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Peer reviewed

Uniform Diffusion of Cooper Pairing Mediated by Hole Carriers in Topological $\text{Sb}_2\text{Te}_3/\text{Nb}$

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ABSTRACT

Spin-helical Dirac fermions at a doped topological insulator's boundaries can support Majorana quasiparticles when coupled with *s*-wave superconductors, but in *n*-doped systems, the requisite induced Cooper pairing in topological states is often buried at heterointerfaces or complicated by degenerate coupling with bulk conduction carriers. Rarely probed are *p*-doped topological structures with nondegenerate Dirac and bulk valence bands at the Fermi level, which may foster long-range superconductivity without sacrificing Majorana physics. Using ultrahigh-resolution photoemission, we report proximity pairing with a large decay length in *p*-doped topological Sb₂Te₃ on superconducting Nb. Despite no momentum-space degeneracy, topological and bulk states of Sb₂Te₃/Nb exhibit the same isotropic superconducting gaps at low temperatures. Our results unify principles for realizing accessible pairing in Dirac fermions relevant to topological superconductivity.

KEYWORDS: Proximity effects, topological superconductivity, *p*-doped topological insulators, interband superconducting coherence, flip-chip method, thin-film heterostructures

Majorana zero modes in topological superconductors have enamored fundamental condensed-matter physics in recent years,¹⁻⁵ as their non-Abelian exchange statistics is conducive for building fault-tolerant qubits.^{3,4} Nevertheless, an intrinsic topological superconductor with bulk spin-triplet superconductivity or an effective *p*-wave pairing state is quite rare,⁴⁻⁹ especially since many candidates require delicate elemental alloying or are themselves highly contentious.⁶⁻⁹ A more common contender for hosting Majorana bound states is a topological insulator coupled with an *s*-wave superconductor,^{4,5,10-15} wherein an isotropic proximity-induced superconducting gap arises in the spin-helical Dirac fermions.⁸⁻¹⁵ Such

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3 pairing can subsist at both boundaries of the topological insulator if Cooper pairs have sufficient
4 phase coherence over large distances,^{14–18} but mechanisms for mediating this robust
5 superconductivity in the nontrivial boundary states remain fiercely debated.^{14–21}
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10 Fortunately, for heavily *n*-doped topological insulators on niobium with conduction band
11 (CB) carriers, quantum-mechanical coupling between bulk and surface states rather simply
12 fosters long-range proximity pairing.^{15–18} Yet even this scenario does not necessarily apply to
13 heavily *p*-doped topological insulators (Figure 1A,B). In *n*+ doped Bi₂Se₃, the Fermi level
14 crosses the topological surface states (TSS) and CB, which nearly overlap in momentum space
15 (Figure 1A).^{15,22} Consequently, a large proximity-induced gap emerges in the TSS of
16 Bi₂Se₃/Nb.^{15–17} For bulk insulating *n* doped (Bi_{1–*x*}Sb_{*x*})₂Te₃ with *x* = 0.62, the Fermi level lies in
17 the bulk band gap, crossing the TSS above the Dirac point (Figure 1A).^{18,23} No clear proximity
18 pairing is observed here for (Bi_{1–*x*}Sb_{*x*})₂Te₃/Nb, suggesting bulk CB are important for transiting
19 pairing into the TSS.^{15–18} Further increasing the alloy ratio *x* to *x* = 1 induces a Lifshitz transition
20 to *p*+ doped Sb₂Te₃ (Figure 1A) with the Fermi level pinned to bulk valence bands (VB).^{23–26} At
21 this stage, the Fermi surface (Figure 1B) exhibits well-separated hole pockets due to the TSS and
22 VB.^{24,25} Thus, unlike Bi₂Se₃, Sb₂Te₃ is a clean topological material with bulk and surface states
23 well separated in *k* space. This *k*-space separation can impact proximity pairing mediated by the
24 bulk states,^{15,18} but such intrinsic issues and proximity pairing overall in *p*-doped systems are
25 rarely examined.^{11–21}
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47 Here, by conducting ultrahigh-resolution photoemission of heavily *p*-doped topological
48 Sb₂Te₃ films on superconducting Nb, we find an isotropic superconducting gap opening within
49 experimental error at low temperatures. Like bulk insulating (Bi_{1–*x*}Sb_{*x*})₂Te₃/Nb, topological
50 Sb₂Te₃/Nb is a simple system for stringently tuning quantum-mechanical interactions relevant to
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3 proximity effects:^{15–18} The electronic structure of Sb_2Te_3 near the Fermi level has bulk and
4 surface states at very different momenta (Figure 1B),^{24–26} and bulk Nb has the highest transition
5 temperature of all elemental *s*-wave superconductors ($T_{\text{C,Nb}} = 9.26 \text{ K}$).^{27–30} By fabricating
6 $\text{Sb}_2\text{Te}_3/\text{Nb}$ using our very own cleavage-based “flip-chip” method,^{15,18} we create a topological
7 material on Nb where hole-like Dirac and bulk VB bands do not overlap in momentum space at
8 the Fermi level. Despite this separation, proximity-induced superconductivity quantified as a
9 function of Sb_2Te_3 thickness reveals appreciable superconducting gaps of identical magnitude in
10 the TSS and VB, implying that Cooper pairing is transferred from bulk VB to TSS through
11 internal proximity effects mediated by interband superconducting coherence.^{6–9} This discovery
12 of *s*-wave superconductivity on $\text{Sb}_2\text{Te}_3/\text{Nb}$ surfaces clarifies routes towards accessible pairing in
13 the TSS, which could herald emergent physics, including topological superconductivity, in
14 nanoscale devices.

