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Measurement of $|V_{cb}|$ and the Form-Factor Slope in $\overline{B} \to D\ell^- \overline{\nu}_\ell$ Decays in Events Tagged by a Fully Reconstructed *B* Meson

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We present a measurement of the Cabibbo-Kobayashi-Maskawa matrix element $|V_{cb}|$ and the formfactor slope ρ^2 in $\bar{B} \to D\ell^- \bar{\nu}_\ell$ decays based on $460 \times 10^6 B\bar{B}$ events recorded at the Y(4S) resonance with the BABAR detector. $\bar{B} \to D\ell^- \bar{\nu}_\ell$ decays are selected in events in which a hadronic decay of the second B meson is fully reconstructed. We measure $\mathcal{B}(B^- \to D^0\ell^- \bar{\nu}_\ell)/\mathcal{B}(B^- \to X\ell^- \bar{\nu}_\ell) = (0.255 \pm 0.009 \pm 0.009)$ and $\mathcal{B}(\bar{B}^0 \to D^+\ell^- \bar{\nu}_\ell)/\mathcal{B}(\bar{B}^0 \to X\ell^- \bar{\nu}_\ell) = (0.230 \pm 0.011 \pm 0.011)$, along with the differential decay distribution in $\bar{B} \to D\ell^- \bar{\nu}_\ell$ decays. We then determine $\mathcal{G}(1)|V_{cb}| = (42.3 \pm 1.9 \pm 1.4) \times 10^{-3}$ and $\rho^2 = 1.20 \pm 0.09 \pm 0.04$, where $\mathcal{G}(1)$ is the hadronic form factor at the point of zero recoil.

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In the standard model (SM) of electroweak interactions, the rate of the semileptonic $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ decay is proportional to the square of the Cabibbo-Kobayashi-Maskawa (CKM) [1] matrix element $|V_{cb}|$, which is a measure of the weak coupling of the *b* to the *c* quark. The length of the side of the unitarity triangle opposite to the well-measured angle β is proportional to $|V_{ub}/V_{cb}|$, making the determination of $|V_{cb}|$ an important test of the SM description of *CP* violation. In addition, imprecise knowledge of $|V_{cb}|$ is a significant uncertainty limiting comparison of *CP* violation measurements in *K*-meson decays with those in *B*-meson decays [2].

 $|V_{\rm cb}|$ has been extracted from inclusive semileptonic B decays [3] and exclusive decays $\bar{B} \to D\ell^- \bar{\nu}_{\ell}$ and $\bar{B} \to$ $D^*\ell^-\bar{\nu}_\ell$ [4]. The results rely on different QCD calculations. For inclusive decays, the decay rate is predicted by an expansion in inverse powers of the *b*-quark mass and in terms of the strong coupling constant α_s , while exclusive decays are expressed in terms of form factors with a normalization taken from Heavy Ouark Symmetry and nonperturbative QCD calculations. The theoretical uncertainties of these two approaches are independent, and the measurements have, to a large extent, uncorrelated statistical and systematic uncertainties. This makes the comparison of $|V_{cb}|$ from inclusive and exclusive decays a powerful test of our understanding of semileptonic decays. The most recent results differ by more than 2 standard deviations, with the error on the exclusive measurements larger by a factor >2 [5]. The $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ decay is to a large extent complementary to the $\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$, which depends on three form factors and therefore requires a full angular analysis. Improvements in the measurements of the exclusive decay rates are highly desirable, in particular, for $\bar{B} \rightarrow$ $D\ell^-\bar{\nu}_\ell$ decays where, at present, the experimental uncertainties dominate. Studies of $\bar{B} \rightarrow D\ell^- \bar{\nu}_{\ell}$ decays have previously been reported by the Belle [6], CLEO [7], ALEPH [8], and BABAR [4] Collaborations.

