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A chaotic-dynamical conceptual model to describe fluid flow and Contaminant Transport in a fractured vadose zone

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### **Publication Date**

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## A Chaotic-Dynamical Conceptual Model to Describe Fluid Flow and Contaminant Transport in a Fractured Vadose Zone

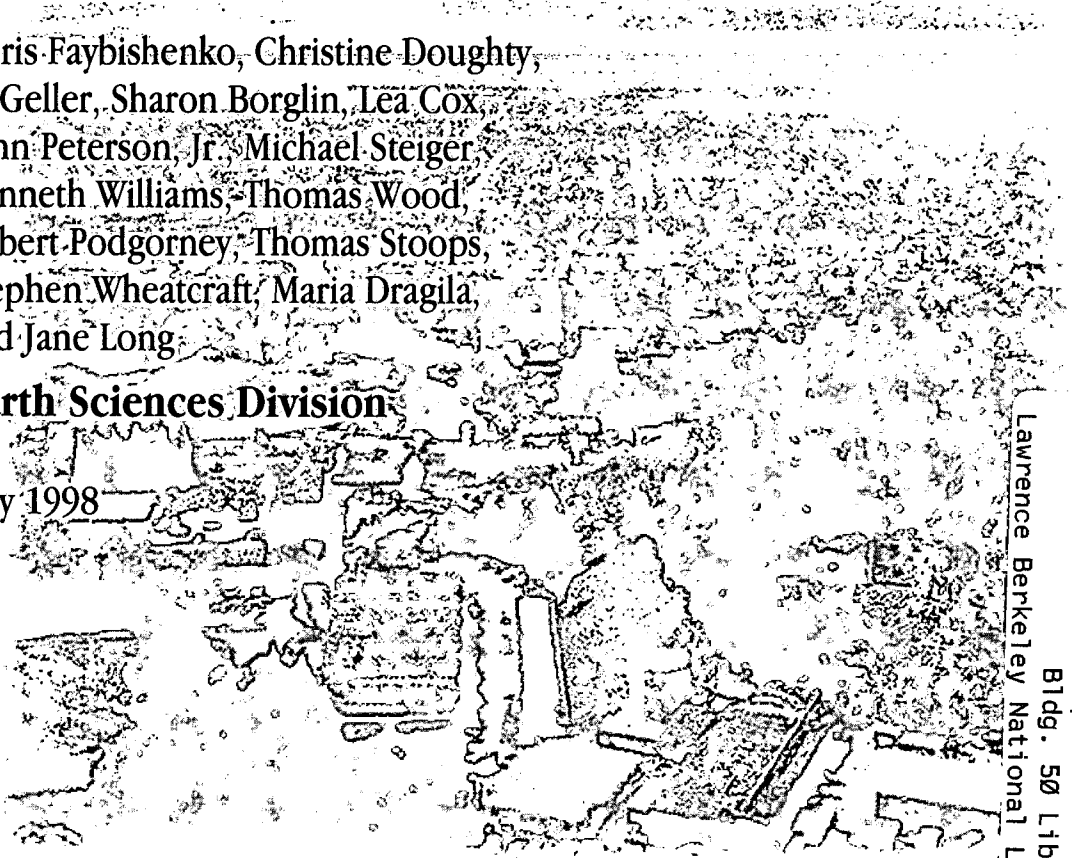
1997 Progress Report and Presentations  
at the Annual Meeting

Ernest Orlando Lawrence  
Berkeley National Laboratory  
December 3-4, 1997

Boris Faybishenko, Christine Doughty,  
Jil Geller, Sharon Borglin, Lea Cox,  
John Peterson, Jr., Michael Steiger,  
Kenneth Williams, Thomas Wood,  
Robert Podgorney, Thomas Stoops,  
Stephen Wheatcraft, Maria Dragila,  
and Jane Long

Earth Sciences Division

July 1998



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**A Chaotic-Dynamical Conceptual Model to Describe Fluid Flow and  
Contaminant Transport in a Fractured Vadose Zone**

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July 1998

1997 Progress Report and Presentations at the Annual Meeting held at  
Ernest Orlando Lawrence Berkeley National Laboratory on  
December 3-4, 1997

**Lawrence Berkeley National Laboratory  
EMSP Annual Progress Report - December 1997**

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# I.

## FY 97 Summary Report:

### **A Chaotic-Dynamical Conceptual Model to Describe Fluid Flow and Contaminant Transport in a Fractured Vadose Zone**

#### **ABSTRACT**

Understanding subsurface flow and transport processes is critical for effective assessment, decision-making, and remediation activities for contaminated sites. However, for fluid flow and contaminant transport through fractured vadose zones, traditional hydrogeological approaches are often found to be inadequate. In this project, we examine flow and transport through a fractured vadose zone as a deterministic chaotic dynamical process, and develop a model of it in these terms. Initially, we examine separately the geometric model of fractured rock and the flow dynamics model needed to describe chaotic behavior. Ultimately we will put the geometry and flow dynamics together to develop a chaotic-dynamical model of flow and transport in a fractured vadose zone.

We investigate water flow and contaminant transport on several scales, ranging from small-scale laboratory experiments in fracture replicas and fractured cores, to field experiments conducted in a single exposed fracture at a basalt outcrop, and finally to a ponded infiltration test using a pond of 7 by 8 m. In the field experiments, we measure the time-variation of water flux, moisture content, and hydraulic head at various locations, as well as the total inflow rate to the subsurface. Such variations reflect the changes in the geometry and physics of water flow that display chaotic behavior, which we try to reconstruct using the data obtained.

In the analysis of experimental data, a chaotic model can be used to predict the long-term bounds on fluid flow and transport behavior, known as the attractor of the system, and to examine the limits of short-term predictability within these bounds. This approach is especially well suited to the need for short-term predictions to support remediation decisions and long-term bounding studies.

#### **I.1 OBJECTIVES AND STRUCTURE OF THE PROJECT**

Our primary objective is to determine when and if deterministic chaos theory is applicable to infiltration of fluid and contaminants through the vadose zone in fractured rock. To the extent that

this theory is applicable we will develop algorithms for predicting flow and transport based on this theory.

In classical analysis, the system components are commonly taken to be cubes of equivalent porous media that tessellate the volume of interest. The rules used to describe multi-phase fluid flow are commonly given by Richard's Equation, a version of Darcy's Law, which describes how much fluid will be transferred as a function of the hydraulic head gradient and relative permeability.

For the case of infiltration in fractured rock, we will describe the geometry of the fracture network and determine the rules describing how fluid is transmitted as dynamical processes. The result of evaluating these processes will be an entirely new approach to the description of flow and transport behavior. The objectives of this project will be achieved through the development of:

- A hierarchical description of fracture geometry that controls fluid flow and transport,
- A dynamical description of infiltration and transport of contaminants in single fractures,
- An algorithm for flow and transport that combines the hierarchical geometry and the description of dynamical flow and transport,
- Appropriate techniques needed to detect chaotic behavior of flow in the field,
- Evaluation of deterministic chaos in laboratory and field experiments,
- Field investigations were conducted at the Box Canyon site in Idaho near the INEEL.

## **I.2 BACKGROUND INFORMATION ON CHAOTIC DYNAMICS AND FRACTAL STRUCTURES**

One of the central problems in the prediction of water, heat, and mass transfer in soils and fractured rocks is how to use past observations in order to predict the future. Field measurements can only employ a limited number of probes that cannot collect all needed information. Consequently, the quality of prediction using classical deterministic and stochastic differential equations with a set of initial and boundary conditions and volume-averaged parameters may be poor. One of the alternative approaches views a time series of data as a result of chaotic dynamics, which can appear even in a simple deterministic system. Random-looking data may in fact represent chaotic rather than stochastic processes. For predictive purposes, it is critical to recognize which is which, because for chaotic systems often only short-term predictions can be made. For example, it was shown that the weather predictability will approach zero for predictions of more than two weeks (Lorenz, 1982).

The differences between regular (non-chaotic deterministic), random, and chaotic systems are illustrated in Figure 2.1, which shows trajectories typical for each type of motion. Note that the flow trajectories for chaotic systems are different from both regular and stochastic systems. In general, the term chaotic process is used to describe a dynamical process with the following features: random processes are not a dominant part of the system, the trajectories describing the future states of the system are strongly dependent on initial conditions, adjacent trajectories diverge exponentially with time, the information on initial conditions cannot be recovered from later states of the system, and behavior is often characterized by an attractor that has a fractal geometry.

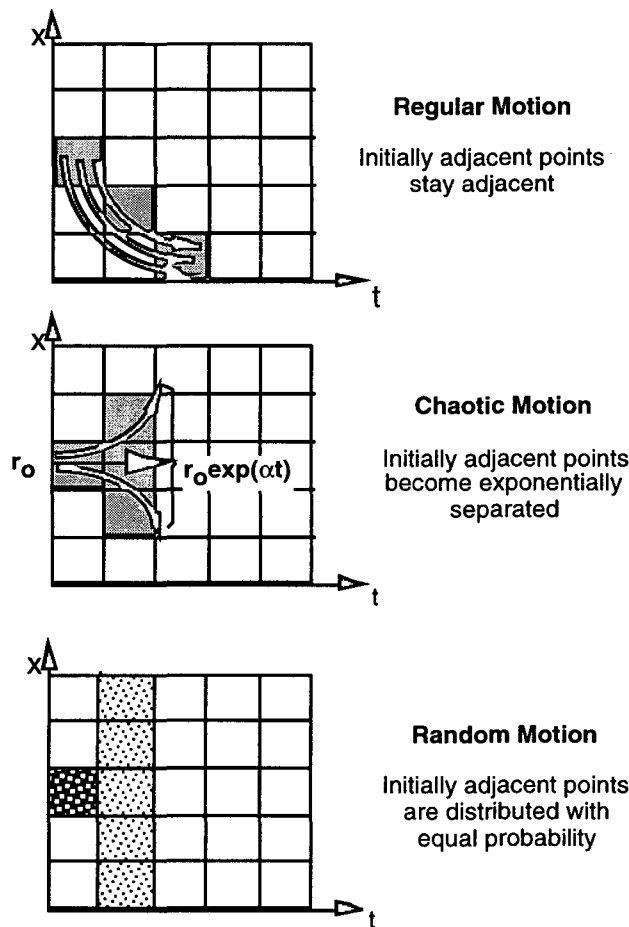


Figure 2.1 Comparison of regular (i.e., non-chaotic deterministic), chaotic, and random behavior (modified from Schuster, 1993).

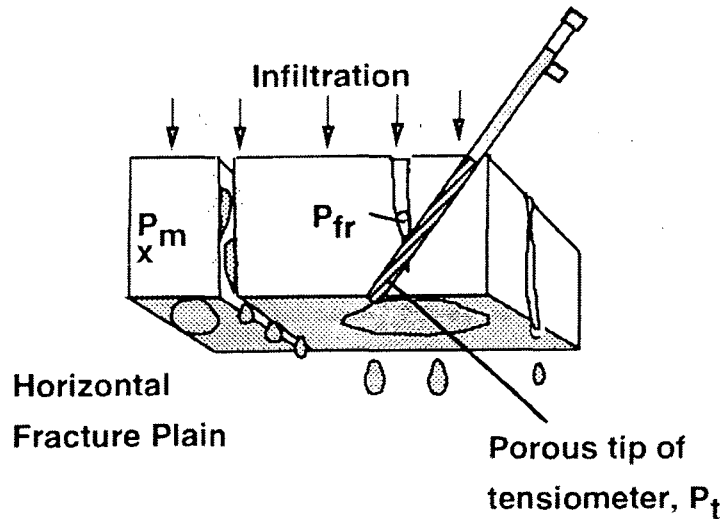
Chaotic flow behavior in heterogeneous fractured media may result from hydrodynamic instabilities and a sensitive dependence of flow on (1) boundary conditions (precipitation, ambient temperature and pressure, groundwater fluctuations, etc.), (2) initial conditions (distribution of water content, pressure, and temperature), and (3) the current state of the system (water content, pressure, and temperature). Flow depends upon coupled effects of several non-linear factors such as the geometrical connectivity of the fracture system, air entrapment and its removal, clogging of the conductive fractures, biofilms, kinetics of the matrix-fracture water exchange, variability of effective hydraulic porosity and hydraulic permeability, and others.

The coupled effect of several non-linear processes in an unsaturated heterogeneous and fractured material causes non-linear behavior, governed by non-linear ordinary and partial differential equations, which may have bounded, nonperiodic solutions. These equations may be either: (1) purely deterministic where no random quantities appear in the equations (Moon, 1987; Tsonic, 1992), (2) chaotic-stochastic, or (3) have a noisy component (Kapitaniak, 1988). Therefore, one of the main problems in data analysis is to properly identify the type of the equation describing the flow system.

There are numerous examples of dynamical systems that display non-linear chaotic behavior for some system parameters. Some examples relevant to our study are: avalanche fluctuations



resulting from the perturbation of sandpiles of various sizes (Rosendahl et al., 1993), falling off of water droplets (Cheng et al., 1989), atmospheric temperature, river discharge, and precipitation (Pasternack, 1996; Pelletier, 1996), and oxygen isotope concentrations (Nicolis and Prigogine, 1989). One of the simplest examples is a dripping faucet (Shaw, 1984). Figure 2.2 shows a conceptual model of flow in fractured rocks based on a model of irregularly dripping water through a fracture, which produces non-periodic and non-repetitive behavior in both time and space.



**Figure 2.2** Conceptual model of flow and measurement in partially saturated fractured rocks.  $P_m$  = matrix water pressure;  $P_{fr}$  = fracture water pressure;  $P_t$  = tensiometer water pressure

It has been recognized that fractal structure is a possible indication of chaotic behavior of a system (Mandelbrot, 1977). Fractal analysis has been applied to many earth sciences problems, such as topography, fault traces, fracture networks, fracture surfaces, porous aggregate geometry, permeability distribution, flow and transport through heterogeneous media, erosion and chemical dissolution, etc. La Pointe (1988) used fractal geometry to characterize fracture density and connectivity. There are several papers in which the fractal properties of fractured tuff at Yucca Mountain were investigated (e.g., Carr, 1989). Fractal analysis was also used to predict bypass flow in rocks (Nolte et al., 1989; Cox and Wang, 1993) and clay soils with vertically continuous macropores (Hatano and Booltink, 1992).

### **I.3 LABORATORY TESTS (LBNL)**

#### ***I.3.1 Introduction and Motivation***

Observations of water seepage in fractures in the laboratory have shown the pervasiveness of highly localized and extremely non-uniform flow paths in the plane of the fracture (Geller et al., 1996). These channels exhibit intermittent flow behavior as portions undergo cycles of draining and filling, and small connecting threads snap and reform. This unsteady behavior occurs even in the presence of constant pressure boundary conditions. These observations motivated us to study dripping water between parallel plates as an idealized model of some of the flow behavior characteristic of water seepage through fractured rock. This study extends the classic chaos

experiment of the “dripping faucet” to drips in the presence of capillary forces as they are affected by the surface properties and the small aperture of the parallel plates.

The objective of these experiments is to collect data records that can be analyzed to determine whether or not, and under what conditions, the dripping of water in parallel plates is chaotic, random, or periodic. This work was further motivated by preliminary experiments that showed the sensitivity of pressure measurements to the formation and release of water drops through a needle in open air and inserted between parallel plates. Much of this year’s work was invested in developing the experimental system to reliably obtain usable data records.

### ***1.3.2 Experimental Results***

Experiments were performed at a variety of flow rates to evaluate the system for chaotic behavior. Four basic types of experiments were conducted. Type A are pressure fluctuations caused by the 28 gauge needle dripping water into open air. Type B measure the baseline pressure fluctuations of the 28 gauge needle delivering water with a constant pressure condition at the needle outlet. (A constant pressure at the needle outlet was maintained by submerging the needle tip under water.) Type C use the 28 gauge needle to deliver water between smooth glass plates with a 0.35 mm gap at an angle of 60 degrees from the horizontal. Type D are identical to type C except for the use of rough glass plates. In each experiment, a constant flow rate of water was delivered as the magnitude of the pressure at the syringe needle was measured.

The smooth glass plates (type C) experiments were run at flow rates of 0.25, 0.5, 1.0, 1.5, 2.0, and 3.0 ml/hr. Typical pressure data for these flow rates are shown in Figure 3.1. In Figure 3.2 the frequency of drips and height of the average pressure fluctuation are plotted against the flow rates of the experiments in Figure 3.1. The experiments plotted in Figure 3.2 show a trend toward more frequent drip events and decreased height of pressure fluctuation as the flow rate increased. Visual observation of the drip events confirmed an increase in length of the thread of water as flow rate increased. However, duplicate experiments at each flow rate demonstrated that both the height of pressure fluctuations and the frequency of the drips vary between type C experiments with the same flow rate. The formation of the threads appear to depend qualitatively upon the initial condition of the plates. Some of the factors suspected to influence the drip frequency and length of thread formation are the amount of moisture on the plates, whether the drip was following a pre-existing flow path determined by a previous flow rate, and the cleanliness of the plates.

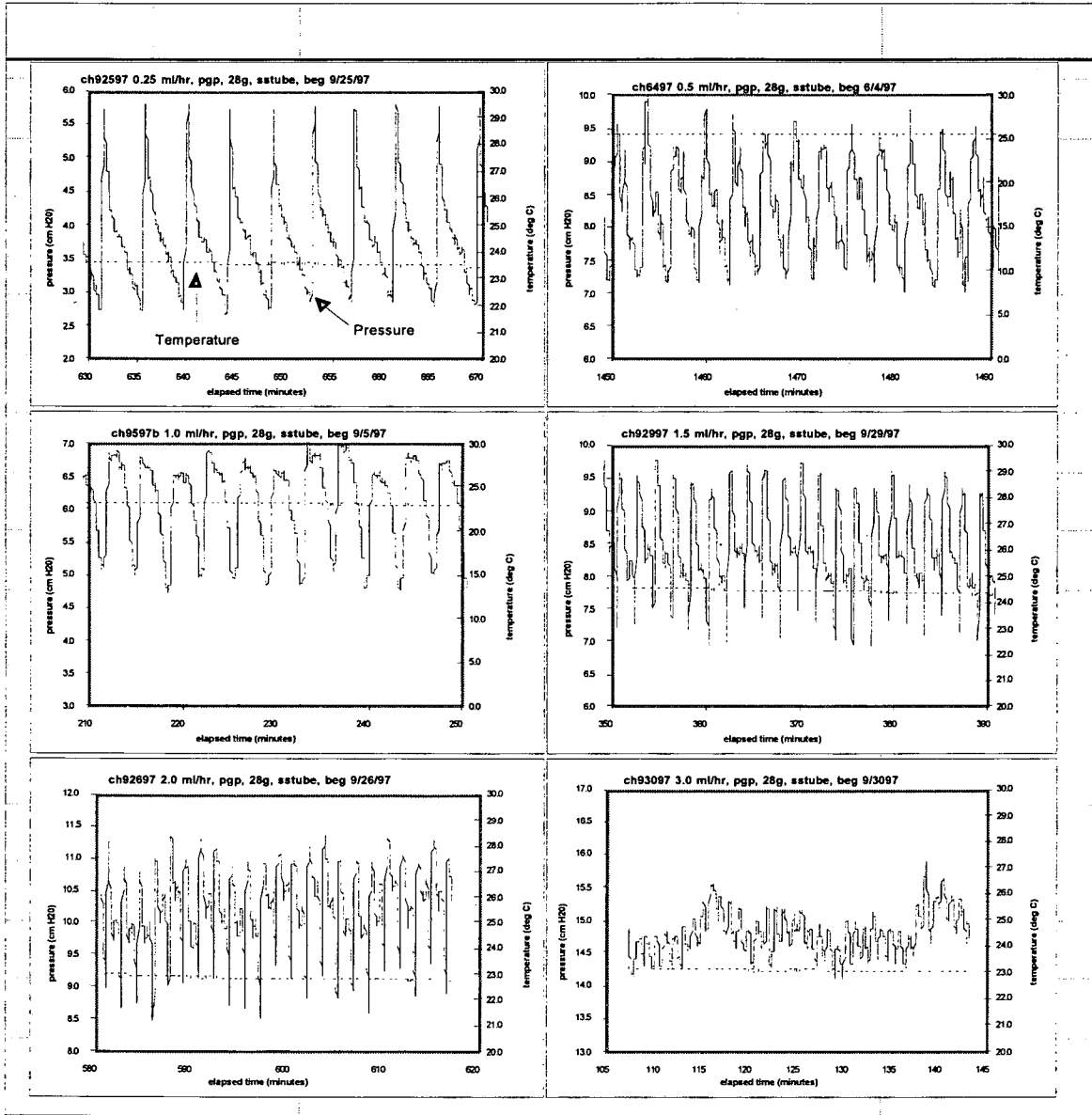


Figure 3.1: Smooth parallel glass plates. Pressure fluctuations caused by dripping water between smooth parallel glass plates at flow rates of 0.25, 0.5, 1.0, 1.5, 2.0, 3.0 ml/hr.

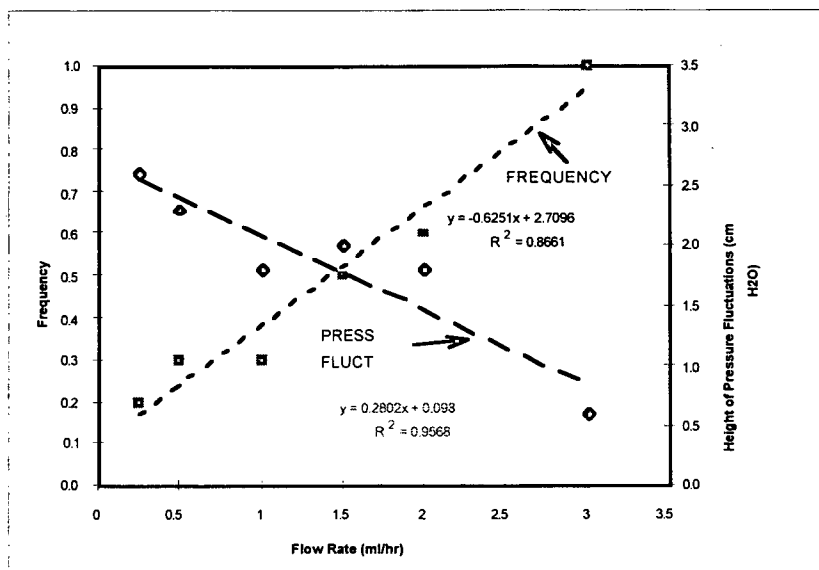


Figure 3.2: Observed trends in frequency and magnitude.

Experiments in roughened glass plates were conducted to test the effect of surface variability on drip behavior. Two types of plates were utilized: sand-blasted and shower-door glass (type D) plates. Both plates were separated by 0.35 mm shims. The sandblasted plates had an overall consistency of fine sandpaper with an even coating of fine (approximately 0.1 mm) irregularities on the surface. When the water was introduced into the sandblasted plates, a halo developed on the plate as the water advanced and film flow occurred, but drops did not form. The pressure signature observed from the sandblasted plates was similar to that observed for the baseline monitoring (see below).

The shower-door glass plates had larger, smooth irregularities or nubs on the surface (average scale of 2-3 mm). When the drips were introduced into the shower glass plates, the larger spaces between the nubs allowed drips to form at the end of the needle. The drops grew to different sizes before they snapped off and moved down the plate. Occasionally, short threads formed before the drop snapped off completely. After snapping off, the drop either moved quickly down the plate and was removed from the system or it remained close to the end of the needle, held back by a narrow throat formed by adjacent nubs. When the next drop formed, it tended to combine with the previous drop and the new larger drop would travel down between the plates.

The pressure fluctuation from the drips of water from the 28 gauge needle into open air (type A experiments) were recorded as a basis for comparison to the glass plate experiments. It was determined that the presence of capillary forces induced by the glass plates causes a decrease in drip frequency and a decrease in the height of the pressure fluctuation.

The experiments demonstrate the variation of observed pressure fluctuations and the importance of both identifying and controlling initial conditions to achieve consistent results. Although quantitative analysis of the results is not yet complete, these features suggest that chaotic dynamics play an important role.

#### I.4 FRACTURED ROCK OUTCROP EXPERIMENTS (INEEL)

The outcrop scale experiments were designed and conceptualized to fill a gap of knowledge between the laboratory and field (Box Canyon, Idaho) scales of investigation. A research site was

selected at Hell's Half Acre Lava Field in Idaho where a single fracture could be studied. The site consisted of a basalt outcrop approximately 1 m thick that extended approximately 1.5 m outward from the rock wall. An infiltration gallery (0.5 x 1 m) was constructed above the fracture to perform constant head infiltration tests. On the underside of the overhang, drip sensors were installed to count and timestamp drops of water falling from the fracture. More traditional monitoring parameters, such as tension, temperature, and barometric pressure were also collected. Figure 4.1 shows the general site and instrument layout.

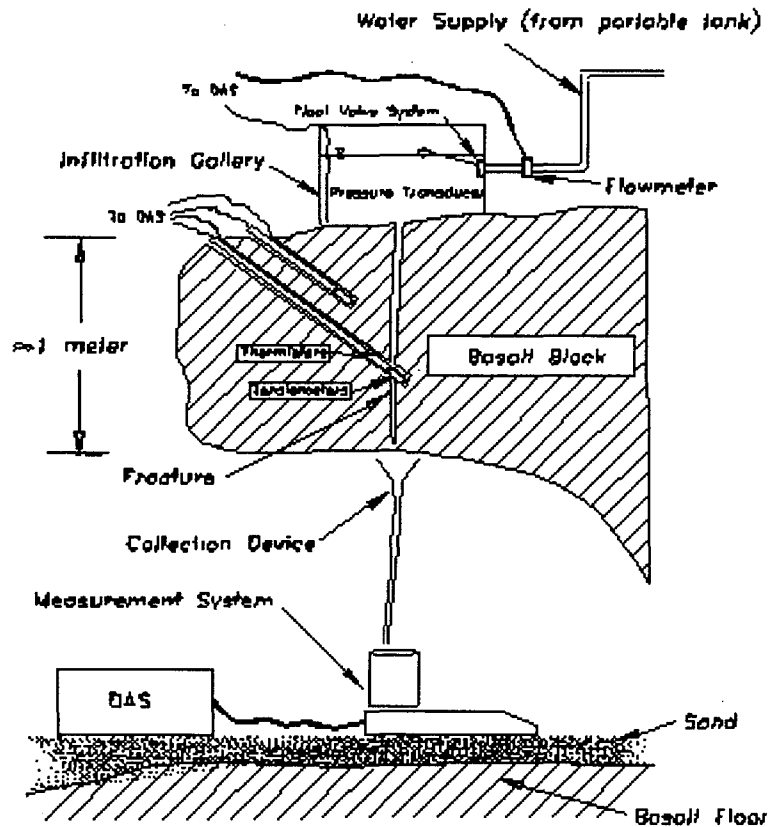


Figure 4.1. Field site characteristics and instrument layout. Note figure not to scale.

The field site was instrumented to collect data that would be amenable to a chaotic-dynamical analysis, which typically requires long time-series of data. Data collected included time stamping individual drip events for 20 distinct drip locations (to perform an analysis similar to that in Shaw, 1984); measurements of the inflow and outflow rates into the system (to compare temporal and spatial variability as well as do mass balance calculations); and moisture tension, temperature, and barometric pressure (to examine and compare with flow and drip data).

#### ***1.4.1 Field Test Setup and Instrumentation***

Field work at the site began in June 1997 and continued until October 1997. Seven ponded infiltration tests were conducted, each with 4 to 48 hour duration and a varying amount of dry-out time (hours to weeks) between tests. Individual drips were monitored as they landed, using an array of specially designed piezo-electric sensors that sent a signal to the data acquisition system in response to the pressure increase accompanying a landing drip.

### ***1.4.2 Field Observations and Preliminary Data Analysis***

Preliminary reductions indicate that between 0 and 20,000 drips were collected for each location during each test. During the later tests (4-7) over 5,000 drip events were recorded at approximately 50% of the drip locations. The parameters of moisture tension, temperature, barometric pressure, and flow rates/water levels were collected at 1 minute intervals for the duration of the tests.

As the data analysis has yet to be conducted, a detailed discussion of the results cannot be presented at this time, however the following were observed during the testing:

- Flow rates were observed to vary between and during tests, ranging from near negligible inflow rates to as high as 0.8 l/min;
- The ambient moisture conditions in the basalt may exhibit some control on the flow through the fracture;
- Temporal and spatial variability was observed in the location of the first appearance of drips.

### **I.5 BOX CANYON PULSED PONDED INFILTRATION EXPERIMENT (LBNL)**

The Box Canyon, Idaho experiment consists of a series of pulses of ponded infiltration, in which a fixed volume of water containing a known concentration of tracer (potassium bromide) is added to the pond all at once, allowed to infiltrate for two days, then pumped out of the pond, allowing air to enter the subsurface. This sequence of water and air boundary conditions is believed to be conducive to the development of chaotic flow and chemical transport behavior in the fractured basalt. In addition to monitoring water infiltration and evaporation rates from the pond, two types of measurements were conducted in the subsurface below the infiltration pond in order to study the flow and transport behavior in fractured basalt. First, time series of measurements at point locations were collected, to study the local dynamics of flow and transport and examine it for chaotic behavior. Second, snapshots of the spatial distribution of moisture and tracer movement were collected with geophysical techniques, to study the geometrical pattern of flow and transport and examine it for evidence of fractal geometry.

#### ***1.5.1 Infiltration Tests and Pond Data Collected***

Three pulse infiltration tests of approximately 48 hours each were conducted in September-October 1997. Table 5.1 shows specifics for each test.

Table 5.1. Pulsed ponded infiltration tests conducted at Box Canyon in 1997.

Beginning of ponding	Test number	Volume added (m <sup>3</sup> )	Duration of ponding (days)	Volume infiltrated and evaporated (m <sup>3</sup> )
9/11/97 12:15	1	11.23	2.02	5.55
9/18/97 14:56	2	11.03	2.08	5.37
10/2/97 15:40	3	11.00	2.01	4.63

Potassium bromide slurry was added to the tanks before each test resulting in a concentration of approximately 3 mg/L. Water samples were taken from the tanks and the pond once infiltration began to check for uniformity of concentration. Analysis of these water samples is ongoing.

Water levels in the pond were measured and cumulative infiltration rates accounting for evaporation were calculated for each test. Evaporation was monitored using a pool within the berm walls. As can be seen from the final column of Table 5.1, the cumulative flow rate into the pond decreased from pulse to pulse.

### ***1.5.2 Point Measurements***

Time domain reflectometry (TDR) measurements were taken during the three infiltration tests and during dormant periods. During infiltration, measurements were taken every 15 minutes, and during dormant periods, every 1 or 2 hours, depending on the length of time between the tests.

Electrical resistivity (ER) measurements using miniature ER probes were taken at 15 minute intervals during and between tests. Forty-five existing probes installed at multiple depths in 5 wells were used as well as newly installed single probes placed in the bottom of 3 wells. Thirteen probes were placed within the pond, and 1 probe was placed in the water tank.

Tensiometry measurements of water pressure were done using 26 tensiometers installed within and outside the pond.

Water sampling was conducted using suction lysimeters installed in boreholes. Sampling was carried out a total of 17 times. The purpose of the sampling was to detect the movement of the bromide tracer, and construct breakthrough curves as the water infiltrated downward through the fractured basalt. Analysis of the water samples is ongoing.

### ***1.5.3 Geophysical Measurements***

Neutron well logging provides a one-dimensional picture of moisture distribution. It was carried out in 7 wells 10-12 times before, during, and after each ponding period. Preliminary results indicate increases in water content during infiltration in wells located within and close to the pond.

Cross-borehole ground penetrating radar (GPR) provides a two-dimensional tomogram of moisture distribution by using variations in the velocity of electromagnetic waves with dielectric constant. GPR surveys were conducted between six different well pairs. Preliminary analysis confirms that ambient conditions are wetter this year than last year, but radar tomograms still identify the central fracture zone and the rubble zone as low velocity zones.

Electrical resistivity tomography (ERT) provides a three-dimensional picture of the subsurface electrical conductivity distribution, which may be related to moisture distribution. ERT measurements were provided by Steam Tech, Inc. These measurements involved the development of special ER probes installed in three deep (20 m) boreholes outside the pond, three shallow (2 m) boreholes within the pond, and 15 surface ER probes. The data analysis is ongoing.

## **1.6 NON-LINEAR DYNAMICAL PROCESSES IN UNSATURATED FRACTURE FLOW (UNR)**

Systems exhibiting chaotic behavior are characterized by the ability to make short-term predictions. Long-term predictions are impossible because of an exponential loss rate of information on the system state. We identify and develop the conditions under which chaotic behavior in unsaturated flow can be expected so that realistic limits can be placed on predictions about the future state of the system. We cast the problem in terms of thin film flow in fractures with aperiodic saturation events using Navier-Stokes governing equations. Initial conditions consist of constant inflow rates at the top of the fracture. If the rates are small enough and surface tension dominates, the thin film will reach a steady flow rate. Above a certain threshold flow rate, as gravity begins to dominate, periodic solitons develop. Above still another threshold, aperiodic solitons take over, and the flow characteristics are chaotic.

## I.7 ESTIMATING TOTAL MASS OF CONTAMINANT PLUMES FROM SPARSE WELL DATA (LBNL)

A major problem we encounter in trying to develop models (chaotic or otherwise) for flow and transport in fractured basalts is that it is extremely difficult to develop a picture of the overall spatial structure of these processes from isolated point measurements, due to the extreme heterogeneity of the system.

We consider the estimation of the total mass of a contaminant plume as a model problem to investigate means of using sparse data effectively. Generally, the estimation of the volume or mass and shape of the plume is based on sampling and analyzing water and soil. We have generated several complex hypothetical contaminant plumes. We then test the ability of different prediction methods and different sample spacing to estimate the mass of the contaminant plume. Comparisons among the methods should tell us something about the performance of different estimation methods for different types of complex distributions. They should also indicate what resolution of sampling is required to make an acceptable mass estimation.

### I.7.1 Methods

We approach the problem of sample minimization by using several simulated heterogeneous distributions obtained from fractal generating algorithms, and a real distribution obtained from a fracture infiltration experiment. We initially select 15 well locations, based on a quasi-random scheme, along a two-dimensional cross-section. The extension of this approach to three dimensions would involve taking several two-dimensional cross-sections. The wells are sampled at equally spaced vertical intervals. Sequential predictions of the total mass of contaminant are computed as each successive well is sampled. Figure 7.1 shows the fractal plume and the wells used to sample the field. The numbers indicate the sequence in which the wells are sampled.

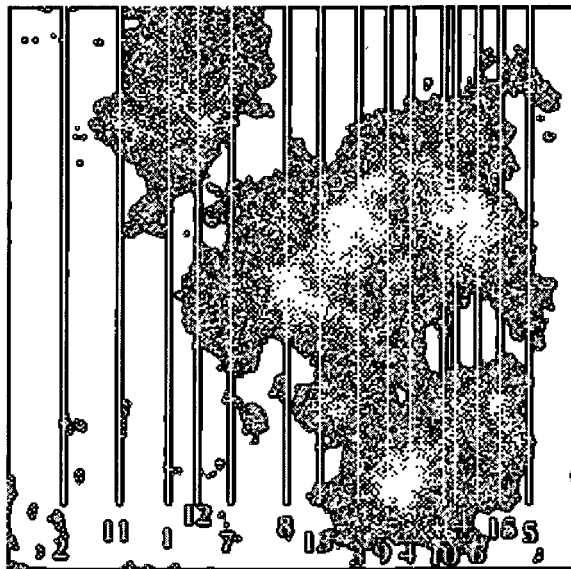


Figure 7.1. Synthetic contaminant plume with fractal geometry and locations of sampling wells.

We use several estimation techniques such as simple averaging, spatial integration, fractal and neural network models, to predict the total mass of the plume from the sample data. Parameters of the concentration distribution for the plume determined from the sparse well data were compared to those for the computer-generated plume. The convergence of the estimated plume mass to the



actual known mass, as well as the number of wells required for convergence, were used as criteria to compare the different methods.

### 1.7.2 Preliminary Results

Analyzing the concentration distribution, we found little or no spatial correlation between samples collected from adjacent wells, indicating that the wells are far enough apart to provide independent information. In general, for the examples we studied simple averaging, spatial integration, and neural network predictions performed comparably well and estimates of total mass did not significantly improve after five wells had been sampled. In contrast, the fractal-based methods proved less successful, in part because they depend strongly on the value of the fractal dimension of the plume, which is very difficult to determine from sparse well data. A comparison of some of the estimation methods is plotted in Figure 7.2 for a synthetic fractal plume with a fractal dimension prescribed to be 1.5. This plot shows how the estimation changes as each additional well is sampled. The bar indicates a perfect estimation. Interestingly, the least successful method is a fractal-based method that assumes a fractal dimension of 1.5, supposedly the actual fractal dimension of the plume. The much better performance of a fractal method that uses a fractal dimension of 1.3 suggests that perhaps the algorithm used to create the plume does not actually produce the desired fractal dimension. This topic is currently under investigation.

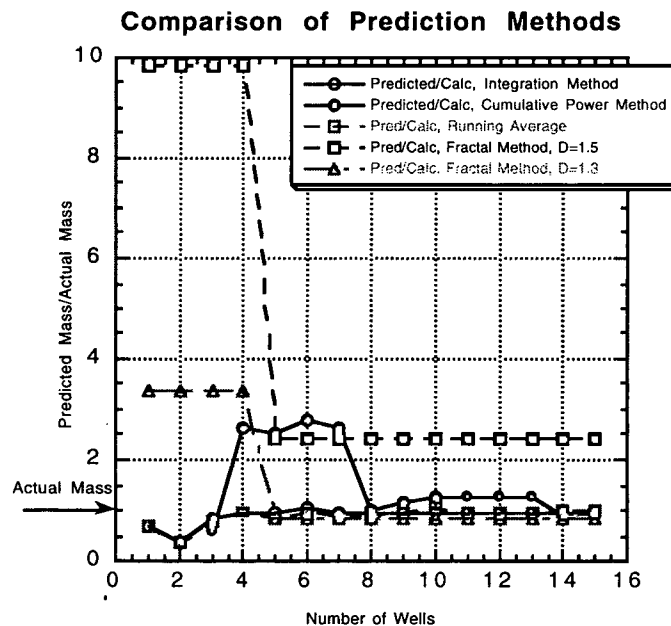


Figure 7.2. Summary of predictions for a fractal plume with a fractal dimension prescribed to be 1.5. The curves labeled cumulative power method, fractal 1.5, and fractal 1.3 all use various forms of fractal-based approaches.

## **I.8 TOPICS OF ON-GOING RESEARCH**

### ***I.8.1 Theoretical***

- Study the physics of water flow and chemical transport in fractured rocks using dynamical models of chaos theory, fuzzy logic, and a combined fuzzy-chaotic approach (a tool for managing and optimizing remediation activities under conditions for which chaotic processes are important).
- Use fractal and neural network approaches to determine three-dimensional spatial distributions of properties or processes in soils and fractured rocks from point-type measurements in boreholes.
- Apply the theory of linguistic variables to lithological analysis of data from boreholes.
- Re-examine water flow and tracer transport in fractured basalt from the Large-Scale Infiltration Test in light of chaotic dynamic models.
- Compare laboratory and field methods for the determination of quasi-saturated hydraulic conductivity of soils, and use a deterministic-chaotic model to describe a variable hydraulic conductivity within the zone of fluctuation of water table.
- Examine the relationship between the spatial structure of geologic heterogeneity (using methods of fractal geometry) and chaotic dynamics, as related to infiltration through a fractured basalt vadose zone.
- Construct and investigate fractal structures created with iterated function systems (IFS), which can simulate realistic characteristics of natural fracture patterns in basalt.

### ***I.8.2 Experimental***

- Evaluate the performance of tensiometers in fractured rocks, using laboratory cores and modeling, taking into account the interaction between the matrix and fractures.
- Use ground penetrating radar to investigate flow in soils and fractured rocks.
- Use 2-D and 3-D ERT to evaluate zones of preferential flow in fractured rocks.
- Conduct a series of pulsed infiltration tests at Box Canyon and Hell's Half Acre field sites in Idaho.

## **I.9 ACKNOWLEDGMENT**

This work was sponsored by the Environmental Management Science Program managed by the Office of Environmental Management and the Office of Energy Research, of the U.S. Department of Energy under Contract No. DE-AC03-76SF00098. The report was reviewed by Ardyth Simmons and Janet Jacobsen.

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# II.

## APPENDIX

### PRESENTATIONS AT THE ANNUAL MEETING.

DECEMBER 3-4, 1997

## II.1

# BOX Canyon Infiltration Test Summary of 1996-97 Results

**Boris Faybishenko and Michael Steiger**

Goal: Develop a conceptual model of geometry and physics of liquid flow and chemical transport for an intermediate scale of investigations in unsaturated-saturated fractured basalt

# Environmental Management Sites with Fracture Rocks

• INEEL, Idaho, Basalt

• NTS, Nevada, Tuff

• Oak Ridge, Tennessee,  
Shale & karst

• LANL, New Mexico  
Tuff and basalt

• Hanford, Washington  
Basalt

• SLAC, California  
Sedimentary rock

• PPL, New Jersey  
Sandstone & shale aquifer

# Outline

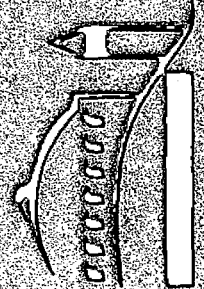
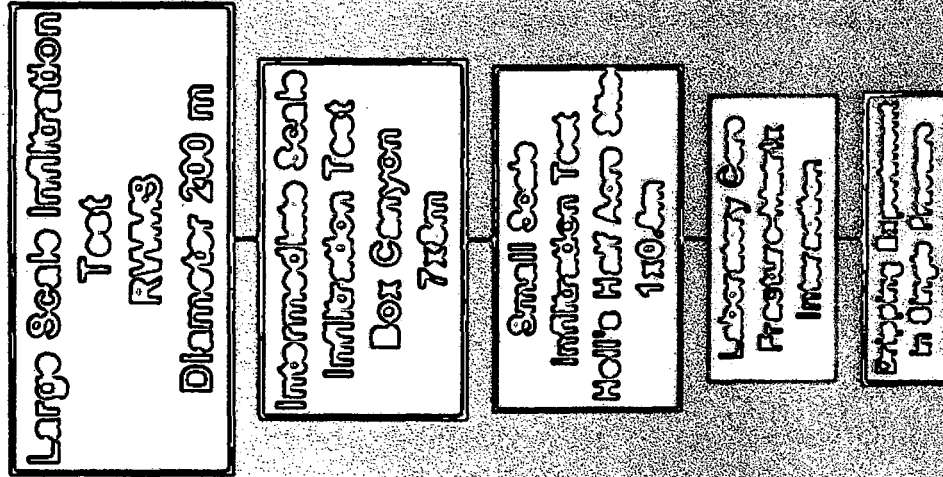
- Box Camyon site in a hierarchy of investigations in fractured basalt
- Geology
- Well layout, types of measurements and tests
- Flow rate
- Water pressure
- Breakthrough curves
- Water level in boreholes
- Moisture content
- Borehole single ER probes
- Conclusions

# INEEL Needs

- VOCs and radionuclides (Cs, Sr, U, Tc) in groundwater and perched water zones in *fractured rock* at 200 to 600 ft depths

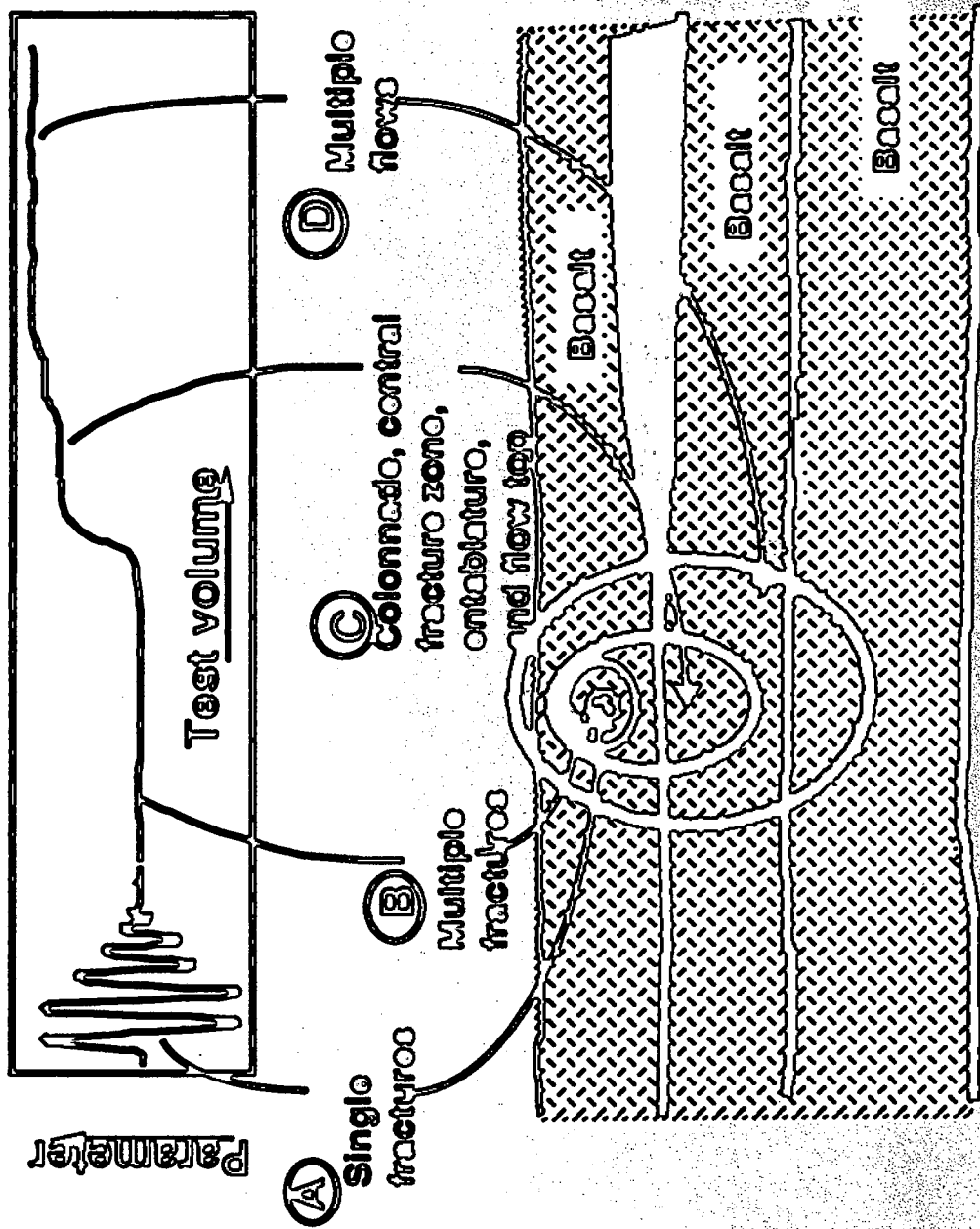


# Hierarchy of Tests

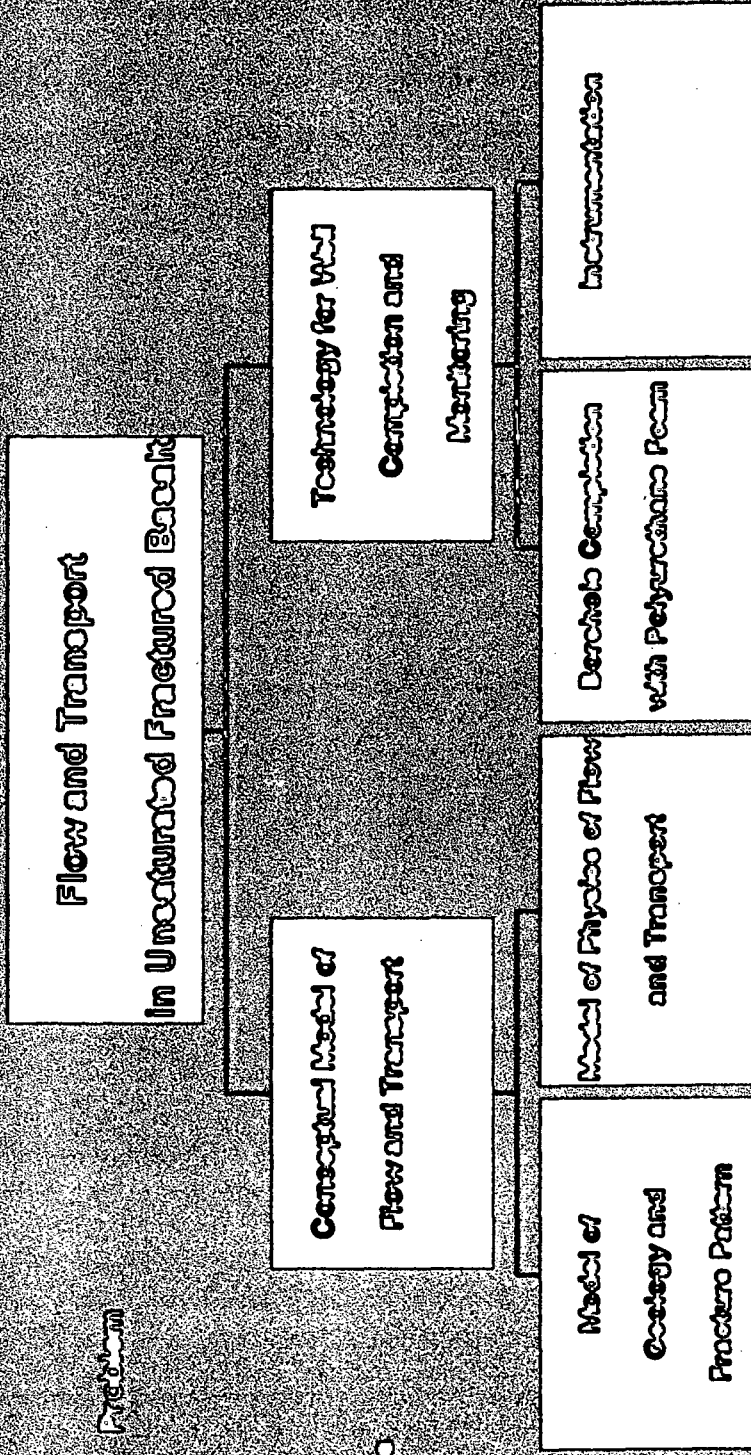


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# Hierarchy of Scales in Basalt



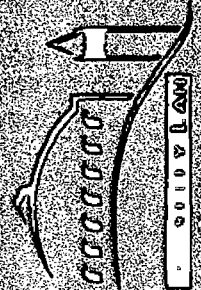
Modified from DOE, 1986



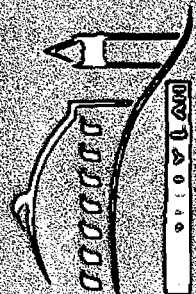
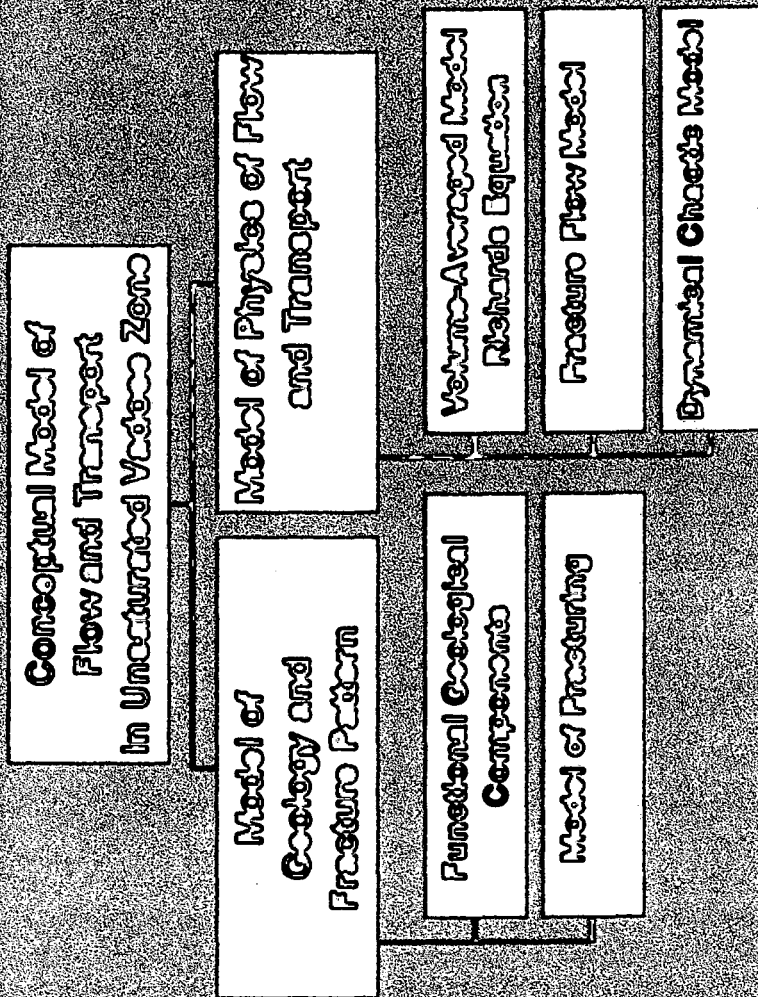
Problem

Concepts

Steps



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UNIVERSITY OF MARYLAND

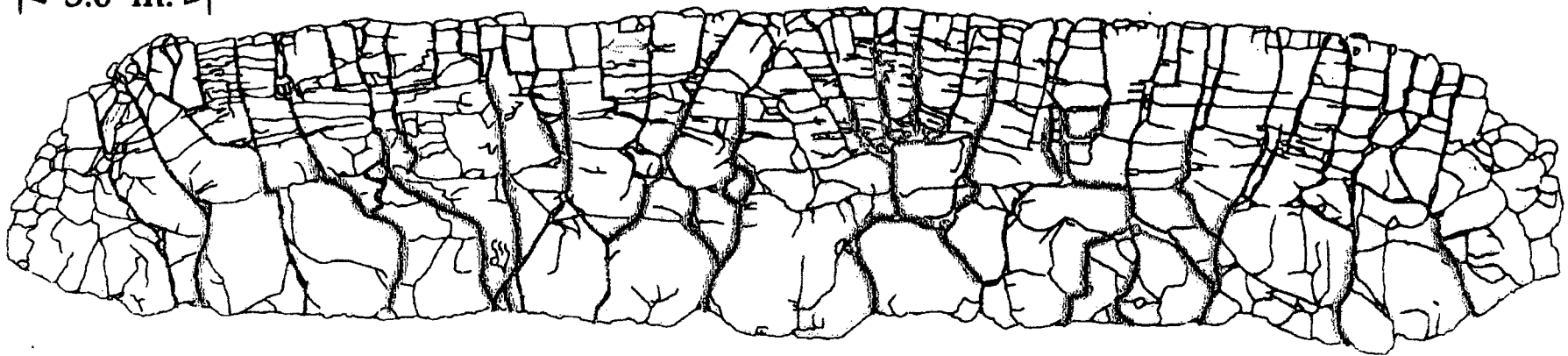


CENTRO DE GEOLOGIA APLICADA  
 INSTITUTO NACIONAL DE CIENCIAS Y TECNOLOGIA

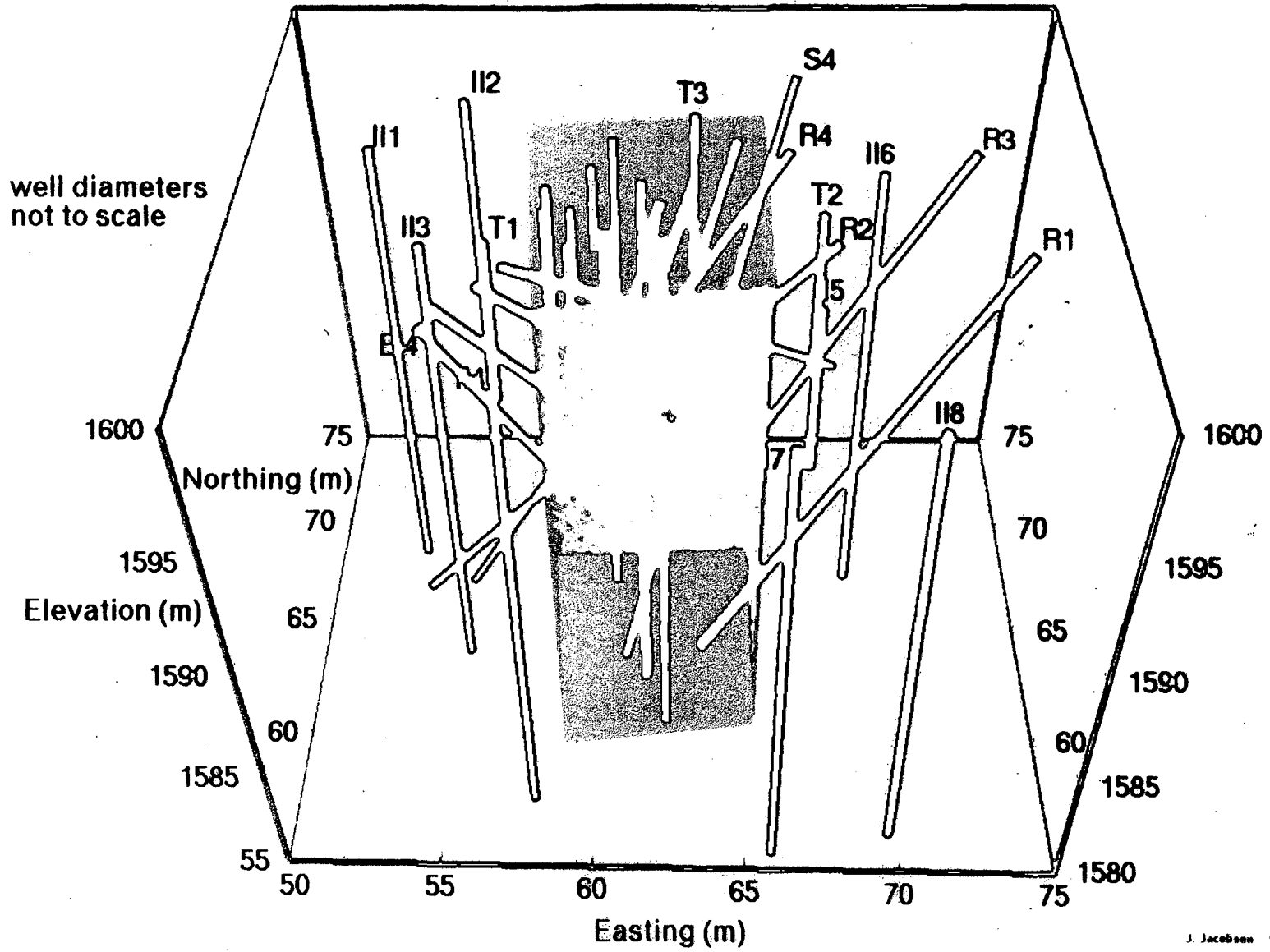
## Binary connectivity map of the fractures exposed below the investigation site at Box Canyon

Red shading → Interpreted flow pathways from surface given simple percolation  
Blue shading → field evidence of past fluid flow egress from canyon wall

▷ 3.0 m. ▷



# Perspective View of Well Locations - Box Canyon, Idaho

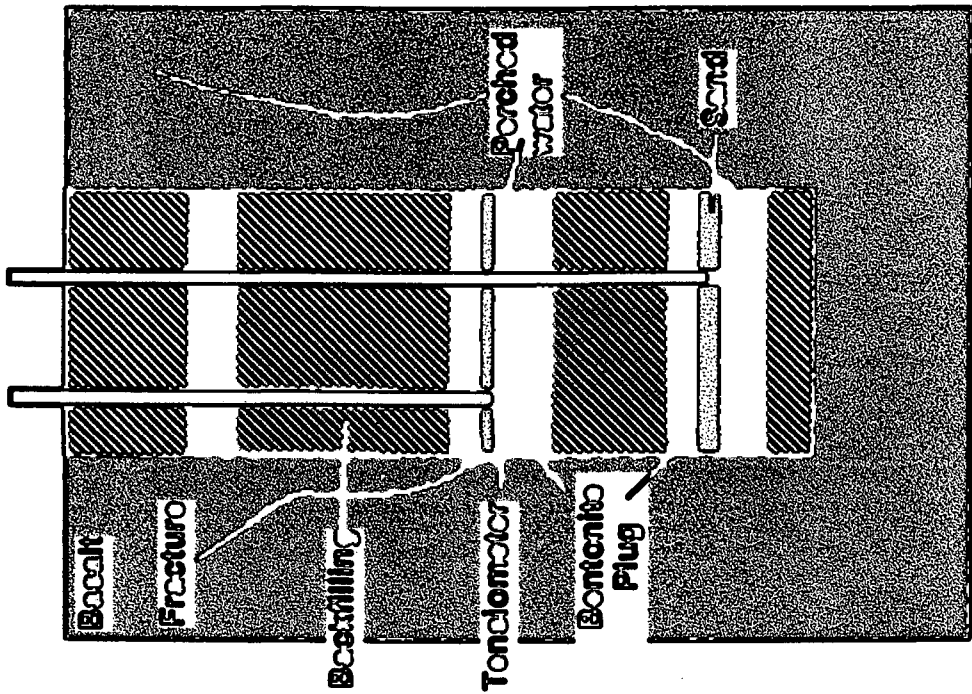


# Single- and Cross-Borehole Monitoring Technology for Fractured Rocks

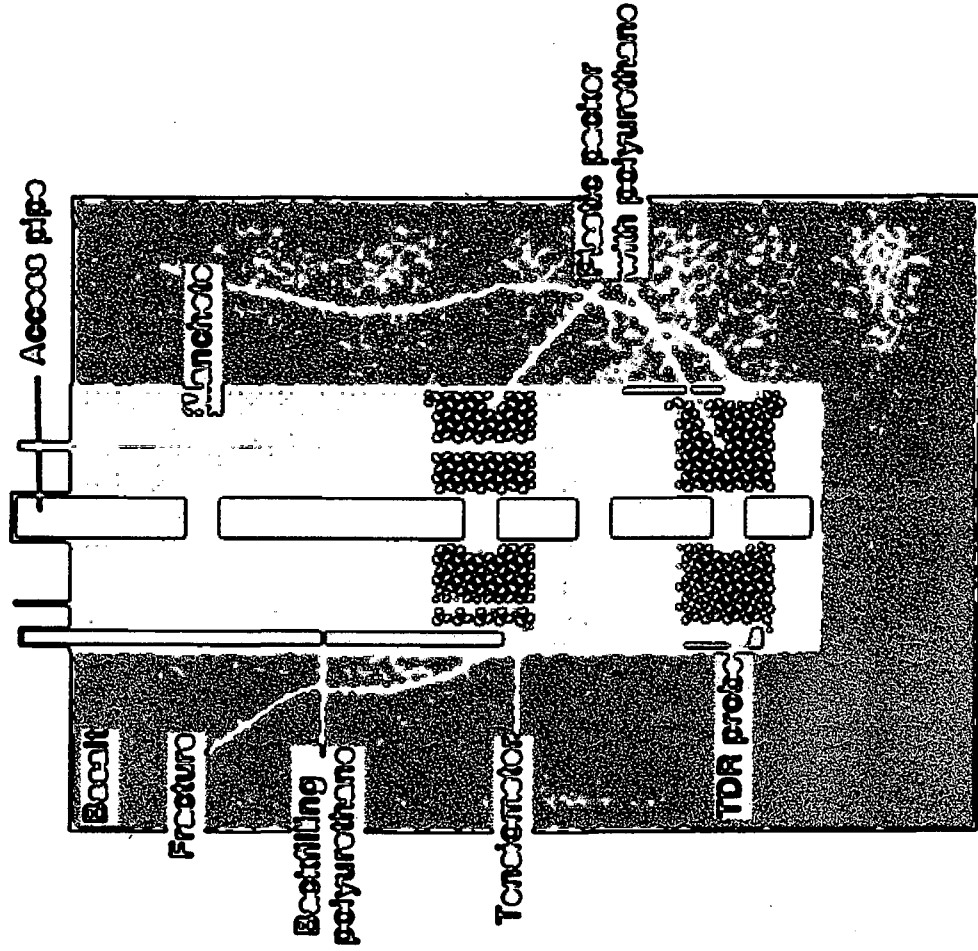
- Slanted wells (to intersect vertical fractures)
- Borehole completion using polyurethane foam
- “Single-type” probes - tensiometers, suction lysimeters, time domain reflectometry, TDR, thermistors, miniature electrical resistivity, and ER, and
- Cross-hole measurements - GPR, and ERT

# Installation Technology

Conventional

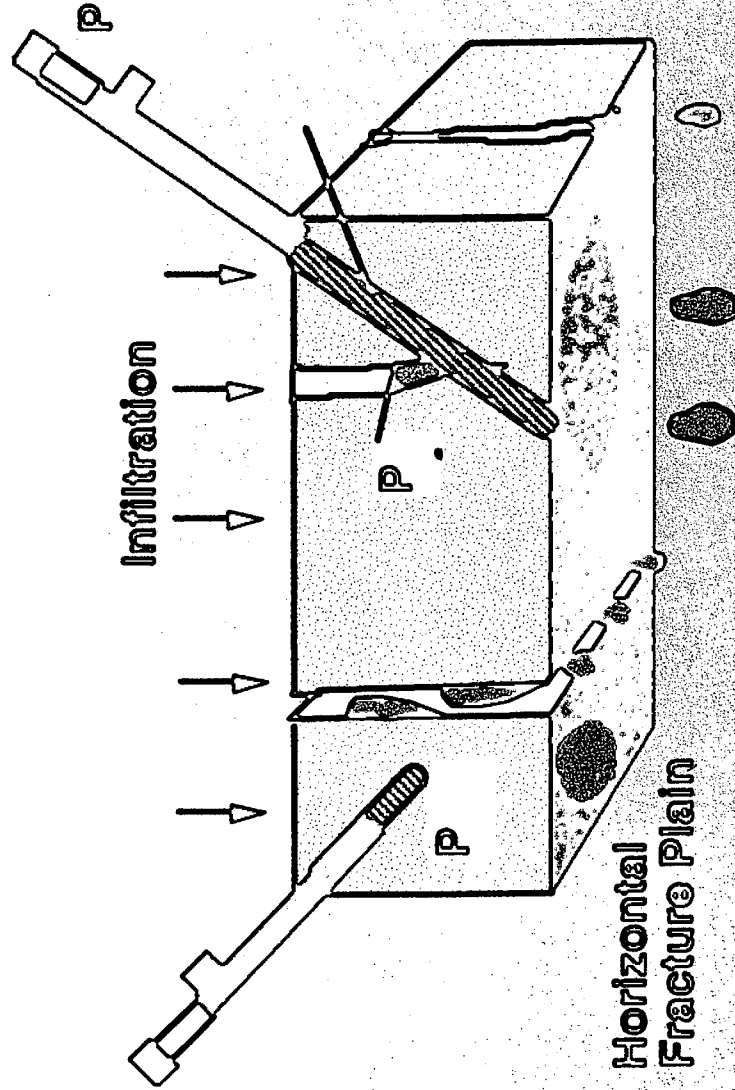


New



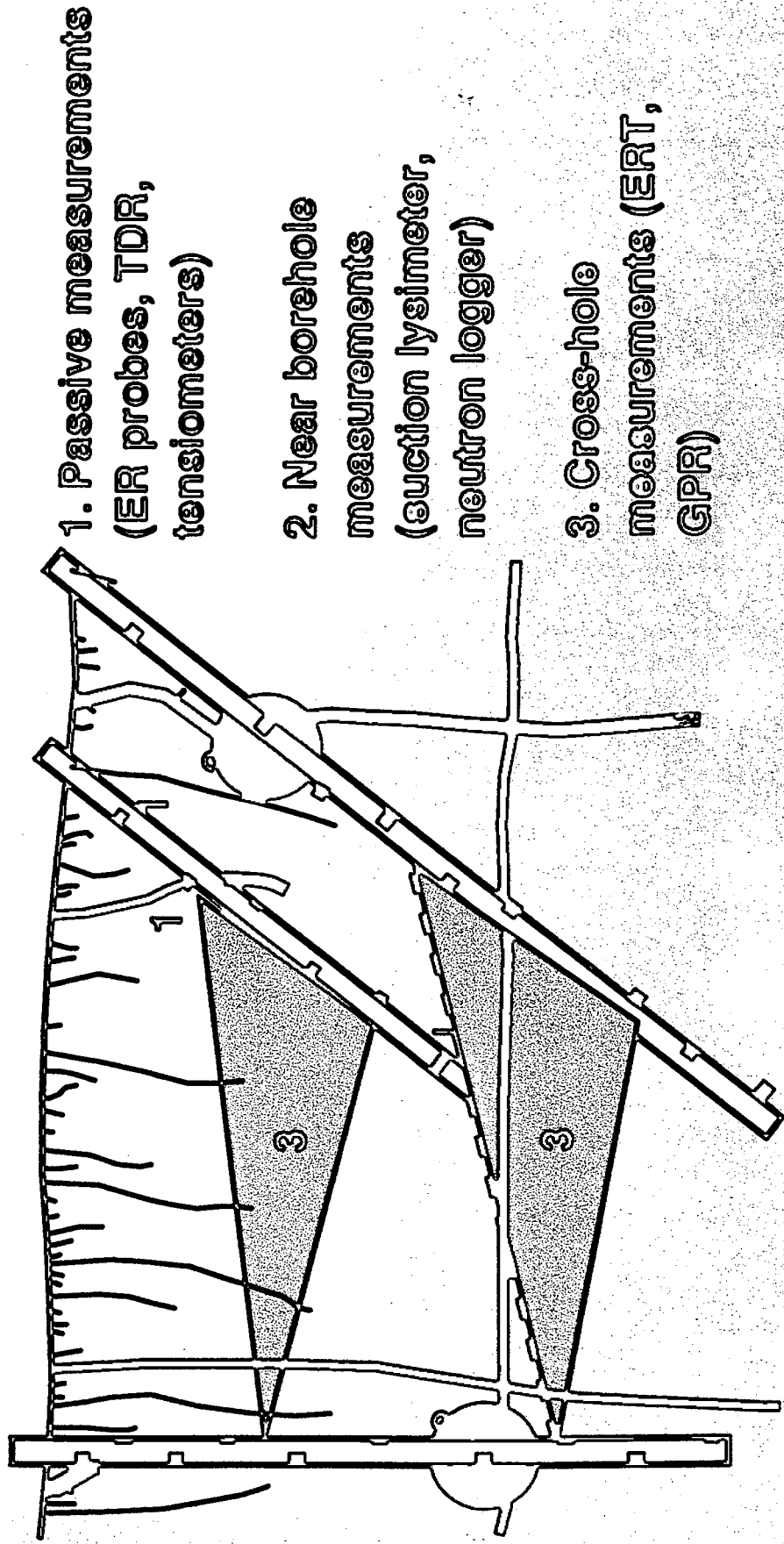


# Conceptual Model of Tensiometry Measurements

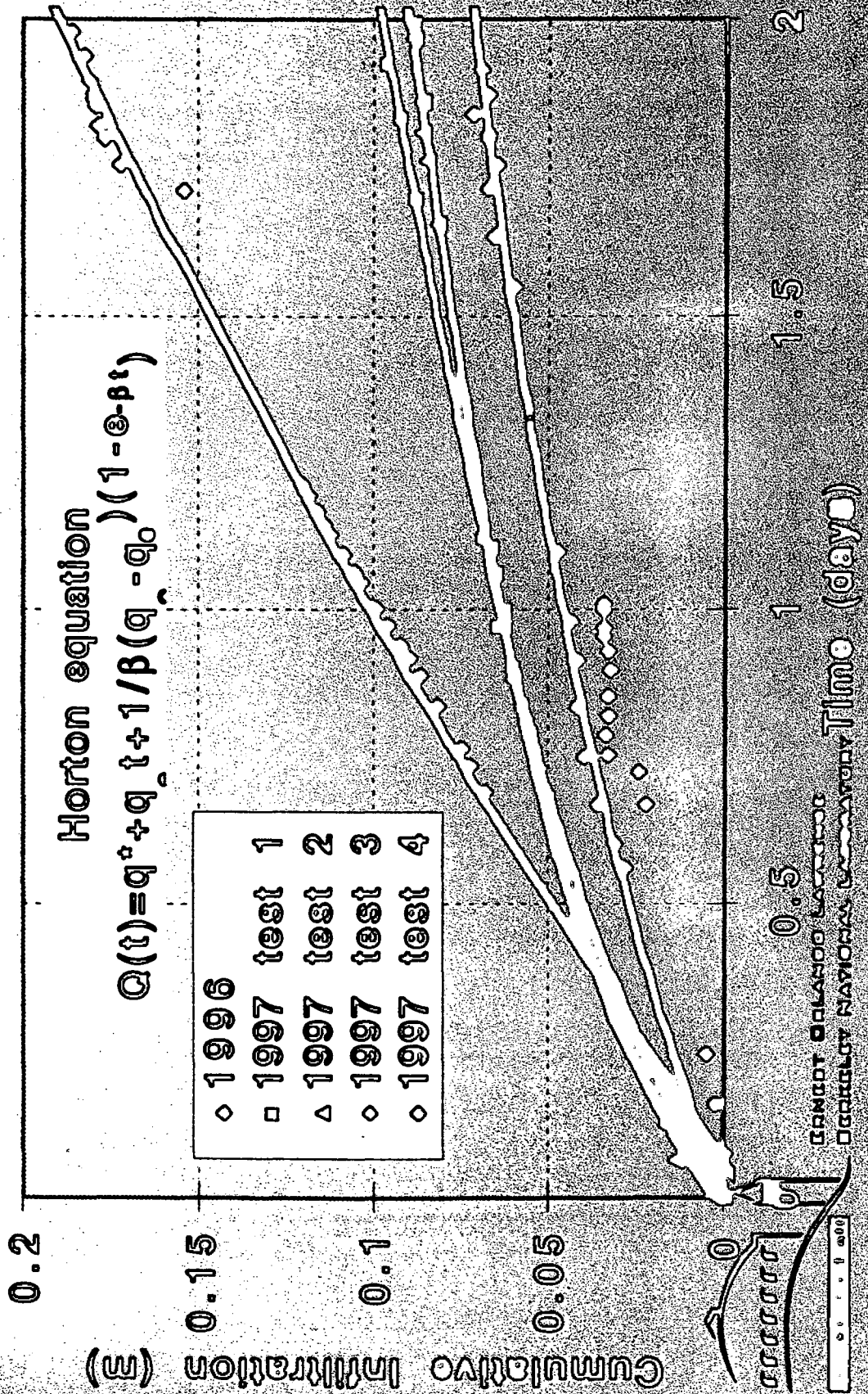


$$P = \alpha(t)P_{mx} + \beta(t)P_{fr} + \gamma(t)P_a$$

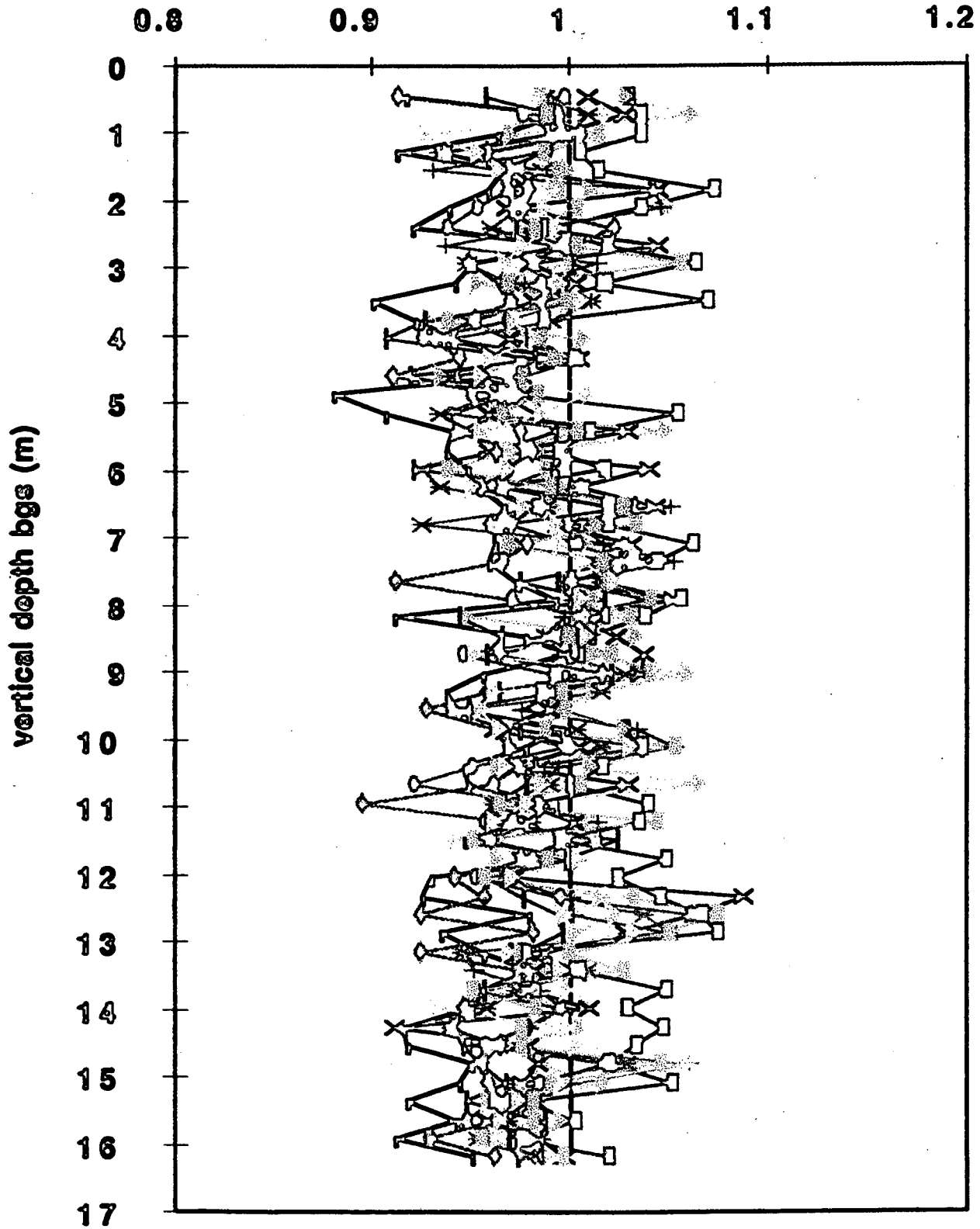
# Scheme of Zones of Influence of Sensors in Fractured Rocks



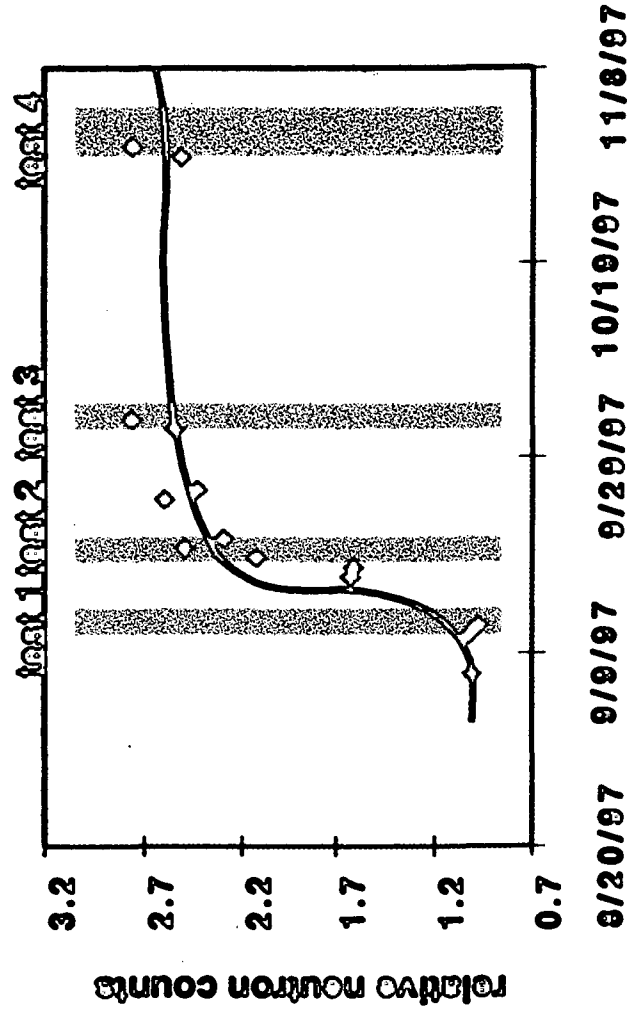
# Cumulative Infiltration Box Canyon Pulsed Infiltration Tests



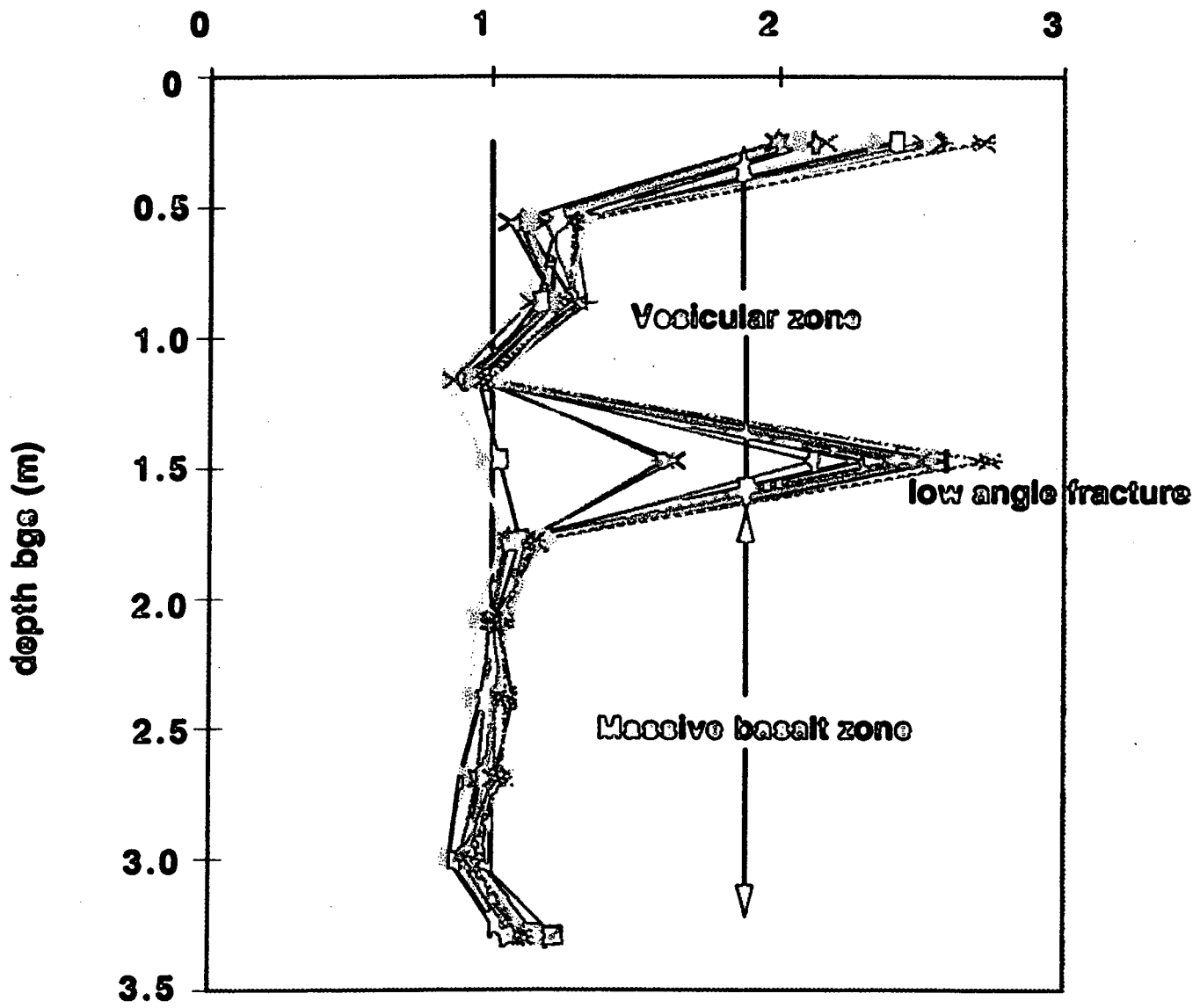
**Relative neutron counts in well R1 before, during,  
and after each pulsed infiltration test**



Time trend of neutron counts for  
well T10 (1.5 m bgs)



**Relative neutron counts in well  
T10 (note change in axis)**



# Moisture content

(based on neutron logging)

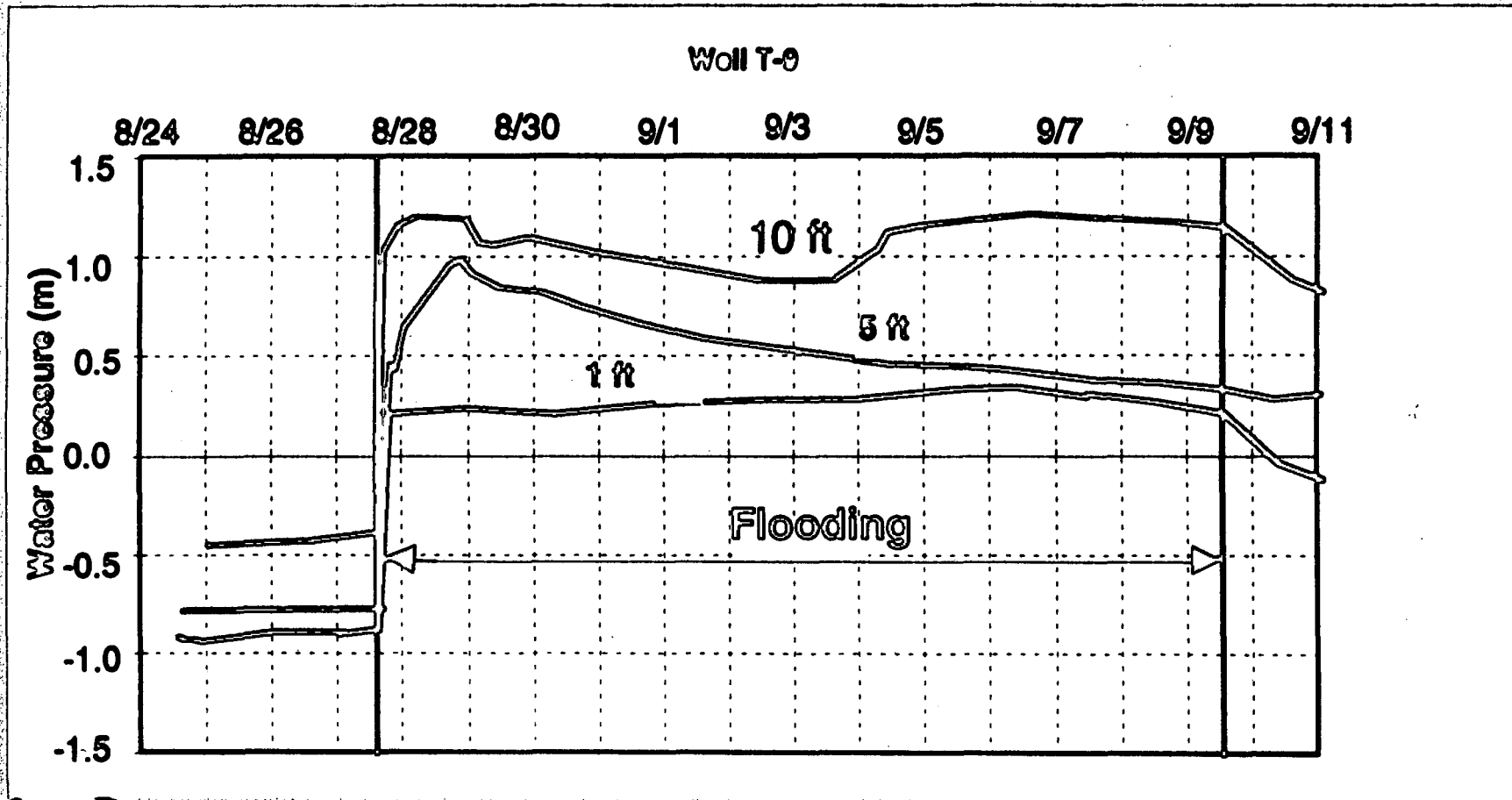
- The same lithological units were affected in 1996 and 1997
- The rocks are much more saturated in 1997 than in 1996
- NO changes in the slanted holes during the 1997 tests
- Changes from the surface to 1.5 m within the pond in 1997

# Results of Measurements of Water Pressure

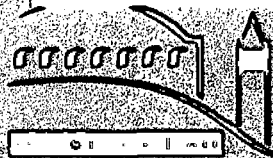
- Fast response
- Preferential and bypass flow
- Fracture-matrix interaction



# Changes of Water Pressure during the 1996 Infiltration Test



36

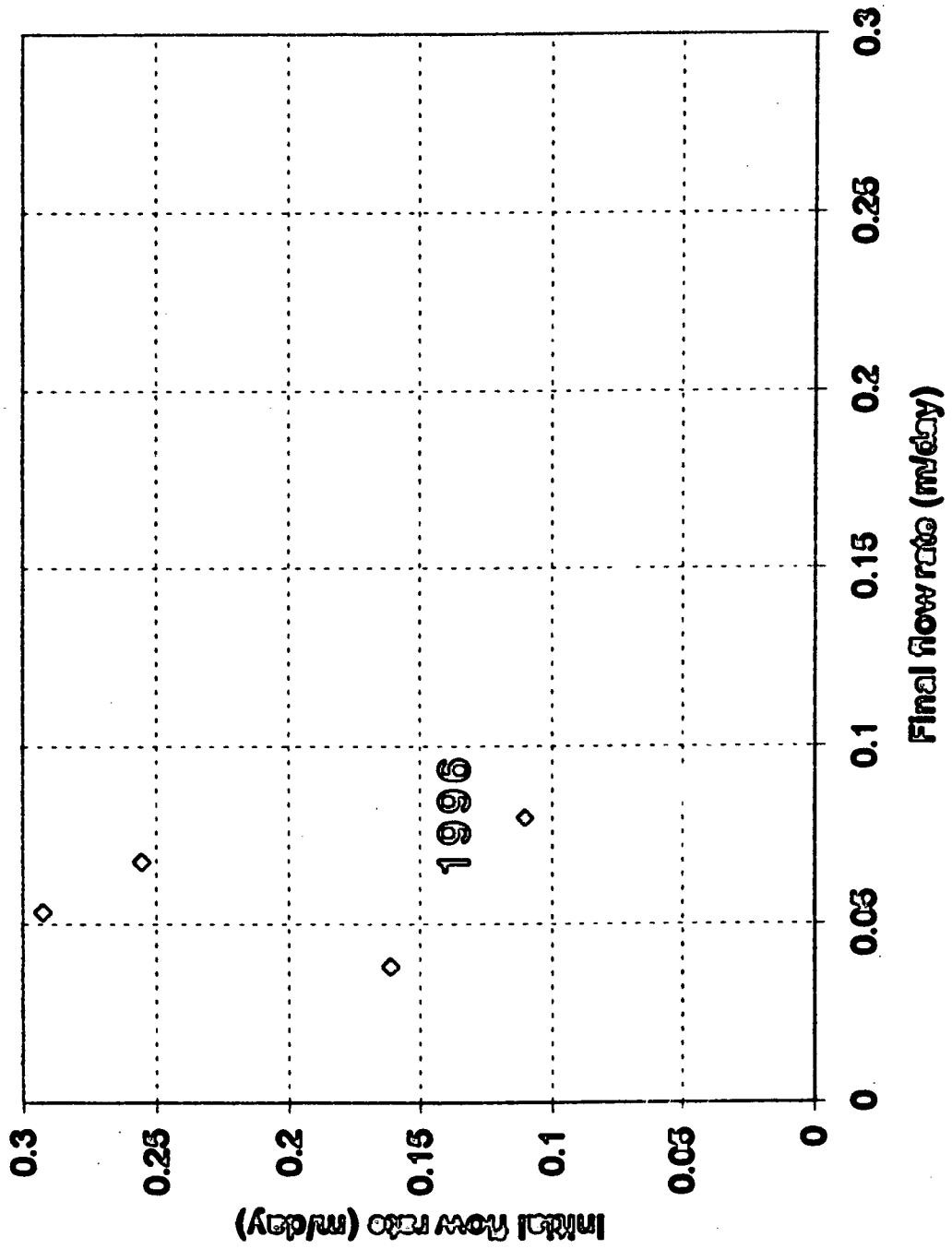


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# What Does a Tensiometer Measure in Fractured Rocks?