33 RESULTS AND DISCUSSION

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35 **Confirming *p*-Type Doping and Fabricating $\text{Sb}_2\text{Te}_3/\text{Nb}$.** High-quality, heavily *p*-doped
36 Sb_2Te_3 films with thicknesses $N = 3–7$ quintuple layers (QL) (1 QL $\approx 1 \text{ nm}$) are grown using
37 molecular beam epitaxy (MBE) onto bilayer-graphene-terminated SiC, as verified by *in situ*
38 angle-resolved photoemission spectroscopy (ARPES) (Figures S1 and S2). Specifically, ARPES
39 and second-derivative spectra along $\overline{\Gamma\text{M}}$ of as-grown 7 QL Sb_2Te_3 exhibit only the lower half of
40 the topological Dirac cone and bulk VB located away from the zone center (Figure 1C).^{23–26}
41 Moreover, no bulk VB overlap with the TSS in momentum space at the Fermi level, even in
42 bulk-like 7 QL Sb_2Te_3 (Figures 1C and S2). Corresponding Fermi surface maps of Sb_2Te_3 films
43 also reveal typical band topologies for *p*-doped topological insulators:^{24,25} A round contour
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3 centered at the $\bar{\Gamma}$ point due to the TSS and an elongated spoke along each $\bar{\Gamma M}$ from hole-like VB
4 (Figure 1B,D). Evidently, all Sb_2Te_3 films are *p*-doped with bulk and surface bands crossing the
5 Fermi level at very different momenta—quite unlike the nearly degenerate bulk CB and TSS of
6 *n*+ doped Bi_2Se_3 in Figure 1A.^{14,15,22}
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12 All $\text{Sb}_2\text{Te}_3/\text{Nb}$ films are fabricated using a “flip-chip” technique we invented for
13 assembling van der Waals materials onto arbitrary superconductors,¹⁵ which sidesteps mixed
14 interfacial structures and Nb diffusion encountered when growing topological films on Nb.^{19,31}
15 After MBE growths of Sb_2Te_3 films on bilayer-graphene-terminated SiC, a 60-nm-thick bulk Nb
16 film is deposited atop using magnetron sputtering at 25 °C (Figure 1E, step 1). Each sample is
17 then flipped over, attached to a polished Cu plate by an electrically conductive epoxy, and finally
18 capped with a cleavage pin (Figure 1E, steps 2 and 3). Just prior to photoemission, each thin-film
19 structure is cleaved *in situ* by pushing against the cleavage pin (Figure 1E, step 4) to separate the
20 substrate held in place by weak incommensurate van der Waals bonding, yielding Sb_2Te_3 films
21 with thicknesses set by MBE on superconducting Nb.^{15,18} Large, mirrorlike $\text{Sb}_2\text{Te}_3/\text{Nb}$ surfaces
22 perfect for ARPES are easily obtainable with this flip-chip method (Figures S3 and S4).
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40 **Pairing in Bulk and Topological Bands of Flip-Chip $\text{Sb}_2\text{Te}_3/\text{Nb}$.** Ultrahigh-resolution
41 photoemission measurements are undertaken with *p*-polarized 5.821-eV and/or 6.994-eV
42 photons at temperatures $T = 1.5\text{--}10$ K. Typical constant energy contours near the Fermi level at
43 $T < 2$ K for $\text{Sb}_2\text{Te}_3/\text{Nb}$ are presented in Figure 2A–C. A representative dataset for proximity
44 pairing in $\text{Sb}_2\text{Te}_3/\text{Nb}$ —one with constant energy contours, temperature-dependent band maps of
45 the TSS and VB close to the Fermi level, and energy distribution curves (EDCs) at strategically
46 chosen Fermi surface momenta—is summarized for the 4 QL case in Figure 2C–E. Like the
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3 Fermi surface map of its as-grown counterpart (Figure 1D), constant energy contour maps at