The $\bar{B} \rightarrow D\ell^- \bar{\nu}_{\ell}$ differential decay rate $d\Gamma_D/dw$ [9] depends on the hadronic matrix element describing strong-interaction effects in $\bar{B} \rightarrow D$ transitions. In the limit of very small lepton masses ($\ell = e$ or μ), their effect can be parametrized by a single form factor G(w):

$$\frac{d\Gamma_D}{dw} = \frac{G_F^2 |V_{\rm cb}|^2}{48\pi^3 \hbar} M_D^3 (M_B + M_D)^2 (w^2 - 1)^{3/2} \mathcal{G}^2(w), \quad (1)$$

where G_F is the Fermi coupling constant, and M_B and M_D are the masses of the *B* and *D* mesons, respectively. The variable *w* denotes the product of the *B* and *D* meson 4-velocities V_B and V_D , $w = V_B \cdot V_D = (M_B^2 + M_D^2 - q^2)/(2M_BM_D)$, where $q^2 \equiv (p_B - p_D)^2$, and p_B and p_D are the 4-momenta of the *B* and *D* mesons.

In the limit of infinite heavy quark masses, G(w) coincides with the Isgur-Wise function [10]. This function is normalized to unity at zero recoil, where q^2 is maximum. Corrections to the heavy quark limit have been calculated based on unquenched [11] and quenched lattice QCD [12]. Thus $|V_{cb}|$ can be extracted by extrapolating the differential decay rate to w = 1. To reduce the uncertainties associated with this extrapolation, constraints on the shape of the form factor are necessary. Several functional forms have been proposed [13]. We adopt the parametrization suggested in Ref. [14], where the nonlinear dependence of the form factor on w is expressed in terms of a single shape parameter, the form-factor slope ρ^2 . In Ref. [12] the form factor G(w) has been computed at a few points above the zero recoil limit, up to w = 1.2. This allows us to extract $|V_{\rm cb}|$ in a region where the rate is much larger, avoiding the large extrapolation to w = 1.

In this Letter, we present a measurement of $d\Gamma_D/dw$ for $\bar{B}^0 \to D^+ \ell^- \bar{\nu}_\ell$ and $B^- \to D^0 \ell^- \bar{\nu}_\ell$ decays from which we extract $G(w)|V_{cb}|$ at w = 1.0 and at few points with w >1.0. The analysis is based on data collected with the BABAR detector [15] at the PEP-II asymmetric-energy e^+e^- storage rings. The data consist of 417 fb⁻¹ recorded at the Y(4S) resonance, corresponding to approximately $460 \times 10^6 B\bar{B}$ pairs. An additional sample of 40 fb⁻¹, collected at a center-of-mass (c.m.) energy 40 MeV below the Y(4S) resonance, is used to study background from $e^+e^- \rightarrow ff(f = u, d, s, c, \tau)$ continuum events. We also use samples of GEANT4 Monte Carlo (MC) simulated events that correspond to about three times the data sample size. The simulation models $\bar{B} \rightarrow D^{(*)} \ell^- \bar{\nu}_{\ell}$ decays using calculations based on heavy quark effective theory (HQET) [14], $\bar{B} \rightarrow D^{**} (\rightarrow D^{(*)} \pi) \ell^- \bar{\nu}_{\ell}$ decays using the ISGW2 model [16], and nonresonant $\bar{B} \rightarrow D^{(*)} \pi \ell^- \bar{\nu}_{\ell}$ decays using the Goity-Roberts model [17]. The MC simulation includes radiative effects such as bremsstrahlung in the detector material and final-state radiation modeled by PHOTOS [18].

Semileptonic decays are selected in $B\bar{B}$ events in which a hadronic decay of the second *B* meson (B_{tag}) is fully reconstructed, following the same criteria used in Ref. [19] and briefly summarized here. We first reconstruct the semileptonic decay selecting a lepton with momentum in the c.m. frame $p_{\ell}^* > 0.6$ GeV and a well-reconstructed D^0/D^+ candidate with the correct charge correlation with the lepton. Then we reconstruct the B_{tag} decays in about 1000 different charmed hadronic modes $\bar{B} \rightarrow D^{(*)}Y$ where *Y* represents a combination of π^{\pm} , π^0 , K^{\pm} , or K_S^0 [20]. The kinematic consistency of a B_{tag} candidate with a *B* meson decay is evaluated requiring $5.27 < m_{\rm ES} \equiv \sqrt{s/4 - (p_B^*)^2} <$ 5.29 GeV, where \sqrt{s} is the total c.m. energy, and p_B^* and E_B^* denote the momentum and energy of the B_{tag} candidate in the c.m. frame.