- The gauge pressure is primarily affected by the conducting component that transmits water into or out of the ceramic cup of the tensiometer:
  - During drying - by matrix pressure, and
  - During wetting - by the fracture pressure.

**Initial flow rate vs. Final flow rate for pulsed infiltration tests  
(1997) and continuous infiltration test (1996)**



# Types of Tests

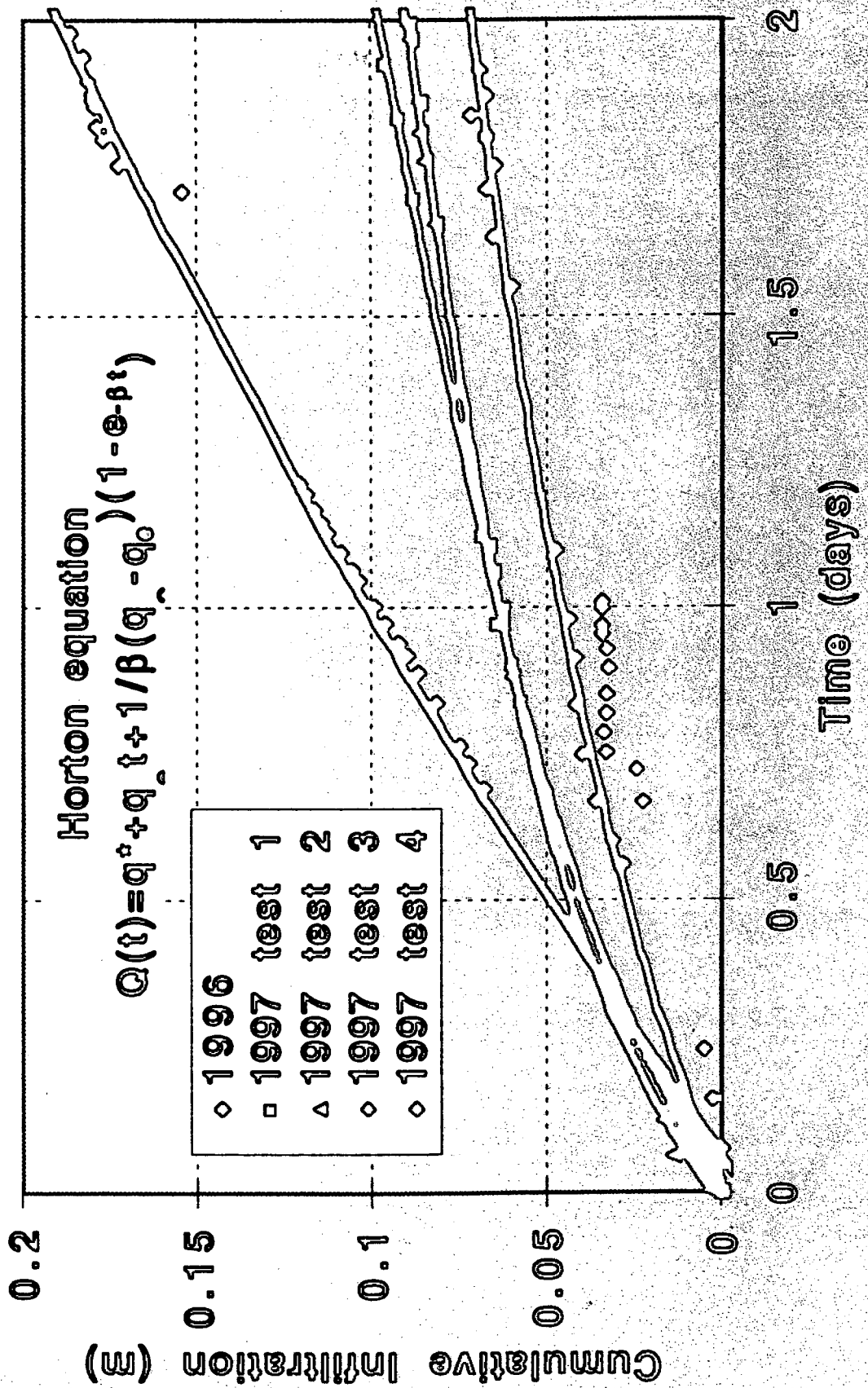
- 1996 - 2-week continuous ponding including a 2-day pulse of 3 g/l KBr
- 
- 1997 - Four 2-day pulses of ponding with 3 g/l of KBr

		August																																	
		1	2	3	4	5	6	7	0	0	10	11	12	13	14	15	16	17	10	10	20	21	22	23	24	20	20	27	20	20	30	31			
date																																			
function																																			
location	BY																																		
MT																																			
G																																			
WA																																			
CA																																			
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community																																			
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CL																																			
		September																																	
		1	2	3	4	5	6	7	0	0	10	11	12	13	14	15	16	17	10	10	20	21	22	23	24	20	20	27	20	20	30	30			
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		1	2	3	4	0	0	7	0	0	10	11	12	13	14	15	16	17	10	10	20	21	22	23	24	20	20	27	20	20	30	31			
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CA																																			
GA																																			
community																																			
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test	start of bonding	end of bonding	Volume of H <sub>2</sub> O infiltrated (m <sup>3</sup> )	mass of soil infiltrated (kg)
test 4	10/30/87 13:21	11/3/87 12:00	0.20	50.37
test 3	10/5/87 12:40	10/4/87 10:00	3.01	11.23
test 5	01/8/87 14:20	01/50/87 10:40	2.01	12.03
test 1	01/11/87 15:12	01/13/87 15:42	2.45	10.50
test 7	-	-	51.13	03.30
test 8	01/51/80 15:57	01/01/80 11:00	52.00	38.04

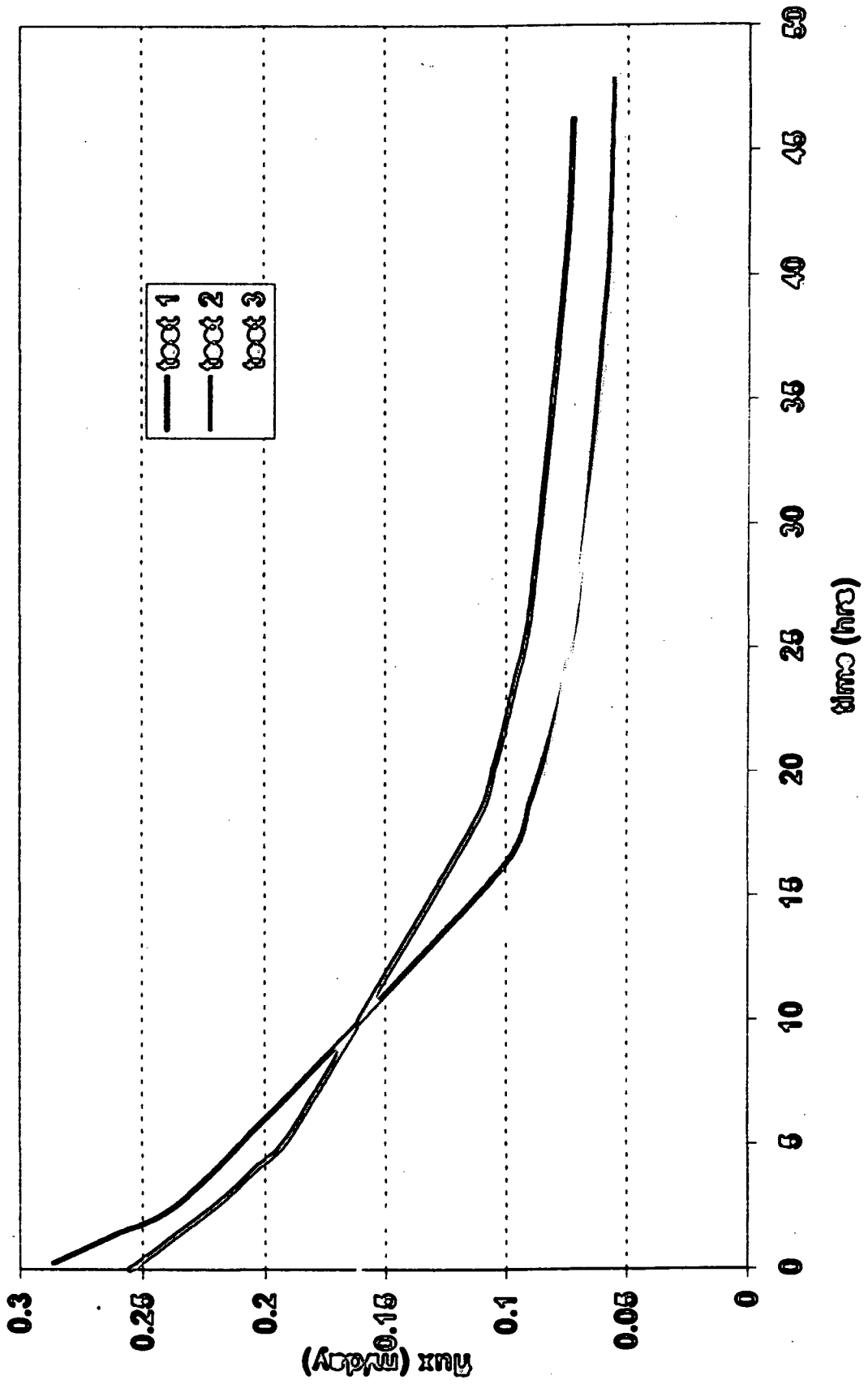


# Cumulative Infiltration Box Canyon Pulsed Infiltration Tests





Instantaneous flux for pulsed infiltration tests calculated from parameters using Horton's equation



# Flow rate

- Exponential temporal decrease in the flow rate in all tests
- Significant variation of the flow rate at the beginning of infiltration, and then convergence to a narrow range

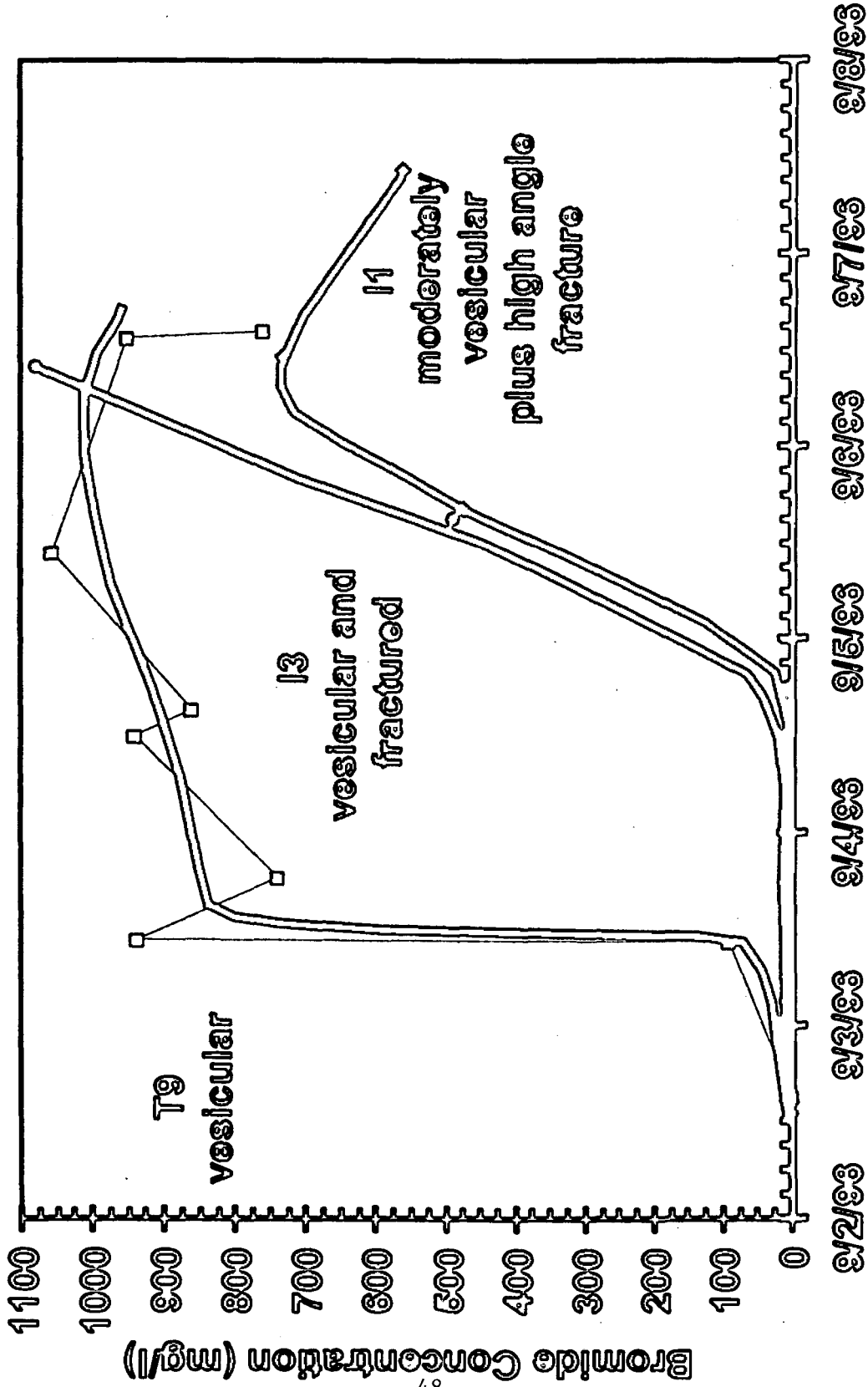
# Miniature ER probes

- Background Conditions:
  - Lower resistivity in fracture zones and rubble zones
  - Higher resistivity in dense basalt zones
- Infiltration Tests:
  - Decrease in resistivity as affected by the tracer movement in hydraulically conductive zones:
    - Central fractured zone
    - Rubble zone
    - Some single fractures
  - No changes in dense basalt

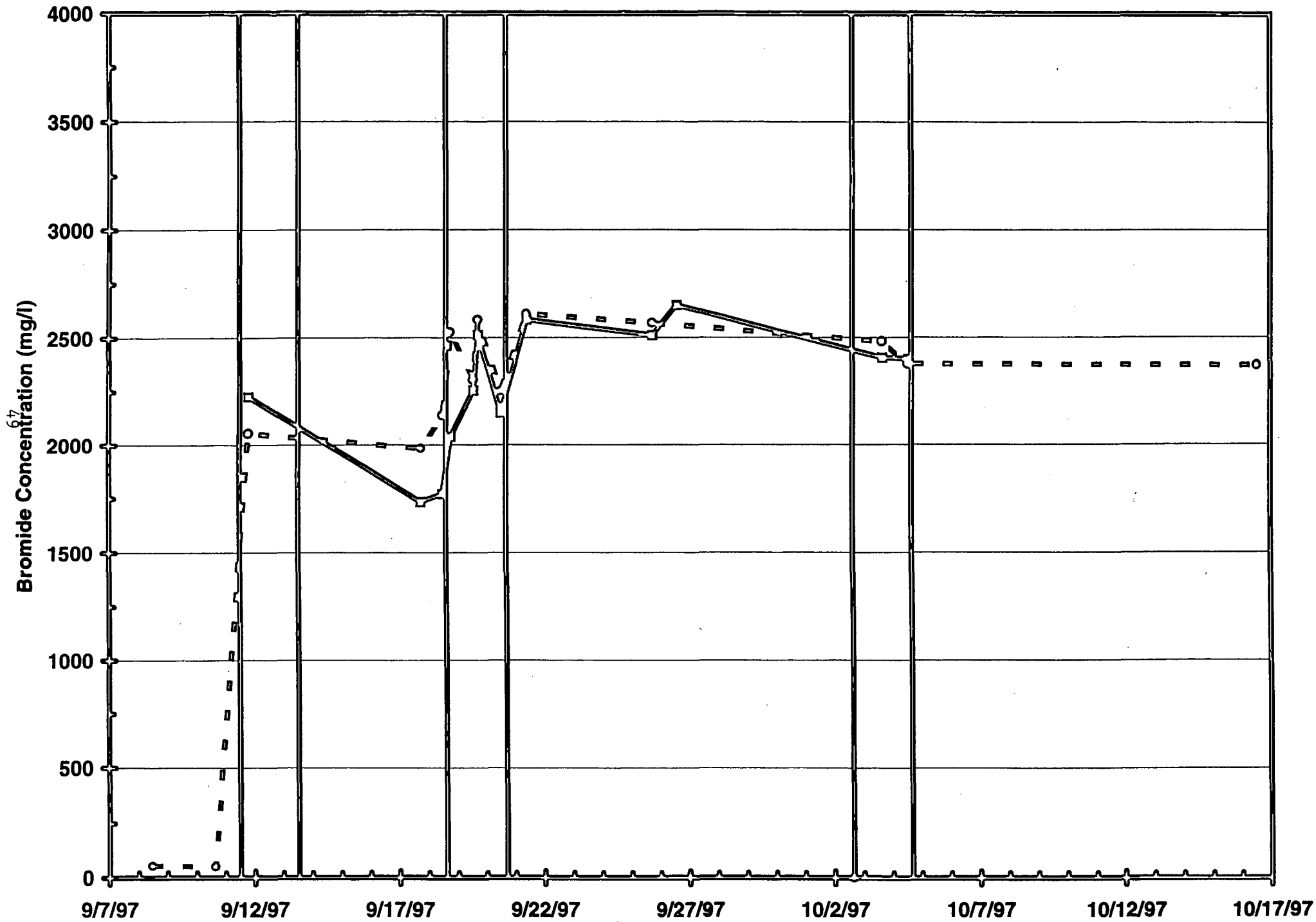
# Breakthrough Curves

- Multi-modal curves associated with transport through different sets of fractures
- Advective transport is a main process of chemical transport

Bromide tracer breakthrough, Depth 0.3 m. 1996 Infiltration Test at Box Canyon, Idaho. All three wells are located within the infiltration pond.



Well T9 - Depins of 0.3 m (dashed line) and 1.5 m (solid line)



Well T7 - Depths of 0.6 m (2 ft) (dashed line) and 1.8 m (6 ft) (solid line)

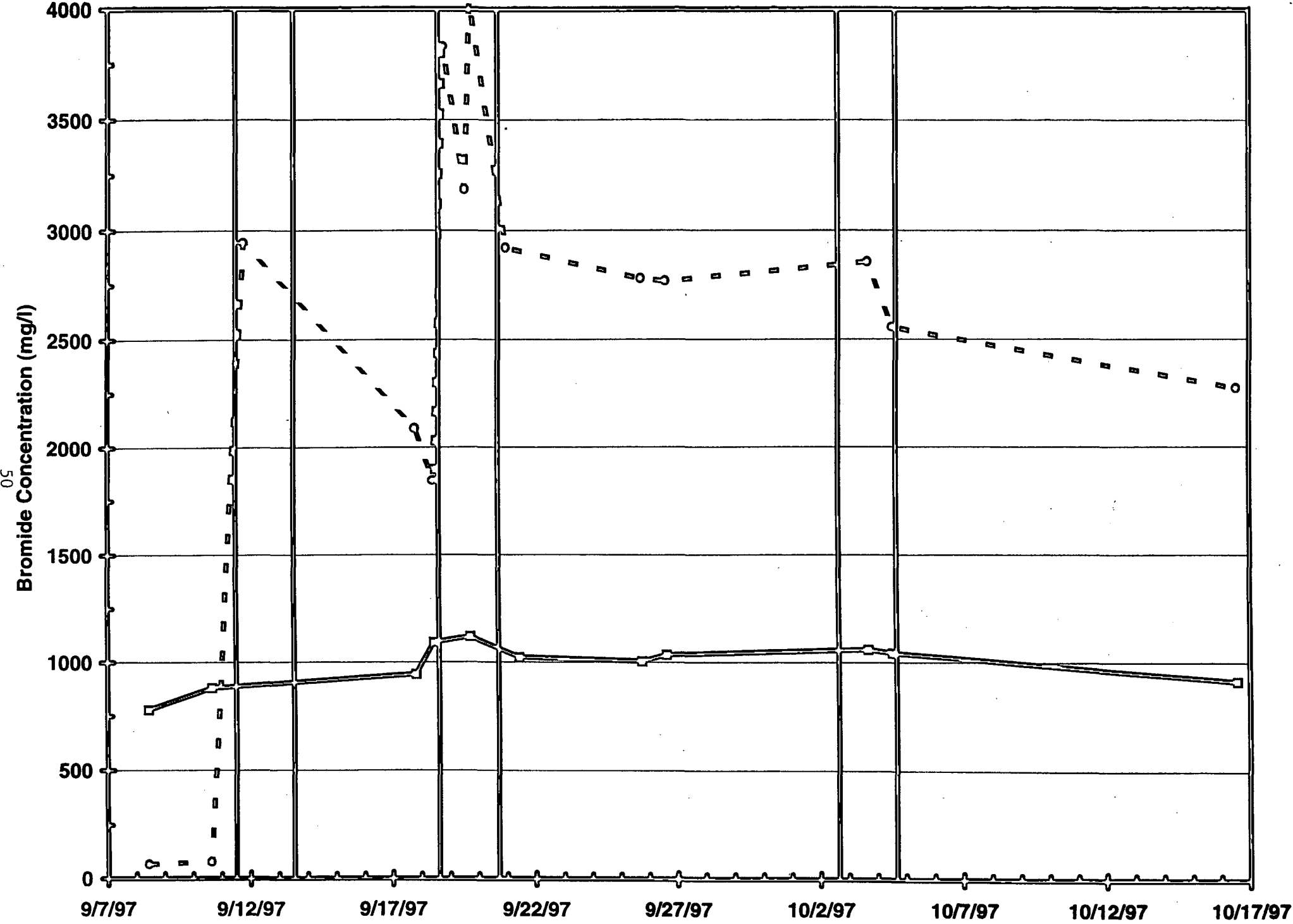
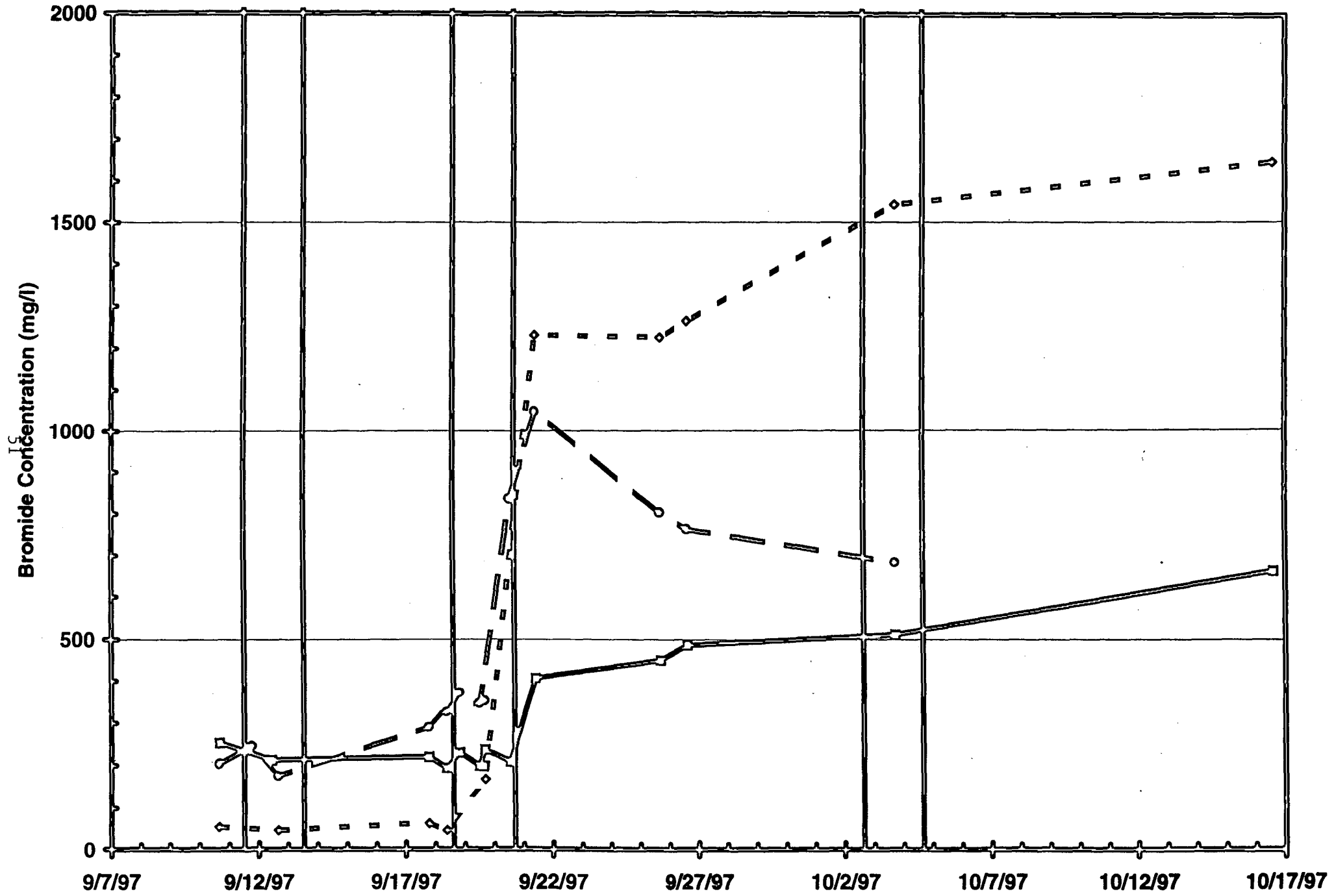
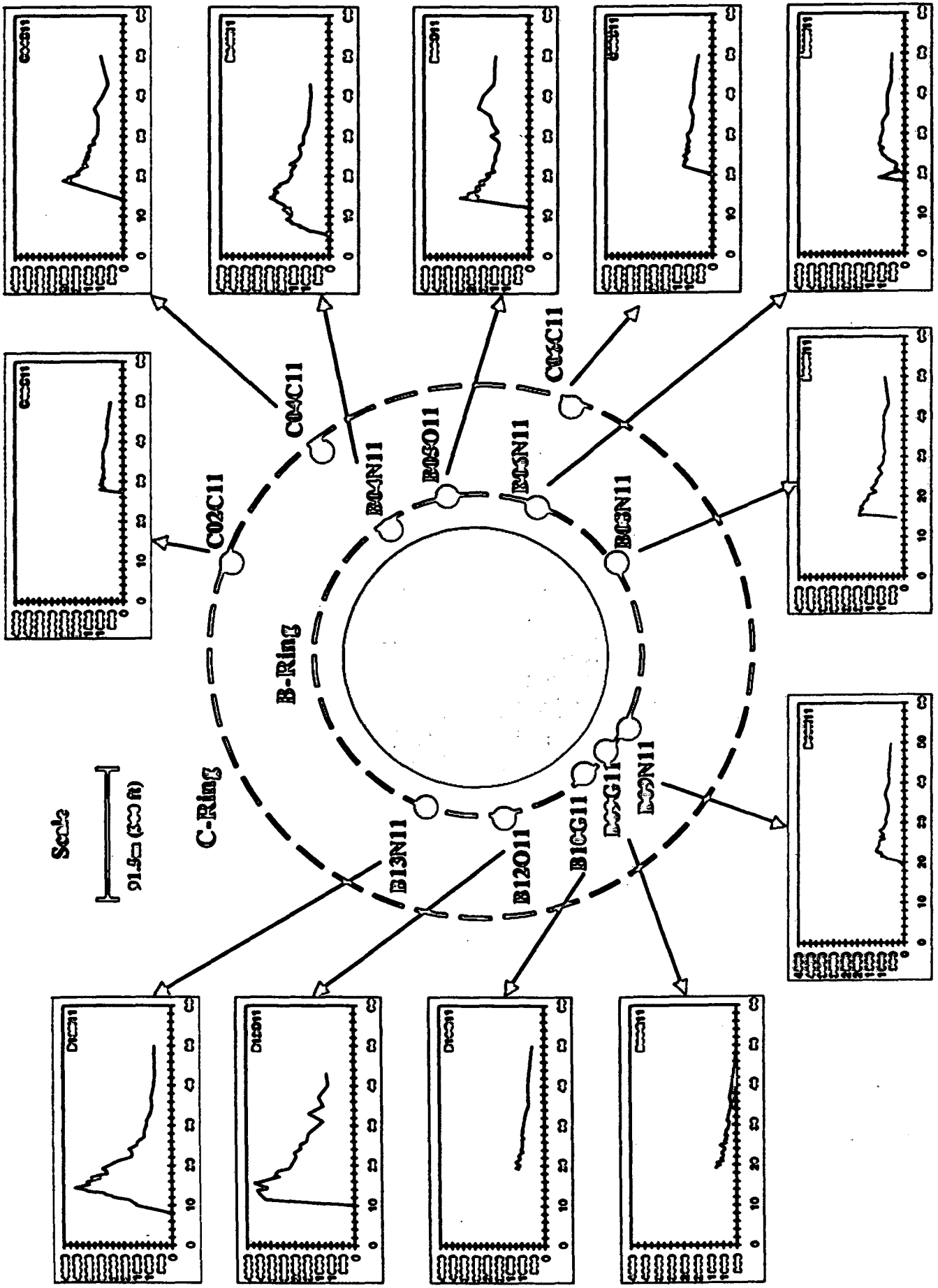


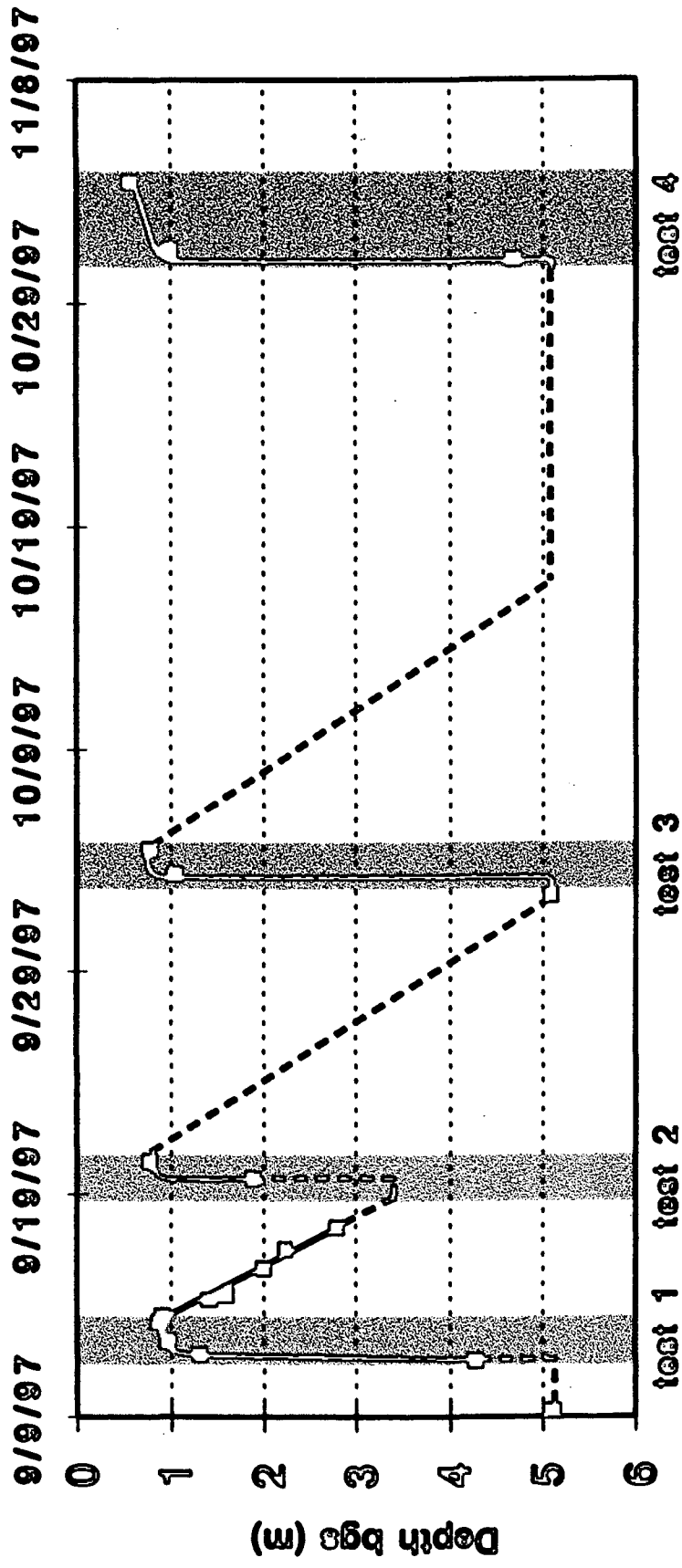
Figure 4 - Depths of 0.6 m (dotted line), 4.3 m (dashed line), and 5.8 m (solid line). Note change in vertical scale.





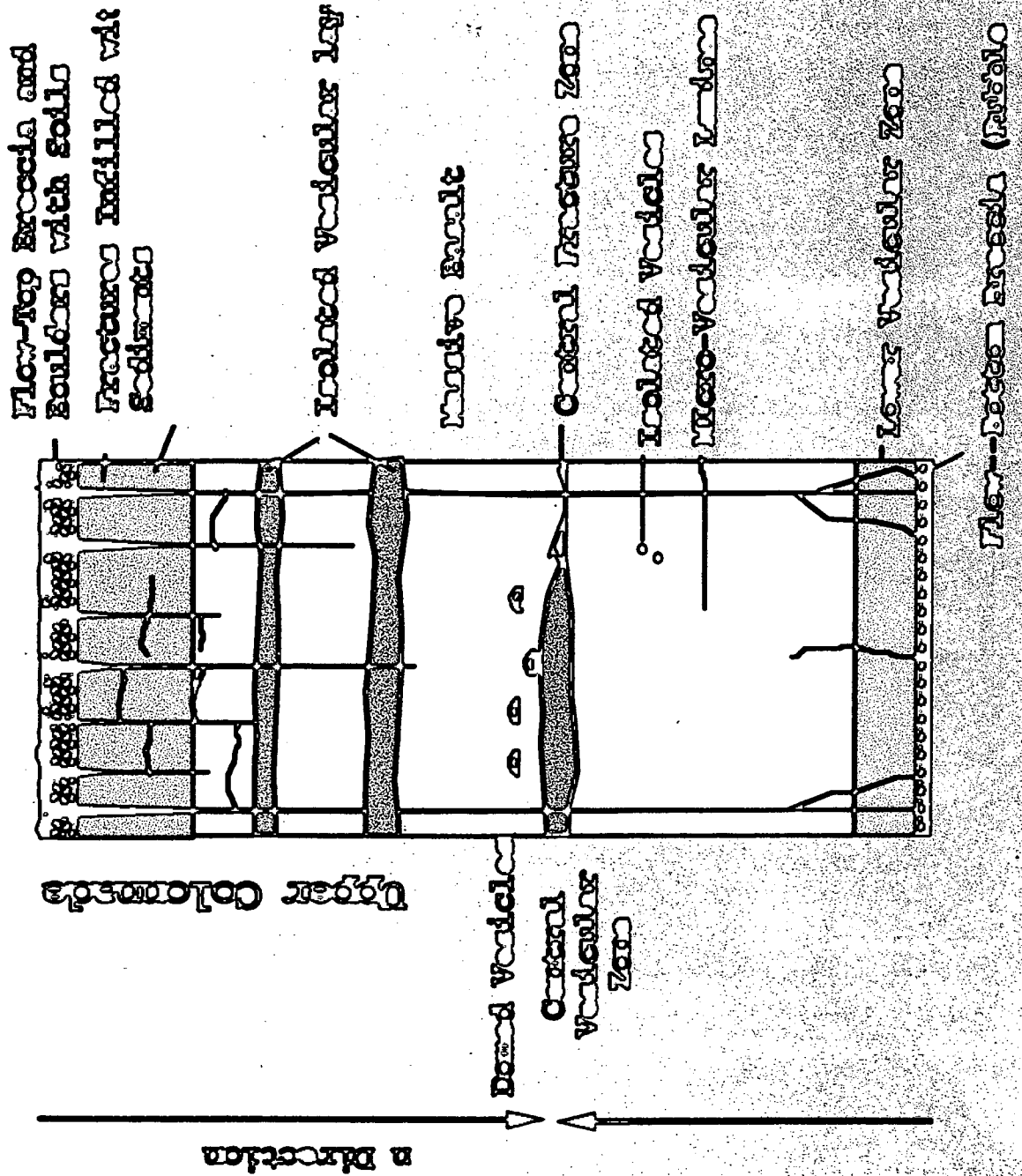


Water level in well I-5 during pulsed infiltration tests



# Geological Components of

## Fractured Basalt



## Fractured Basalt:

- is highly heterogeneous with localized and fast flow paths.
- has non-conductive fractures and matrix where contaminants are accumulated.

# Numerical Models

- TOUGH2
- PathFinder
- Chaotic Model

# IMPROVED CONCEPTUAL MODEL OF WATER FLOW IN FRACTURED BASALT

- Transient unsaturated-saturated conditions
- Variable temporal and spatial permeability of soils and rocks
- Preferential flow:
  - vertical flow along column bounding fractures
  - lateral flow in the central fractured zone and rubble zone
- Rapid redistribution of water in fractures
- Sorption of water by matrix
- Entrapped air
- Small changes in initial and boundary conditions may lead to significant changes in water pressure, saturation, permeability

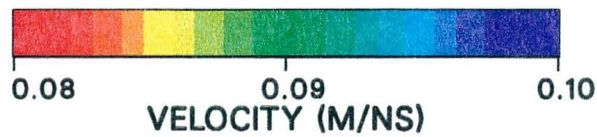
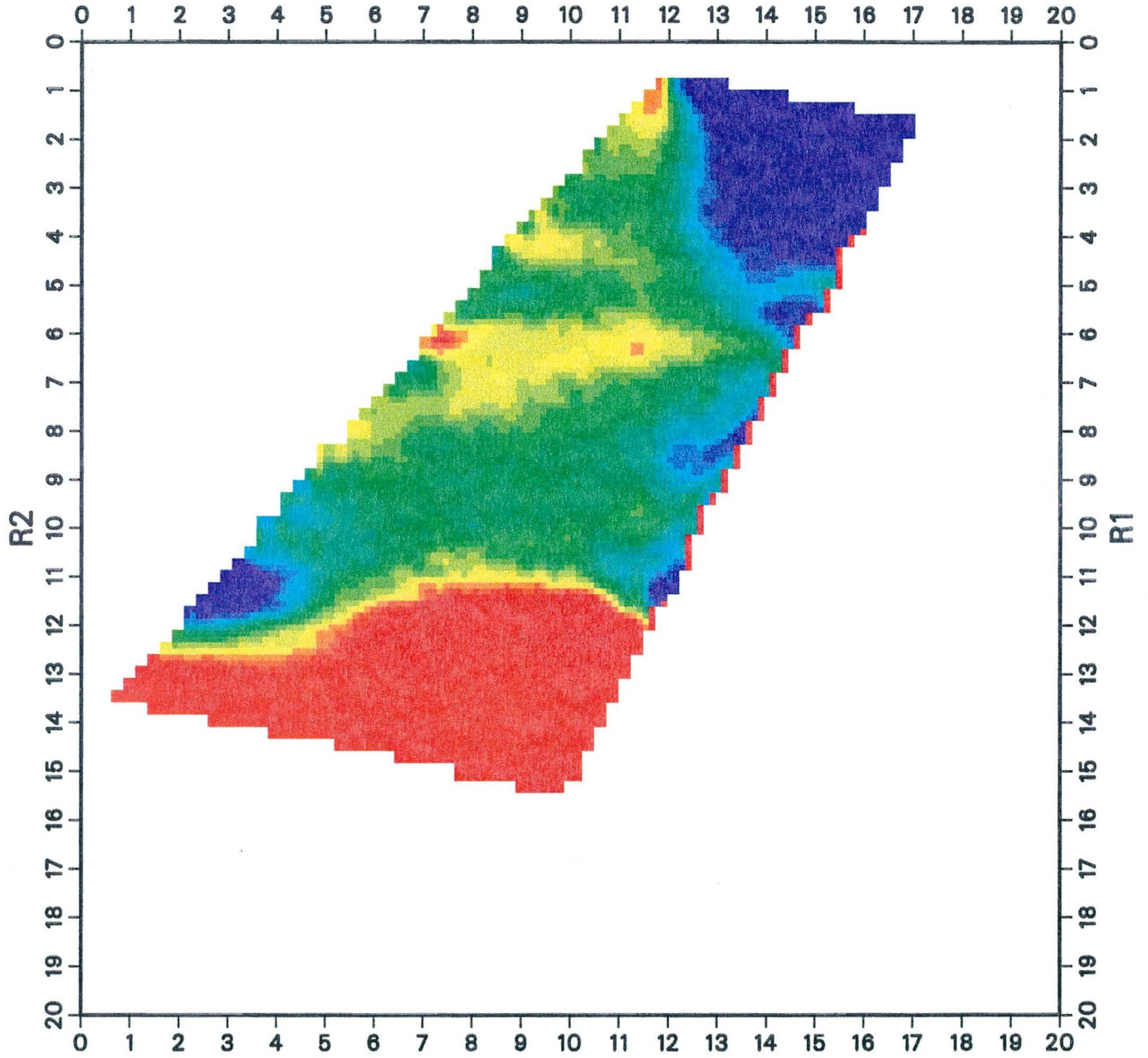
## II.2

# Radar Results at Box Canyon

**John Peterson**

# BOX CANYON R2-R1 PULSE1 TEST

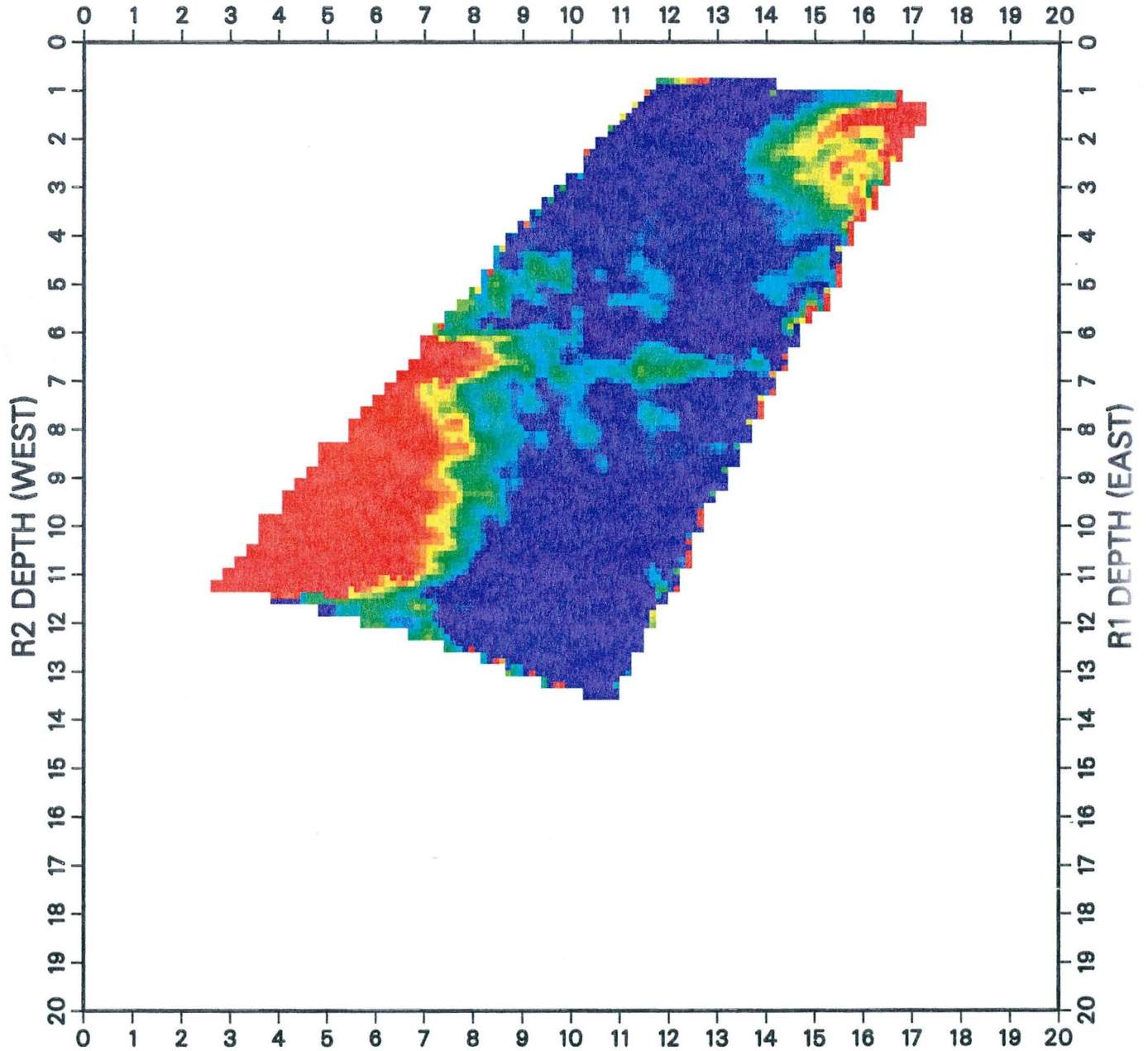
PRE 9/8/97





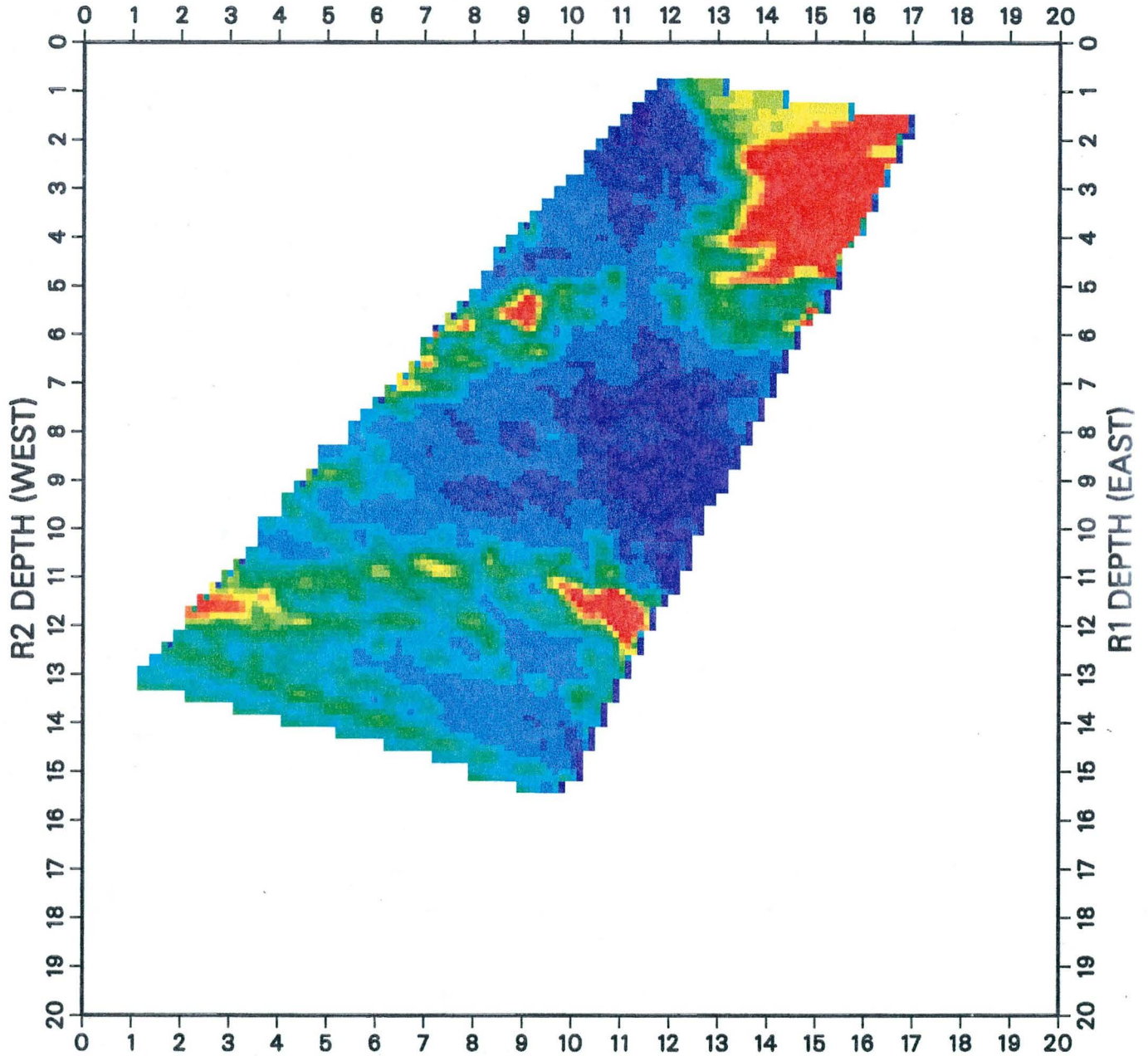
# BOX CANYON R2-R1 PULSE2 TEST

97 - 96 9/18/97 - 7/24/96



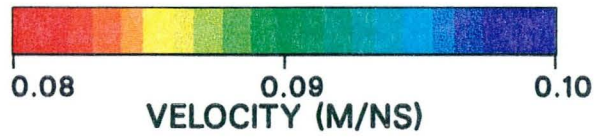
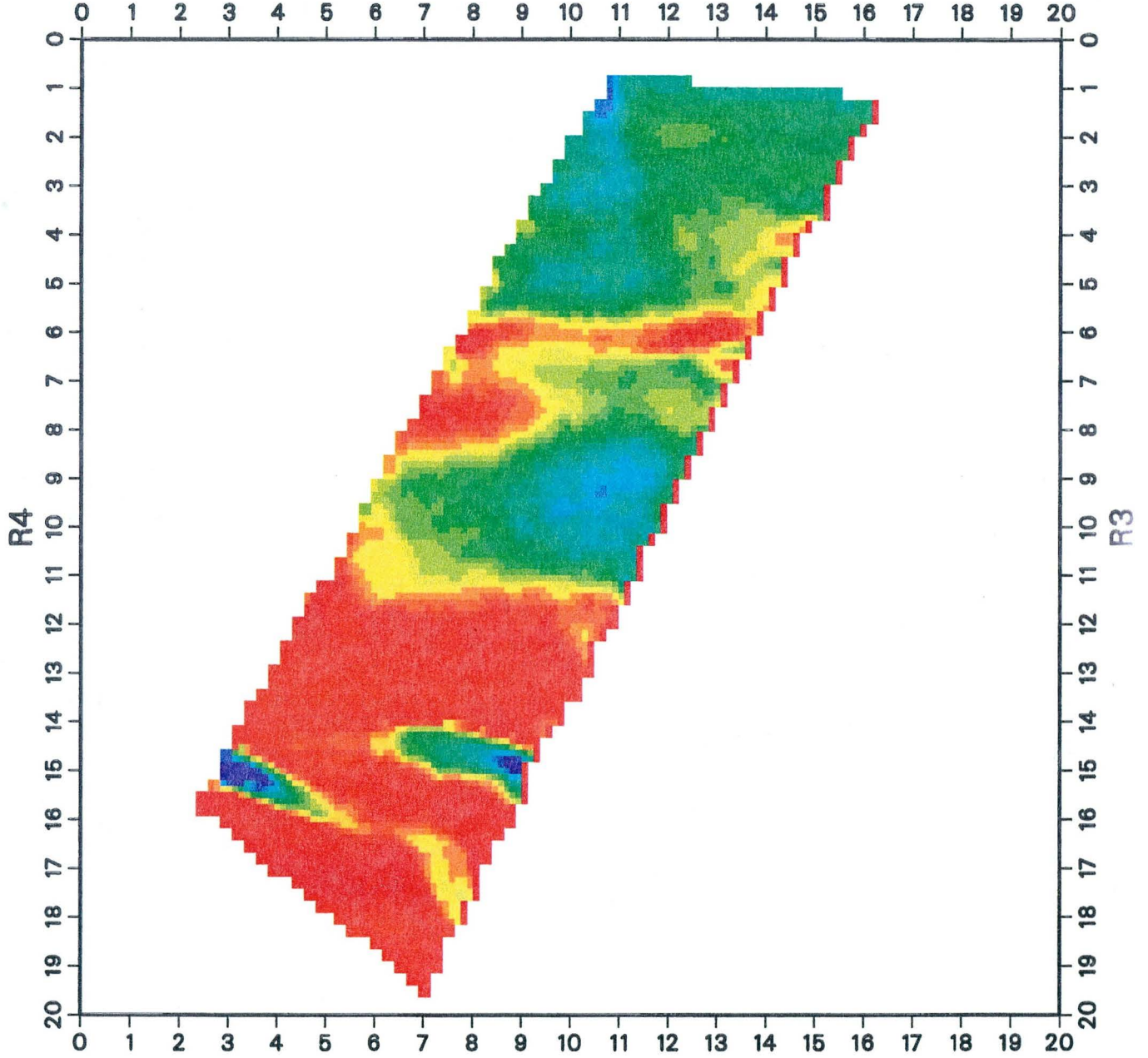
# BOX CANYON R2-R1 PULSE1 TEST

DURING-PRE 9/12/97 - 9/8/97



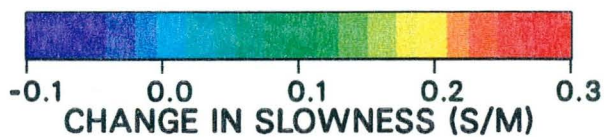
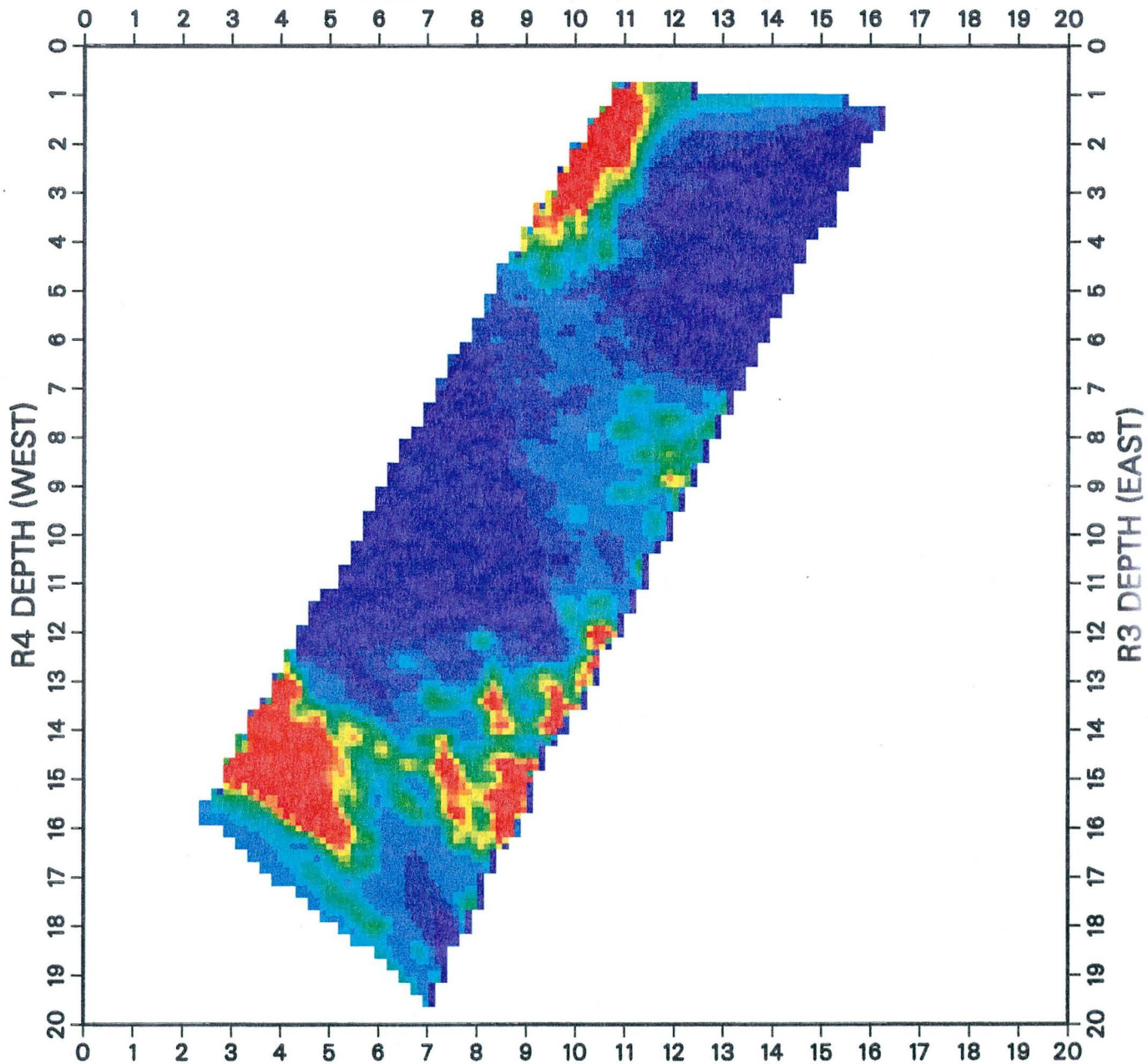
# BOX CANYON R4-R3 PRE PULSE1 TEST

9/10/97



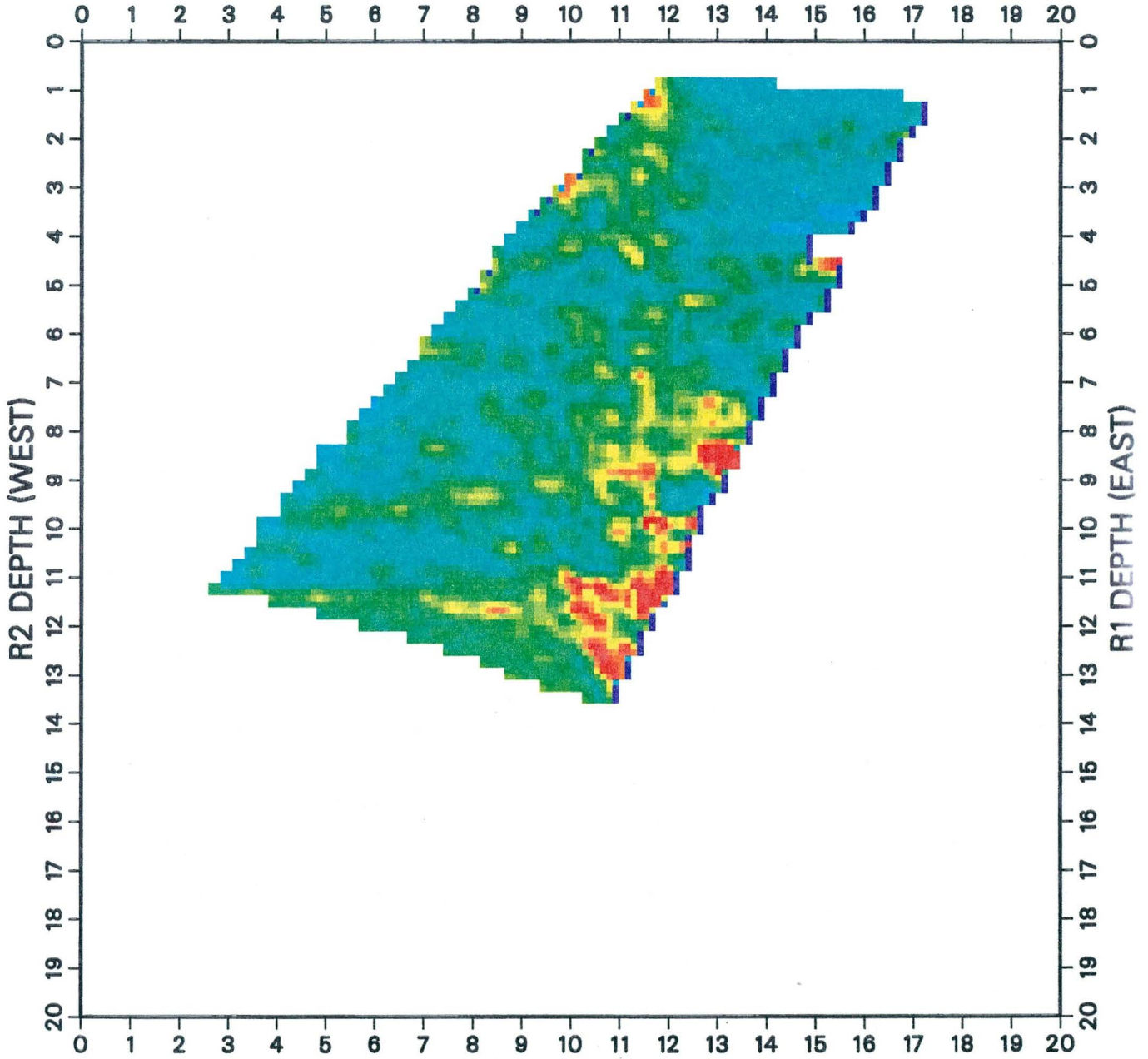
# BOX CANYON R4-R3 DURING-PRE

PULSE1 TEST 9/13/97 - 9/10/97



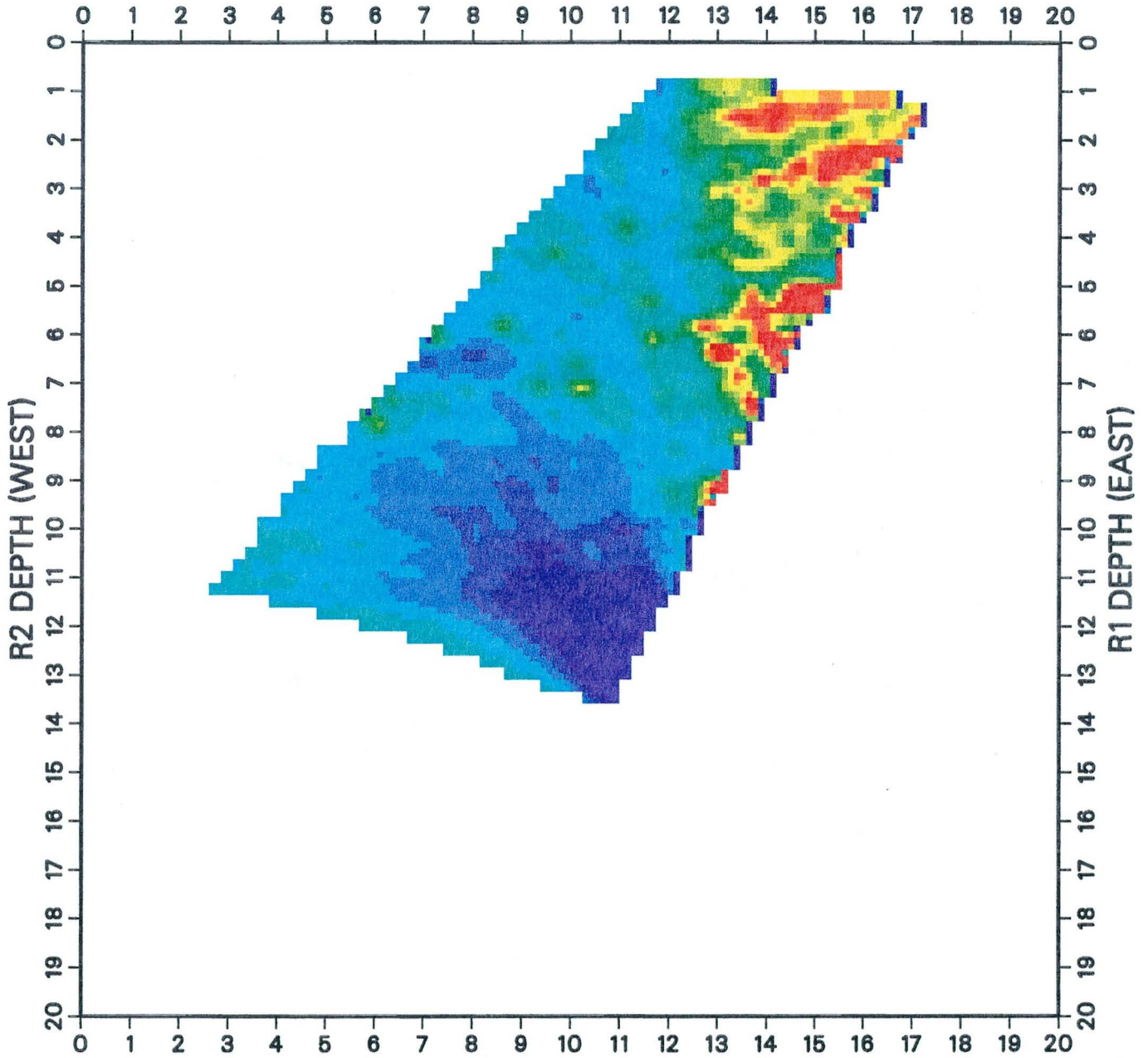
# BOX CANYON R2-R1 PULSE2 TEST

3 - 1 9/20/97 - 9/18/97



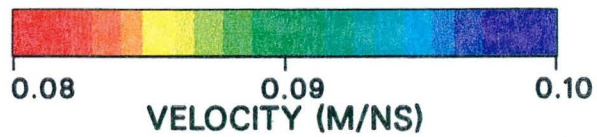
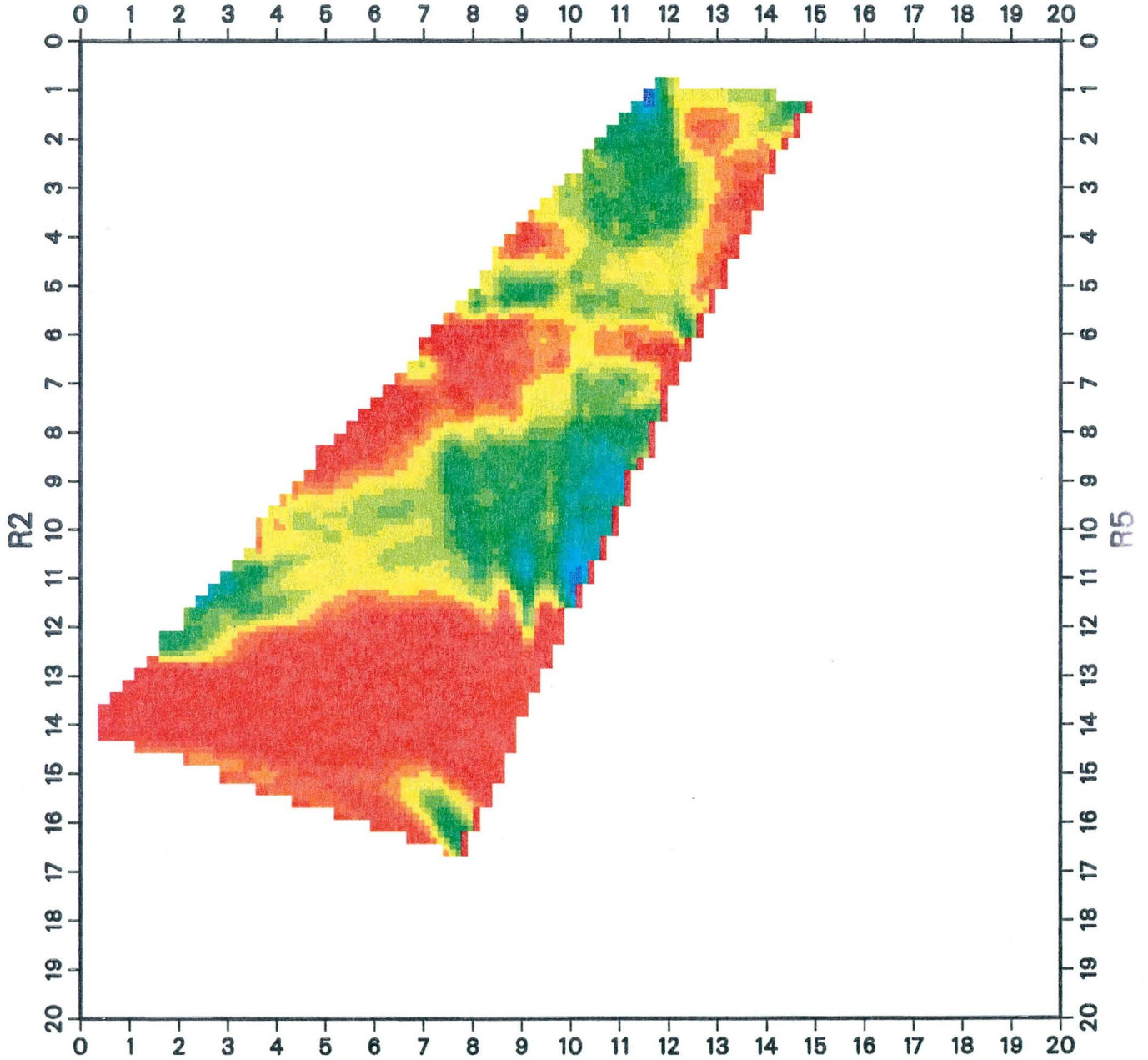
# BOX CANYON R2-R1 PULSE2 TEST

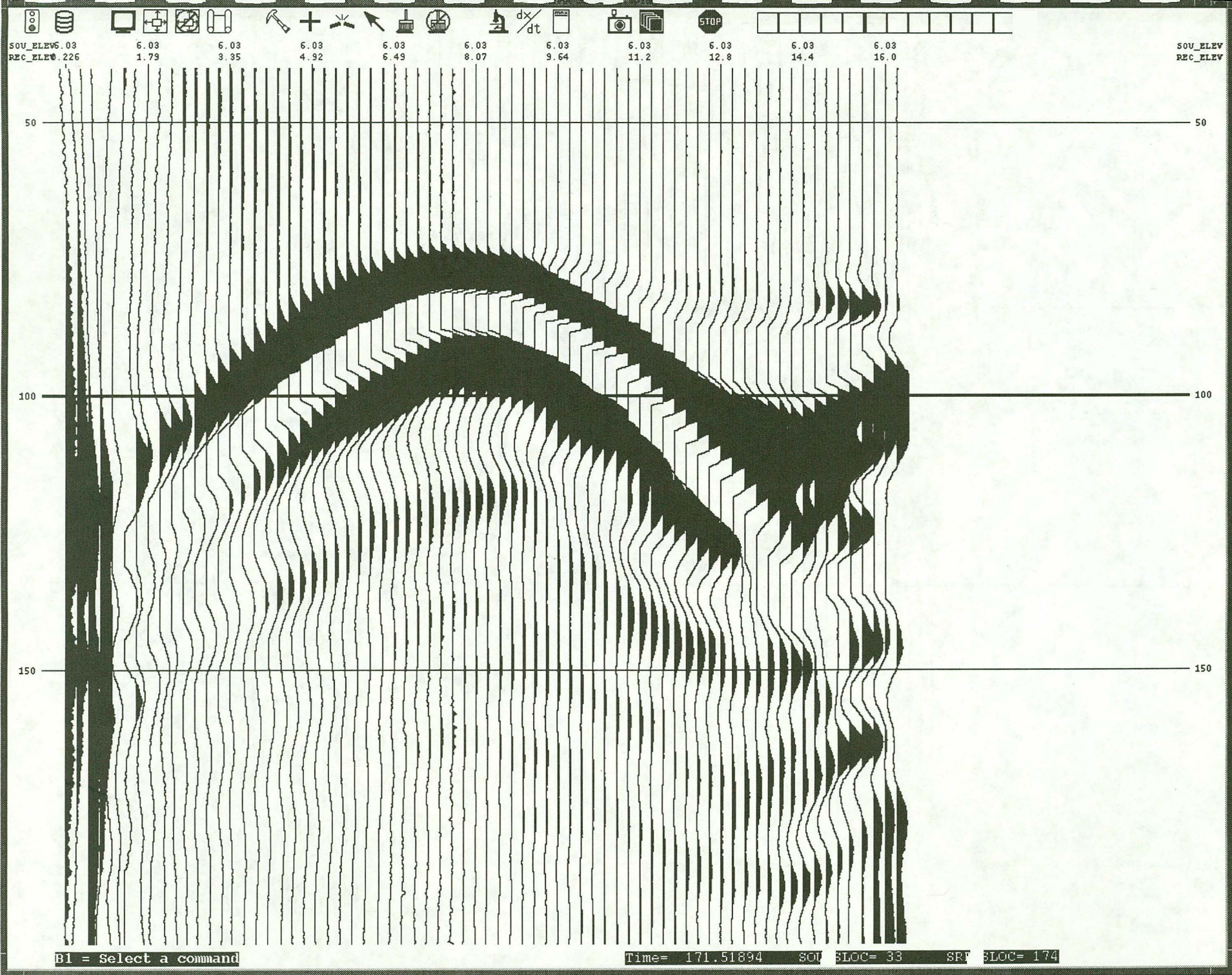
1 - PLS1 9/18/97 - 9/12/97



# BOX CANYON R2-R5 PRE

9/9/97





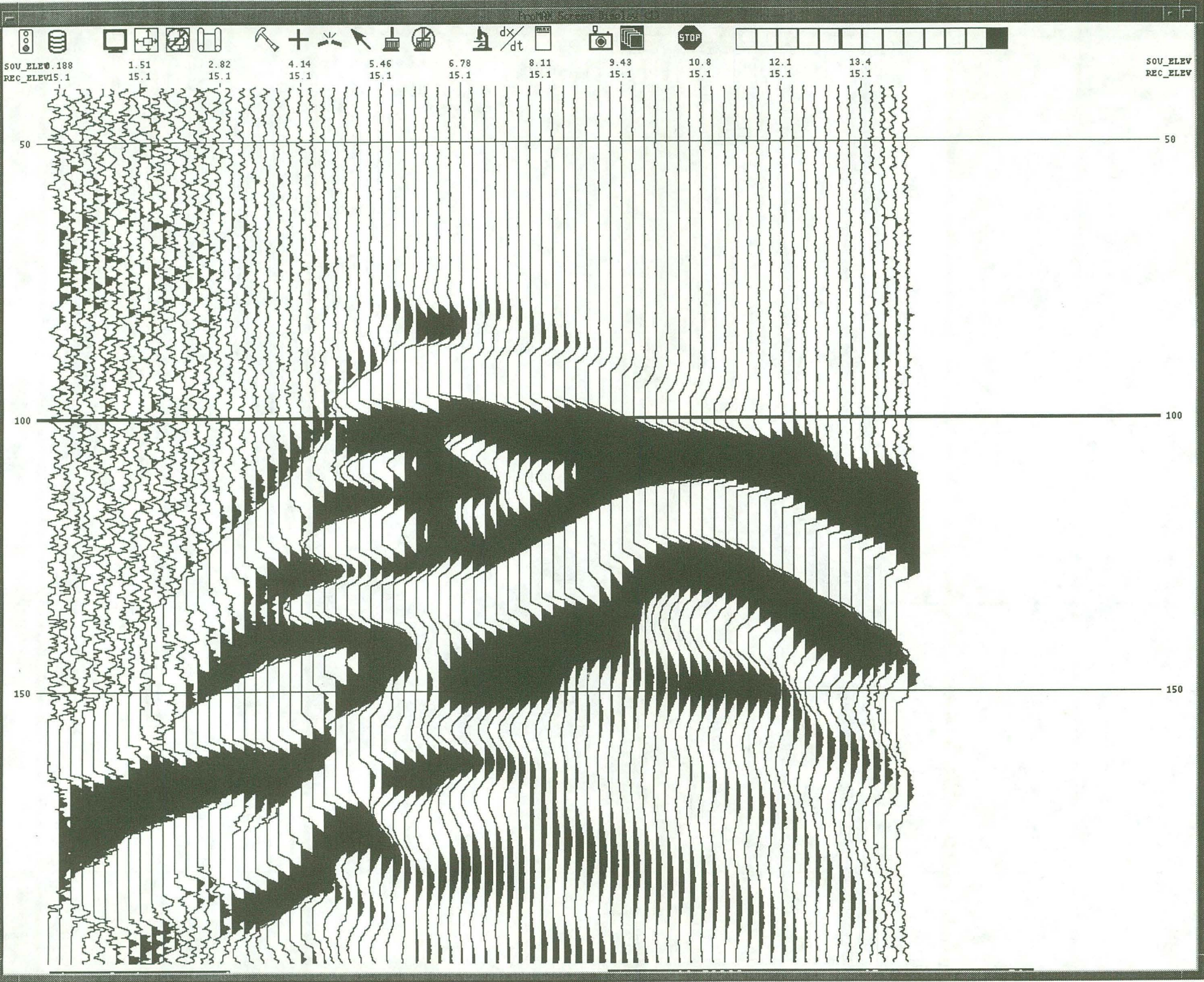
SOU_ELEV 03	6.03	6.03	6.03	6.03	6.03	6.03	6.03	6.03	6.03	6.03	6.03	SOU_ELEV
REC_ELEV 226	1.79	3.35	4.92	6.49	8.07	9.64	11.2	12.8	14.4	16.0		REC_ELEV

67

B1 = Select a command

Time= 171.51894 SOU \$LOC= 33 SRF \$LOC= 174





SOU\_ELEV 188  
REC\_ELEV 15.1

1.51 2.82  
15.1 15.1

4.14 5.46  
15.1 15.1

6.78 8.11  
15.1 15.1

9.43 10.8  
15.1 15.1

12.1 13.4  
15.1 15.1

SOU\_ELEV  
REC\_ELEV

89

50

50

100

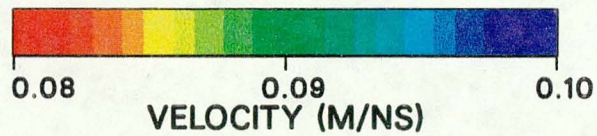
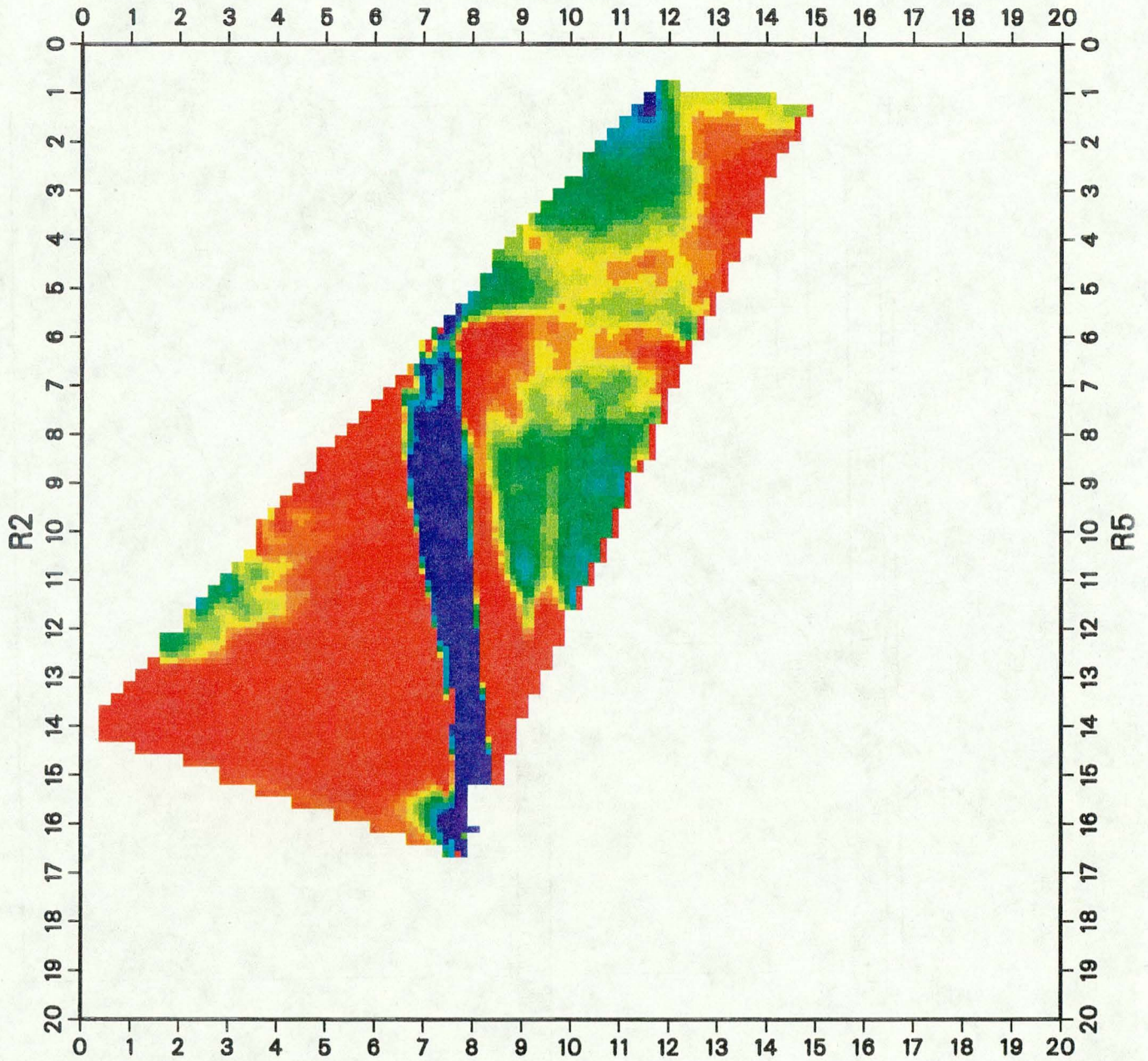
100

150

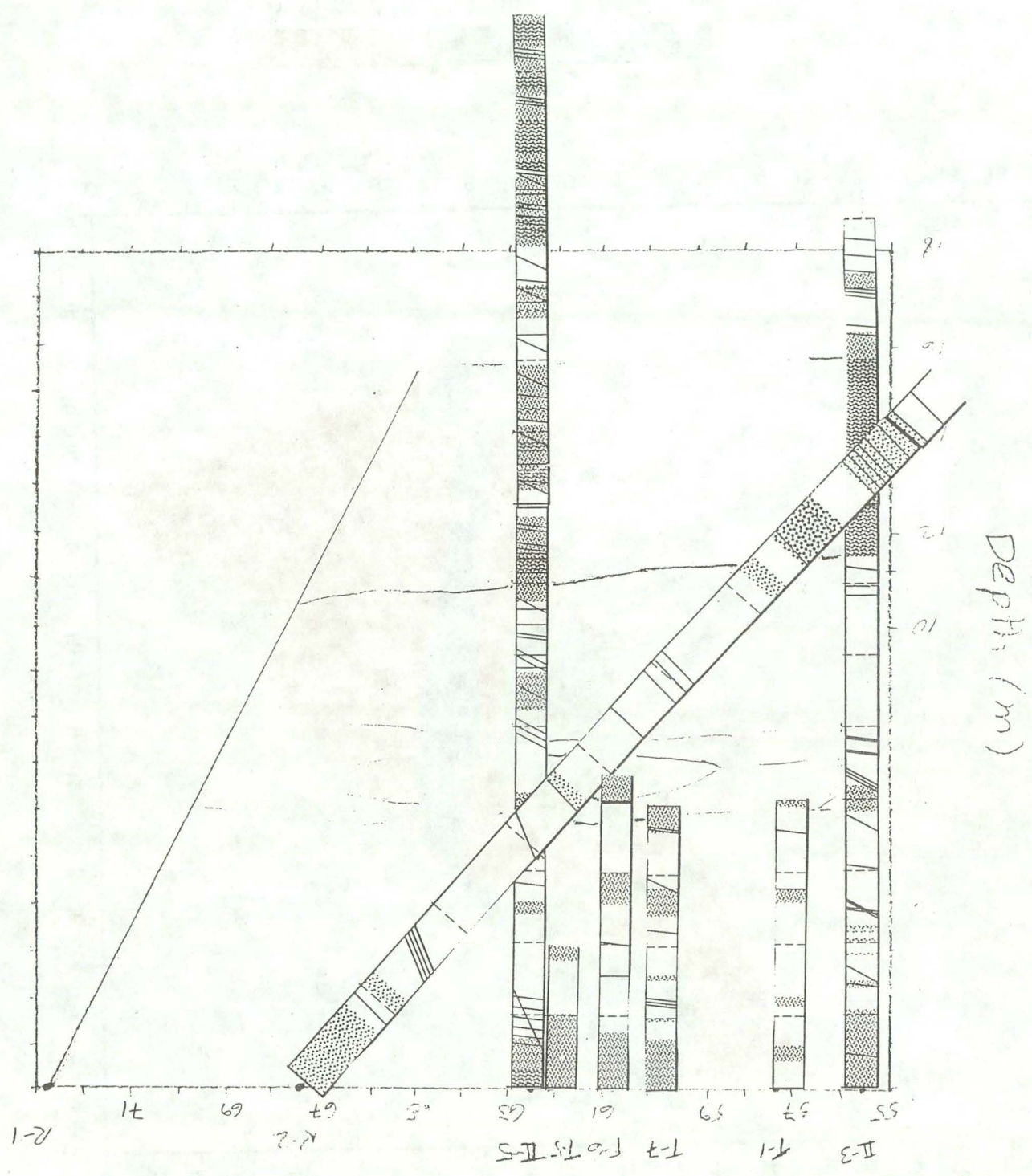
150

# BOX CANYON R2-R5 PRE

9/9/97



Handwritten notes at the top of the page, possibly including a title or reference number.