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5 6.994-eV and 5.821-eV photon energies for 7 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ each possess a zone-centered,
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7
8 hooplike contour and an intensity arm along $\overline{\Gamma\text{M}}$ due to the hole-like TSS and VB, respectively
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10 (Figure 2A).^{24,25} Similar statements are duly noted for the constant energy contour maps of 3 QL
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12 and 4 QL flip chips (Figure 2B,C), though the density of bulk-like VB near the Fermi level in the
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14 3 QL case is reduced due to quantum-size effects (Figure S2).^{22,32,33} Incidentally, all these
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16 constant energy contours flaunt complex variations in photoemission intensity as a function of
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18 photon energy and/or in-plane momenta (Figure 2A–C), attributable to matrix element effects
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20 tied to the surface's orientation relative to the incident photon beam's electric field.³²
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24 Quintessential features of proximity pairing at temperatures below the superconducting
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26 transition temperature of bulk Nb arise in temperature-dependent band maps of 4 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$
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28 (Figure 2D). Namely, band mappings of TSS and VB features exhibit thermally broadened
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30 Fermi-level cutoffs at $T = 10$ K, but as the temperature is reduced to $T = 1.8$ K, superconducting
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32 coherence peaks and associated leading-edge shifts emerge at all in-plane momenta (Figure 2D),
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34 indicative of induced superconducting order in both the TSS and VB. The development of a
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36 coherence peak at momenta other than the Fermi momenta is due to quasiparticle interference
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38 augmented by superconducting phase coherence.^{6–9} Despite their differences in Fermi
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40 momentum along $\overline{\Gamma\text{M}}$ (k_y -direction) (Figure 2C), all EDC datasets in Figure 2E show virtually
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42 identical temperature-dependent leading-edge shifts and thus proximity-induced gaps, which we
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44 quantify by modelling superconducting EDCs with Gaussian-broadened Dynes functions having
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46 Fermi-level cutoffs and BCS mean-field dependencies for the superconducting gaps (Figure 2E,
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48 blue curves). That is, the superconducting Dynes density of states (DOS) at binding energy E_B
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with pair-breaking parameter Γ and superconducting gap $\Delta = \Delta(T)$ is

$$N_S(E_B, \Gamma, \Delta) = \text{Re} \left(\frac{|E_B + i\Gamma|}{\sqrt{(E_B + i\Gamma)^2 - \Delta^2}} \right), \quad (1)$$