Semileptonic *B* decays are identified by their missing mass squared, $m_{\text{miss}}^2 = [p_{Y(4S)} - p_{B_{\text{tag}}} - p_D - p_\ell]^2$, calculated from the measured particles 4-momenta. For correctly reconstructed signal events, the only missing particle is the neutrino and m_{miss}^2 peaks at zero. Other semileptonic *B* decays, like $\bar{B} \rightarrow D^{(*,**)} \ell^- \bar{\nu}_\ell$, where at least one particle is not reconstructed (feed-down), yield larger values of m_{miss}^2 .

We measure $G(1)|V_{cb}|$ and the form-factor slope ρ^2 by a fit to the *w* distribution. We examine the data and MC events in ten equal-size *w* bins in the interval 1 < w < 1.6. Since the *B* momentum is known from the fully reconstructed B_{tag} in the same event, *w* is reconstructed with good precision, namely, to ~0.01, which corresponds to about 2% of the full kinematic range.

The $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ signal yield in each bin of w is obtained from the m_{miss}^2 distribution in data by an extended binned maximum likelihood fit [21]. We assume that the data sample is described by contributions from four different sources: $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ signal events, feed-down from other semileptonic B decays, combinatorial $B\bar{B}$ and continuum background, and fake lepton events (mostly from hadronic *B* decays with hadrons misidentified as leptons). The probability density functions (PDFs) are derived from the MC predictions for the different semileptonic *B* decay $m_{\rm miss}^2$ distributions. We use the off-peak data to provide the continuum background normalization. The shape of the continuum background distribution predicted by the MC simulation is consistent with that obtained from the offpeak data. The measured $m_{\rm miss}^2$ distributions are compared with the results of the fits for two different w intervals in Fig. 1.

We perform a least-squares fit to the observed signal yields in the ten bins of w. We minimize a χ^2 defined as

$$\chi^{2} = \sum_{i=1}^{10} \frac{(N_{\text{data}}^{i} - \sum_{j=1}^{N_{\text{MC}}^{i}} W_{j}^{i})^{2}}{(\sigma_{\text{data}}^{i})^{2} + \sum_{j=1}^{N_{\text{MC}}^{i}} W_{j}^{i2}},$$
(2)

where the index *i* refers to the *w* bin and the index *j* runs



FIG. 1 (color online). Fit to the m_{miss}^2 distribution in two different *w* intervals for $B^- \rightarrow D^0 \ell^- \bar{\nu}_{\ell}$: the data (points with error bars) are compared to the results of the overall fit (sum of the solid histograms). The PDFs for the different fit components are stacked in the order shown in the legend.

over all MC events in bin *i*; N_{data}^i is the observed number of signal events found in the *i*th bin and σ_{data}^i the corresponding uncertainty. The expected signal yields are calculated at each step of the minimization from the reweighted sum of N_{MC}^i simulated events. Each weight is the product of two terms: $W_j^i = W^{\mathcal{L}} \times W_j^{i,\text{theo}}$, where $W^{\mathcal{L}}$ is an overall fixed scale factor, which accounts for the relative integrated luminosity of the data and signal MC events, and $W_j^{i,\text{theo}}$ is computed using the true *w* value of the event *j* and depends on $\mathcal{G}(1)|V_{cb}|$ and ρ^2 , which are free parameters determined in the fit that are recalculated at each step of the minimization.

We first fit the *w* distributions for the charged and neutral $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ samples separately and then perform a fit to the combined $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ sample. In Fig. 2, we show the comparison between the data and the fit results for the combined sample. The measured values of $\mathcal{G}(1)|V_{cb}|$ and ρ^2 , with the corresponding correlation ρ_{corr} obtained from the fit, are reported in Table I. The branching fraction is derived by integrating Eq. (1) and dividing by the appropriate *B*-meson lifetime.

