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Data-driven background model for the CUORE experiment

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We present the model we developed to reconstruct the CUORE radioactive background based on the analysis of an experimental exposure of 1038.4 kg yr. The data reconstruction relies on a simultaneous Bayesian fit applied to energy spectra over a broad energy range. The high granularity of the CUORE detector, together with the large exposure and extended stable operations, allow for an in-depth exploration of both spatial and time dependence of backgrounds. We achieve high sensitivity to both bulk and surface activities of the materials of the setup, detecting levels as low as 10 nBq kg⁻¹ and 0.1 nBq cm⁻², respectively. We compare the contamination levels we extract from the background model with prior radio-assay data, which informs future background risk mitigation strategies. The results of this background model play a crucial role in constructing the background budget for the CUPID experiment as it will exploit the same CUORE infrastructure.

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I. INTRODUCTION

The Cryogenic Underground Observatory for Rare Events (CUORE [1]) is a ton-scale cryogenic detector located at Laboratori Nazionali del Gran Sasso (Italy). The primary physics goal of the experiment is to search for neutrinoless double-beta decay ($0\nu\beta\beta$) of ¹³⁰Te [2]. $0\nu\beta\beta$ is a hypothetical lepton-number-violating process that, if observed, would demonstrate that neutrinos are Majorana fermions and that lepton number is not a symmetry of nature. Due to the low-background and excellent energy resolution, the experiment is well placed to study other rare decays such as the Standard-Model-allowed two-neutrino double-beta decay ($2\nu\beta\beta$) of ¹³⁰Te and to search for exotic phenomena such as *CPT* or Lorentz non-conservation, charge-violating phenomena, and $0\nu\beta\beta$ via Majoron emission [3].

A thorough understanding of the CUORE background is essential to perform these studies. For example, a robust reconstruction of the background components allows a precise measurement of both half-life and spectral shape of $2\nu\beta\beta$ of ¹³⁰Te [4]. This provides a benchmark to validate approximation methods employed to calculate double- β nuclear matrix elements. In addition, much of the CUORE cryogenic infrastructure will be used to host a next-generation experiment, the CUORE upgrade with Particle IDentification (CUPID [5]). Thus, the characterization of the background by this system on the CUORE detector is essential to build a robust, data-driven background budget for the CUPID experiment.

In this work, we present a comprehensive description of the model used to reconstruct the CUORE data and provide a detailed assessment of the radioactive contamination of

the cryogenic infrastructure and detector components based on a Bayesian analysis, which includes prior information from materials screening carried out as part of CUORE construction.

II. EXPERIMENT OVERVIEW

In this section we briefly summarize the CUORE detector and cryogenic infrastructure, as well as the data selection and production, which are needed for context to describe the model we developed to reconstruct the data. More complete and detailed descriptions of the experiment and infrastructure are available in [6–9].

The CUORE detector (Fig. 1) is a close-packed array of 988 TeO₂ individual crystals operated as cryogenic calorimeters (also called bolometers) arranged into 19 towers of 13 four-crystal floors, i.e. 52 crystals per tower. Each bolometer is instrumented with a Ge Neutron Transmutation Doped (NTD) thermistor to measure the temperature, and with a Si heater to stabilize the detector gain against long-term temperature drifts induced by the cryogenic system. The crystals are supported in the tower structure by a set of copper frames and held in position by Polytetrafluoroethylene (PTFE) spacers. The path for the electrical connection between the on-crystal instrumentation and the front-end electronics [10,11] is provided by copper traces deposited on flexible PEN substrates which span the length of each tower. The detector array is anchored to a copper tower support plate (TSP) placed at the center of a custom ³He/⁴He dilution refrigerator that allows the operation of the bolometers at a temperature of about 10 mK.

The CUORE cryostat comprises six nested copper vessels, which thermalize at decreasing temperatures from room temperature down to 10 mK. Each thermal stage is named for its approximate temperature or by the corresponding component of the dilution unit: 300 K, 40 K, 4 K,

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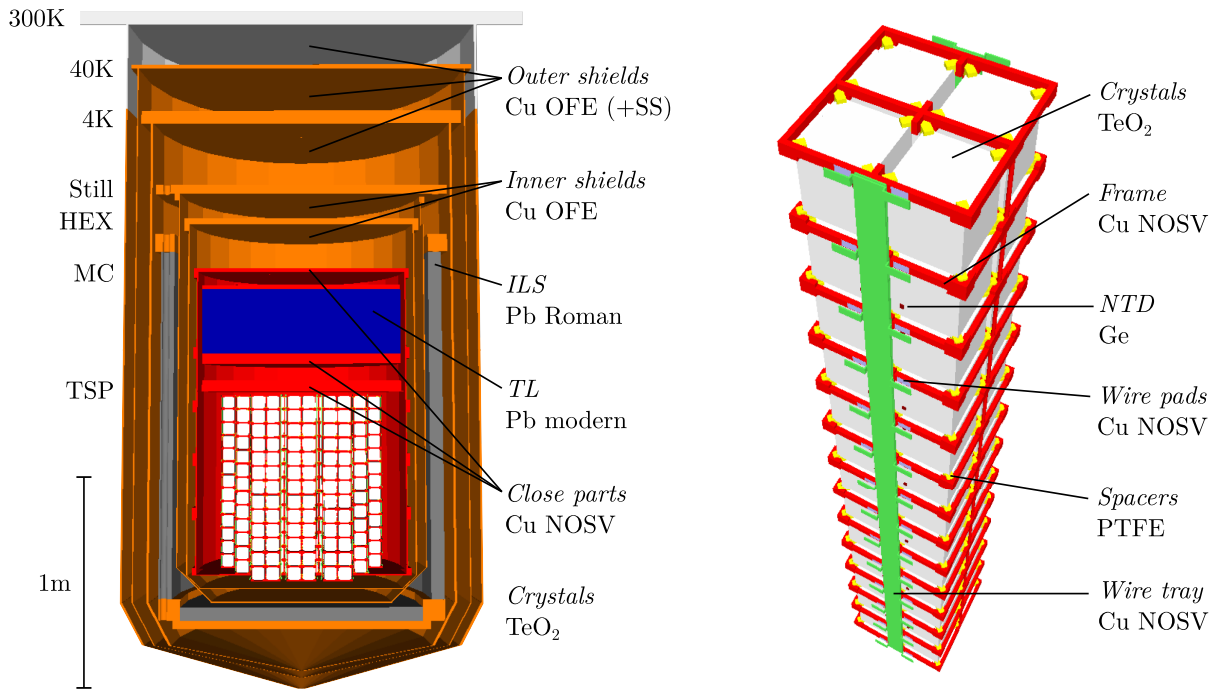


FIG. 1. Left: rendering of the CUORE cryostat and detector as implemented in the Monte Carlo simulation; the actual length scale is reported as a reference. On the left, the different thermal stages are reported; on the right, the volumes are presented as grouped in the Monte Carlo, together with the material they are made of. The TeO₂ crystals are depicted in white, the NOSV copper components in red, the OFE copper in orange, the TL in blue, the ILS in gray and the 300K stainless steel in light gray. Right: detailed view of a CUORE tower, where all the different components are showed in different colors: TeO₂ crystals in white, NOSV-copper frames in red, PTFE supports in yellow, NOSV-copper wire trays in green, and NOSV-copper wire pads in blue.

800 mK or still, 50 mK or heat exchanger (HEX) and 10 mK or mixing chamber (MC). Inside the cryostat, two lead shields protect the detector from the external radioactivity: the inner lead shield (ILS) is suspended between the 4 K and the still stages and provides shielding both laterally as well as from below. The top lead (TL) is positioned below the MC plate and provides shielding from the cryogenic apparatus above. Outside the cryostat, the room temperature external lead shield (ELS) and a neutron shield (made of polyethylene and a layer of boric acid) provide additional shielding from the side and from below.

To minimize background in the experiment, radio-pure materials were selected through dedicated assay campaigns [12]. *Ultracleaning* treatments were developed and applied to the corresponding material [13] to mitigate background induced from residual α decays on critical surfaces. Furthermore, storage and handling protocols were implemented to minimize recontamination during assembly, installation and commissioning of the detector array [14,15].

CUORE began taking data in April 2017 and, to date, more than 2 t yr of TeO₂ exposure have been collected [16]. The data collection is organized into *datasets*, which we define as accumulations of about 1 – 2 months of so-called physics runs sandwiched between a few days of calibration

runs. The physics runs are used for the $0\nu\beta\beta$ search and other studies, including modeling the background sources. The set of data considered for this work corresponds to about a half of the collected exposure, specifically 1038.4 kg yr, and is the same exposure previously analyzed to search for $0\nu\beta\beta$ decay in 2022 [17].

For each detector, we acquire and save a continuous data stream. We trigger thermal pulses by means of the optimum trigger, a trigger algorithm based on the optimum filter (OF [18]), that allows to maximize the signal-to-noise ratio in the frequency domain. We then define 10-s time windows (which include 3-s pretrigger) around the triggered pulse and we apply the OF to compute the pulse amplitude. We correct for gain fluctuations caused by temperature drifts of the system by continuously monitoring the detector response to heater pulses [19]. More specifically, we inject onto the crystals fixed-energy reference pulses every 300 s, and in each run and for each detector we construct the distribution of the tagged pulser events in the amplitude vs baseline space—the baseline is computed as the average value of the pretrigger and acts as a proxy for the crystal’s temperature. We then fit this distribution to determine the detector gain, for which we correct by applying a rotation to the physical pulses. The stabilized pulse amplitudes are converted to energy values by using dedicated calibration data. We use multiple γ

lines from the from ^{232}Th and ^{60}Co sources, which are lowered in the cryostat during the calibration runs, and we fit the energy response by means of a second-order polynomial.

