there were indications of resonant structure in that partial wave, could be superposed one or two Breit-Wigner resonances. An approximation to single channel unitarity was realized in the conventional way by writing the scattering amplitude  $T$  as  $T = T_B + S_B T_R$ <sup>29</sup> where the subscripts  $B$  and  $R$  refer to the background and resonant amplitudes. Two resonances in the same partial wave were similarly combined.

Each background amplitude was made explicitly unitary by parametrizing it in terms of a variable scattering length  $A$ , viz.,

$$T_B = \beta A / (1 - i\beta A) . \quad (1)$$

It is essential to introduce a centrifugal barrier factor  $\beta$  to accommodate the large momentum interval spanned by the analysis; for this we write<sup>30</sup>

$$\beta = \frac{k}{E} \left( \frac{k^2}{k^2 + R^{-2}} \right)^\ell \quad (2)$$

where  $k$  is the incident c.m. wave number,  $E$  is the c.m. energy,  $R$  is the radius of interaction and  $\ell$  is the orbital angular momentum. The complex scattering length is conveniently written as  $A = a + ib$ <sup>2</sup>, so that the imaginary part which represents absorption always remains positive. Further momentum dependence is contained in the coefficients  $a$  and  $b$  which are expanded in Legendre polynomials:

$$a = \sum_n a_n P_n(y) \quad \text{and} \quad b = \sum_n b_n P_n(y) . \quad (3)$$

The argument  $y$  of the Legendre polynomial  $P(y)$  is linearly related to the momentum spanning the fitted interval,  $-1 \leq y \leq 1$ . For the large S and P wave background amplitudes, three complex coefficients were usually found to be necessary in order to achieve a reasonable fit to the data; for the  $D_3$  waves one complex amplitude was sufficient, this being further reduced to one real amplitude for higher waves. Thus D and higher angular momenta backgrounds were parametrized by constant scattering lengths whereas S and P wave backgrounds assumed a more flexible behavior while retaining the unitary feature.

Resonant amplitudes were expressed as Breit-Wigner resonances,

$$T_R = \frac{\Gamma_e}{2(M-E) - i\Gamma} \quad (4)$$

where  $E$  is the c.m. energy.  $M$ , the resonance mass, is a free parameter as are the total width at resonance  $\Gamma_r$  and the elasticity  $x$ , related to the elastic width  $\Gamma_e$  and the total width  $\Gamma$  by  $x = \Gamma_e/\Gamma$ . The energy dependent widths appearing in Eq. 4,  $\Gamma = \beta\Gamma_r/\beta_r$  and  $\Gamma_e = \beta\Gamma_{er}/\beta_r$ , contain the centrifugal barrier factor  $\beta$  described previously, with  $\beta_r$  evaluated at resonance. For  $S_{01}$ ,  $S_{11}$ , and  $P_{01}$  resonances (we use the conventional notation  $L_{I 2J}$ ) where large non-resonant backgrounds are present, it was found necessary to introduce a phase factor in order to achieve a good fit. In principle, the introduction of this phase factor could result in the combined amplitude exceeding the unitary limit, but in practice these amplitudes always fell within the unitary circle. For several of the prominent resonances, additional parameters allowing for a linear dependence of the elasticity  $x$  on the c.m. energy were introduced. Since no significant improvement in the fit was attained by this additional

freedom, the elasticities were taken to be independent of energy.

At the thresholds for the processes  $K^-p \rightarrow \Lambda\eta$  and  $K^-p \rightarrow \Sigma^0\eta$  a rapid rise has been observed in the reaction cross sections with a subsequent fall-off at higher energy, the overall behavior being consistent with  $S_{01}$  and  $S_{11}$  resonant excitation.<sup>31,32</sup> Accordingly, we have introduced cusps to the elastic parametrization at the thresholds to reflect the observed enhancements in these channels. This was done by adding a partial width for these processes to the total width. Thus

$$\Gamma_T = \Gamma + \gamma_Y(p) \quad (5)$$

replaced  $\Gamma$  in the above resonance expressions. Here  $p$  is the momentum of the  $\eta$  in the c.m. and  $\Gamma$  is the total width without the  $\eta$  channel while  $\gamma_\Lambda$  and  $\gamma_\Sigma$  are free parameters controlling the strength of the cusp. Since  $p$  becomes  $+i|p|$  when analytically extended below threshold, the amplitude has a singularity in speed at threshold accompanied by a  $90^\circ$  left-hand turn in the trajectory on an Argand plot as the threshold is traversed from below.<sup>33</sup>

The well established 3 and 4 star resonances<sup>34</sup> were introduced from the outset with their accepted values of masses, widths, and elasticities. A minimum was achieved in these conditions by first varying the background parameters and then the parameters of the resonances. Attempts were then made to improve this minimum-structure solution by adding resonances to those background amplitudes whose energy dependences were suggestive of resonances or to those partial waves where resonances have previously been identified in the reaction channels  $K^-p \rightarrow \Sigma\pi$  or  $K^-p \rightarrow \Lambda\pi$ . If a significant improvement in the fit was thereby achieved, the resonance

was retained. Several well-established resonances with masses above our fitted region but whose influence was felt at lower energy were introduced with fixed parameters, as was the  $D_{05}$  resonance seen clearly only in the  $\Sigma\pi$  channel. The best fit had a  $\chi^2$  of 2523 with 1659 data points.

#### IV. RESULTS AND COMPARISON WITH OTHER ANALYSES

The results of this analysis appear in the following tables and figures. Table II lists the resonance parameters obtained in the best fit, while Table III contains those of the background and other parameters. The resulting partial wave amplitudes are tabulated every 20 MeV/c in Table IV. The Argand diagrams for the S and P wave amplitudes are displayed in Fig. 1 where they are compared with those of the RL-IC analysis.<sup>8</sup> In Fig. 2 we exhibit the fits to the total elastic and charge exchange cross sections and in Fig. 3 the fits to the polynomial coefficient ratios  $A_n/A_0$  of both angular distributions. Figure 4 shows the fit to the elastic  $180^\circ$  cross section. Fits to the polarization are shown at selected momenta in Fig. 5 where they are compared with two other analyses. The resulting momentum dependence of the polarization coefficients  $B_n$  can be seen in Fig. 6. The total  $K^-\bar{p}$  and individual isospin-decomposed cross sections are shown in Fig. 7 while our real parts of the forward scattering amplitudes for  $K^-\bar{p}$  and  $K^-\bar{n}$  appear in Fig. 8. Figure 9 shows the measured charge exchange differential cross section at  $0^\circ$  and  $180^\circ$  compared with our fit. We also compare the  $0^\circ$  cross section with the dispersion relation prediction of Ref. 12. Predictions for the so far unmeasured charge exchange polarization and

for the  $K^-n$  angular distribution and polarization are shown at selected momenta along with those of other analyses in Fig. 10.

#### A. S-waves

We first discuss the individual partial wave amplitudes shown in Fig. 1 with emphasis on their resonant structure. Both the  $S_{01}$  and  $S_{11}$  amplitudes exhibit cusp behavior at their respective  $\Lambda\eta$  and  $\Sigma\eta$  thresholds. The need for cusps is most evident in our precision measurement of the charge exchange cross section.<sup>24</sup> Here the rapid variations observed in this cross section as the thresholds are traversed cannot be followed with the cusps suppressed. Figure 11 is an expanded view of the region of these thresholds showing the fits to our data with and without cusps along with a comparison of  $\chi^2$  for the two cases.

In addition to the narrow  $S_{01}$  resonance at  $\Lambda\eta$  threshold,<sup>31</sup> we find that a second broad resonance in this amplitude makes a substantial improvement in  $\chi^2$ . This resonance overlaps the lower one so that the manner in which the two resonances are combined with each other as well as with the large  $S_{01}$  background seems to influence the mass found for the upper resonance. Thus, although our Argand diagram is similar to that of the RL-IC analysis,<sup>8</sup> the mass they obtain for the upper resonance is about 100 MeV higher than ours. On the other hand, the two analyses for the lower mass narrow resonance are in reasonable accord with each other and with evidence found for the resonance in the  $\Lambda\eta$  channel. A comparison is made in Table V of the parameters deduced for this and other S and P wave resonances found both by our single channel analysis and by others.<sup>8,31,32,35-38</sup>



The mass and width of the  $S_{11}$  resonance near  $\Sigma\eta$  threshold agree fairly well with the values found from  $\Sigma\eta$  production<sup>32</sup> and with those found by the RL-IC analysis.<sup>8</sup> A second  $S_{11}$  resonance has also been suggested by RL-IC to lie just above our region of investigation. We do not confirm this resonance because the introduction of this additional structure into our program did not bring about an improvement in  $\chi^2$ .

### B. P-waves

The presence of a substantial and rapidly growing P wave amplitude in our lower momentum region is most evident in the swift rise in the  $A_1/A_0$  coefficient for  $K^-p$  elastic scattering as seen in Fig. 3. This leads to a very low value of the  $180^\circ$  elastic cross section in the vicinity of 600 MeV/c (Fig. 4). Neither of these behaviors is well-fitted either by our analysis or by others. Most agree that the P wave interference needed to produce this behavior comes mainly from the  $P_{01}$  amplitude, and there have been several suggestions that it resonates in the vicinity of 1600 MeV.<sup>5,8</sup> With the addition of our new charge exchange angular distributions, the mass and width of this resonance have changed considerably from that of our previous analysis,<sup>9</sup> which did not contain these data. We now obtain a mass of 1700 MeV and a very broad width of about 600 MeV. There has been a recent theoretical suggestion<sup>39</sup> for the inclusion of a ninth member into the stable  $J^P = 1/2^+$  baryon octet with this mass, with an elasticity of 0.23, and with an even greater width of approximately 1000 MeV. Given the large uncertainty associated with such a broad resonance, our solution is compatible with this interpretation. However, a different parametrization of the background can seriously

alter the values found for such a broad resonance without appreciably affecting the Argand diagram. Thus although the mass and width found in this analysis are quite different from those found in the RL-IC analysis and even from our previous work, the Argand diagrams are very similar.