where $\Delta = \Delta(0) \tanh(1.74 \sqrt{T_C/T - 1})$.^{7,15,34} Here, the zero-temperature gap $\Delta(0)$ is a universal fitting parameter in the analysis of each temperature-dependent EDC dataset (Figures 2E, 3, and 4), while T_C is the transition temperature of flip-chip $\text{Sb}_2\text{Te}_3/\text{Nb}$, which is within experimental error equivalent to that of bulk Nb as determined from transport of 60-nm-thick Nb film (Figure S5).²⁷⁻³⁰ The agreement between raw EDCs and their corresponding fits is excellent for 4 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ and overall suggests that the TSS and VB have similar superconducting gaps, evocative of an isotropic gap in the 4 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ Fermi surface (Figure 2C–E). However, these conclusions apply equally well to other N QL $\text{Sb}_2\text{Te}_3/\text{Nb}$, as shown by their fitted topological and bulk EDCs in Figure 3. Meanwhile, as the thickness of N QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ increases from $N = 0$ to 7, superconductivity at the surface exhibits a characteristic decay with obvious superconducting features no longer visible in 7 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ (Figure 3), all reflective of the expected phase decoherence of Cooper pairs with increasing distance away from the superconducting heterointerface.^{14-21,35}

Momentum-Resolved Zero-Temperature Gaps in $\text{Sb}_2\text{Te}_3/\text{Nb}$. To more explicitly highlight the isotropic nature of the proximity gap, Figure 4A plots all deduced zero-temperature gaps $\Delta(0)$ versus Sb_2Te_3 film thickness, while Figure 4B displays these same thickness-dependent $\Delta(0)$ but now resolved as a function of in-plane momenta along $\overline{\Gamma\text{K}}$ (k_x -direction) and $\overline{\Gamma\text{M}}$ (k_y -direction) of $\text{Sb}_2\text{Te}_3/\text{Nb}$. Clearly, for a given Sb_2Te_3 thickness, the induced gap is the same across the Fermi surface, indicative of an isotropic s -wave gap (Figure 4A,B). In line with

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3 thickness-dependent EDCs in Figure 3, $\Delta(0)$ decreases with increasing Sb_2Te_3 film thickness so
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5 that at a 7 QL thickness, only a small superconducting gap is inferred (Figure 4A). Furthermore,
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7 the decay length λ of Cooper pairs penetrating into an Sb_2Te_3 film of thickness z may be
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9 estimated by fitting the thickness dependence of $\Delta(0)$ with an exponential function (Figure 4A,
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11 blue curve) given by

$$12 \quad \Delta(0) = \Delta_0 \exp\left(-\frac{z}{\lambda}\right), \quad (2)$$

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15 where $\Delta_0 = 1.591$ meV is the zero-temperature superconducting gap of Nb found from
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17 simultaneous fitting of pure Nb data (Figure 3, top panel). The extracted decay length is λ
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19 $= 4.668 \pm 0.003$ QL. Also, by suggestion of the thickness-dependent behavior of $\Delta(0)$, a linear
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21 fit (Figure 4A, red curve) gives a lower bound estimate for $\Delta(0)$ in the 7 QL system, which is
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23 comparable to the analyzer's maximum energy resolution (~ 0.1 meV).^{15,36–38} Overall, our results
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25 demonstrate the opening of an isotropic *s*-wave gap in all $\text{Sb}_2\text{Te}_3/\text{Nb}$ Fermi surfaces and
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27 therefore that the TSS and VB—located at different momenta at the Fermi level—possess
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29 comparable zero-temperature gaps (Figures 3 and 4).