R1-R2 PLANE

II.3

# ERT Results from the Box Canyon Infiltration Experiment

Douglas LaBrecque

and

Gail Heath

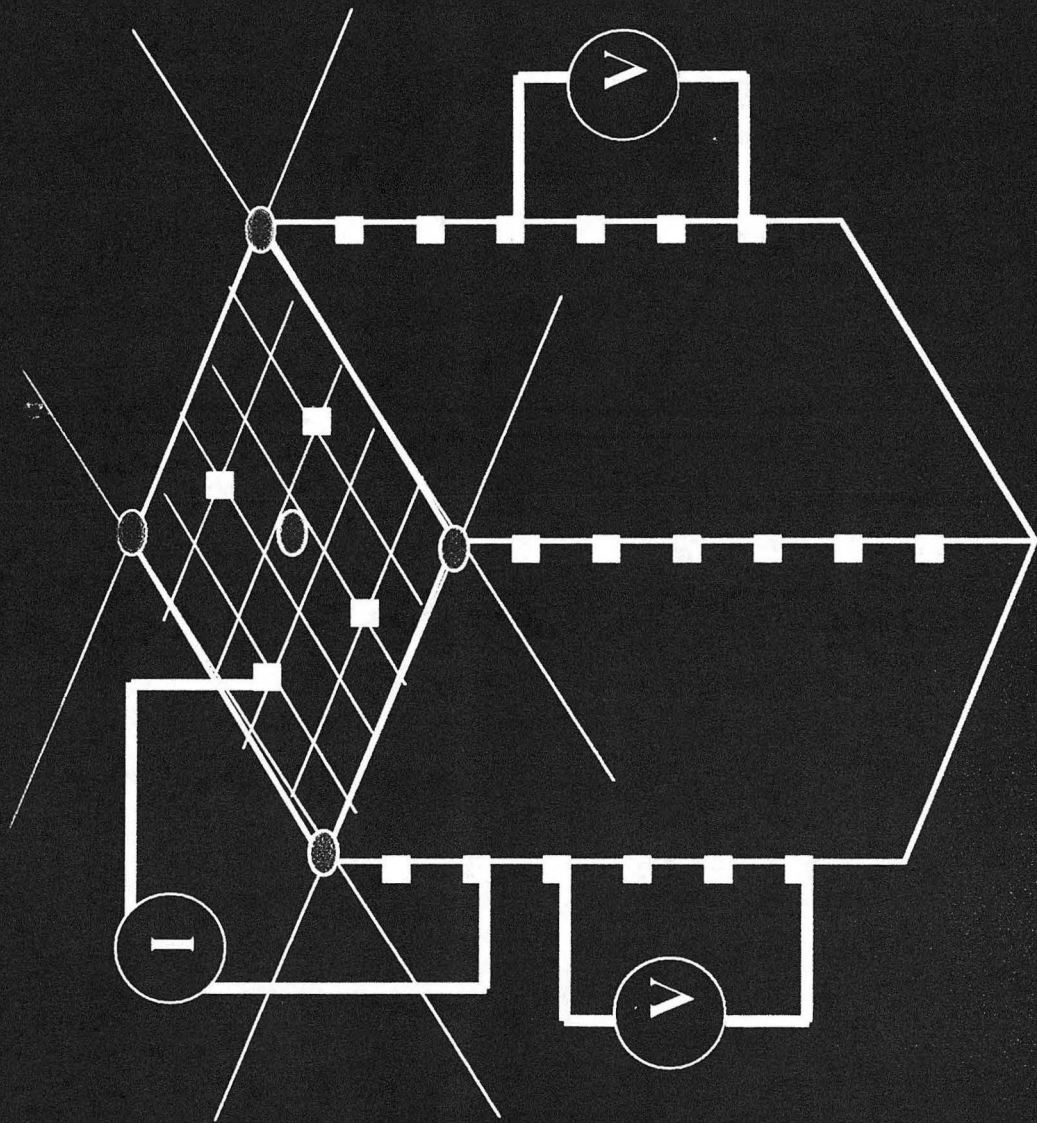
SteamTech Environmental Services



## Outline

- The ERT Method
- BXC Setup
  - ◆ Large Scale Survey Configuration
  - ◆ Small Scale Survey Configuration
- Results
  - ◆ Small Scale Survey
  - ◆ Large Scale Survey
- Conclusions

# 3D Electrical Resistivity Tomography



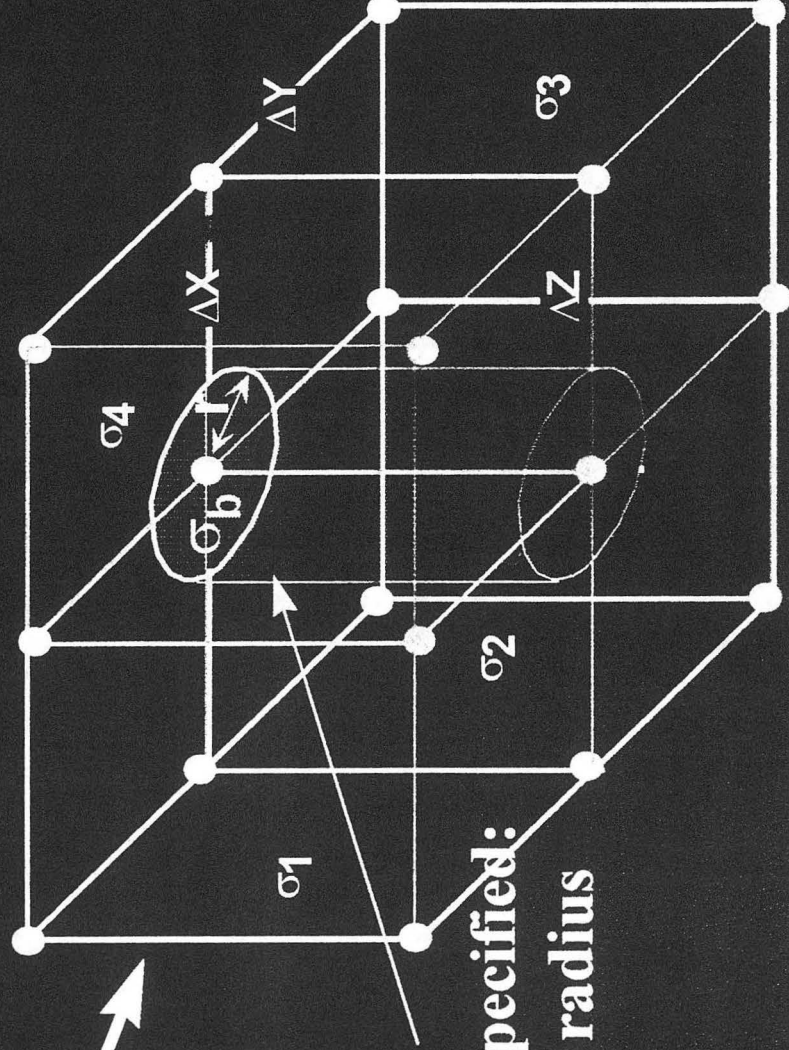
# The 3D Impedance Problem

3D Finite Differences forward modeling

Inverse problem solved with a Preconditioned Conjugate

Gradients technique

Effects of conductive boreholes and anomalous objects can be modeled



parameters to be specified:  
**conductivity and radius**

# Nonlinear Inversion

Iteratively update the vector of parameters

$$\underline{P}_{k+1} = \underline{P}_k + \underline{\Delta P}_k$$

by approximately solving the linear system

$$\underline{\Delta P}_k = - ( \underline{A}_k^T \underline{W} \underline{A}_k + \underline{R} )^{-1} ( \underline{W} ( \underline{D} - F(\underline{P}_k) ) - \underline{R} \underline{P}_k )$$

with the Conjugate-Gradient Method



# Scale Survey

# Wells With Packers



Packer 3



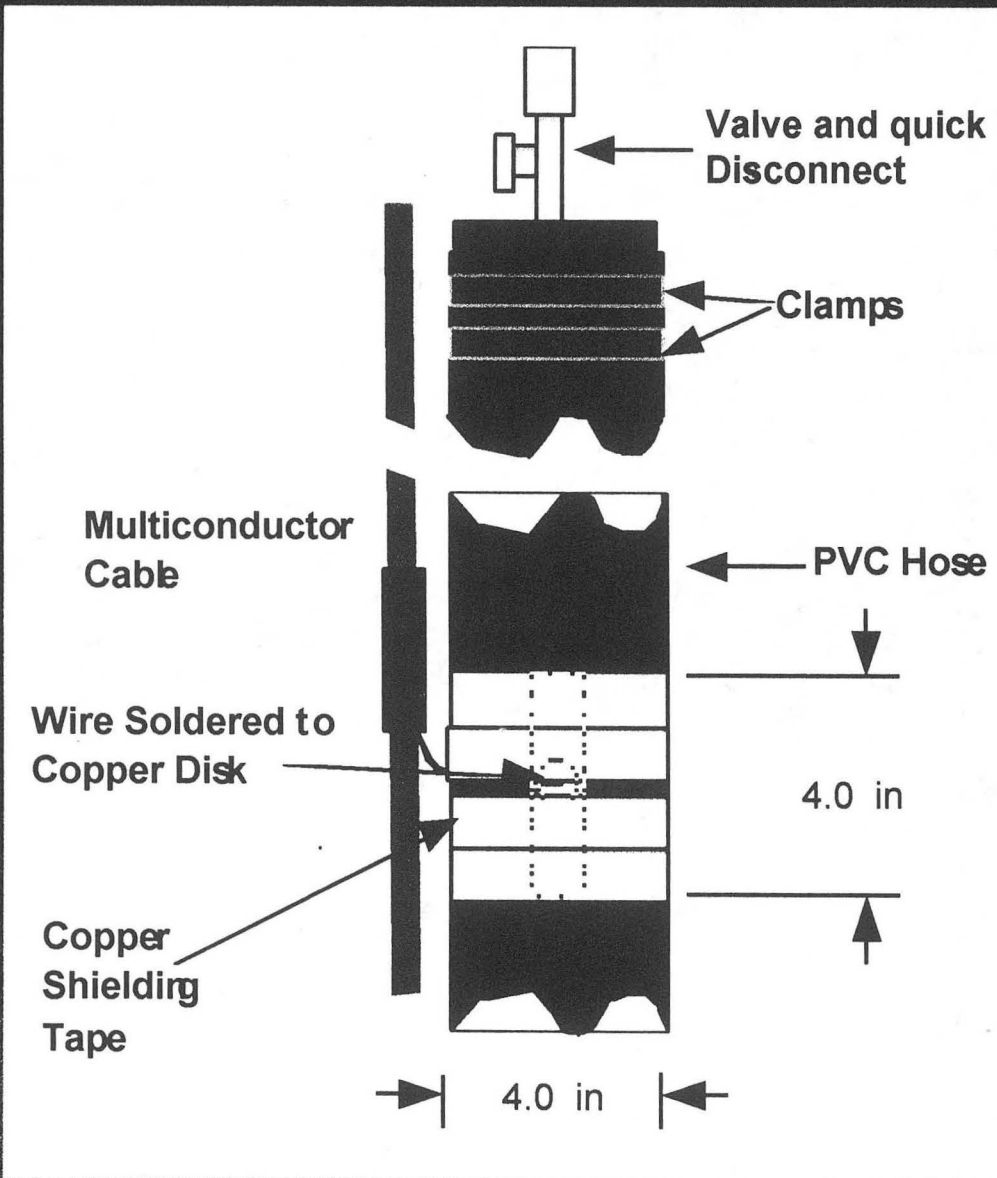
Packer 1



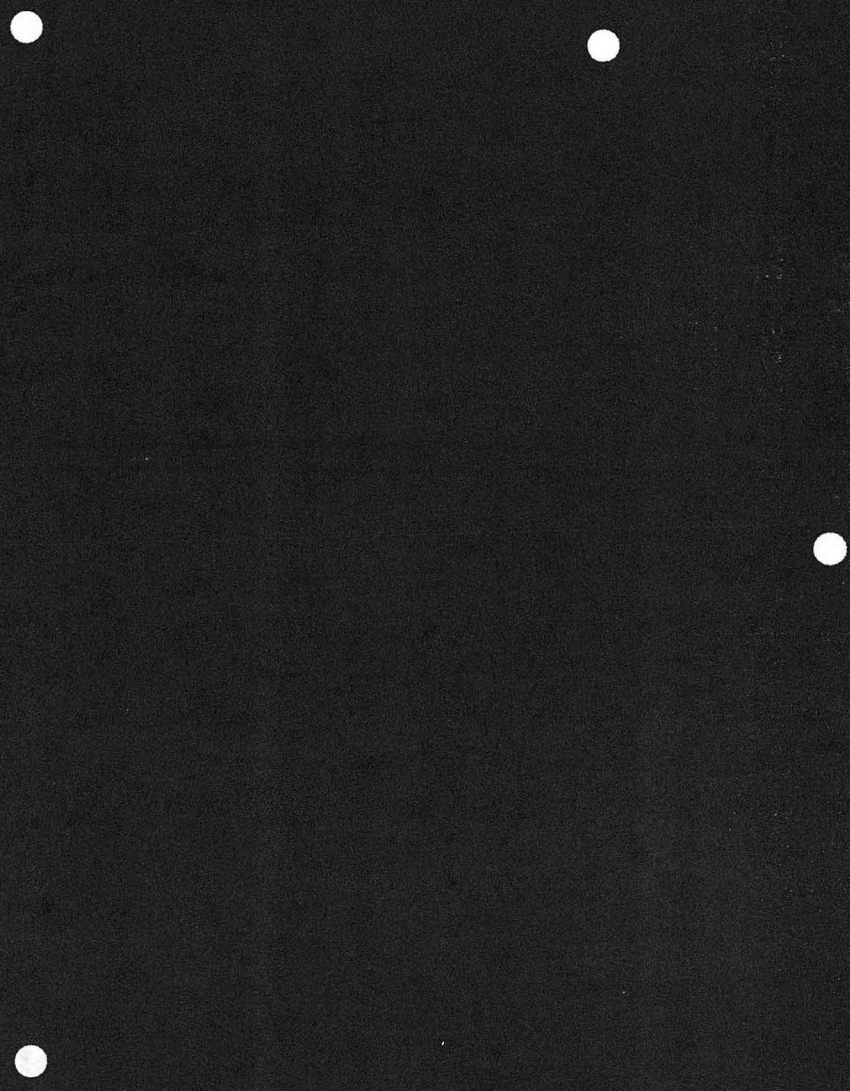
Packer 2

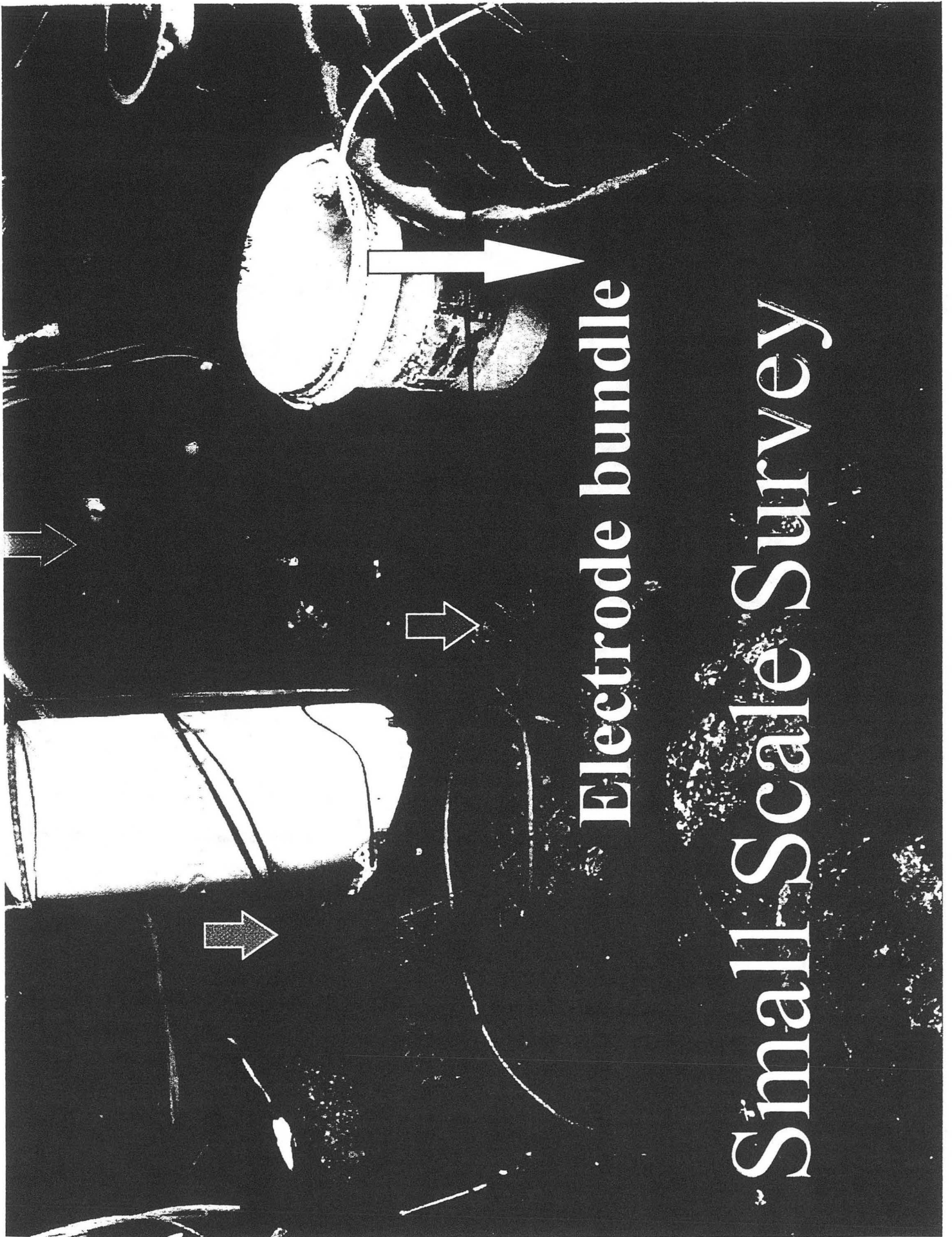


# Packer Design



# Large Scale Survey Method Electrode Configuration

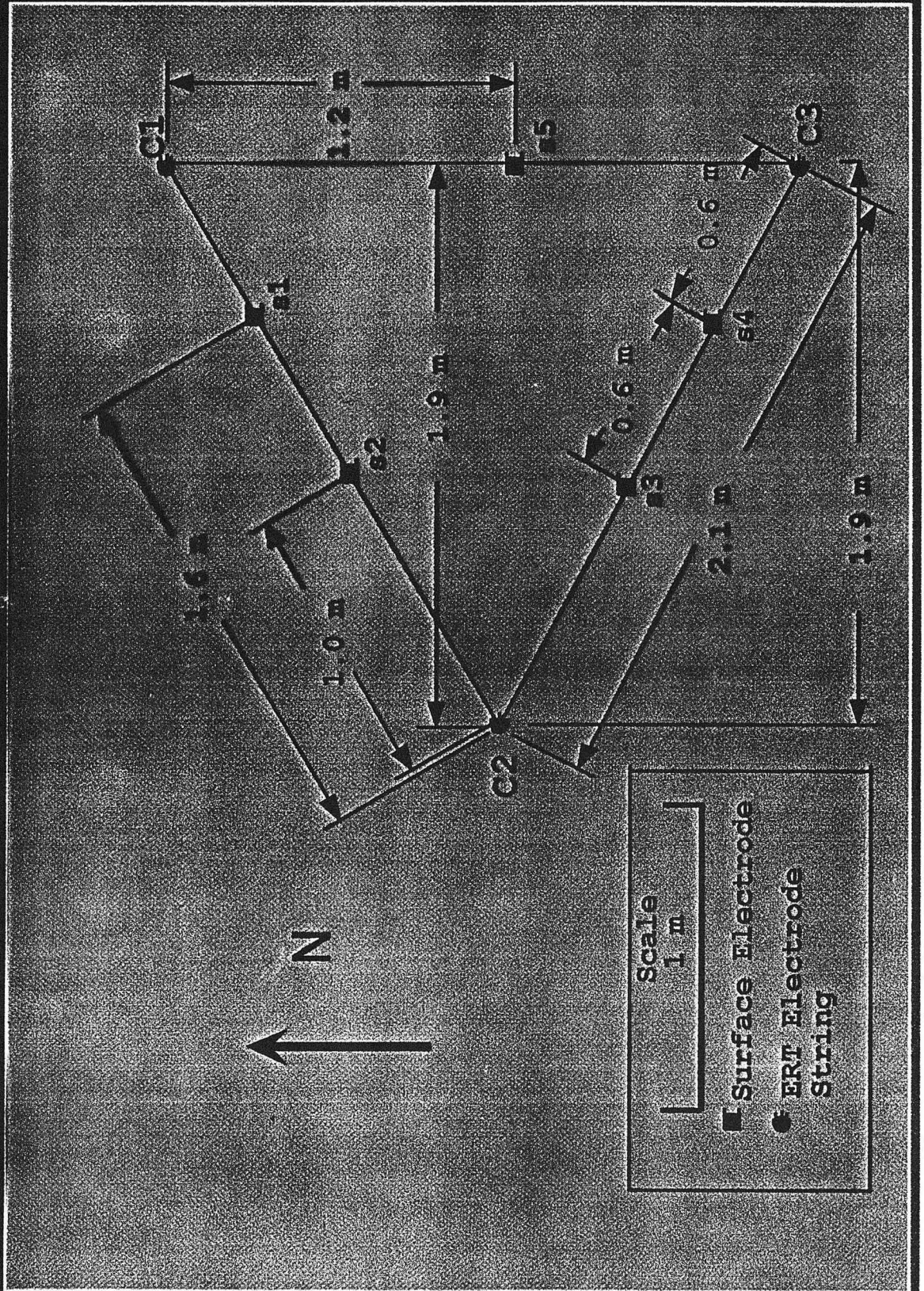




**Electrode bundle**

**Small Scale Survey**

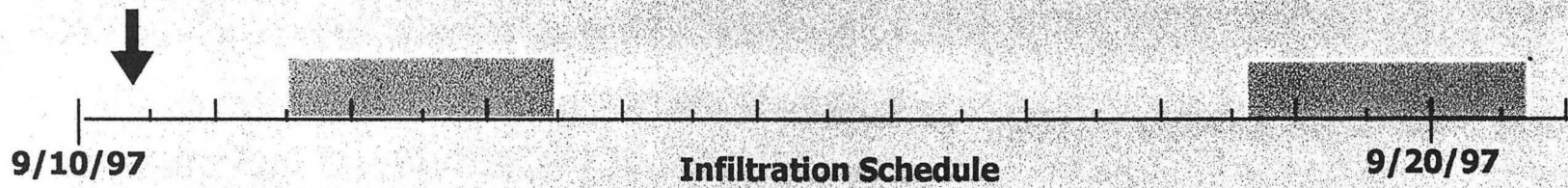
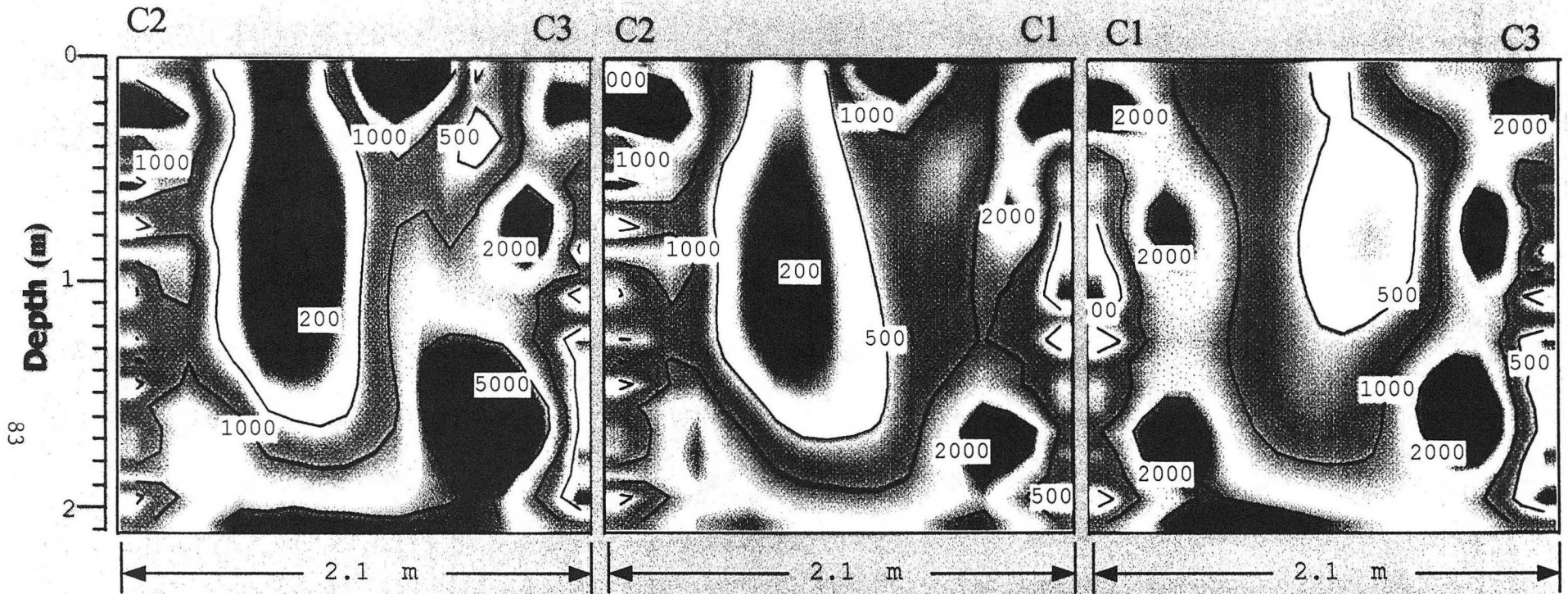
# Layout of Small Scale Survey





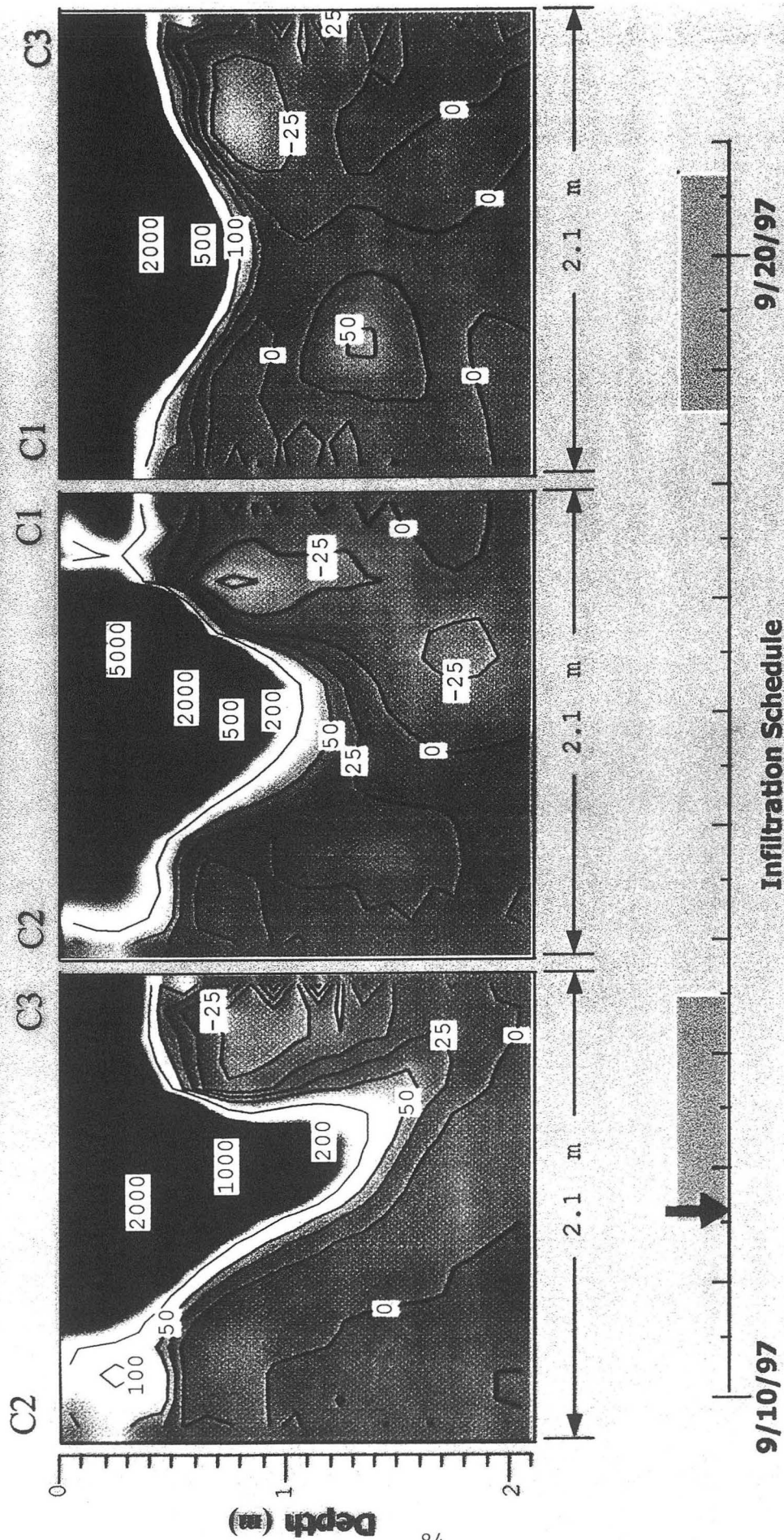
# Small Scale Survey Results

# Small-Scale Survey 9/11/97 10:00 hours Background Resistivity

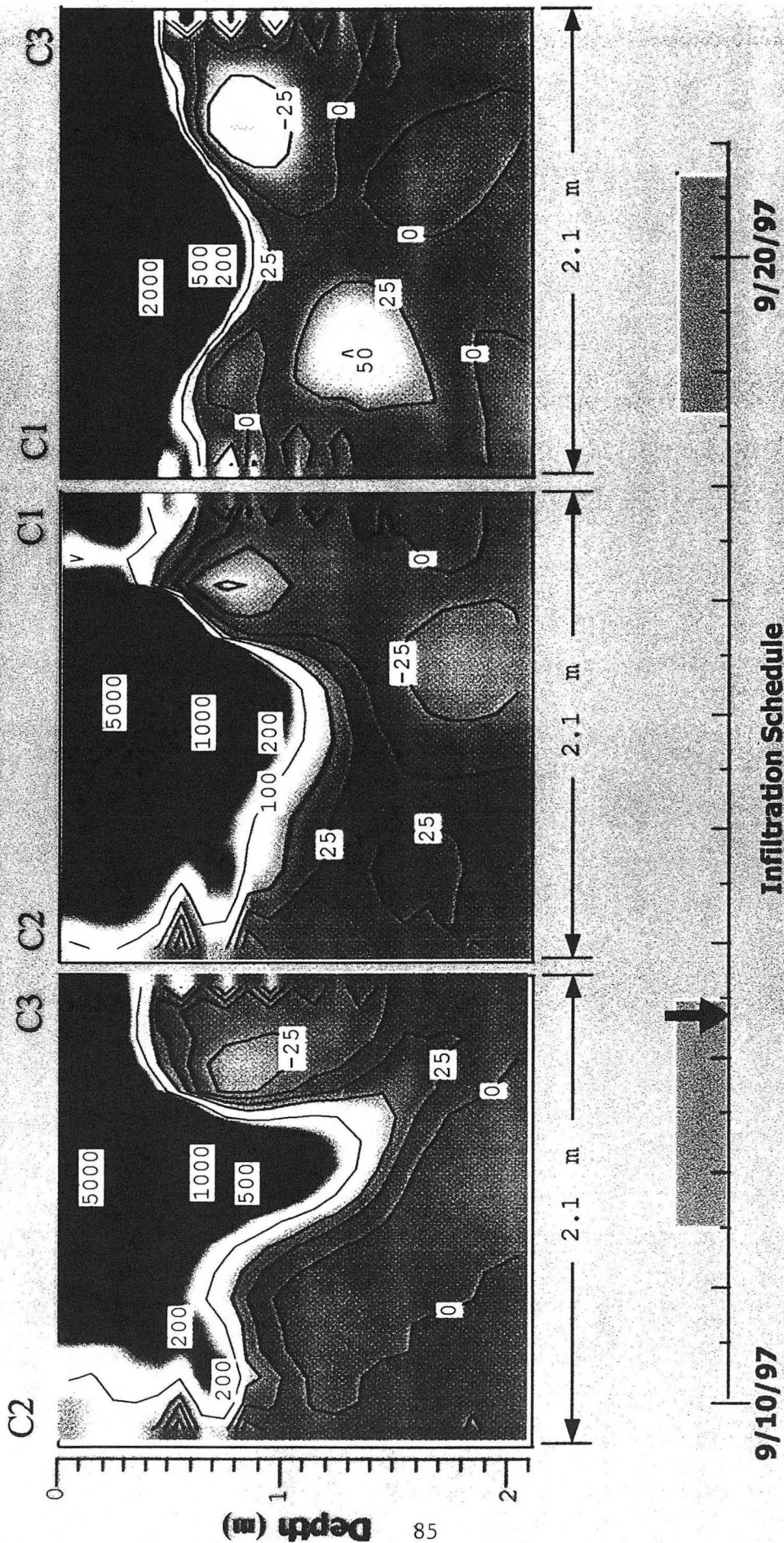




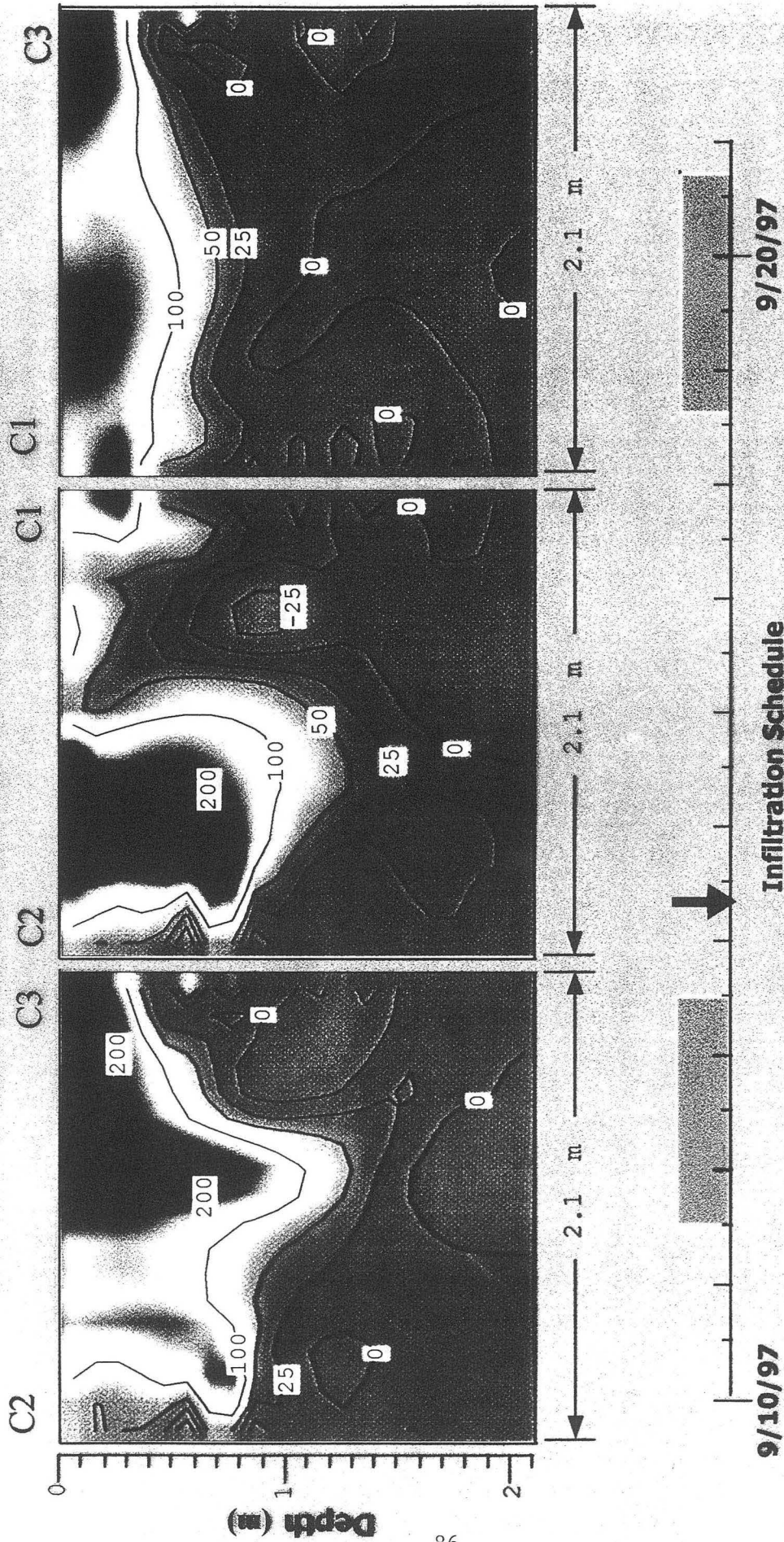
**Small-Scale Survey 9/11/97 13:20 hours  
Percent-Difference from 9/11/97 10:00 Hours**



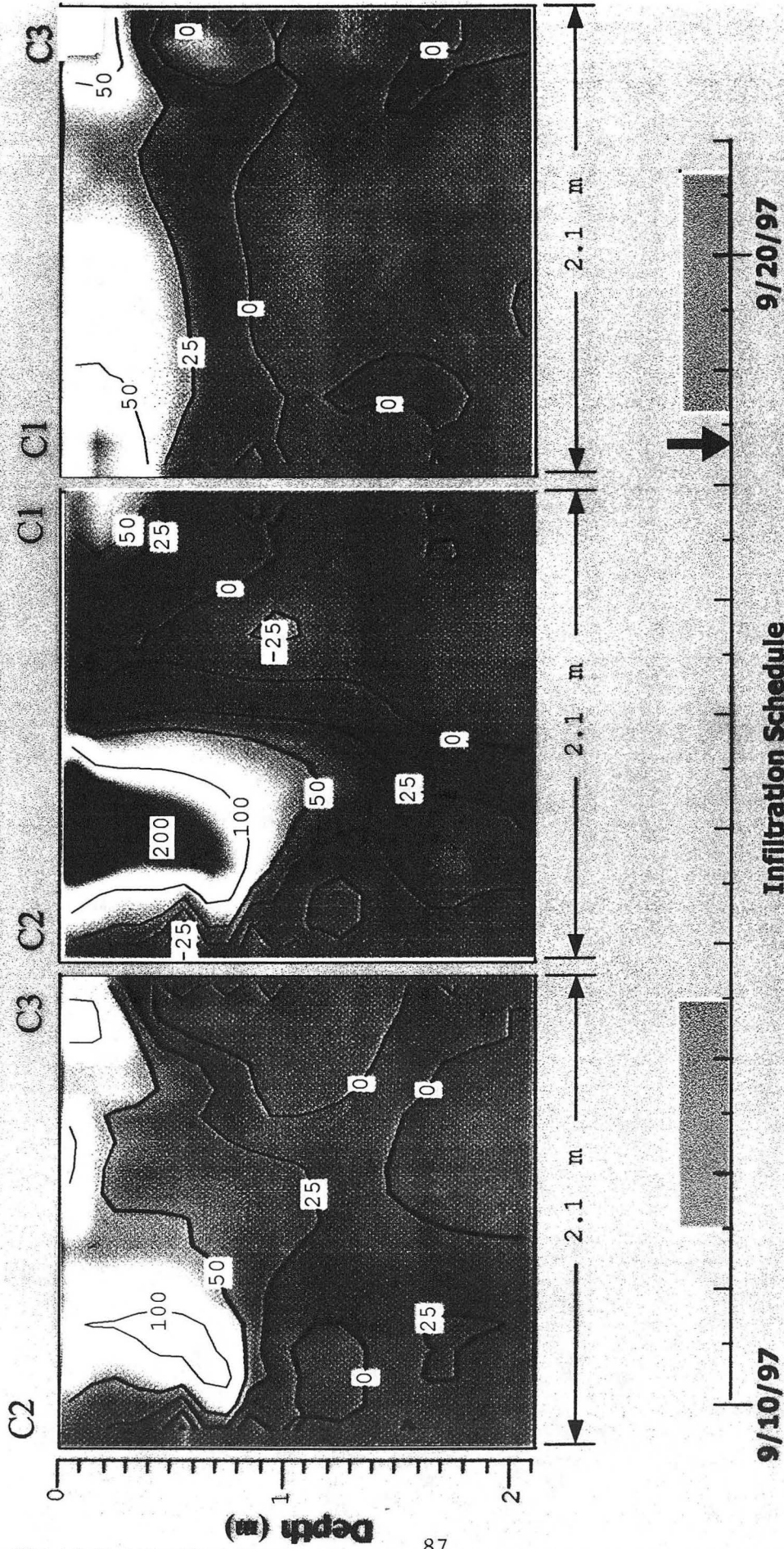
**Small-Scale Survey 9/13/97 8:10 hours  
Percent-Difference from 9/11/97 10:00 Hours**



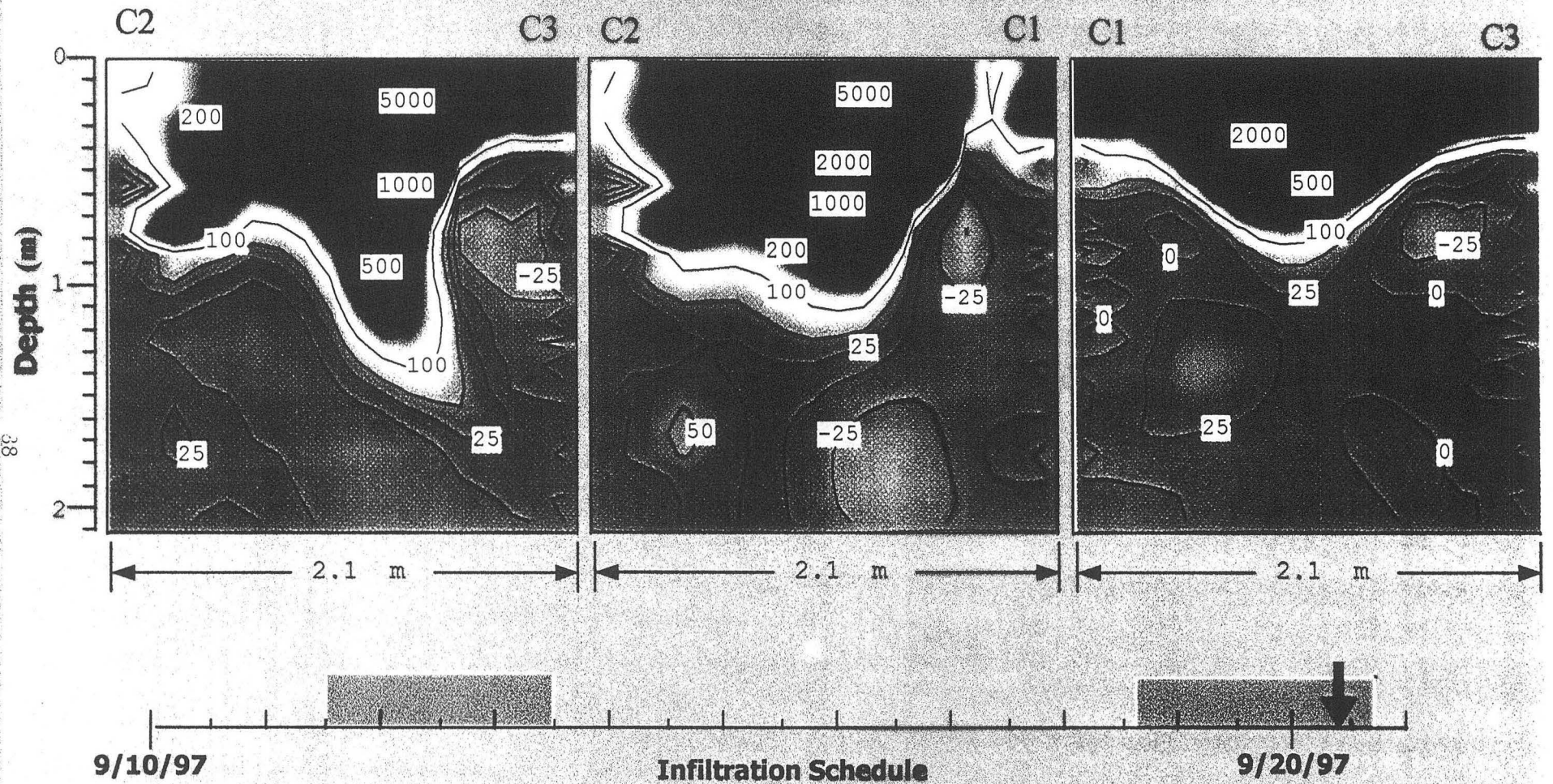
**Small-Scale Survey 9/14/97 8:20 hours  
Percent-Difference from 9/11/97 10:00 Hours**



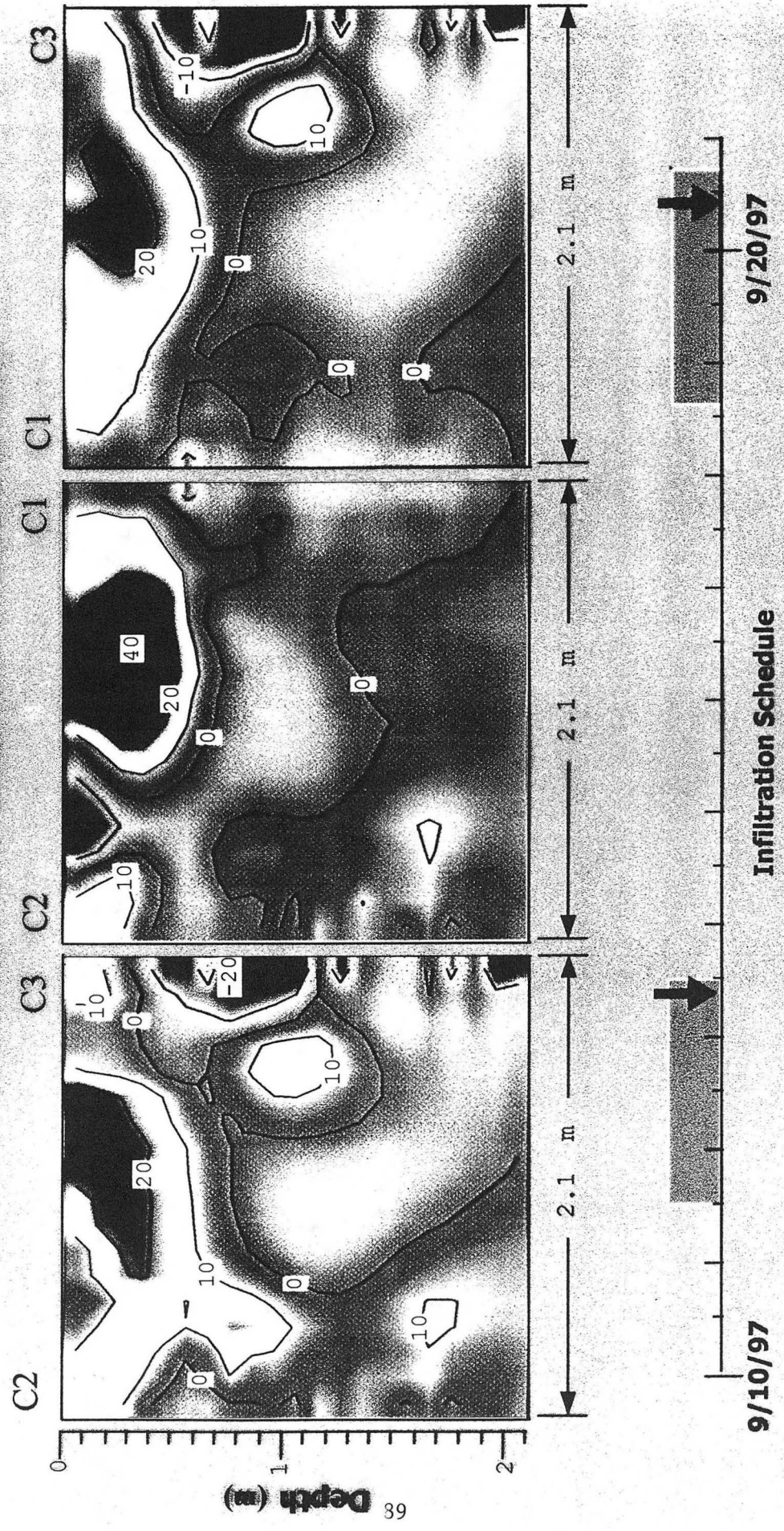
**Small-Scale Survey 9/18/97 10:20 hours  
Percent-Difference from 9/11/97 10:00 Hours**



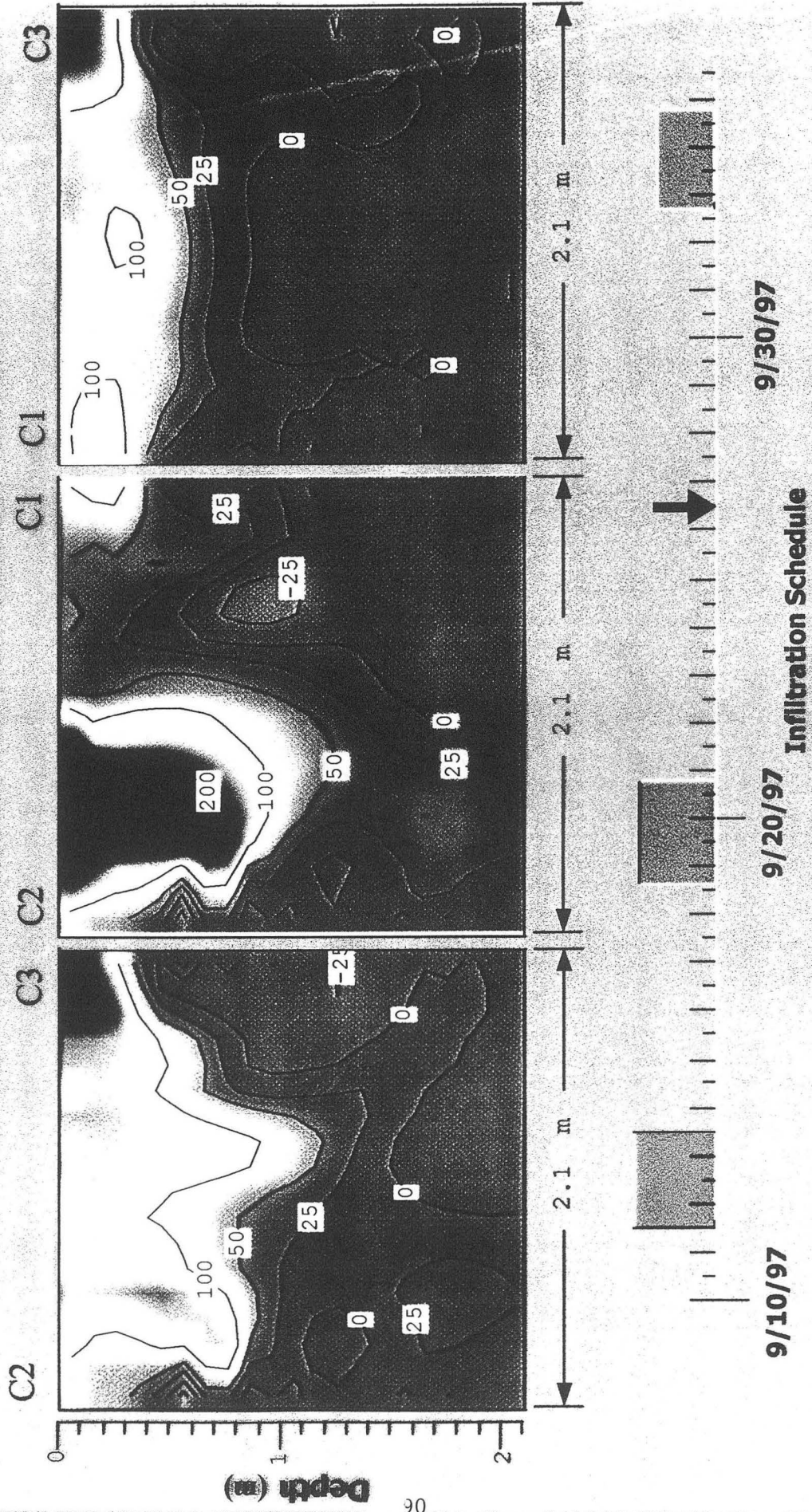
# Small-Scale Survey 9/20/97 11:00 hours Percent-Difference from 9/11/97 10:00 Hours



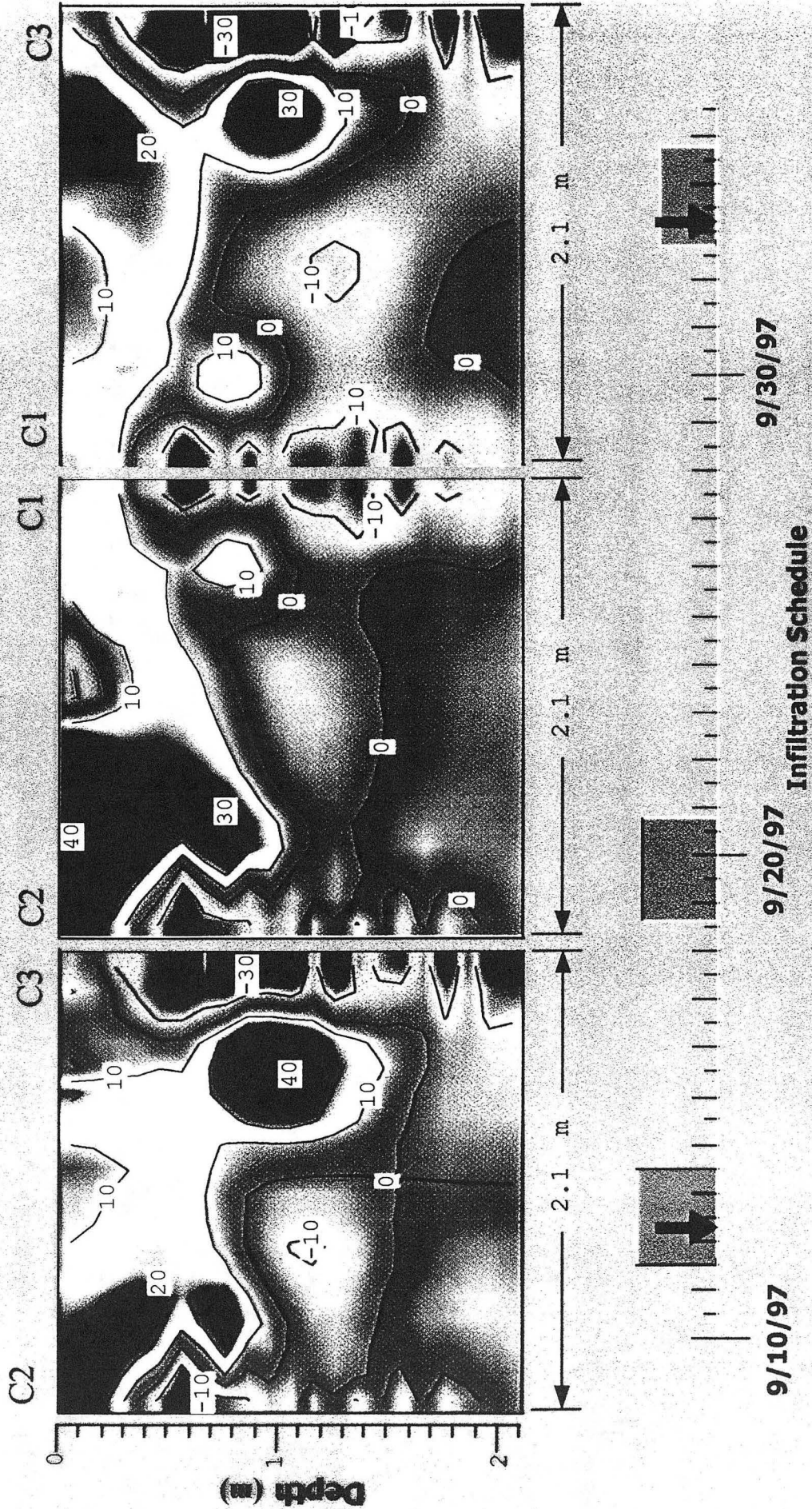
**Small-Scale Survey 9/18/97 20:40 hours  
Percent-Difference from 9/11/97 14:30 Hours**



**Small-Scale Survey 9/26/97 12:00 hours  
Percent-Difference from 9/11/97 10:00 Hours**

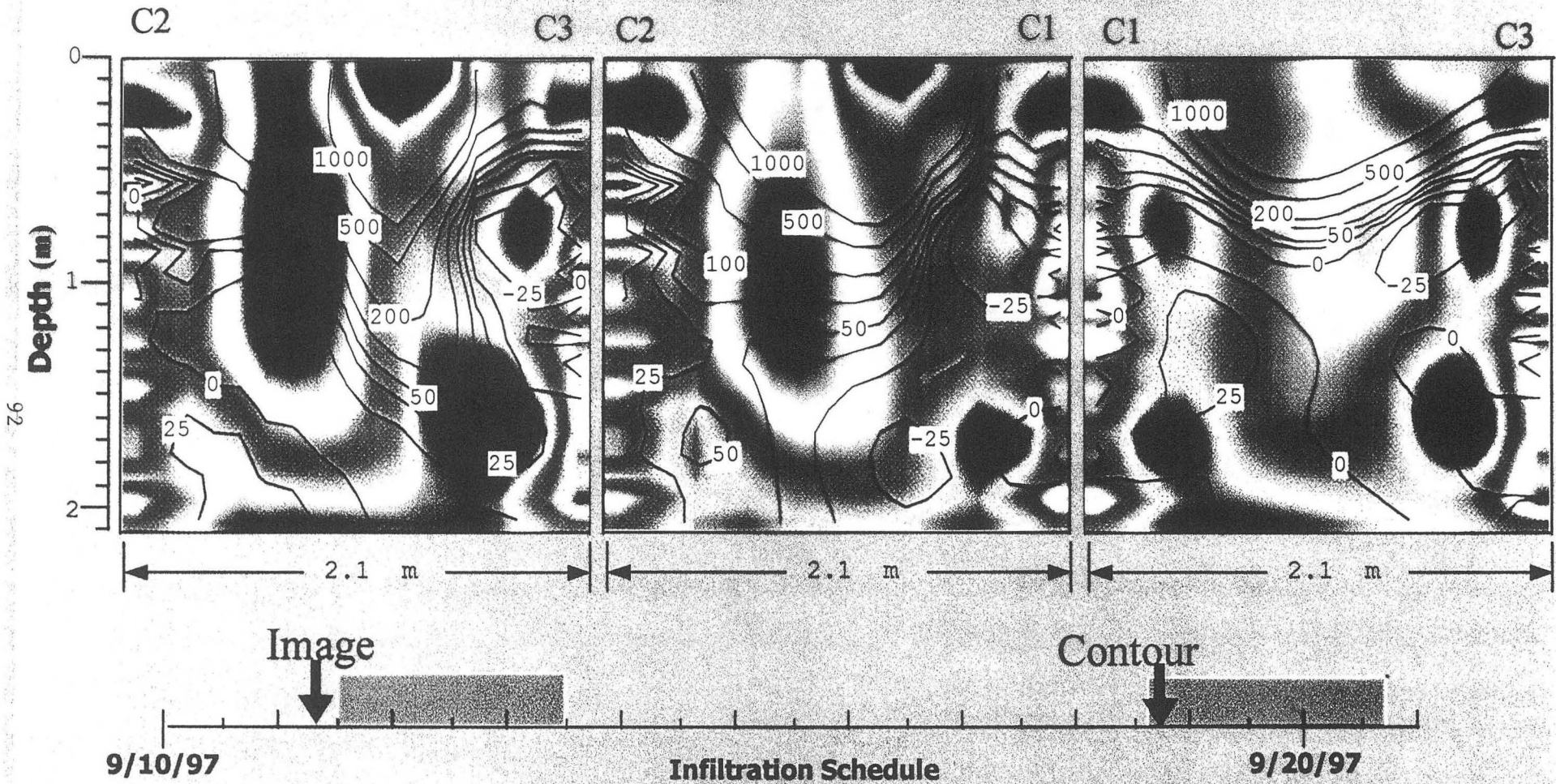


**Small-Scale Survey 10/03/97 8:20 hours  
Percent-Difference from 9/12/97 9:40 Hours**





# Small-Scale Survey Percent-Difference Contours from 10/18 Overlaid on Background Resistivity Images



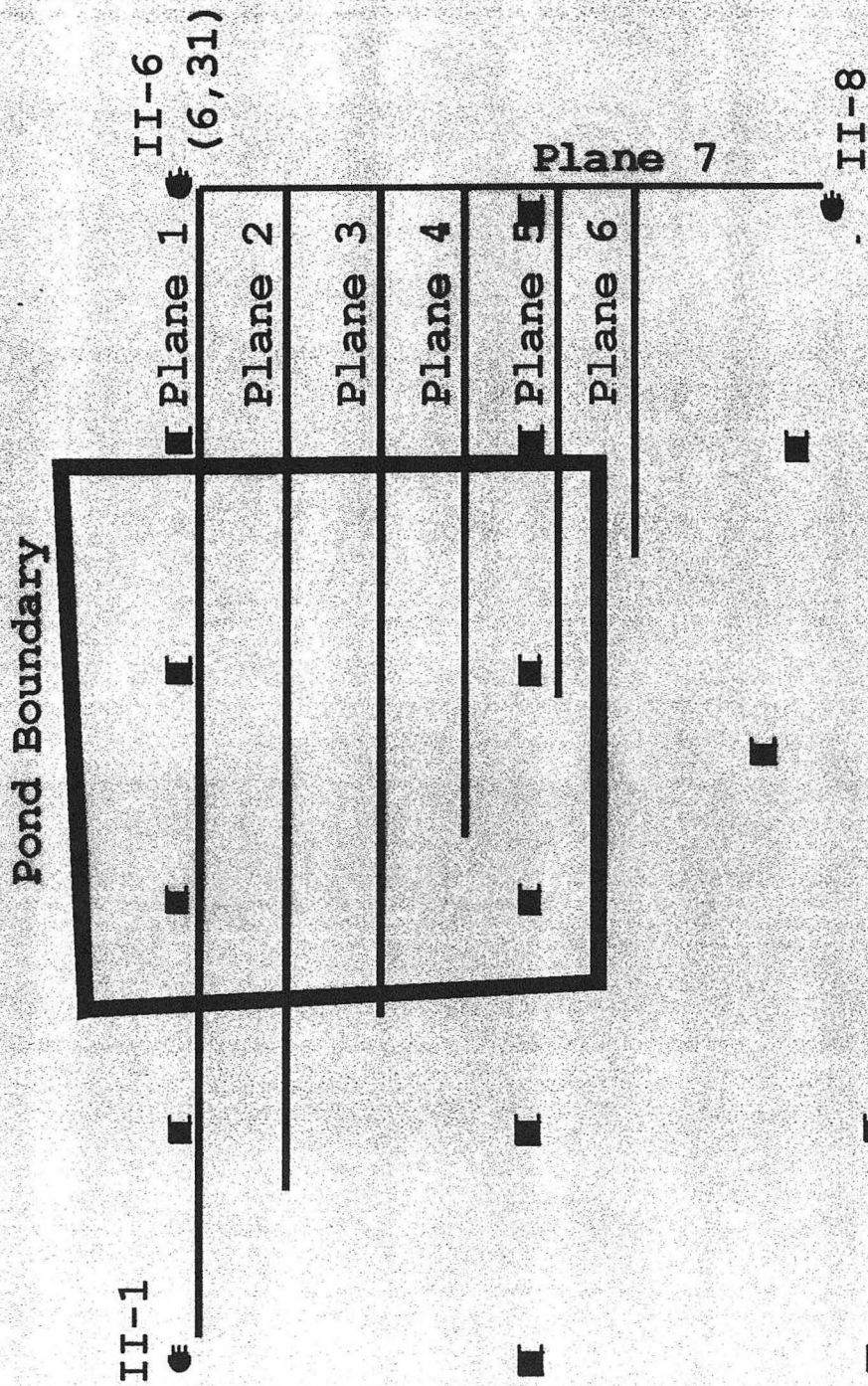
# Conclusions

- Inner Survey Showed Two Types of Pathways:
  - ◆ Very Rapid Infiltration
  - ◆ Slower (Permeation?) Paths
- There Were Cumulative Long Term Changes from Experiment to Experiment Primarily in the Slower Pathways

# Survey Results



# Location of Planes for Large Scale Survey Images

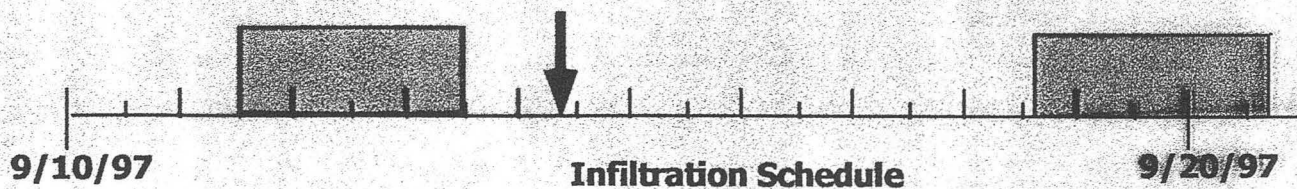
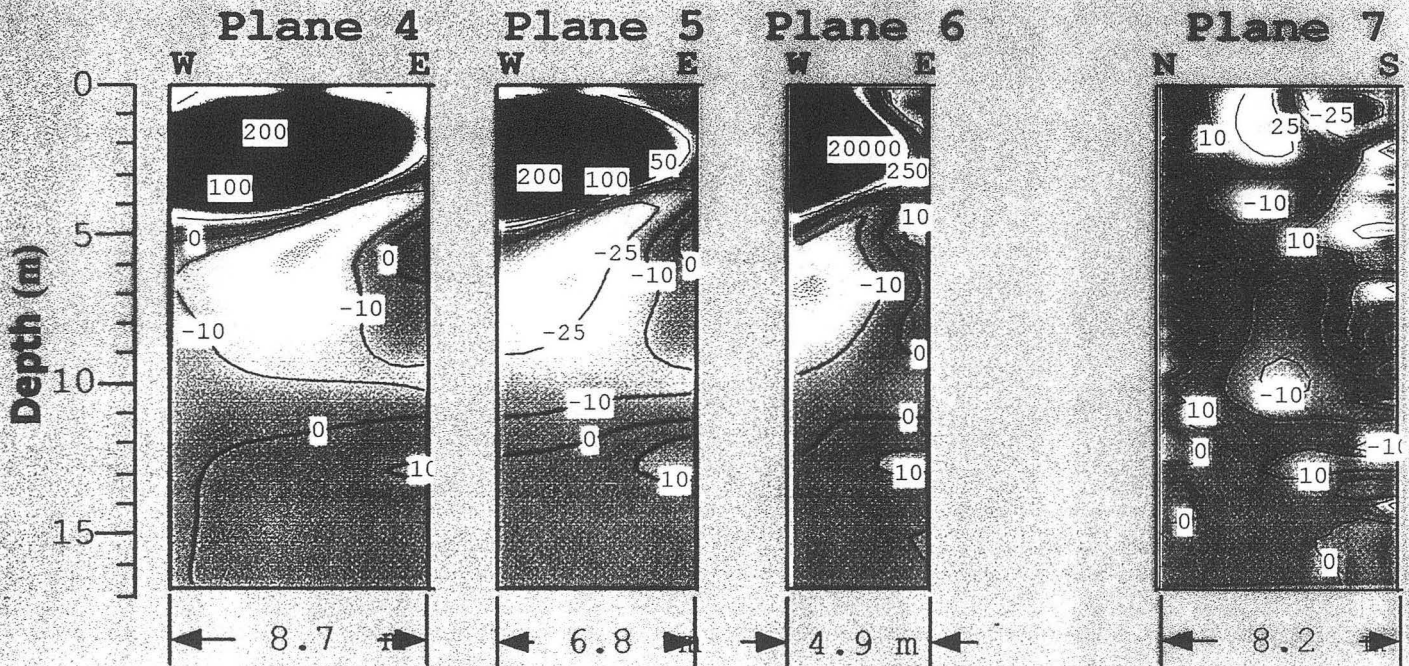
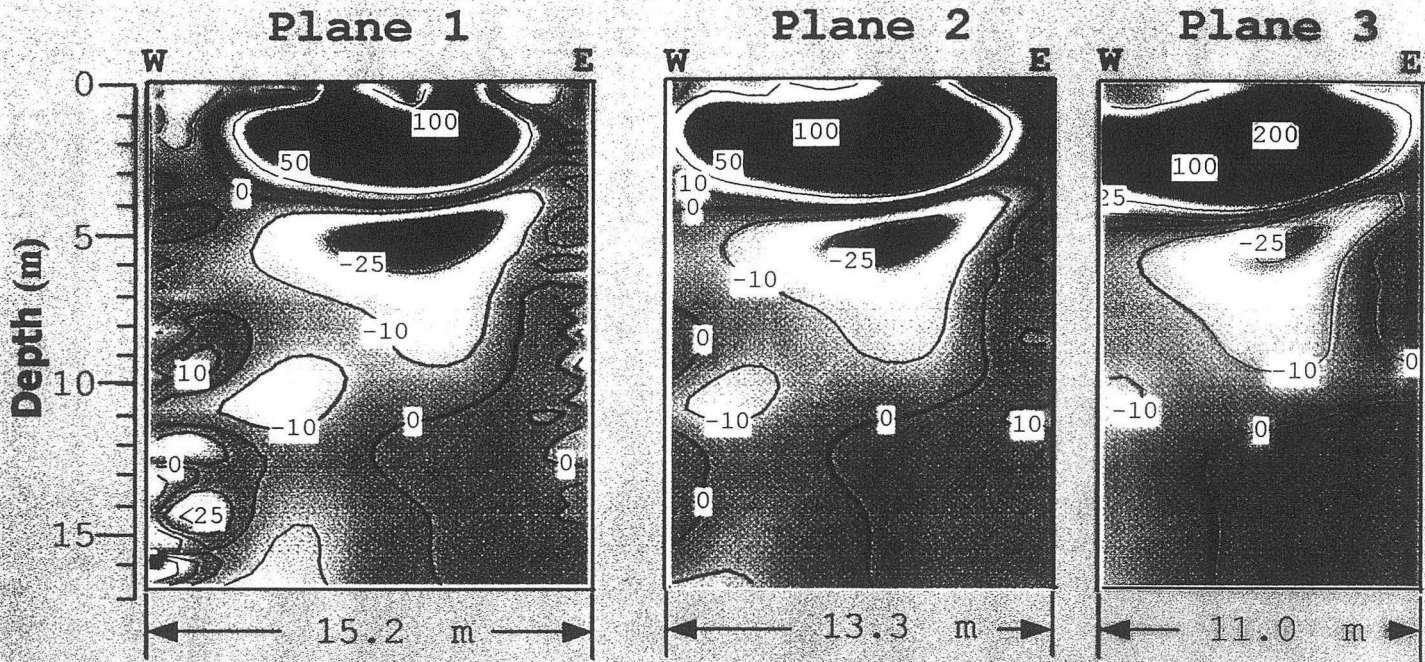






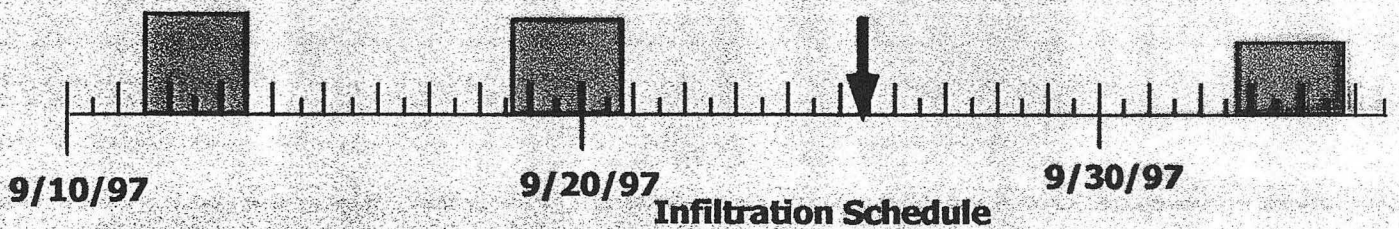
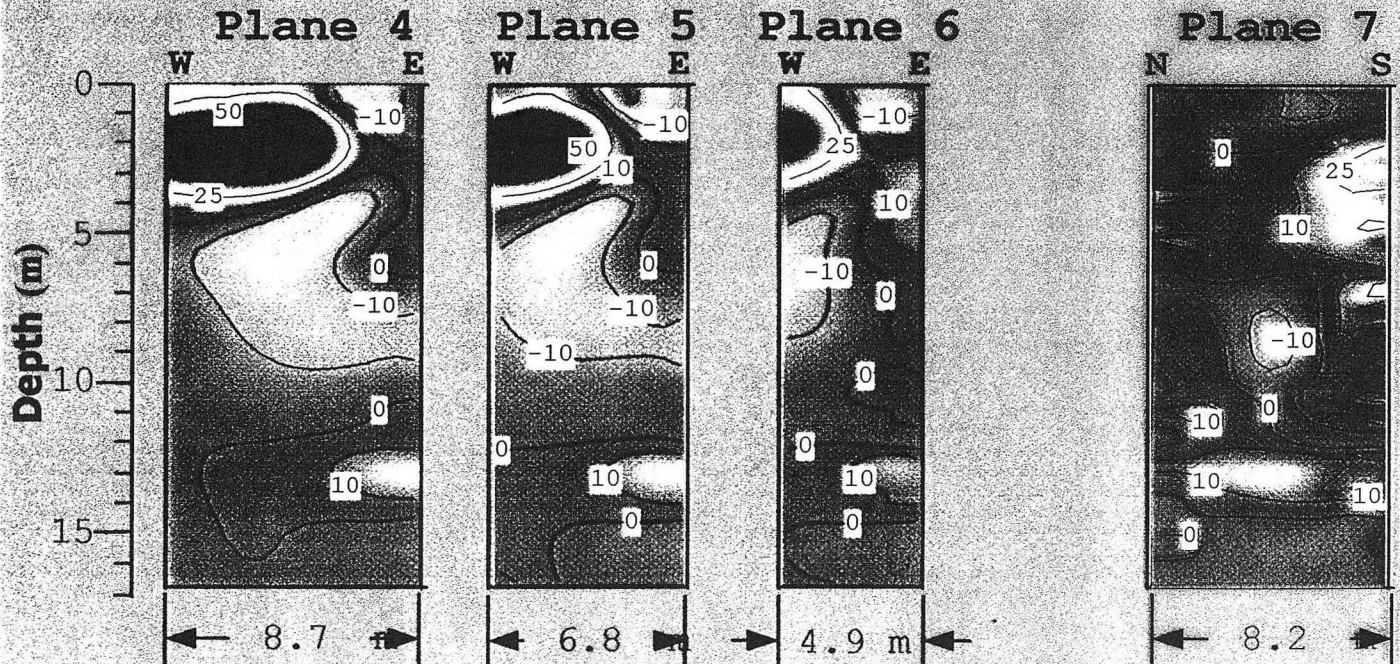
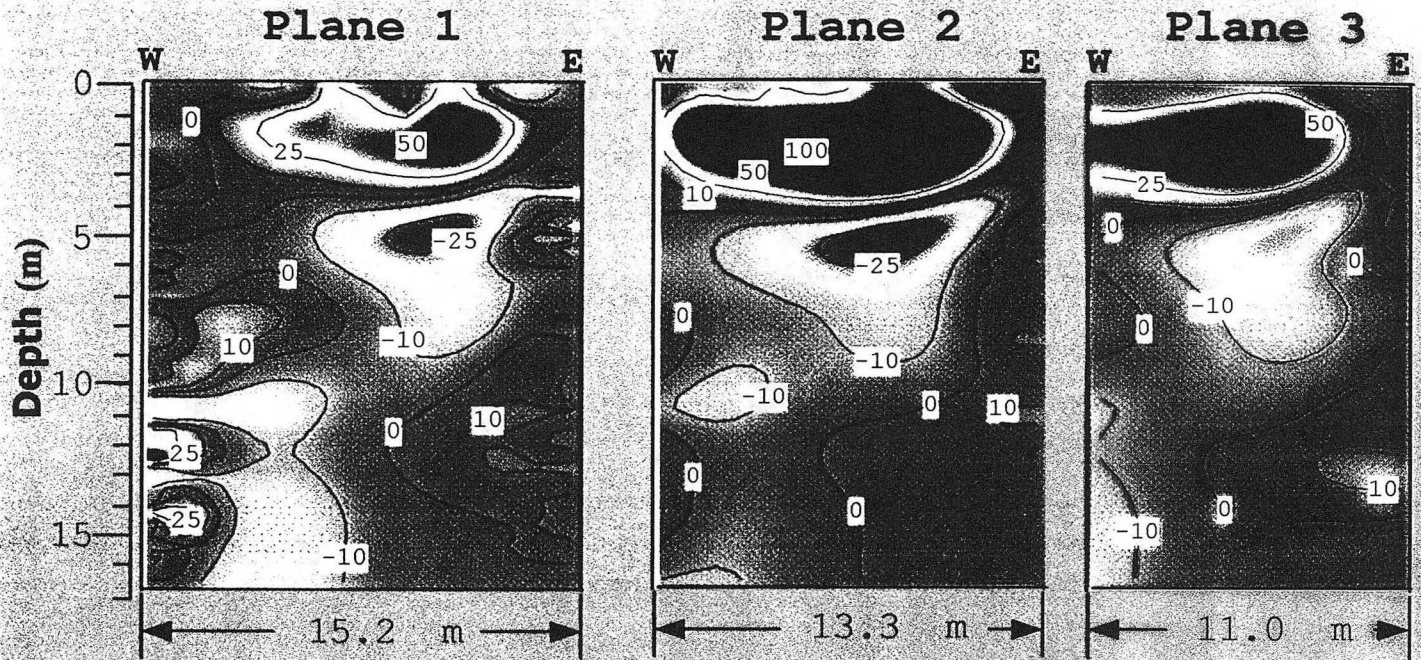
# Outer Survey 9/14/97 13:00 Hours