A second  $P_{01}$  resonance at a higher mass has been suggested by the RL-IC analysis, but when introduced into our program was not found to yield a lower  $\chi^2$ .

The recent improvements in the data bank in the  $\bar{K}N$  channel have led to much better evidence for a relatively narrow resonance in the  $P_{11}$  amplitude in the intricate region between 700 and 800 MeV/c where three other amplitudes are known to resonate. Our  $P_{11}$  resonance parameters agree quite well with those of Hart<sup>35</sup> who relies heavily on unpublished higher statistics  $\bar{K}N$  bubble chamber data in this region. However, we are only in vague accord with the RL-IC analysis which finds very different values for this resonance in their  $\bar{K}N$  and in their  $\Sigma\pi$  analyses (See Table V), leading them to suggest that there are in fact two distinct resonances. Since our  $\bar{K}N$  and their  $\Sigma\pi$  analysis agree in mass, this now appears to be an unnecessary complication. This resonance is nearly degenerate in mass and width with the well-established  $D_{13}(1670)$ .

The  $P_{03}$  amplitude grows to prominence throughout our energy region, but, as with other analyses, we find that this large amplitude is better parametrized at lower energies as a background with a clear resonance appearing only near 1900 MeV. Apart from the well-known  $\Sigma(1385)$ , the  $P_{13}$  amplitude shows no resonant behavior, in agreement with other studies.

### C. Other waves

Most partial wave analyses agree concerning the existence and parameters of resonances in higher angular momentum states. In our former analysis,<sup>9</sup> the  $D_{13}$  (1670), which is known to have a relatively weak coupling to the  $\bar{K}N$  channel, gave a mass and width discordant with better evidence from other channels. However, with the addition of our angular distribution data, these parameters are now in excellent agreement with accepted values.

Finally we consider the recent indications for a number of narrow  $\bar{K}N$  states found by Carroll et al.<sup>27</sup> in the analysis of their total  $K^-p$  and  $K^-d$  cross sections. Although neither of these measured cross sections show direct evidence for new structure, when decomposed into pure isospin cross sections, four new resonances emerge in the  $I=1$  channel and two in  $I=0$ , all lying between 500 and 900 MeV/c. They appear as narrow structures with low elasticity and their locations are indicated by arrows in Fig. 7. None of the other data in the  $\bar{K}N$  channel show any evidence for these structures although most are too poor in statistical accuracy to reveal resonances so weakly coupled to the elastic channel. However, support for the most prominent of these structures, the  $I=1$  bump at 546 MeV/c (1582 MeV) comes from reanalysis of CHS bubble chamber data by Litchfield<sup>40</sup> who identifies a  $D_{13}$  resonance of nearly identical mass and width in the reaction  $K^-p \rightarrow \Lambda\pi$ . In our previous work<sup>9</sup> we investigated the consistency of  $I=1$  resonances at 546 and 602 MeV/c with the rest of the  $\bar{K}N$  data and concluded that if they exist they are probably not in the S or P states. Our charge exchange angular distribution experiment showed no evidence for new structures, and one must await

further precise measurements to resolve these questions.

#### D. Discussion of results

In Table II we have indicated by stars the status of hyperon resonances in 1976 as assigned by the Particle Data Group,<sup>34</sup> and in parentheses have shown the changes in this attribution which we believe should be made on the basis of this analysis.

We next consider the uncertainties inherent in this partial wave analysis. The problems of ambiguities that have troubled the energy-independent pion-nucleon partial wave analyses have been of less concern in the  $\bar{K}N$  system where, because the data are generally not as precise, energy-dependent analyses have been the rule. Here with several prominent  $Y^*$  resonances (such as the  $D_{03}(1520)$ ,  $D_{15}(1765)$  and  $F_{05}(1815)$  whose quantum numbers have been established by a variety of means) extending over most of the fitted interval, ambiguities are effectively removed. Only in the mass region of 1600 MeV where there are no prominent structures could there be any possibility of radically different solutions fitting the data equally well.

A more legitimate concern centers on the manner in which the background is parametrized and how this affects the parameters and even the need for the less prominent resonances. In this regard it is illuminating to compare our analysis with the recent RL-IC work<sup>8</sup> where the backgrounds were introduced in a very different way. A comparison of the Argand diagrams of the lower partial waves for the two analyses can be found in Fig. 1. The general structures appear very similar and will probably remain as lasting features of future partial wave analyses. It is in

the interpretation of these features in terms of resonances, particularly when they are broad and of low elasticity, where the somewhat arbitrary choice of background complexity and parametrization plays an important role. The differences in resonance parameters found by the two analyses reflect this uncertainty.

We have also explored another expansion for the background. As an alternative to the chosen parametrization (Eq. 3), the  $a$  and  $b$  coefficients of the scattering length  $A=a+ib$  were instead expanded as

$$a = \sum_n a_n \left(\frac{P}{E}\right)^{2n} \quad \text{and} \quad b = \sum_n b_n \left(\frac{P}{E}\right)^{2n} \quad (6)$$

where  $P$  and  $E$  are the c.m. momentum and energy.

For low energies such a dependence would be suggested by the effective range expansion. This yielded  $\chi^2 = 2842$ , i.e. more than 300 higher than our best fit. Since this new parametrization is less adaptable to variations at low energy, it may argue for the existence of further structure in the lower part of our energy region where the data indicate that there are deficiencies in the parametrization. Unfortunately it is here, in the region above 400 and below 700 MeV/c, that the measurements are least accurate.

We have also tried to reduce the number of background parameters since an over-parametrized background can to some degree simulate a resonance or at least reduce its contribution. On the basis of these attempts, a case could be made for diminishing the number of parameters for the  $P_{11}$ ,  $P_{03}$ , and  $P_{13}$  backgrounds, while the other amplitudes appear to require the chosen expansion. It should be noted that the background amplitudes alone tend to have counter clockwise Argand trajectories as a function of energy in the manner of resonances, although with a different

energy dependence. With these considerations in mind, it is likely that a more refined analysis with better data will reveal greater resonant contributions to the amplitudes and perhaps more broad resonances than the solution which we present here.

The uncertainties we assign to the resonance parameters appearing in Table II were estimated by studying the change when the backgrounds were altered in various ways described above, as well as by investigating the stability of the parameters to the removal of our charge exchange angular distribution data. There is, of course, further information available about many of these resonances from other two body channels, particularly if the resonance in question has a large branching fraction into another channel.

Finally we consider how this analysis and that of RL-IC<sup>8</sup> and UCL<sup>10</sup> differ with regard to directly measurable quantities. In Fig. 5 we exhibit the polarization in  $K^-p$  elastic scattering at several recently measured momenta. Both our analysis (which uses these data) and that of RL-IC lead to very nearly the same polarization, in good agreement with experiment. However the UCL amplitudes do not accommodate the rapidly diminishing polarization displayed by the data below 750 MeV/c. Since their  $J=\frac{1}{2}$  amplitudes, in both S and P waves, differ substantially from ours and from RL-IC at low momenta, the  $K^-p$  polarization reflects this difference. Presumably the major reason for this difference lies in the fact that UCL did not use the high statistics bubble chamber data in the vicinity of 400 MeV/c to stabilize the amplitudes at low momentum. In Fig. 10 the predictions for the unmeasured  $\bar{K}^0n$  and  $K^-n$  polarizations and the  $K^-n$  differential cross sections are displayed at four c.m. energies.

Again there are generally only minor differences between our solution and that of RL-IC whereas a major difference in  $\bar{K}n$  polarization at low energy distinguishes the UCL solution from the others.

## V. CONCLUSIONS

We have presented in Table II our best estimates of the status and parameters of hyperon resonances with masses between 1500 and 1950 MeV. These are based on our partial wave analysis of all the latest available  $\bar{K}N$  data from formation experiments. Our amplitudes are in good agreement with those of similar analysis of older data by the RL-IC group,<sup>8</sup> although certain resonance parameters differ significantly. Some of these differences probably result from the inclusion of new precision data while others, pertaining to the broad resonances, can be ascribed to different background parameterizations and to a different way of combining resonances and backgrounds. On the other hand, our amplitudes in low partial waves disagree substantially with the recent UCL solution<sup>10</sup> at low momentum where new polarization measurements have shown the UCL solution to be in error.

Most of the momentum-dependent structure within the  $\bar{K}N$  data bank can be well-fitted by the contemporary set of resonances with no compelling necessity for the introduction of further resonances. However, data between 430 and 700 MeV/c are sparse, sometimes discordant, and occasionally difficult to fit. Since there are no prominent resonances

in this region to guide the analysis, additional experimental work here would be highly desirable. In particular, it would be of interest to redetermine the individual  $I=1$  and  $I=0$  total cross sections to ascertain the systematic uncertainty inherent in the currently available cross sections and the reliability of the structures claimed therein.