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Fundamental to realizing long-range induced pairing in doped topological insulators on
Nb is the presence of bulk VB or CB carriers (Figures 1A and 2), but the Fermi surface topology
of *p*-doped Sb_2Te_3 —namely, hole-like TSS and VB well separated in momentum space
(Figure 1D)—and its role in channeling or hindering this superconductivity have been
overlooked.^{15,18} Cooper pairing induced into Sb_2Te_3 via Andreev reflection at the heterointerface
is transported to the Sb_2Te_3 surface through bulk VB hole carriers since unlike topological
quasiparticles, their wavefunctions are spatially distributed throughout Sb_2Te_3 (Figures S6–

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3 S9).^{32,33} Naturally, such Cooper pairs lose their phase coherence at large distances away from the
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5 Sb₂Te₃/Nb heterojunction as the proximity-induced gap decays with increasing Sb₂Te₃ thickness
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7 (Figures 3 and 4).^{15–18,35} Upon reaching the surface through VB carriers, Cooper pairing is
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9 transmitted into the TSS through internal proximity effects imposed by interband
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11 superconducting coherence in momentum space,^{6–9} because the TSS are localized within the first
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13 couple QL (Figures S6–S9) and cannot couple effectively with Cooper pairs at the Sb₂Te₃/Nb
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15 interface. This coherence is also inherited from the underlying Nb, which manifests an *s*-wave
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17 superconducting gap across its Fermi surface at low temperatures.^{7,39,40}
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21 Thus, while hole-like bulk VB in *p*-doped Sb₂Te₃/Nb are pure channels nondegenerate
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23 with TSS at the Fermi level, they are nevertheless arbitrators of self-induced proximity effects
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25 that impress isotropic *s*-wave gaps onto the TSS.^{6–9} This situation contrasts from that of *n*-doped
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27 Bi₂Se₃/Nb, where the TSS and bulk CB are nearly degenerate at the Fermi level, which evidently
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29 enhances quantum-mechanical coupling and thus sharing of superconductivity between these
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31 states.^{15,18} Incidentally, per Figure 4A, the quasiparticle coherence length of Cooper pairs in
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33 Sb₂Te₃/Nb (~4.7 QL) is also smaller than that of Bi₂Se₃/Nb (~8.4 QL);¹⁵ the difference is
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35 attributable to coherent band structure mismatch of the doped topological insulator with Nb,^{39,40}
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37 whose Fermi surface possesses multiple zone-centered bulk pockets—like Bi₂Se₃ but unlike the
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39 spatially localized TSS contour of Sb₂Te₃ (Figure 1B).^{22,25} Lastly, since an *s*-wave gap arises in
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41 the spin-helical TSS (Figures 2–4), Sb₂Te₃ as a topological metal on Nb could host Majorana
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43 zero modes due to its Fermi surface topology of nondegenerate surface and bulk contours
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45 (Figure 2A–C),^{8–10,16} but trivial VB carriers may obscure transport properties of these topological
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47 effects.^{13,18,23,26} Overall, for doped topological insulators on Nb, if there are prominent bulk states
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49 at the Fermi level—even those separated in momentum space from the TSS, a long-range and
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3 isotropic superconducting gap will emerge on topological surfaces at low temperatures. Our
4 findings add greater engineering flexibility for realizing robust pairing in nontrivial boundary
5 states of artificial topological structures, which should guide searches for emergent quasiparticle
6 excitations needed for building topological qubits.
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14 **METHODS**