In order to reduce the systematic uncertainty on the measurement of $G(1)|V_{cb}|$ and the branching fractions, we normalize the exclusive signal yield to the yield of inclusive semileptonic decays, $\bar{B} \rightarrow X \ell^- \bar{\nu}_\ell$, in events tagged by a fully reconstructed hadronic *B* decay. The inclusive $\bar{B} \rightarrow X \ell^- \bar{\nu}_\ell$ decays are selected by identifying one charged lepton with $p_\ell^* > 0.6$ GeV and the charge expected based on the B_{tag} decay. In the case of multiple



FIG. 2 (color online). (a) Signal yield *w* distribution obtained summing $B^- \to D^0 \ell^- \bar{\nu}_\ell$ and $\bar{B}^0 \to D^+ \ell^- \bar{\nu}_\ell$ events. The data (•) are compared to the results of the overall fit (histogram). (b) $\mathcal{G}(w)|V_{cb}|$ distribution corrected for the reconstruction efficiency, with the fit result superimposed.

 B_{tag} candidates in an event, we select the decay mode with the highest purity, estimated from the MC prediction for the fraction of true decays in the m_{ES} signal region. Background components that peak in the m_{ES} signal region include cascade *B* meson decays, for which the lepton does not come directly from the *B*, and hadronic decays; they are subtracted using the corresponding MC predictions. The $\bar{B} \rightarrow X \ell^- \bar{\nu}_\ell$ yield is obtained from a maximum likelihood fit to the m_{ES} distribution of the B_{tag} candidates, as described in Ref. [19]. The fit yields $(198.9 \pm 1.6) \times 10^3$ events for the $\bar{B}^0 \rightarrow X \ell^- \bar{\nu}_\ell$ sample and $(116.3 \pm 1.0) \times$ 10^3 events for the $\bar{B}^0 \rightarrow X \ell^- \bar{\nu}_\ell$ sample. The corresponding reconstruction efficiencies, including the B_{tag} reconstruction, are 0.39% and 0.25%, respectively. We investigated numerous sources of systematic uncertainties, whose contributions are listed in Ref. [22]. The largest uncertainties are due to differences in the efficiency of the B_{tag} selection between the exclusive $\bar{B} \to D\ell^- \bar{\nu}_\ell$ and inclusive $\bar{B} \to$ $X\ell^-\bar{\nu}_\ell$ decays (a relative 1.5% systematic uncertainty on $|V_{\rm cb}|$), the $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ fit procedure (1.3%), and the uncertainties on the branching fractions of the reconstructed D decay modes and $\bar{B} \to D^{**} \ell^- \bar{\nu}_{\ell}$ decays (1.1%). The uncertainties due to the detector simulation are established by varying, within bounds given by data control samples, the tracking efficiency of all charged tracks (0.7%), the calorimeter efficiency (0.9%), and the lepton identification efficiency (0.9%). We evaluate the systematic uncertainties associated with the MC simulation of various signal and background processes: photon conversion and π^0 Dalitz decay, B cascade decay contamination (0.8%), and flavor cross feed (0.2%). The uncertainty arising from radiative corrections (0.1%) is studied by comparing the standard results with those obtained when PHOTOS is not used. We take 30% of the difference as a conservative systematic uncertainty. We vary the $\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$ form factors (0.4%) within their measured uncertainties [4] and use a HQET parametrization [23] to describe $\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_{\ell}$ decays (0.3%). We evaluate an uncertainty associated with the $\bar{B} \rightarrow X \ell^- \bar{\nu}_{\ell}$ fitting procedure (0.8%) and with the absolute branching fraction $\mathcal{B}(\bar{B} \to X \ell^- \bar{\nu}_\ell)$ used for the normalization (0.8%).