## FOOTNOTE AND REFERENCES

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TABLE I. Data used in the fit.

<u>Type of data</u>	<u>References</u>	<u>Momentum (MeV/c)</u>	<u>Data Points</u>	$\chi^2$
(1) $d\sigma/d\Omega(K^-p)$	2	365 - 425	35	113
	13	436 - 1200	396	360
	3	960 - 1320		
	17	610 - 943		
(2) $d\sigma/d\Omega(180^\circ, K^-p)$	2, 3, 13, 21	365 - 1320	51	113
(3) $D(K^-p), D(K^-n)$	12	375 - 1320	22	63
(4) $K^-p$ polarization	23	650 - 1071	135	229
	22	865 - 1330	374	389
(5) $d\sigma/d\Omega(\bar{K}^0 n)$	2	365 - 425	35	93
	13	436 - 1200	295	483
	14	862 - 1011		
	3	960 - 1320		
	11	515 - 956	132	312
(6) $\sigma(\bar{K}^0 n)$	24	515 - 1066	48	113
(7) $\sigma_T$	2	365 - 425	7	28
	27	436 - 1066	36	55
	25, 28	1080 - 1320	7	22
(8) $\sigma_0, \sigma_1$	27	436 - 1066	72	129
	25, 28	1080 - 1320	14	21
Total			1659	2523

TABLE II. Resonance parameters.

State (a)	M	$\Gamma$	Amplitude (b)
$L_{I2J}$	(MeV)	(MeV)	
$S_{01}^{****}$	$1671 \pm 3$	$29 \pm 5$	$0.17 \pm 0.03$
$S_{01}^{**(*)}$	$1725 \pm 20$	$185 \pm 20$	$0.28 \pm 0.05$
$S_{11}^{***(*)}$	$1770 \pm 10$	$161 \pm 20$	$0.33 \pm 0.05$
$P_{01}^{**(*)}$	$1703 \pm 100$	$593 \pm 200$	$0.14 \pm 0.05$
$P_{11}^{**(*)}$	$1679 \pm 10$	$38 \pm 10$	$0.10 \pm 0.05$
$P_{03}^{***(*)}$	$1908 \pm 10$	$119 \pm 20$	$0.34 \pm 0.05$
$P_{13}^{****}$	[1385]	$20 \pm 10$	$0.15 \pm 0.05$
$D_{03}^{****}$	$1520 \pm 0.5$	$15.4 \pm 0.5$	$0.45 \pm 0.03$
$D_{03}^{****}$	$1692 \pm 5$	$64 \pm 10$	$0.22 \pm 0.03$
$D_{13}^{****}$	$1679 \pm 10$	$56 \pm 20$	$0.11 \pm 0.03$
$D_{05}^{****}$	[1825]	[90]	$0.02 \pm 0.02$
$D_{15}^{****}$	$1777 \pm 5$	$116 \pm 10$	$0.37 \pm 0.03$
$F_{05}^{****}$	$1819 \pm 2$	$72 \pm 5$	$0.60 \pm 0.03$
$F_{15}^{****}$	$1937 \pm 20$	$161 \pm 20$	$0.14 \pm 0.05$
$F_{17}^{****}$	[2030]	[180]	[0.2]
$G_{07}^{****}$	[2100]	[250]	[0.3]

(a) Stars show the status of the resonance in 1976 as assigned by the Particle Data Group. Stars in parenthesis indicate the changes in this attribution which we believe should be made on the basis of this analysis.

(b) The amplitudes listed correspond to the diameter of the resonant circles. When absorptive processes are present they become  $\eta_B \Gamma_e / \Gamma$  where  $\eta_B$  is the absorption parameter of the background.

TABLE III. Background and cusp parameters as defined in Eqs. 3, 2, and 5.

<u>Amplitude</u>	<u>a<sub>1</sub></u>	<u>b<sub>1</sub></u>	<u>a<sub>2</sub></u>	<u>b<sub>2</sub></u>	<u>a<sub>3</sub></u>	<u>b<sub>3</sub></u>
S <sub>01</sub>	-.536	1.401	-.001	-.807	.145	.280
S <sub>11</sub>	.287	.783	.045	.019	.217	.084
P <sub>01</sub>	.078	.746	-.487	.079	-.497	-.147
P <sub>11</sub>	.085	.416	.105	.022	-.108	.012
P <sub>03</sub>	.387	.155	.150	.280	.091	.045
P <sub>13</sub>	.030	.159	.175	.356		
D <sub>03</sub>	.227	-.332				
D <sub>13</sub>	.130	-.384				
D <sub>05</sub>	.125					
D <sub>15</sub>	.037					
F <sub>05</sub>	-.033					
F <sub>15</sub>	.000					
F <sub>07</sub>	.039					
F <sub>17</sub>	.025					
G <sub>07</sub>	.059					
G <sub>17</sub>	.030					
R	2.20 fm.					
γ <sub>Λ</sub>	.104					
γ <sub>Σ</sub>	.385					



TABLE V. S and P wave resonance parameters. Comparison of this work with some other single channel analyses.

Resonance	Analysis	Channel	Mass	Width	Amplitude <sup>(a)</sup>
S <sub>01</sub> (I)	Berley et al. (31)	$\Lambda\eta$	1666	22	.24
	CHS (36)	$\overline{KN}$	1663	26	.14
	RL-IC (8)	$\overline{KN}$	1670	45	.17
	" (8)	$\Sigma\pi$	1670	45	.35
	This analysis	$\overline{KN}$	1671	29	.17
S <sub>01</sub> (II)	Bricman et al. (37)	$\overline{KN}$	1872	100	.18
	RL-IC (8)	$\overline{KN}$	1823	230	.39
	This analysis	$\overline{KN}$	1725	185	.28
S <sub>11</sub> (I)	Jones (32)	$\Sigma\eta$	1760	92	.23
	RL-IC (8)	$\overline{KN}$	1768	60	.14
	" (8)	$\Lambda\pi$	1710	68	.09
	This analysis	$\overline{KN}$	1770	161	.33
S <sub>11</sub> (II)	RL-IC (8)	$\overline{KN}$	1955	200	.49
P <sub>01</sub> (I)	RL-IC (8)	$\overline{KN}$	1567	117	.24
	" (8)	$\Sigma\pi$	1584	191	.17
	This analysis		1703	593	.14
P <sub>01</sub> (II)	RL-IC (8)	$\overline{KN}$	1856	144	.22
	" (8)	$\Sigma\pi$	1846	180	.20
P <sub>11</sub>	Hart (35)	$\overline{KN}$	1658	40	.11
	RL-IC (8)	$\overline{KN}$	1738	72	.14
		$\Sigma\pi$	1676	117	.16
	This analysis	$\overline{KN}$	1679	38	.10
P <sub>03</sub>	Conforto et al. (38)	$\overline{KN}$	1883	80	.25
	RL-IC (8)	$\overline{KN}$	1900	72	.18
	This analysis	$\overline{KN}$	1908	119	.34

(a) In our analysis the amplitude shown for the elastic channel when significant absorptive backgrounds are present is  $\eta_B \Gamma_e / \Gamma$ , corresponding to the diameter of the resonant circle. The amplitudes for other reactions,  $\sqrt{\Gamma_e \Gamma_i} / \Gamma$  are listed here only to indicate the strength of the signal in that channel.

FIGURE CAPTIONS

Fig. 1. Argand diagrams of the S- and P- wave amplitudes. The solid curves are the results of this analysis while the dashed curves show the RL-IC<sup>8</sup> solution. Numbers are c.m. energies in GeV with intervals of 0.1 GeV indicated by bars. The locations of resonance masses in each partial wave are indicated by circles. S wave cusps at  $\Lambda\eta$  and  $\Sigma^0\eta$  thresholds are explicitly accommodated in our analysis and manifest themselves on the Argand diagrams as singularities in speed accompanied by 90° discontinuities in direction.<sup>33</sup>

Fig. 2. The total elastic and charge exchange cross sections calculated in this analysis and compared to the experimental data which we fit.

Fig. 3. The Legendre polynomial coefficient ratios  $A_n/A_0$  of the angular distributions for elastic and charge exchange scattering calculated in this analysis and compared to the experimental coefficients which we fit. Symbols are as in Fig. 2 except for "This expt." which refers to Ref. 11.

Fig. 4. The differential cross sections at 180° for elastic  $K^-p$  scattering calculated in this analysis and compared to the experimental data which we fit.

Fig. 5. Fits to some of the recently measured polarizations of Ehrlich et al.<sup>23</sup> in  $K^-p$  elastic scattering at selected momenta.



FIGURE CAPTIONS Continued

Fig. 6. The experimental polynomial coefficients  $B_n$  of the product  $IP = \chi^2 \sum_n B_n P_n^1$  of the  $K^-p$  angular distribution times the polarization plotted at the momenta where we fit the polarization directly and compared to the predictions of our partial wave analysis.

Fig. 7. The total  $K^-p$  cross sections and the  $I=0$  and  $I=1$  cross sections used in this analysis compared with our fit. The arrows indicate the locations and widths of six new resonances claimed by Carroll et al.<sup>27</sup>

Fig. 8. The real parts of the  $K^-p$  and  $K^-n$  forward scattering amplitudes in the lab. calculated by this analysis and compared to a dispersion relation calculation. The latter were introduced into the fit at approximately 100 MeV/c intervals with errors of  $\pm 0.05$  fm as indicated by the open circles. Solid points correspond to actual measurements of real parts.