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17 **Fabrication of $\text{Sb}_2\text{Te}_3/\text{Nb}$.** Before MBE growths of Sb_2Te_3 thin films at the University of
18 Illinois, 6H-SiC(0001) substrates were degassed at $\sim 500^\circ\text{C}$ for an hour and then annealed
19 repeatedly to $\sim 1300^\circ\text{C}$, yielding bilayer-graphene-terminated surfaces. Afterwards, high-purity
20 Sb and Te were co-evaporated from an electron-beam evaporator (Sb) and an effusion cell (Te)
21 onto substrates heated to 280°C . The Te/Sb flux ratio was 10:1, and the growth rate was
22 typically ~ 15 min per QL. Subsequently, Sb_2Te_3 films were annealed at 310°C for ~ 30 min to
23 obtain smoother surfaces, as demonstrated by *in situ* reflection high-energy electron diffraction
24 (RHEED) and photoemission. To fashion $\text{Sb}_2\text{Te}_3/\text{Nb}$ flip chips, all Sb_2Te_3 films were coated
25 with a 60-nm-thick polycrystalline (110)-oriented Nb film by magnetron sputtering at an Ar gas
26 pressure of 6 mTorr and a power of 140–150 W; this deposition was done at $\sim 25^\circ\text{C}$ to inhibit
27 interdiffusion of Nb into Sb_2Te_3 .^{15,19,31} Each sample was then flipped over and glued onto a
28 polished Cu plate with a low-temperature-curing Ag epoxy; a cleavage pin was lastly attached to
29 the substrate's backside using similar epoxy.
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49 **Photoemission Measurements.** Ultrahigh-resolution ARPES was performed at the Institute for
50 Solid State Physics at The University of Tokyo in a laser-based setup, which consists of vacuum
51 ultraviolet lasers with photon energies 6.994 eV and 5.821 eV, a Scienta HR8000 analyzer, and a
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3 sample manipulator cooled with superfluid liquid helium. Each $\text{Sb}_2\text{Te}_3/\text{Nb}$ was
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5 crystallographically aligned onto the sample holder *ex situ* before cleavage based on the SiC
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7 substrate's high-symmetry cleavage planes and also the as-grown film's ARPES and RHEED
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9 measurements. Here, the geometry chosen had the momentum axis of each laser-ARPES map
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11 nominally parallel to $\overline{\Gamma\text{K}}$ (k_x -direction). Any sample misalignment was minimal per constant
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13 energy contour mappings of flip chips after cleavage (Figure 2). During laser-ARPES, the
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15 sample's temperature was tuned from 10 K down to 1.5 K, and the energy resolutions were
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17 ~ 1.6 meV and ~ 0.8 meV (or better) for 6.994-eV and 5.821-eV lasers, respectively. All
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19 $\text{Sb}_2\text{Te}_3/\text{Nb}$ EDCs, from which BCS zero-temperature gaps were determined via eq 1, were
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21 acquired by integrating the ARPES intensity within $\pm 0.015 \text{ \AA}^{-1}$ of the indicated momentum
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23 component k_x along $\overline{\Gamma\text{K}}$. For details about the Fermi-level calibration and simultaneous fittings