Subsequently, we apply a series of event-selection criteria in order to exclude nonphysical events. These criteria include temporal cuts to eliminate periods of hardware malfunctions, pulse-quality cuts and pulse-shape cuts. In particular, we perform a principal component analysis (PCA) decomposition of signal-like events selected from calibration the γ peaks and produce pulse templates (similar to the OF average pulses) which enclose $> 90\%$ of the pulse variance. By projecting the triggered events onto these templates, we are able to assign high scores to pulses with a closer match and low scores to pulses deviating from the expected shape. Leveraging on the compact design of our detector, where adjacent-crystal distances span between ~ 8 mm and ~ 5 cm (for crystals on different towers), we build multiplets of multicrystal events occurring within a $\mathcal{O}(\text{ms})$ time window. Depending on the specific analysis, we can use the different multiplets in order to exploit several event topologies that likely share a common physics source.

III. BACKGROUND SOURCES AND MONTE CARLO SIMULATIONS

The CUORE background events passing the data-quality selections originate from radioactive contaminants in the experimental setup or from particle fluxes in the external environment, that we call background sources. Each background source produces energy spectra with distinctive features, such as peaks due to γ -rays and α -particle interactions, continuous spectra from β decays or structures due to multisite events or emissions in time coincidence, depending on their location and strength. Moreover, thanks to the modularity of our detector, we exploit signals detected in time coincidence to assess the contamination producing α -decays on crystal surfaces. This also allows maximizing the information on background sources which produce multicrystal events. The CUORE background model aims to determine the activity of the different background sources, by disentangling their contribution to the experimental spectra. This is done by fitting to the data a linear combination of the background sources' induced spectra, obtained with Monte Carlo simulations. The production of the Monte Carlo is a two-step process. First, the simulations for each hypothetical source within the setup are generated with QShields, a Geant4 [20,21] application that simulates particle propagation and interaction throughout the CUORE cryostat and detector; we make use of the standard physics lists QGSP_BERT_HP and Livermore_EM, for hadronic and electromagnetic processes, respectively. Then, the outputs are processed by a software tool, named Ares, which applies the detector response to the raw Monte Carlo and provides as output

simulated events which resemble real data acquired with CUORE.

A. Simulation production

A realistic description of the CUORE geometry and materials in the simulation is crucial for the construction of the background model. In QShields, all the elements described in Sec. II are implemented in the geometrical description. We run a Monte Carlo simulation for each background source identified by a preliminary analysis of the data. In each simulation, a specific radionuclide (or decay chain) is generated in one of the volumes of the geometry, whereas the particle propagation is always considered for the whole geometry. The same contaminant in different volumes can result in very degenerate background spectra, whose differences are below the statistical uncertainty of the experimental data and cannot be disentangled. Therefore, some adjacent volumes are grouped together as having the same contamination if they give completely degenerate spectra. Moreover, setup components which are made of the same grade of material and underwent the same cleaning treatments are assumed to have equal bulk and surface contamination. We designate the following seven main source volumes or volume groups:

- (1) *Crystals*: the TeO_2 crystals, excluding the NTDs and heaters, as they contribute negligibly to the background [12].
- (2) *Close parts*: refer to parts which are close to the detectors, with and without direct line-of-sight to the crystals. Items with direct line-of-sight include the PTFE spacers holding the crystals and copper parts (tower frames, supports for readout wires, tiles covering the inside of the MC shield, guide-tubes of the calibration system [22]). Items with no direct line-of-sight are the MC shield, the TSP, and the plates that sandwich the TL. The copper in the *close parts* volume is electrolytic tough-pitch copper, known commercially as NOSV copper [23], and was selected for its low radioactivity and high thermal conductivity at low temperatures, crucial for the operation of the detector. Although the MC shield is also made of NOSV copper, it underwent a different surface cleaning procedure. Therefore, we assign it the same bulk contamination activity as the other close components but treat its surface contamination separately. PTFE spacers and other NOSV copper parts underwent different ultra-cleaning [6]. Nonetheless, the total mass of PTFE is significantly lower than that of close NOSV-copper tower components and dedicated study could not distinguish their background contribution; therefore PTFE contaminants have been neglected.
- (3) *Inner shields*: thermal radiation shields between the MC and the ILS, namely the HEX and Still vessels and respective top plates. They are made from oxygen-free electrolytic (OFE) C10100 copper.

TABLE I. List of the simulated volumes and contaminants. The arrows indicate fractions of a decay chain assumed to be in secular equilibrium. The partial chain $^{210}\text{Bi} \rightarrow ^{206}\text{Pb}$ has been used to simulate the contamination in equilibrium with ^{210}Pb in *ILS* and *ELS*. This has been done to save computational time, since the contribution from the decay of ^{210}Pb alone is negligible for these volumes. The *MC* volume has been isolated from *close parts* in dealing with superficial contamination because the MC thermal shield underwent a different surface cleaning due to its large size. The internal surface of the shield is covered with tiles, hence the background induced by the MC surface contamination mainly comes from the β/γ radiation of the decay chains. Analogously, we simulate a surface contamination of ^{210}Pb on the *HEX* volume.

Volume	Material	Contaminants
<i>Bulk</i>		
Crystals	TeO ₂	$^{130}\text{Te} \rightarrow 2\nu\beta\beta$, $^{232}\text{Th}/^{228}\text{Ra} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{230}\text{Th}/^{230}\text{Th}/^{226}\text{Ra} \rightarrow ^{210}\text{Pb}/^{210}\text{Pb} \rightarrow ^{206}\text{Pb}$, $^{235}\text{U} \rightarrow ^{231}\text{Pa}/^{231}\text{Pa} \rightarrow ^{207}\text{Pb}$, ^{190}Pt , ^{147}Sm , ^{125}Sb , $^{110\text{m}}\text{Ag}$, $^{108\text{m}}\text{Ag}$, ^{60}Co , ^{40}K
Close parts	Cu NOSV	$^{232}\text{Th} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{206}\text{Pb}$, $^{235}\text{U} \rightarrow ^{207}\text{Pb}$, ^{137}Cs , ^{60}Co , ^{54}Mn , ^{40}K
Inner shields	Cu OFE	$^{232}\text{Th} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{206}\text{Pb}$, ^{137}Cs , ^{60}Co , ^{54}Mn , ^{40}K
ILS	Pb Roman	$^{232}\text{Th} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{206}\text{Pb}$, $^{108\text{m}}\text{Ag}$
Outer shields	Cu OFE	$^{232}\text{Th} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{206}\text{Pb}$, ^{137}Cs , ^{60}Co , ^{54}Mn , ^{40}K
	Stainless steel	
	Superinsulation	
TL	Pb	$^{232}\text{Th} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{206}\text{Pb}$, $^{210}\text{Bi} \rightarrow ^{206}\text{Pb}$
ELS	Pb	$^{210}\text{Bi} \rightarrow ^{206}\text{Pb}$, ^{207}Bi
(External)	...	Cosmic- μ flux
<i>Surface</i>		
Crystals	TeO ₂	$^{232}\text{Th}/^{228}\text{Ra} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{230}\text{Th}/^{230}\text{Th}/^{226}\text{Ra} \rightarrow ^{210}\text{Pb}/^{210}\text{Pb} \rightarrow ^{206}\text{Pb}$, $^{235}\text{U} \rightarrow ^{231}\text{Pa}/^{231}\text{Pa} \rightarrow ^{207}\text{Pb}$
Close parts (no MC)	Cu NOSV	$^{232}\text{Th} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{206}\text{Pb}$, $^{210}\text{Pb} \rightarrow ^{206}\text{Pb}$, $^{235}\text{U} \rightarrow ^{207}\text{Pb}$
MC	Cu NOSV	$^{232}\text{Th} \rightarrow ^{208}\text{Pb}$, $^{238}\text{U} \rightarrow ^{206}\text{Pb}$, $^{210}\text{Pb} \rightarrow ^{206}\text{Pb}$, $^{235}\text{U} \rightarrow ^{207}\text{Pb}$
HEX	Cu OFE	$^{210}\text{Pb} \rightarrow ^{206}\text{Pb}$

- (4) *ILS*: shield made of ancient Roman lead, which is depleted of ^{210}Pb [24].
- (5) *Outer shields*: thermal radiation shields outside the ILS, namely the 4 K, 40 K, and 300 K stage vessels and their respective top plates made of OFE copper. This source volume also includes the stainless-steel cap of the 300 K vessel and superinsulation installed in the cryostat as their contributions to the background are completely degenerate.
- (6) *TL*: shield made of specially selected low-radioactivity lead.
- (7) *ELS*: shield made of commercial low-radioactivity lead but different from that of TL.

QShields can generate and propagate photons, electrons, positrons, α particles, nuclear recoils, neutrons and muons. All primary particles and their resulting secondaries are propagated down to keV energies. Nuclear transitions are based on a customized implementation of the *GARadioactiveDecay* database, which keeps track of the time correlations in the radioactive chains. Bulk contamination is simulated assuming the radio-nuclides uniformly distributed inside the volumes. The only exception to this is our treatment of ^{40}K contamination in one of the towers of the *crystals* volume, which is further described in

Appendix A. Surface contamination is assumed uniform over the surfaces and the corresponding radioactivity concentrations follow exponentially decreasing depth (d) profiles $\exp(-\lambda d)$, where λ is the characteristic depth. To better model the shape of structures we observe in the data associated with α decays, we consider depths spanning from the nm to the tens-of- μm scale.

The identification of the contaminants to be simulated is the combined result of an extensive campaign of radio-assay measurements on different materials. Furthermore, the expectations from the modeling of the CUORE-0 background [25], and the search for distinctive features in the CUORE experimental data contributed to this identification.