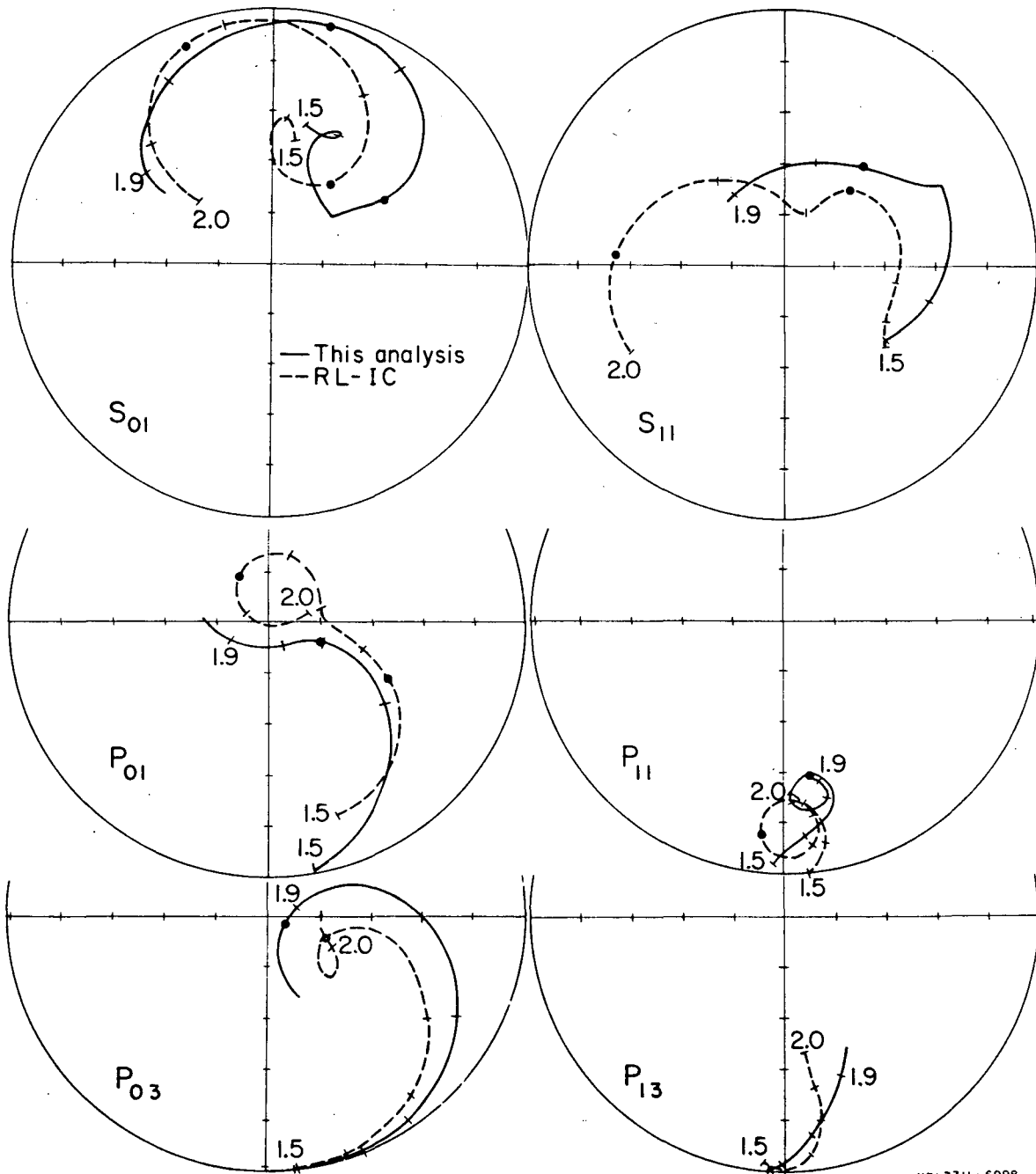
Fig. 9. The measured charge exchange differential cross sections at  $0^\circ$  and  $180^\circ$  compared with the fit of this partial wave analysis. The  $0^\circ$  cross section predicted from the dispersion relation of A. Martin<sup>12</sup> is also shown.

Figure 10. Comparison between our predictions (solid lines), those of the RL-IC analysis (dashed lines) and those of UCL (dotted lines) for the unmeasured charge exchange polarization and for the  $K^-n$  polarization and angular distribution at selected c.m. energies as a function of the  $K^-$  c.m. scattering angle.

FIGURE CAPTIONS Continued

Fig. 11. Expanded view of the fit to our precision charge exchange cross sections of Ref. 24 in the vicinity of  $\Lambda\eta$  and  $\Sigma^0\eta$  thresholds showing the best overall fit obtained with and without cusps. The  $\chi^2$  coming from these 20 data points in  $\pm 50$  MeV/c intervals surrounding the thresholds is 55 with cusps and 185 without cusps. The total  $\chi^2$  decreases by 266 when the additional two degrees of freedom associated with the two cusp parameters  $\gamma_\Lambda$  and  $\gamma_\Sigma$  are introduced.