## Percent Difference from 9/11/97 11:00 Hours



# Outer Survey 9/25/97 13:00 Hours

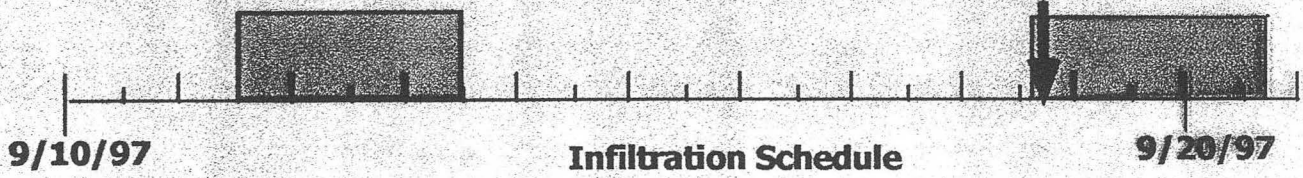
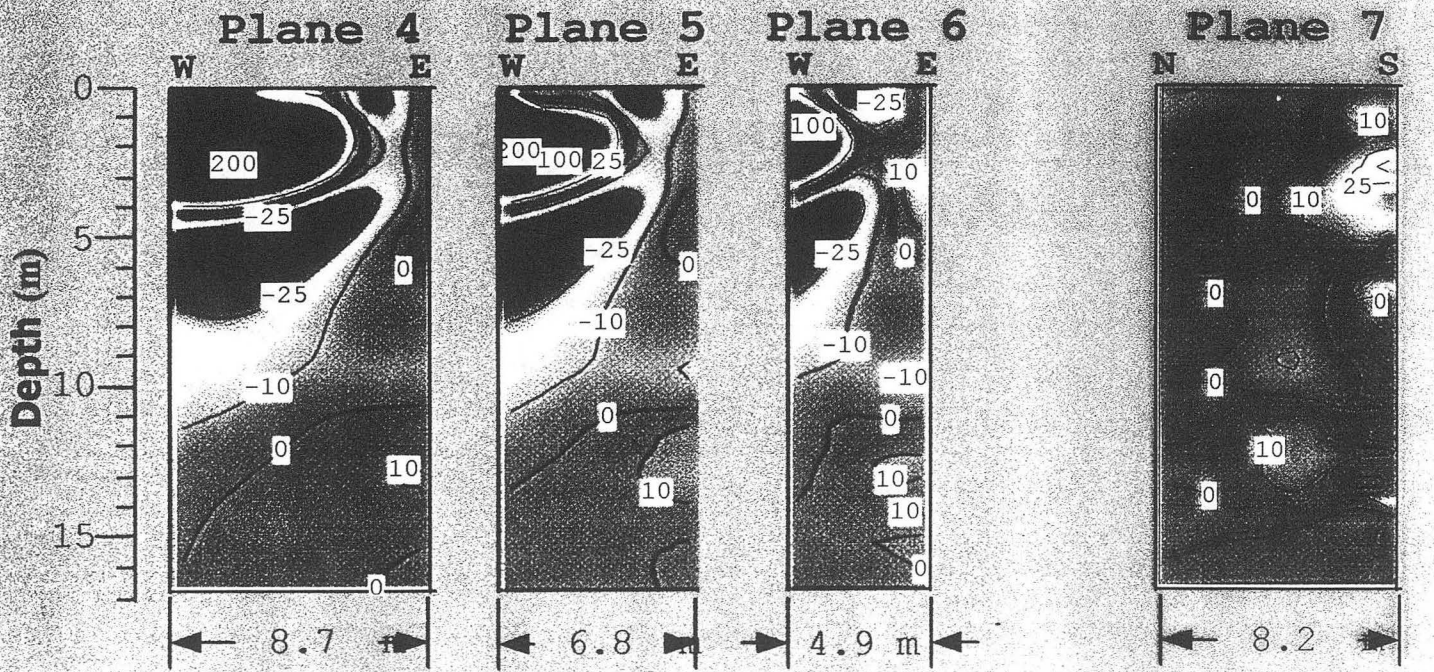
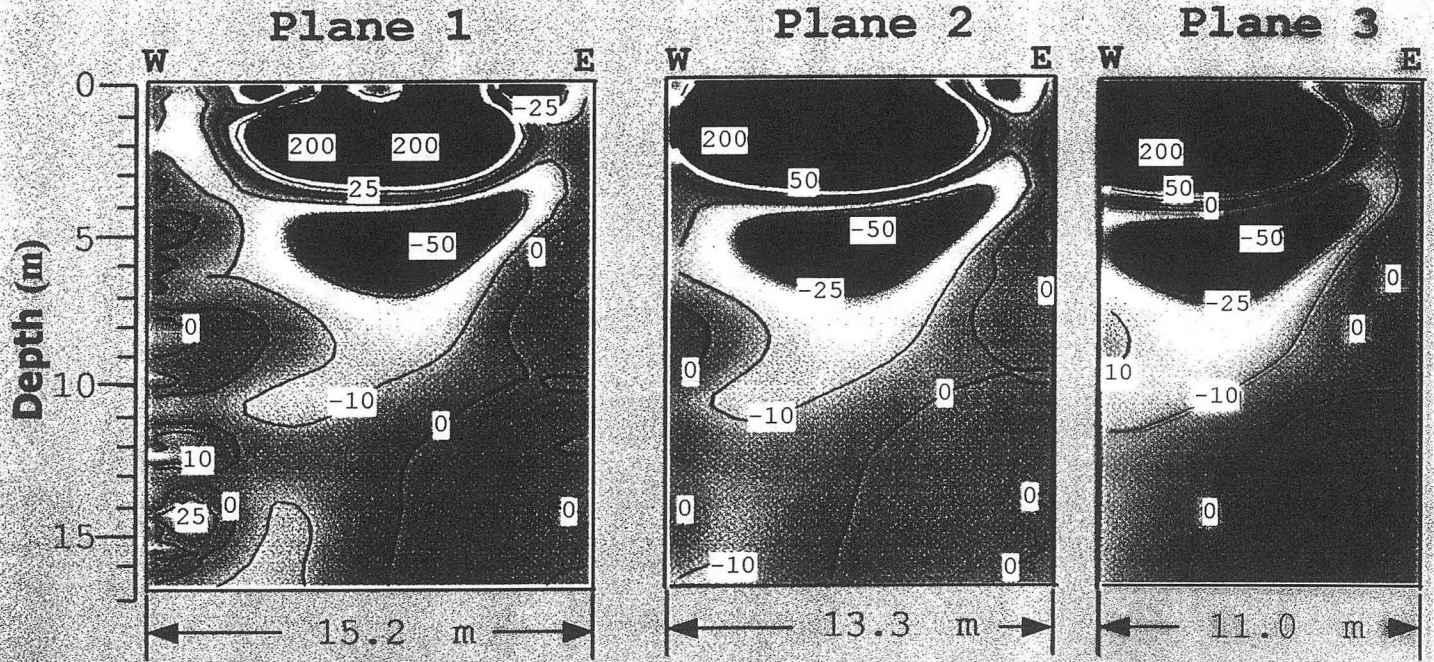
## Percent Difference from 9/11/97 9:00 Hours





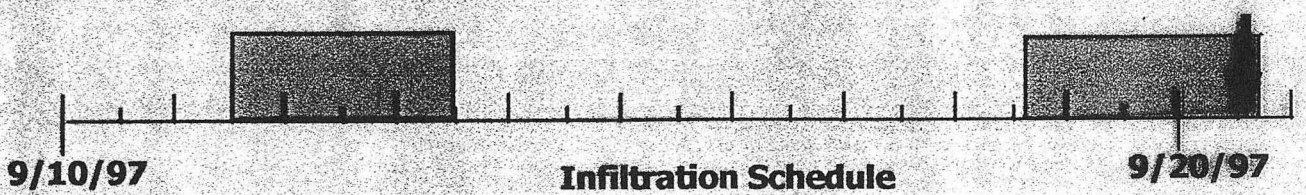
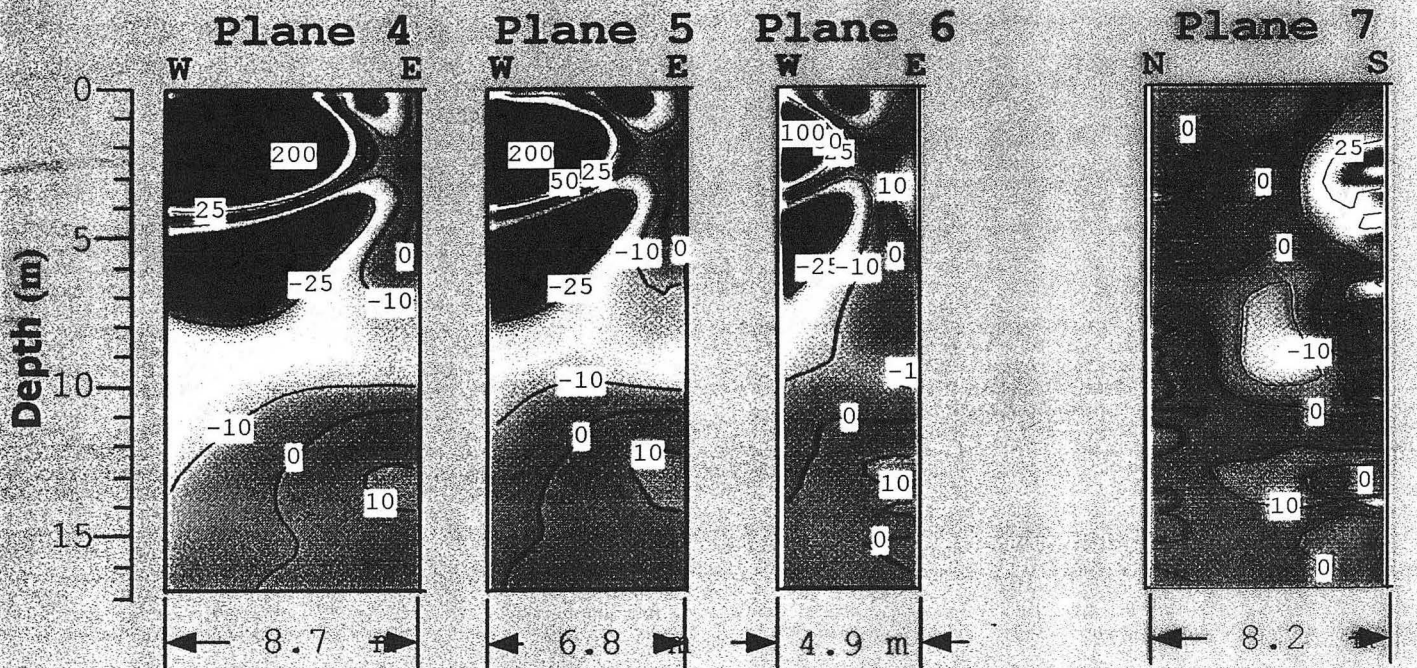
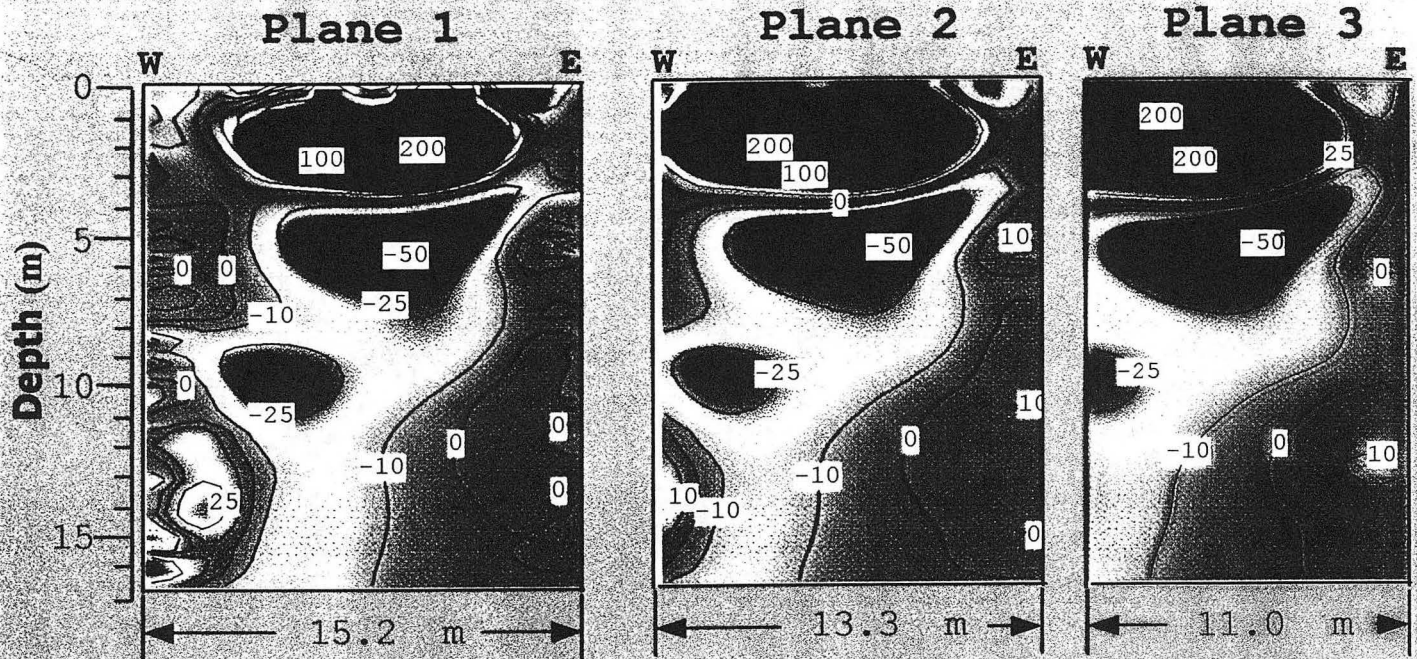
# Outer Survey 9/18/97 18:00 Hours

## Percent Difference from 9/11/97 9:00 Hours



# Outer Survey 9/20/97 14:00 Hours

## Percent Difference from 9/11/97 9:00 Hours



# Conclusions

- Large Scale Survey Results Were Disappointing
  - ◆ Substantial Artifacts Indicate a “Blind Spot” Below the Pond
  - ◆ Observed Changes at Depths Were Small ~10 to 20%
- It is Not Clear if the Changes Are Small or if We Just Missed the Major Flow Paths

INEEL

A Chaotic-Dynamical Conceptual Model  
to Describe Fluid Flow and Contaminant  
Transport in a Fractured Vadose Zone

Outcrop Infiltration Experiments-1997

Project Status

T.R. Wood, Field Team Leader

R.K. Podgorney

T.S. Stoops, Manager

# Outline for Project Status Summary Meeting with DOE-ID 12/2/97

- Purpose and Benefits of Chaos Research
- Achievements of Project To-Date
- Current Project Life-Cycle Status
- Activities Scheduled for FY-98

# Benefits of a Chaotic-Dynamical Model of Flow and Transport in a Fractured Vadose Zone

- Traditional methods and paradigms describe systems in parameters which reflect average behavior - not adequate for complex geometries and time-dependent processes
- New algorithms will improve our ability to determine what is knowable and thus may have a significant impact on regulatory issues
- The system attractor can be used to predict the long-term bounds on fluid flow and transport

# Highlights of INEEL Dynamical-Chaos Project Achievements

- Successful completion of meso-scale fractured rock field test at Hell's Half Acre
- Collection of over 300,000 data points for chaotic analysis
- Observed chaotic behavior in fractured basalt flow
- Papers/Presentations: 2 at GSA; 1 at AGU
- Patent applications:
  - Radial Laser Surveyor
  - Remote Leak Detector
  - Structural Integrity Evaluation System

# A Chaotic-Dynamical Conceptual Model to Describe Fluid Flow and Contaminant Transport in a Fractured Vadose Zone

Outcrop Infiltration Experiments-1997

R.K. Podgorney

T.S. Stoops, Manager

T.R. Wood, Team Leader

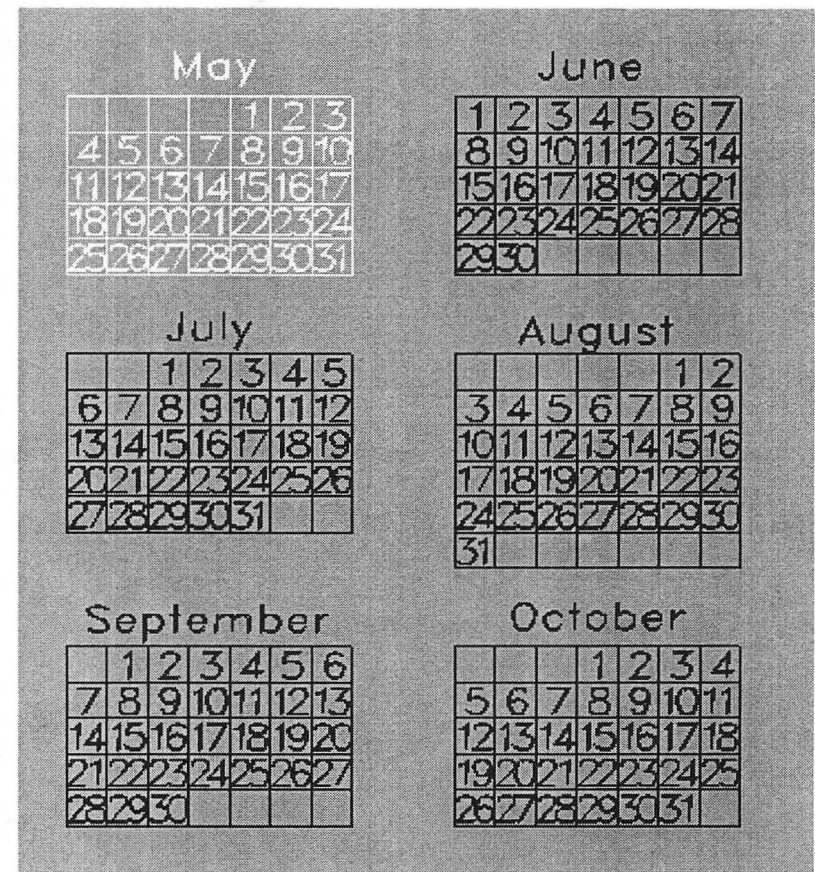


# Objectives

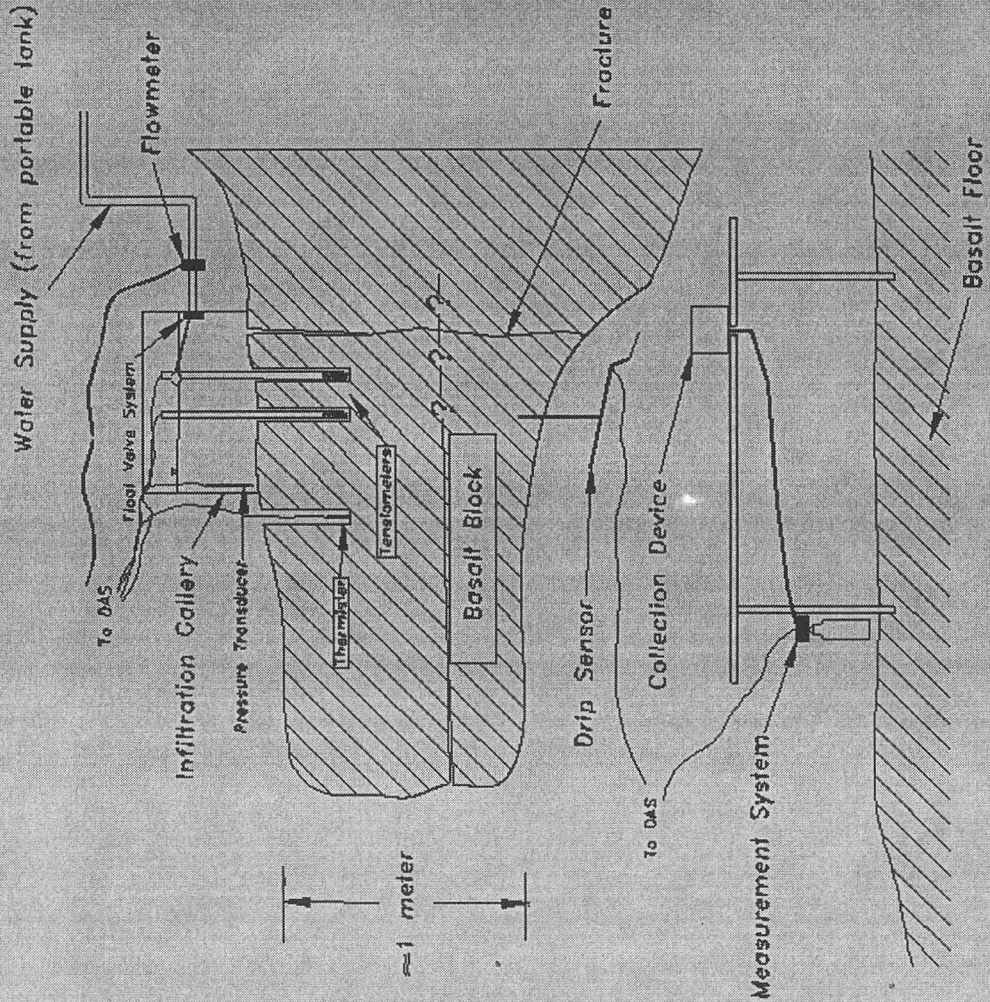
- Quantify hydraulic properties of fractures at the scale of investigation of approximately 1 meter
- Collect datasets which can be analyzed in a chaotic-dynamical fashion
  - Drip interval
  - Tension time series
  - Temporal and spatial variation of outflow
- Provide analogous dataset to previous chaotic analysis (e.g., Shaw, 1984)
- Determine if an attractor exists that describes the behavior of the system

# Overview of Activities

- Test Conceptualization
- Instrument Development
- Site Selection
- Site Preparation
- Test Execution
- Data Reductions and Dissemination
- Data Analysis



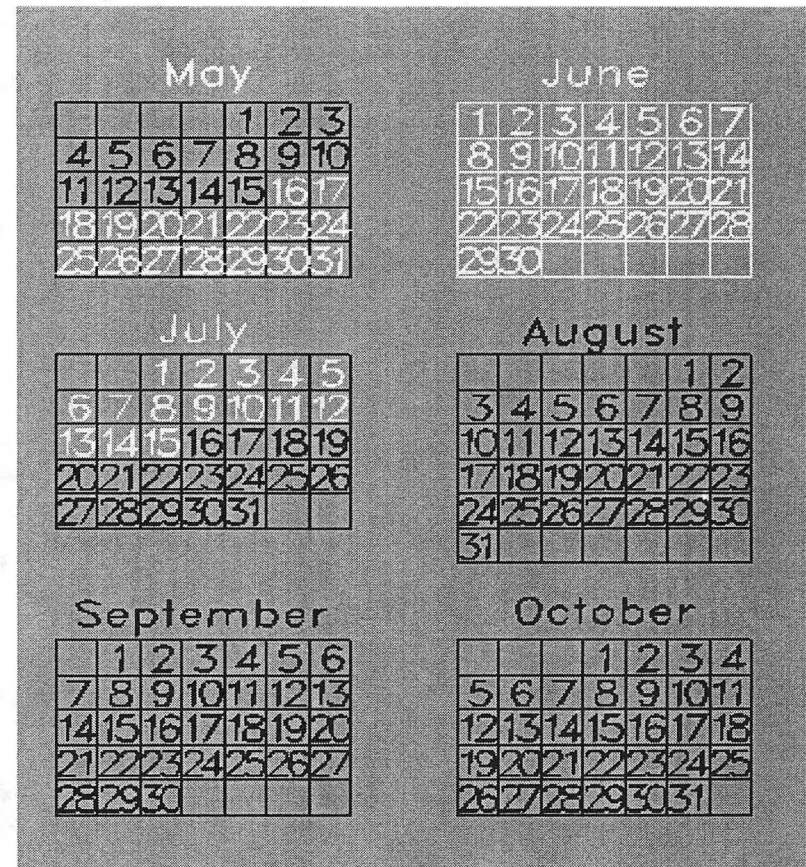
# Conceptual Diagram

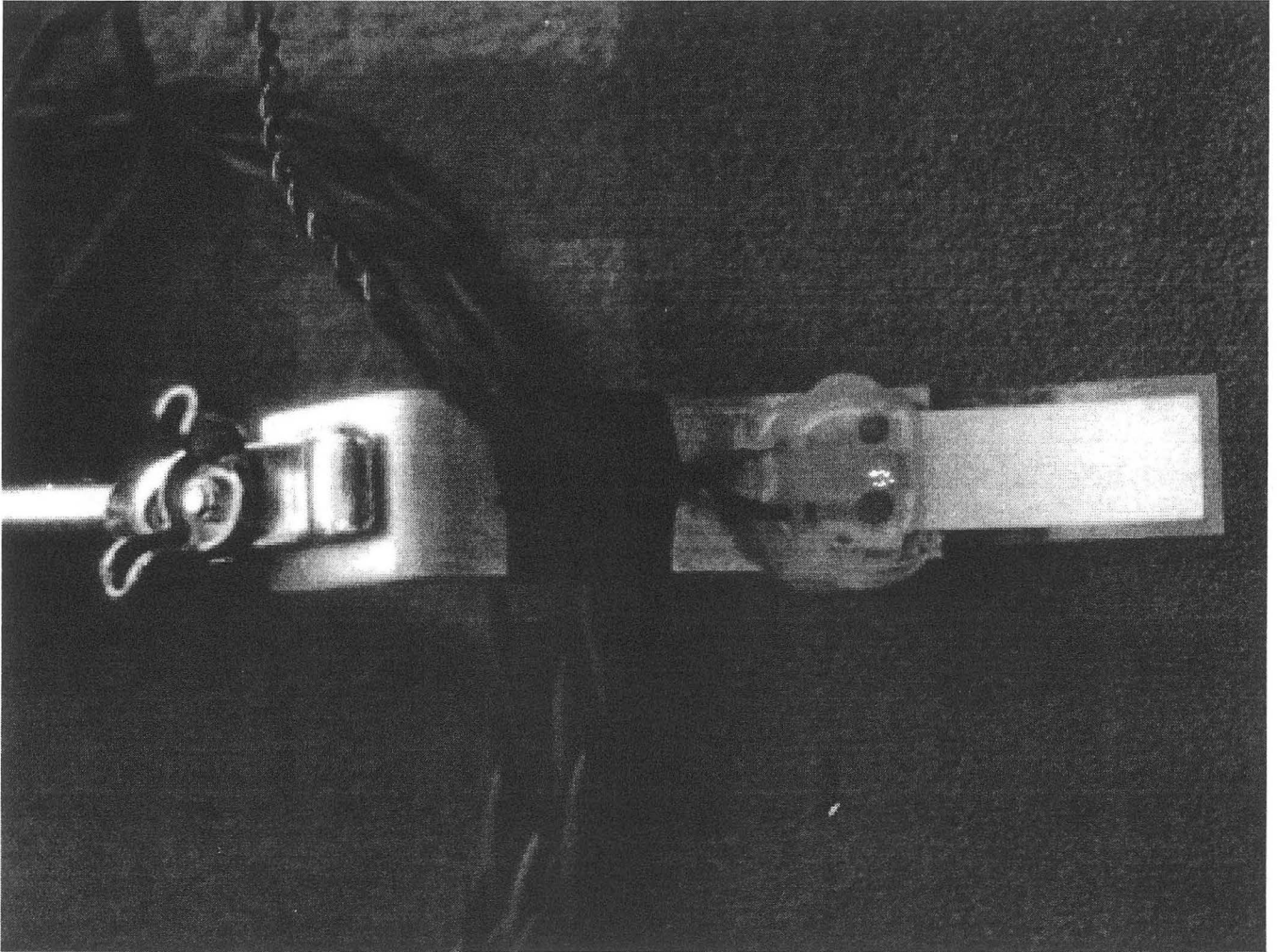


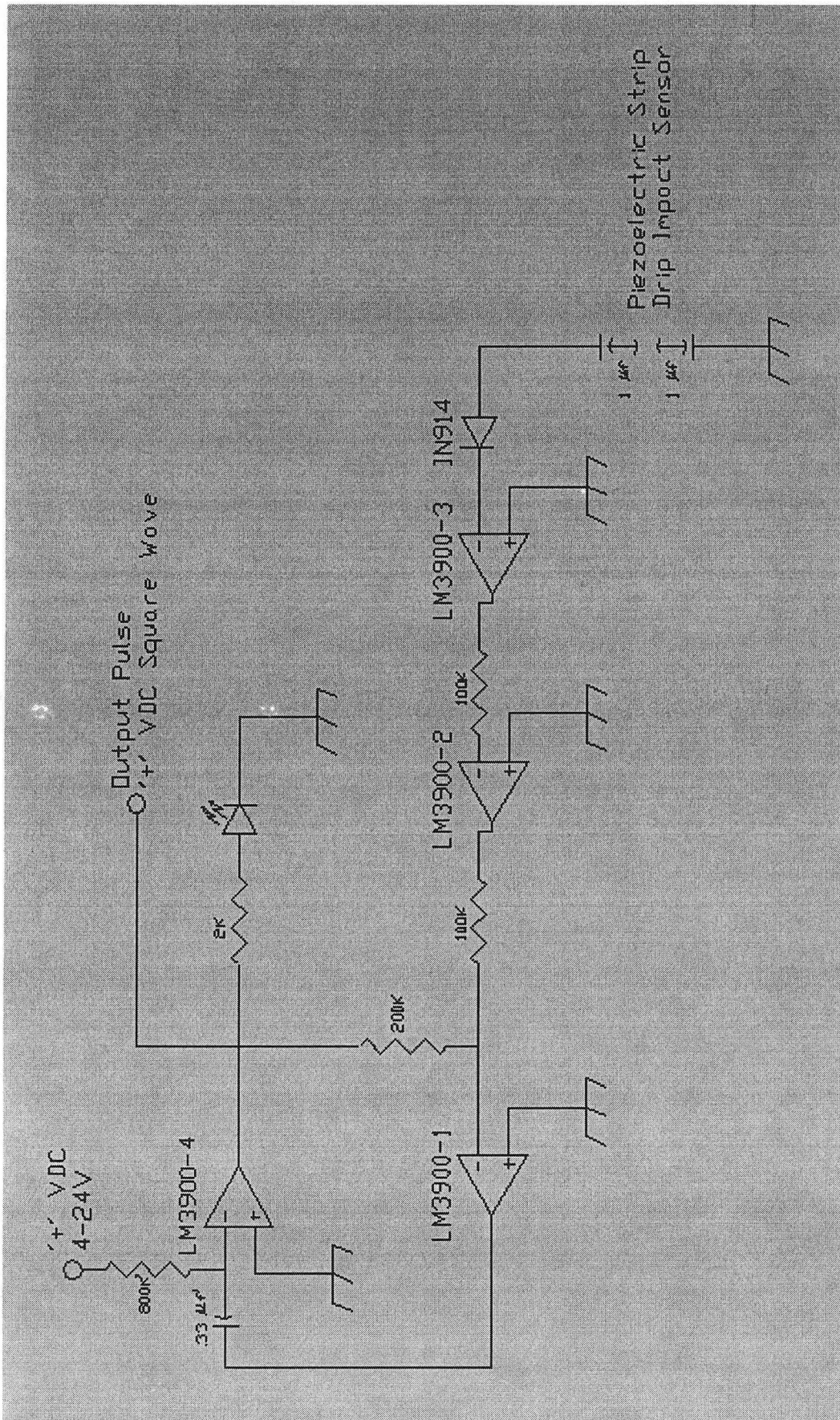
Note: Not to scale.

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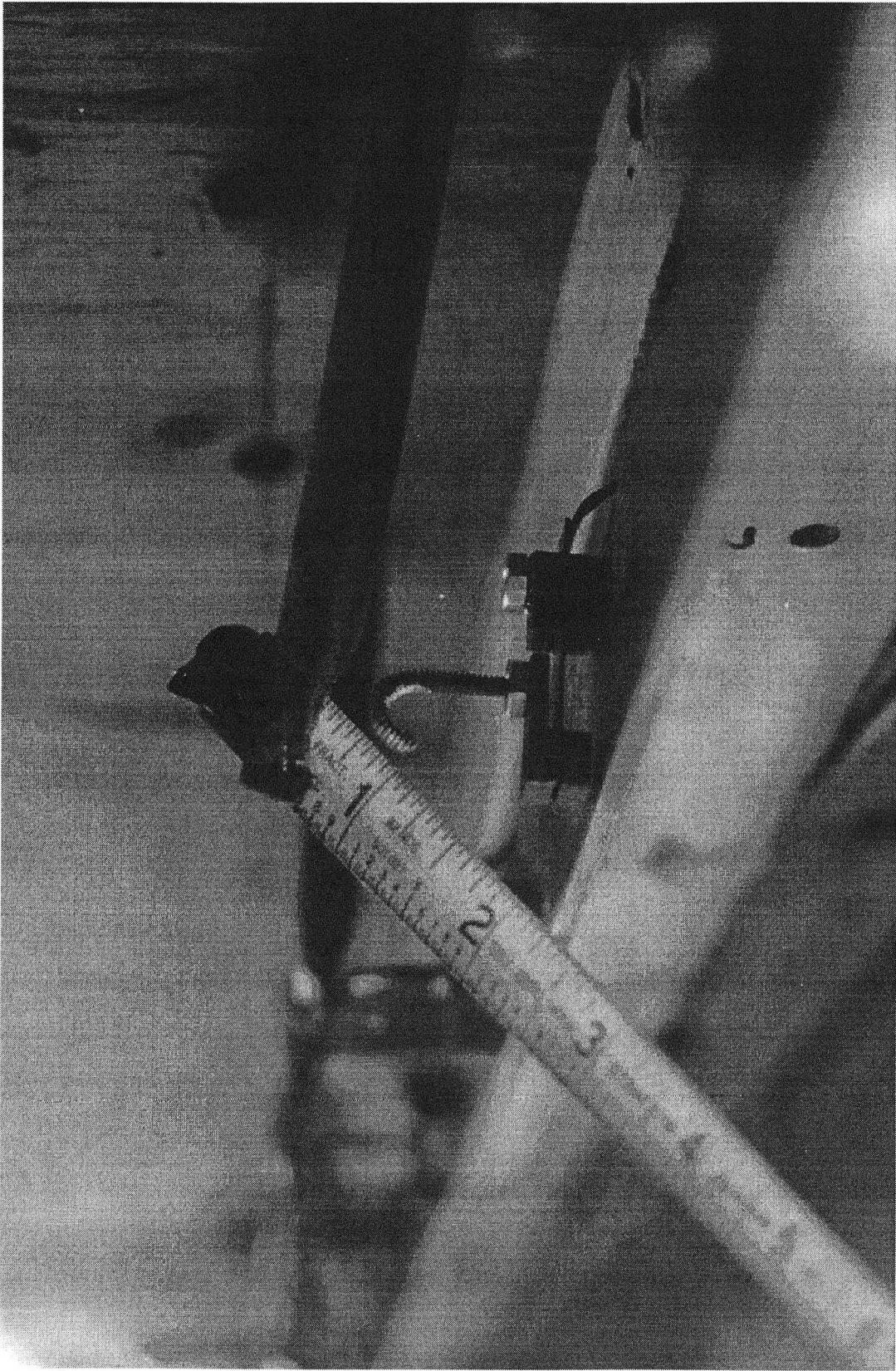






Piezoelectric Strip  
Drip Impact Sensor

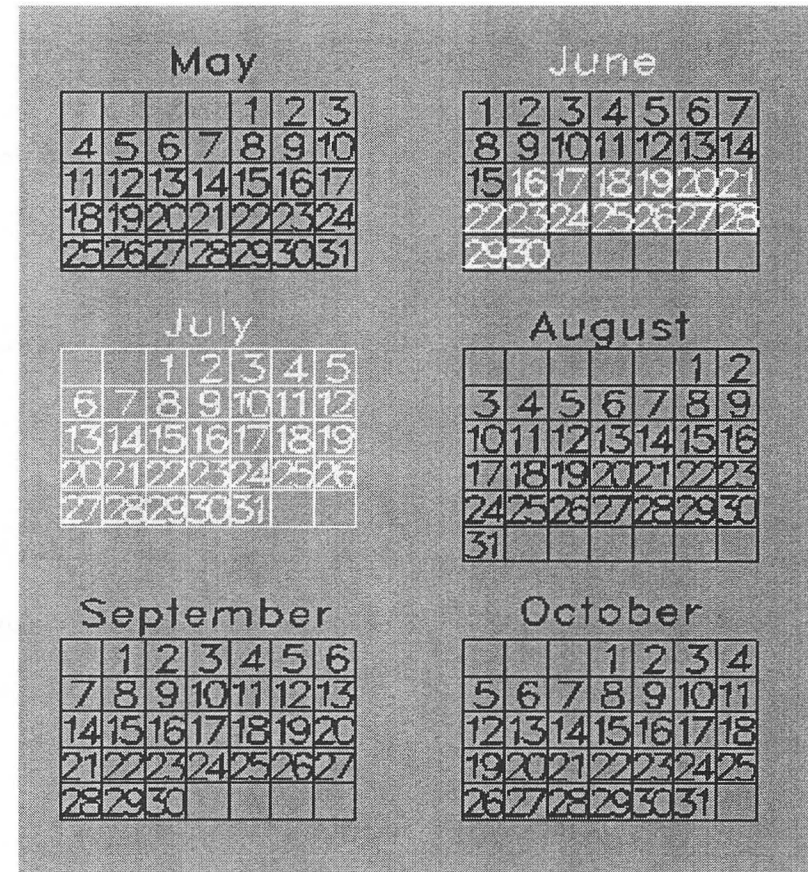


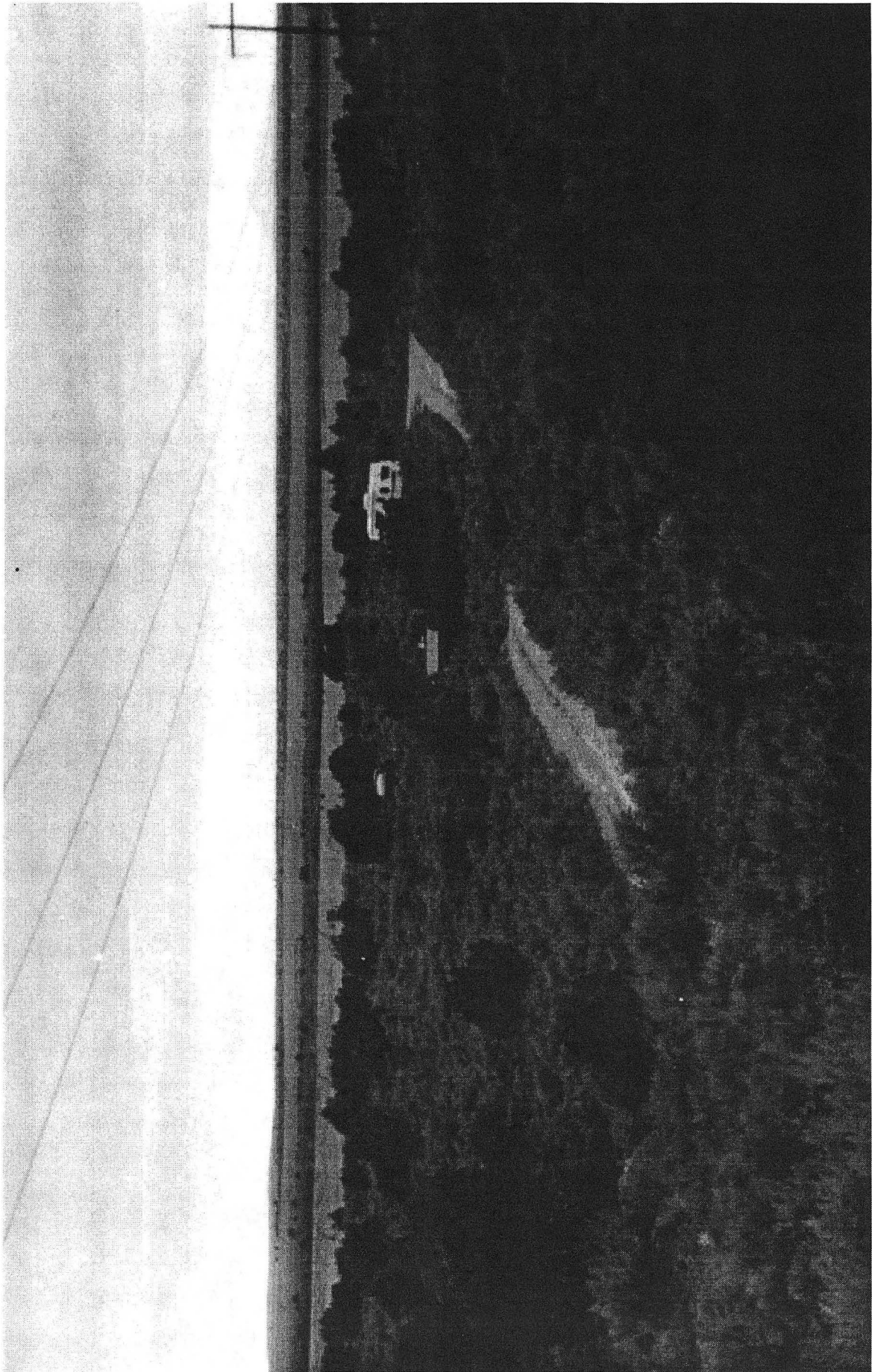


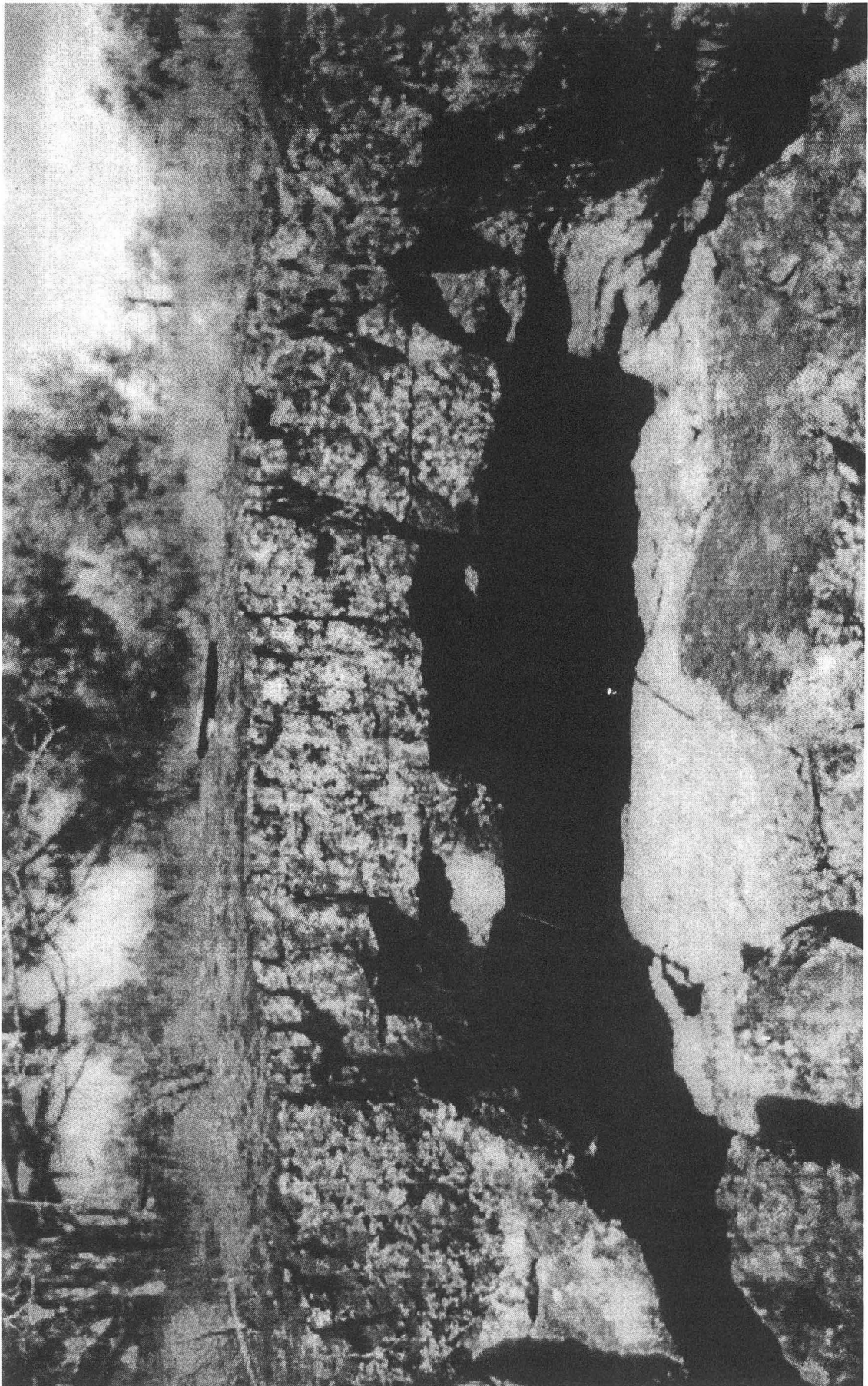


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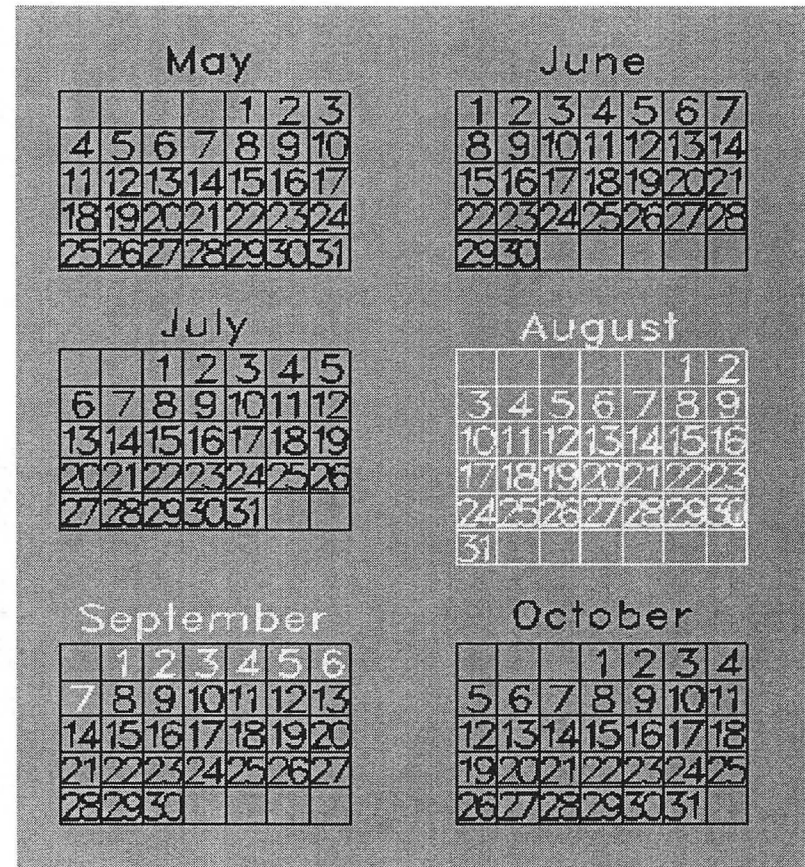


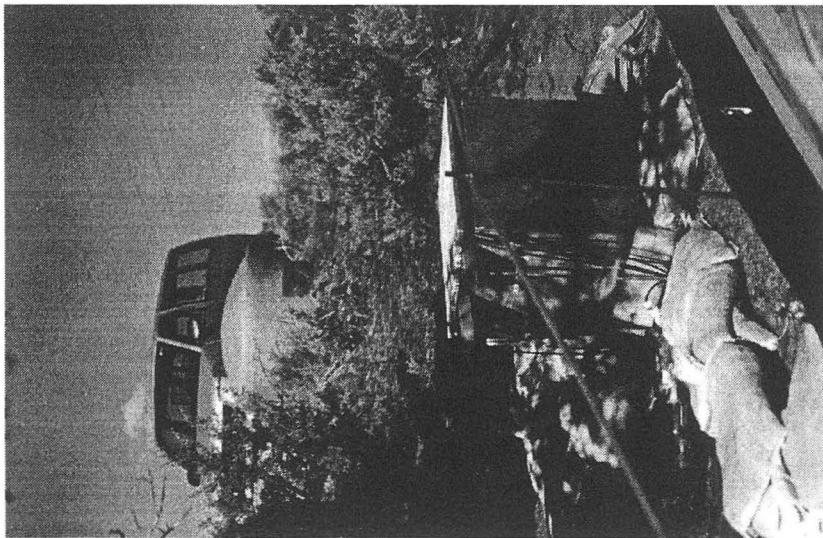
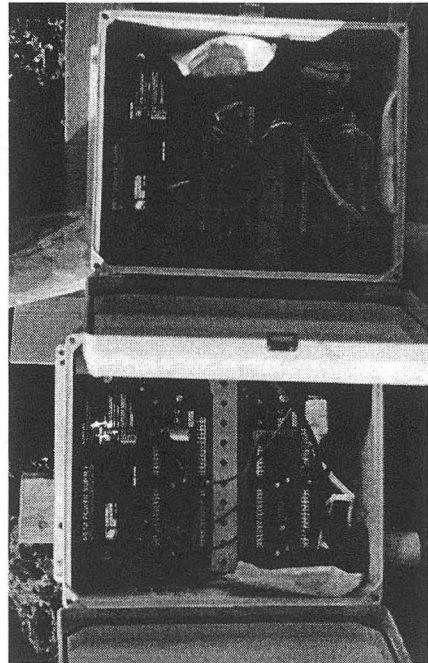
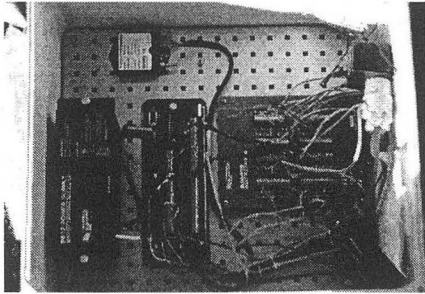
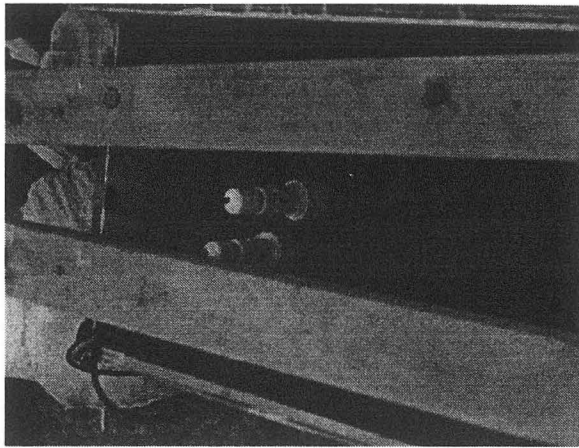




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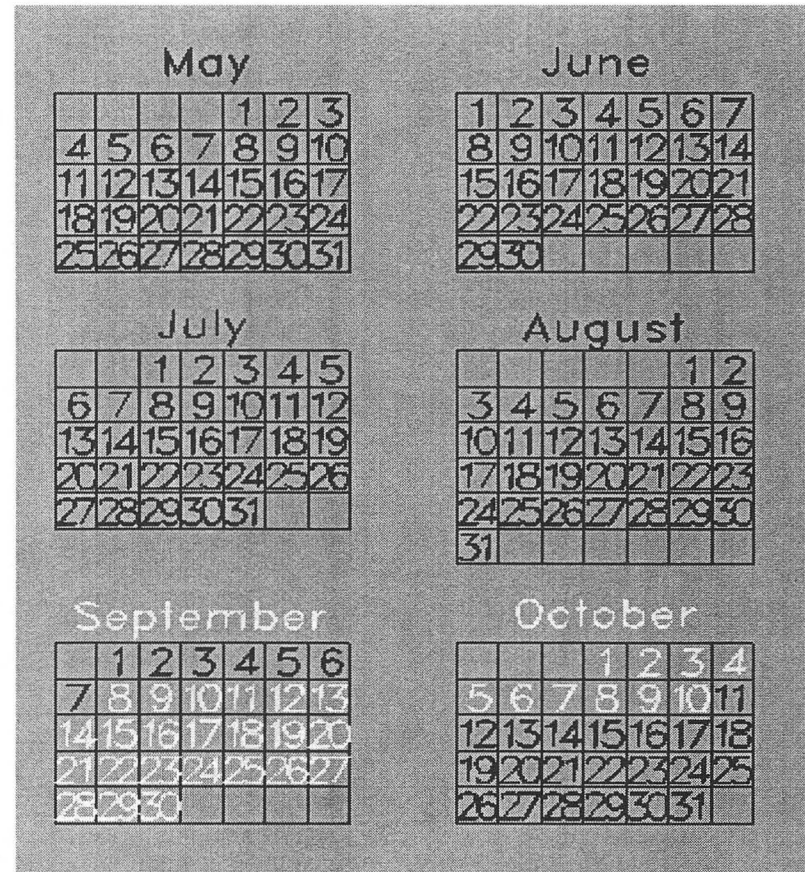


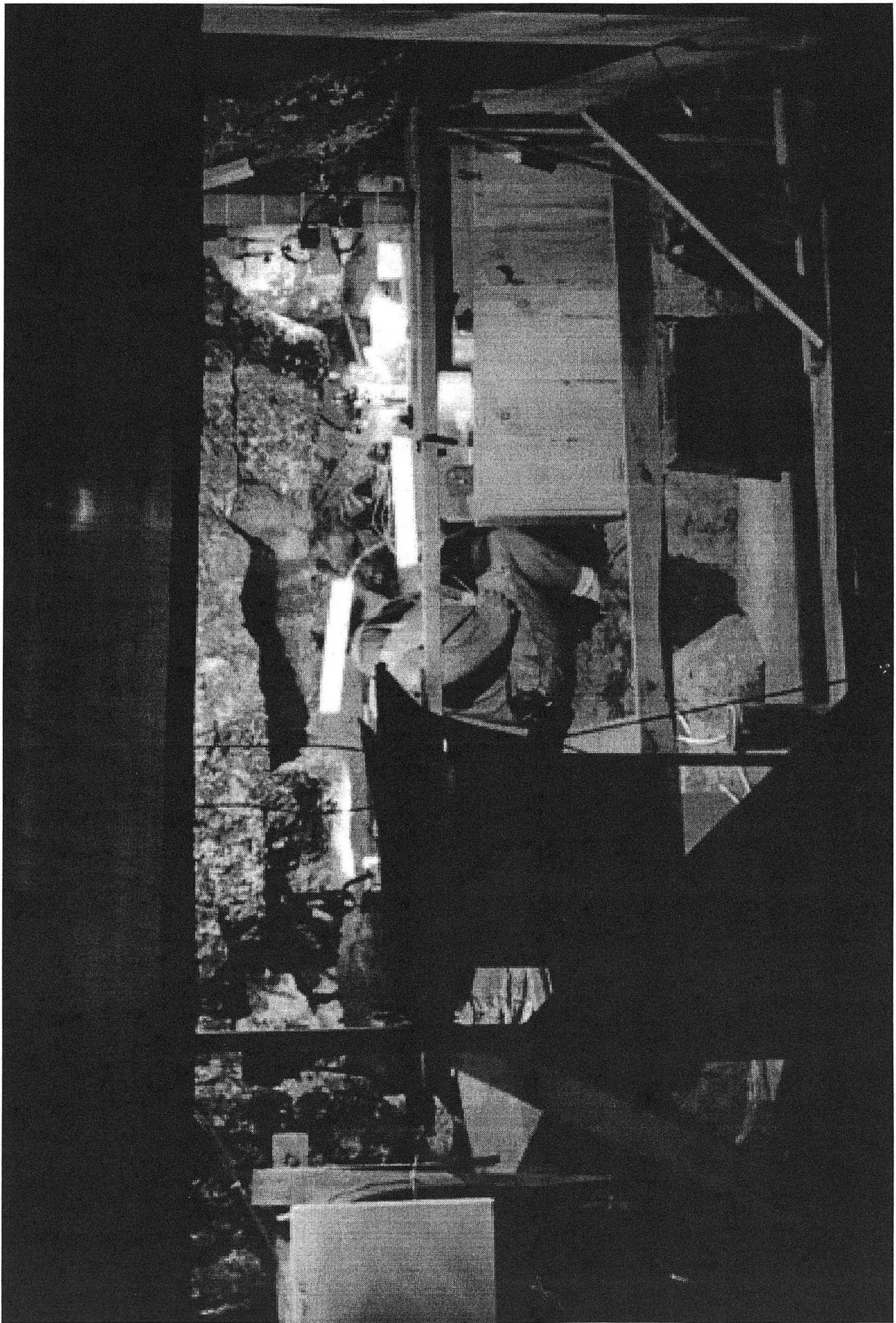




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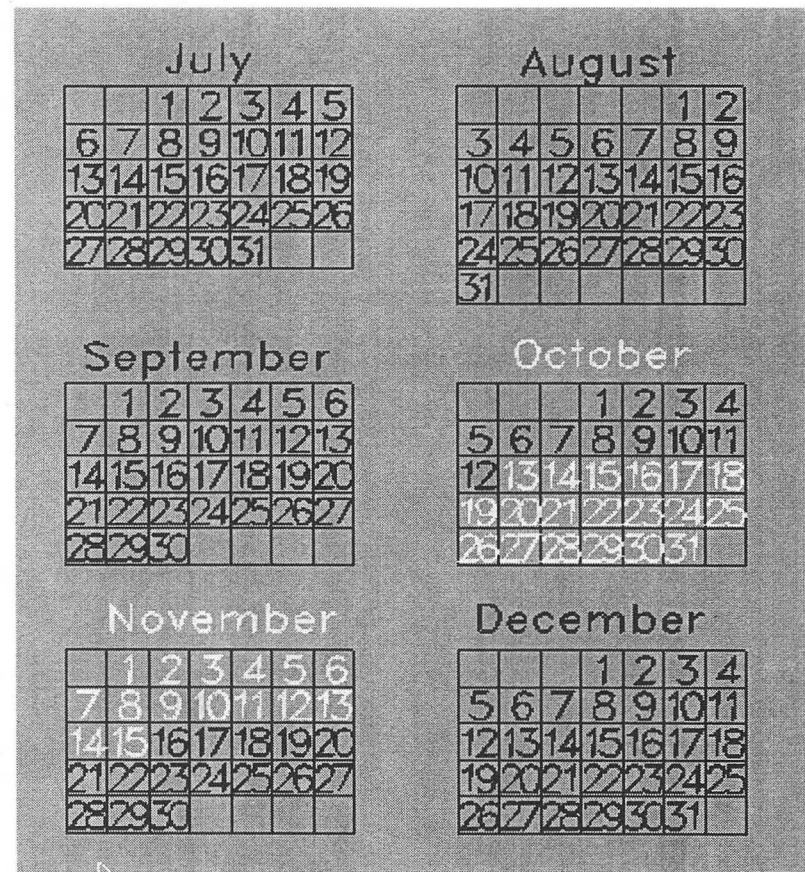




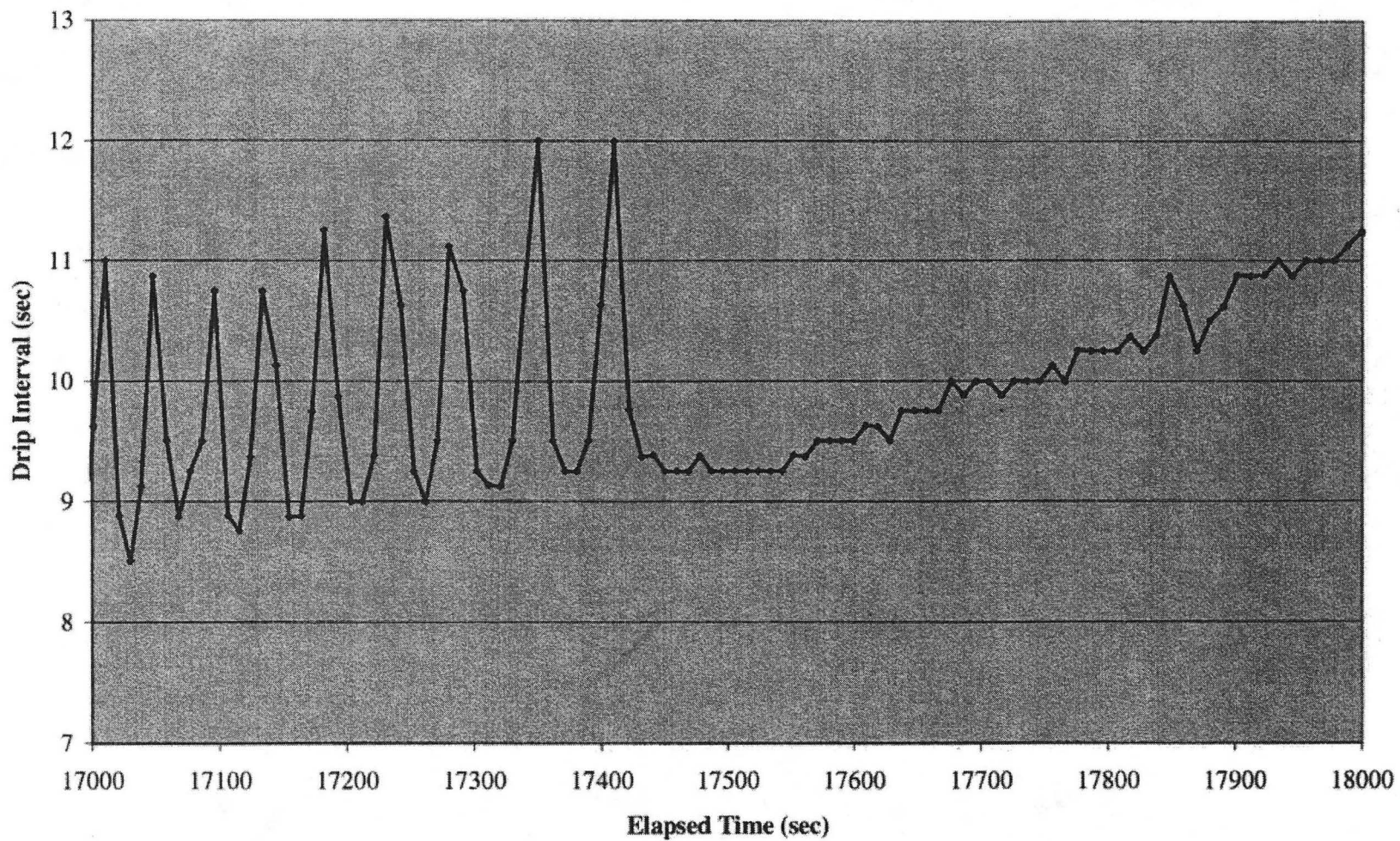


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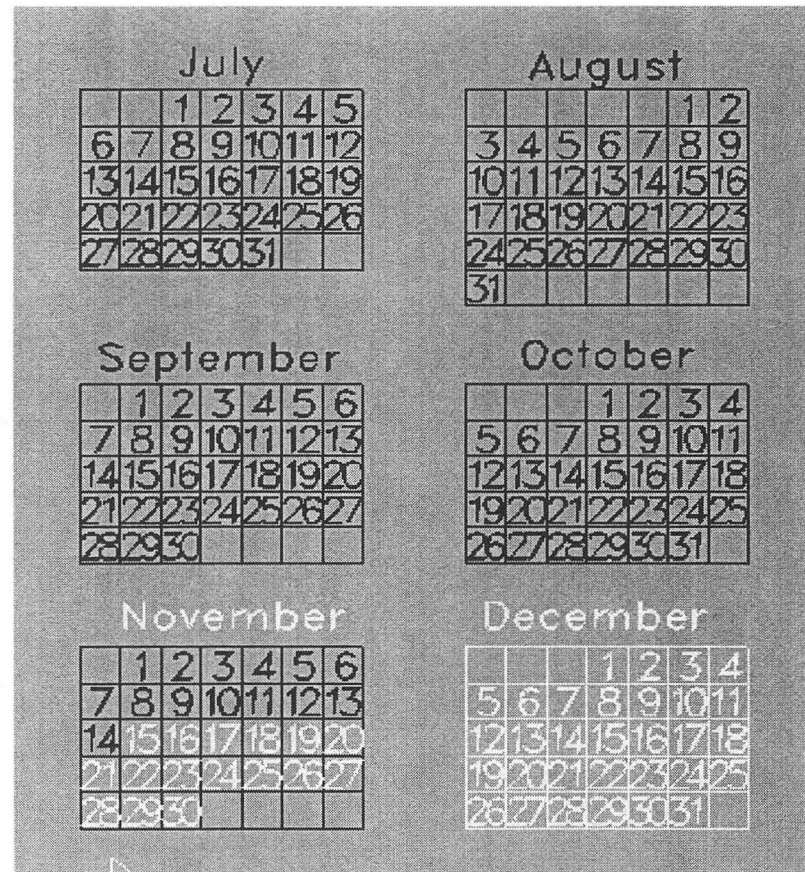


### Drip Interval, Test 3, Location 7

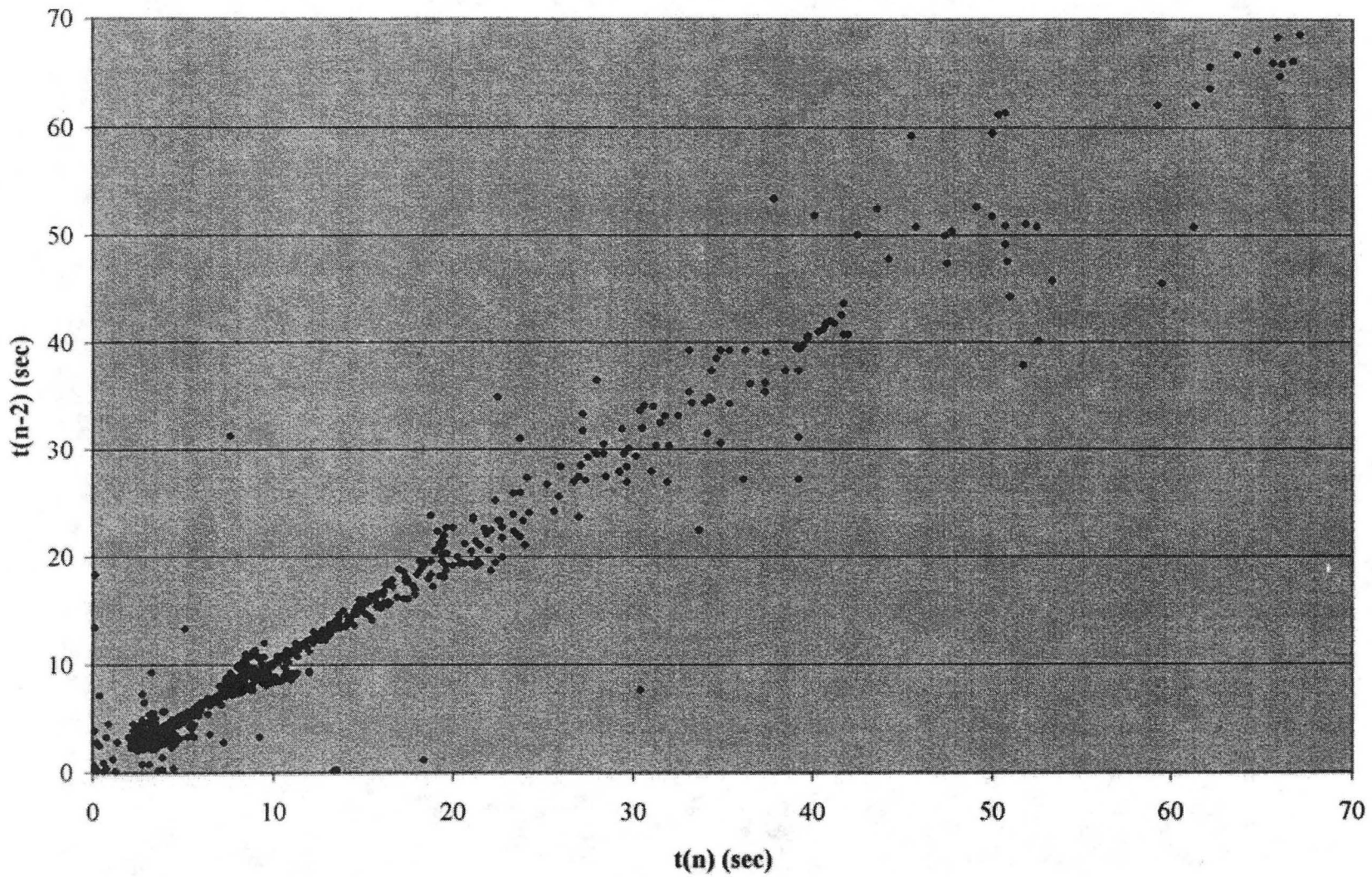


# Overview of Activities

- Test Conceptualization
- Instrument Development
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- Data Reductions and Dissemination
- Data Analysis



**Pseudo-Phase Space Map  
Test 3, Drip Location 7**





# Dynamical-Chaos is Currently in its second year

- First year activities were focused on collecting a data set of sufficient size and quality to perform chaotic analysis
- Second year will analyze data and focus and refine equipment and approach for second year of intermediate scale testing in fractured basalt
- Third year of project will build ties from the micro-, meso- and macro-scale for full scale

# FY-98 Scheduled Activities

- Team meeting December 3-5 to summarize results of summer field work
- Winter of 1998 will focus on data analysis and development of instruments for measuring in moisture movement in fractures
- Summer 1998 will focus again on meso-scale testing at Hell's Half Acre (new site(s) and monitoring equipment

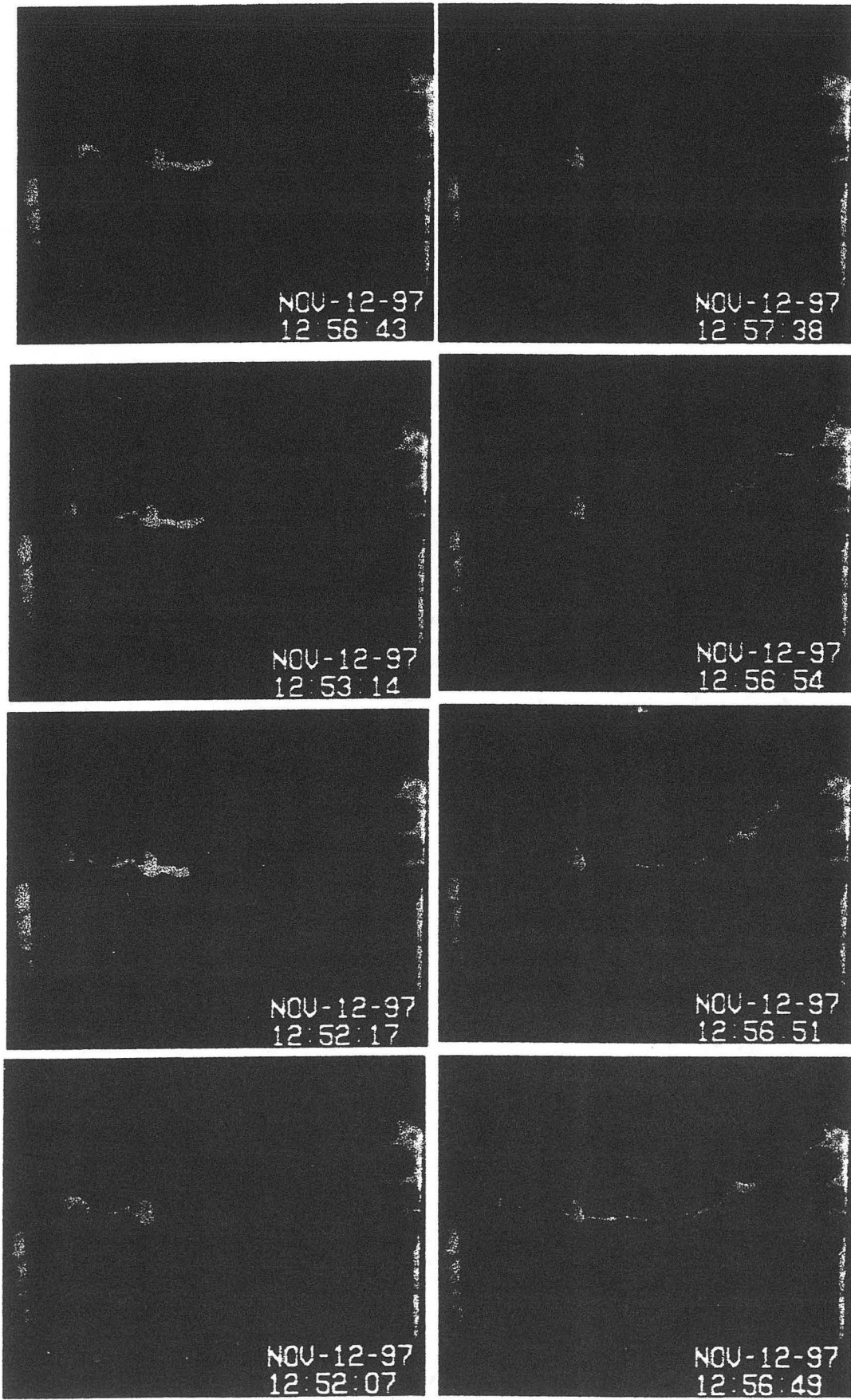
# II.5

## Laboratory Studies

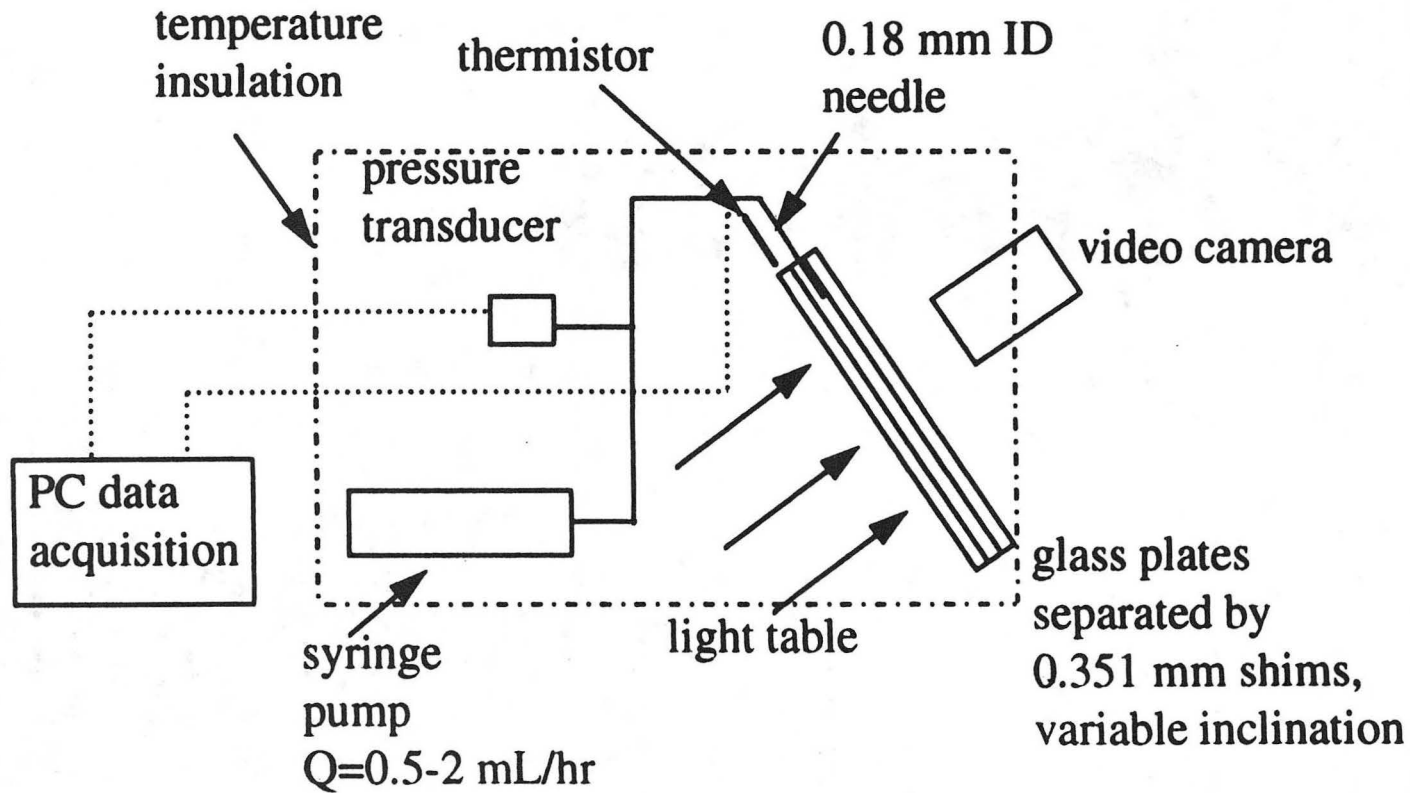
Jil Geller & Sharon Borglin

- Consider drips in parallel plates as an analog to water seepage in fractures
- Extension of the “dripping faucet” model to drips in parallel plates under influence of capillary forces
- Obtain records of the pressure signal to monitor drip behavior
- Vary flow rates, surface texture and angle of inclination

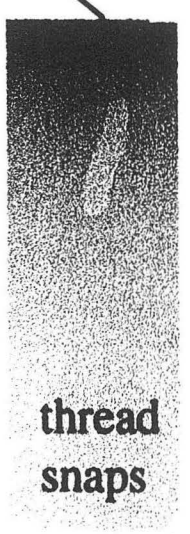
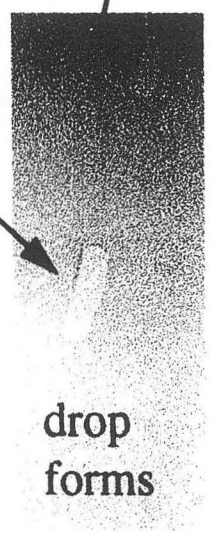
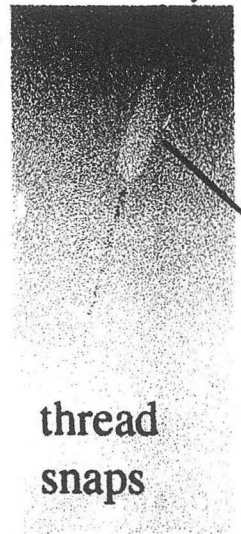
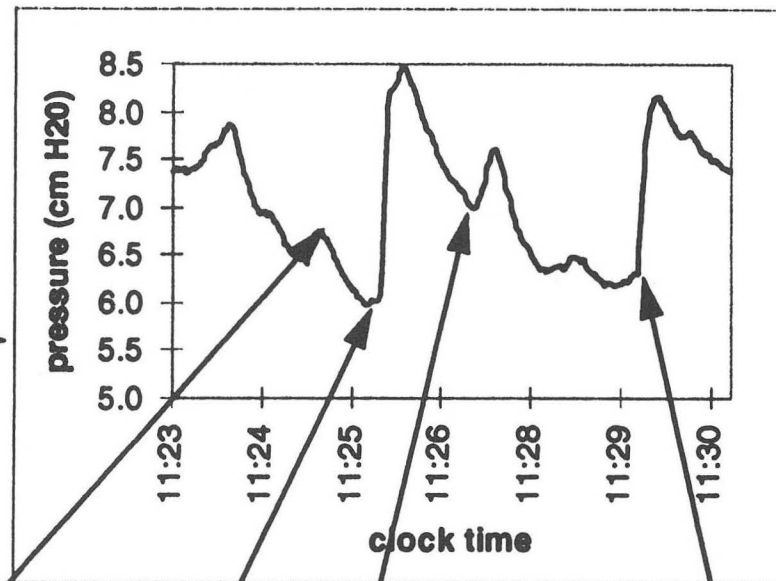
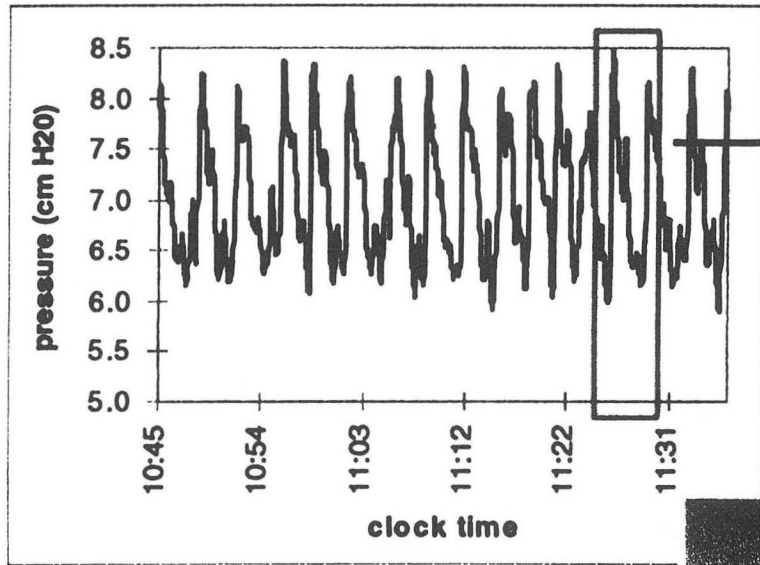