The full list of contaminants in each volume is reported in Table I. The complete decay chains of ^{238}U and ^{232}Th are simulated for all volumes, except for *ELS*. For both *TL* and *ELS*, the lower part of the ^{238}U decay chain, from ^{210}Bi to ^{206}Pb is simulated, assuming it in equilibrium with a contamination of ^{210}Pb .¹ The decay chain of ^{235}U is

¹In order to save computational time, we neglect the decay of the ^{210}Pb itself, since it induces a negligible background.

simulated only for *crystals* and *close parts* because of its very weak signatures in the data; its activity is fixed with respect to that of ^{238}U by their natural activity ratio. In TeO_2 and copper we simulate the primordial radio-nuclide ^{40}K . We consider cosmogenic-activation isotopes, namely ^{125}Sb , $^{110\text{m}}\text{Ag}$, $^{108\text{m}}\text{Ag}$ and ^{60}Co in TeO_2 , and ^{60}Co and ^{54}Mn in copper. We also include the fallout products ^{207}Bi in lead (found during radio-assays) and ^{137}Cs in copper (observed in the past CUORE-0 data). Other contaminants of TeO_2 are the long-lived ^{190}Pt , which is contained in macroscopic residues inside the crystals as left-over of the platinum crucibles used during the growth process [26], and a possible contamination of ^{147}Sm (see Appendix B). Lastly, we include in *crystals* the decay of ^{130}Te via $2\nu\beta\beta$ assuming the single-state-dominance model to simulate its spectrum. This work is not devoted to the precise determination of the $2\nu\beta\beta$ spectral shape, and this choice is not impacting the results; previous studies have hinted to a preference for this model [4].

Backgrounds outside the experimental apparatus (neutrons and environmental γ -rays) are shielded at a level that makes them completely negligible for reconstructing the data. The only simulation that does not originate from a volume in the CUORE geometry is the cosmic muon flux.

B. Simulation processing

The QShields output undergoes a post-processing phase implemented in *Ares*, to convert the raw Monte Carlo into CUORE-like data, accounting for detector response effects and data selection cuts made in the analysis [19,27]. In particular, we assign a dataset and a timestamp to the events and include dataset-dependent information, i.e., detector energy resolution, the status of the individual channels (for example active or inactive) and the event-selection efficiencies. In the case of α decays, we apply a quenching factor (QF) to both the α particle and the recoiling nucleus, as described in Appendix B. We account for unresolvable pile-up effects by merging energy depositions occurring in the same crystal within a time window of 5 ms; the outcome is a single event with energy equal to the sum of the individual depositions associated with the event. We discard the resolvable pile-up, i.e. events occurring in the same crystal with a time distance larger than 5 ms but with overlapping acquisition windows. We select events with reconstructed energies greater than 40 keV. This threshold is sufficiently low to fully include structures produced by recoiling nuclei in low-Q-value α decays, while still high enough to exclude the energy region where our control of efficiencies is limited. We also discard events with reconstructed energies larger than 10 MeV, at the limit of our detector dynamic range (saturated events).

Finally, we compute the event *multiplicity* defined as follows: events isolated in time and space are labeled as

multiplicity 1 ($\mathcal{M}1$); events occurring inside a time window of ± 30 ms and involving neighboring crystals closer than 15 cm are grouped into higher multiplicities labeled $\mathcal{M}2$, $\mathcal{M}3$ and so on according to the number of crystals involved. The introduction of the multiplicity label is based on the assumption that events close in space and time likely originate from the same physical process. The sum of the individual energies in the same multiplet is referred to as total-energy of the event.

The simulated spectra at different multiplicities are then used to reconstruct the corresponding ones built with the CUORE data.

IV. FIT PROCEDURE

The CUORE data used to build the background model are organized into a collection of binned energy histograms containing $\mathcal{M}1$ and $\mathcal{M}2$ events. We currently do not consider higher-multiplicity spectra, as we find they provide little additional information to the background model. The only exception is given by the high-multiplicity data used to fix the prior distribution of the muon-induced background (see Sec. IV C). We assume that the number of counts in each bin follows a Poisson probability distribution $Pois(n, \nu)$, where n is the number of events observed by CUORE and ν is the expected value. The latter is defined as a linear combination of the bin counts in the simulated spectra coming from the different background sources, each weighted by its normalization factor. Therefore, considering the i th bin for the energy spectrum κ we can write:

$$\nu_{\kappa,i} = \sum_j N_j (w_{\kappa,i})_j, \quad (1)$$

where index κ runs over the collection of histograms into which the data are organized, including both $\mathcal{M}1$ and $\mathcal{M}2$ events, j runs over the background sources, N_j is the normalization factor of source j , and $(w_{\kappa,i})_j$ is the i th bin content of the spectrum κ for the source j . The total likelihood takes the form

$$\mathcal{L}(\{N_j\}|\text{data}) = \prod_{\kappa} \prod_i Pois(n_{\kappa,i}, \nu_{\kappa,i}) \quad (2)$$

and the normalization factors are the fit parameters. We assign a prior probability distribution to each N_j (see Sec. IV C) and through Bayesian statistical inference using the likelihood outlined in Eq. (2), we sample the multidimensional posterior. The sampling procedure is managed by a Markov-Chain Monte Carlo through a Gibbs sampling algorithm implemented in the JAGS software [28].² Eventually, the activity of each background source is

²The JAGS-based analysis tool has been firstly developed for the background model of CUORE-0 [25] and became a standard for the background models of other $0\nu\beta\beta$ bolometric experiments [29–32].

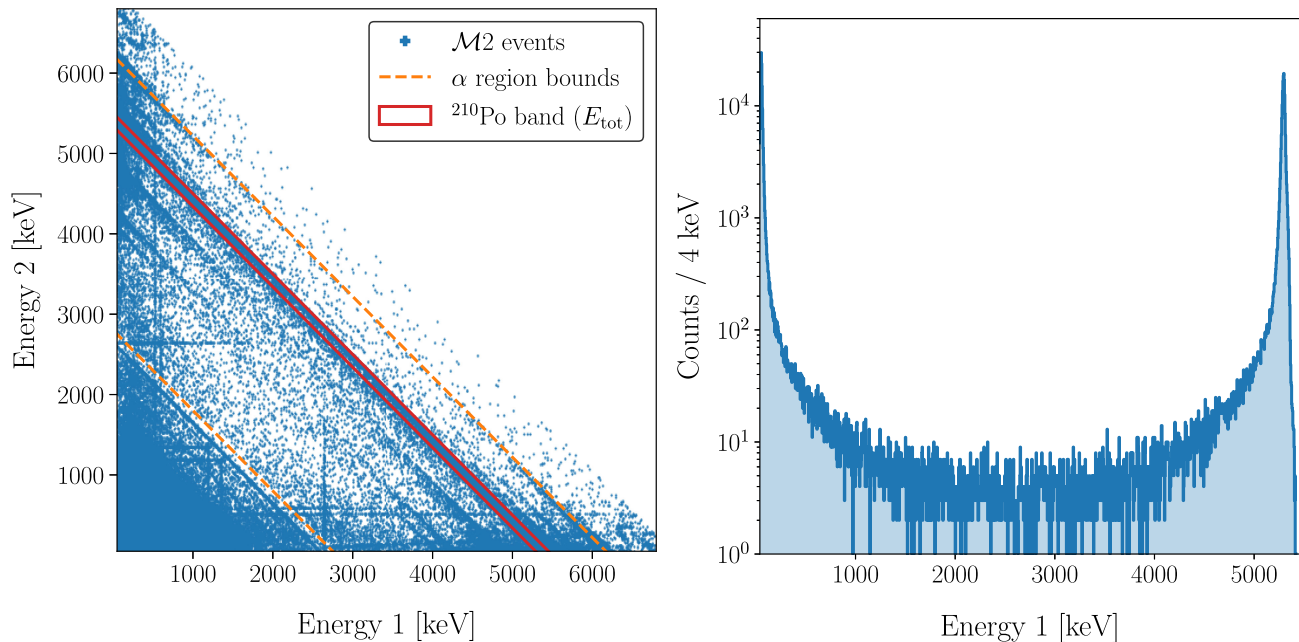


FIG. 2. Left: individual energy depositions in $\mathcal{M}2$ data. The diagonal bands represent events with a constant total-energy shared between the two detectors involved. As an example, the region enclosed by the solid red line corresponds to total energies around the decay of ^{210}Po at 5.4 MeV (summing to the α energy and to the Q-value). The vertical and horizontal bands correspond to full-energy photo-peaks, where almost the totality of the γ -ray energy is registered by one of the two detectors involved in the $\mathcal{M}2$ event. Right: projection of the ^{210}Po -decays for $\mathcal{M}2$ events (region inside the solid red line) onto the x-axis. The peaks at ~ 100 keV ~ 5300 keV are due to the cases of α particle and a recoiling nucleus detected in two different crystals; the region in-between is populated by events where the α particle deposits a fraction of its energy in both crystals.

directly proportional to $\langle N_j \rangle$, that is the mode of the corresponding marginalized posterior distribution.

A. Diagonal-band method

The fit of the $\mathcal{M}2$ spectra allows us to exploit the collective information from the individual energy depositions of multi-crystals events to disentangle different background components. In our previous work [25], the data reconstruction was performed by simultaneously fitting the $\mathcal{M}1$ energy spectrum together with $\mathcal{M}2$ energy and $\mathcal{M}2$ total-energy spectra, that are built by using the same data. In this analysis, we employ a novel *diagonal-band* method, in which we consider multiple uncorrelated $\mathcal{M}2$ energy spectra, thus including precious physical information coming from the $\mathcal{M}2$ total-energy spectrum while eliminating any redundancy.

To describe this procedure, we initially focus on the $\mathcal{M}2$ total-energy spectrum in the range (2.7–6.8) MeV, which we refer to as the α region, as most of the events are produced by α decays. This is shown in Fig. 2, where we depict the α region through the $\mathcal{M}2$ energy-deposition scatter plot. The diagonal bands correspond to $\mathcal{M}2$ events whose total-energy is about-constant, shared differently between the two involved crystals. These bands are mainly caused by α decays happening on the crystal surface, where one crystal detects the recoiling nucleus and possibly a

fraction of the energy of the emitted α particle, while the other crystal detects the remaining part of the α -particle energy. By analyzing the experimental $\mathcal{M}2$ total-energy spectrum, we identify the peaks at the Q-values of the α decays of ^{232}Th and ^{238}U chains (Table VII). We then select the events laying inside the diagonal band associated to a certain total-energy peak and we project its content onto one of the two axes: the corresponding $\mathcal{M}2$ energy spectra built from simulations are used for data reconstruction. As an example, the events due to the α decay of ^{210}Po (red bordered region in Fig. 2) have been selected by consider a total-energy between 5340 and 5500 keV. By repeating this method for a set of disjoint total-energy intervals, we generate a set of $\mathcal{M}2$ spectra. The vast majority of the events within each $\mathcal{M}2$ spectrum stems from the same contaminant in different locations. As a result, the degeneracy between background sources is mitigated and the correlations are reduced.