$\bar{K} N \rightarrow \bar{K} N$



XBL7711 - 6998

Fig. 1

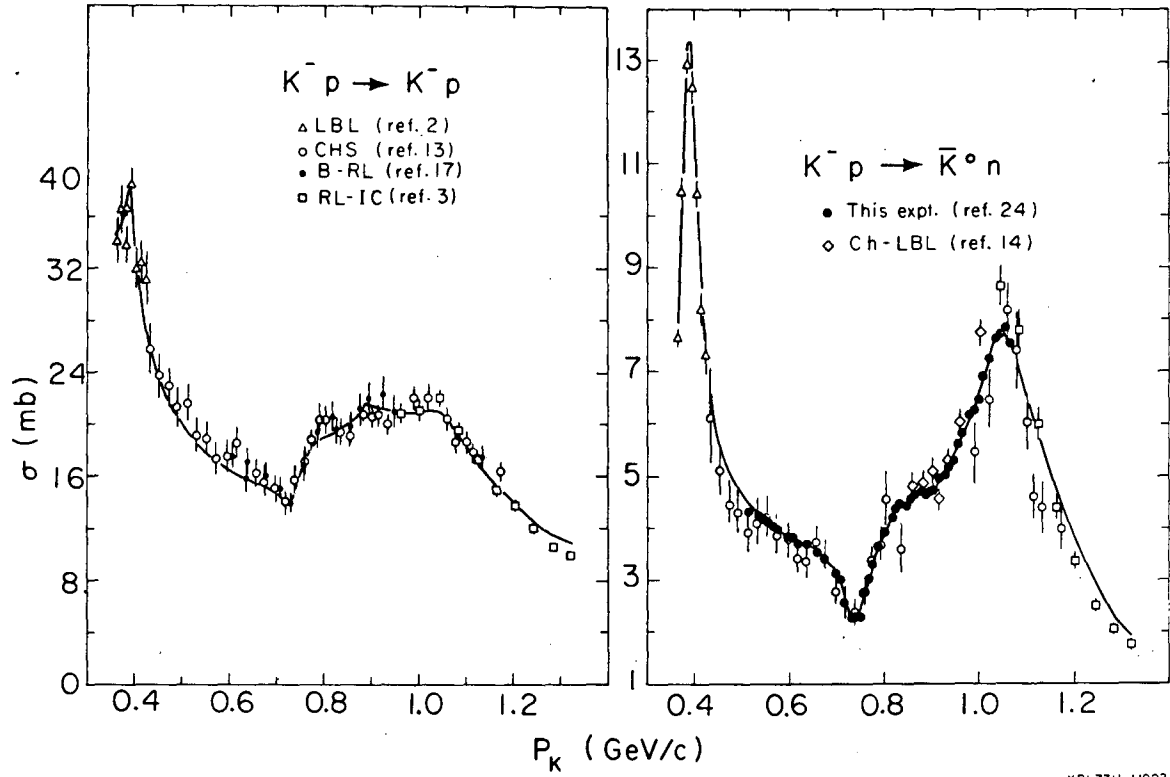


Fig. 2

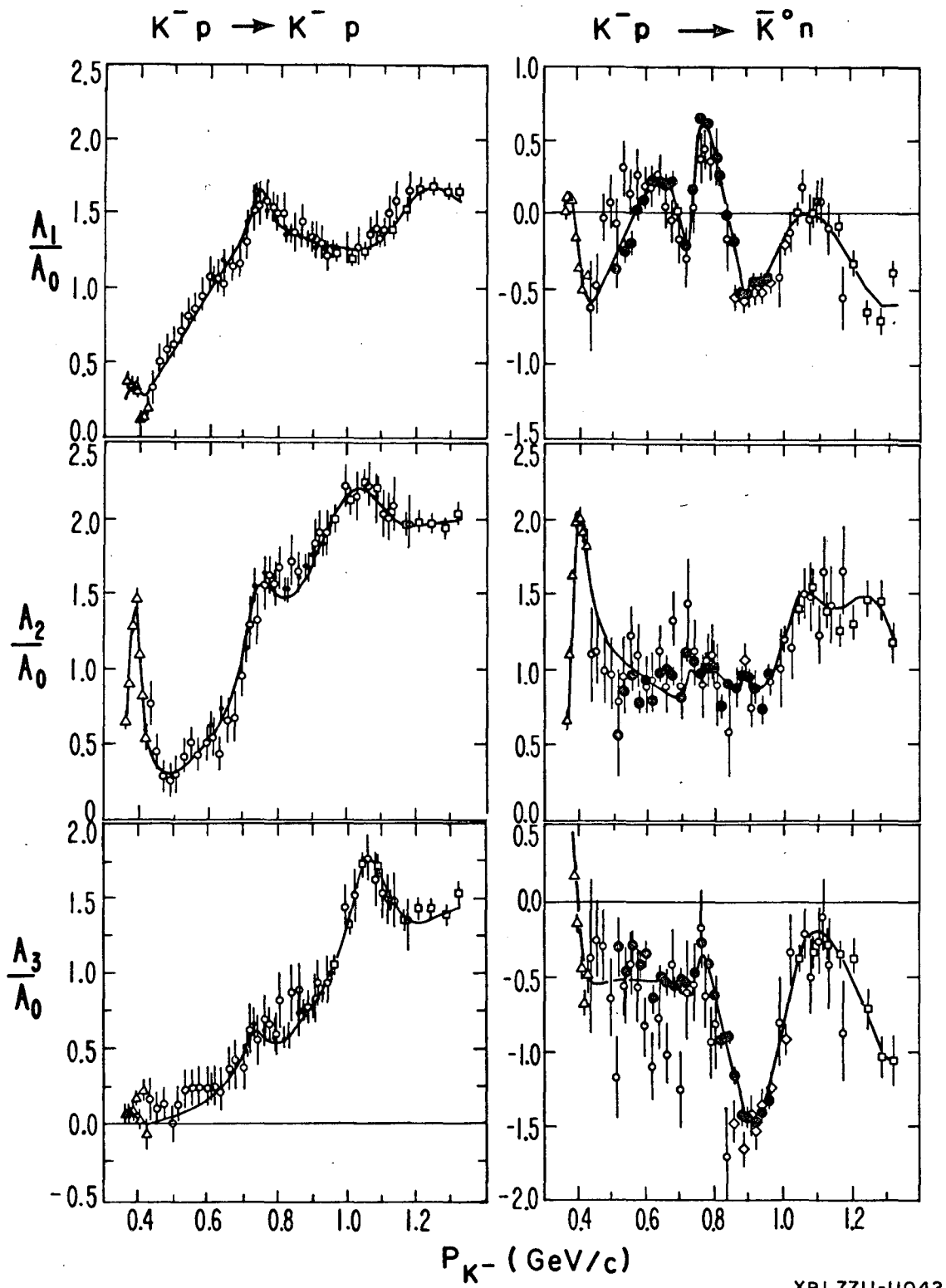