# Behavior of Dripping Water in Parallel Plates



# Use of Pressure Record as Indicator of Drip Behavior



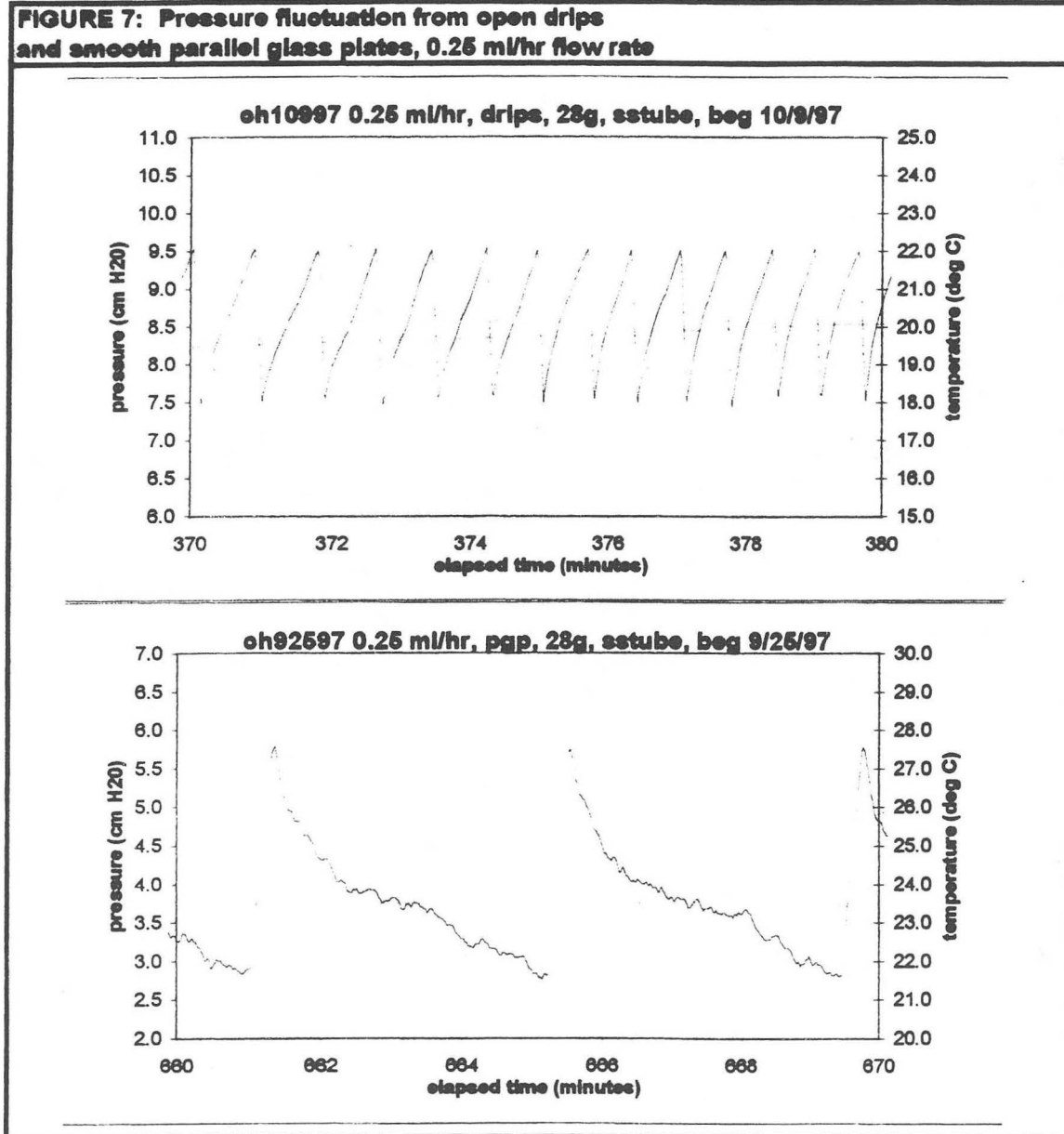
## Record of Experiments

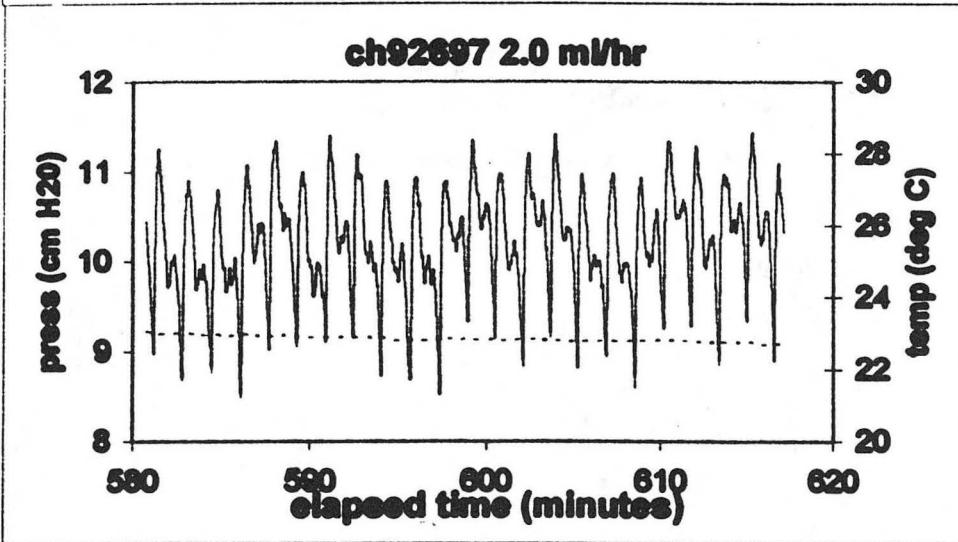
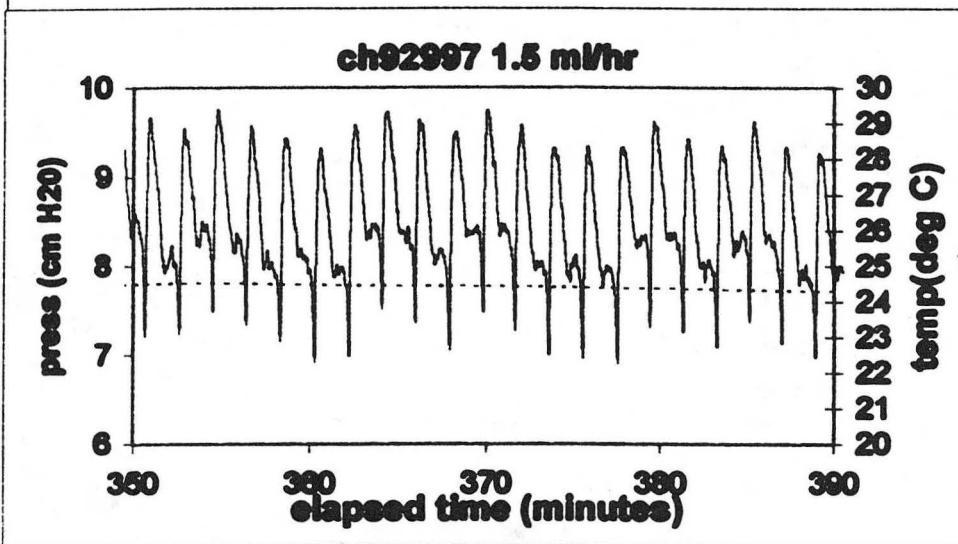
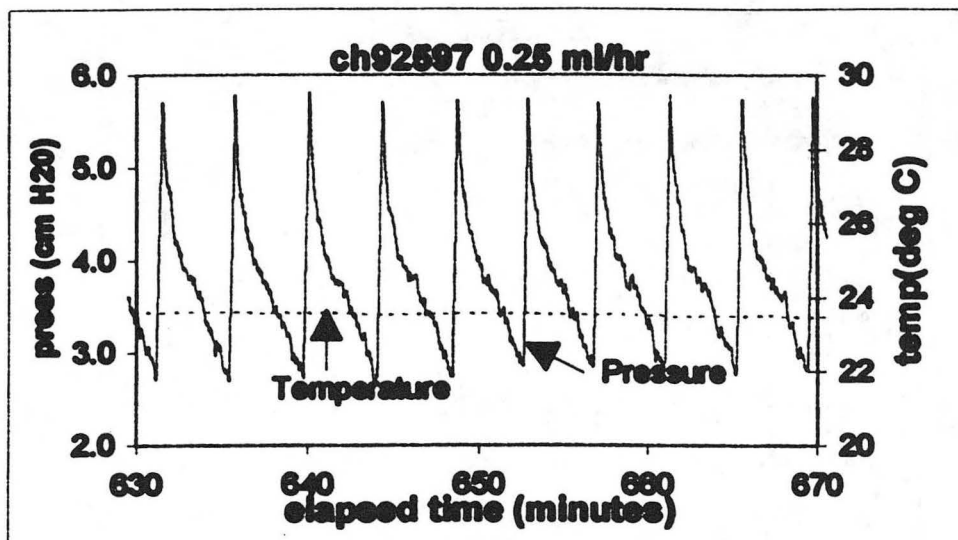
Smooth Parallel Plates			Open Drips		
date	flowrate (mL/hr)	estimated # snaps	date	flowrate (mL/hr)	estimated # snaps
6/4/97 <sup>#</sup>	0.5	676	6/18/97	1	1133
6/5/97	0.5	648	6/20/97	0.5	3823
6/7/97	1	853	10/9/97	0.25	1403
6/7/97	0.5	512	Obscure Glass Plates		
9/5/97*	2	109	date	flowrate (mL/hr)	estimated # snaps
9/5/97	1	93	7/29/97*	0.5	448
9/8/97	0.5	49	7/30/97	0.5	433
9/9/97	1	202	7/31/97	0.5	544
9/11/97	1	233	8/25/97	0.25	186
9/22/97*	1	112	Baseline		
9/23/97	1	584	date	flowrate (mL/hr)	
9/24/97	0.5	636	10/7/97	1.5	
9/25/97 <sup>#</sup>	0.25	406	10/8/97	0.5	
9/26/97 <sup>#</sup>	2	659	10/8/97	1	
9/29/97	1.5	440	10/9/97	2	
9/30/97	3	512	10/9/97	3	
10/6/97	1	148	10/9/97	0.25	
10/7/97 <sup>#</sup>	1.5	150			

\*initially dry plates

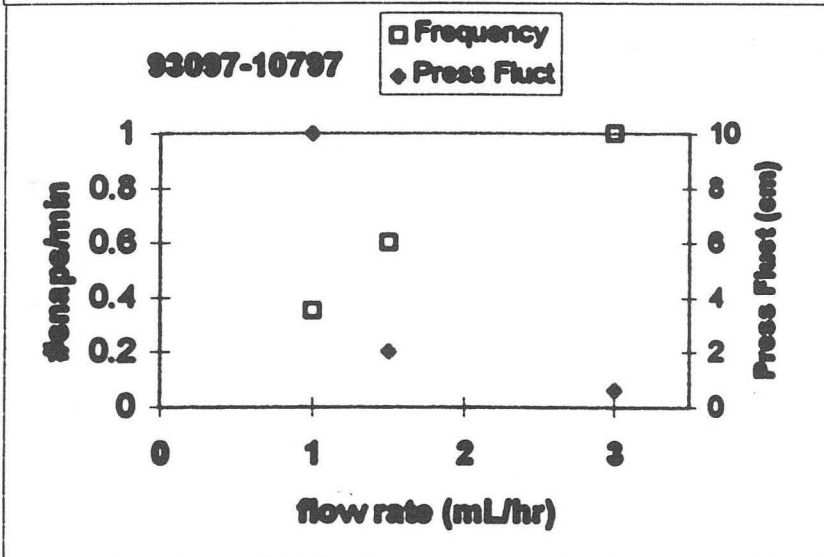
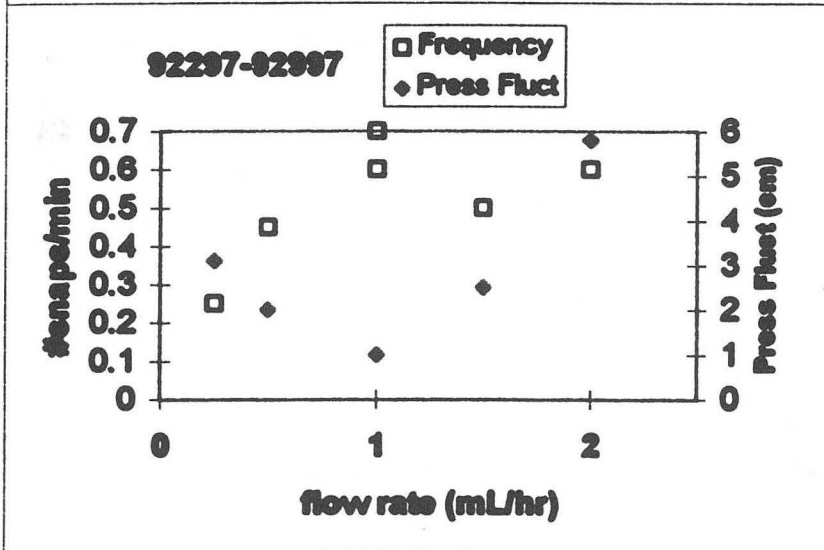
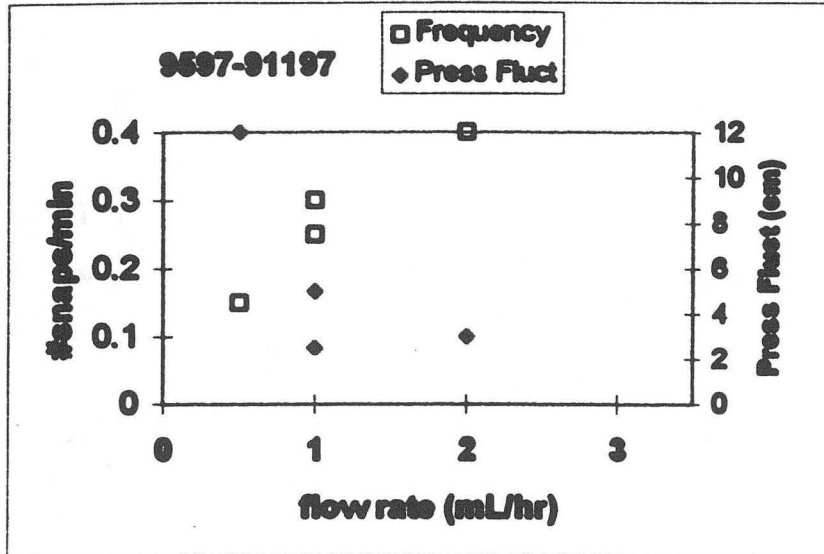
<sup>#</sup> video taped

**FIGURE 7: Pressure fluctuation from open drips and smooth parallel glass plates, 0.25 ml/hr flow rate**

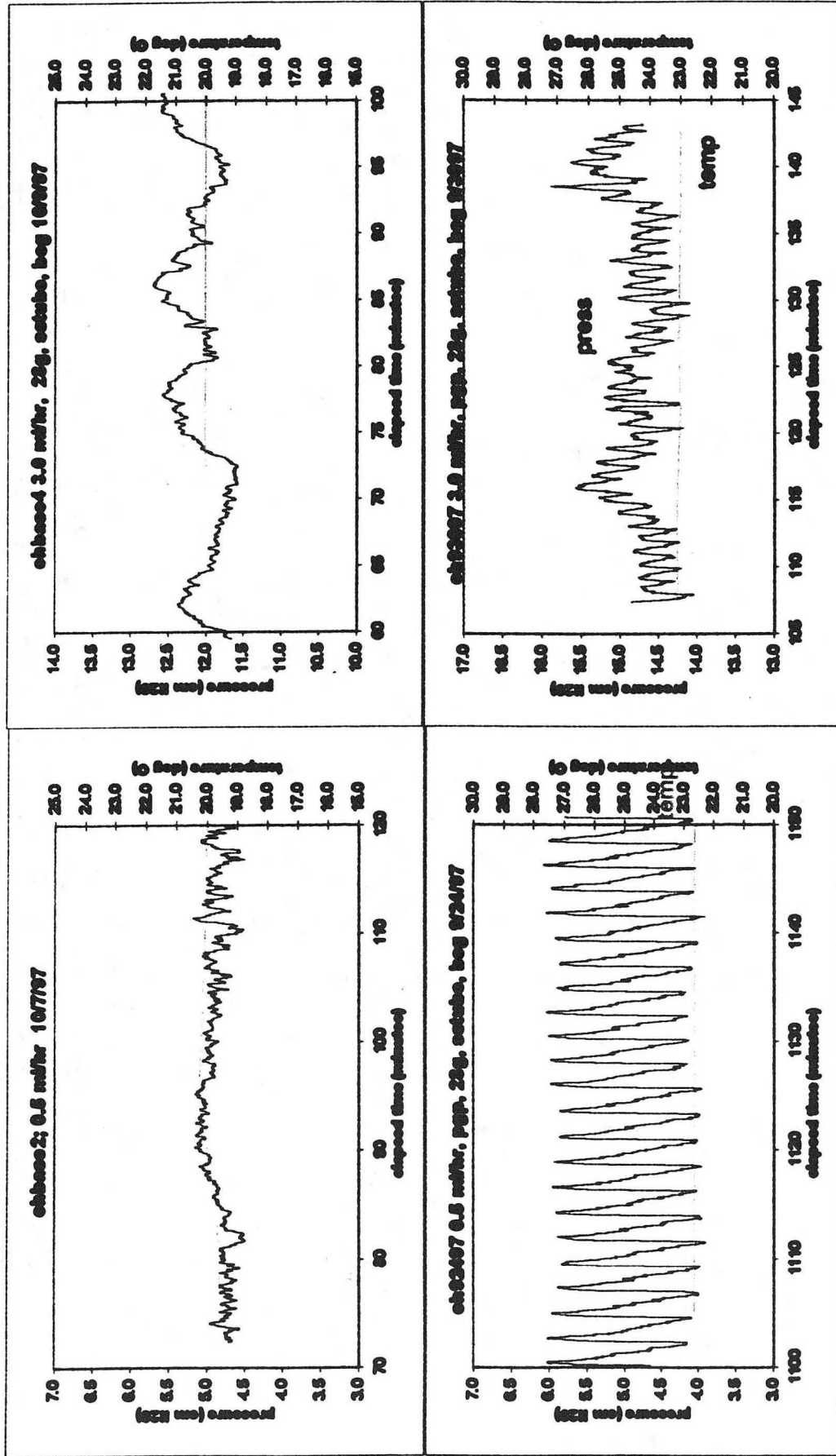




**Smooth Parallel Glass Plates**



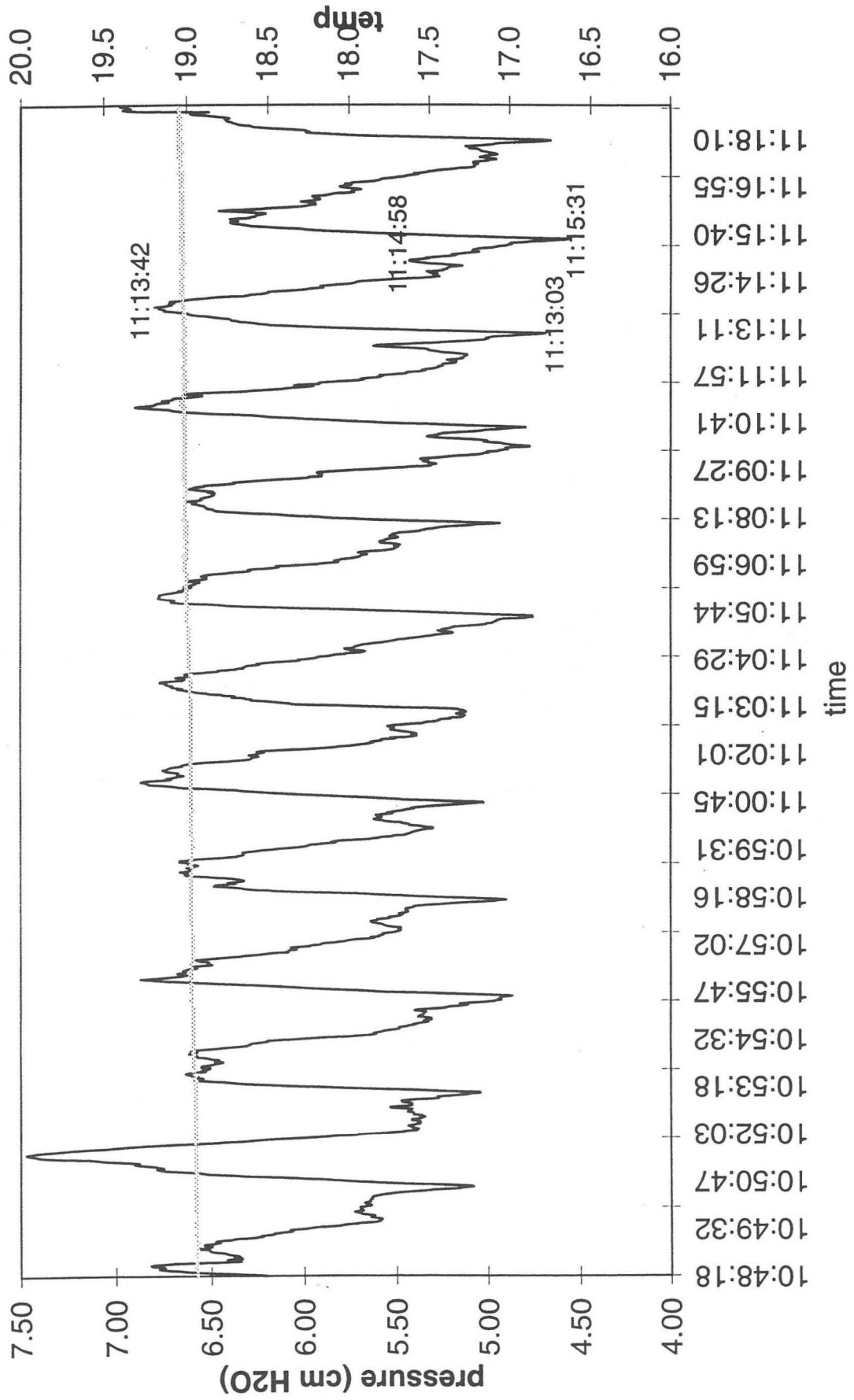
**FIGURE 9: Comparison of baseline to drip data for two flowrates**

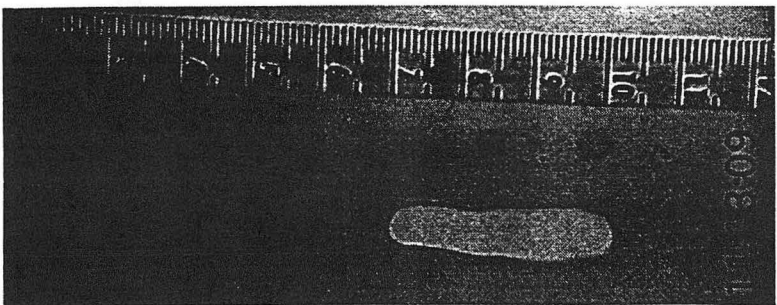
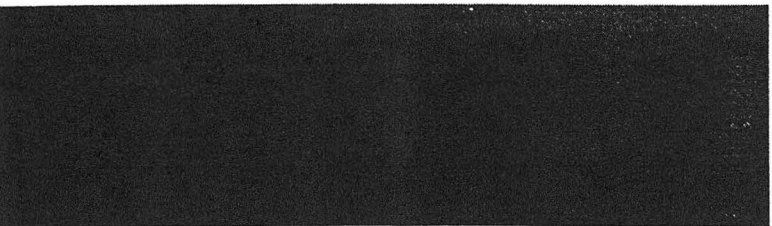
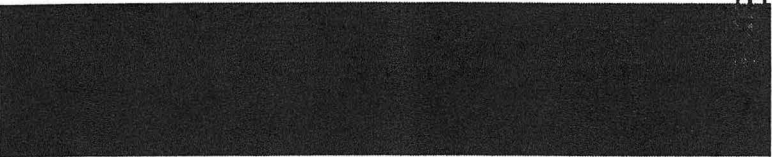
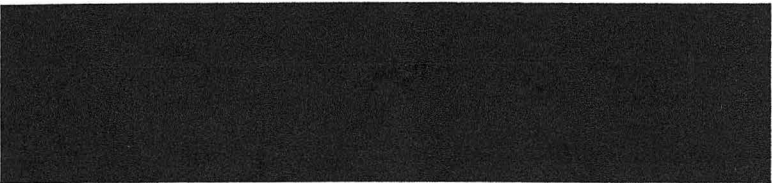
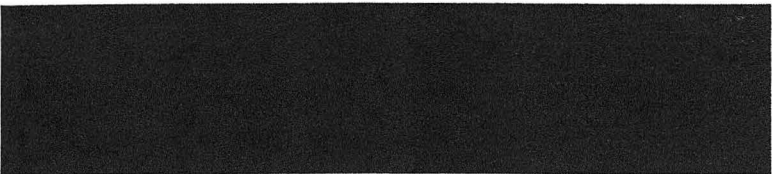
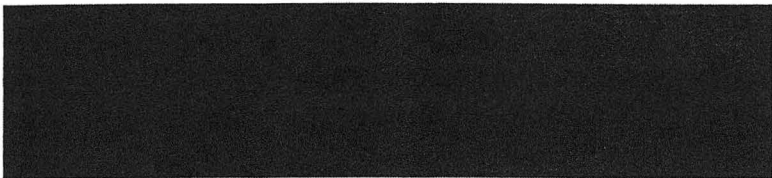
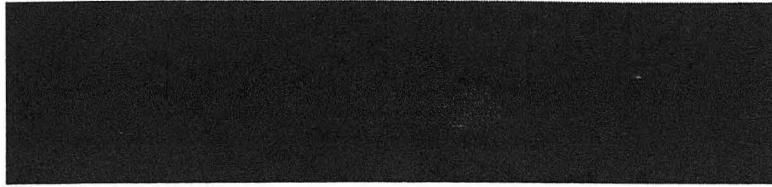
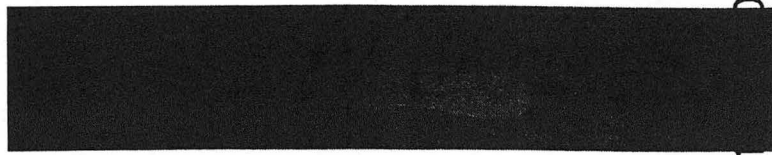




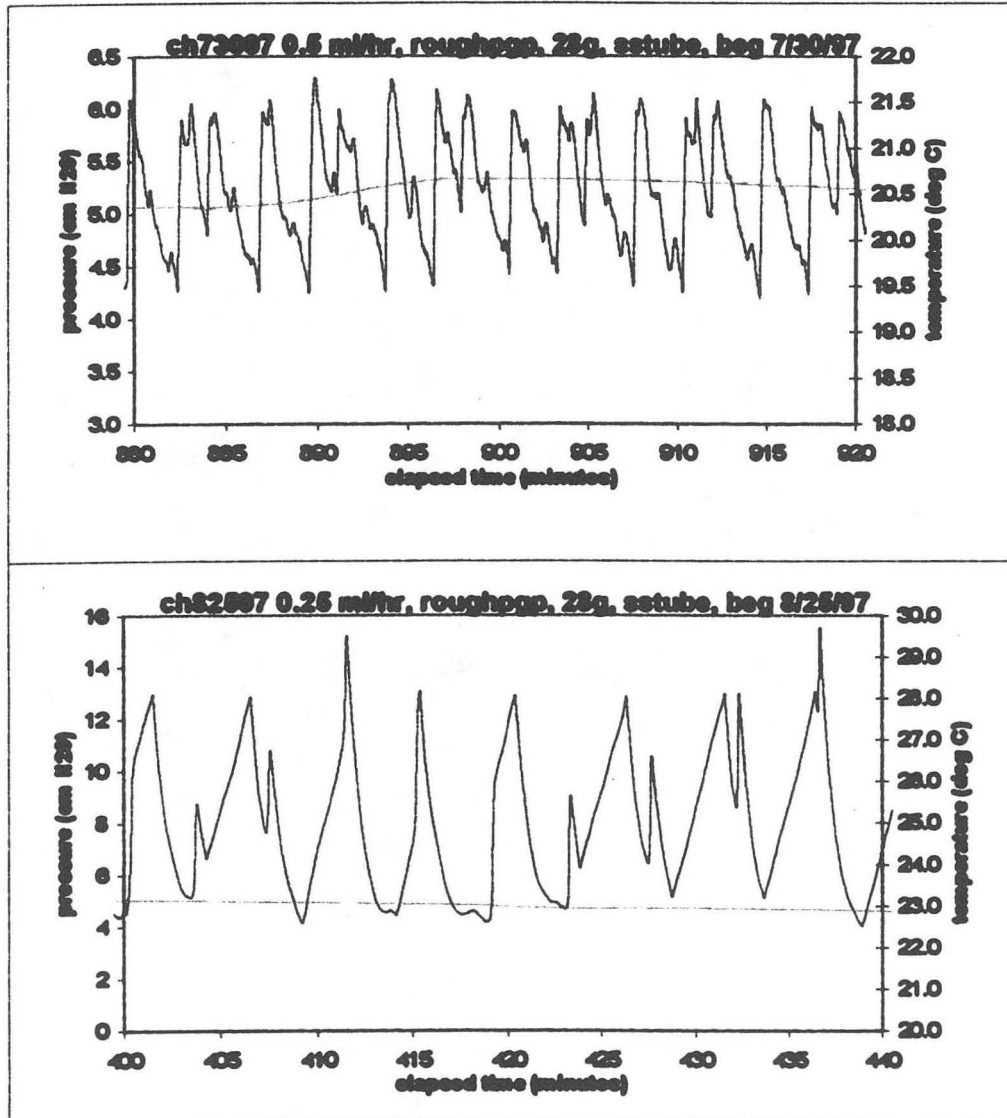
ch10/7/97 1.5 mL/hr

— press  
..... temp





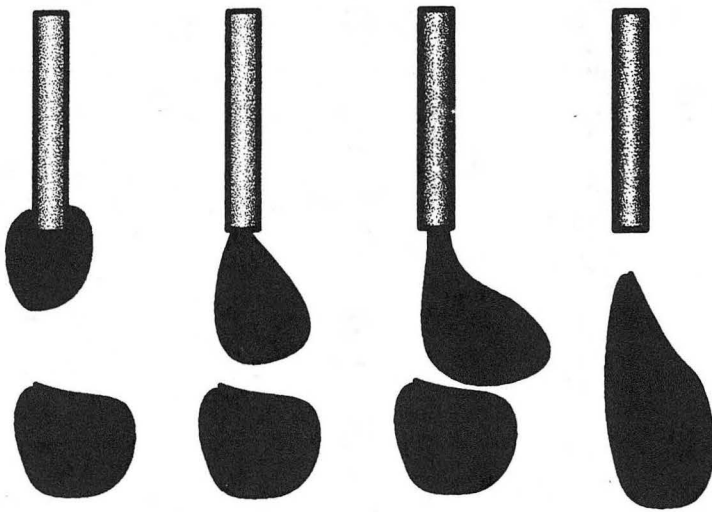
**FIGURE 6: Parallel shower-door glass plates, 0.5 and 0.25 ml/hr.**



# Modes of dripping in "shower-door" plates



Initially dry plates



Coalescing w/ trapped water

# General Observations in Parallel Plates

- Drips follow pre-wetted paths and path varies with each new assembly
- Frequency of snaps and magnitude of pressure fluctuations increase with flow rate, although absolute values vary from “non-contiguous” runs
- Systematic baseline pressure fluctuations at higher flow rates
- No pressure fluctuations beyond baseline for film flow in sand-blasted glass plates (need higher flow rate)
- Drop coalescence in “shower-door” glass drives snapping from needle due to water-trapping near needle (no observed threads)

# Transition to Chaotic Behavior: What affects initial conditions of drop formation?

## Drips in open air

- “sawtooth” pattern for small needle diameter - systematically increase needle diameter? needle angle?

## Drips in smooth glass parallel plates

- length of thread a function of flow rate - expect transition at higher flow rates (until limit of continuous thread)
- “meandering” thread - at higher flow rates, lower angles of inclination, variable surface texture, needle angle and opening
- partial thread snaps - ???

## II.6

# TOUGH2 Modeling

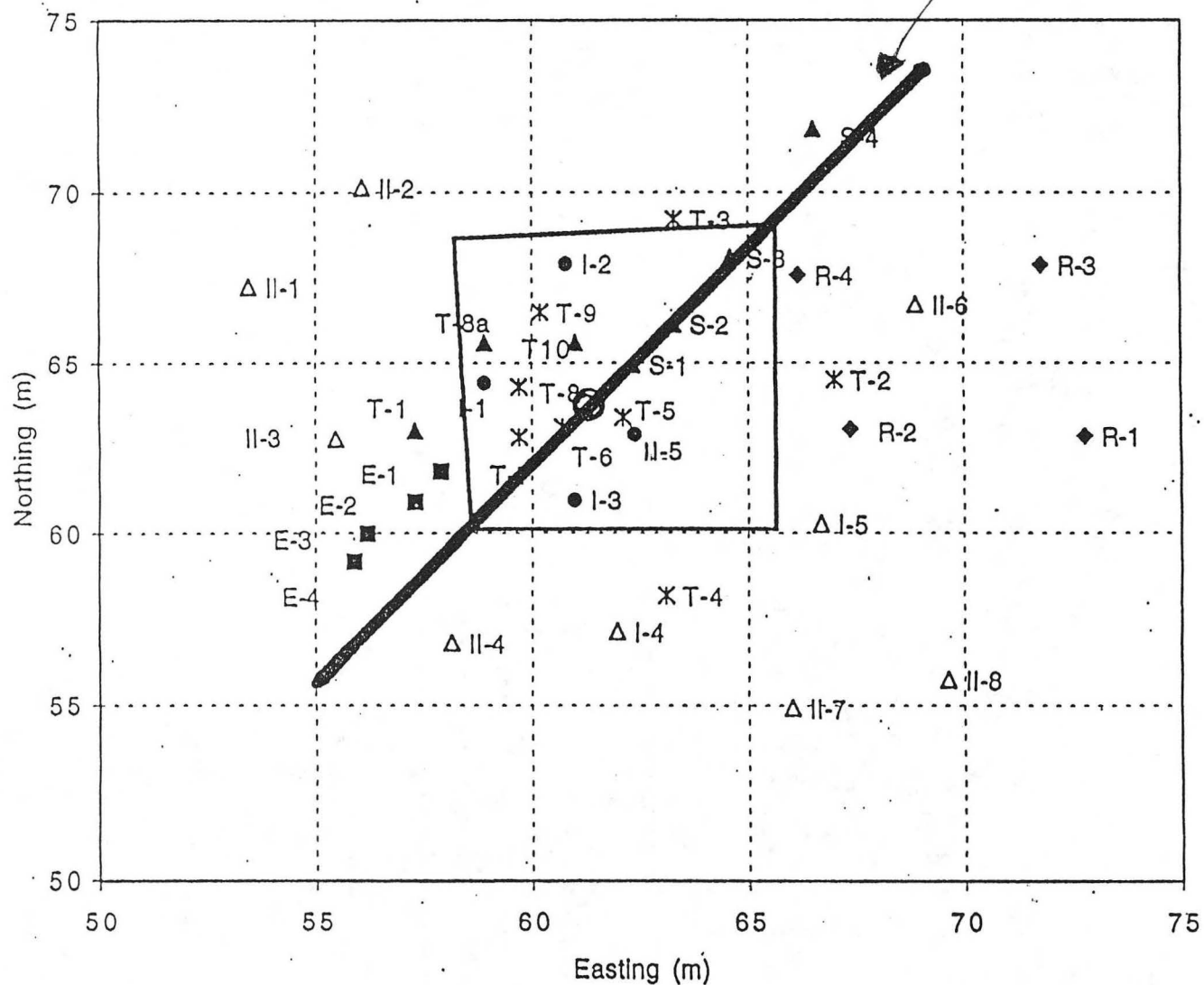
Christine Doughty  
Berkeley Lab

Objective: Use traditional, non-chaotic models of subsurface flow and transport to identify features of real behavior that can be captured this way, and hence do not require a chaotic explanation

- Spatial distributions
- Time series

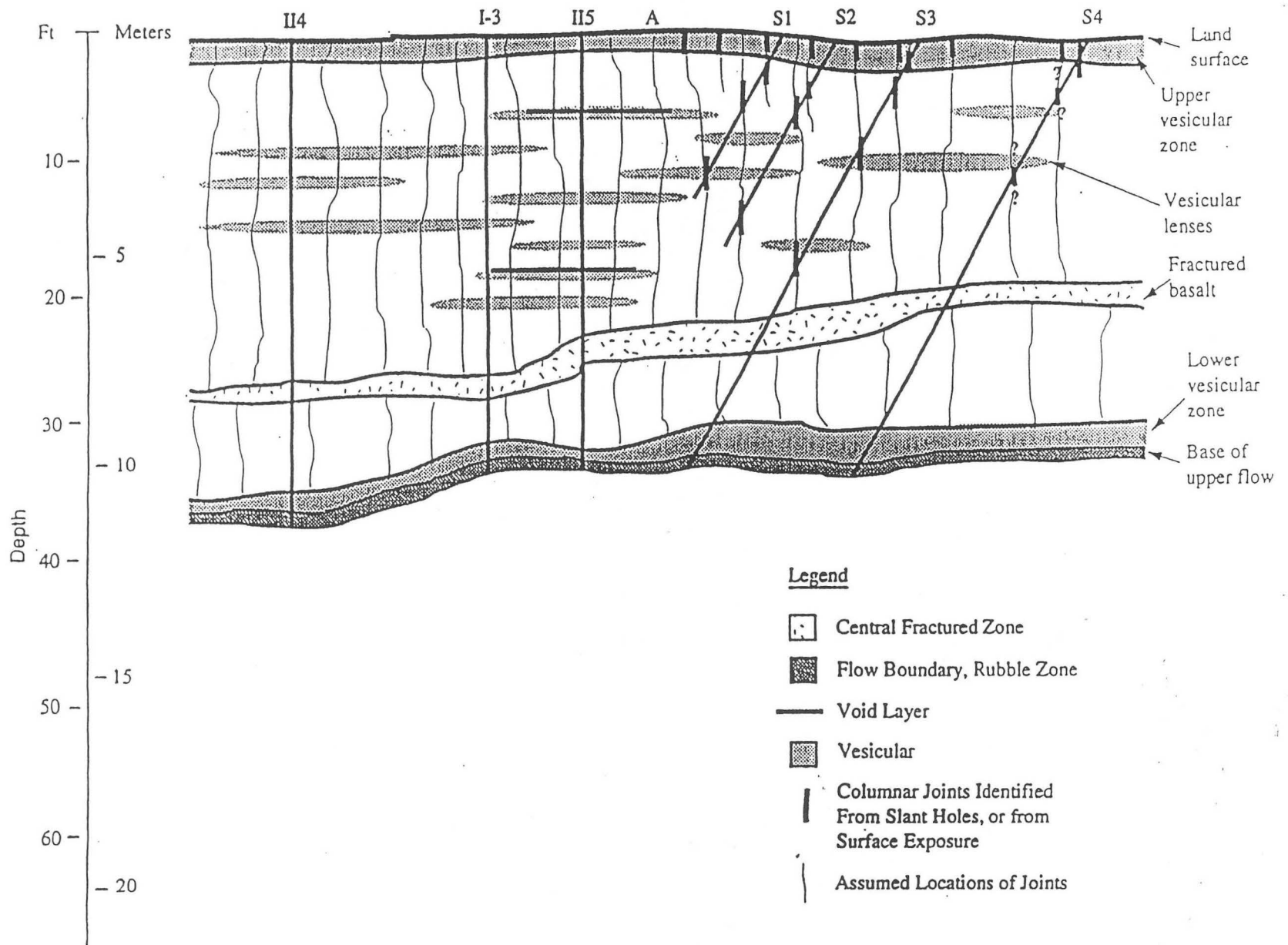
# Box Canyon Well Layout

Location of 2D Model

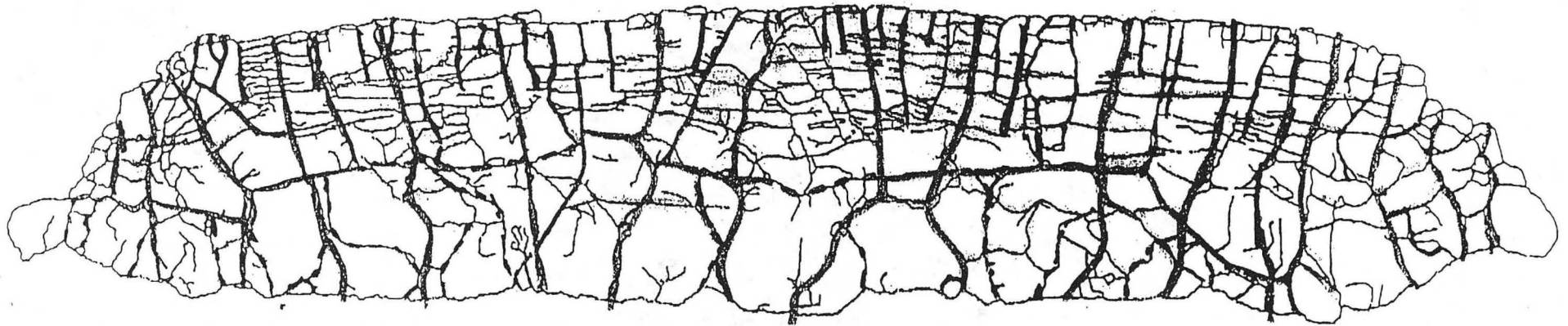




# Geologic Cross-Section at Model Location



# Fracture Map at Box Canyon Cliff Face



149

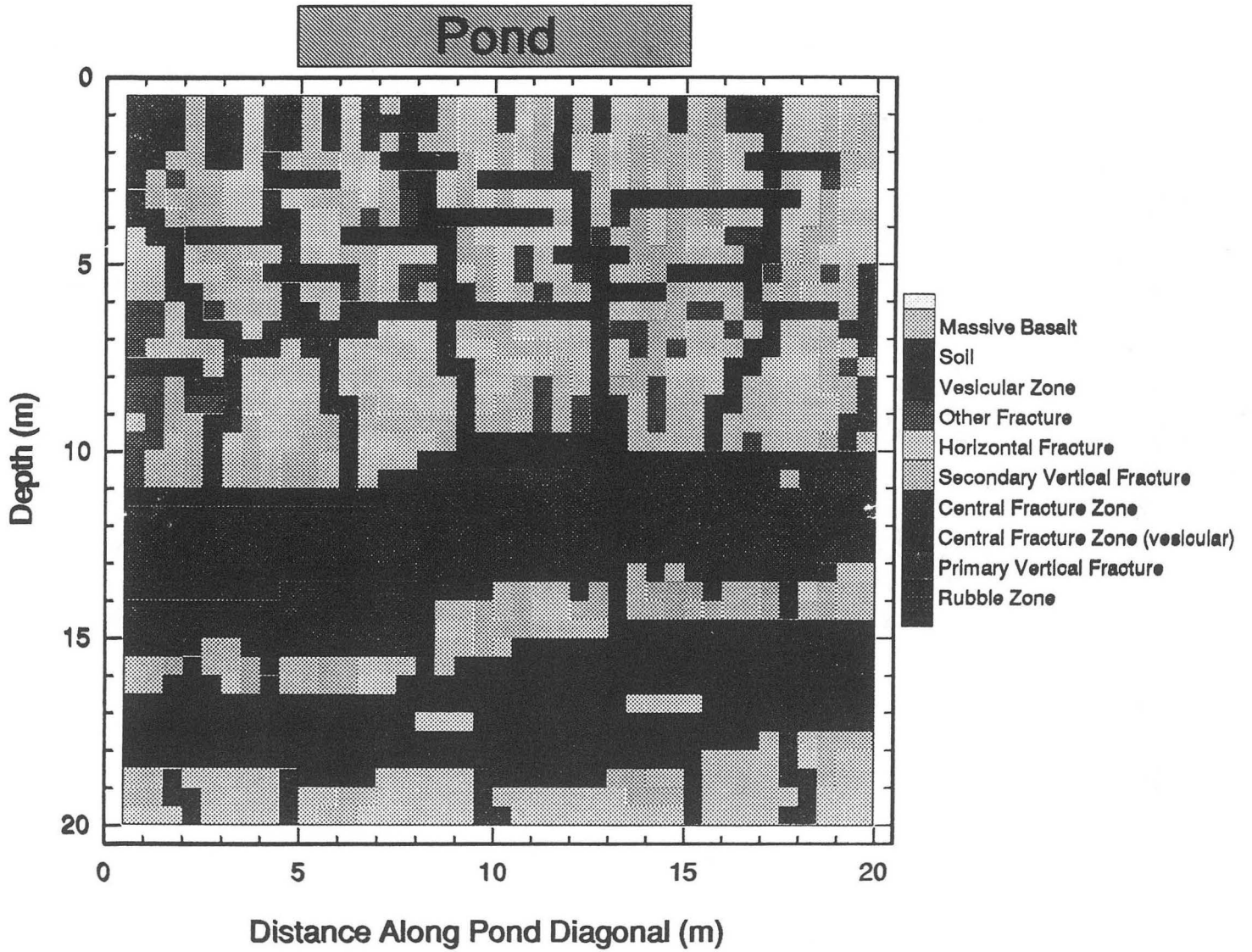
5 m

## Geometrical Classification of the Fracture System Exposed at the Box Canyon Cliff Face

- H0 - central zone horizontal fracture
- - - H1 - central visicular zone
- H2 - connect V0 with V1 and V2
- H3 - connect V2
- H4 - dead-end

- V0 - connect top and bottom of basalt flow
- V1 - connect top of basalt flow with V0
- V2 - connect top of basalt flow with horizontal fractures
- V3 - internal vertical fractures (betwen #3)
- - - V4 - connect bottom of flow with horizontal fractures
- V5 - dead-end

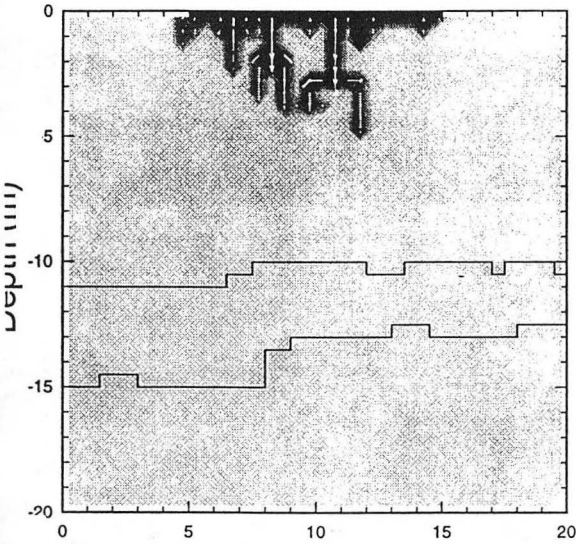
# Numerical Model



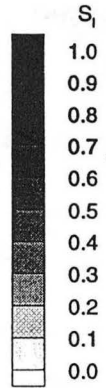
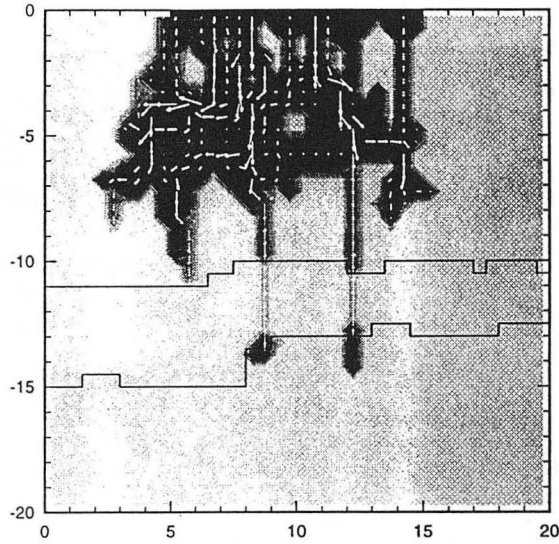
# Ponded Infiltration Results

## Model with No Air Entrapment

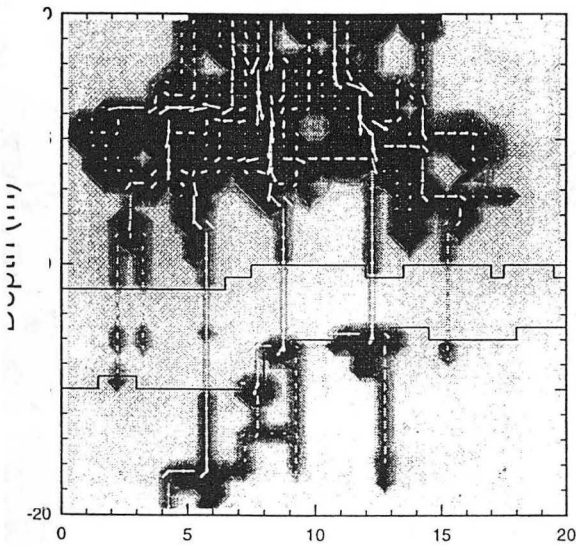
One Week Infiltration



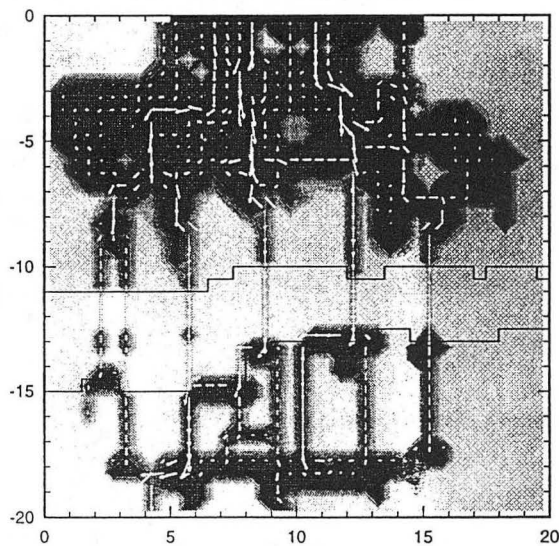
Two Weeks Infiltration



Three Weeks Infiltration



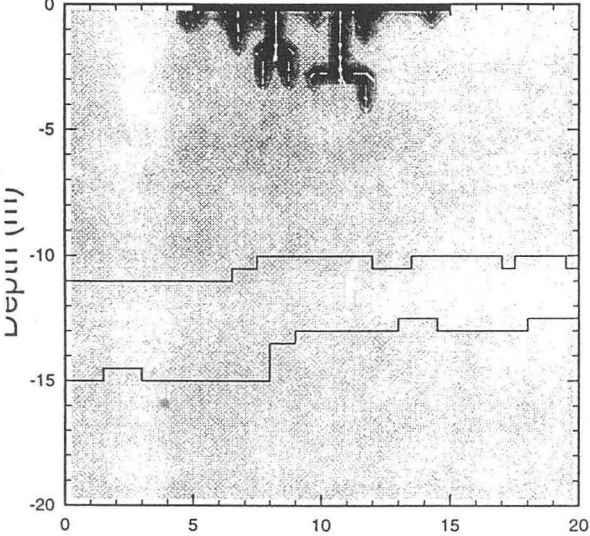
Four Weeks Infiltration



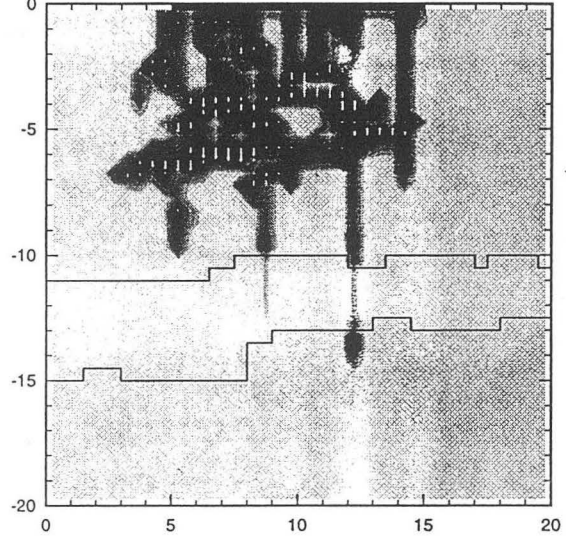
# Ponded Infiltration Results

## Model with Entrapped Air

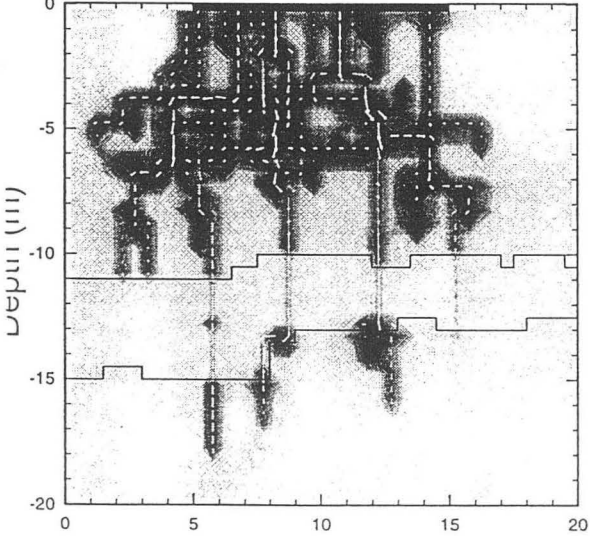
One Week Infiltration



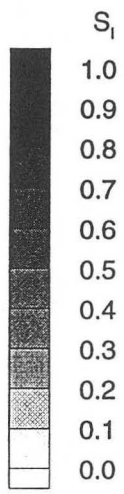
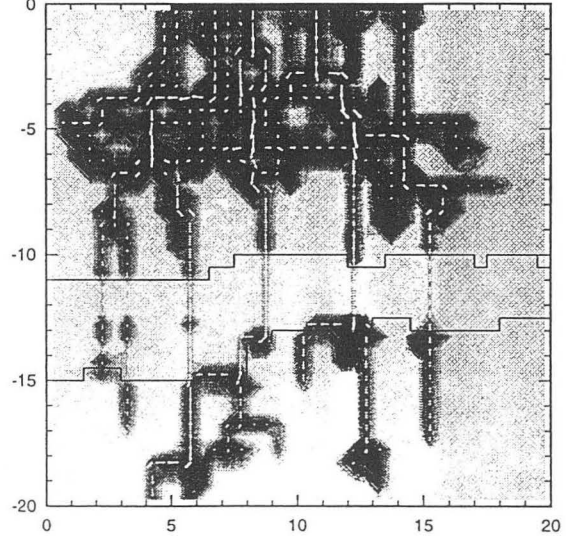
Two Weeks Infiltration



Three Weeks Infiltration

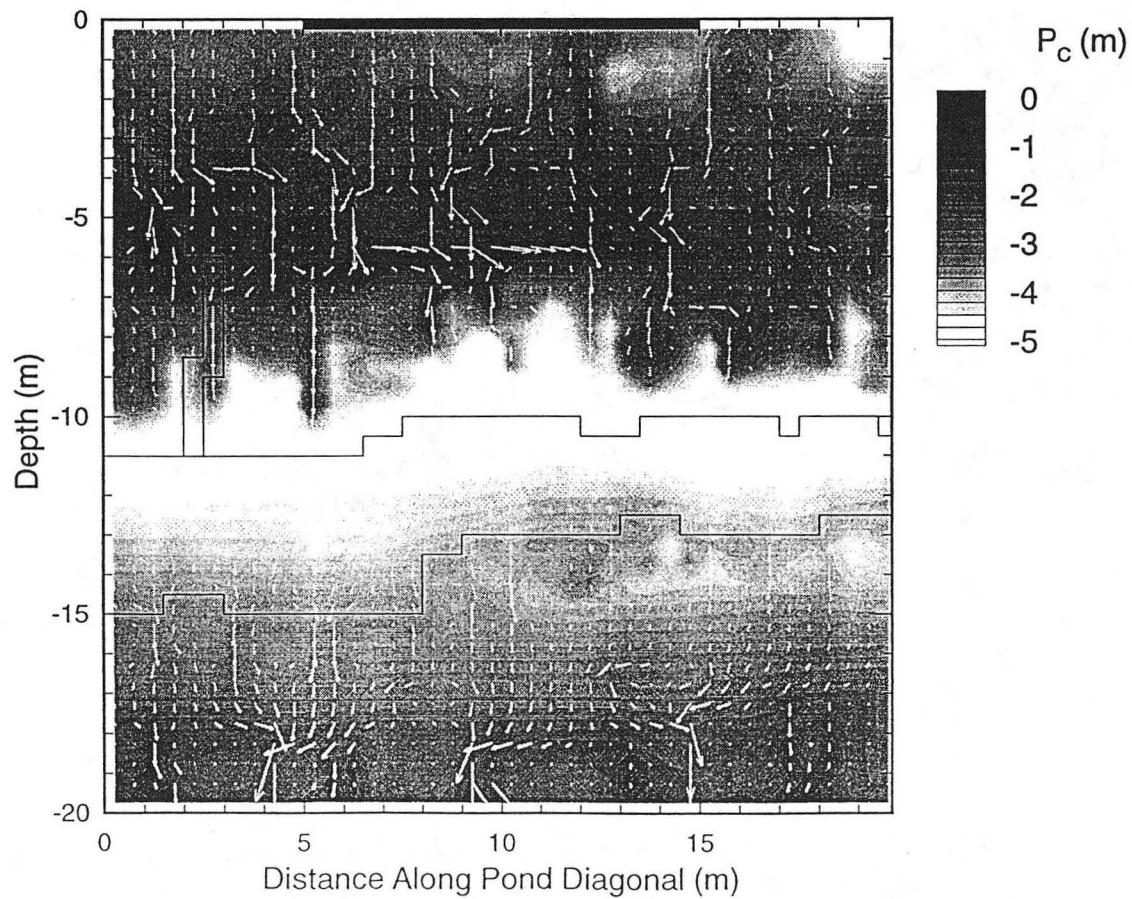
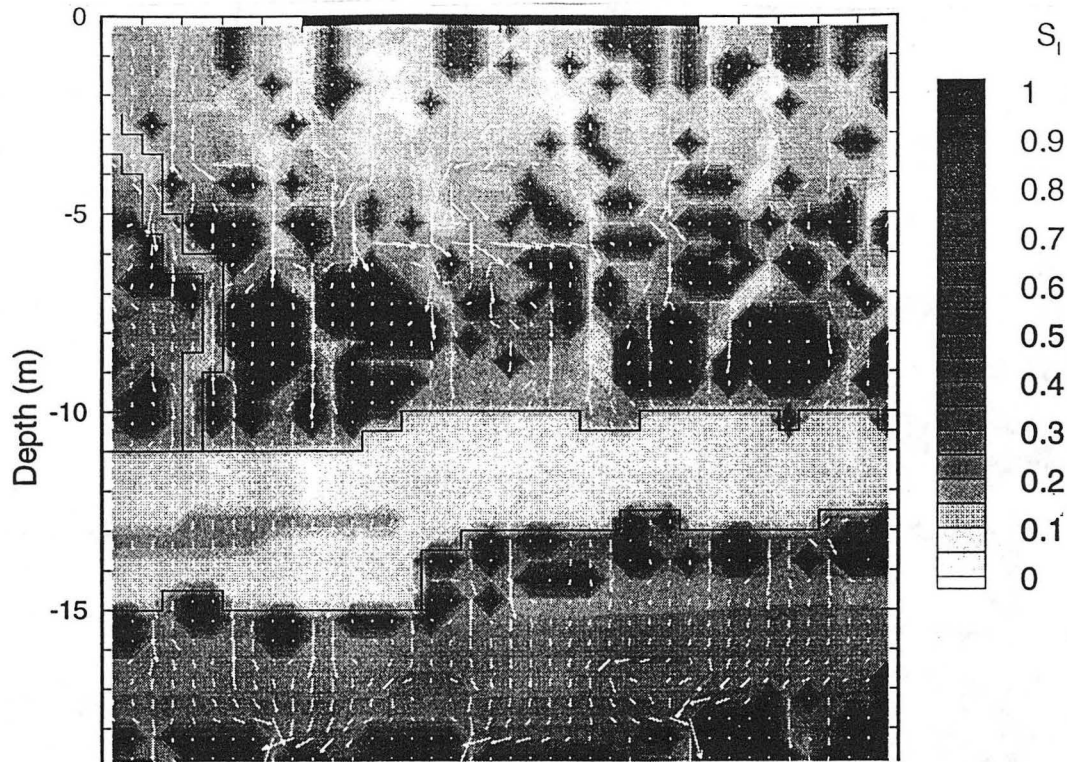


Four Weeks Infiltration



# Natural State

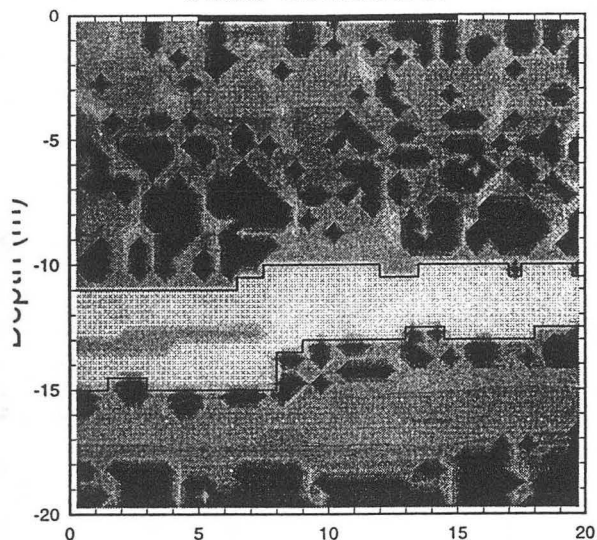
Model with Capillary Pressure and Background Infiltration



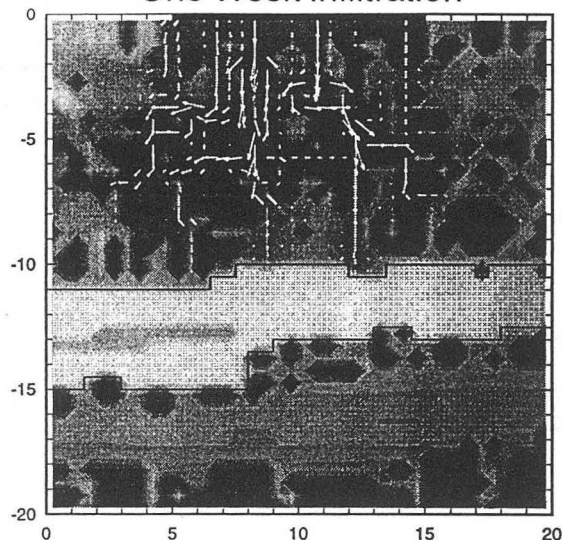
# Ponded Infiltration Results

## Model with Capillary Pressure and Background Infiltration

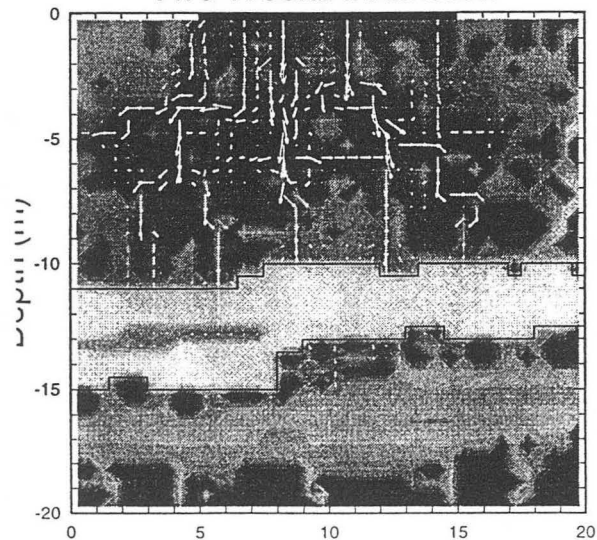
Initial Conditions



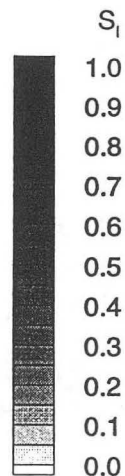
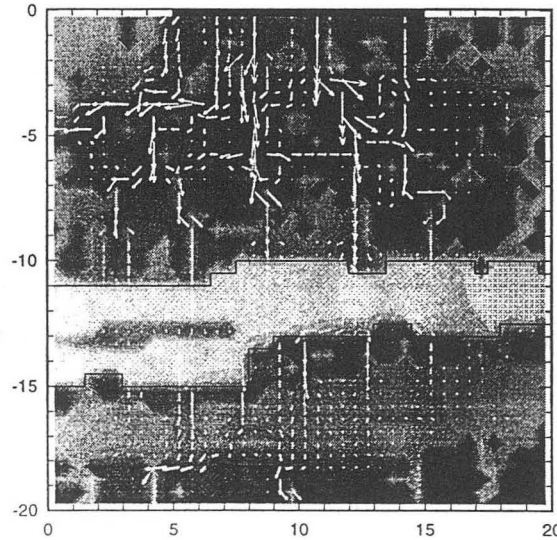
One Week Infiltration



Two Weeks Infiltration

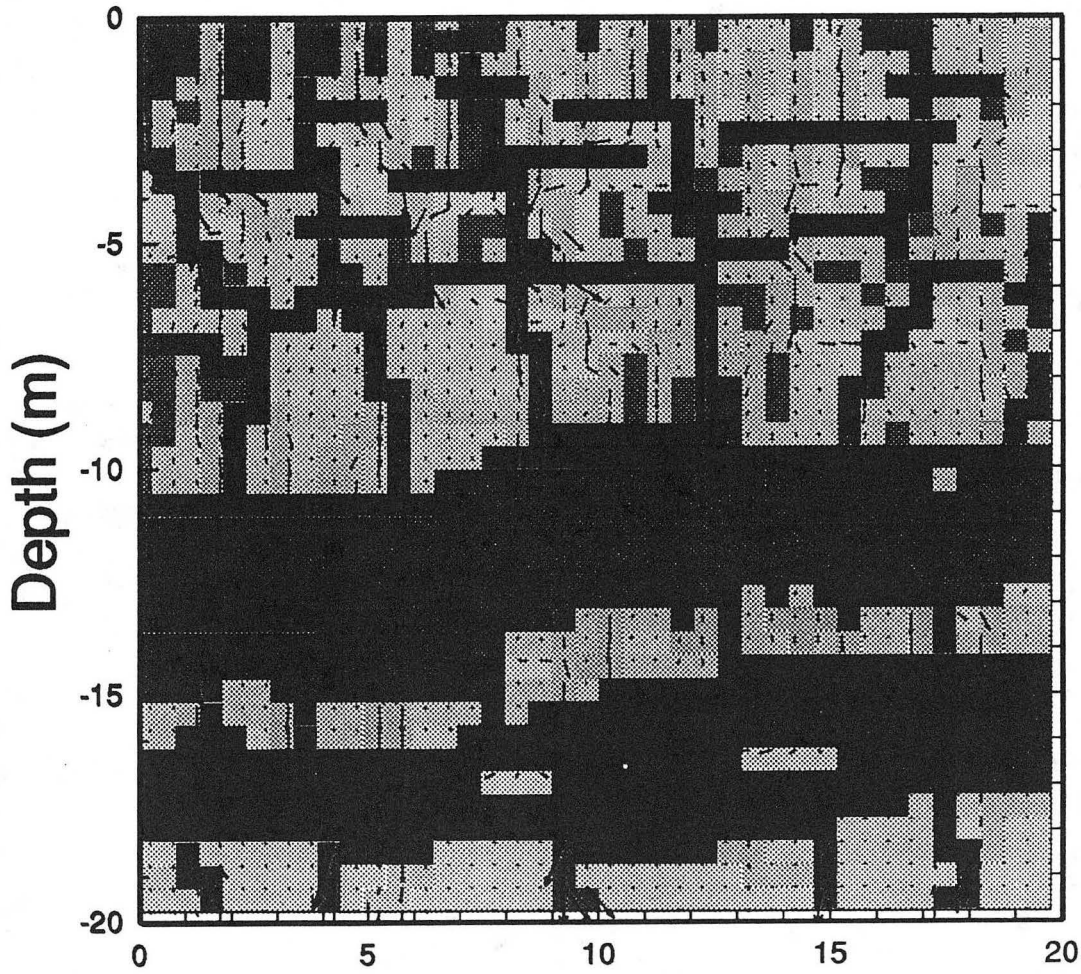


Four Weeks Infiltration



# Liquid Flow Field

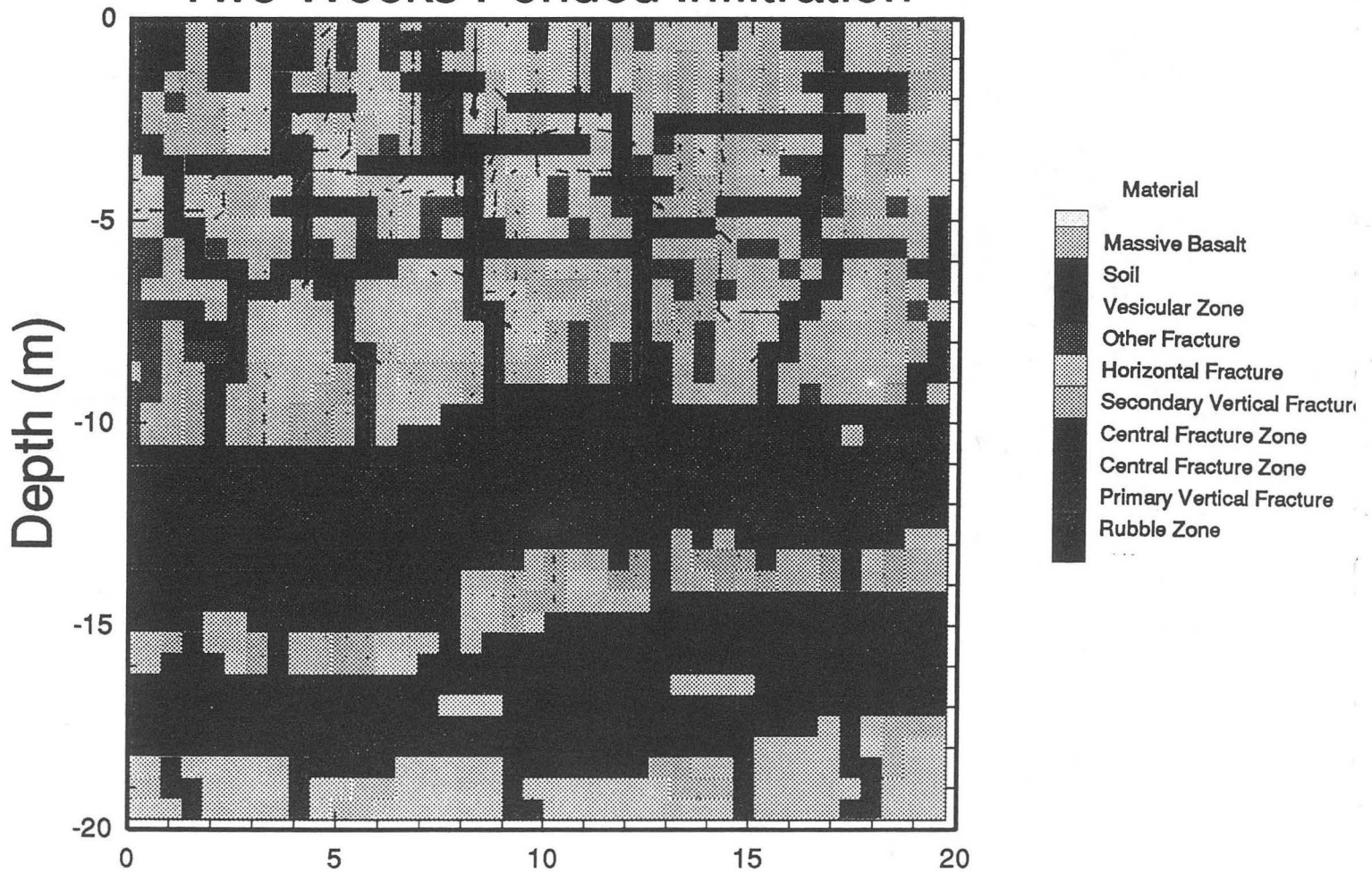
## Ambient Infiltration of 0.2 mm/day



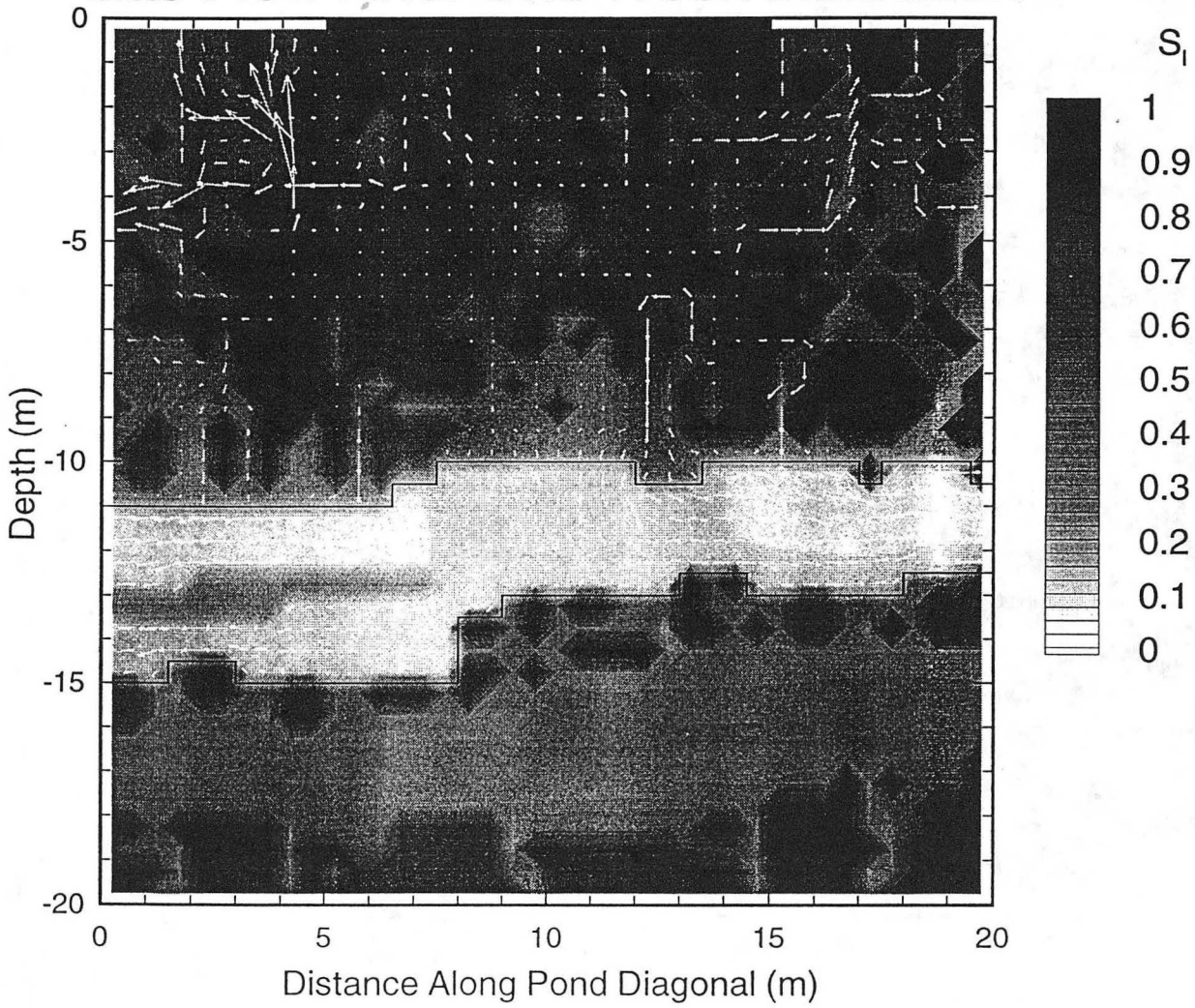


# Liquid Flow Field

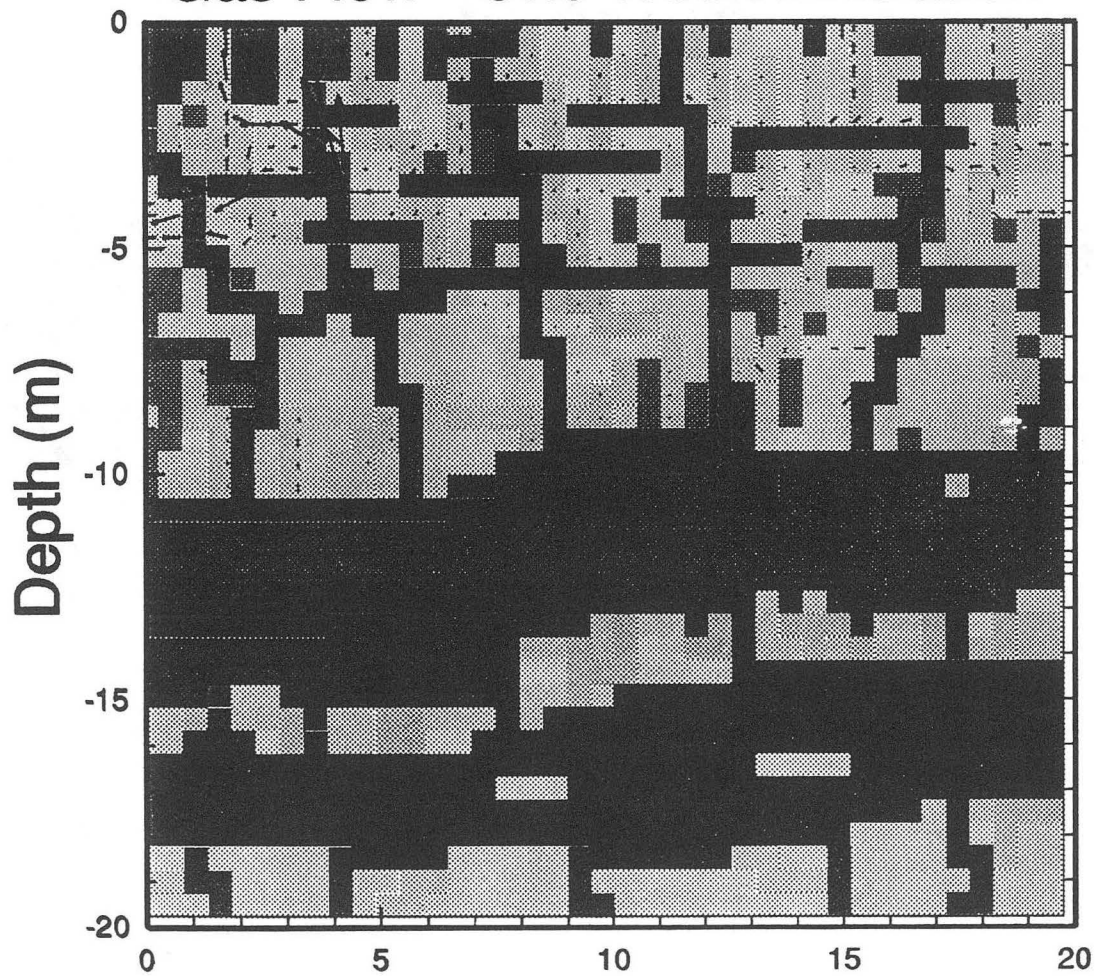
## Two Weeks Pondered Infiltration



# Gas Flow After One Week Infiltration

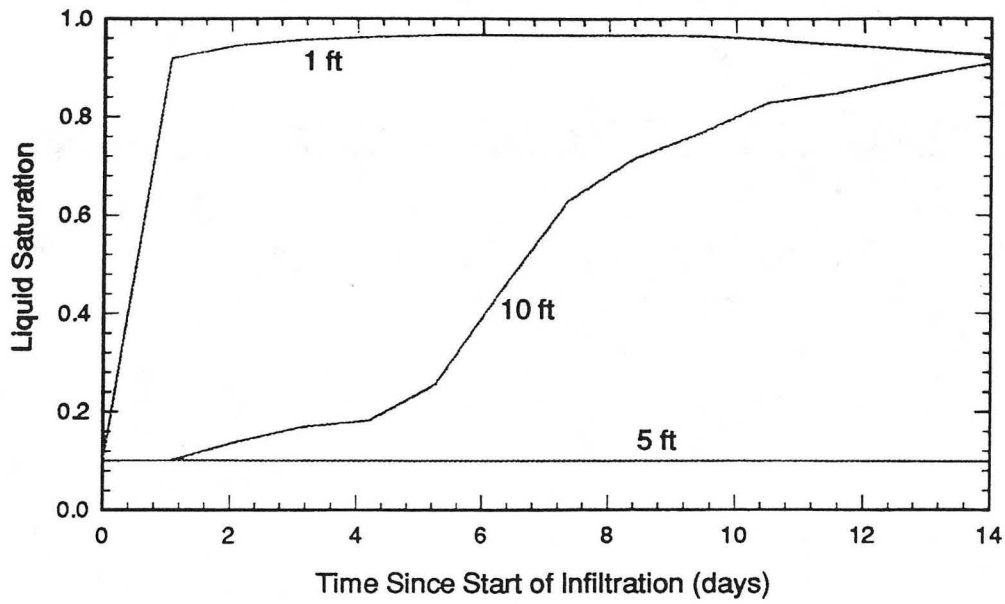


# Gas Flow - One Week Infiltration

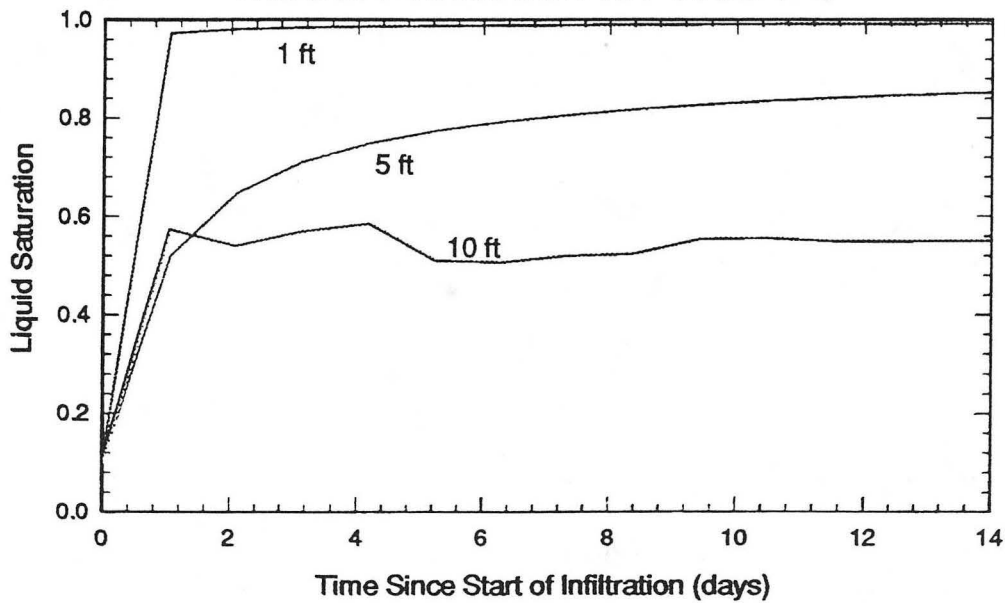


# Model with Entrapped Air

## Model Prediction for Well T-5

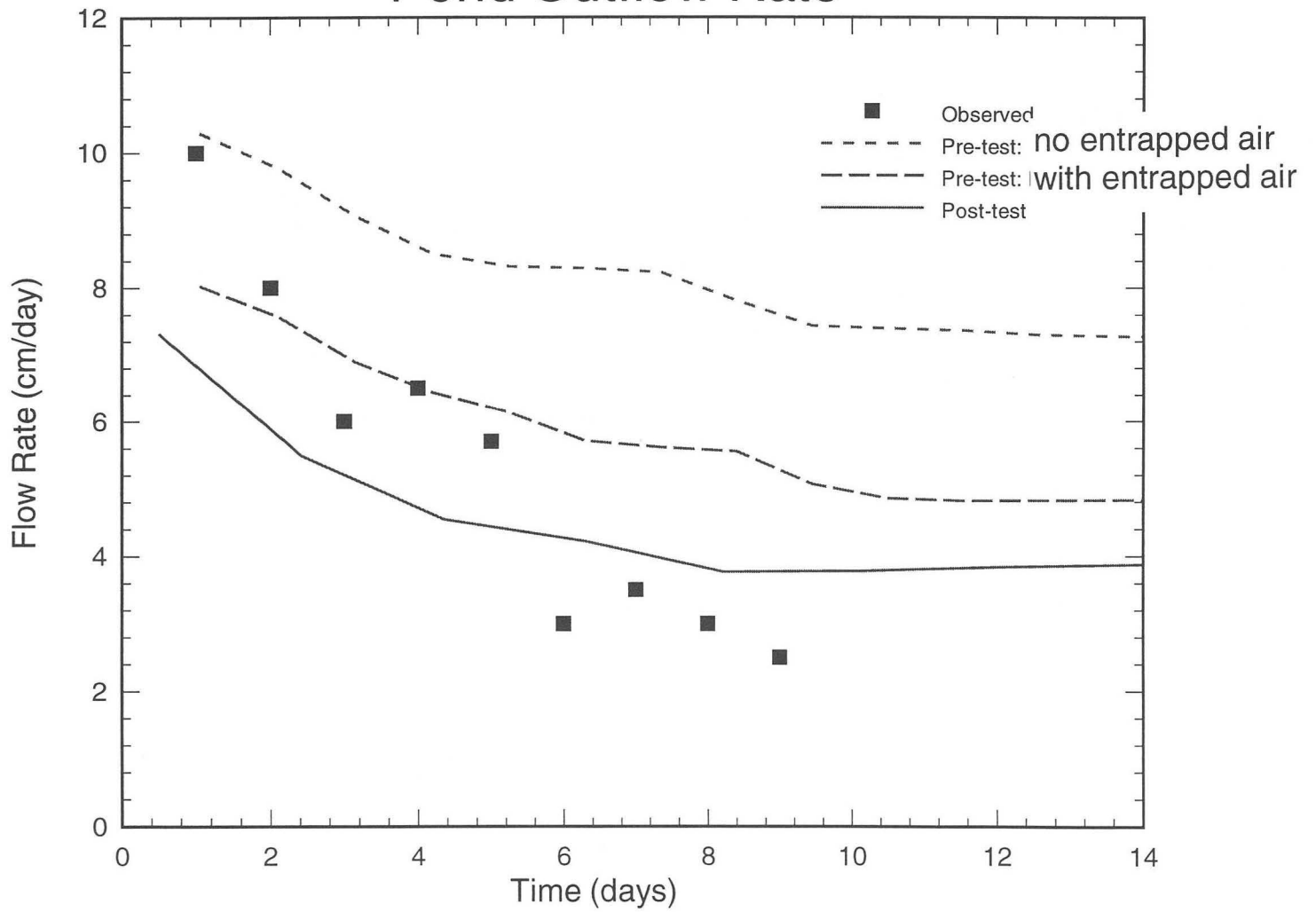


## Model Prediction for Well T-9

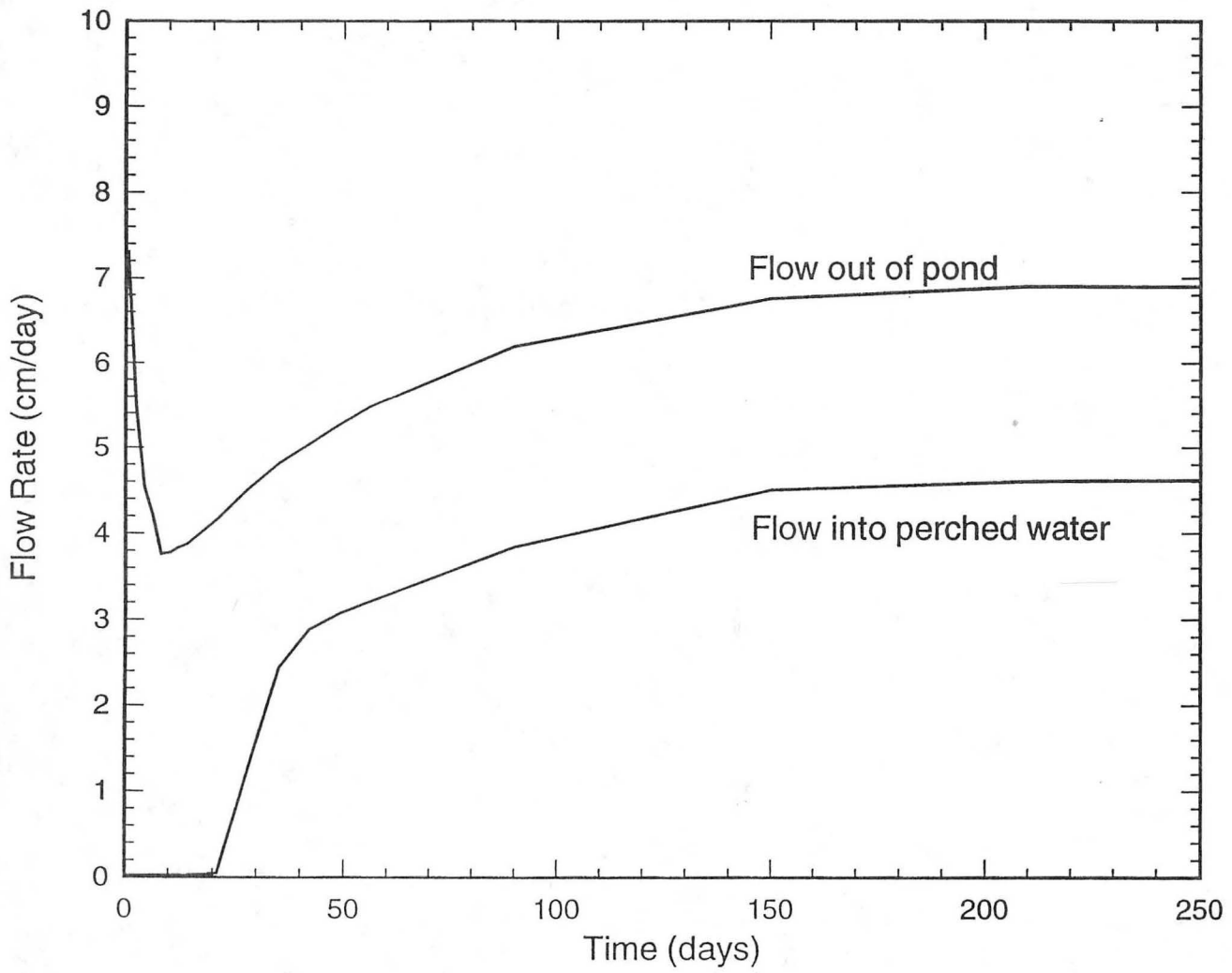


BC116\_OBS.PLT  
~~BE~~ SL\_OBS9.STY  
SL\_OBS5.STY

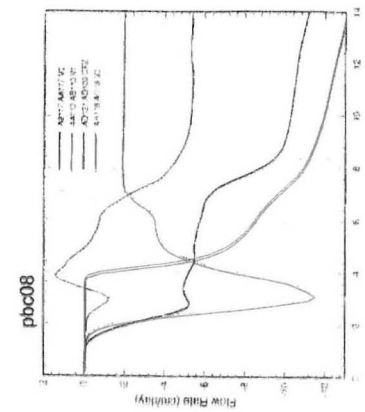
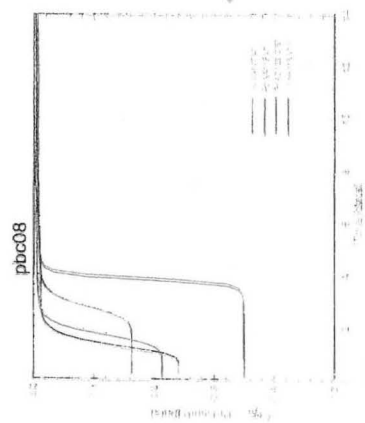
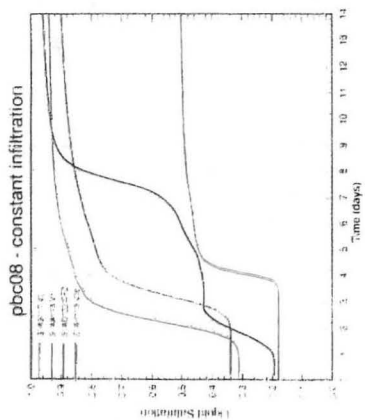
### Pond Outflow Rate