The selected intervals do not cover the whole α region. Each selected diagonal band corresponds to a peak in the total-energy spectrum, while we exclude tails where the spectrum shape is not sufficiently well modeled in the simulation and regions in between peaks where no structure is present. Ideally, the total energy of an $\mathcal{M}2$ event corresponding to an α decay should mainly fall within a narrow band around the transition Q-value, however we observe wide tails characterized by an increase in the count

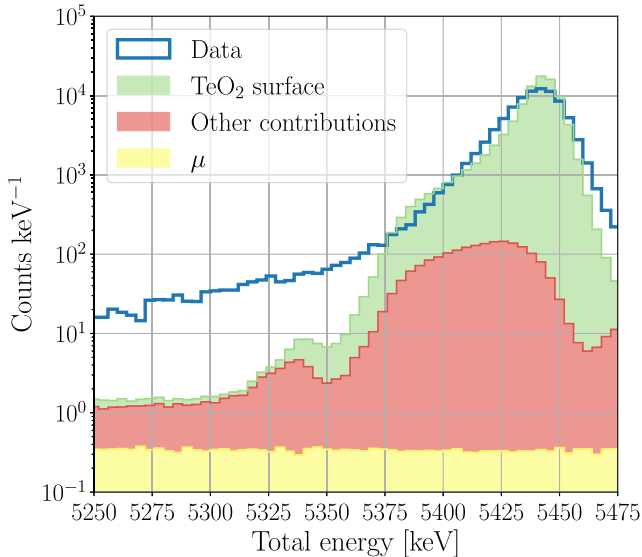


FIG. 3. Zoom-in on the 5.4-MeV α peak of ^{210}Po . The data are depicted in blue while the backgrounds, organized to emphasize the main expected contributions, are shown as stacked histograms. A fraction of the events lies in the long tail on the low-energy side; this structure is probably due to surface effects affecting the decays originating from the surface of detectors. Since we lack an effective model explaining these effects, the Monte Carlo reconstruction (see Sec. V for details on the individual contributions) is not able to fully describe this region.

rate when approaching the Q-value (Fig. 3). We explored two possible origins for these events: α particles or daughter nuclei scattering out of a crystal and ending up in a passive material; or $\mathcal{M}2$ event not being due to an α decay but rather some other multi-crystal event such as muon showers. However, the former has an extremely low probability of occurrence, while the latter requires a muon flux which is inconsistent with that observed in the experimental hall. The energy ranges in question are predominantly populated by α decays originating from the surface of detectors, which suggests that we are observing unmodeled surface effects. The fraction of events contained in these off-peak energy intervals is relatively small, $\sim 6\%$, therefore we exclude them from the reference background-model fit. To be conservative, we quote as a systematic uncertainty the difference between the fit with and without these regions included (Sec. IV D).

Analogously to the α case, we also split the region below 2.7 MeV, which we refer to as the γ region, into independent diagonal bands based on the peaks identified in the total-energy spectrum (Table VI). Since we can explain all the structures visible in the total-energy spectrum of the γ region, here the bands cover the whole energy range.

B. Energy window and binning

The fit window spans over the energy range (0.2–6.8) MeV, apart from the $\mathcal{M}2$ spectra of the α region,

for which we set the lower bound to 40 keV in order to fully exploit the information on energy depositions of recoiling nuclei (~ 100 keV). Widening the fit toward lower energies worsens the data-reconstruction quality because of possible missing or poorly modeled background contributions and uncertainties on the detector response. At the same time, extending the upper bound to higher energies offers little benefit, as there are a few events and very few structures identifiable in the spectrum and our knowledge of energy-dependent quantities such as calibration and data-selection efficiencies becomes poor.

We build the fit energy histograms using nonuniform energy bins. In the γ region, around each identified line, we define single bins whose width is equivalent to 5 times the energy resolution computed at the centroid of the peak. We divide the regions that fall in between γ -ray peaks into equally sized bins, with a minimum size of 15 keV for the $\mathcal{M}1$ spectra and 40 keV for the $\mathcal{M}2$ spectra. This partition avoids systematic effects due to the energy calibration and peak-shape modeling. In the α region, since we lack a satisfactory model of the off-peak tails, we manually select the bin edges to include all the counts from a specific spectral feature inside single wide bins. If required, we then merge adjacent bins to reach a minimum number of 50 counts per bin. A summary of all the identified lines used to define the binning in both the α and γ regions is reported in Appendix C.

C. Prior selection

As inputs to the Bayesian model, we make use of prior probability distributions which describe our existing knowledge of a specific contamination or, equivalently, fit parameter. When no *a priori* information is applicable, we assume a uniform probability distribution ranging from zero to the maximum value that prevents the simulated component exceeding the data.³ Conversely, we make use of prior information the CUORE-0 background model [25] or from independent sources, when available. If a contamination has been measured, we assign a Gaussian probability with corresponding mean and standard deviation; in cases where there is only an upper limit, we take as prior an exponential distribution whose 90% quantile matches the limit at 90% CL.

For surface contamination of detector and near-detector elements, we observe contributions higher than what we would have inferred from CUORE-0, mainly for the ^{210}Pb surface contamination of *close parts*. This is possibly due to recontamination of surfaces during the period when the towers were under storage. Therefore, in these cases we do not make use of priors based on external measurements.

³In order to be more conservative, we compute maximum value of the prior by accounting for the statistical uncertainty of both data and Monte Carlo, therefore, fluctuating the data upward by 2σ and the Monte Carlo downward by 2σ .

We set a prior for the simulation of cosmic muons as well. Since the $\mathcal{M}1$ and $\mathcal{M}2$ energy spectra contain few muon-induced events, leaving the muon normalization unconstrained leads to a significant overestimation of the high-multiplicity spectra, which receive the main contribution from muons. Therefore, we first fit these high-multiplicity data and extract the prior of the corresponding normalization factor. The total muon flux we obtain is compatible with that measured by MACRO [33].

D. Systematics

Inevitably, some of the assumptions made constructing the background model are a potential source of systematic uncertainty. Examples include our parametrization of the detector response to α particles with a QF, the assumption that the background contributions are uniformly distributed in each volume, and the assumption that activities are constant over time.

We identify different classes of systematic uncertainties which share a common cause in the fit specifications and we estimate their impact on the background model results by repeating the fit while varying these specifications. We then compare the result with the default fit and use the difference we observe to quantify the associated systematic uncertainty.

In particular, we take into account the following effects:

Binning: we consider different (constant) bin-widths for the γ region and we perform a separate fit where we include the off-peak intervals in the $\mathcal{M}2$ spectra associated with the α region.

Energy threshold: we move the low-energy cut off of the fit in the range (150–250) keV.

Geometry: we individually fit each floor and each tower of CUORE.

Dataset: we individually fit each of the 15 datasets used in this analysis.

^{90}Sr : we repeat the fit adding a contamination of ^{90}Sr in the TeO_2 (see Appendix B).

We note that for the *binning* and *energy threshold* classes, exploring the systematic variation of the results requires fitting partially or completely overlapping set of data. Therefore, when computing the corresponding uncertainty, we conservatively pick the largest deviation from the default fit. For the *geometry* and *dataset* classes, where the fit is repeated on independent subdivisions of the data, we quantify the associated systematic as the average distance of the results from the default fit, weighted for the inverse-square of the posterior width. In both cases, if the reference fit converges to a value different from zero, we then subtract in quadrature the average statistical uncertainty of the single fits; conversely, if the reference fit is compatible with zero, we quote a 90% credibility interval (CI) limit.

Concerning the $2\nu\beta\beta$, despite this work is not focused on the decay spectral shape, we tested alternative models to the

single-state-dominance and verified that the choice has a negligible impact on all the contaminants.

V. RESULTS

In Fig. 4, we show the reconstruction of the CUORE data with the background model. The top plot contains the fit of $\mathcal{M}1$ events, while the bottom one depicts the projections of the $\mathcal{M}2$ energy histograms used for the fit onto a single spectrum. In general, we observe a good agreement between the fit and the observed data and we find only a few bins in the $\mathcal{M}1$ reconstruction which show significant residuals. These are mainly in the α region, where our understanding of the detector response is incomplete and we cannot describe the peak shape, and around 2.2 MeV, where we observe an excess in the counts.

By grouping the different contributions according to the volumes used to simulate the CUORE geometry, we obtain the spectrum decomposition of Fig. 5. In the low-energy region until 400 keV, the leading contribution to the background is represented by Bremsstrahlung photons following the β decay of ^{210}Bi , mainly from the *TL*, *HEX*, and *MC* volumes. Between 500 keV and 2 MeV, the spectrum is dominated by the $2\nu\beta\beta$ of ^{130}Te . The remaining part of the γ region mostly sees a continuum from the very-shallow contamination of ^{232}Th , ^{238}U , and ^{210}Pb mainly from *close parts*. The α region contains the contribution of multiple α emitters from the U and Th decay chains due to contaminants shared between *crystals*, mostly producing full-energy peaks, and *close parts*, giving a continuum due to degraded α -events from copper. This results in a flat spectrum until 4 MeV, below which the line of ^{190}Pt from the bulk contamination of the crystals is the only clear signature present. Above we see multiple peaks, the most prominent coming from the decay of ^{210}Po .

The complete list of reconstructed activities is reported in Tables II and III for the bulk and surface contributions, respectively. Each activity is provided either as a value, with associated statistical uncertainty, or as a limit. In the former case, we extract the mode of the posterior probability distribution and take the narrowest 68%-interval containing the mode to estimate the uncertainty; in the latter case, we take the 90% quantile of the posterior. We compute systematic uncertainty ranges for each class according to the procedure described in the previous section and the systematic uncertainty reported is the narrowest interval that contains these bands.