Fig. 3

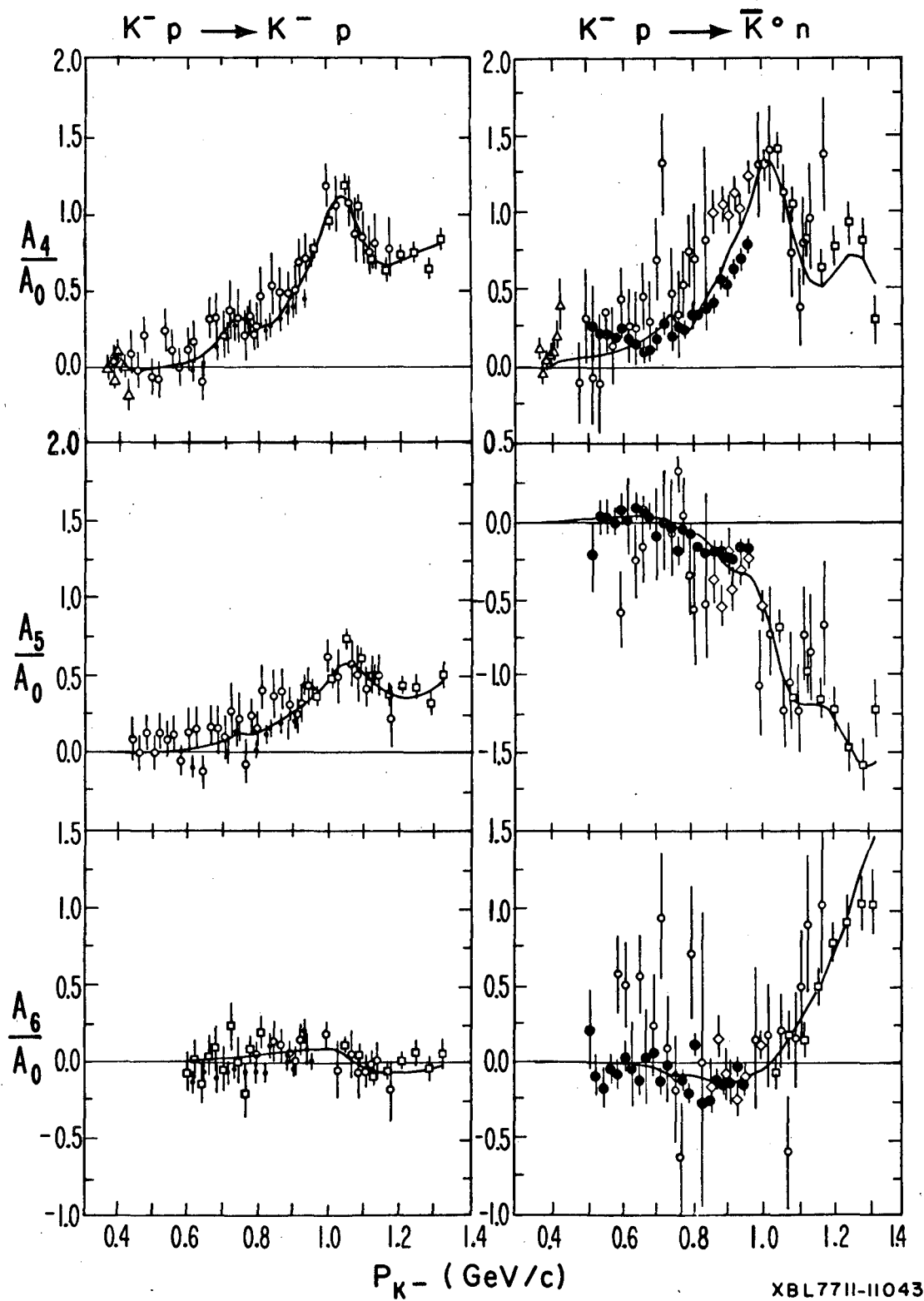
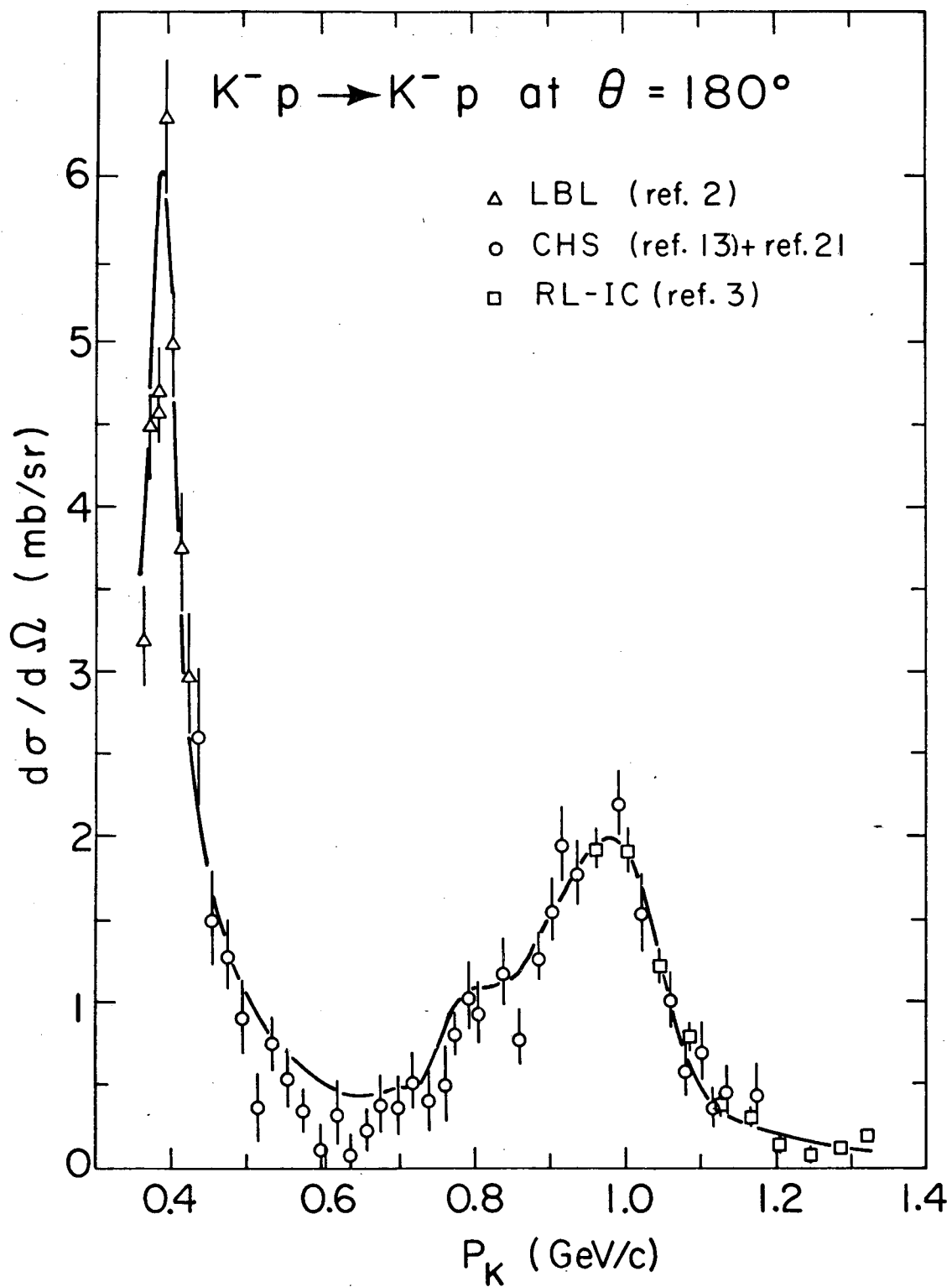
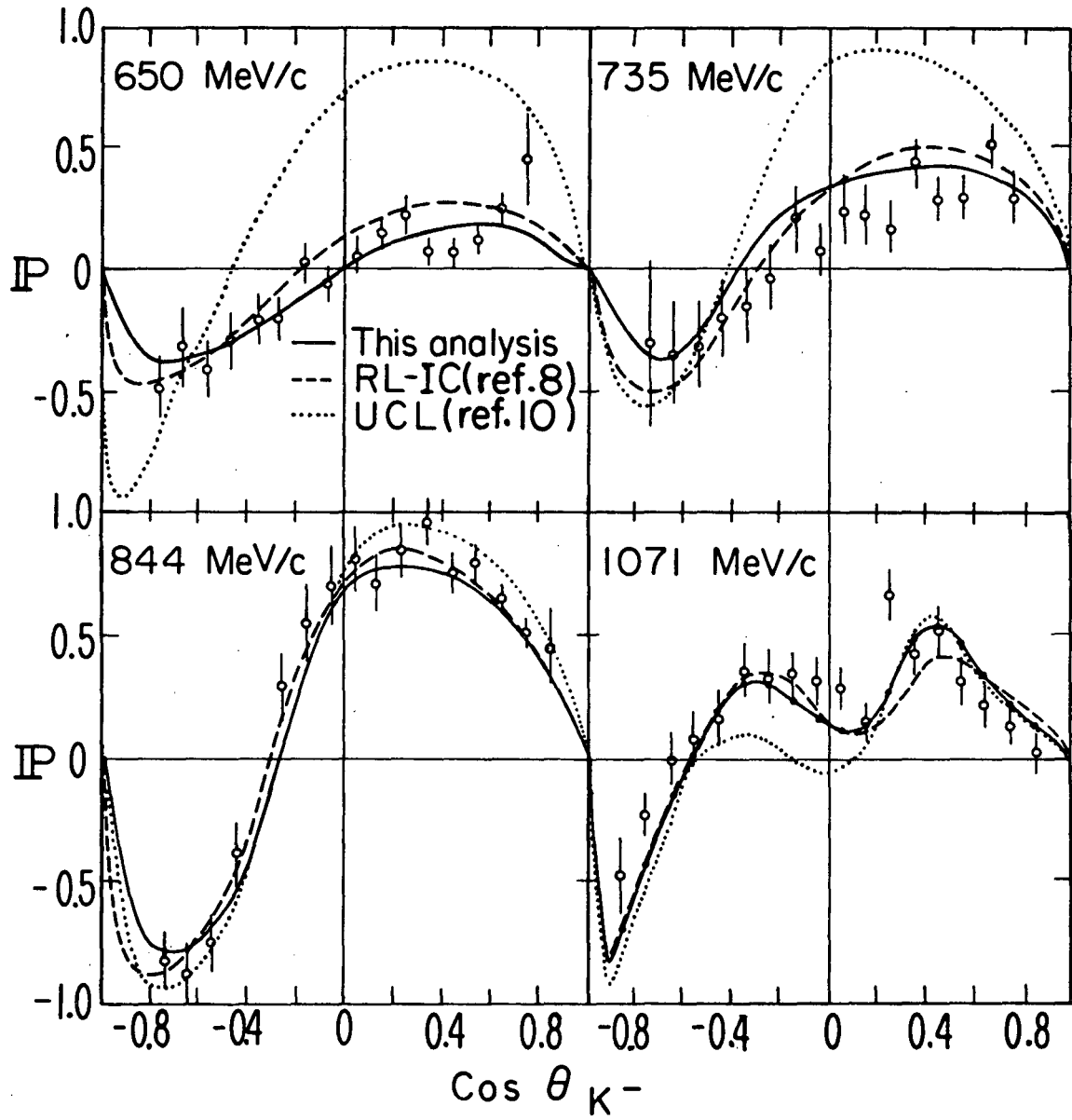