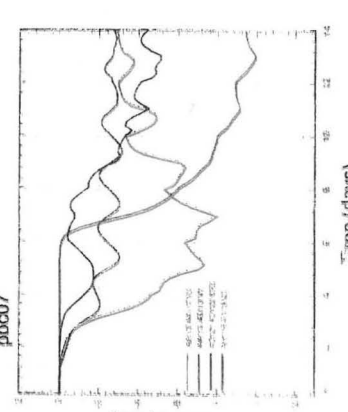
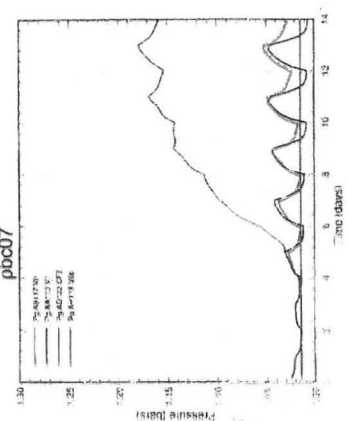
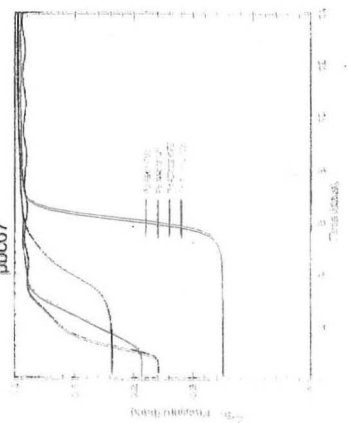
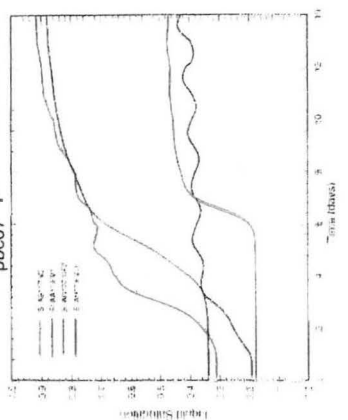
## Long-term Flow Rates



# Comparison Between Continuous and Pulsed Ponding



## pbc07 pulsed infiltration

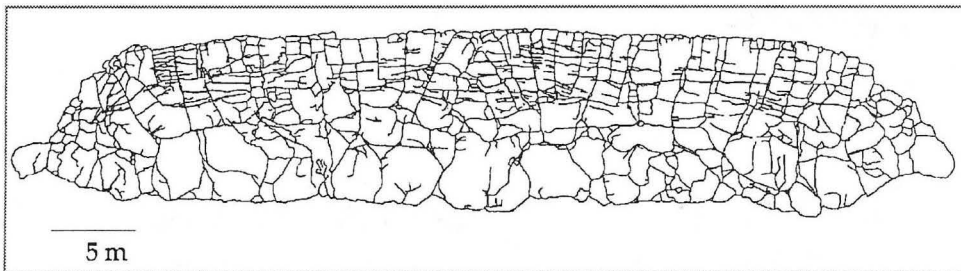
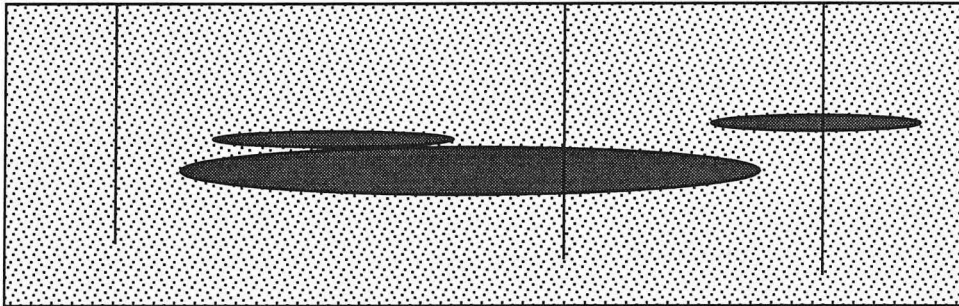


# II.7

## Estimating Total Mass of Contaminant Plumes from Sparse Well Data

Masoud Nikraves, Lea Cox, Boris Faybishenko

*Lawrence Berkeley National Laboratory, Berkeley, CA*



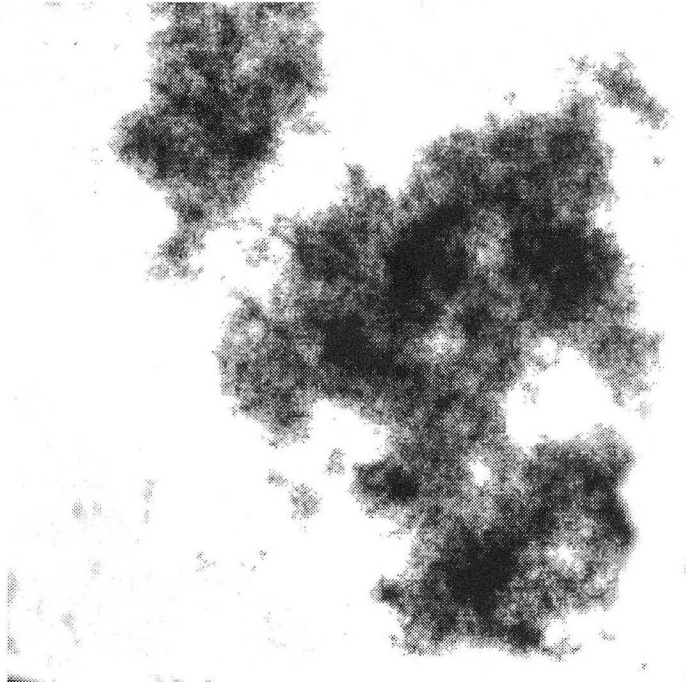


# Objectives

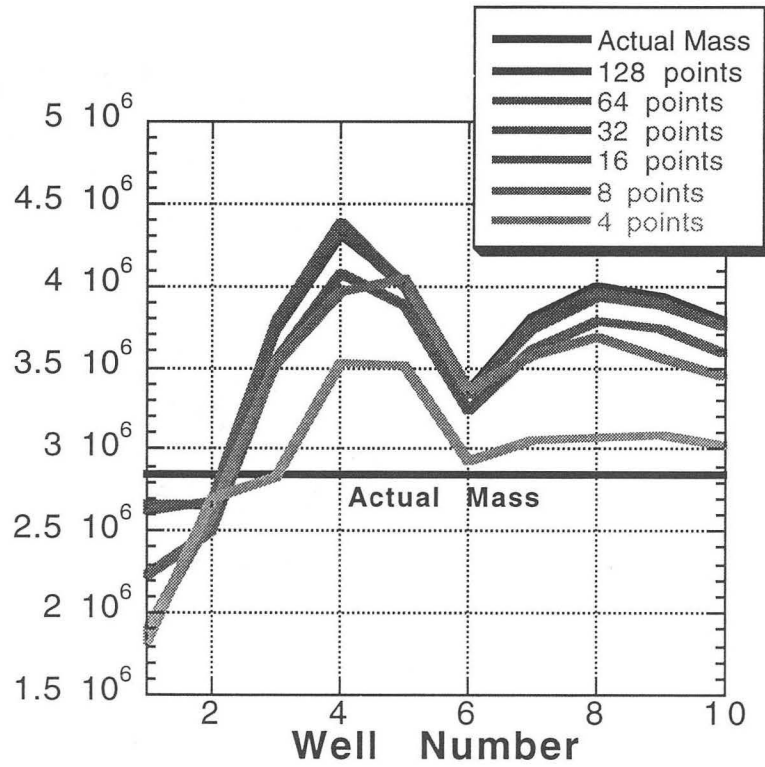
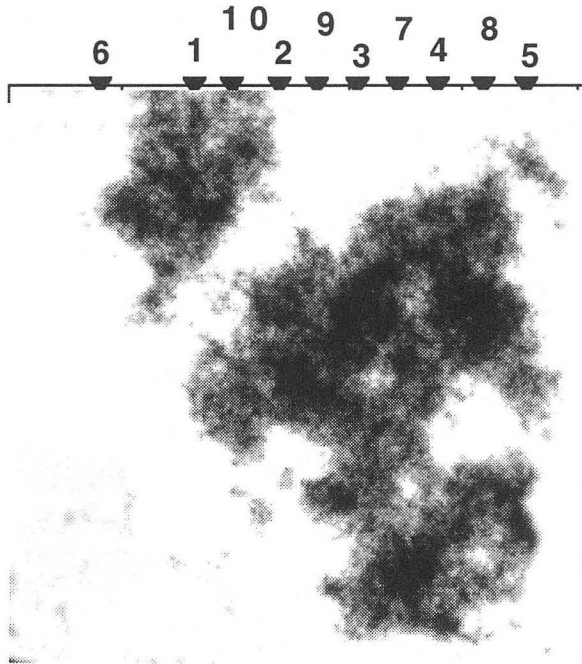
- **test and compare different methods for interpolating distribution of contaminants**
  - 1) simple averaging**
  - 2) fractal methods**
  - 3) neural network**
- **minimize number of wells needed to estimate the total mass of contaminant**

# Generation of Fractal Plume

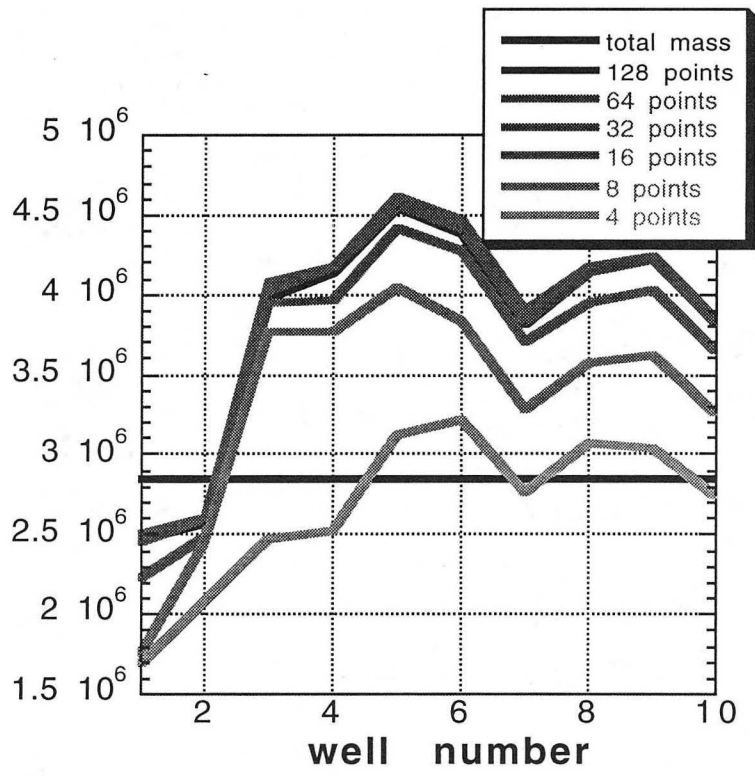
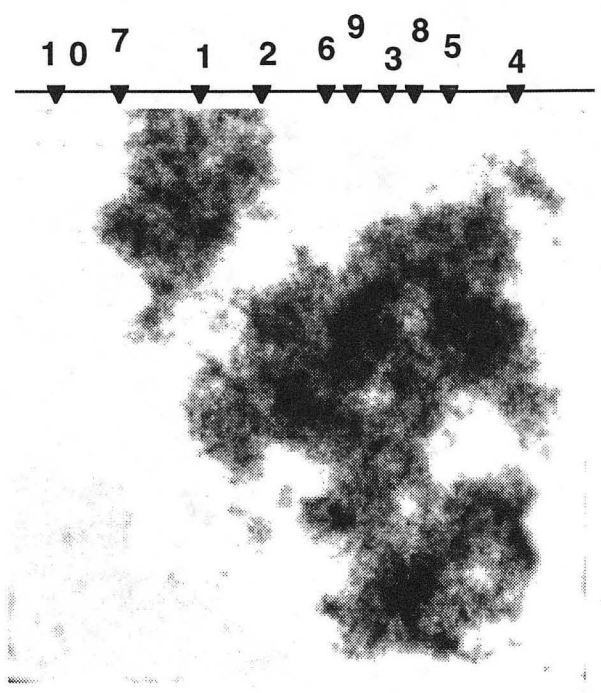
- fractal surface generator software (Russ, 1995) with midpoint displacement option
- fractal dimension of 2.5
- 256 x 256 pixels
- cutoff of 50 to simulate detection limit



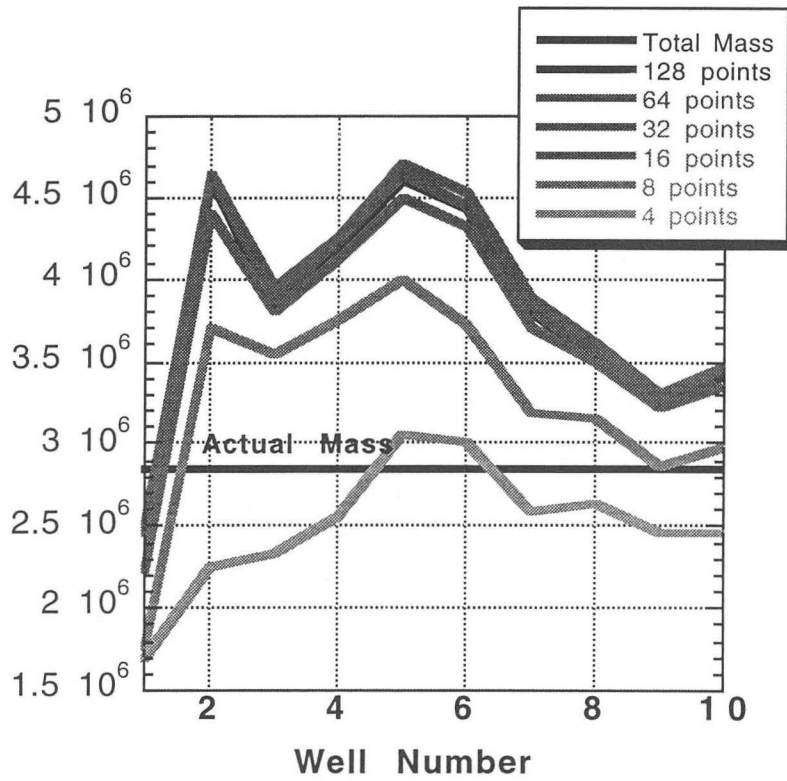
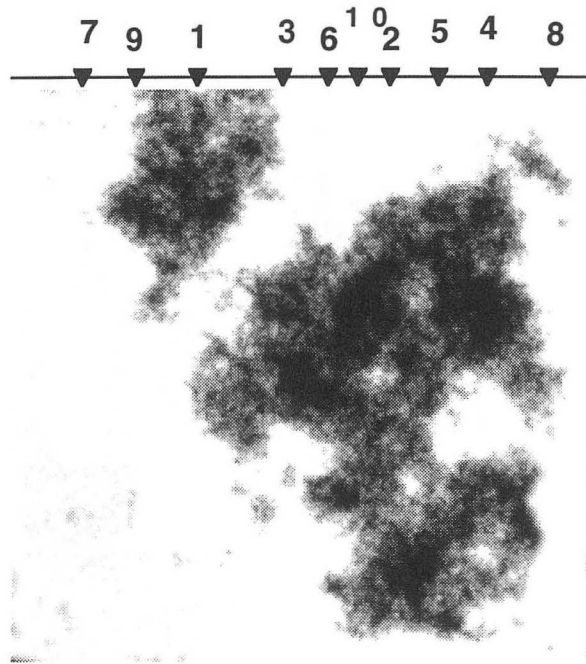
# Simple Averaging: Case 1



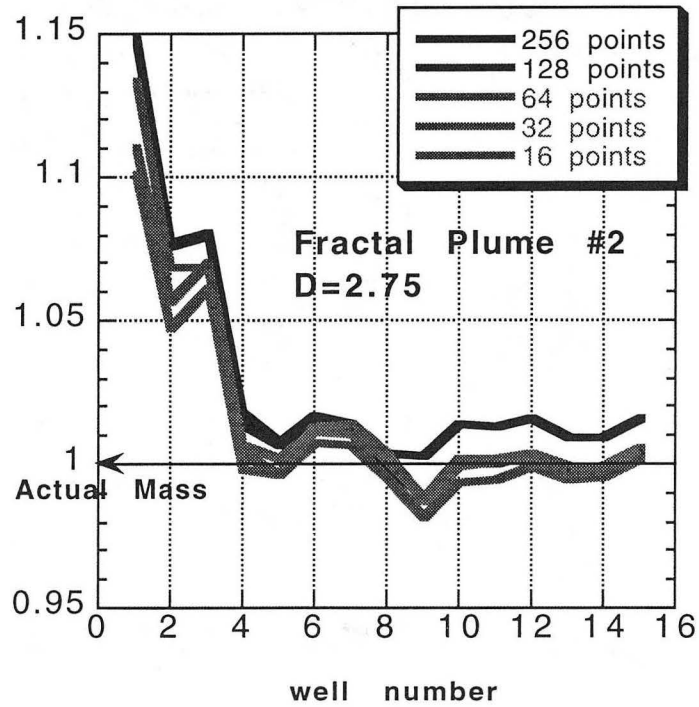
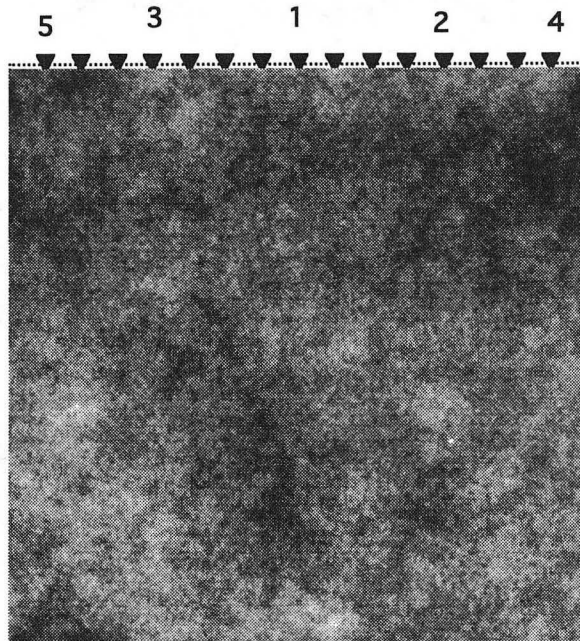
# Simple Averaging: Case 2



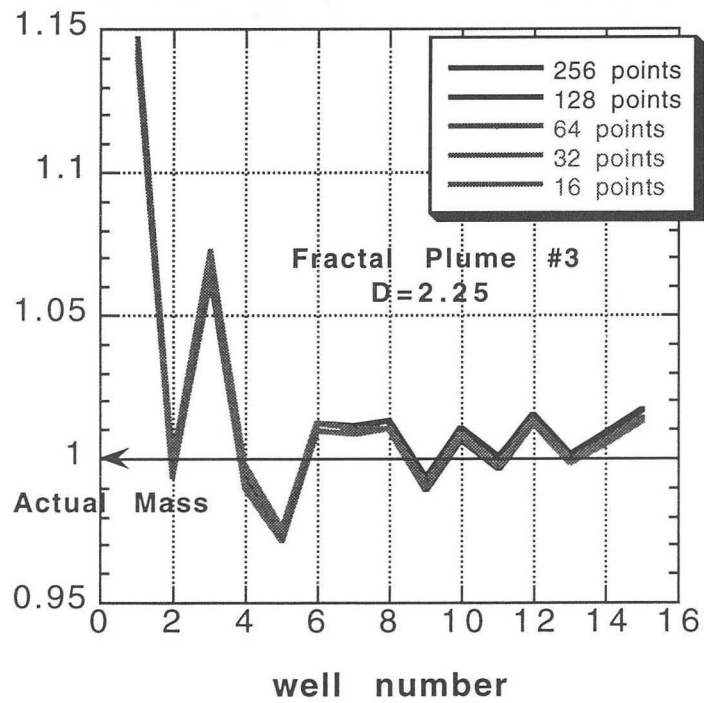
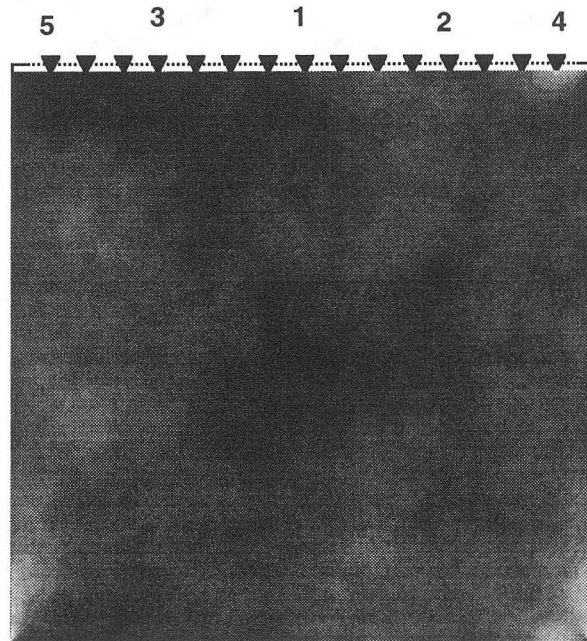
# Simple Averaging: Case 3



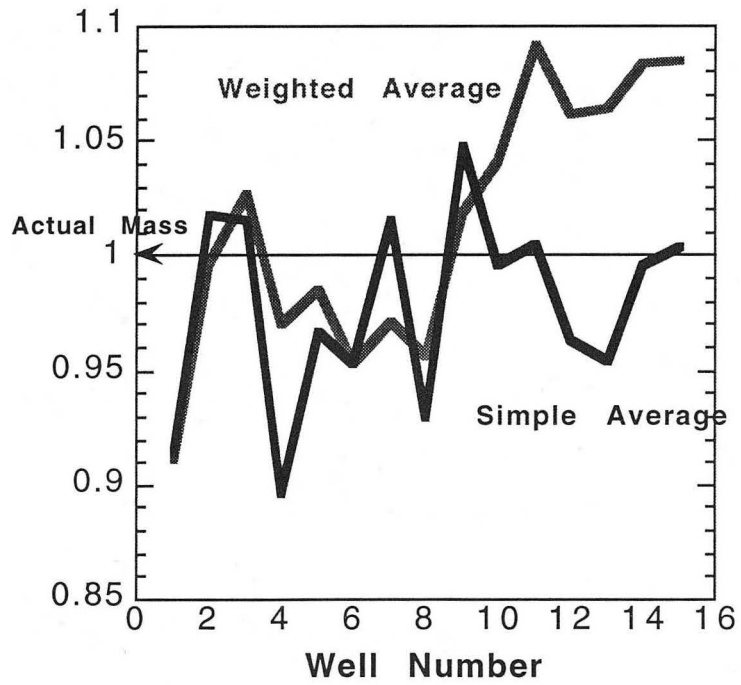
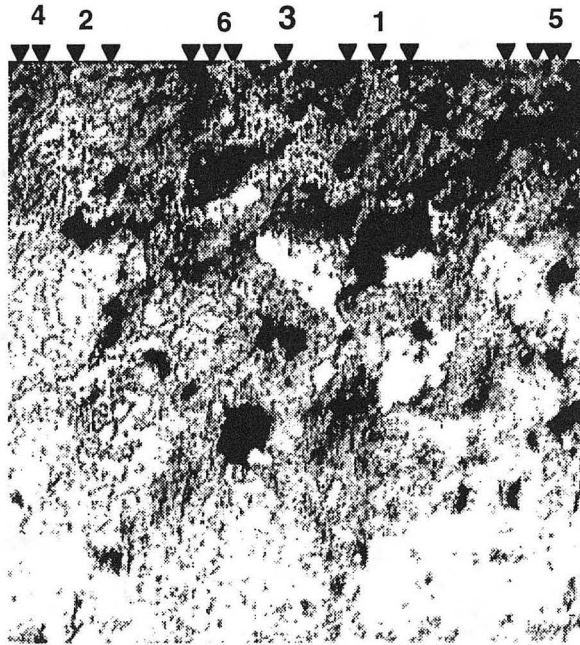
# Fractal Plume #2, D=2.75



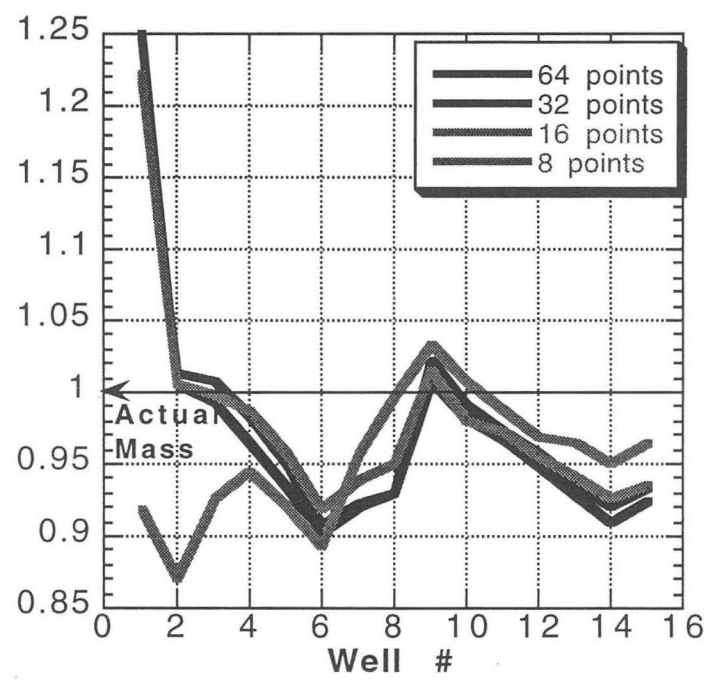
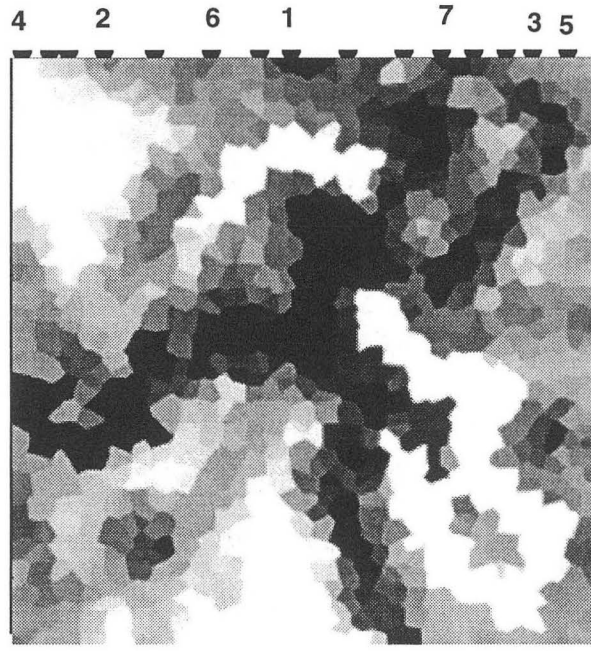
# Fractal Plume #3, D=2.25



# Yucca Mountain Fracture







## Fractal Methods

- **Total Mass  $\sim (a) (r)^D$**
- **Uncertainty in “a” and in “D”**

**sparse data**

**variations with each well**

**methods of measurement**

**Conclusion: Fractal Methods not useful for this type of problem**

Method of Measurement	Case #1 (D=2.5)	Case #2 (D=2.75)	Case #3 (D=2.25)
Slit Island	2.31	2.60	2.14
Kolmogorov Box	2.49	2.68	2.37
RMS versus Area	2.19	2.37	2.17
Minkowski Cover	2.19	2.42	2.10
Hurst	2.57	2.67	2.36

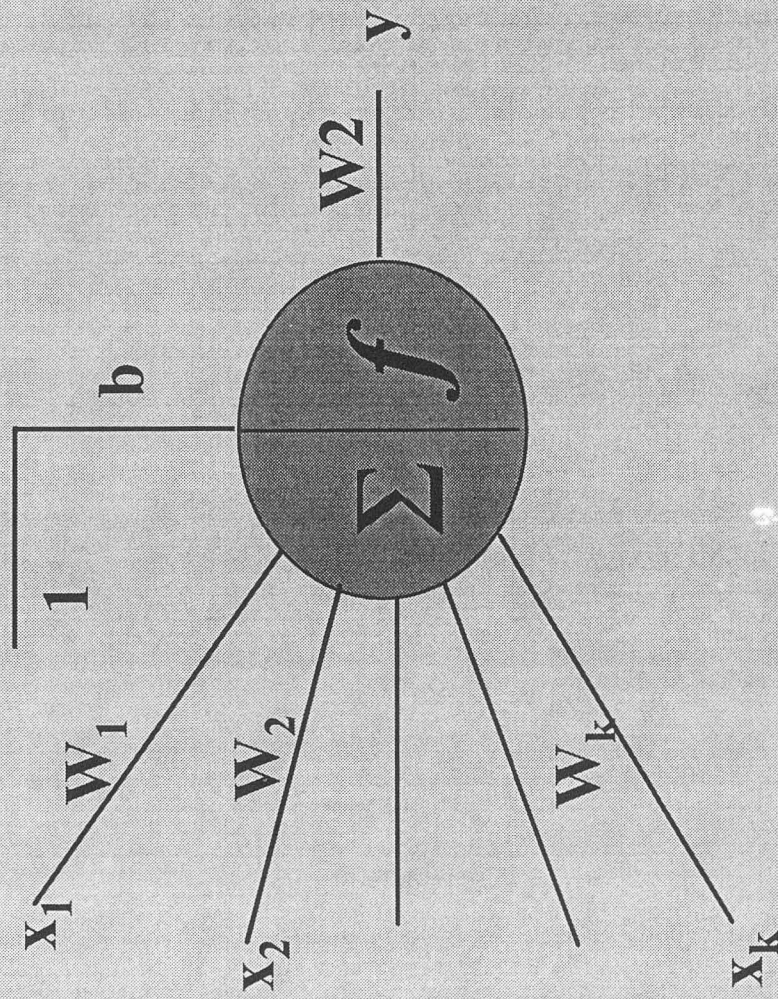
## Why Neural Network?

- **Structure Free**
- **Nonlinear Mapping**
- **Multivariable Systems**
- **Train Easily Based on Historical Data**
  - **Ability to Learn**
  - **Ability to Predict**
  - **Parallel Processing**
  - **Fault Tolerance**

**Much Like Human Brain**

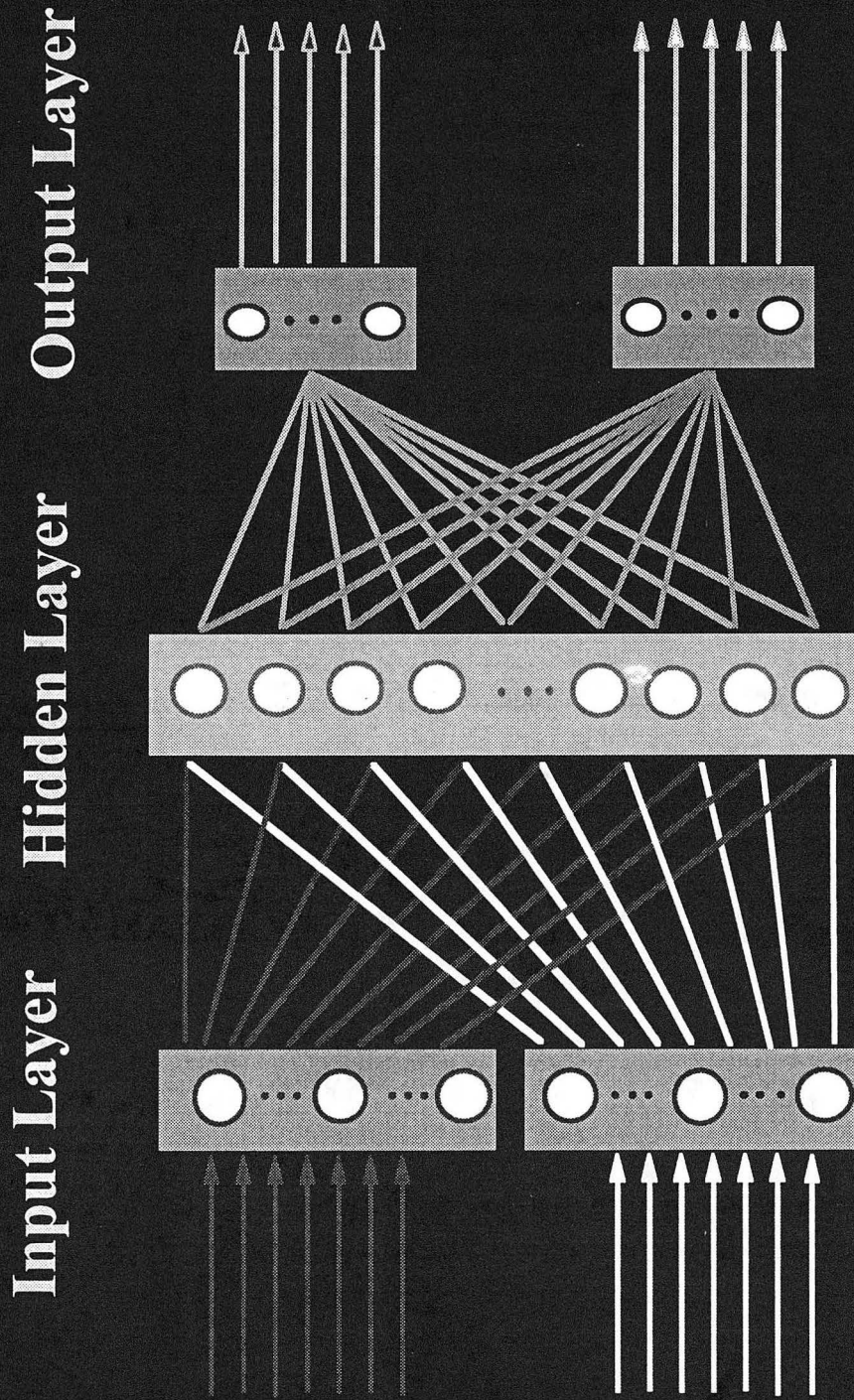
# Neural Network Model

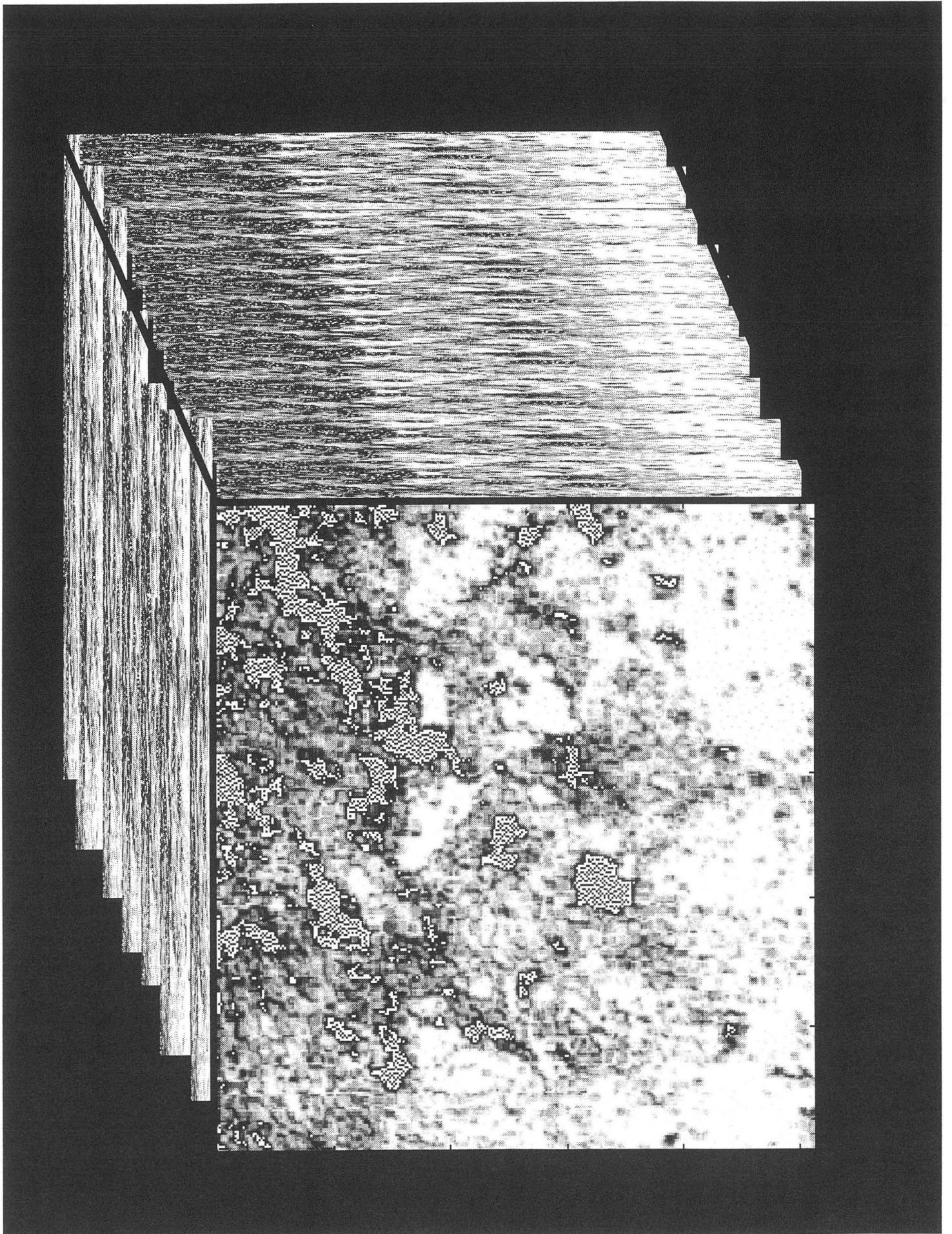
- **each node is a processing unit and manipulates the input vector to give output**
- **utilizes weighting factors, internal thresholds and transfer functions**
- **prespecify the topology of the node connections**
- **use statistics and probability to reduce the output error**
- **interpolation and extrapolation confined to the region defined by the measurements**
- **no sharp boundaries**

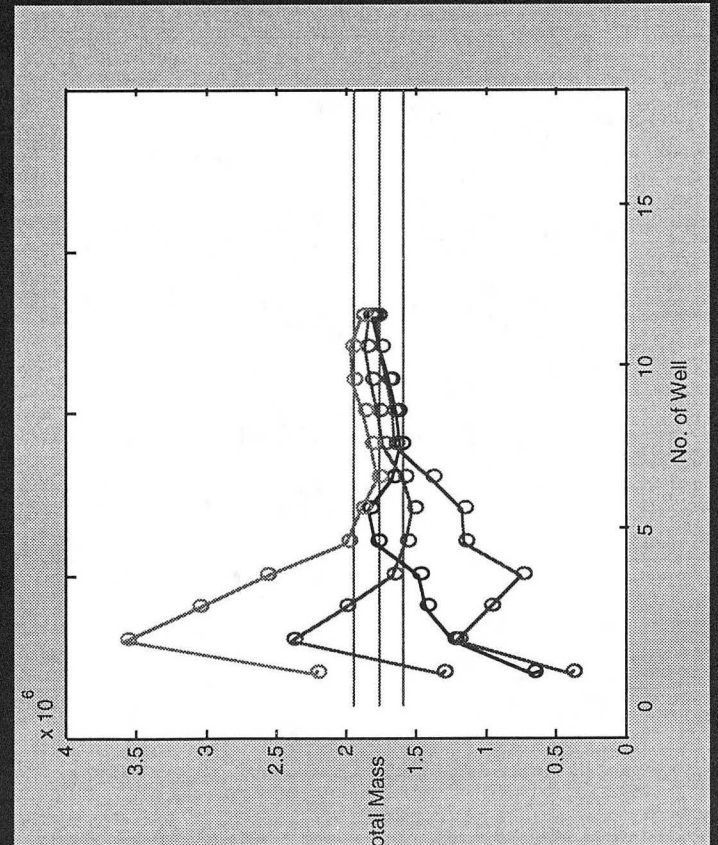
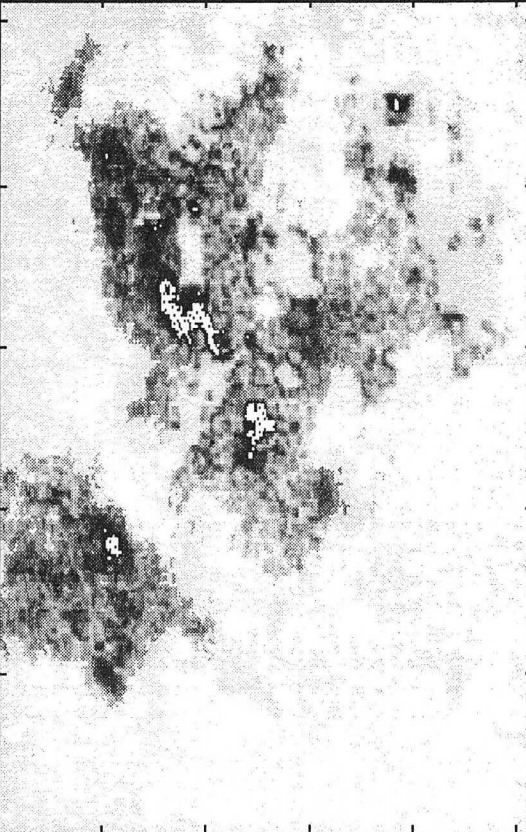
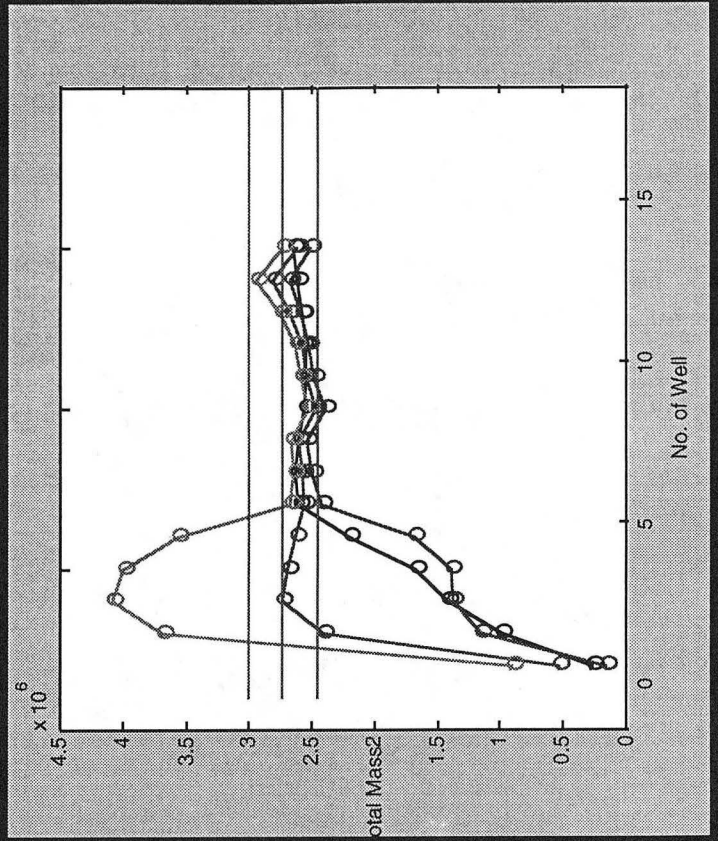
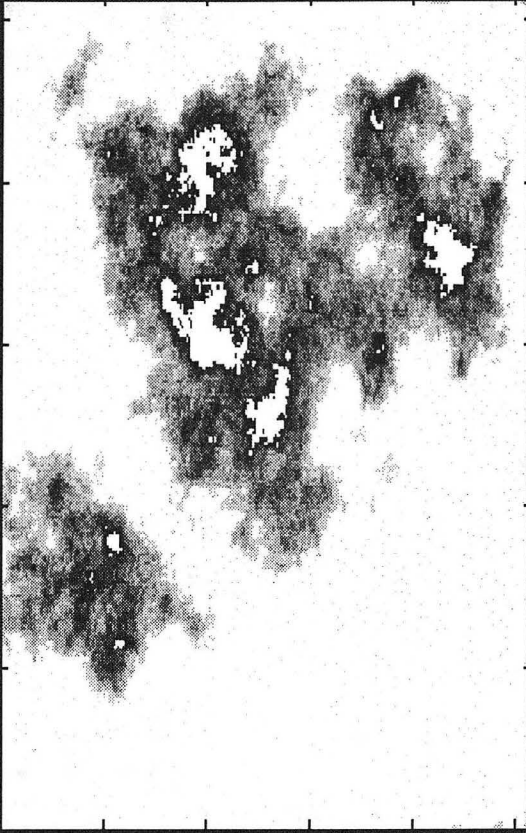


$$y = f [ b + w_1 x_1 + w_2 x_2 + \dots + w_k x_k ] \cdot w_2$$

# *Typical Neural Network*







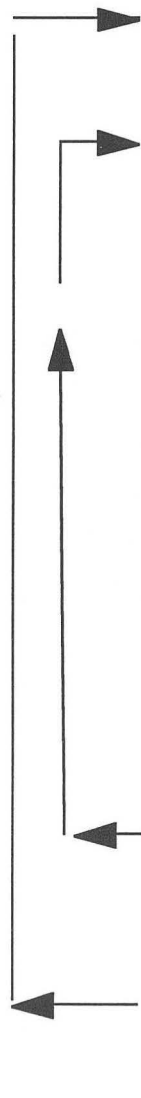


# Conclusions

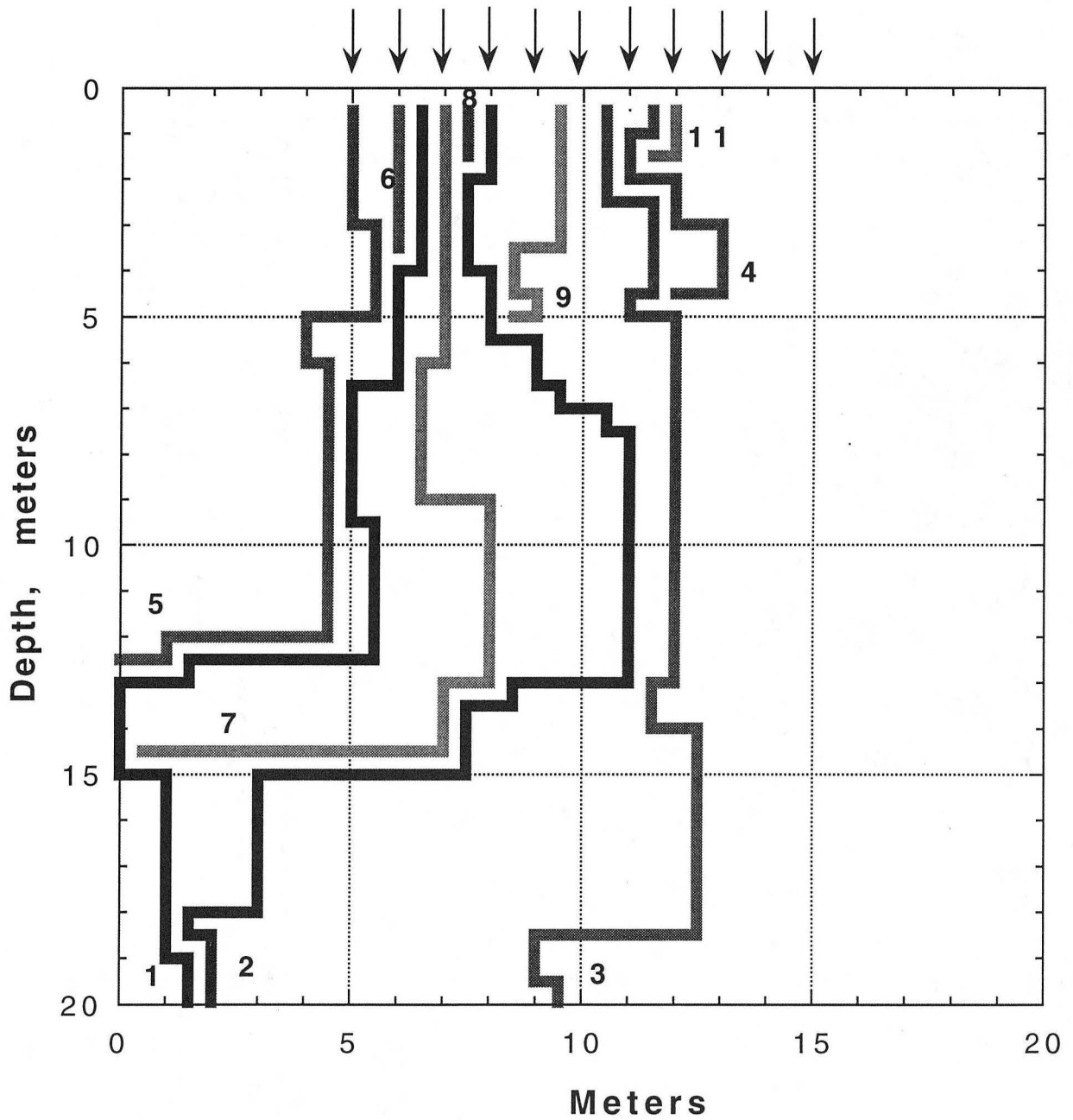
- **simple averaging predictions show sensitivity to initial wells selected**
- **higher resolution sampling does not always lead to a better prediction**
- **simple averaging predictions did not improve after 5 wells were drilled**
- **fractal methods not applicable to this type of problem**
- **neural network approach can help optimize the location and number of wells**

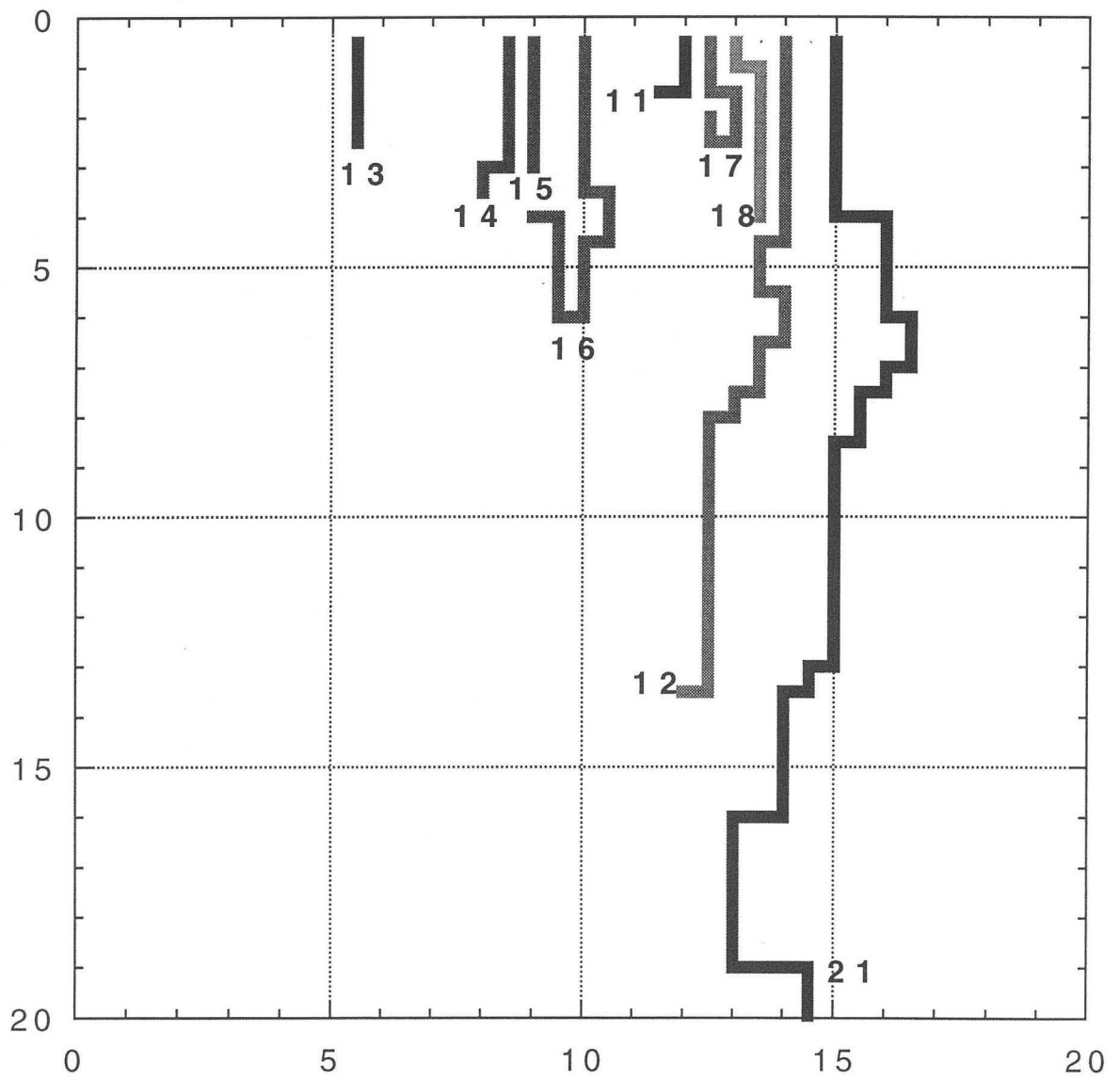
# Pathfinder Code

- **very simple and fast approach to simulating infiltration into complex geometries**
- **complementary to more complex codes such as TOUGH2**
- **easy to modify parameters and initial conditions**
- **given a map of permeabilities, finds the channel of least resistance**

- 
- **Find largest aperture with no water at top boundary(active site); fill with water**
  - **identify nearest neighbors to active site**
    - compute capillary pressures between active site and nearest neighbors
    - compute gravity pressure between active site and nearest neighbors
    - summation of pressures between active site and nearest neighbors
    - identify new active site(the neighbor with the maximum combined capillary and gravity force); fill with water
  - **calculation of area and volume; repeat steps until flow stops (trapping or bottom boundary)**
  - **Return to top boundary; select next largest aperture; continue until no more paths are available or until a designated infiltration volume is exceeded**

# Box Canyon Simulation Infiltration Paths





## II.8

# Tensiometers in Fractured Rock: Experiment and Modeling

*S. Finsterle, B. Faybishenko, and P. Persoff*

*Earth Sciences Division*

*Lawrence Berkeley National Laboratory*

## **Outline**

- Introduction
- Design Calculations
- Experimental Results
- Concluding Remarks

# Motivation

- Fractures are pathways for fast and preferential flow of contaminants.
- Direct measurements of the transient hydraulic response of fracture-matrix systems are needed.
- The interaction between tensiometer and formation should be studied.

# Problems

- Tensiometer tip in fractured rock contacts both fracture and matrix.
- Fracture and matrix are not in equilibrium during transient flow events.
- Gauge water pressure includes matrix and fracture pressure components.
- Porous tip of tensiometer may lead to local redistribution of water.



# Objectives

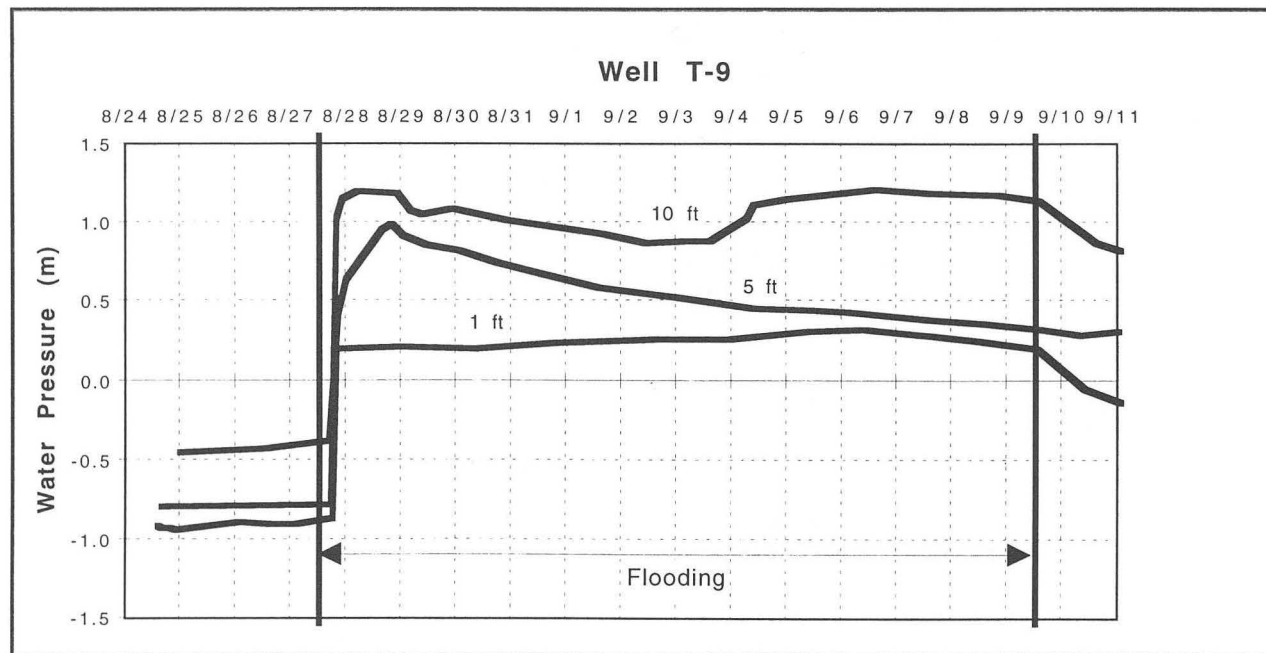
- Study the performance of the tensiometer installed in unsaturated fractured rock under draining and wetting conditions
- Explore the possibilities of deconvolving the observed tensiometer pressure into fracture and matrix components

# Methods

- Analyze field data from tensiometers in fractured formations
- Perform laboratory experiments on fractured core
- Perform numerical simulations of unsaturated flow in fracture-matrix system, including interaction with tensiometer

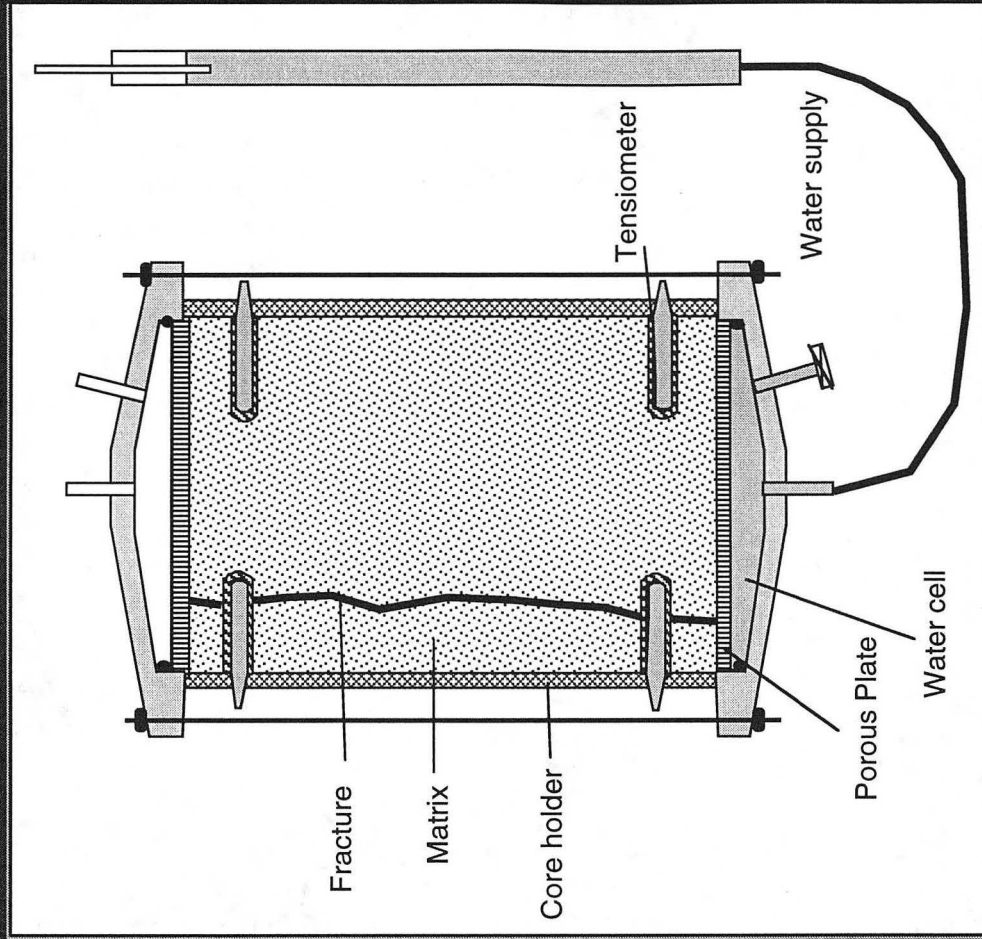
# Field Experiment

- Tensiometer measurements at three different depths prior to and during ponded infiltration experiment in fractured basalt (Box Canyon Site, INEEL)
- Immediate pressure response to infiltration at all depth
- Slow pressure response to drainage



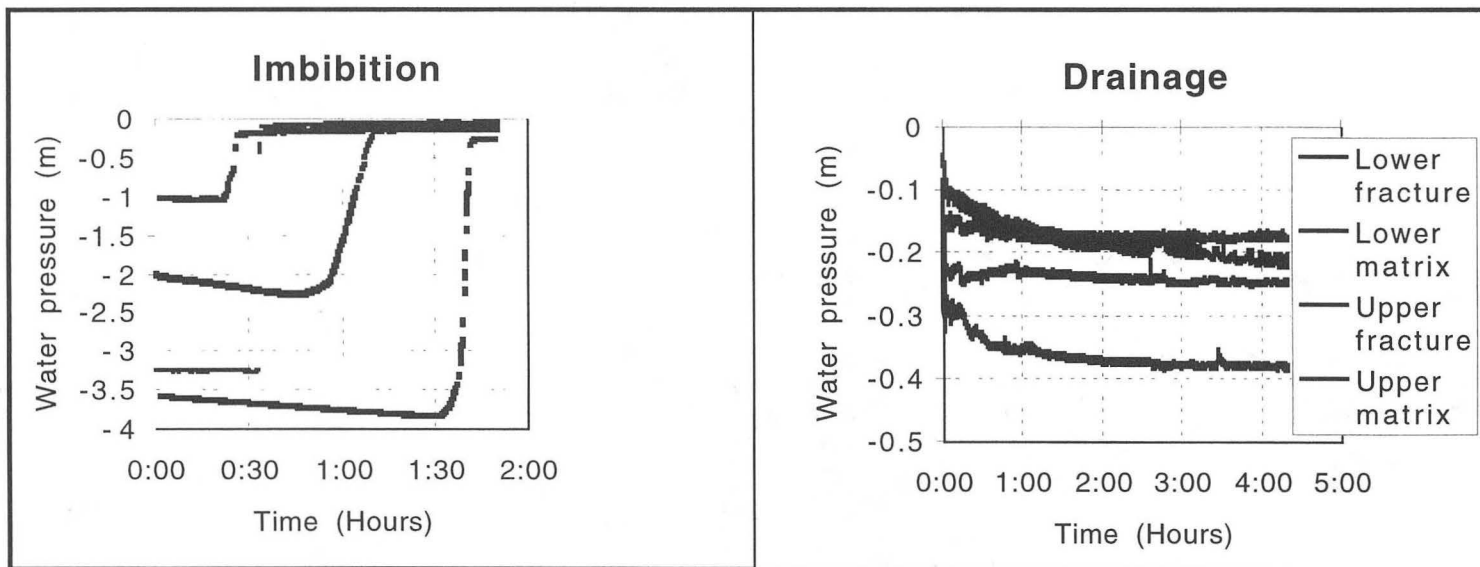
# Laboratory Experiment

- Fractured core in flow cell for drainage and imbibition experiment
- Tensiometers installed in matrix and intersecting fracture at two levels

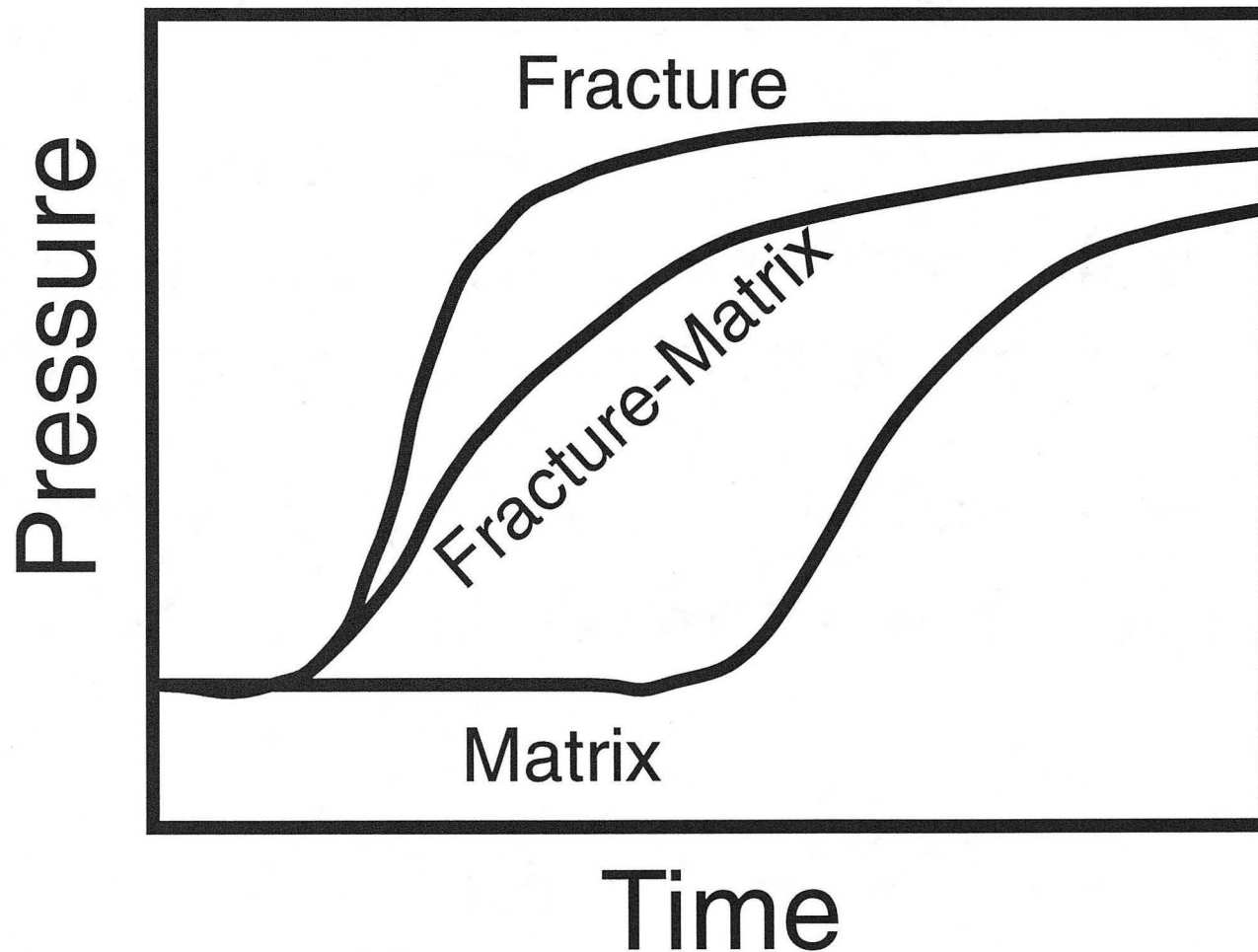


# Imbibition and Drainage in Fractured Basalt Core

- During imbibition, the response of the fracture tensiometers is fast, followed by transient effects caused by water imbibition into the matrix. During drainage, the responses of the fracture and matrix tensiometers are identical because the fracture is drained immediately.
- The presence of a fracture leads to a strong hysteretic behavior in the observed water pressure.



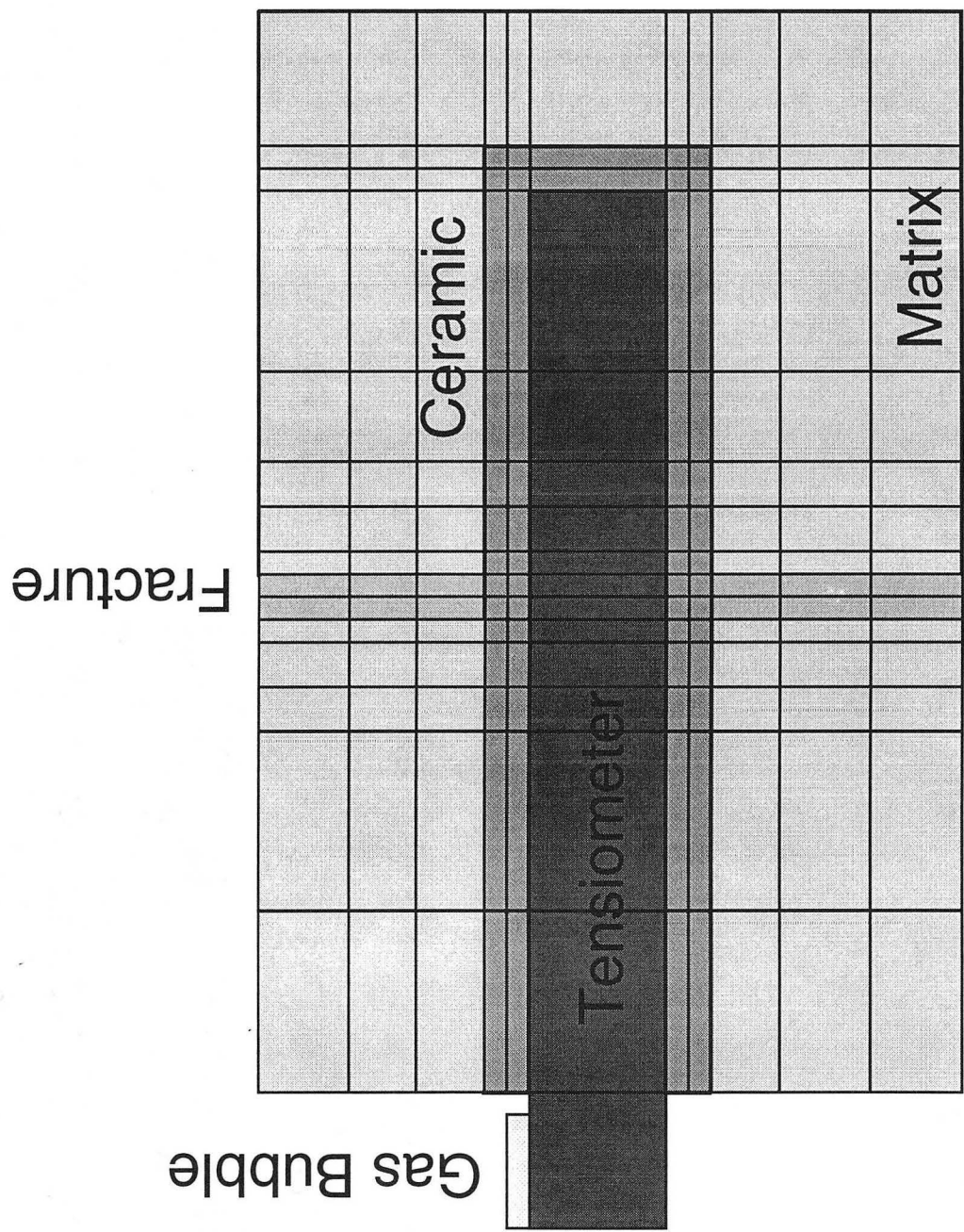
# Tensiometer in Fracture-Matrix System During Imbibition



# Modeling Approach

- Simulation of two-phase flow (gas and liquid) in fracture-matrix system.
- Accurate representation of air-pocket tensiometer (ceramic cup, water-filled tubing, air bubble)
- Initial drainage from both sides for ten days under -0.9 bars of suction, followed by ponded imbibition from top for ten days.

# Discretization of Tensiometer





# Modeling Approach (cont.)

- Examination of saturation distribution and flow patterns during drainage and imbibition.
- Examination of pressure in fracture and matrix; comparison with pressure in tensiometer air bubble.
- The calculations were performed with the TOUGH2 simulator for multi-phase, multi-component flow in porous media.

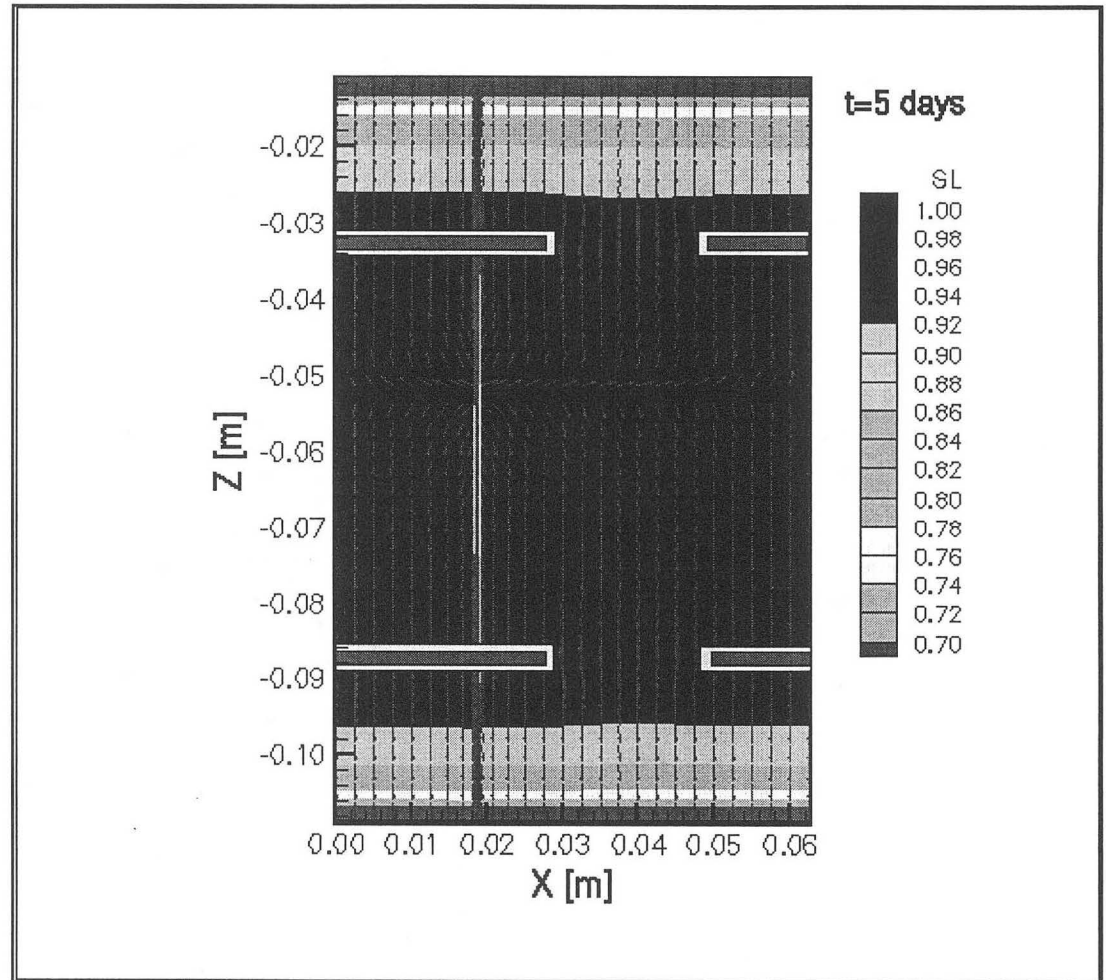
# Parameter Set

Parameter	Matrix	Fracture
permeability $k$ , $m^2$	5.00E-17	1.00E-12
matrix porosity	0.23	-
fracture aperture, $\mu m$	-	1.00E+02
van Genuchten $\alpha$ , $Pa^{-1}$	3.84E-04	5.43E-02
van Genuchten $n$	1.47	1.47

# Drainage

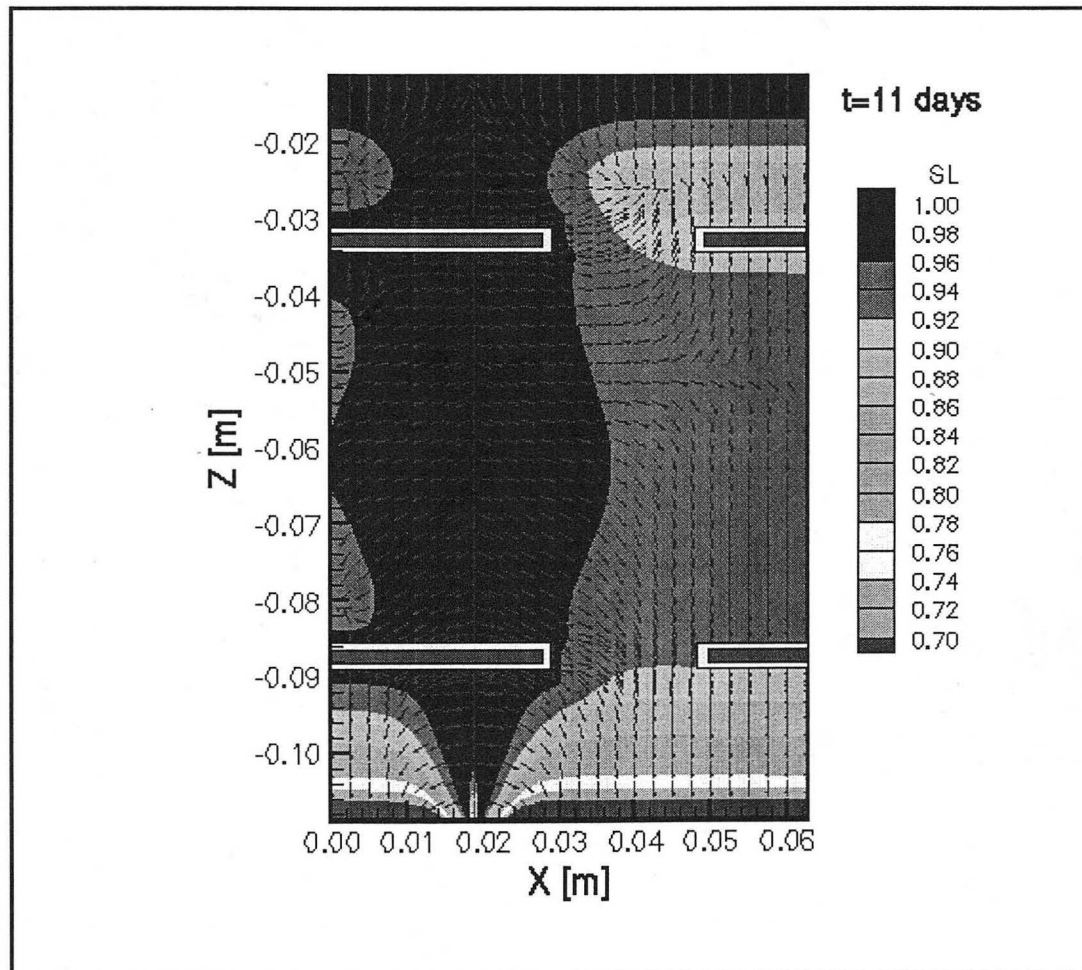
The fracture drains immediately. Drying progresses inward from both ends. The flow field is slightly affected by the presence of the tensiometer.