From the fit to the combined $\bar{B} \rightarrow D\ell^- \bar{\nu}_\ell$ sample, we measure $G(1)|V_{cb}| = (42.3 \pm 1.9 \pm 1.4) \times 10^{-3}$. Using an unquenched lattice calculation [11], corrected by a factor of 1.007 for QED effects, we obtain $|V_{cb}| = (39.2 \pm 1.8 \pm 1.3 \pm 0.9_{\rm FF}) \times 10^{-3}$, where the third error is due to the theoretical uncertainty in G(1). As an alternative, we use a quenched lattice calculation based on the step scaling method (SSM) [12] and obtain $|V_{cb}| = (40.9 \pm 1.8 \pm 1.4 \pm 0.7_{\rm FF}) \times 10^{-3}$. The authors of [12] report the lattice determination of G(w) for finite momentum transfer. Although quenched, this calculation allows the extraction of $|V_{cb}|$ avoiding the large extrapolation to w = 1. For example, from a linear interpolation around w = 1.2, we obtain $|V_{cb}| = (40.7 \pm 1.3 \pm 1.4 \pm 1.0_{\rm FF}) \times 10^{-3}$. We re-

TABLE I. Fit results for each sample. The last column reports the result of the \bar{B}^0/B^- combined fit (here \mathcal{B} refers to \bar{B}^0 decays). We also report signal yields and reconstruction efficiencies integrated over the full *w* range. Absolute branching fractions (last row) are derived from relative branching fractions using $\mathcal{B}(B \to X \ell^- \bar{\nu}_\ell)$ from Ref. [5].

	$B^- \rightarrow D^0 \ell^- \bar{\nu}_\ell$	$\bar{B}^0 \longrightarrow D^+ \ell^- \bar{\nu}_\ell$	$\bar{B} \rightarrow D \ell^- \bar{\nu}_\ell$
$G(1) V_{\rm cb} \cdot 10^3$	$41.0 \pm 2.1 \pm 1.3$ $1.14 \pm 0.11 \pm 0.04$	$44.9 \pm 3.2 \pm 1.6$ 1 29 ± 0.14 ± 0.05	$42.3 \pm 1.9 \pm 1.4$ 1 20 ± 0.09 ± 0.04
$ ho_{ m corr} \ \chi^2/{ m ndf}$	0.943 3.4/8	0.950 5.6/8	0.952 9.9/18
Signal Yield Reconstruction Efficiency $\mathcal{B}(B \rightarrow D\ell^- \bar{u}_c)/\mathcal{B}(B \rightarrow X\ell^- \bar{u}_c)$	2147 ± 69 (1.99 ± 0.02) × 10 ⁻⁴ (0.255 ± 0.009 ± 0.009)	1108 ± 45 (1.09 ± 0.02) × 10 ⁻⁴ (0.230 ± 0.011 ± 0.011)	$(0.223 \pm 0.006 \pm 0.009)$
$\mathcal{B}(B \to D\ell^- \bar{\nu}_\ell) / \mathcal{B}(B \to X\ell^- \bar{\nu}_\ell)$	$(0.255 \pm 0.009 \pm 0.009)\%$ $(2.29 \pm 0.08 \pm 0.09)\%$	$(0.250 \pm 0.011 \pm 0.011)$ $(2.21 \pm 0.11 \pm 0.11)\%$	$(0.225 \pm 0.006 \pm 0.009)$ $(2.15 \pm 0.06 \pm 0.09)\%$

port our measurements of $\mathcal{G}(w)|V_{cb}|$ for w > 1 in Ref. [22]. The $|V_{cb}|$ measurement at w > 1 is affected by smaller uncertainties than the one extracted at w = 1.

The results presented here can be combined with a recent *BABAR* measurement [4]. We neglect the tiny statistical correlations among the two measurements and treat the systematic uncertainties as fully correlated. We obtain $G(1)|V_{cb}| = (42.4 \pm 1.7) \times 10^{-3}$ and $\rho^2 = 1.18 \pm 0.06$, with a correlation coefficient of 0.89. We also obtain the branching fraction $\mathcal{B}(\bar{B}^0 \rightarrow D^+ \ell^- \bar{\nu}_\ell) = (2.15 \pm 0.08)\%$. The combined *BABAR* result (using the unquenched lattice calculation [11]) is $|V_{cb}| = (39.2 \pm 1.6 \pm 0.9_{FF}) \times 10^{-3}$, which is consistent with the measurement obtained from $\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$, $|V_{cb}| = (38.6 \pm 0.9_{exp} \pm 1.0_{FF}) \times 10^{-3}$, decays, and also compatible with the inclusive determination of $|V_{cb}| = (41.6 \pm 0.6) \times 10^{-3}$ [5].

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