We tested the stability of the results by repeating the analysis without informative priors, except for the muon normalization. We observe no noteworthy differences with respect to the reference fit. When considering both statistical and systematic uncertainties, all the activities coming from the reference fit are compatible with the considered prior knowledge. The detailed model coupled with the high collected statistics allows CUORE to measure activities

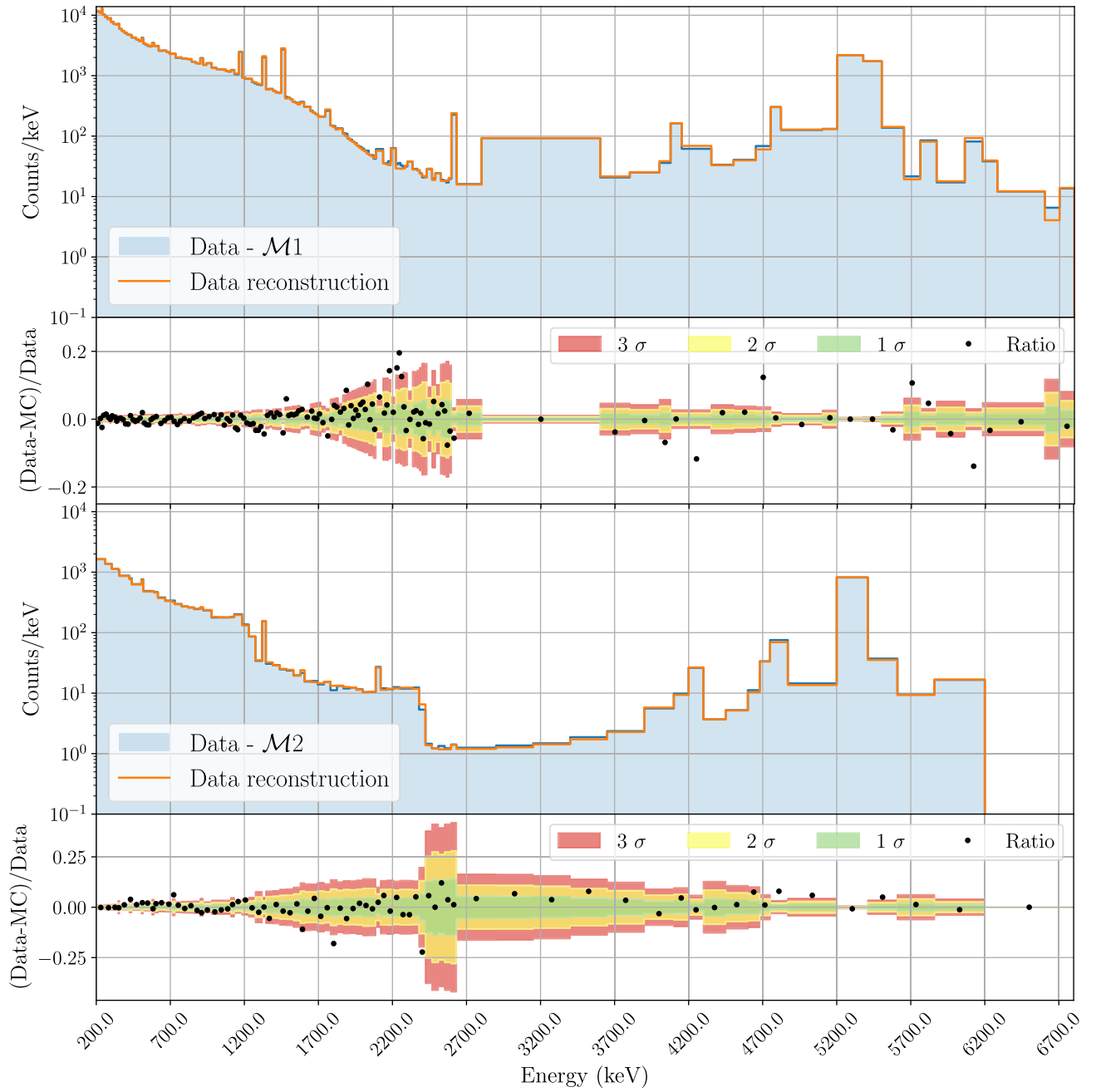


FIG. 4. Top panels: reconstruction of the $\mathcal{M}1$ events and residuals. Bottom panels: cumulative spectrum of the individual $\mathcal{M}2$ events and residuals. The residuals are quoted as fractions of data, with the statistical uncertainties represented as 1σ , 2σ , and 3σ standard-deviation bands. The $\mathcal{M}2$ spectrum ends at 6200 keV because this is the maximum energy for the events in the highest total-energy band taken into account.

down to ~ 10 nBqkg $^{-1}$ for bulk and ~ 0.1 nBqcm $^{-2}$ for surface contamination, reaching the highest sensitivity for very-close sources.

In general, statistical uncertainties are low, on the order of 15% or less. We observe correlations mainly among *close parts*, *inner shields* and *ILS* for ^{60}Co , ^{40}K and the natural decay chains. This is due to the very degenerate contribution of these sources and limited prior knowledge.

Systematic uncertainties caused by varying the *binning* or *energy threshold* are subdominant. On the other hand, the biggest variations are observed in the *geometry* and *dataset* classes. In the *geometry* class, some variations in fit results were expected while others were not. For example, ^{190}Pt is accidentally included during the crystal growth in the form of microscopic clusters and this naturally leads to sparse and unpredictable contamination in the crystals.

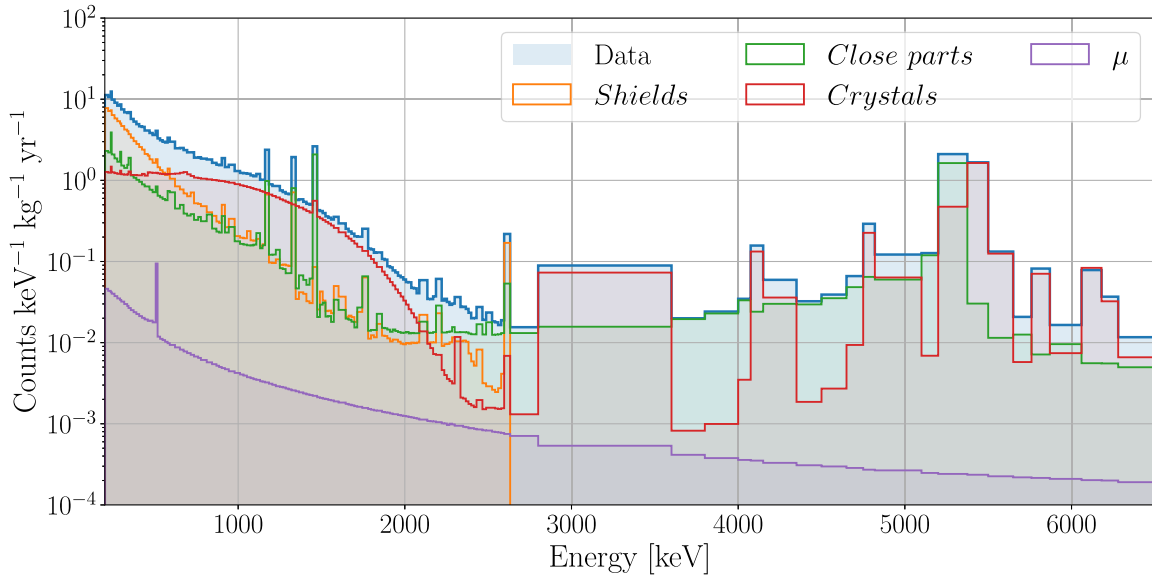


FIG. 5. Decomposition of the CUORE data by source location. The *Shields* group includes the volumes *ELS*, *outer shields*, *TL*, *ILS*, and *inner shields*.

TABLE II. Activities of the bulk contamination. For each volume, the individual contributions are listed; where a single nuclide is reported, we refer to its full decay chain. When present, we include our prior knowledge from either CUORE-0 [25], from radio-assay measurements (HPGe or neutron-activation analysis). The posterior modes, i.e., the fit results, are quoted together with their statistical uncertainty and the largest associated systematic error, which is implicitly expressed with the same order of magnitude of the reference value. When the mode is compatible with zero, we quote the 90% C.I. as a limit on the activity. The activity of ^{235}U is fixed with respect to that of ^{238}U by their natural activity ratio. For the specific activity of ^{40}K in tower 12 see Appendix A.

Volume	Contaminant	Prior [Bq kg ⁻¹]	Mode/Limit [Bq kg ⁻¹]	Systematic	
<i>Crystals</i>	$^{130}\text{Te } 2\nu\beta\beta$		$(3.03 \pm 0.01) \times 10^{-5}$	+0.11 -0.17	
	^{232}Th	$< 1.2 \times 10^{-7}$	CUORE-0	$(2.75 \pm 0.05) \times 10^{-7}$	+0.85 -1.47
	$^{228}\text{Ra} \rightarrow ^{208}\text{Pb}$	$< 7.5 \times 10^{-8}$	CUORE-0	$(1.19 \pm 0.04) \times 10^{-7}$	+0.2 -1.16
	$^{238}\text{U} \rightarrow ^{230}\text{Th}$	$< 3.6 \times 10^{-8}$	CUORE-0	$< 6.36 \times 10^{-10}$	
	^{230}Th	$(2.8 \pm 0.3) \times 10^{-7}$	CUORE-0	$(3.85 \pm 0.06) \times 10^{-7}$	+0.26 -1.3
	$^{226}\text{Ra} \rightarrow ^{210}\text{Pb}$	$< 2.2 \times 10^{-8}$	CUORE-0	$< 4.63 \times 10^{-10}$	
	^{210}Pb	$(1.37 \pm 0.83) \times 10^{-6}$	CUORE-0	$(1.55 \pm 0.02) \times 10^{-6}$	+0.44 -1.48
	$^{235}\text{U} \rightarrow ^{231}\text{Pa}$			$< 2.92 \times 10^{-11}$	
	$^{231}\text{Pa} \rightarrow ^{207}\text{Pb}$			$< 9.06 \times 10^{-10}$	
	^{190}Pt	$(1.95 \pm 0.05) \times 10^{-6}$	CUORE-0	$(1.93 \pm 0.01) \times 10^{-6}$	+0.29 -0.3
	^{147}Sm			$(1.09 \pm 0.12) \times 10^{-8}$	+0.67 -0.58
	^{125}Sb			$(2.93 \pm 0.11) \times 10^{-6}$	+2.42 -1.44
	$^{110\text{m}}\text{Ag}$			$(9.06 \pm 2.44) \times 10^{-8}$	+62.58 -2.45
	$^{108\text{m}}\text{Ag}$			$(6.02 \pm 1.08) \times 10^{-8}$	+2.61 -2.66
	^{60}Co	$(3.0 \pm 1.4) \times 10^{-7}$	CUORE-0	$(1.86 \pm 1.22) \times 10^{-8}$	+4.21
	^{40}K (no Tower 12)	$< 8.2 \times 10^{-6}$	CUORE-0	$(4.30 \pm 0.12) \times 10^{-6}$	+2.62 -1.11
	^{40}K (Tower 12)			$(2.45 \pm 0.68) \times 10^{-5}$	+1.49 -0.63