198

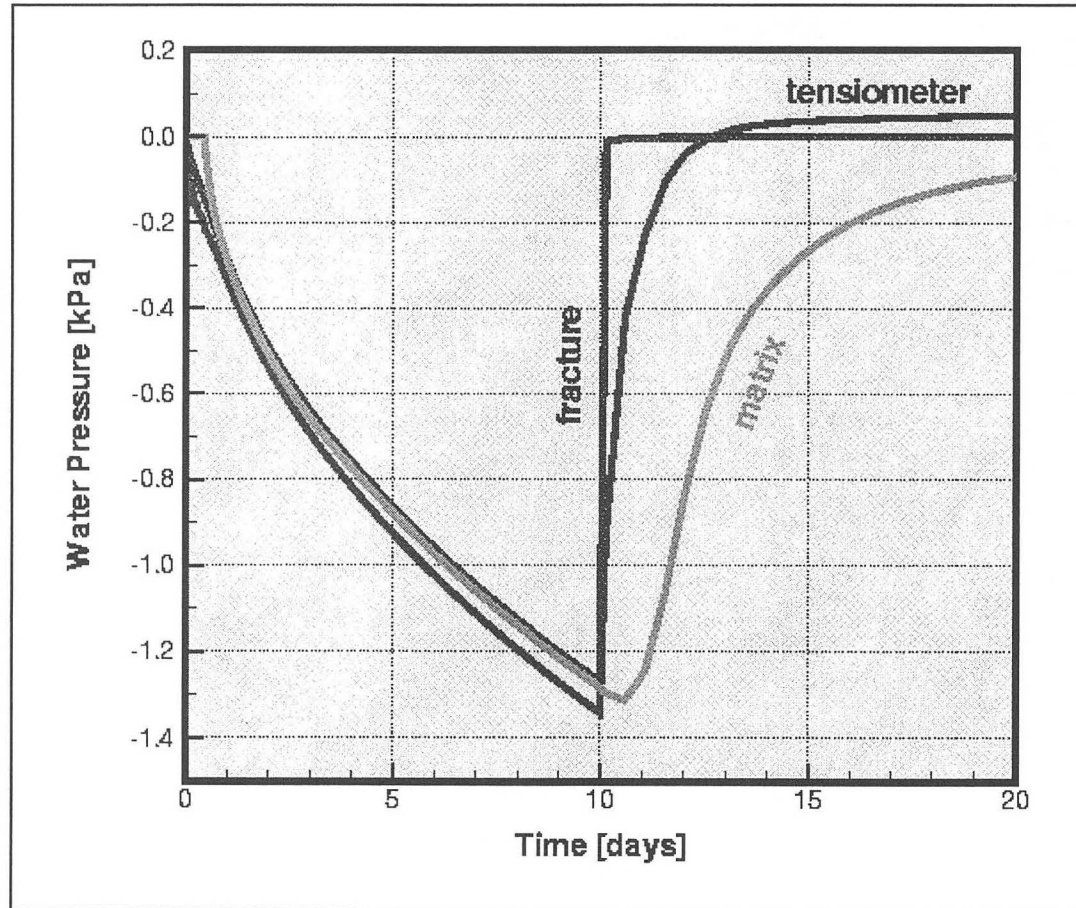


# Imbibition

Imbibition progresses from the fracture into the matrix and axially from the top. The flow field is slightly affected by the presence of the tensiometer.



# Fracture, Matrix, and Tensiometer Pressure



# Conclusions

- The presence of a measuring device in a formation affects the system behavior to be monitored.
- It is therefore necessary to study the interaction between the sensor and the formation to correctly interpret the observed pressure.

## Conclusions (cont.)

- The gauge pressure is primarily affected by the conducting component that transmits water into or out of the ceramic cup of the tensiometer.
- During drying, the gauge pressure is mostly affected by the matrix pressure; during wetting, it is dominated by the fracture pressure.
- The presence of a fracture leads to hysteresis

## II.9

### **2-D modeling of the ERT performance to predict fracture geometry**

**Jeong-Seok Yang**

Purpose of this research:

fracture imaging

resolution of result

different fracture combination modeling



# Forward Modeling

## Generate Synthetic Data

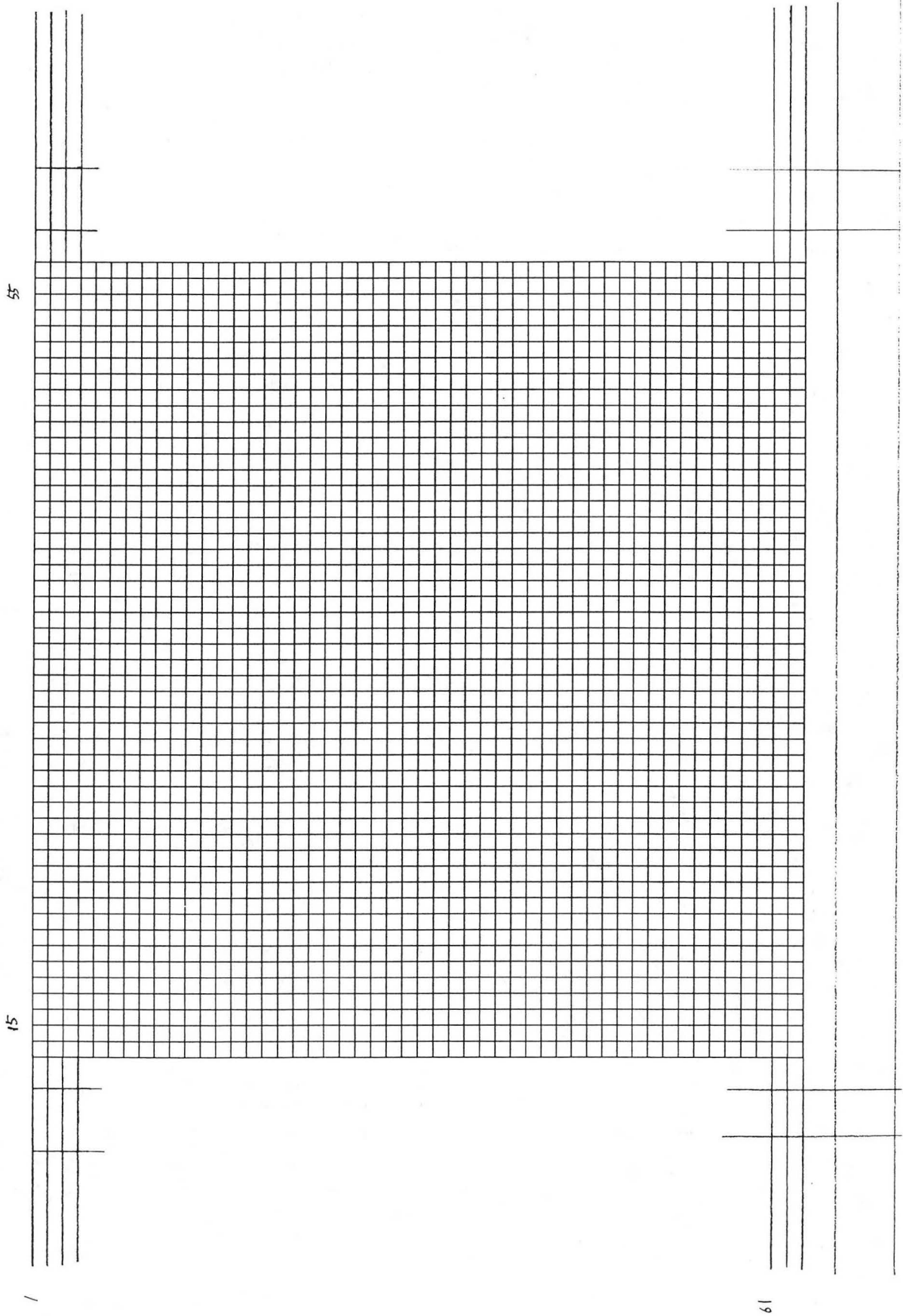
Background Resistivity Value: 1000 Ohm-m

Conductive Zone Resistivity Value: 50 Ohm-m

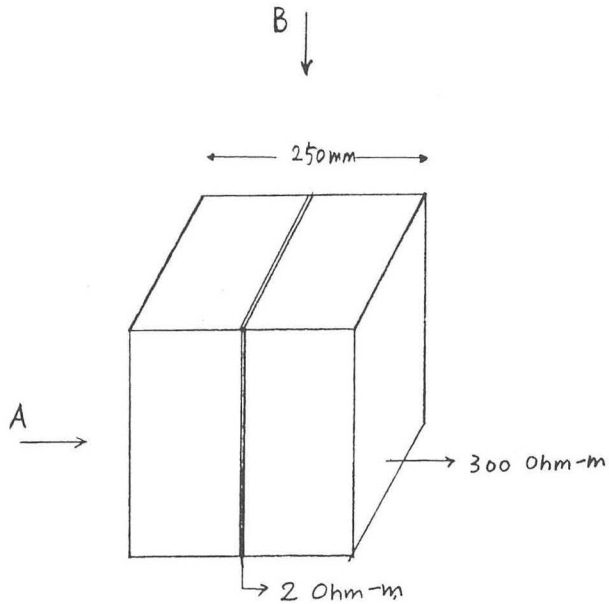
Pole-Pole array was used for the Modeling

# 2-D ERT Modeling

Grid used in the Modeling



# Equivalent Resistivity Values for a Cube contains a Fracture



A.  $\rho_E =$  298.8 Ohm-m (1 mm)  
 288.8 Ohm-m (1 cm)  
 (arithmetic mean)

B.  $\rho_E =$  188.0 Ohm-m (1 mm)  
 43.10 Ohm-m (1 cm)  
 (harmonic mean)

1 mm fracture thickness: normal fracture

1 cm fracture thickness: rubble zone

# Conclusion

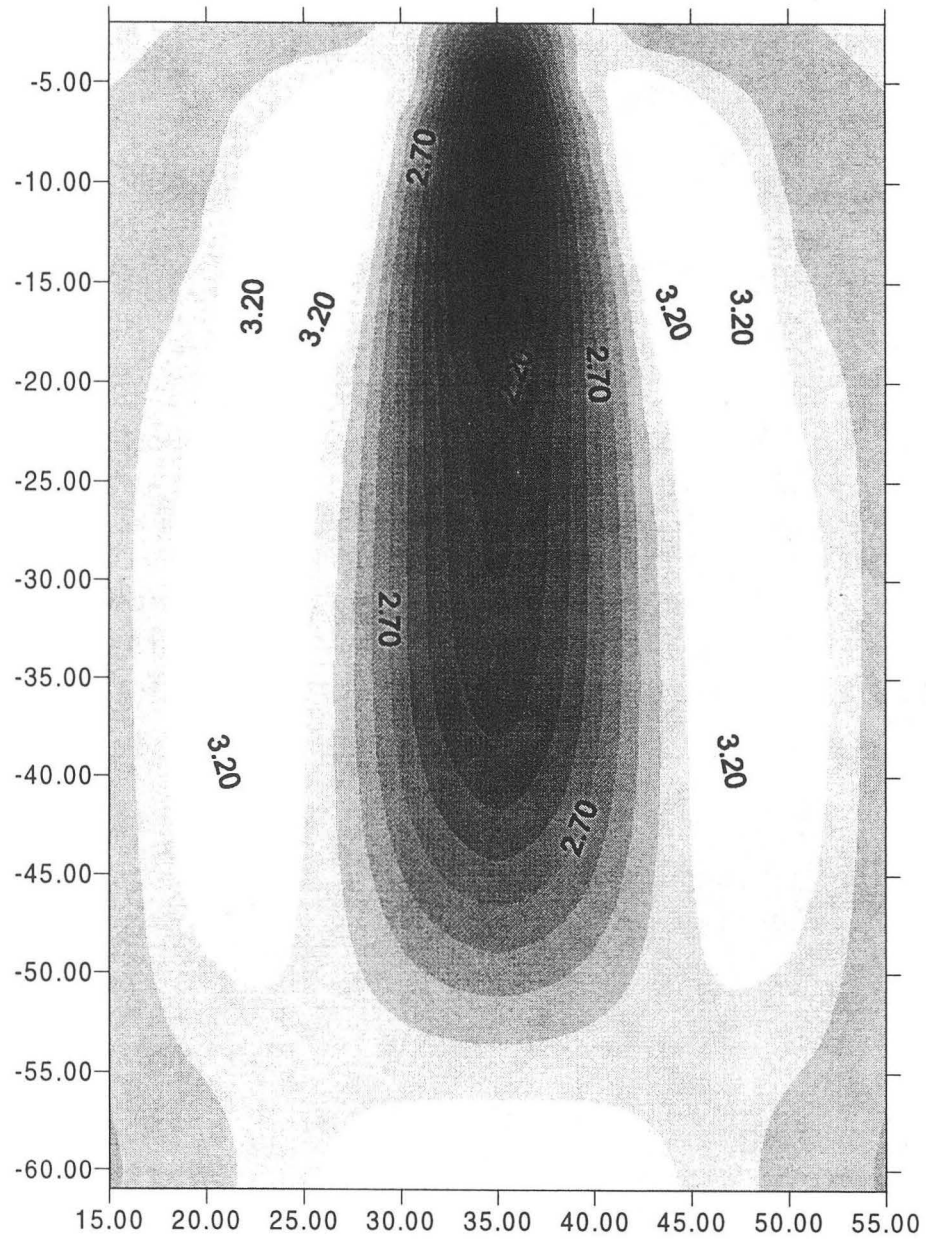
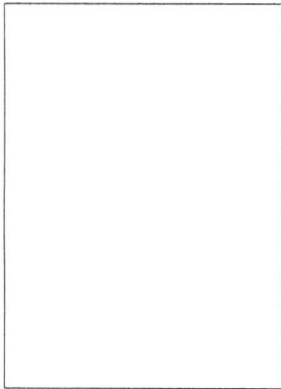
We can have rough information about fracture geometry.

The prediction of the complex geometry of fracture is difficult.

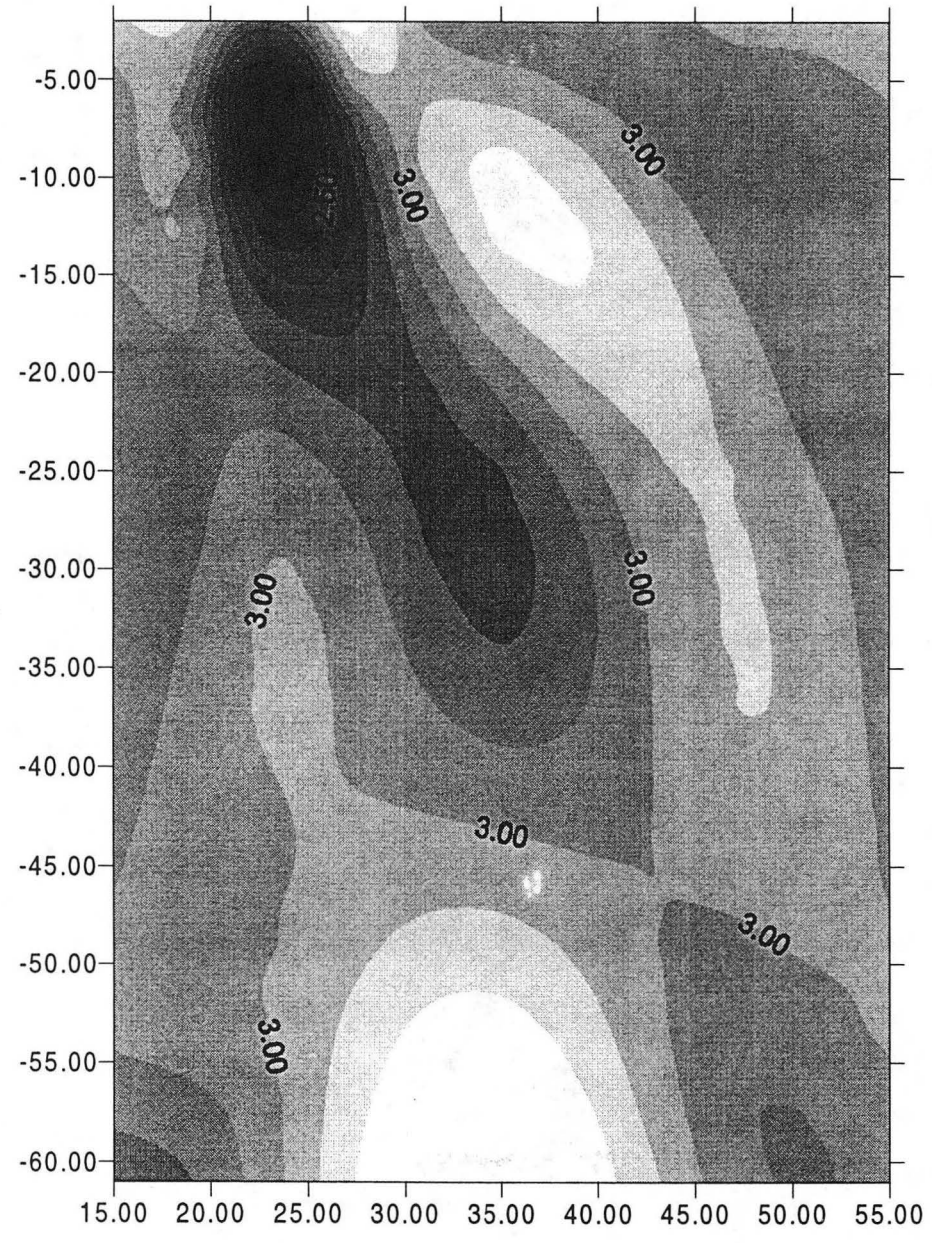
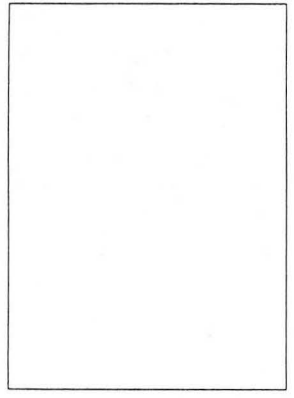
The resolution for shallow depth is good due to surface electrodes.

The bottom part of the inversion result is not reliable.

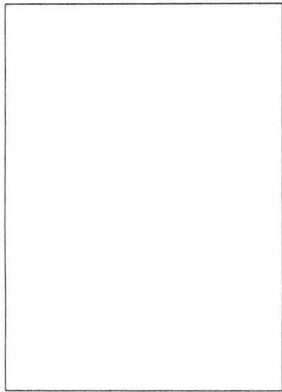
p-1.out  
(34 36 1 71)



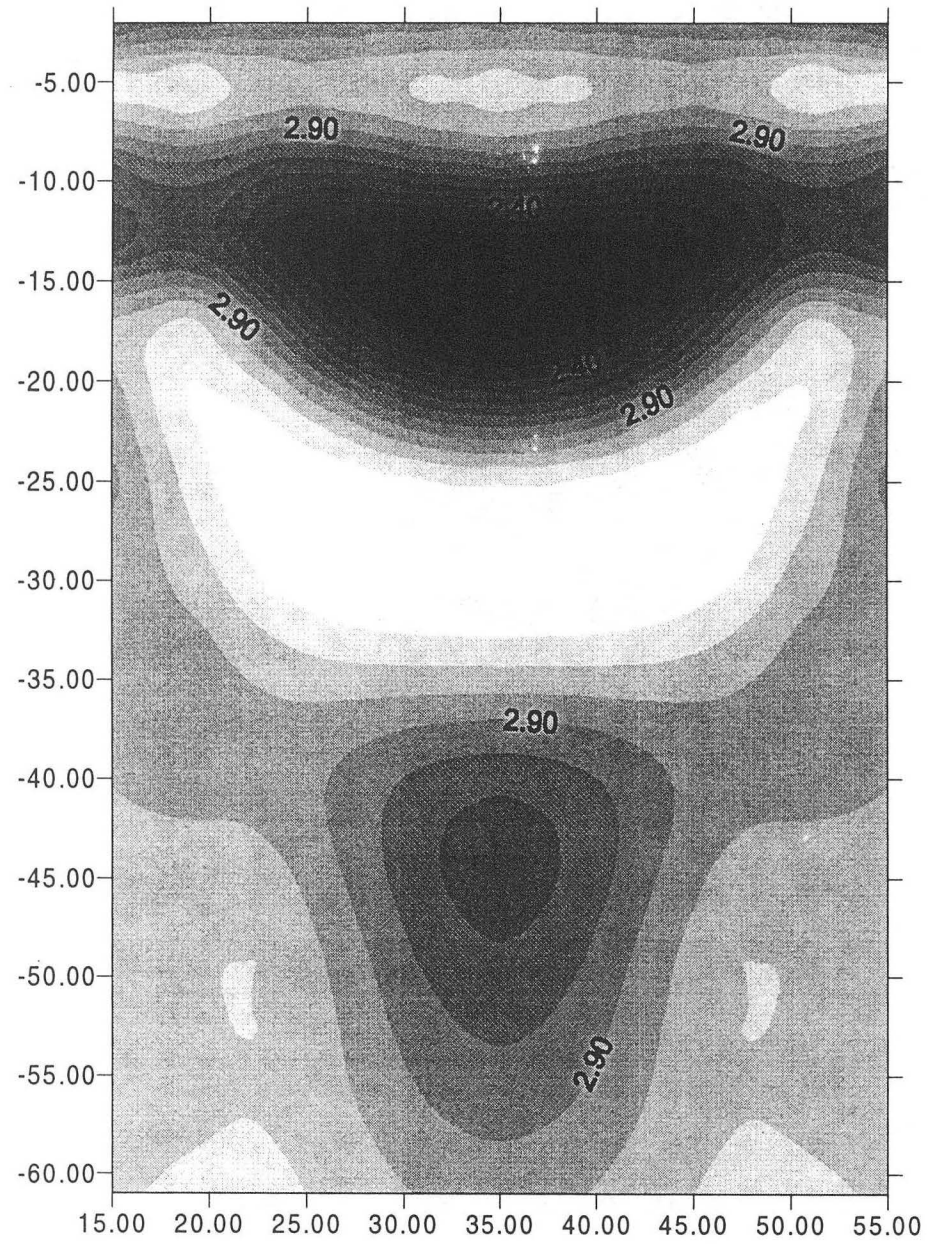
p-2.out  
(22 23 1 71)



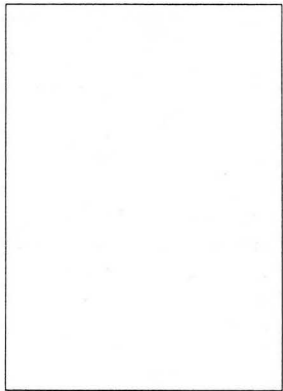
p-3.out  
(5 65 9 10)



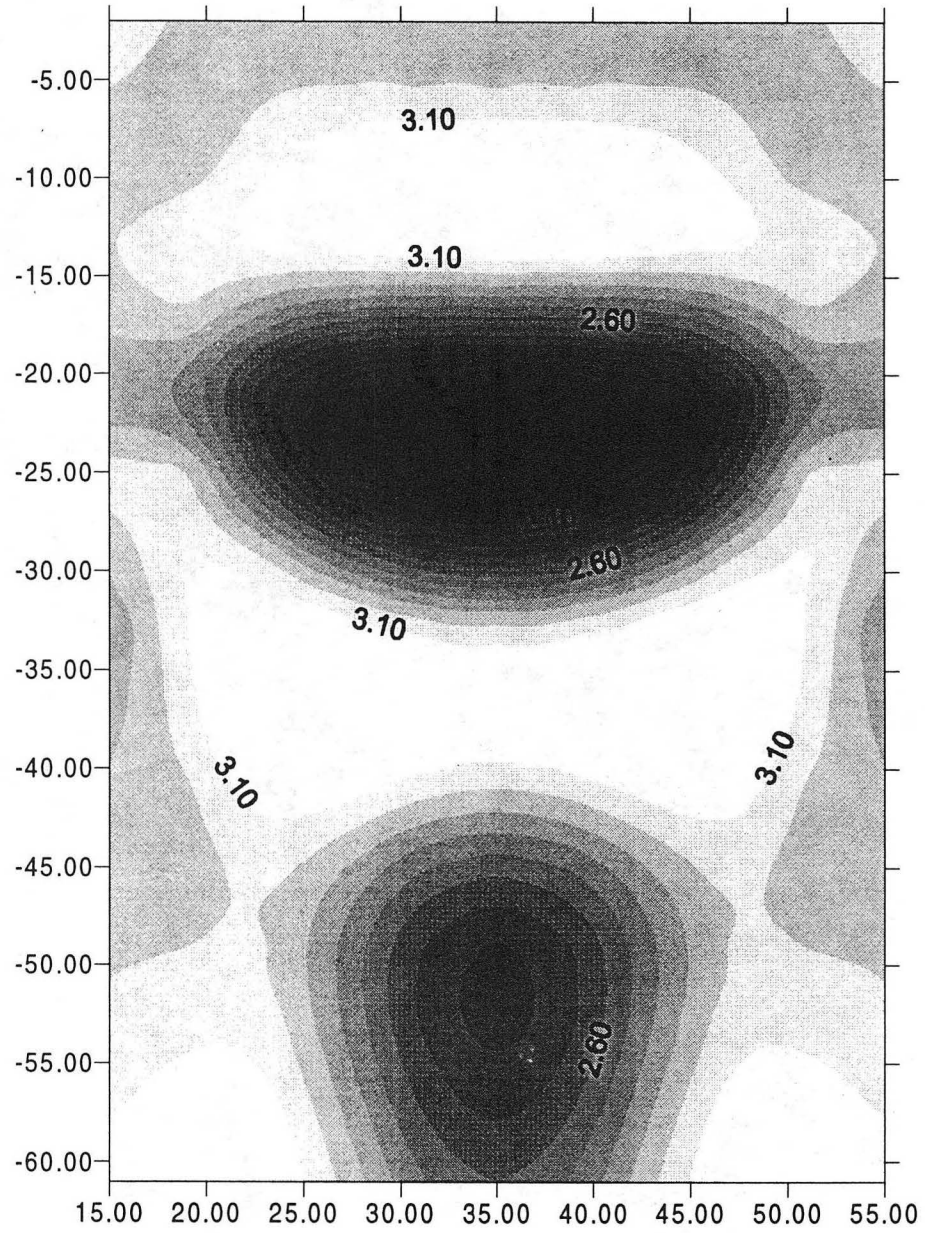
210



p-4.out  
(5 65 20 21)

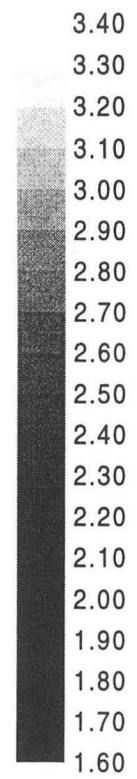
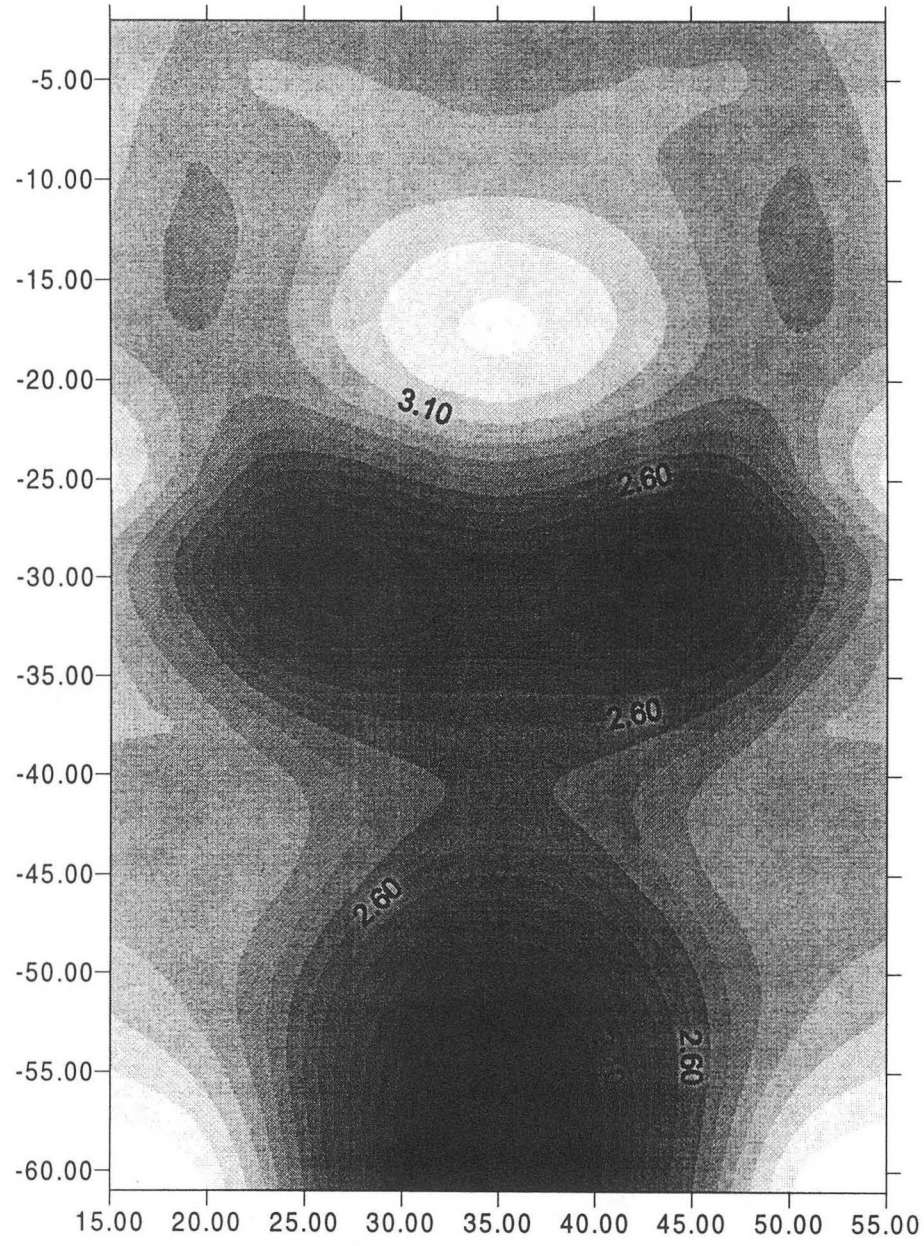
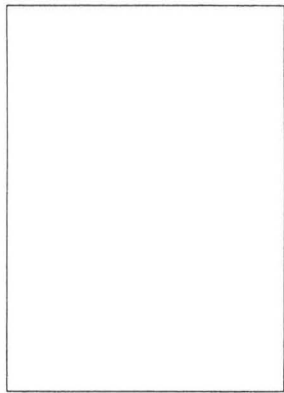


211

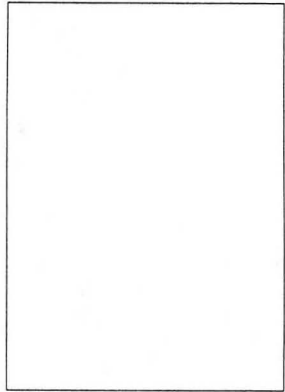




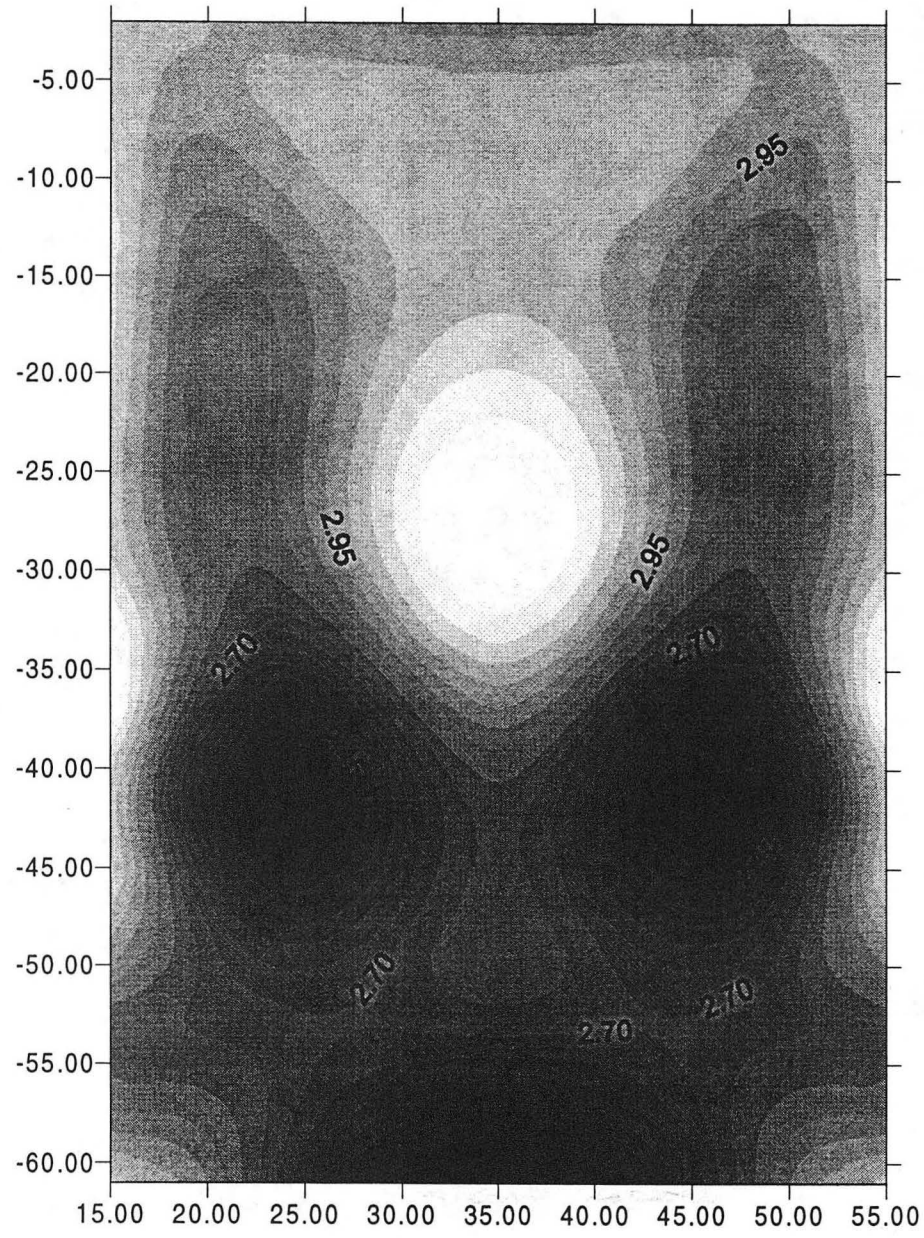
p-5.out  
(5 65 29 30)



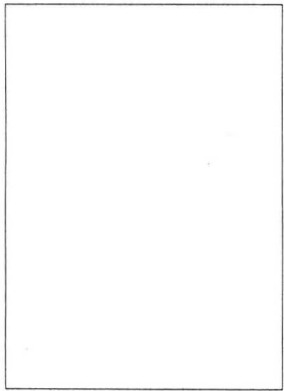
p-6.out  
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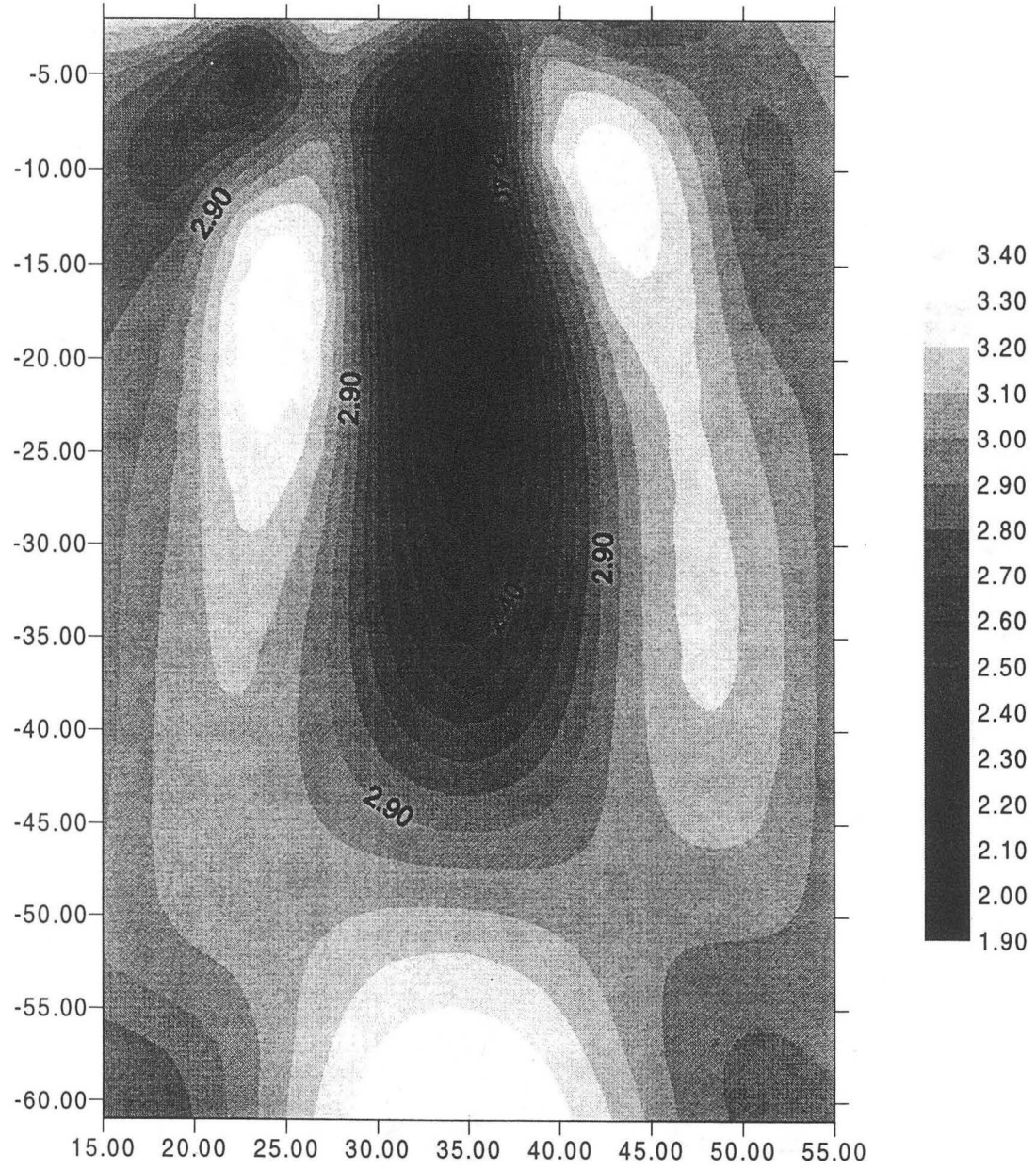
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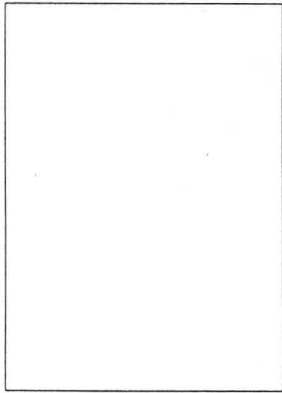
p-7.out  
(34 35 1 71)  
(22 23 1 71)



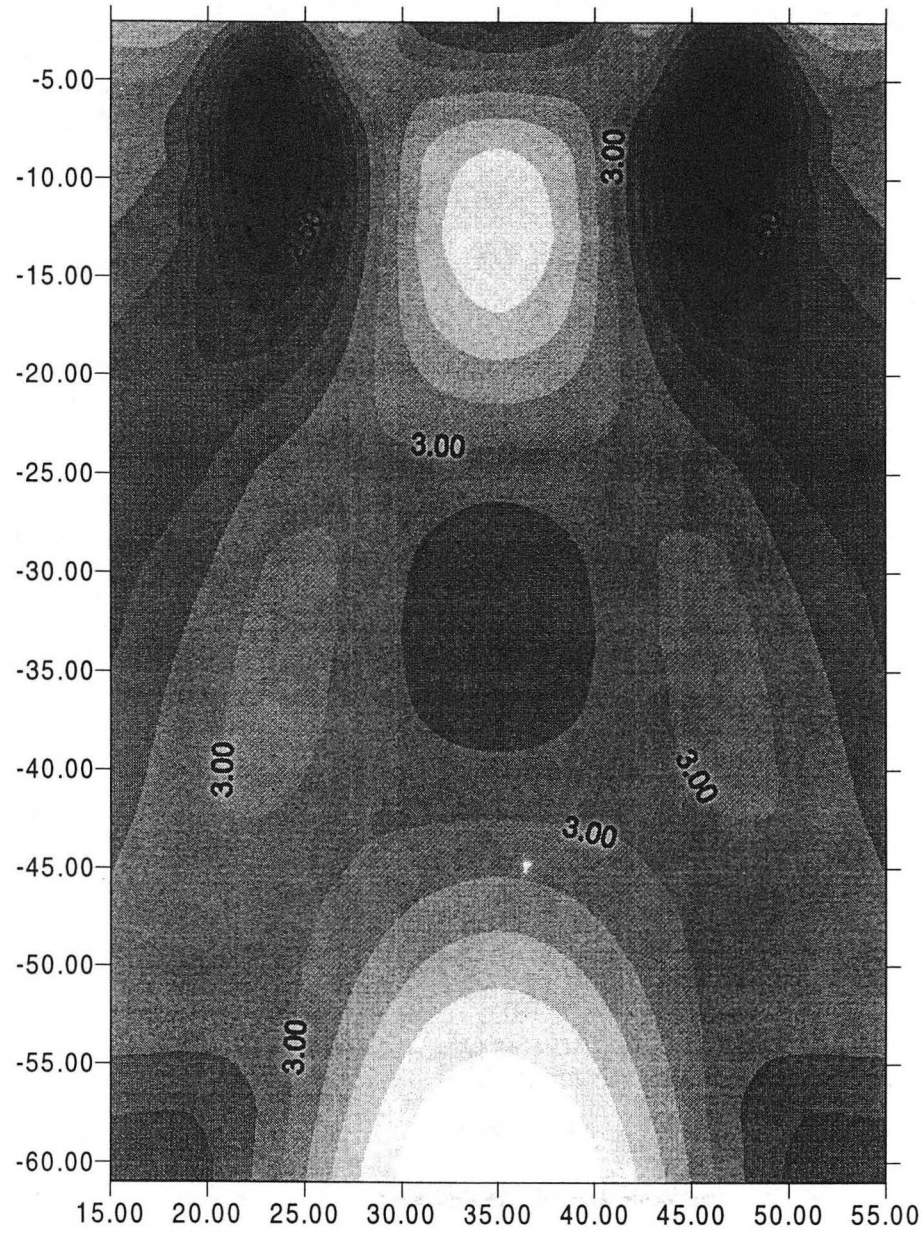
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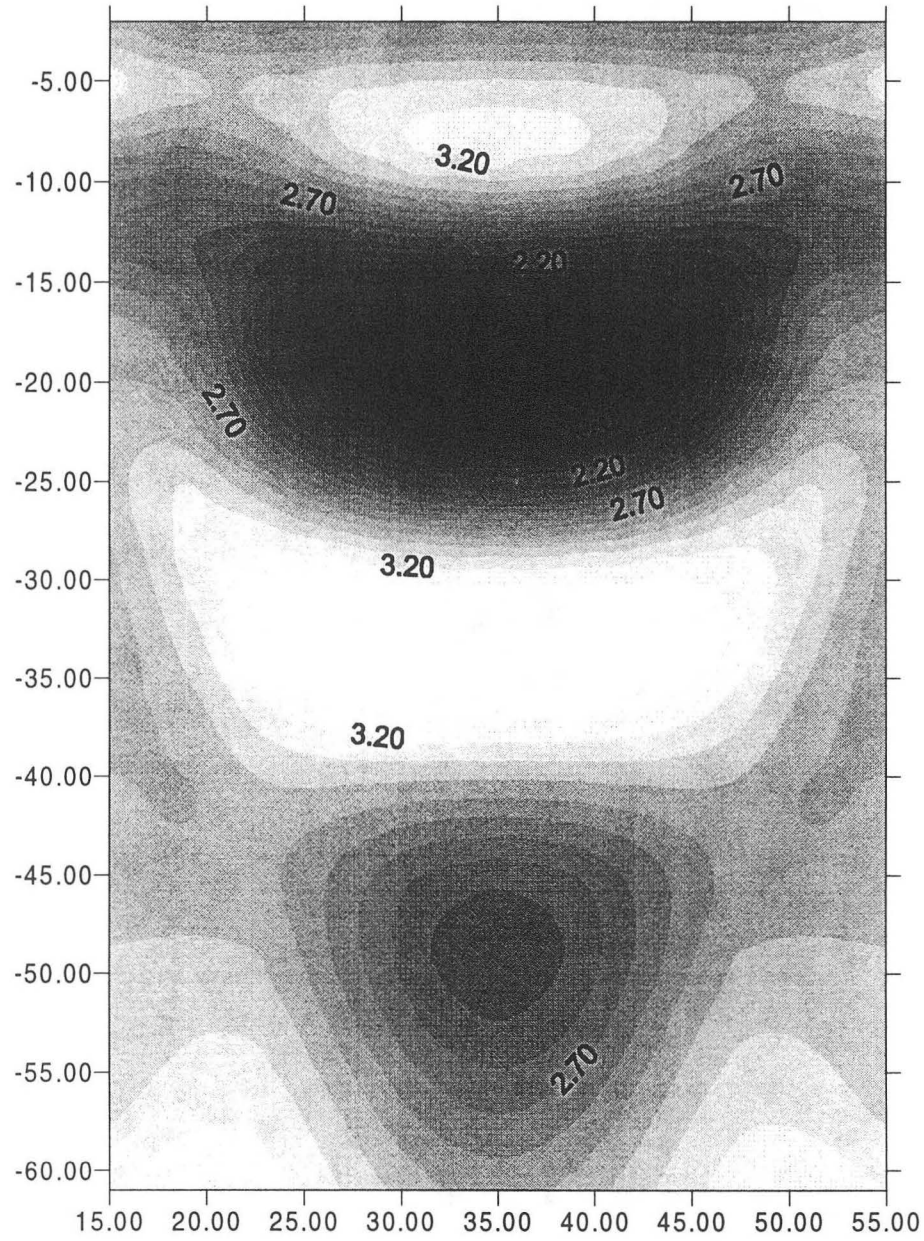
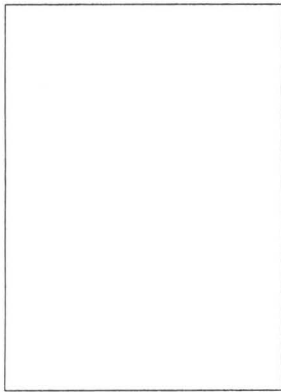
p-8.out  
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(47 48 1 71)



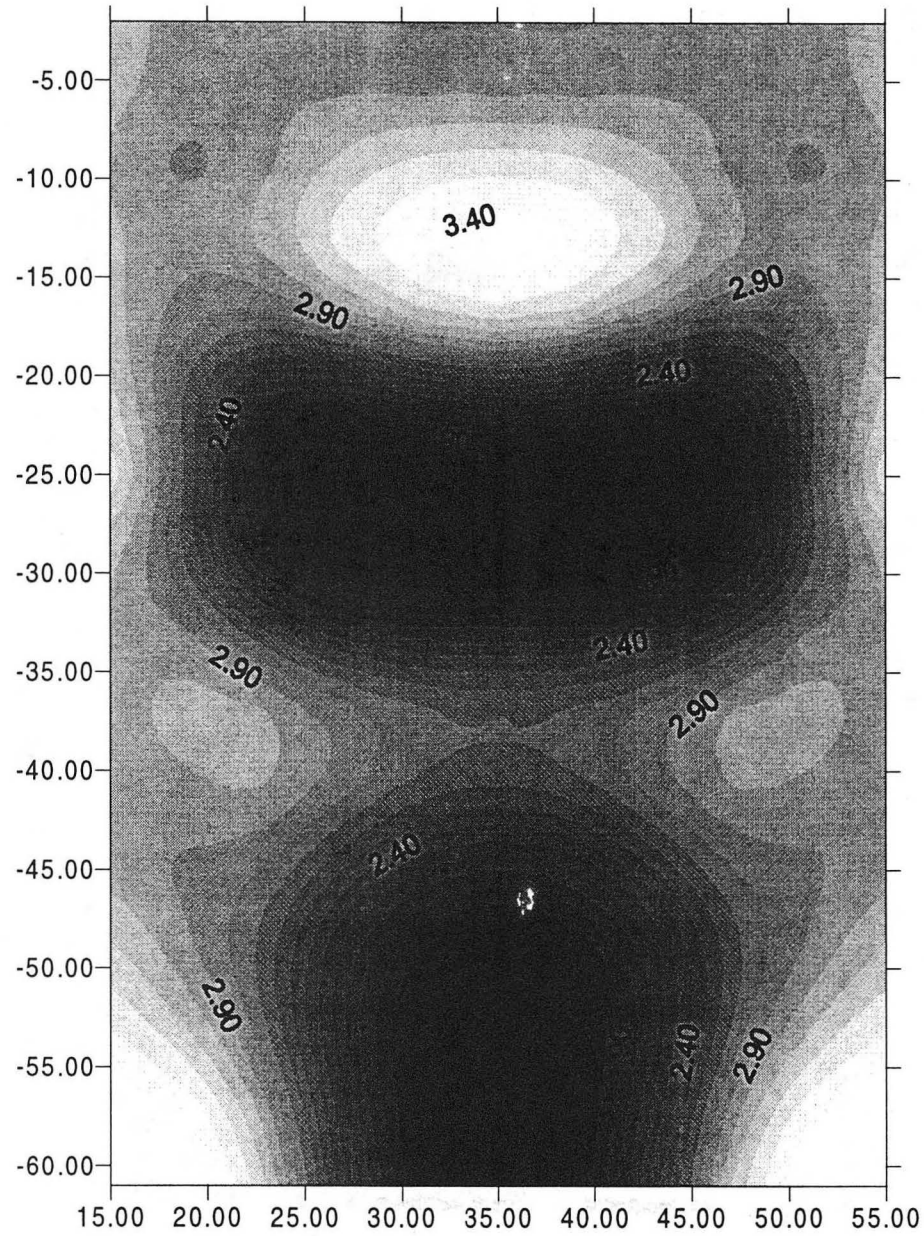
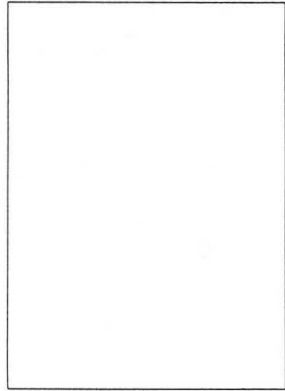
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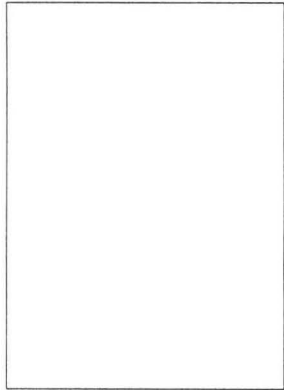
p-9.out  
(5 65 9 10)  
(5 65 20 21)



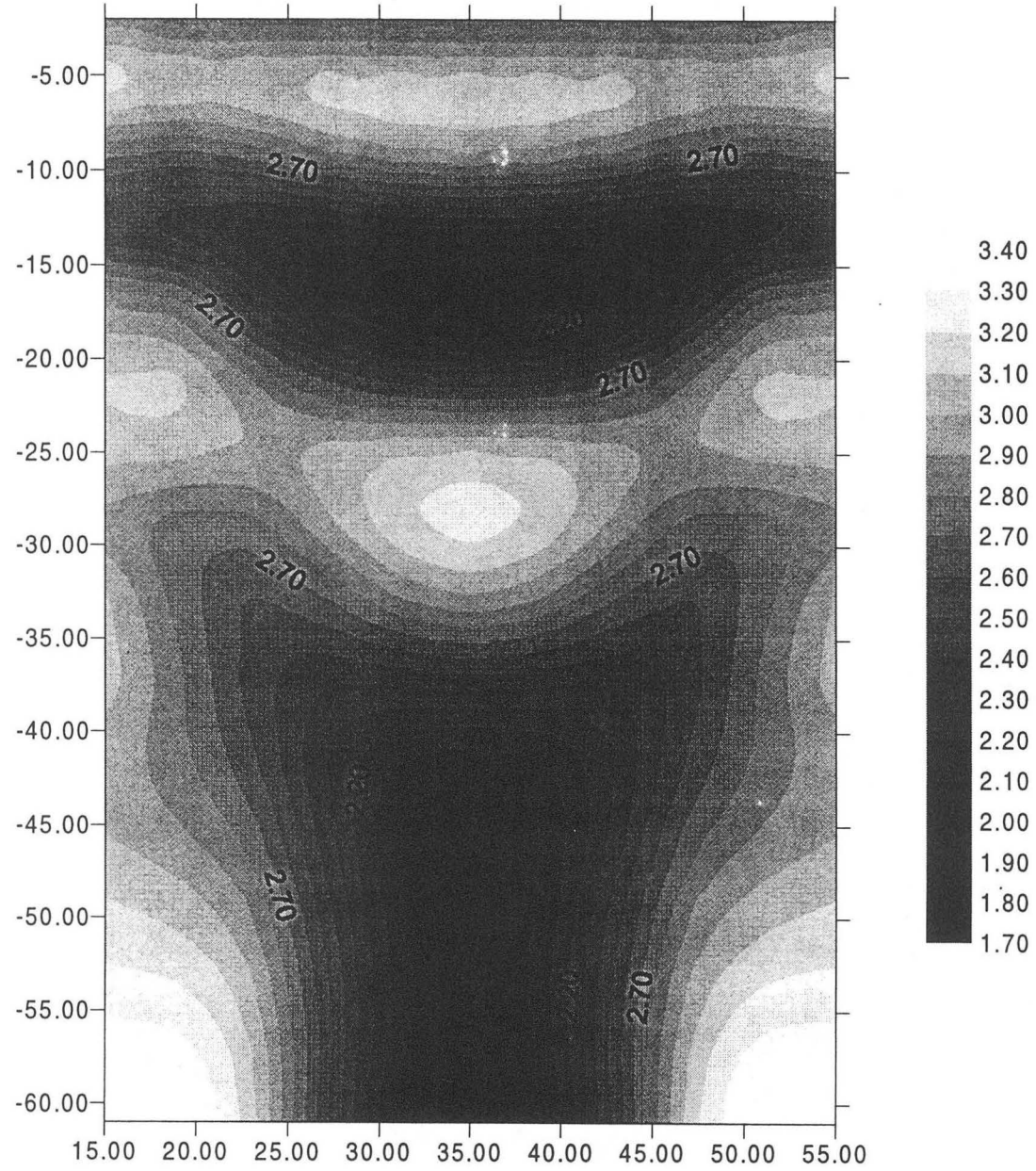
p-10.out  
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(5 65 29 30)



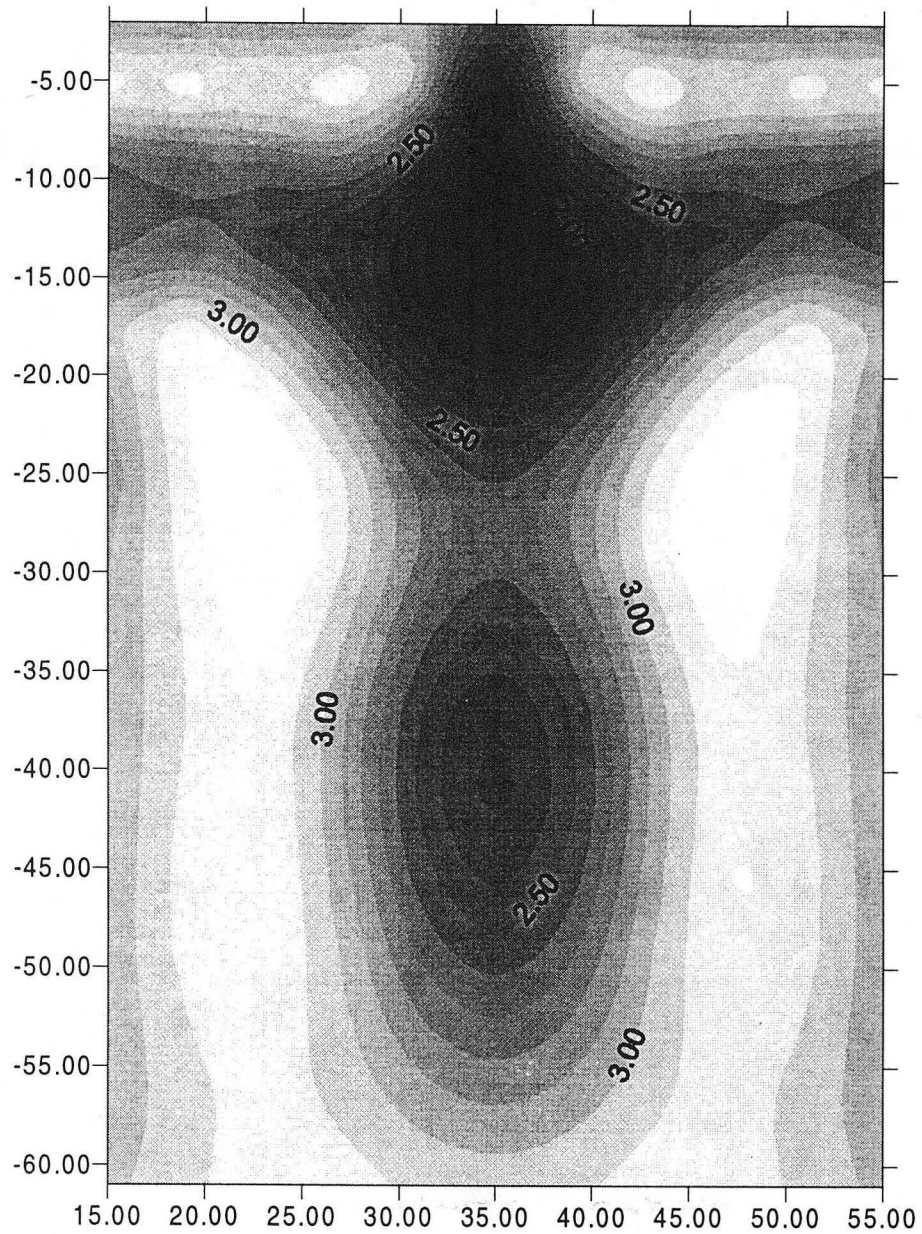
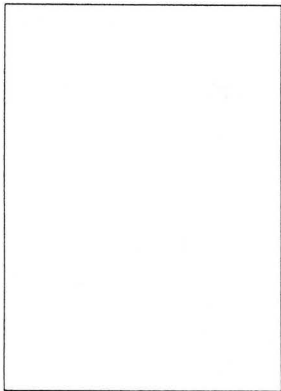
p-11.out  
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(5 65 29 30)



218

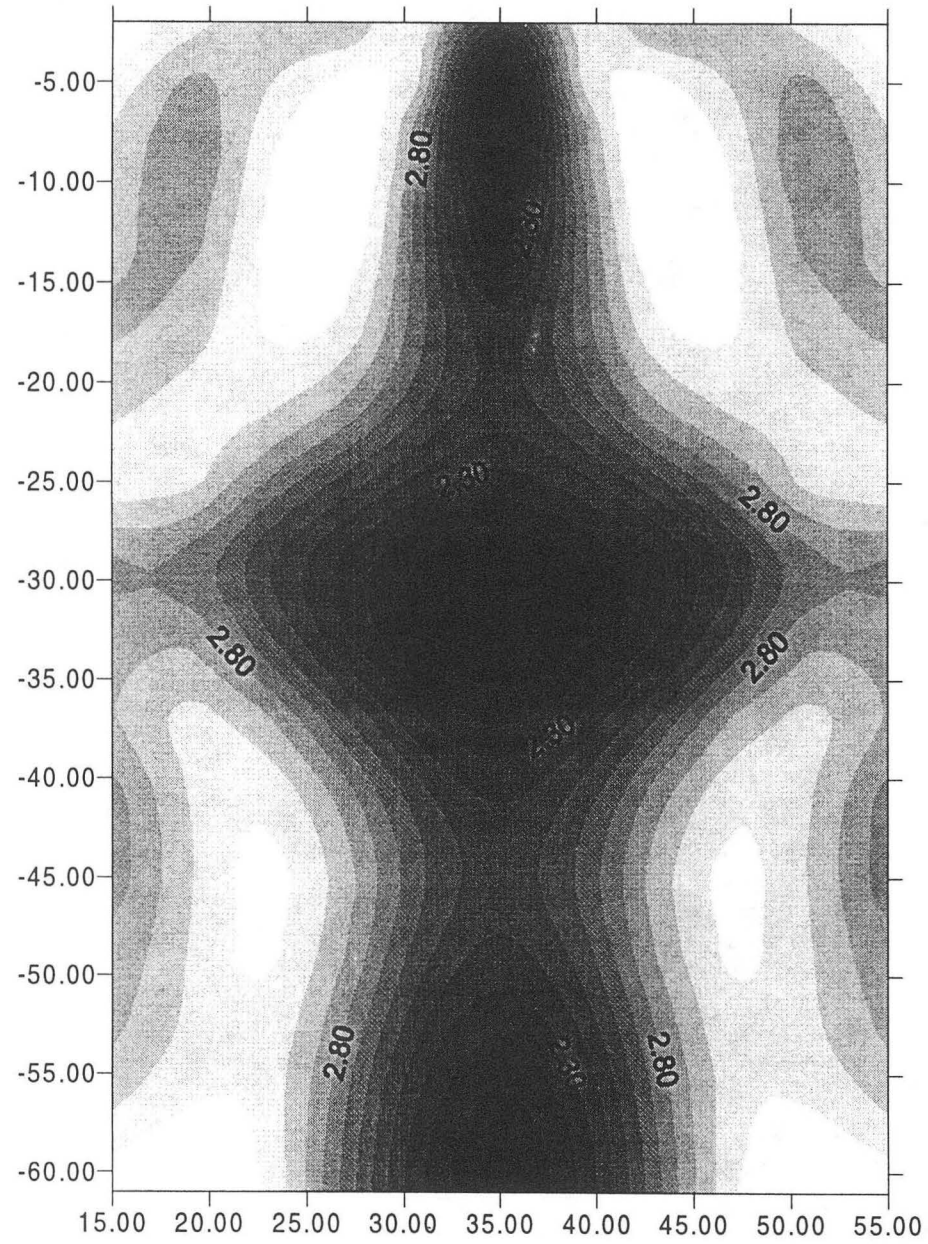
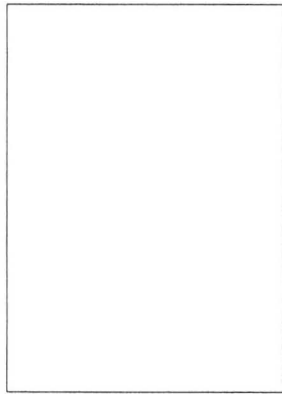


pp1.out  
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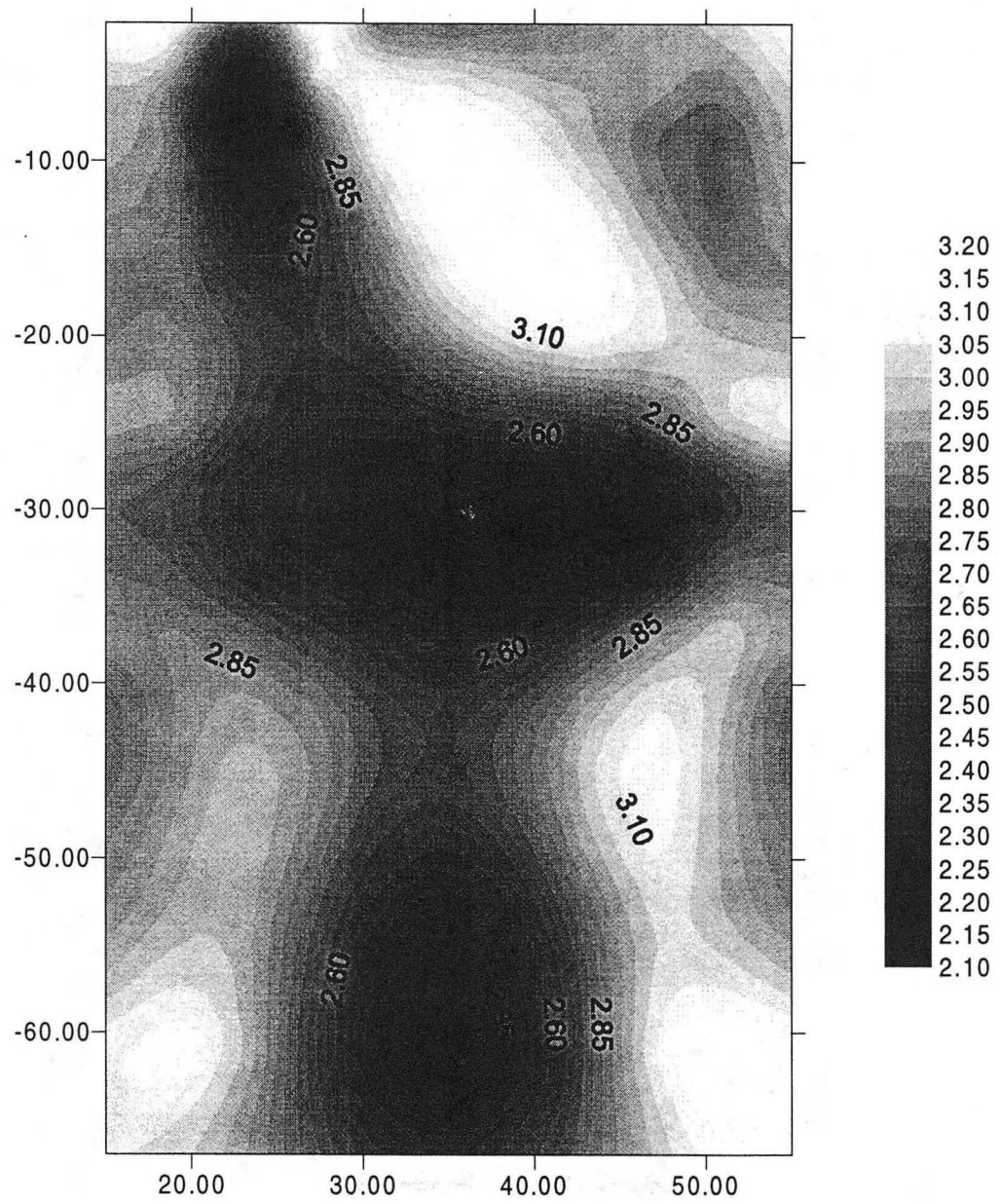




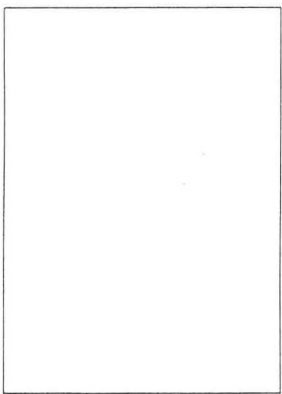
pp2.out  
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(5 65 29 30)



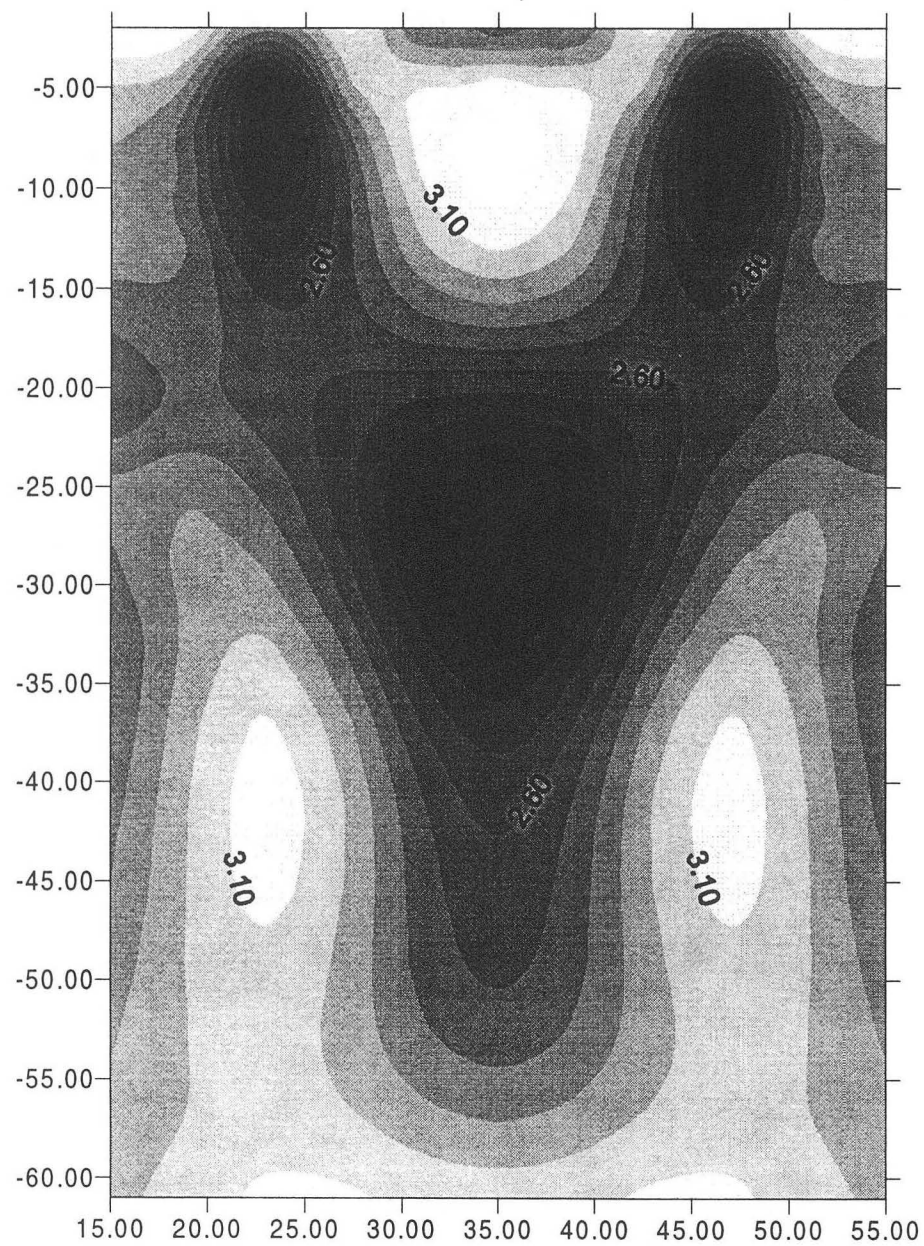
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(5 65 29 30)



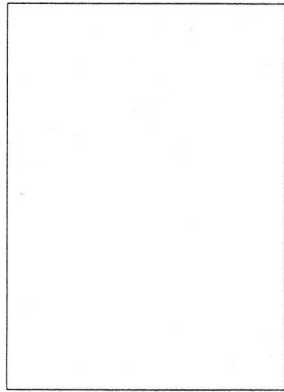
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(5 65 20 21)



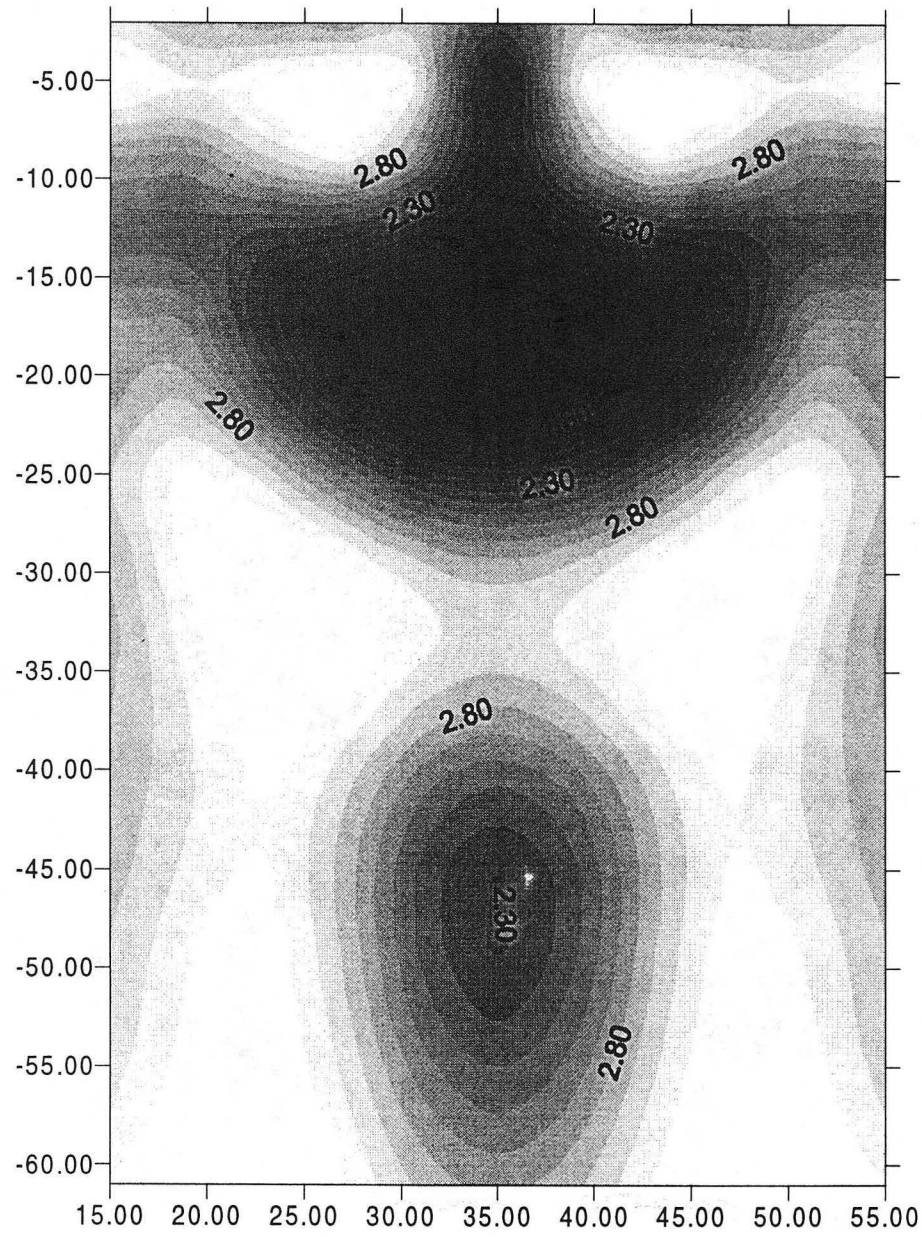
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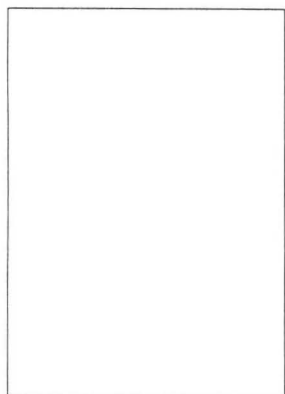
pp5.out  
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(5 65 20 21)



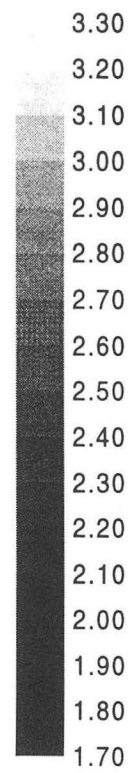
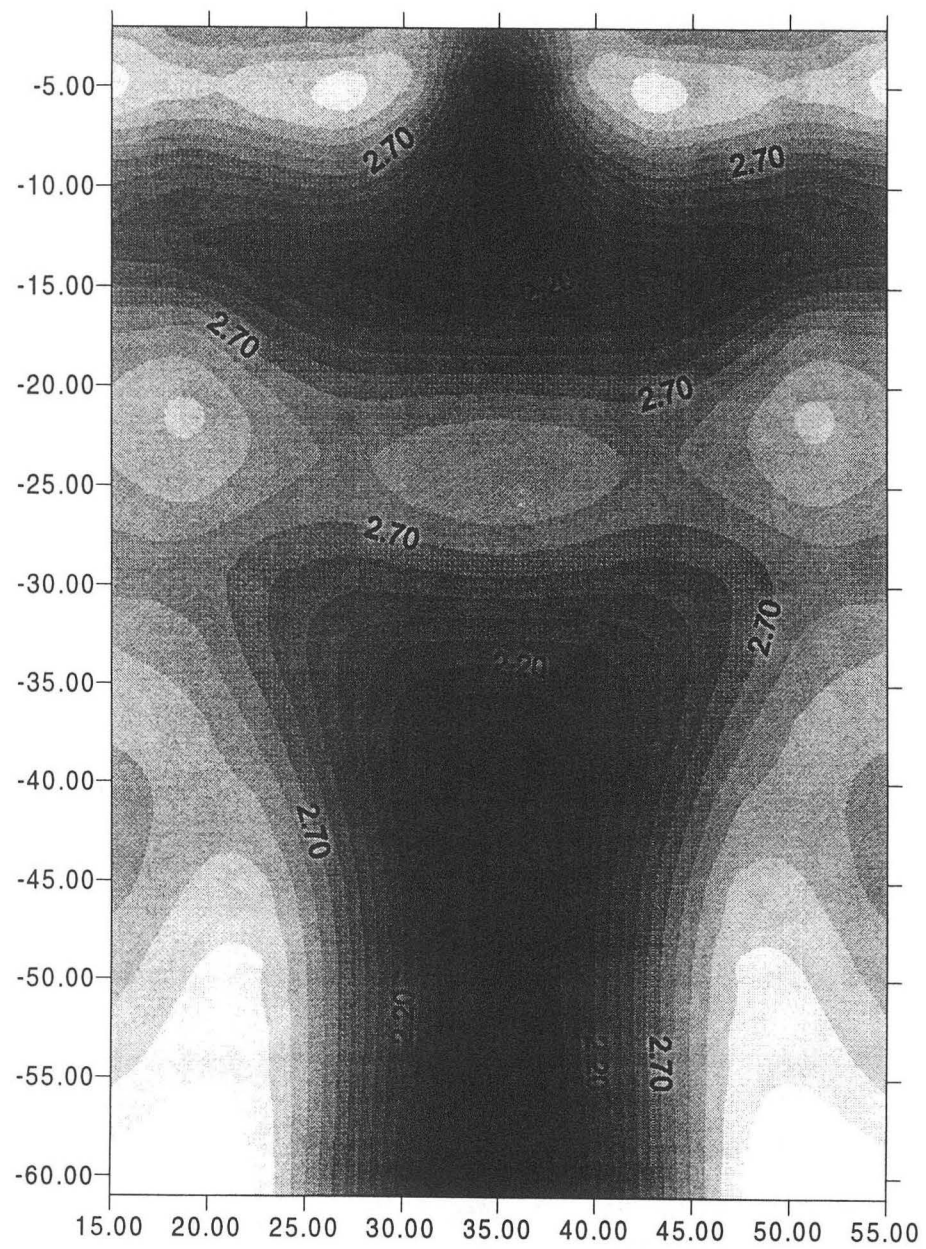
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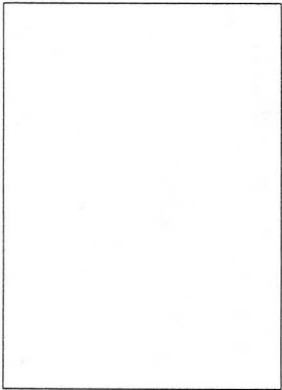
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(5 65 29 30)