Fig. 3a



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Fig. 4



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Fig. 5



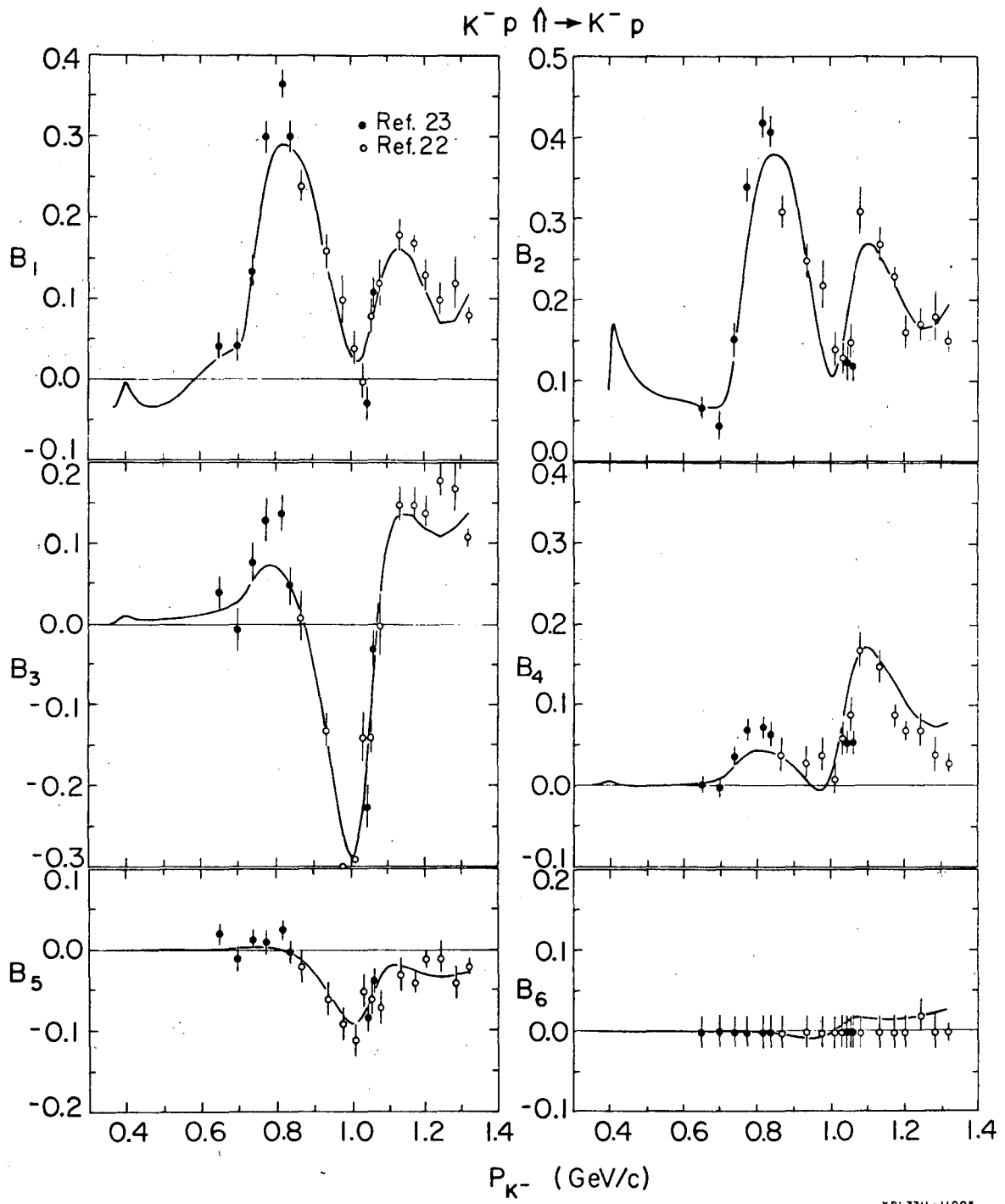


Fig. 6

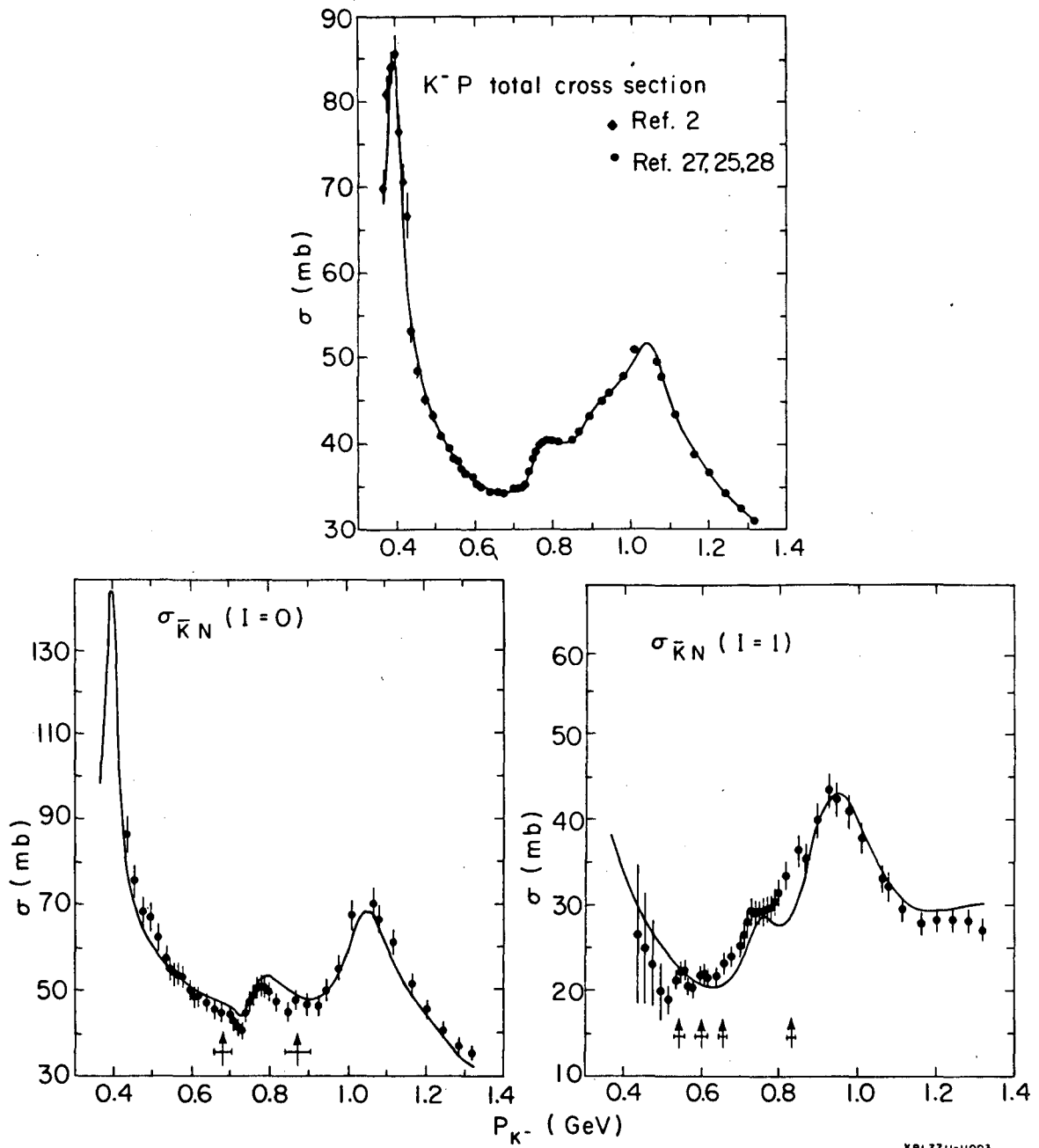
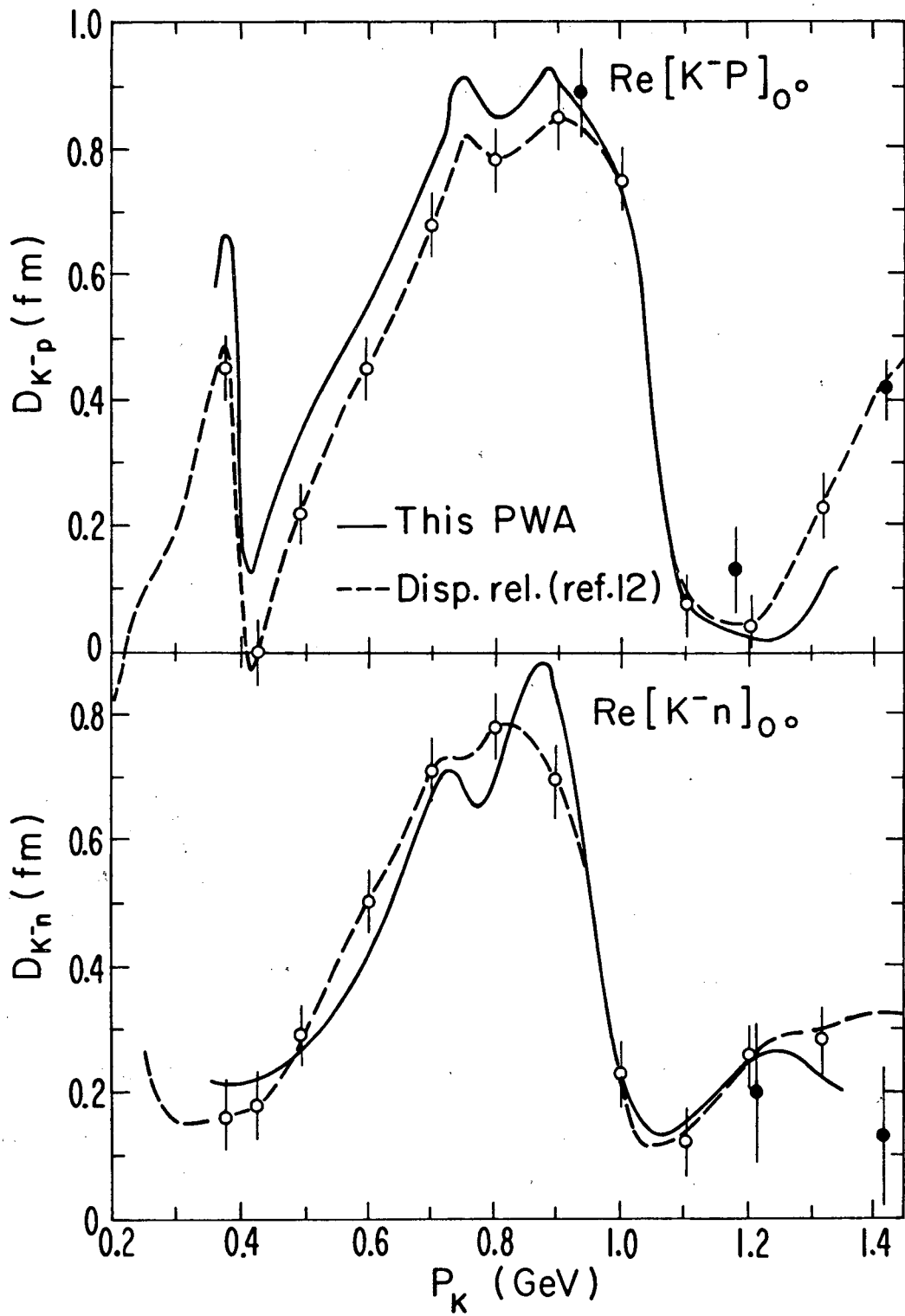
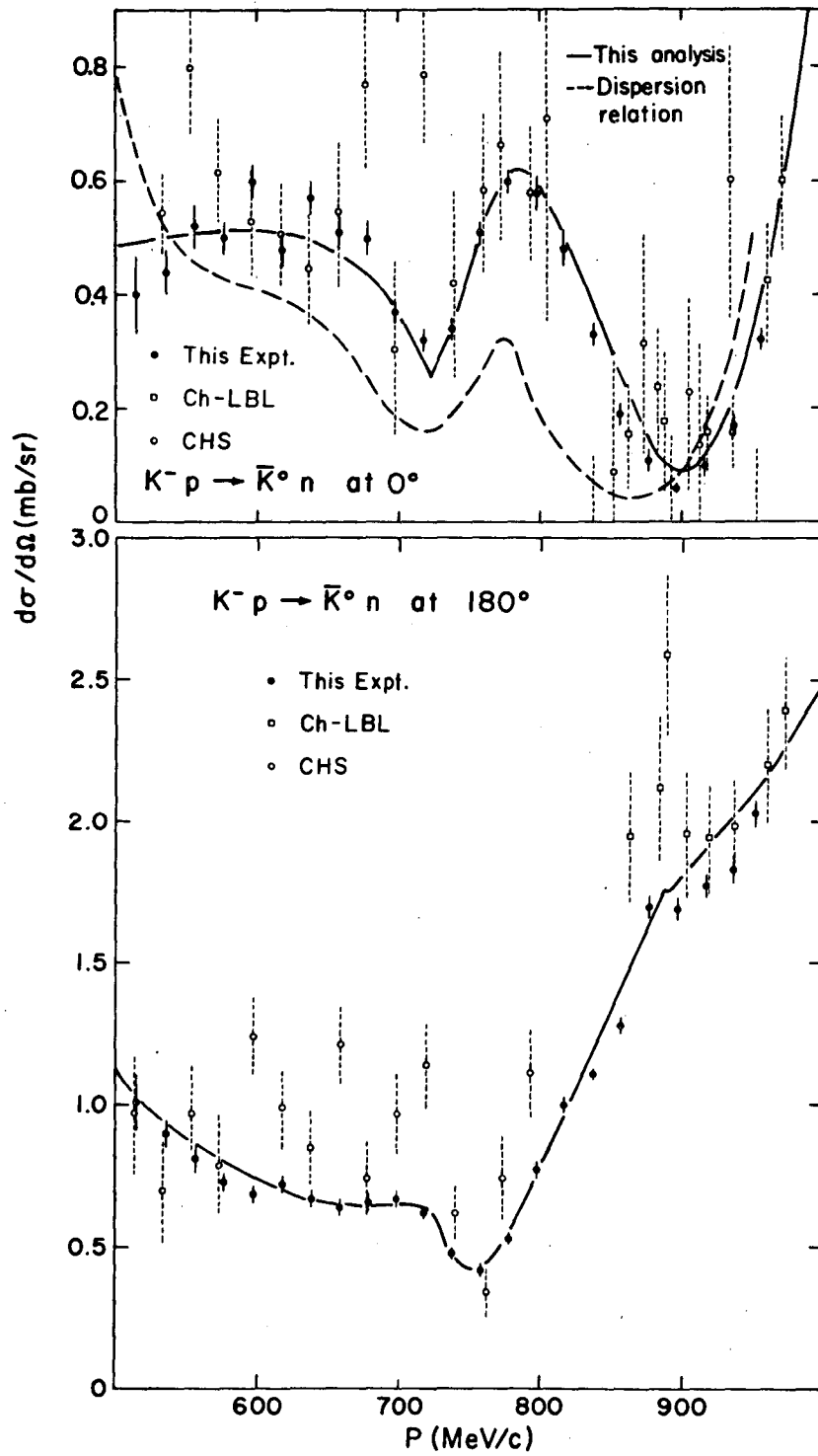