(Table continued)

TABLE II. (Continued)

Volume	Contaminant	Prior [Bq kg ⁻¹]	Mode/Limit [Bq kg ⁻¹]	Systematic	
<i>Close parts</i>					
	²³² Th	$< 2.1 \times 10^{-6}$	CUORE-0	$< 3.88 \times 10^{-7}$	
	²³⁸ U	$< 2.2 \times 10^{-5}$	CUORE-0	$< 4.73 \times 10^{-7}$	
	²³⁵ U			$< 2.17 \times 10^{-8}$	
	¹³⁷ Cs	$< 2.2 \times 10^{-5}$	HPGe	$(1.25 \pm 0.24) \times 10^{-6}$	-0.71
	⁶⁰ Co	$< 2.5 \times 10^{-5}$	HPGe	$(2.04 \pm 0.03) \times 10^{-5}$	+0.32 -0.39
	⁵⁴ Mn	$< 3.1 \times 10^{-5}$	HPGe	$(2.29 \pm 0.33) \times 10^{-6}$	+2.63 -1.93
	⁴⁰ K			$(4.42 \pm 0.06) \times 10^{-4}$	-1.06
<i>Inner shields</i>					
	²³² Th	$< 6.4 \times 10^{-5}$	HPGe	$(4.10 \pm 0.39) \times 10^{-5}$	+1.92 -2.54
	²³⁸ U	$< 5.4 \times 10^{-5}$	HPGe	$(7.71 \pm 5.03) \times 10^{-6}$	+16.51
	¹³⁷ Cs			$< 1.92 \times 10^{-6}$	
	⁶⁰ Co	$< 2.4 \times 10^{-5}$	HPGe	$(1.46 \pm 0.19) \times 10^{-5}$	+4.89 -1.44
	⁵⁴ Mn			$< 3.71 \times 10^{-6}$	
	⁴⁰ K	$< 6.7 \times 10^{-4}$	HPGe	$< 3.48 \times 10^{-5}$	
<i>Outer shields</i>					
	²³² Th			$< 2.45 \times 10^{-5}$	
	²³⁸ U			$< 4.02 \times 10^{-5}$	
	¹³⁷ Cs			$< 7.33 \times 10^{-4}$	
	⁶⁰ Co			$(1.45 \pm 0.04) \times 10^{-3}$	+0.29 -0.87
	⁵⁴ Mn			$< 2.14 \times 10^{-4}$	
	⁴⁰ K			$< 8.61 \times 10^{-4}$	
<i>ILS</i>					
	²³² Th	$(3.9 \pm 2.2) \times 10^{-5}$	CUORE-0	$(1.70 \pm 0.22) \times 10^{-5}$	+0.62 -0.8
	²³⁸ U	$(2.7 \pm 1.0) \times 10^{-5}$	CUORE-0	$< 1.61 \times 10^{-6}$	< 11.44
	^{108m} Ag			$(7.99 \pm 0.78) \times 10^{-6}$	+2.62 -3.72
	⁴⁰ K			$< 3.87 \times 10^{-5}$	< 18.58
<i>TL</i>					
	²³² Th			$(3.06 \pm 1.47) \times 10^{-4}$	+22.95 -2.74
	²³⁸ U	$< 1.1 \times 10^{-3}$	HPGe	$(3.45 \pm 0.36) \times 10^{-3}$	-3.44
	²¹⁰ Bi → ²⁰⁶ Pb			$(1.61 \pm 0.02) \times 10^{+2}$	+0.51 -0.41
	⁴⁰ K	$< 7.6 \times 10^{-3}$	HPGe	$(3.74 \pm 2.64) \times 10^{-3}$	+7.49 -3.01
<i>ELS</i>					
	²¹⁰ Bi			$(3.31 \pm 0.14) \times 10^{+2}$	+1.35 -1.86
	²⁰⁷ Bi			$(2.29 \pm 0.20) \times 10^{-3}$	+1.21 -1.47

On the other hand, we observe that the activities of the most superficial ²¹⁰Pb in both *close parts* and *crystals* show a very scattered distribution when fitting single floors and towers. This is likely due to different exposure to ²²²Rn during the transportation and storage phases before the experiment. Another source of geometric variation shows up as monotonic trends in the activity of ²¹⁰Pb in TL, HEX and MC with respect to top-bottom slices of the detector.

This can be connected with the asymmetrical arrangement of the cryostat elements, concentrated in the upper part (TSP and TL) and around the structure (mainly MC and HEX) which is correctly rendered in the simulation. This points to possible dis-uniformities in the activity of the innermost shields.

Turning to the *dataset* systematic class, we observe relatively small time-related variations in some activities of

TABLE III. Activities of the surface contamination. For each volume, the individual contributions at different depths are listed; where a single nuclide is reported, we refer to its full decay chain. The posteriors modes, i.e., the fit results, are quoted together with their statistical uncertainty and the largest associated systematic error, which is implicitly expressed with the same order of magnitude of the reference value. When the mode is compatible with zero, we quote the 90% C.I. as a limit on the activity. The activity of ^{235}U is fixed with respect to that of ^{238}U by their natural activity ratio.

Volume	Contaminant	Depth [μm]	Mode/Limit [Bq cm^{-2}]	Systematic
<i>Crystals</i>				
	^{210}Pb	0.001	$(7.32 \pm 0.02) \times 10^{-8}$	+4.98 -3.23
	^{232}Th	0.01	$(3.10 \pm 0.14) \times 10^{-10}$	+0.2 -2.98
	$^{228}\text{Ra} \rightarrow ^{208}\text{Pb}$	0.01	$(1.10 \pm 0.03) \times 10^{-9}$	+0.69 -0.19
	$^{238}\text{U} \rightarrow ^{230}\text{Th}$	0.01	$(1.90 \pm 0.03) \times 10^{-9}$	-1.08
	^{230}Th	0.01	$(8.22 \pm 0.32) \times 10^{-10}$	+13.51 -0.4
	$^{226}\text{Ra} \rightarrow ^{210}\text{Pb}$	0.01	$(2.56 \pm 0.04) \times 10^{-9}$	+1.52 -1.12
	$^{235}\text{U} \rightarrow ^{231}\text{Pa}$	0.01	$(8.74 \pm 0.01) \times 10^{-10}$	-0.50
	$^{231}\text{Pa} \rightarrow ^{207}\text{Pb}$	0.01	$(1.05 \pm 0.34) \times 10^{-10}$	+1.07 -0.66
	^{232}Th	0.1	$(3.21 \pm 1.52) \times 10^{-11}$	+3.21
	$^{228}\text{Ra} \rightarrow ^{208}\text{Pb}$	0.1	$(5.34 \pm 0.34) \times 10^{-10}$	-5.27
	$^{238}\text{U} \rightarrow ^{230}\text{Th}$	0.1	$(9.15 \pm 2.65) \times 10^{-11}$	+36.50 -8.35
	^{230}Th	0.1	$(8.64 \pm 2.56) \times 10^{-11}$	+7.75 -3.98
	$^{226}\text{Ra} \rightarrow ^{210}\text{Pb}$	0.1	$(9.10 \pm 0.40) \times 10^{-10}$	+1.31 -8.71
	^{210}Pb	0.1	$(1.31 \pm 0.01) \times 10^{-8}$	+0.29 -0.17
	$^{235}\text{U} \rightarrow ^{231}\text{Pa}$	0.1	$(4.21 \pm 1.22) \times 10^{-12}$	+16.78 -3.84
	$^{231}\text{Pa} \rightarrow ^{207}\text{Pb}$	0.1	$< 6.06 \times 10^{-11}$	
	^{232}Th	1	$(7.77 \pm 1.74) \times 10^{-11}$	-3.81
	$^{228}\text{Ra} \rightarrow ^{208}\text{Pb}$	1	$(1.86 \pm 0.19) \times 10^{-10}$	+10.17 -1.06
	$^{238}\text{U} \rightarrow ^{230}\text{Th}$	1	$(2.84 \pm 0.14) \times 10^{-10}$	+0.51 -1.11
	^{230}Th	1	$(9.32 \pm 1.84) \times 10^{-11}$	+18.73 -5.25
	$^{226}\text{Ra} \rightarrow ^{210}\text{Pb}$	1	$(3.08 \pm 0.15) \times 10^{-10}$	+1.41 -2.58
	^{210}Pb	1	$(5.15 \pm 0.10) \times 10^{-9}$	+0.7 -0.94
	$^{235}\text{U} \rightarrow ^{231}\text{Pa}$	1	$(1.31 \pm 0.06) \times 10^{-11}$	+0.23 -0.51
	$^{231}\text{Pa} \rightarrow ^{207}\text{Pb}$	1	$< 2.23 \times 10^{-11}$	
	^{232}Th	10	$(1.18 \pm 0.28) \times 10^{-10}$	+7.12
	$^{228}\text{Ra} \rightarrow ^{208}\text{Pb}$	10	$(3.29 \pm 1.27) \times 10^{-11}$	+61.54
	$^{238}\text{U} \rightarrow ^{230}\text{Th}$	10	$< 1.99 \times 10^{-11}$	
	^{230}Th	10	$(2.17 \pm 0.25) \times 10^{-10}$	+5.95 -0.78
	$^{226}\text{Ra} \rightarrow ^{210}\text{Pb}$	10	$(1.82 \pm 0.86) \times 10^{-11}$	+10.24 -1.46
	^{210}Pb	10	$(2.23 \pm 0.09) \times 10^{-9}$	+2.48 -2.18
	$^{235}\text{U} \rightarrow ^{231}\text{Pa}$	10	$< 9.15 \times 10^{-12}$	
	$^{231}\text{Pa} \rightarrow ^{207}\text{Pb}$	10	$< 1.37 \times 10^{-11}$	
<i>Close parts</i>				
	^{232}Th	0.01	$(1.35 \pm 0.06) \times 10^{-9}$	+0.51 -0.51
	^{238}U	0.01	$(1.24 \pm 0.07) \times 10^{-9}$	+0.44 -0.68
	^{210}Pb	0.01	$(3.40 \pm 0.02) \times 10^{-7}$	+1.22 -0.96
	^{210}Pb	0.1	$(6.48 \pm 0.25) \times 10^{-8}$	-3.55
	^{235}U	0.01	$(5.71 \pm 0.03) \times 10^{-10}$	+0.20 -0.31