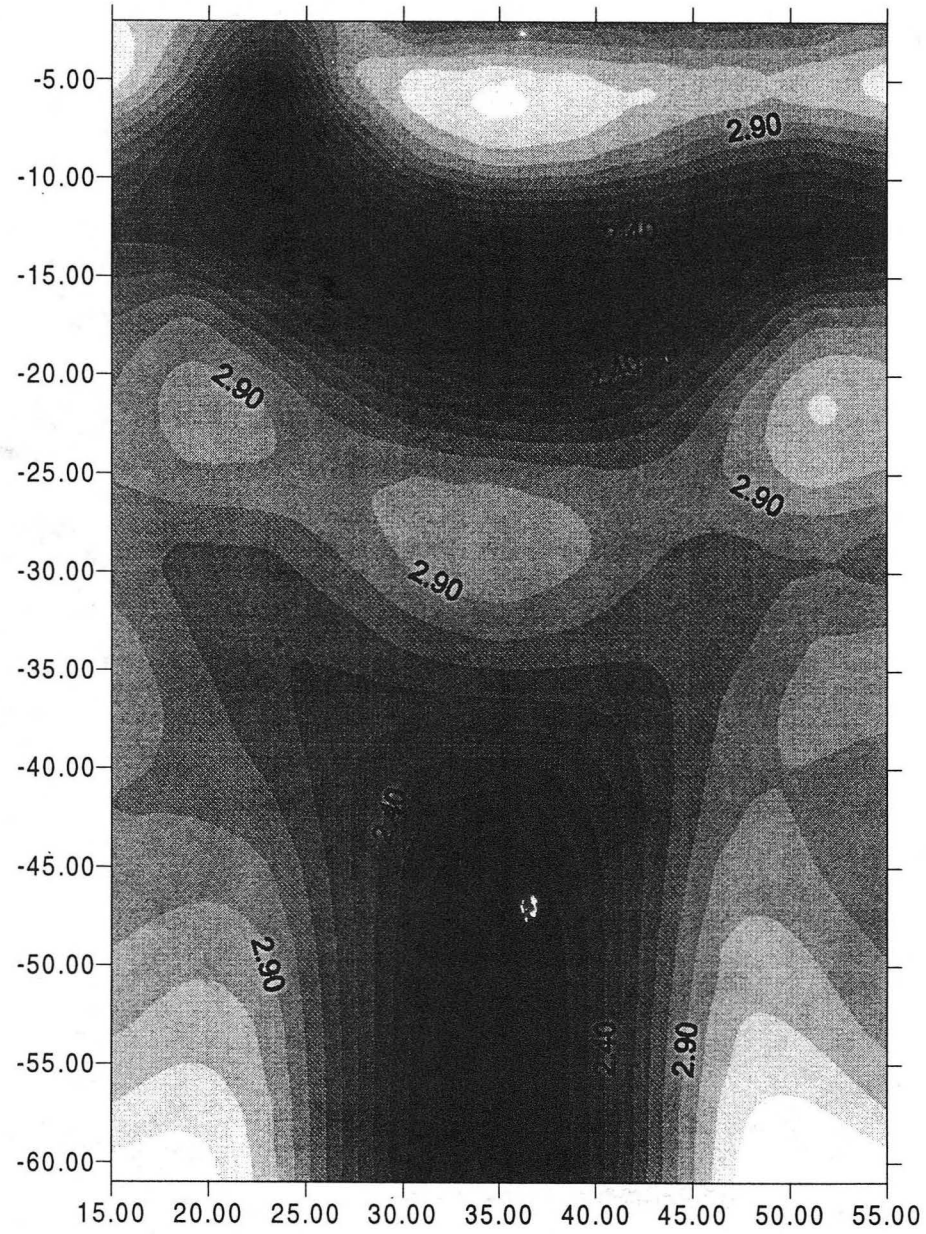
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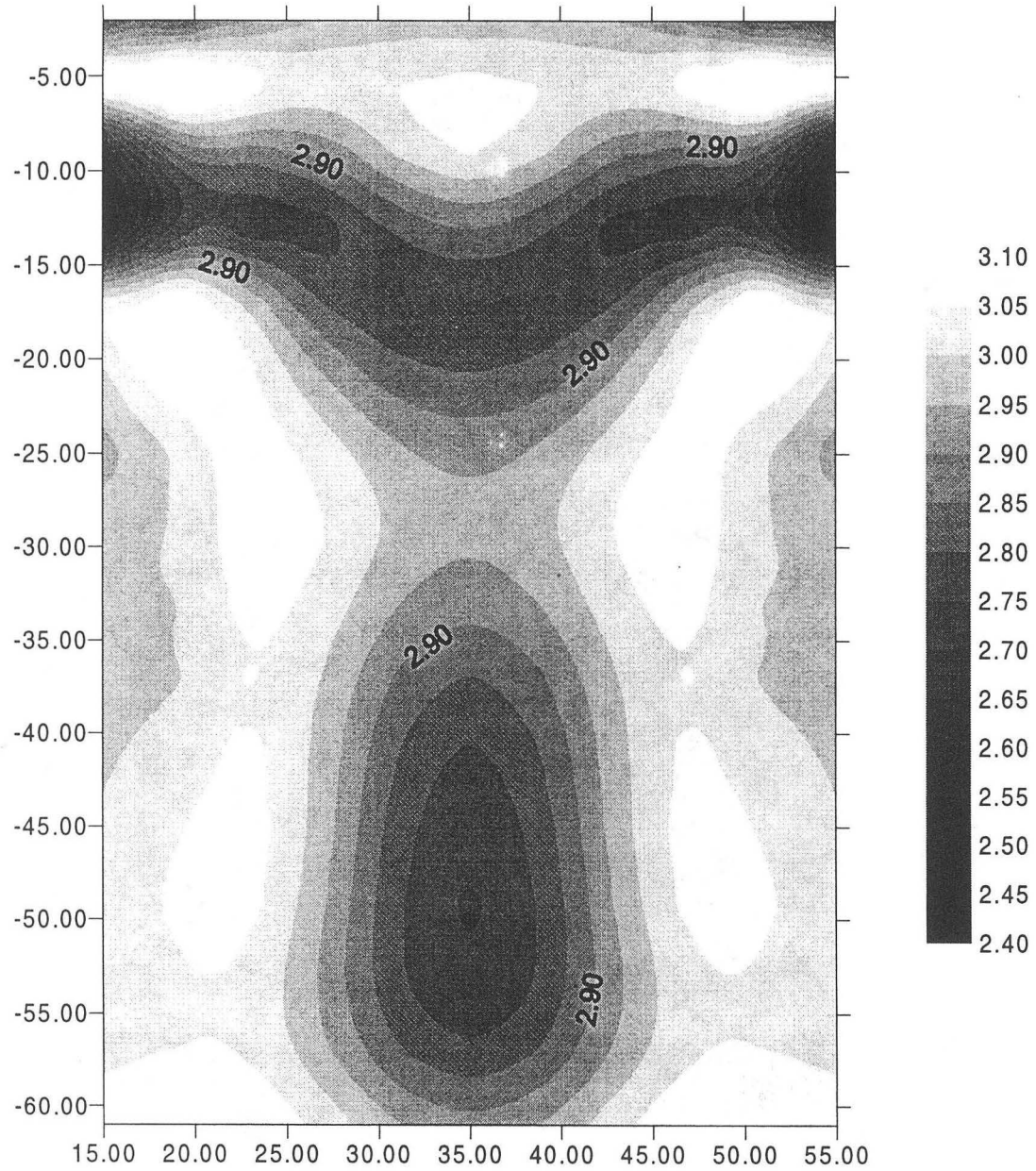
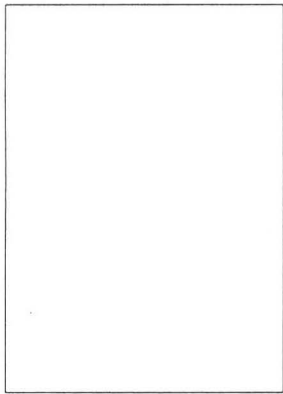
pp7.out  
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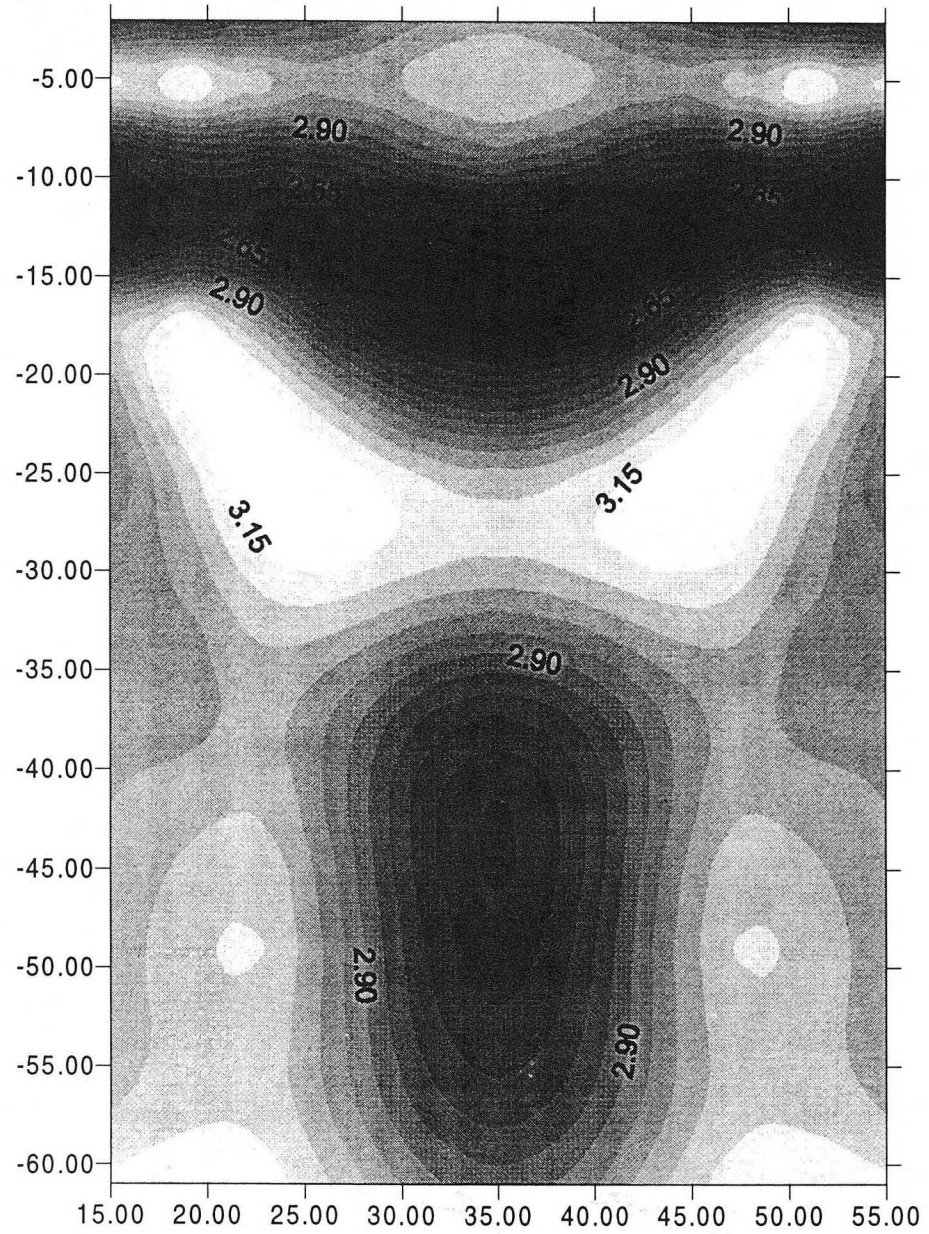
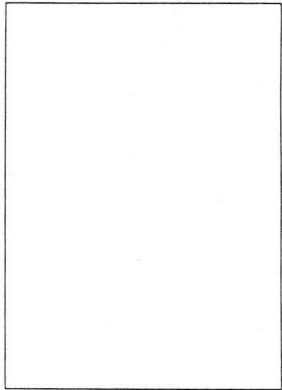
225



pp8.out  
(5 23 9 10)  
(47 65 9 10)



p\_2.out  
(5 30 9 10)  
(40 65 9 10)





II.10

Theory and numerical evaluation  
of the parameters of the chaotic  
behavior of flow

Boris Faybishenko

12/04/97

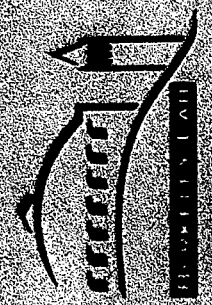
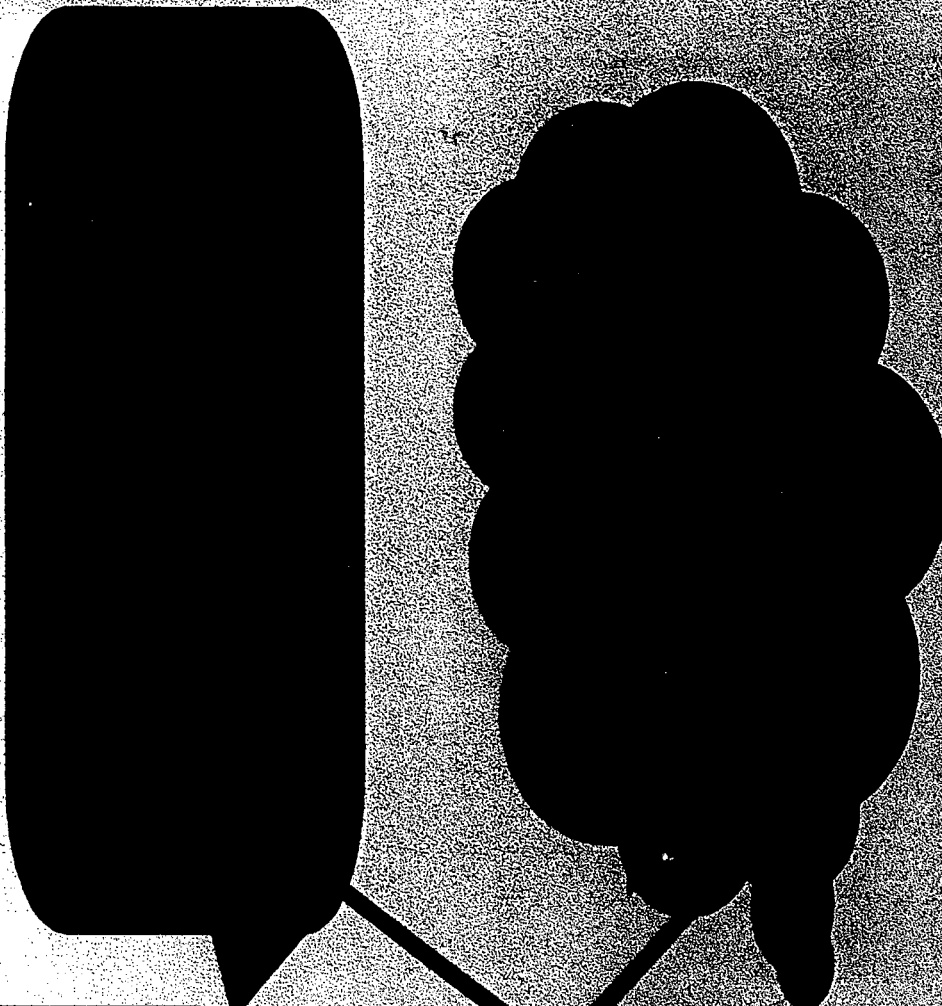
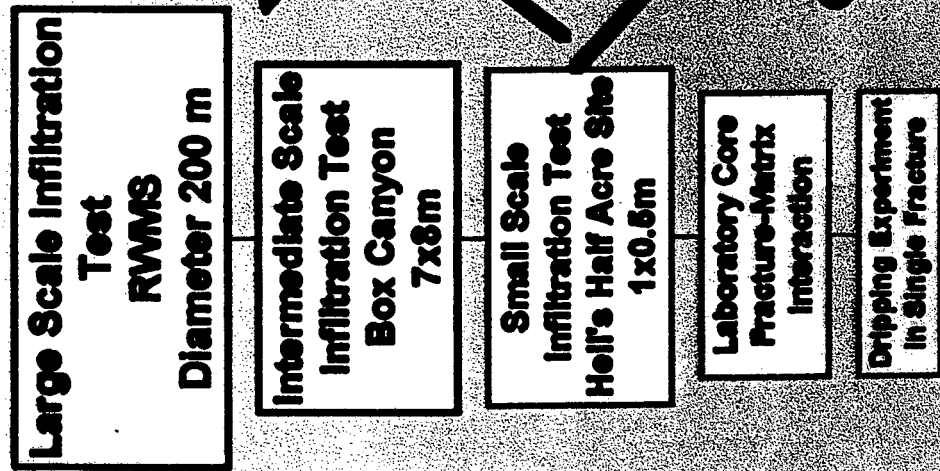
# Introductory Statements

- Random-looking aperiodic behavior may be a product of determinism
- Chaos is mathematically defined as “randomness” generated by simple deterministic systems
- This randomness is a result of the sensitivity to initial conditions

# Outline

- Complexity of unsaturated flow in soils and fractured rocks
- What is deterministic chaos?
- Why do we need to know that chaos is involved in time series data?
- Calculations of chaotic parameters

# Hierarchy of Tests and Models



ERNEST ORLANDO LAWRENCE  
BERKELEY NATIONAL LABORATORY

# Vadose Zone is an Open Dissipative System

- There is an exchange of energy and flux (water, chemicals, gas) between the VZ and the atmosphere and groundwater
- Processes of energy and mass transfer are irreversible, and the phase-space of the system may contract

# Dynamical system

- For a differential equation, the solution is continuous
- For a difference equation, the solution is a map

# Chaotic Dynamical System

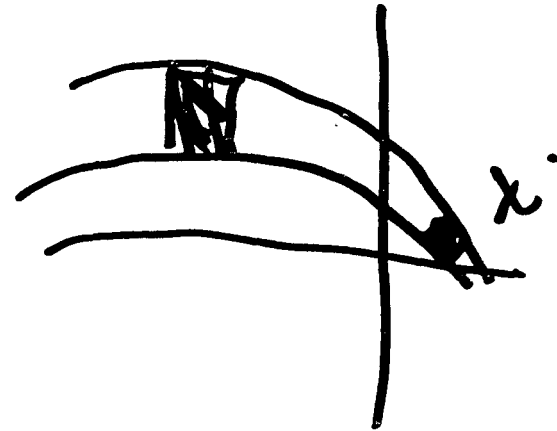
- The evolution of the system is very sensitive to initial conditions
- The system generates randomness
- The attractor (called chaotic, or strange) is the attracting point set representing the closure of a orbit of the system as the time goes to infinity.

# Examples of conservative and dissipative systems

- A conservative system
  - A particle falls with no friction

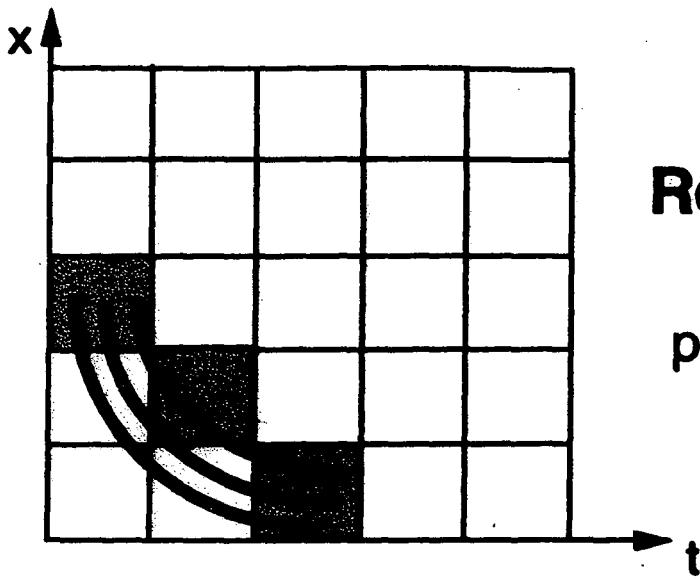
$$dx/dt = v$$

$$dv/dt = g$$



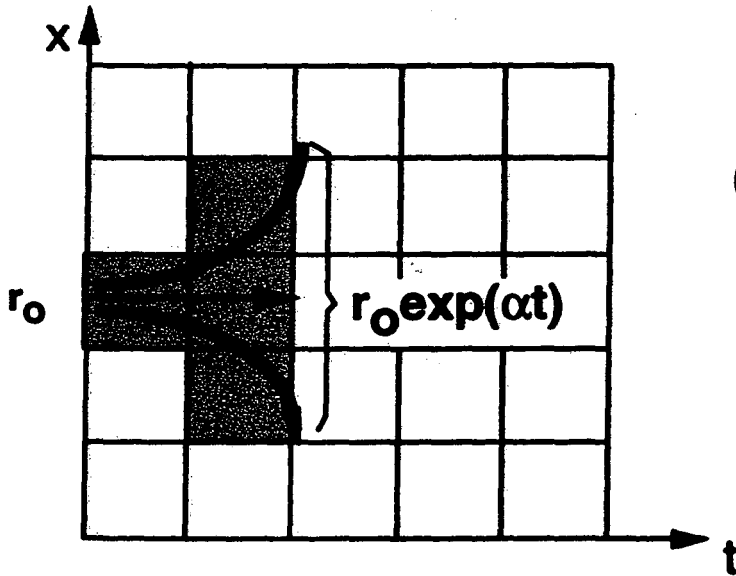
- A dissipative system
  - A particle falls with a friction force,  $-kv$





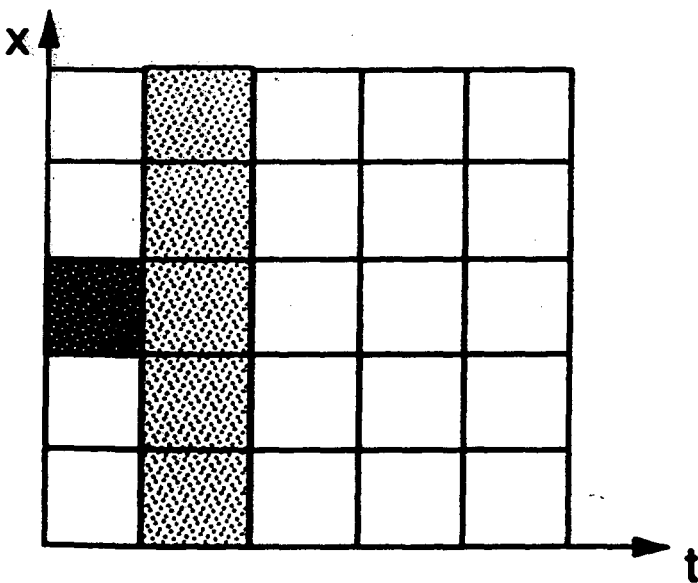
## Regular Motion

Initially adjacent points stay adjacent



## Chaotic Motion

Initially adjacent points become exponentially separated

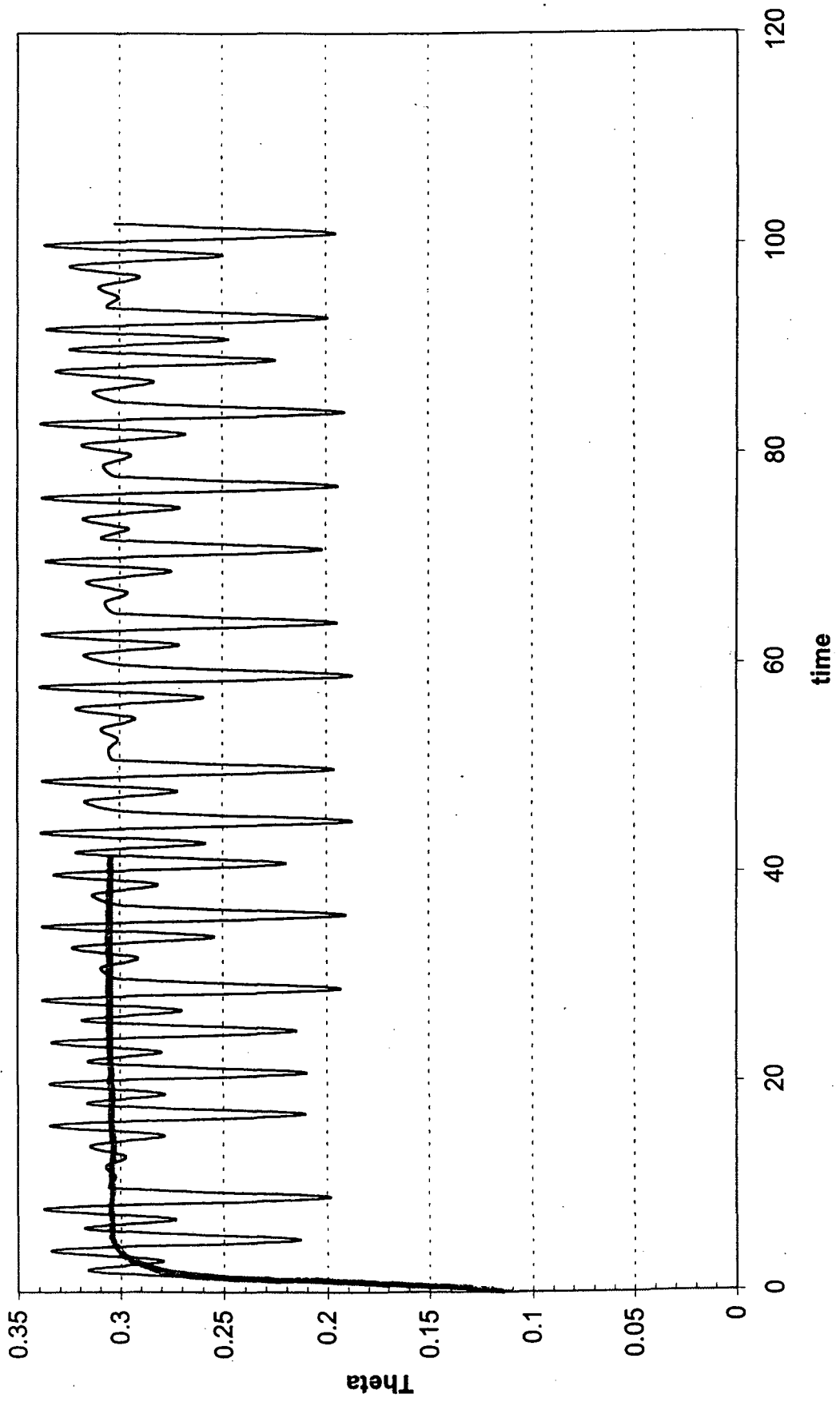


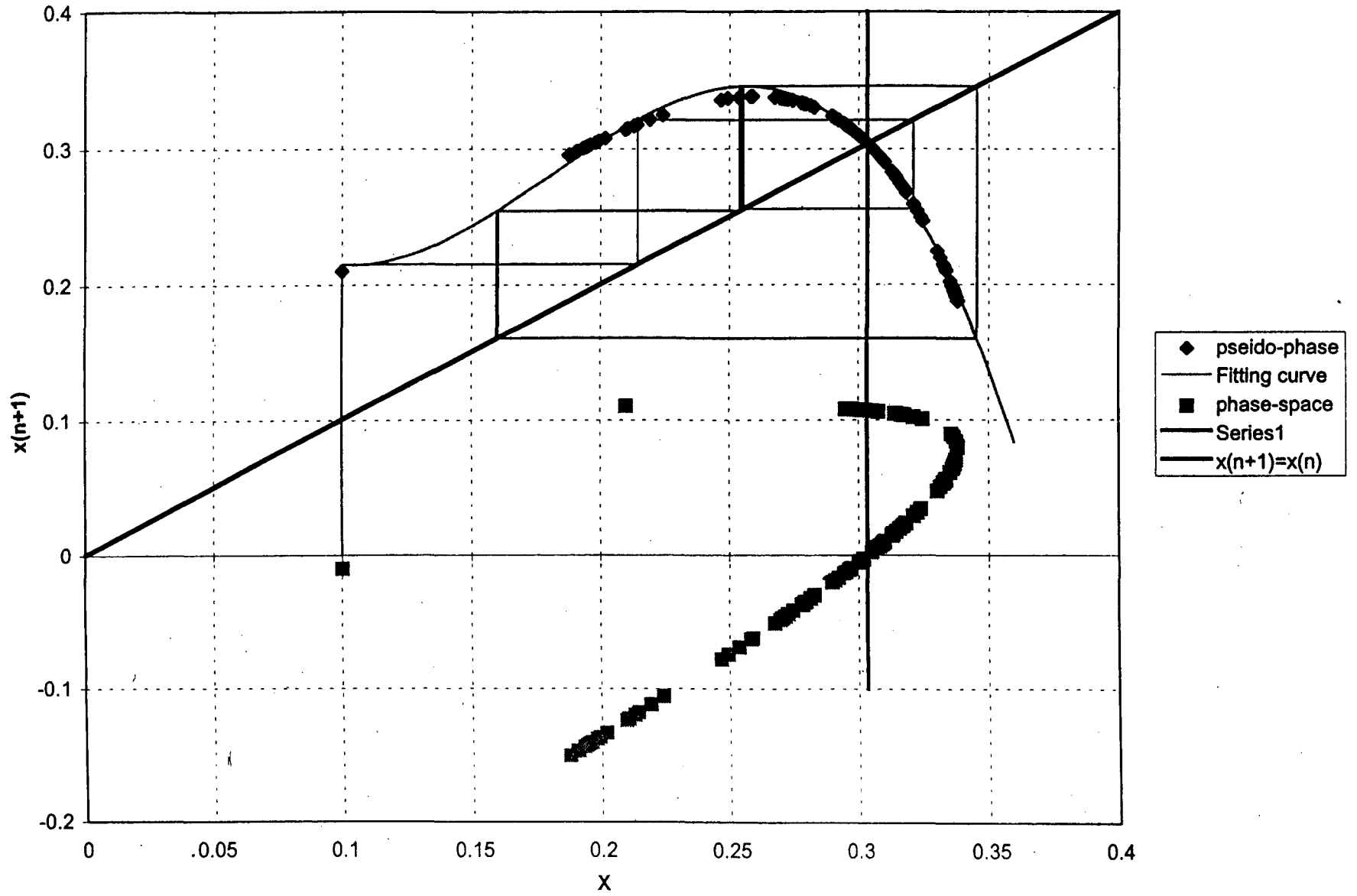
## Random Motion

Initially adjacent points are distributed with equal probability

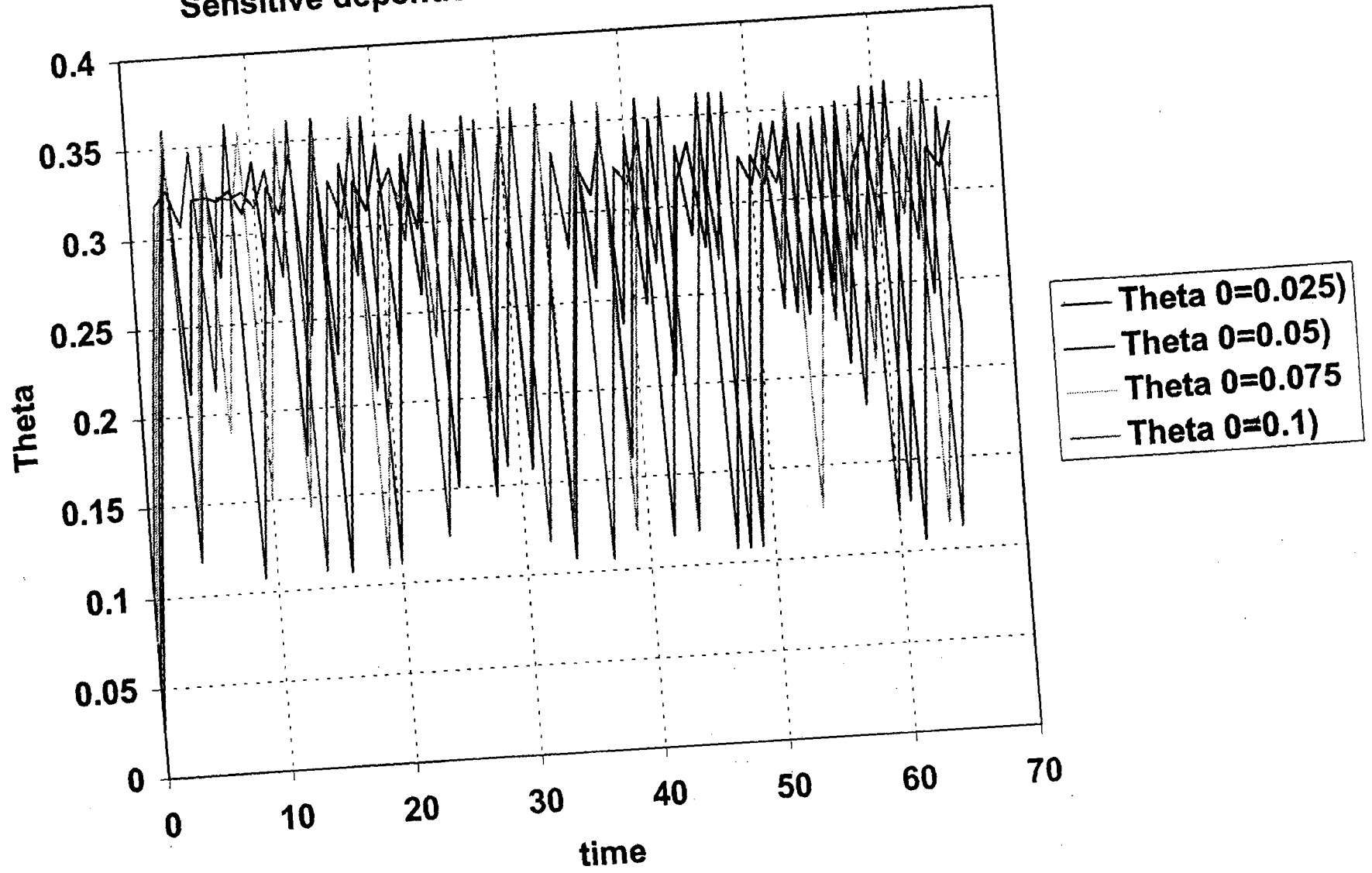
$$T_M \leq \frac{1}{\alpha} \log\left(\frac{1}{r_0}\right)$$

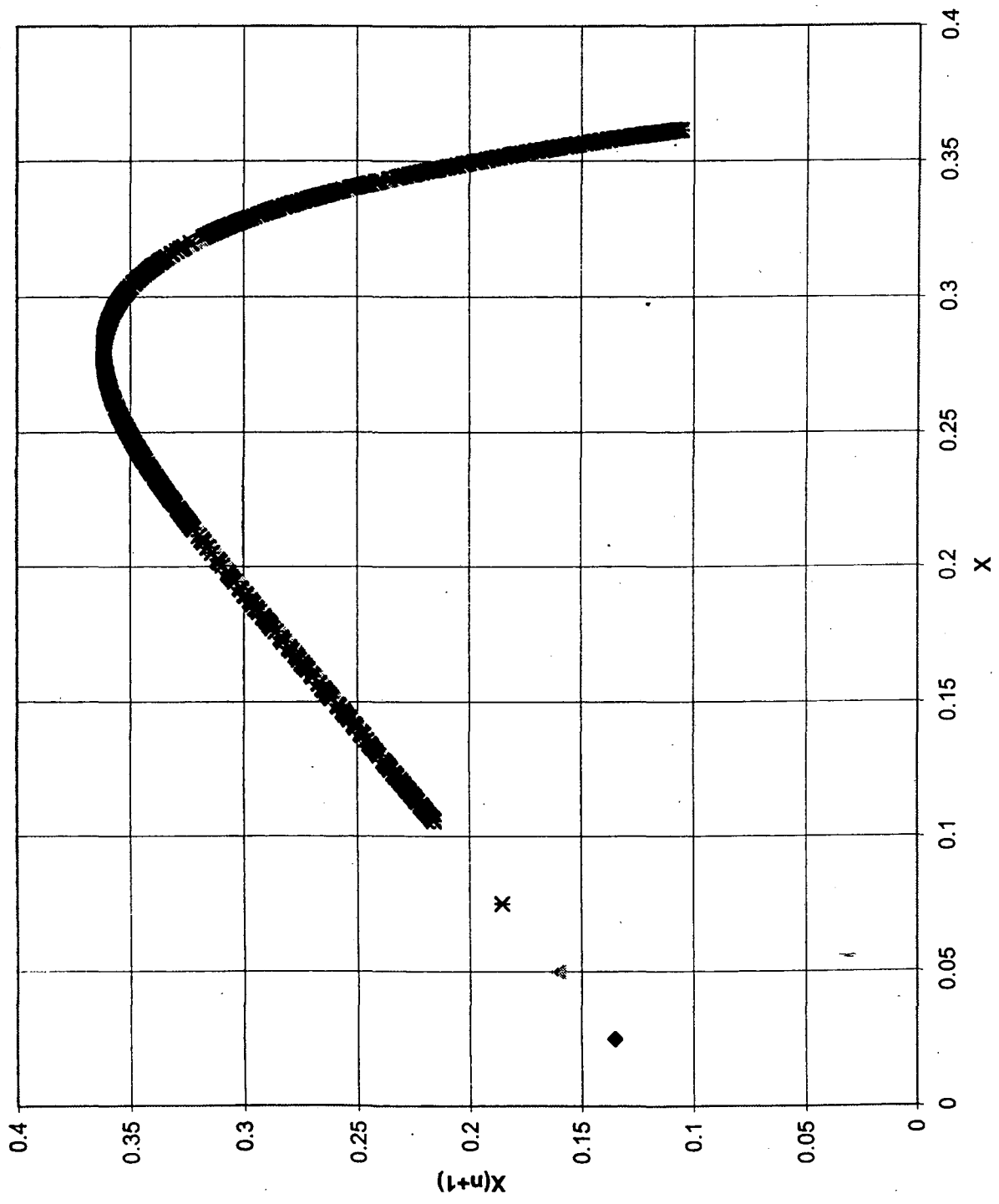
n=8





Sensitive dependence to initial conditions of Theta vs. Time





# Time Series Analysis

- One-dimensional data set,  $X(t)$ , contains the information about some other physical parameters of the system
- No-prior-model approach to detect key properties of the system

The logistic differential equation

$$\frac{dy}{dt} = ry \left(1 - \frac{y}{K}\right) \quad (1)$$

is analogous to the logistic difference equation

$$y_{n+1} = \rho y_n \left(1 - \frac{y_n}{K}\right) \quad (2)$$

$$\frac{dy}{dt} \approx \frac{y_{n+1} - y_n}{h};$$

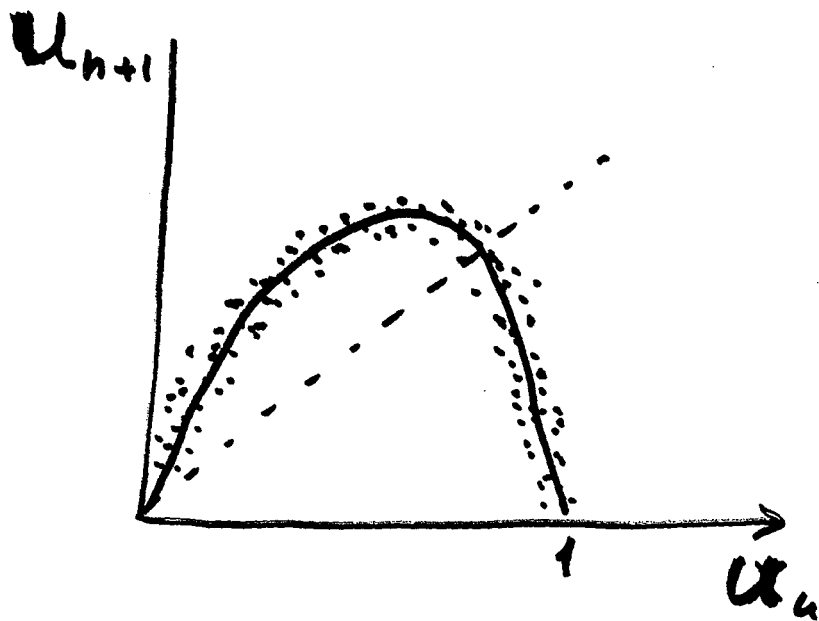
$$\rho = 1 + hr; \quad K = (1 + hr)K/hr$$

$$u_n = y_n/K$$

$$u_{n+1} = \rho u_n (1 - u_n) \quad \begin{array}{l} \text{deterministic} \\ \text{case} \end{array}$$

noisy logistic map

$$u_{n+1} = [\rho + q(n)] u_n (1 - u_n)$$



$q_n$  indicates the fluctuations of the  $\rho$  parameter



# Lyapunov exponent

- The system is evolving from two slightly differing initial states,  $X$ , and  $X+\varepsilon$ :

$$\varepsilon(n) = \varepsilon \exp(\lambda n)$$

$\lambda$  = average rate of divergence

# Lyapunov exponent

$$\begin{array}{c} \varepsilon \\ \hline x_0 \quad x_0 + \varepsilon \end{array}$$

N iterations  $\rightarrow$

$$\begin{array}{c} \varepsilon e^{N\lambda(x_0)} \\ \hline f^N(x_0) \quad f^N(x_0 + \varepsilon) \end{array}$$

# Hurst exponent

$$\Delta X(\lambda \Delta t) = \lambda^H \Delta X(\Delta t)$$

for all  $\lambda > 0$   $0 < H < 1$

$H = \frac{1}{2}$  - Pure Brownian motion

$H = 0$  Position is independent of time  
because  $s \propto t^H$

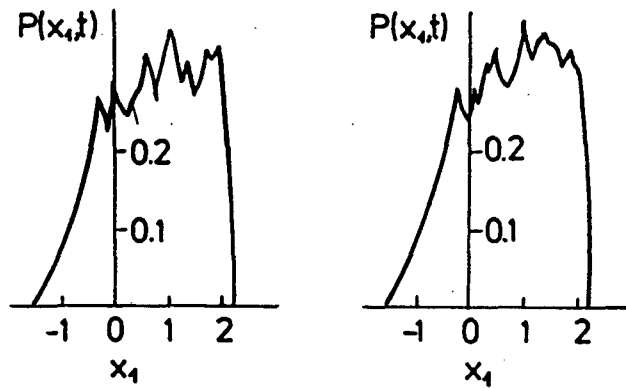
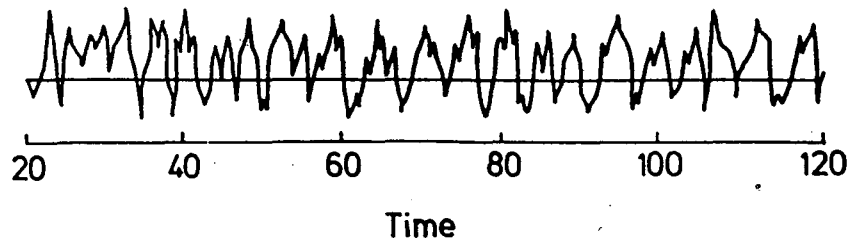


Figure 5.7 : (a)  $t=80.0$  , (b)  $t=120.0$

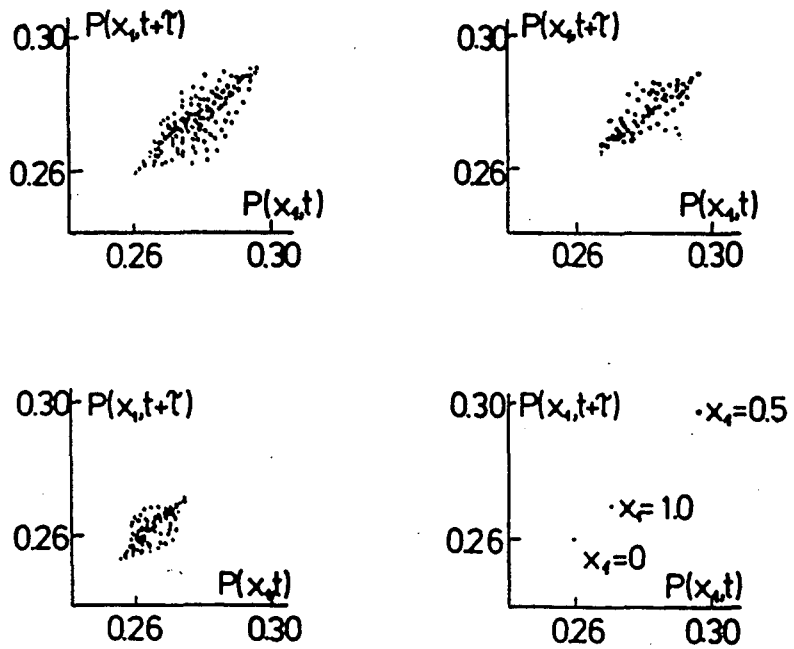


Figure 5.8 : (a)  $x_1=1.0$  , (b)  $x_1=0.5$  , (c)  $x_1=0$  , (a) - (c) chaotic behaviour, (d) regular behaviour,  $\tau=5$ .

# Capacity Dimension

- Called Hausdorff dimension or Fractal dimension

- Box counting method

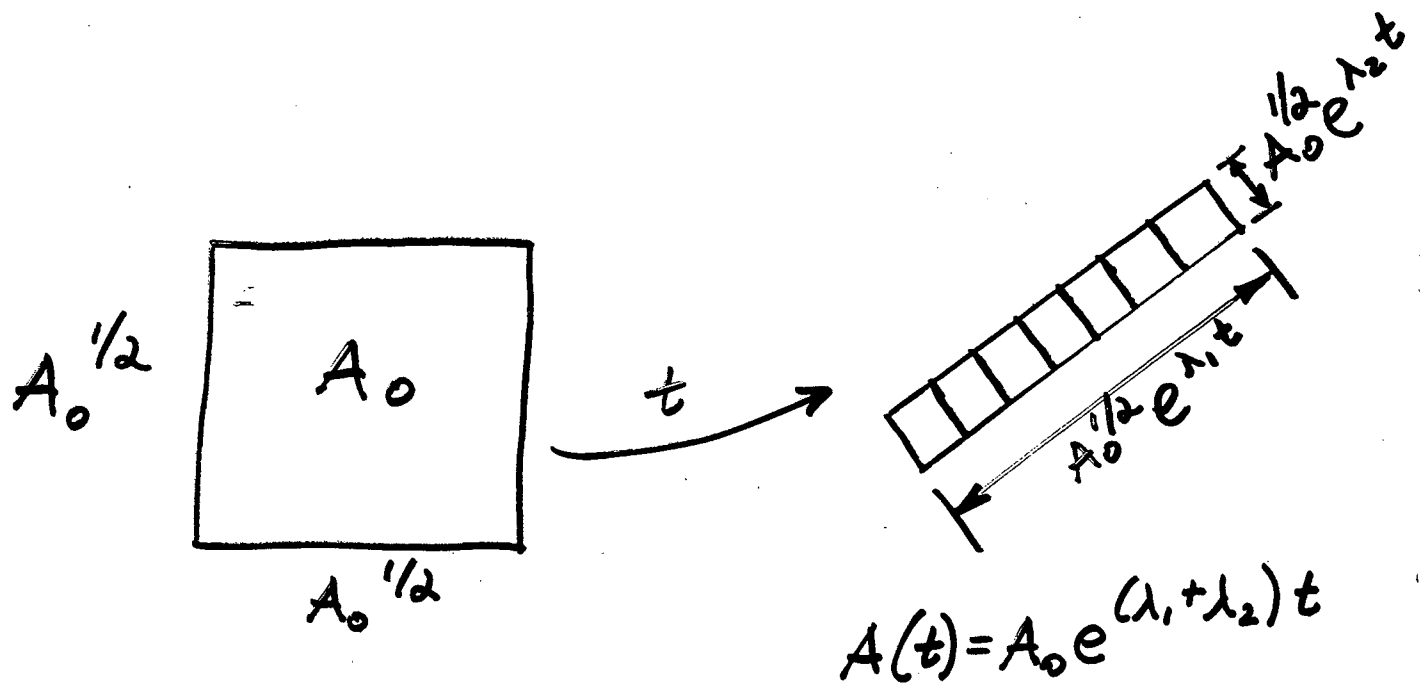
$$d_c = \lim_{\epsilon \rightarrow 0} \log N(\epsilon) / \log(1/\epsilon)$$

# Entropy

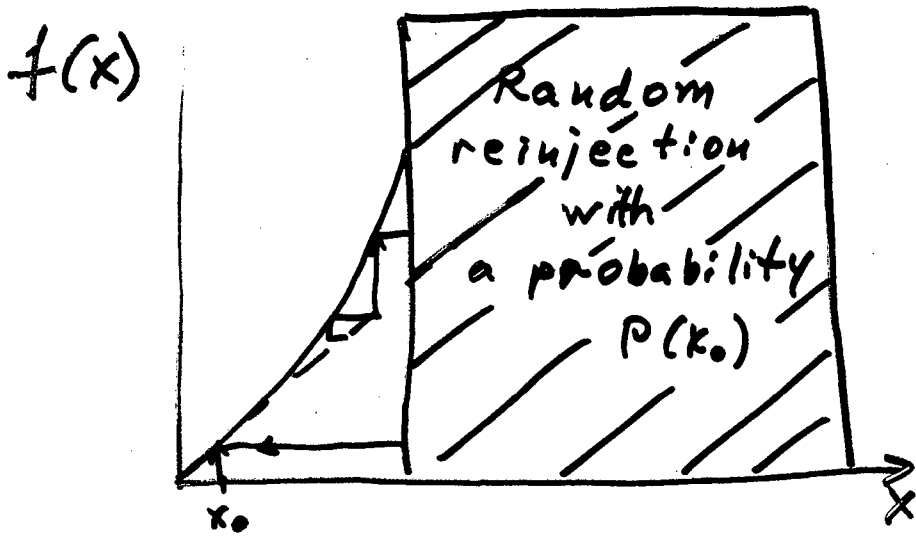
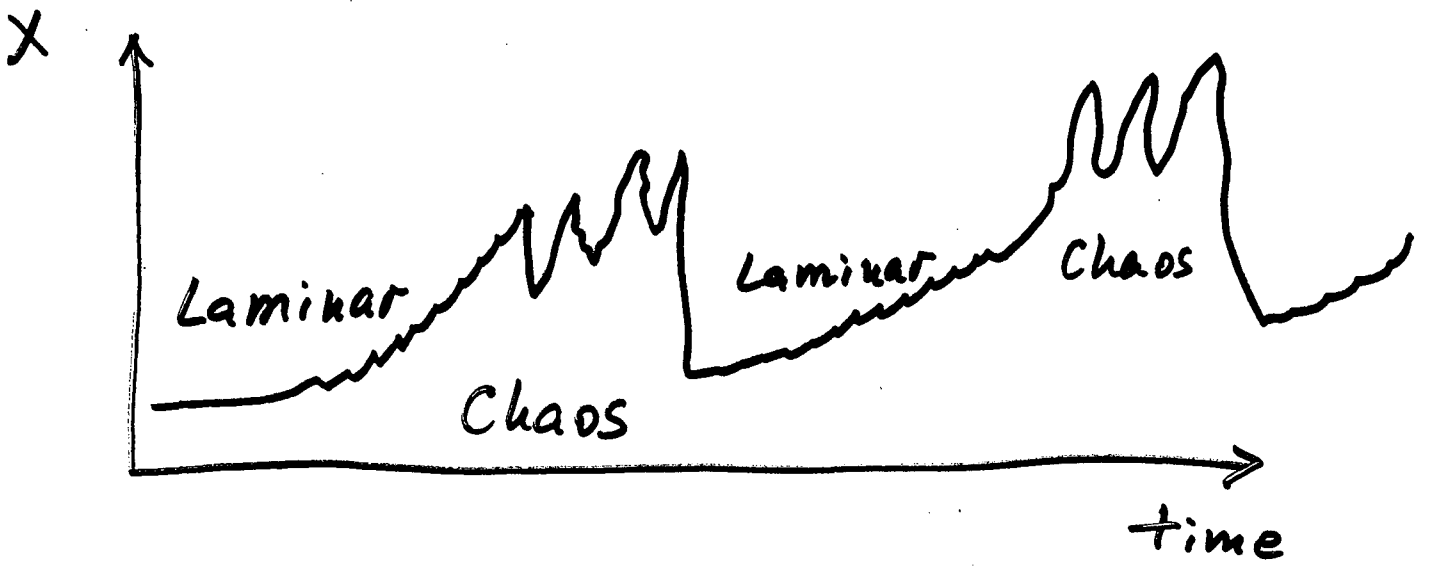
- Comparing the results to a statistical system
- A measure of the disorder in the system

$$S = - \sum p_i \log_2 p_i$$

- With increasing the degree of chaos,  $S$  increases, until it reaches the maximum value for a random system



$\lambda$  = Lyapunov exponent

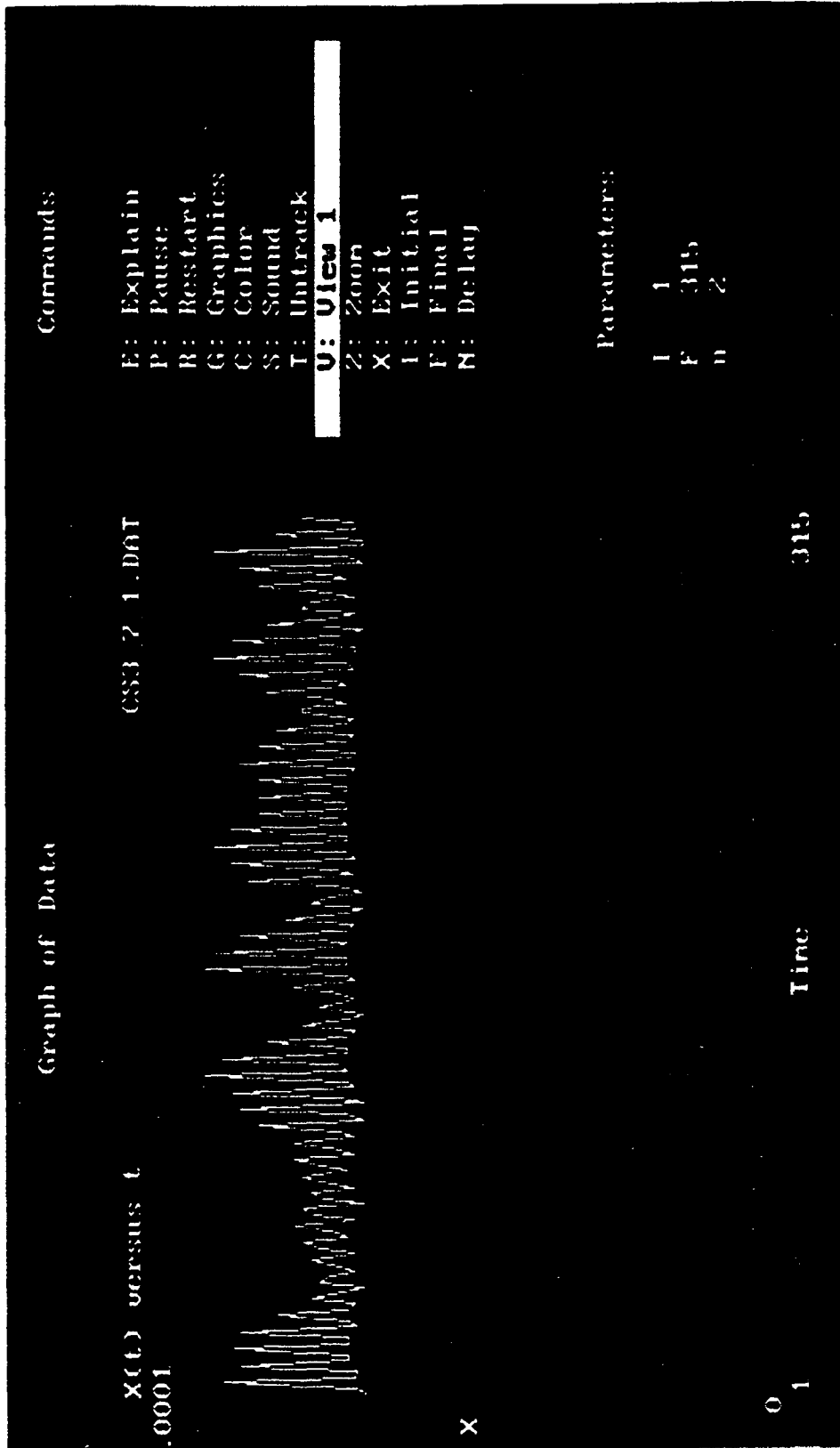




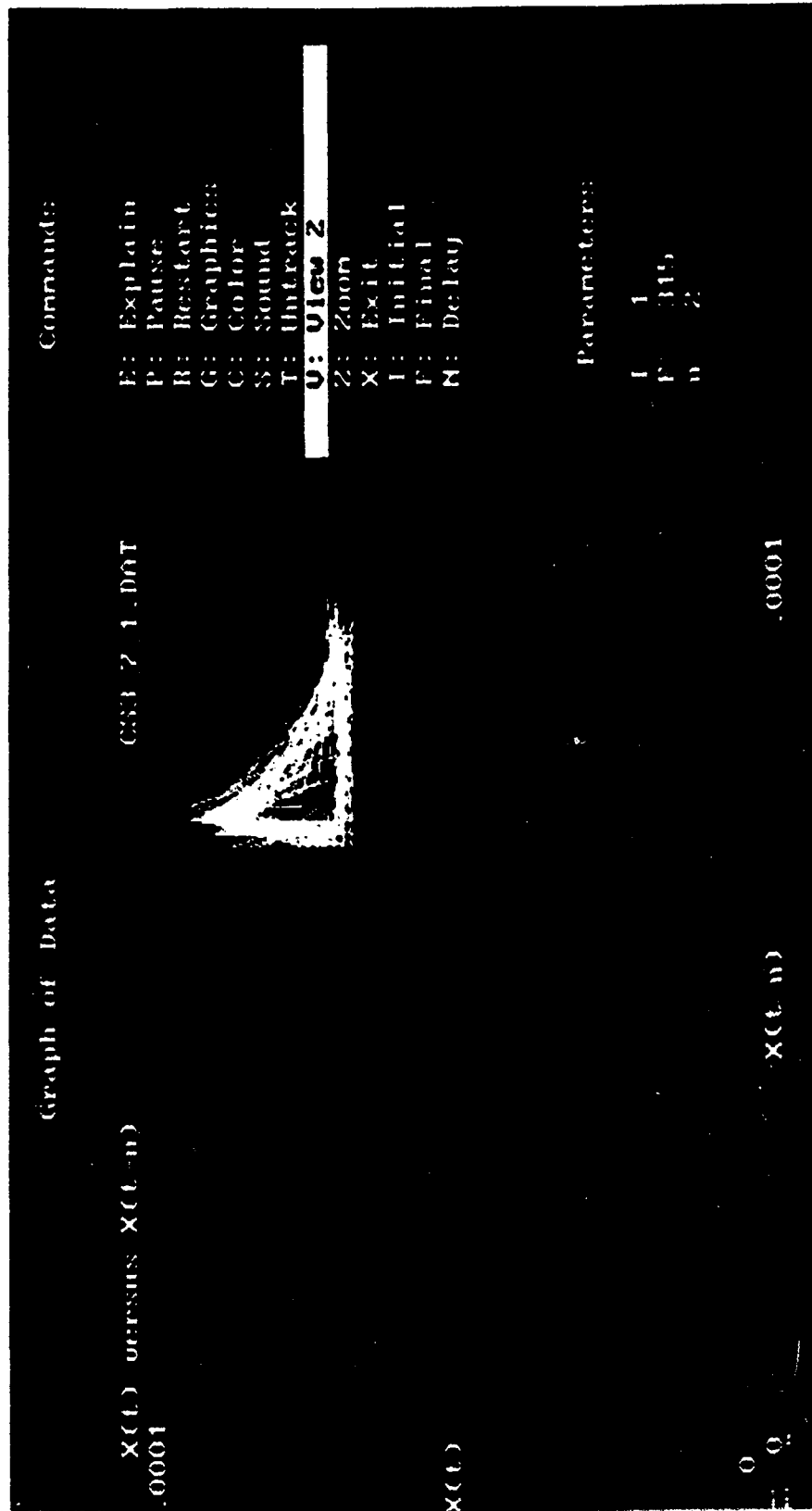
	Chaos	Random	Noise	0.25 ml/hr	0.5 ml/hr	1 ml/hr	2 ml/hr		SC3-t7
No data points	2000	2000		13220	13378	13394	15674		5001
Minimum value	-17.72337	7.77E-04		2.59	3.64	5.39	8.37		6.65E-05
Average value	-0.2358849	0.5030418		3.789	4.903713	6.356282	10.58747		7.62E-05
Maximum value	17.98758	0.9993806		5.84	7.11	7.61	12.3		9.99E-05
Range of data	35.71095	0.9986031		3.25	3.47	2.22	3.93		3.34E-05
Resolution	1.26E-02	2.73E-04		1.00E-02	1.00E-02	1.00E-02	1.00E-02		1.00E-07
Lower quartile	-5.713983	0.2617328		3.24	4.4	6.05	10.2		7.08E-05
Median value	-0.3580765	0.5082129		3.71	4.87	6.33	10.6		7.23E-05
Upper quartile	5.163997	0.7541968		4.13	5.35	6.67	11		8.11E-05
Mode (max probability)	-0.625	0.796875		3.90625	4.21875	6.09375	10.3125		7.03E-05
Aver deviation	6.450353	0.2501415		0.5420973	0.4945862	0.3149368	0.5080337		6.78E-06
Standard deviation	7.916132	0.2886727		0.6915743	0.5860473	0.36666431	0.6420568		8.06E-06
Variance	62.66514	8.33E-02		0.4782749	0.3434514	0.1344272	0.4122369		6.50E-11
Skewness	4.91E-02	-3.08E-02		0.7280276	0.2634546	0.1397251	-0.2310608		0.990818
Kurtosis	-0.6851208	-1.189187		0.1732618	-0.9731036	-0.936166	8.62E-03		-0.333621
Pearson's correlation	0.9634255	1.73E-02		0.9965331	0.993629	0.9885468	0.98848		0.259216
									7.08E-05
Fixed point (estimated)	-0.5625651	0.983019		3.72	4.59	6.72	10.7		
Relative LZ complexity	0.1809354	1.041749	1.04723	0.1253058	0.1465229	0.1903785	0.1929393		0.375938
Dominant frequency (FFT)	0.015625	0.09375	0.2969	3.91E-03	0.0078125	1.17E-03	0		0.15625
Dominant frequency (MEM)	0.003	0.0795		0.003	0.0015	0.0055	0		
Dominant period (FFT)	64	10.66667		256	128	85.3333			6.4
Dominant period (MEM)	333.333	12.557862		333.333	666.6667	181.8182			
Hurst exponent	0.4382105	2.62E-03	-2.93E-03	0.6253539	0.4067501	0.5242398	0.4431641		1.16E-02
Largest Lyapunov exponent	0.075+-0.034	0.895+-0.031	0.78	0.118+-0.096	0.242+-0.03	0.392+-0.019	0.322+-0.101		0.560±0.046
Lyapunov exponent (base e)	0.052+-0.24	0.620+-0.02		.082+-0.067	0.168+-0.021	0.272+-0.013	0.223+-0.07		0.388±0.032
Capacity dimension (appr)	1.807+-0.283		3.145+-0.492	1.437+-0.088	1.453+-0.088	1.391+-0.084	0.944+-0.053		2.926+-0.29
Correlation dimension (appr)	2.002+-0.103		4.555+-0.031	3.699+-0.458	3.641+-0.765				4.958±0.449
Entropy (approx)	0.35	0.413	0.527	0.259	0.231				0.548
BDS statistic	0.334	-16.83684	-11.789	2.031	3.13				6.63E-02
Correlation time	6.101169	0.6435637	0.622	23.05126	16.54703		12.83941		0.853542

# Deterministic, stochastic, chaotic, and noisy components of data

# Outcrop test SC3-T7



# Phase-Space Portrait, SC3-t7



Graph of Data

CS3\_7\_1.DAT

Commands:

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- S: Sound
- T: Untrack
- U: View 3**
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- N: Delay

Parameters:

- I 1
- F 5001
- n 1

X(t) vs X(t-m) vs X(t, 2m)

X(t, 2m)

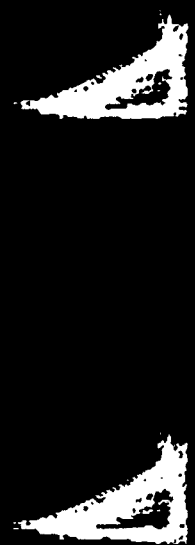
X(t, m)

# Stereo Plot, SC3-t7

Stereo Plot

Graph of Data

CS3 ? 1.DAT



Commands

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- S: Sound
- T: Untrack
- U: View 4**
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- N: Delay

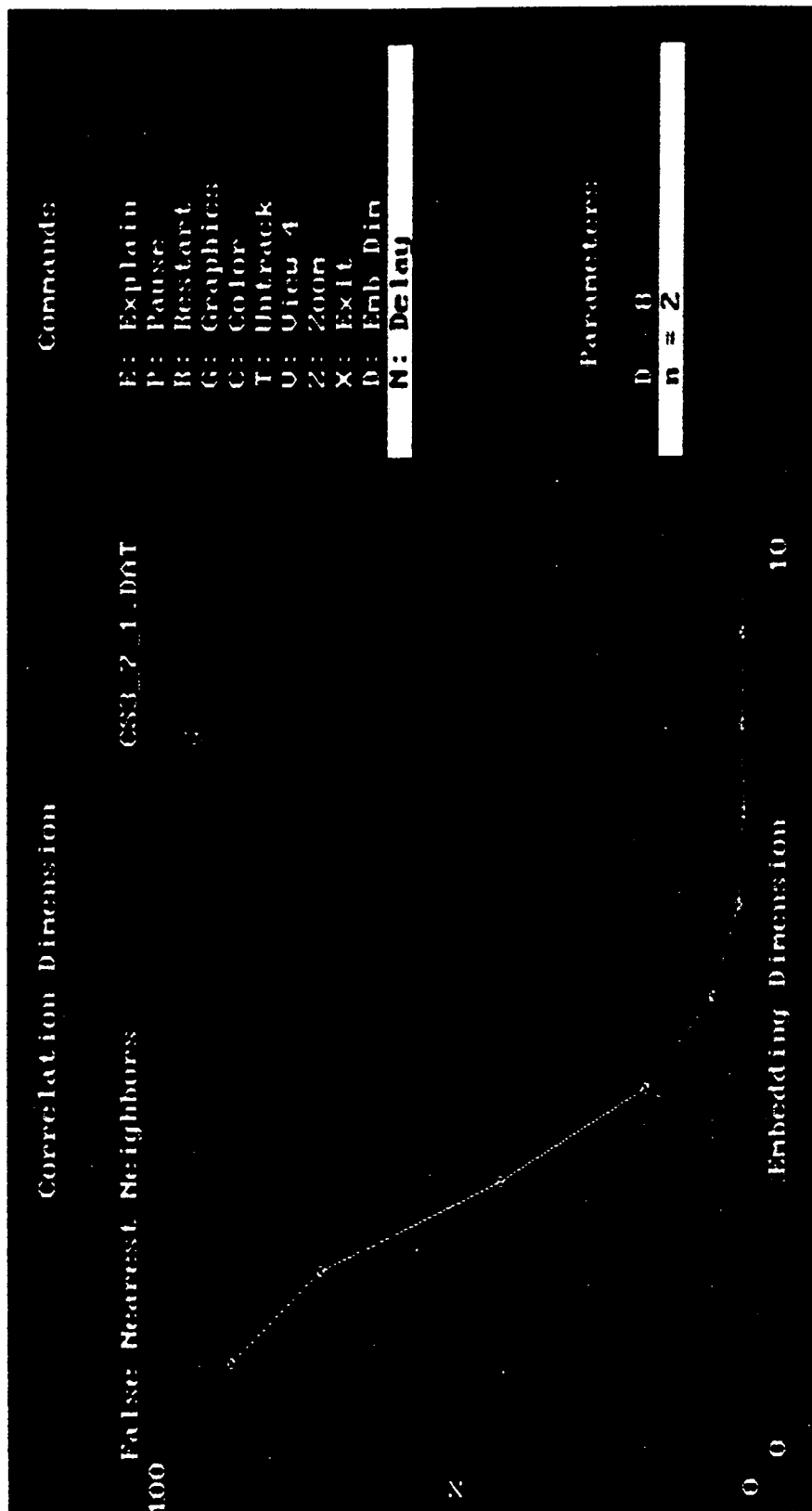
Parameters

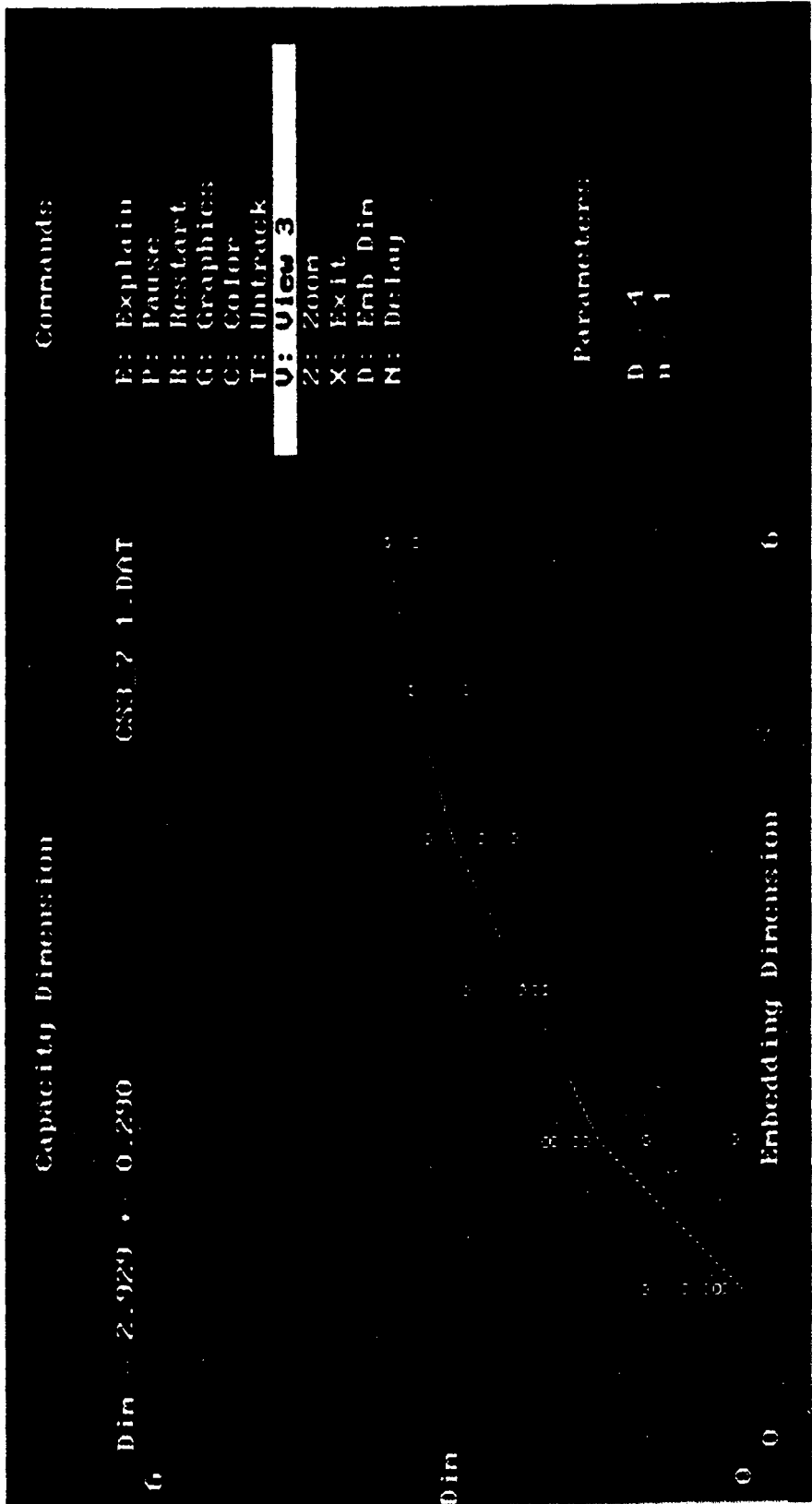
- I 1
- F 315
- N 2

X(t)

X(t, n)

# Determining embedding dimension



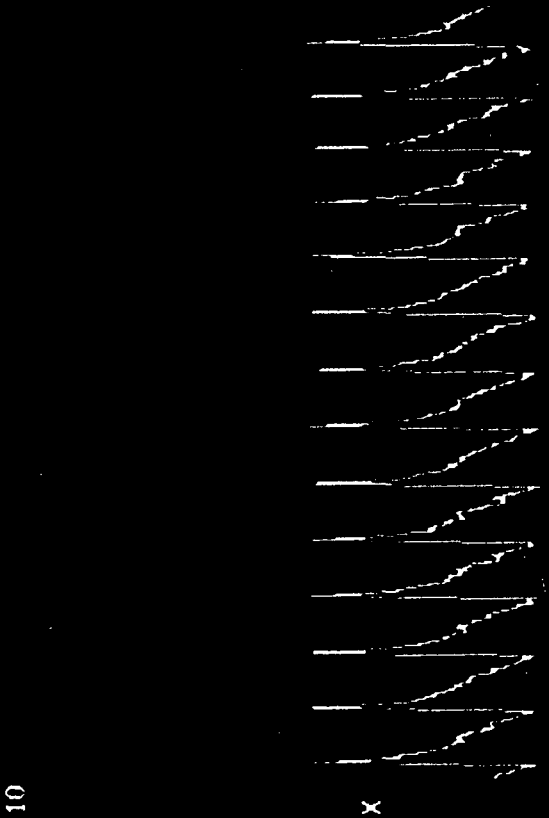




Graph of Data

X(t) versus t

0Z5HL\_1.DAT



3306

Commands

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- S: Sound
- T: Untrack
- U: View 1**
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- N: Delay

Parameters

- I = 1
- F = 3306
- n = 1

Graph of Data

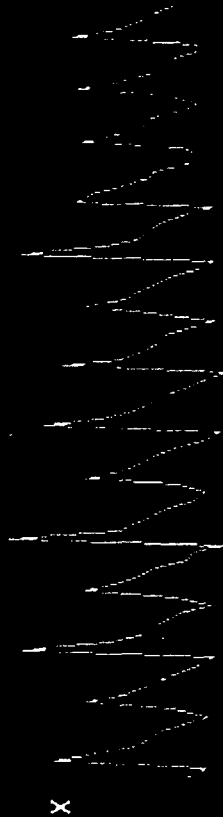
Commands

025HL\_71.DAT

- E: Explain
- P: Pause
- R: Restart
- G: Graphics**
- C: Color
- S: Sound
- T: Untrack
- U: View 1
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- N: Delay

X(L) versus t

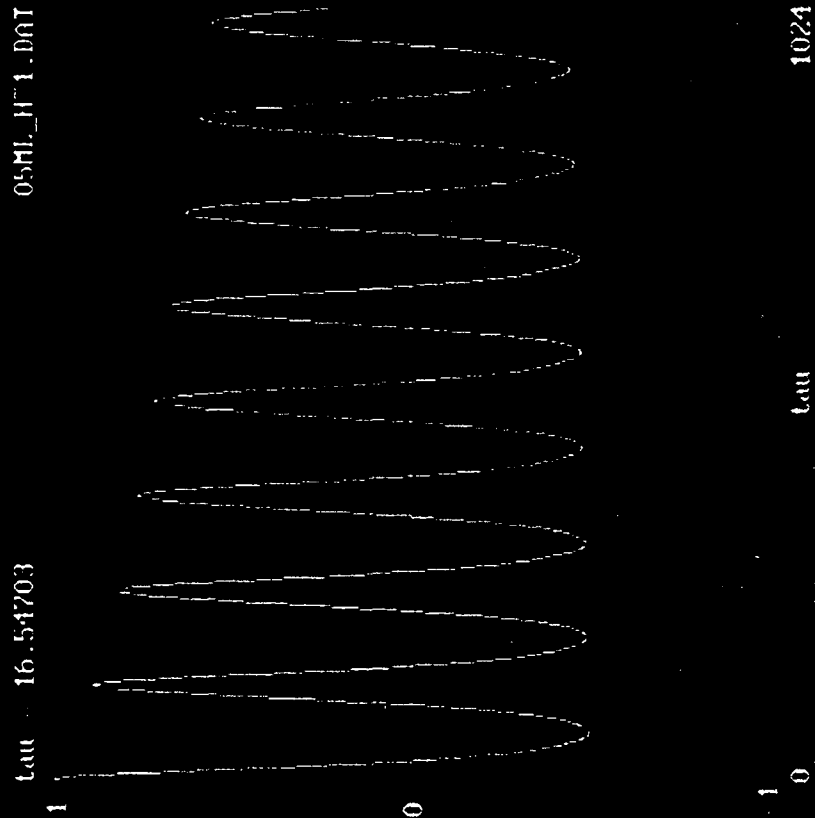
10



Parameters

- I 1
- F 3306
- n 32

Correlation Function



Commands

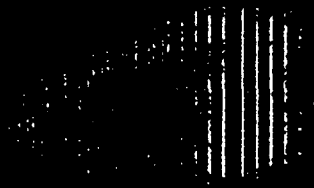
- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- Z: Zoom**
- X: Exit
- M: Max tau

Parameter

n 1024

Phase-Space Plots

$X'(t)$  versus  $X(t)$   
.5



$X'(t)$

10

$X(t)$

.5  
0

Commands

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- T: Track
- U: View 1**
- Z: Zoom
- X: Exit

Phase-Space Plots

$X'(t)$  vs  $X(t)$  vs  $X(t)$   
 $X'(t)$

05ML\_H~1.DAT



Commands

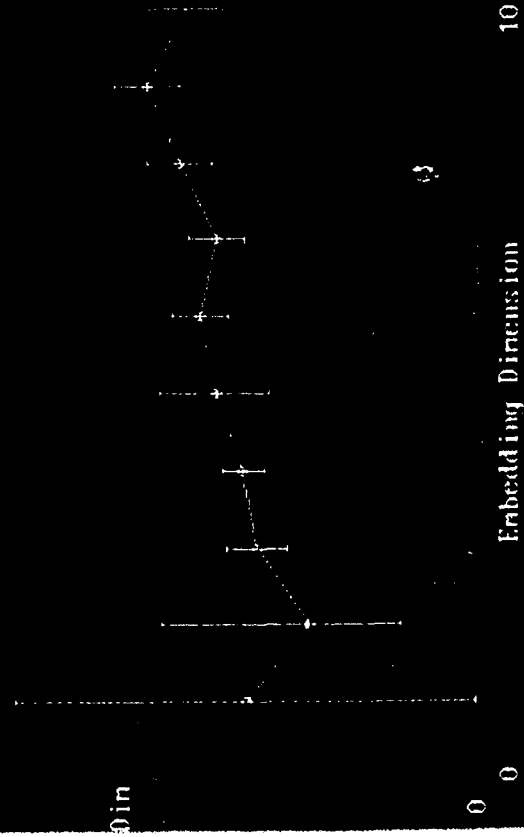
- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- T: Track**
- U: View Z
- Z: Zoom
- X: Exit

X(t)

X''(t)

Correlation Dimension

Din 3.639 +- 0.774  
10  
22 % done  
05ML\_H11.DAT



Commands

E: Explain  
P: Pause  
R: Restart  
G: Graphics  
C: Color  
T: Untrack  
**U: View 3**  
Z: Zoom  
X: Exit  
D: Emb Dim  
N: Delay

Parameters

D 5  
n 1

Commands

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- T: Untrack**
- U: View 3
- Z: Zoom
- X: Exit
- D: Emb Dim
- N: Delay

Capacity Dimension

Din 1.453 +- 0.088

05ML\_F1.DAT

?

Din

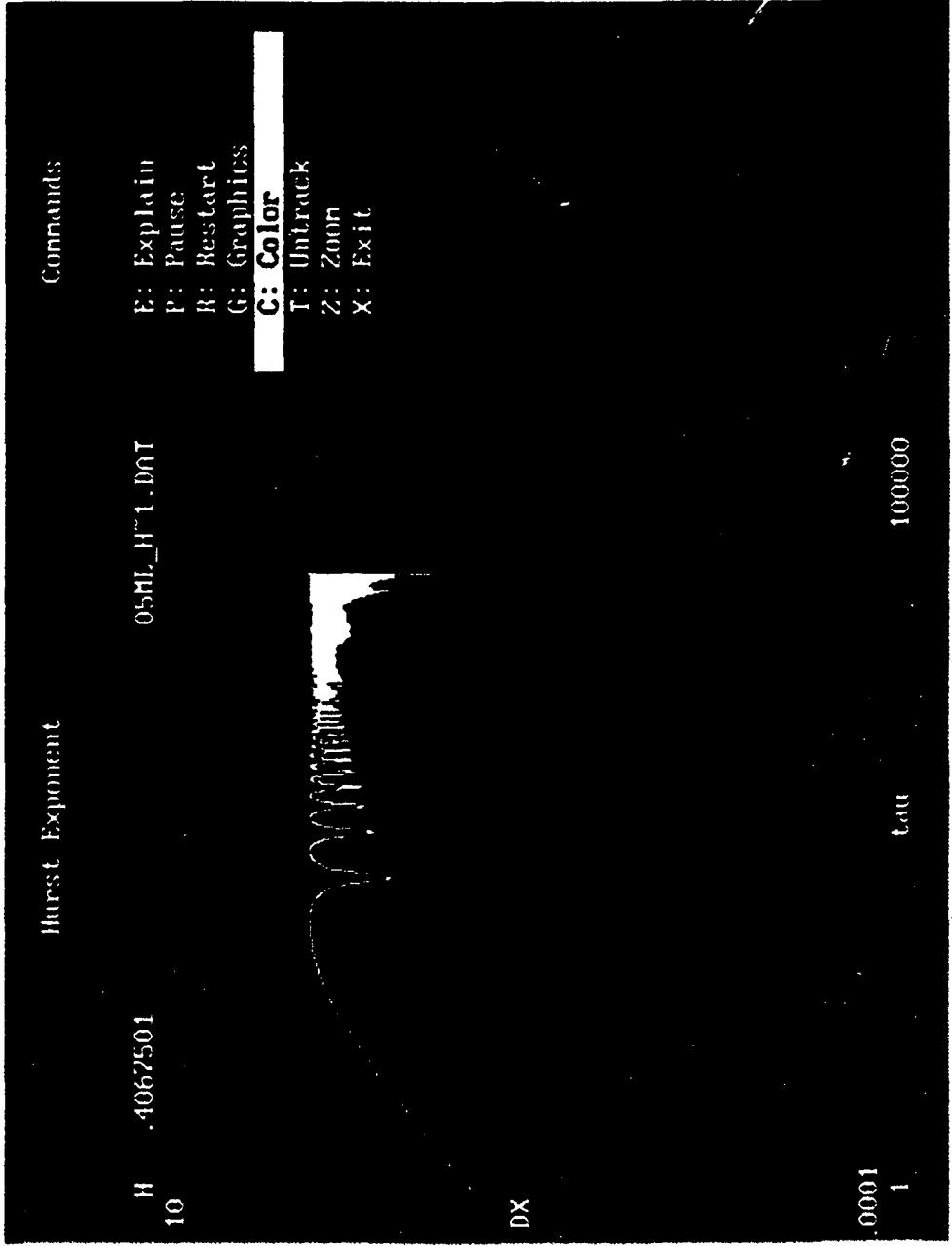
Parameters

D 1  
n - 1

Embedding Dimension

?

0 0





Graph of Data

X(t) versus t

025HL\_3.DAT

20



Time

9220

Commands

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- S: Sound
- T: Untrack
- U: UICU 1**
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- N: Delay

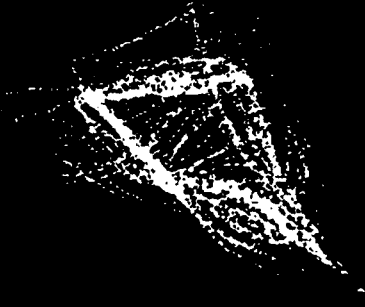
Parameters

- I 1
- F = 9220
- n = 64

Graph of Data

$X(t)$  vs  $X(t-n)$  vs  $X(t-2n)$   
 $X(t)$

025HL\_3.DAT



$X(t-2n)$

$X(t-n)$

Commands

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- S: Sound
- I: Track**
- U: View 3
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- N: Delay

Parameters

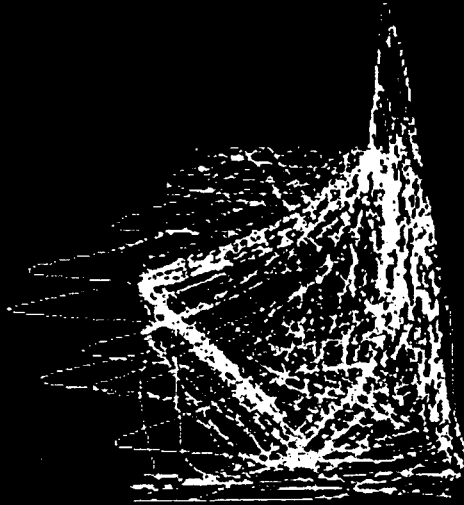
- I 1
- F 9220
- n 64

Graph of Data

X(t) versus X(t-n)

0 20

0 20



Commands

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- S: Sound
- T: Untrack
- V: View Z**
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- N: Delay

Parameters

- I 1
- F 9220
- n 64

025ML\_3.DAT

Graph of Data

Commands

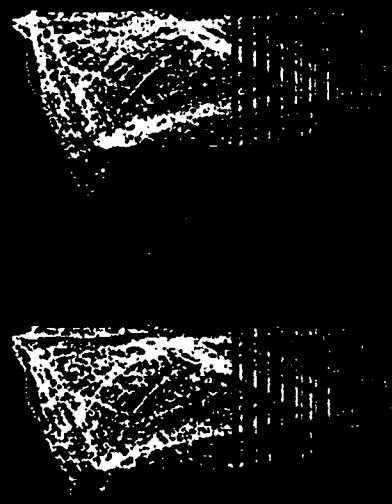
Stereo Plot

025ML\_3.DAT

- E: Explain
- P: Pause
- R: Restart
- G: Graphics
- C: Color
- S: Sound
- T: Track
- U: View 4**
- Z: Zoom
- X: Exit
- I: Initial
- F: Final
- M: Delay

Parameters

- 1 1
- F - 9220
- n 64



X(1:n)

X(1)

# III.

## Life Cycle Planning for Chaotic-Dynamical Research Project

### 1<sup>st</sup> Year (completed)

#### **INEEL**

##### Hells Half Acre

Focus of the research effort was to collect a data set on a small scale field site of sufficient quality and size in order to perform chaotic-dynamical analysis. This data was supported by tensiometer, temperature, head and flow data and instrument development.

Box Canyon Supported Box Canyon tests.

#### **LBNL**

##### Lab

Understand the physics of flow in fractures, and collect data of sufficient quality and size in order to determine if flow in fractures is a chaotic-dynamical process.

Investigated impact of tensiometer on measurements in a fracture using core study

##### Box Canyon

Evaluated possible preferential flow using geophysics

Understand the impact of monitoring approach on data collected

Repeated infiltration tests using tracers and electrical resistivity

Modeled flow using TOUGH2

Data analysis using chaotic-dynamical approach (may lead to a transition from chaotic model at the small scale to a stochastic model at larger field scale)

#### **Reno**

Develop a theoretical approach for data analysis based upon the Navier-Stokes equation

**2<sup>nd</sup> Year**  
**INEEL**

**Hells Half Acre**

Repeat small scale test at one or more sites and modify the test approach based upon the analysis of 1997 data, laboratory testing and instrument development. New testing will involve the use of tracers and geophysics. At the end of the field season a tested fracture will be excavated intact and shipped to Berkeley Lab for further testing

Lab            Verification of monitoring equipment and testing of new instruments

**LBL**

Lab            Data analysis  
Testing will be performed on a variety of plate textures  
Testing on fractured core  
Tracer testing  
Testing on etched glass (etching patterned after Box Canyon Outcrop)

Box Canyon    Pulsed infiltration  
Ponding concurrent with drainage  
Geophysics (use slanted wells and ER probes )  
Development and testing of flow meter for fractured rock (saturated)

Modeling        HHA modeling?  
Lab scale modeling?  
Coordinate modeling with geophysics (use moisture content from TOUGH2 for inverse modeling?)  
Develop approach and software for chaotic-dynamical modeling  
Use CPN moisture content for modeling?

LSIT            Revisit data set using chaotic-dynamical approach?

**Instrument Development**

Impact of monitoring device on the data collected  
Fractured core tensiometer experiment  
Passive/active monitoring approach  
Flow meter for saturated fractured rock and for vadose zone  
Piezo-strips in slanted wells - dripping or flowing along the borehole

**Reno**            To be included

## 3<sup>rd</sup> Year

### **INEEL**

#### Hells Half Acre

Focus on building ties from lab-scale to small-scale to intermediate-scale to full scale  
Continued data analysis  
Instrument development  
Additional Hells Half Acre Testing based on data needs

#### General

Work with problem holders to develop strategies for implementation of technical proposals

#### Lab

Verification of monitoring equipment and testing of new instruments

### **LBNL**

#### Lab

Continued data analysis  
Testing of Hells Half Acre fracture using test approaches developed in year 2  
Analysis of fracture sediment infilling  
Evaluate geometry of field added dye  
Cross-comparison of lab results to INEEL Hells Half Acre field measurements

#### Box Canyon

Possibility of limited field testing at Box Canyon site  
Basic monitoring of drain-out from year 2 tests and natural wetting and drying events

#### Modeling

Modeling at different scales - this may involve a chaotic-dynamical model at small scale and a deterministic model at a larger scale. Probably multi-component. May require some code development.  
With problem holder involvement do a preliminary comparison using new chaotic-dynamical approach to evaluate flow and transport from CERCLA site and contrast to the results from a RI/FS fate and transport model using conventional equivalent porous media approach

#### Instrument Development

Produce demo quality prototype instruments and a conceptual approach for potential application at "live" site  
Develop an "Instrumentation Strategy" including:  
Instruments, passive/active components, hydrogeological and geophysical components

**Reno**

To be included



# IV.

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**Prepared for the U.S. Department of Energy under Contract No. DE-AC03-76SF00098**