Fig. 7



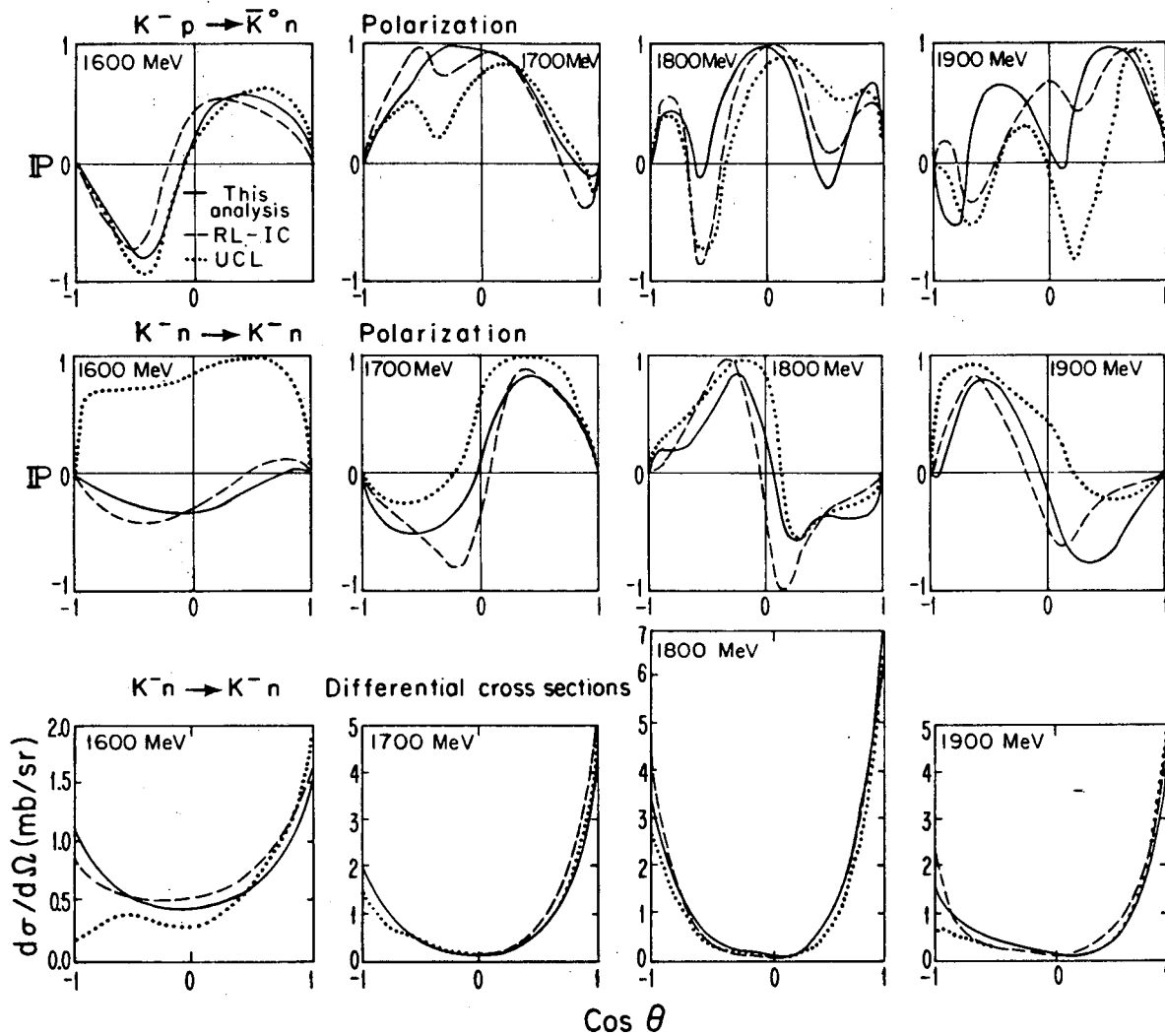
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Fig. 8



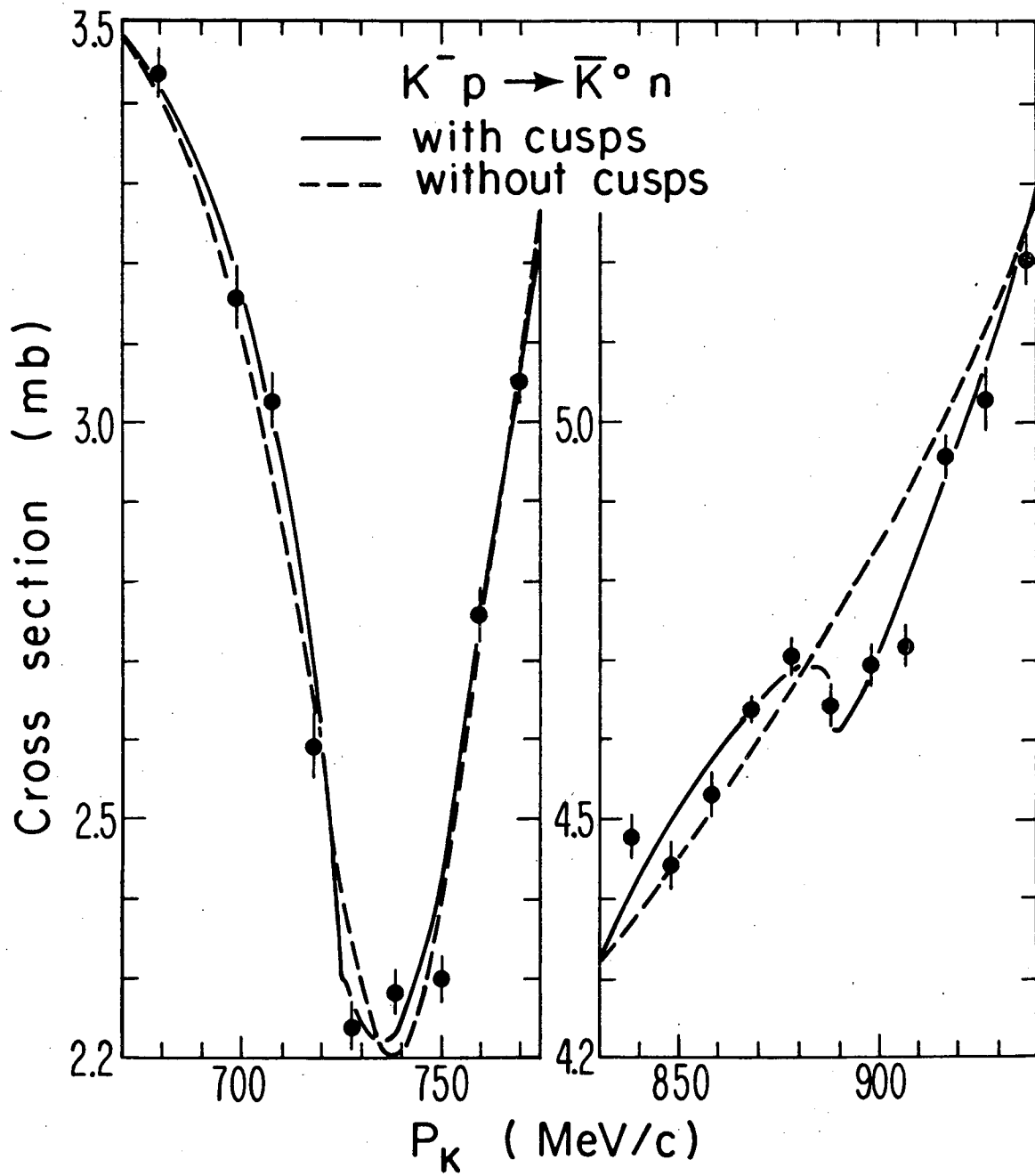
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Fig. 9



XBL7711-11006

Fig. 10



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Fig. 11

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