(Table continued)

TABLE III. (*Continued*)

Volume	Contaminant	Depth [μm]	Mode/Limit [Bq cm^{-2}]	Systematic
	^{210}Pb	1	$(5.23 \pm 0.19) \times 10^{-8}$	+3.15 -0.69
	^{232}Th	10	$(1.15 \pm 0.05) \times 10^{-8}$	+0.34 -0.64
	^{238}U	10	$(8.35 \pm 0.68) \times 10^{-9}$	-3.96
	^{210}Pb	10	$(6.85 \pm 0.69) \times 10^{-8}$	+4.88 -4.23
	^{235}U	10	$(3.84 \pm 0.31) \times 10^{-10}$	-1.82
<i>MC</i>	^{232}Th	0.01	$< 4.36 \times 10^{-9}$	
	^{238}U	0.01	$(6.79 \pm 1.32) \times 10^{-8}$	-6.42
	^{210}Pb	0.01	$< 2.05 \times 10^{-5}$	< 17.11
	^{235}U	0.01	$(3.12 \pm 0.61) \times 10^{-9}$	-2.95
<i>HEX</i>	^{210}Pb		$(8.23 \pm 0.20) \times 10^{-4}$	+6.43 -6.43

isotopes with very long half-life or in equilibrium with their progenitors. However, expected dataset-dependent effects, such as channel status and analysis efficiencies, are accounted for during the *Ares* processing. We therefore fold these into the associated uncertainty as described above. Conversely, there are cases where a time-dependent activity is expected, as for the cosmogenic activation isotopes ^{125}Sb , ^{54}Mn , and ^{60}Co , which have half-lives comparable to the data-collection time of CUORE. For such cases, we compute the systematic uncertainty differently, by utilizing the distance of the single fits with respect to the decay trend computed from the reference fit value, as exemplified in Fig. 6. The starting specific activity for the decay trend is determined from reference-fit specific activity, as it represents the time-integrated counts per dataset over the total exposure of the datasets while the specific decay half-life is fixed to tabulated values. This type of analysis is important to verify *a-posteriori* if the storage time of the components was suitable and to study the continuous material activation underground which gives a time-constant contribution. In addition to the cosmogenic isotopes mentioned above, ^{210}Pb in both *crystals* and *close parts* shows a clear decay in time that matches the expected half-life of ^{210}Po , that is 138.4 days. The component not in equilibrium with ^{210}Pb completely decayed within the first two datasets.

Another interesting result from the background model is the set of components contributing to background in the region of interest for the $0\nu\beta\beta$ search near $Q_{\beta\beta} = 2526.97(23)$ keV [34]. It has to be noted that the cuts adopted for the CUORE background model differ from those of the $0\nu\beta\beta$ studies. In this work, we set a less stringent pulse-shape cut and a different coincidence window. These data-selections have been specifically optimized for this analysis, which covers the whole energy

range of the detector and it is not limited to a narrow region of interest (ROI) around the $Q_{\beta\beta}$. In order to extract the ROI background index (BI), we apply to the MC simulations of the background sources the same pulse-ts and the same coincidence window used for the $0\nu\beta\beta$ analysis. The result is shown in Fig. 7 and has been derived by evaluating the integral of all the background components in the ROI, repeating this procedure for all the fits utilized for the systematic studies. The light blue and blue bars refer to the 16% and 84% quantiles of the resulting distributions,

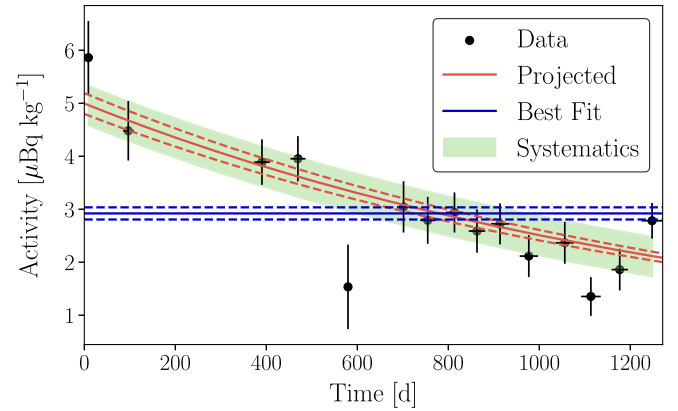


FIG. 6. Activity of ^{125}Sb in the *crystals* volume extracted from the individual-dataset fits (black dots). The blue lines (solid and dashed) depict the mode and the statistical uncertainty of the activity from the best fit, where all the dataset are grouped together. The red line is the projected time-dependent activity, computed by assuming the best fit to be the integral average along time of a decaying activity with the tabulated half-life of 2.76 yr. The green band shows the systematic uncertainty coming from the comparison between each individual-dataset fit and the time-dependent activity obtained by the reference fit.

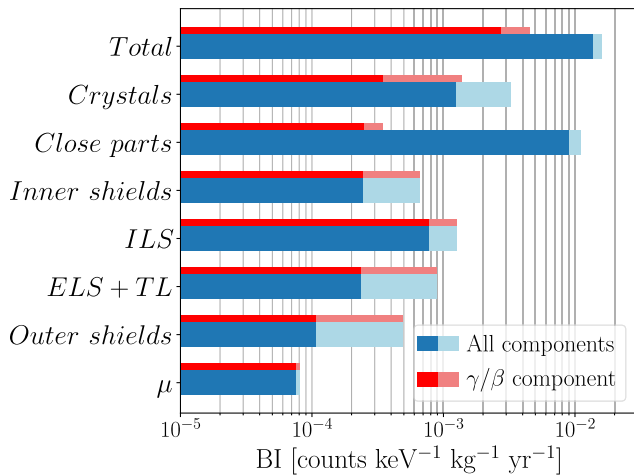


FIG. 7. BI components obtained from the full set of fits used to extract the systematic uncertainty. The light (dark) blue band represent the 16% (84%) quantile of the BI distribution obtained. The red bands indicate the corresponding fraction due to β and γ events.

respectively. Their red counterparts quote the background induced by only considering γ and β particles.

The total BI = $1.48_{-0.10}^{+0.12} \times 10^{-2}$ counts keV $^{-1}$ kg $^{-1}$ yr $^{-1}$, where the value and the uncertainty come from the average BI and the [0.16%, 0.84%] quantiles of the full set of fits used to study the systematic uncertainties, respectively. In particular, we find that approximately 75% of the BI is attributable to α events, mainly coming from the *close parts*, where we define an α event to be one where at least 90% of the event energy came from an α decay. This is consistent with the BI obtained with the $0\nu\beta\beta$ fit applied on the same set of data [17], that is $1.49 \pm 0.04 \times 10^{-2}$ counts keV $^{-1}$ kg $^{-1}$ yr $^{-1}$. Upon comparing these results with the CUORE background projections [12] we observe no noteworthy difference except for *close parts*, which shows a $\sim 15\%$ higher contribution to the BI because of the aforementioned possible recontamination. While the bulk contamination is in line with the projections, surface contamination is higher than expected. Indeed, bulk activities can be easily measured with high precision; however, the reliability of surface contamination estimates is hindered by challenging measurements and potential risk of recontamination during the storage and commissioning phases.

VI. SUMMARY

We presented the background model of the CUORE data based on an exposure of 1038.4 kg yr. The data reconstruction is achieved by means of a multiparametric Bayesian fit of 39 spectra encompassing $\mathcal{M}1$ and $\mathcal{M}2$ events across a broad energy range (0.2, 6.8) MeV. Our model describes the observed data well and comparing the results with the CUORE background projections [12] we

observe that all components match the expectations except for some surface contamination of the *crystals* and *close parts* volumes. These findings reveal the reliability of the materials screening techniques and emphasize the importance of reliable surface contamination assay and monitoring to mitigate the risk of surface contamination. By subdividing the data in geometric and time slices, we can localize background components to analyze and model their spatial distribution across the detector, and we can study the time evolution of specific contamination. This robust reconstruction of the data over a broad energy range is the basis of forthcoming physics analyses which rely on the continuum spectrum observed in CUORE, for example investigation of the $2\nu\beta\beta$ spectrum of ^{130}Te to explore nuclear effects on the spectral shape [30,32,35,36].

The information extracted from this background model guides the design and optimization of the CUPID experiment [5], which will exploit the CUORE cryogenic infrastructure to host an array of ^{100}Mo -enriched scintillating bolometers to search for $0\nu\beta\beta$ decay fully exploring the inverted hierarchy of neutrino masses. The scintillating bolometer technique enables event-by-event vetoing of α -induced events. Therefore, knowledge of the particle origin and locations of background derived from the CUORE background model is crucial to establish the background budget and sensitivity of CUPID.

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APPENDIX A: ^{40}K ON TOWER 12

We adopted a different treatment for the background contribution of ^{40}K compared to all the other Monte Carlo simulations. Examining the number of counts in the 1461-keV line of ^{40}K recorded by each tower, a significant excess is present on tower 12 (Fig. 8). To investigate this, we performed the background model fit on each tower separately and extracted the ^{40}K contribution from each. The result points to a clear surplus coming from the *crystals* of tower 12, with an activity around 5.7 times higher with respect to the average coming from the other towers: no clear deviation from a uniform trend is present for the other volumes. The cause of the higher ^{40}K activity is not certain: it is possible that a recontamination occurred during the two-years-long period in between the assembly of the tower and its installation inside the CUORE detector. Moreover, a fraction of the crystals that constitute tower 12 have been employed in validation runs of the CUORE detector [37] and subsequently repolished; the excess of ^{40}K could be the result of this operation. This procedure allows us to directly include very nonuniform activities directly inside the fit, improving the overall data reconstruction. Moreover, since ^{40}K in *crystals* induces a prominent background in the γ region and it is correlated with the $2\nu\beta\beta$, a more precise description of its distribution

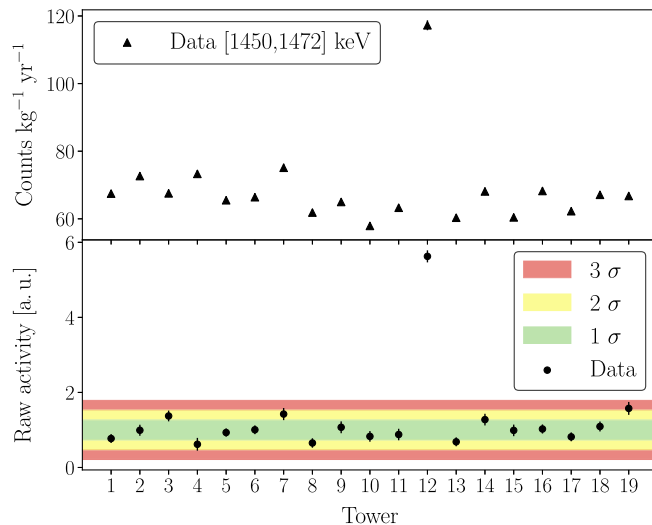


FIG. 8. Top: yield normalized by the exposure for the potassium 1461-keV line of ^{40}K for the 19 towers of CUORE. Tower 12 contains approximately double the events compared to the other towers. Bottom: normalization factor of the ^{40}K contamination in the crystals bulk when performing the fit on the towers individually. The colored bands refer to the 1, 2 and 3 standard deviations coming from the activity distribution when considering all the towers except tower 12.

can in turn lower the systematics induced on the other background components and on the determination of the ^{130}Te half-life.

APPENDIX B: CONTAMINANTS IN TeO_2

When dealing with the *crystals* volume, which is the active component of the detector, we had to meticulously assess whether to incorporate or not specific contaminants associated with TeO_2 .

Thanks to the high statistics collected with CUORE, we observe a peak in the spectrum at ~ 2316 keV, which we cannot associate with any “conventional” γ -ray emission. The most promising candidate for its origin is ^{147}Sm , whose contamination in TeO_2 shows a peak-only spectrum at the Q-value of the α transition at 2311 keV. ^{147}Sm is a naturally occurring isotope and it has been previously found as a crystal contaminant in other cryogenic experiments, where it had been possible to perform tagging of α events [38]. Since a small energy misreconstruction (excess) for α particles in bolometers has always been observed as a result of calibrating the detectors with γ -ray lines [39], we usually model this energy surplus via a QF. Also in this analysis, in the absence of a more satisfactory alternative, we thus simulate a ^{147}Sm contamination in the bulk of *crystals* and later add an *ad hoc* QF.

We conducted dedicated investigations on possible fallout products in TeO_2 , namely ^{137}Cs and ^{90}Sr , which are always produced together. ^{137}Cs has been found in traces in the copper used for CUORE; actually, this contamination alone describes the data in a satisfactory manner. ^{137}Cs exhibits a characteristic γ -ray line at 661.7 keV, which can be used to constrain its activity in TeO_2 . Including a ^{137}Cs contamination in the *crystals* volume, would give an activity < 43 nBq kg^{-1} , making its contribution and effects negligible. Therefore, we decided not to include this contaminant in the *crystals* volume. ^{90}Sr undergoes two consecutive pure β decays, first to ^{90}Y and then to ^{90}Zr , with Q-values of 546.0 and 2280.1 keV, respectively. The resulting spectrum is featureless and degenerate to that by the $2\nu\beta\beta$ decay of ^{130}Te , hence inducing a strong correlation with it. However, due to its short half-life (28.8 yr), its concentration is expected to be smaller than 10^{-20} g/g, a sensitivity that cannot be reached by any material screening technique at present. Moreover, the goodness of fit with a background model including ^{90}Sr does not improve. We therefore decided not to include it in the reference fit but, since this study is devoted to the determination of the possible experimental contamination, we studied the systematics induced by its addition to be conservative.

APPENDIX C: IDENTIFIED PEAKS

The identification of contaminants in the CUORE experiment is mainly based on the recognition of the correspondent characteristic spectral features, such as a peak search in the data. Moreover, the same procedure has been employed to define both the diagonal bands

TABLE IV. List of identified gamma peaks in the γ region of $\mathcal{M}1$ spectrum. *SE* and *DE* refer to single-escape and double-escape peaks, respectively.

E [keV]	Nuclide	E [keV]	Nuclide	E [keV]	Nuclide
238.6	^{212}Pb	768.4	^{214}Bi	1238.1	^{214}Bi
295.2	^{214}Pb	794.9	^{228}Ac	1460.8	^{40}K
338.3	^{228}Ac	803.0	^{210}Po	1588.2	^{228}Ac
351.9	^{214}Pb	834.8	^{54}Mn	1620.5	^{212}Bi
427.8	^{125}Sb	860.6	^{208}Tl	1630.6	^{228}Ac
433.9	$^{108\text{m}}\text{Ag}$	911.2	^{228}Ac	1729.6	^{214}Bi
463.0	^{228}Ac	934.1	^{214}Bi	1764.5	^{214}Bi
511.0	e^+e^-	964.0	^{228}Ac	1847.4	^{214}Bi
583.2	^{208}Tl	969.0	^{228}Ac	2103.5	$^{208}\text{Tl}_{\text{SE}}$
609.3	^{214}Bi	1001.0	$^{234\text{m}}\text{Pa}$	2118.5	^{214}Bi
614.3	$^{108\text{m}}\text{Ag}$	1063.6	^{207}Bi	2204.1	^{214}Bi
657.7	$^{110\text{m}}\text{Ag}$	1120.3	^{214}Bi	2316.5	^{147}Sm
665.4	^{214}Bi	1173.2	^{60}Co	2447.9	^{214}Bi
722.9	$^{108\text{m}}\text{Ag}$	1238.1	^{214}Bi	2505.6	^{60}Co
727.3	^{212}Bi	1332.5	^{60}Co	2614.5	^{208}Tl

TABLE V. List of identified gamma peaks for the $\mathcal{M}2$ gamma bands.

E [keV]	Nuclide	E [keV]	Nuclide
328.0	^{228}Ac	821.5	$^{60}\text{Co}_{\text{SE}}$
351.9	^{214}Pb	835.7	^{228}Ac
409.5	^{228}Ac	911.2	^{228}Ac
427.9	^{125}Sb	950.0	$^{40}\text{K}_{\text{SE}}$
434.2	$^{108\text{m}}\text{Ag}$	969.0	^{228}Ac
511.0	e^+e^-	1120.3	^{214}Bi
583.2	^{208}Tl	1173.2	^{60}Co
609.3	^{214}Bi	1332.5	^{60}Co
722.9	$^{110\text{m}}\text{Ag}$	1592.5	$^{208}\text{Tl}_{\text{DE}}$
768.4	^{214}Bi	1764.5	^{214}Bi
794.9	^{228}Ac	2103.5	$^{208}\text{Tl}_{\text{SE}}$

used to generate the spectra for the data reconstruction, and the binning for energy histograms. Therefore, we identified all the peaks in the γ region for both $\mathcal{M}1$ and $\mathcal{M}2$ energy spectra as well as the α peaks in the $\mathcal{M}2$ total-energy data and report the results in Tables IV–VII.

TABLE VI. List of γ emitters used to define the $\mathcal{M}2$ total-energy bands in the γ region.

E [keV]	Nuclide	E [keV]	Nuclide
511.0	e^+e^-	1460.5	^{40}K
583.2–609.3	^{208}Tl - ^{214}Bi	1509.2	^{214}Bi
722.9–727.3	$^{108\text{m}}\text{Ag}$ - ^{212}Bi	1588.2	^{228}Ac
834.8	^{54}Mn	1620.5–1630.6	^{212}Bi - ^{228}Ac
911.2	^{228}Ac	1661.3	^{214}Bi
969.0	^{228}Ac	1729.6	^{214}Bi
1063.7	^{207}Bi	1764.5	^{214}Bi
1120.3	^{214}Bi	1847.4	^{214}Bi
1173.2	^{60}Co	2103.5–2118.6	$^{208}\text{Tl}_{\text{SE}}$ - ^{214}Bi
1238.1	^{214}Bi	2204.1	^{214}Bi
1332.5	^{60}Co	2447.9–2505.6	^{214}Bi - ^{60}Co
1377.7–1408.0	^{214}Bi	2614.5	^{208}Tl

TABLE VII. List of α emitters used to define the $\mathcal{M}2$ total-energy bands in the α region.

Q-value [keV]	Nuclide	Q-value [keV]	Nuclide
4081.6	^{232}Th	5520.1	^{228}Th
4269.7	^{238}U	5590.3	^{222}Rn
4770.0	^{230}Th	5788.9	^{224}Ra
4857.7–4870.6	^{234}U - ^{226}Ra	6114.7	^{218}Po
5407.5	^{210}Po	6207.4	^{212}Bi

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