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25 of zero-temperature gaps (Figures S10 and S11), see the discussion in the Supporting
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27 Information and methods in prior works.^{15,18,36–38} ARPES maps of as-grown Sb_2Te_3 were
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29 garnered at the University of Illinois at 30 K using a Scienta-Omicron VUV5k He lamp
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31 (21.22-eV photons) and a Scienta R4000 analyzer. Preliminary ARPES data to validate the
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33 flip-chip methodology were obtained at Beamline 10.0.1.1 (HERS) at the Advanced Light
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35 Source, Lawrence Berkeley National Laboratory.
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45 **Computational Details.** First-principles calculations of freestanding Sb_2Te_3 films (Figures S6–
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47 S9) were conducted in the Quantum Espresso package⁴¹ under the generalized gradient
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49 approximation with Perdew-Burke-Ernzerhof functionals.⁴² Spin-orbit coupling was included.
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51 Projected augmented wave pseudopotentials with an energy cutoff of 612 eV were employed,⁴³
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53 and a periodic slab geometry with a vacuum gap larger than 15 Å was adopted in the modeling of
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3 each Sb_2Te_3 film. The lattice constants of N QL Sb_2Te_3 for $N > 3$ were set to the bulk values
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5 ($a = 4.26 \text{ \AA}$ and $c = 30.46 \text{ \AA}$),²⁶ while 3 QL Sb_2Te_3 was allowed to relax via Grimme dft-D3
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7 corrections⁴⁴ with residual atomic forces less than 1 meV/\AA . Band structure calculations were
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9 performed on Γ -centered $12 \times 12 \times 1$ Monkhorst-Pack grids⁴⁵ with the self-consistent
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11 convergence criterion for the total ground-state energy set to 10^{-7} eV .
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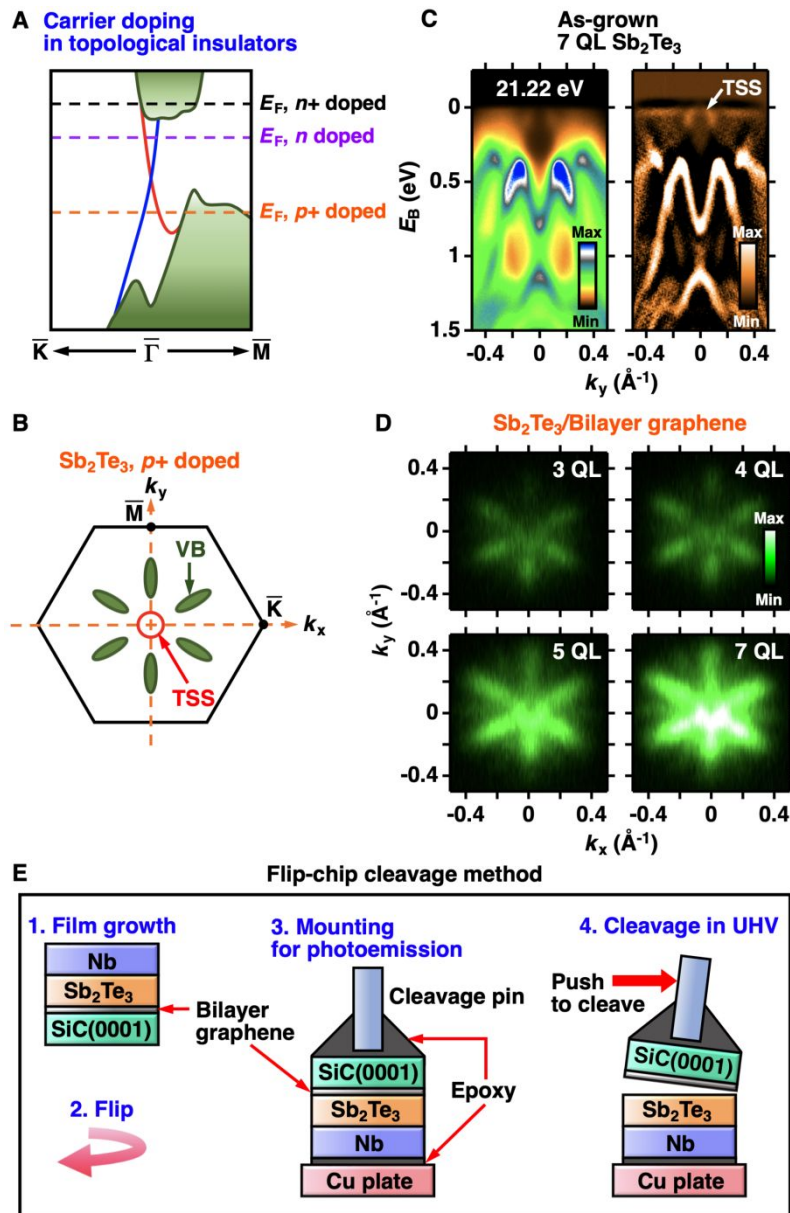


Figure 1. Fabricating $p+$ doped Sb_2Te_3 for Nb-based flip chips. (A) Schematic band structure of bulk carrier doping in topological insulators; dashed lines indicate Fermi levels for $n+$ (black), lightly n (purple), and $p+$ (orange) doped systems. (B) Sketch of the Fermi surface of Sb_2Te_3 , which consists of elongated VB hole pockets (green) and a zone-centered TSS contour (red). (C) Photoemission spectra (left) and its two-dimensional second derivative (right) of as-grown 7 QL Sb_2Te_3 on bilayer graphene measured at 30 K along $\overline{\Gamma\text{M}}$ using 21.22-eV photons.

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3 (D) Fermi surface maps of Sb_2Te_3 films taken at 30 K with 21.22-eV photons; to obtain each
4 mapping, the ARPES intensity was integrated within ± 10 meV of the Fermi level. (E) Diagram
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6 summarizing our flip-chip method for fabricating Sb_2Te_3 films on Nb.
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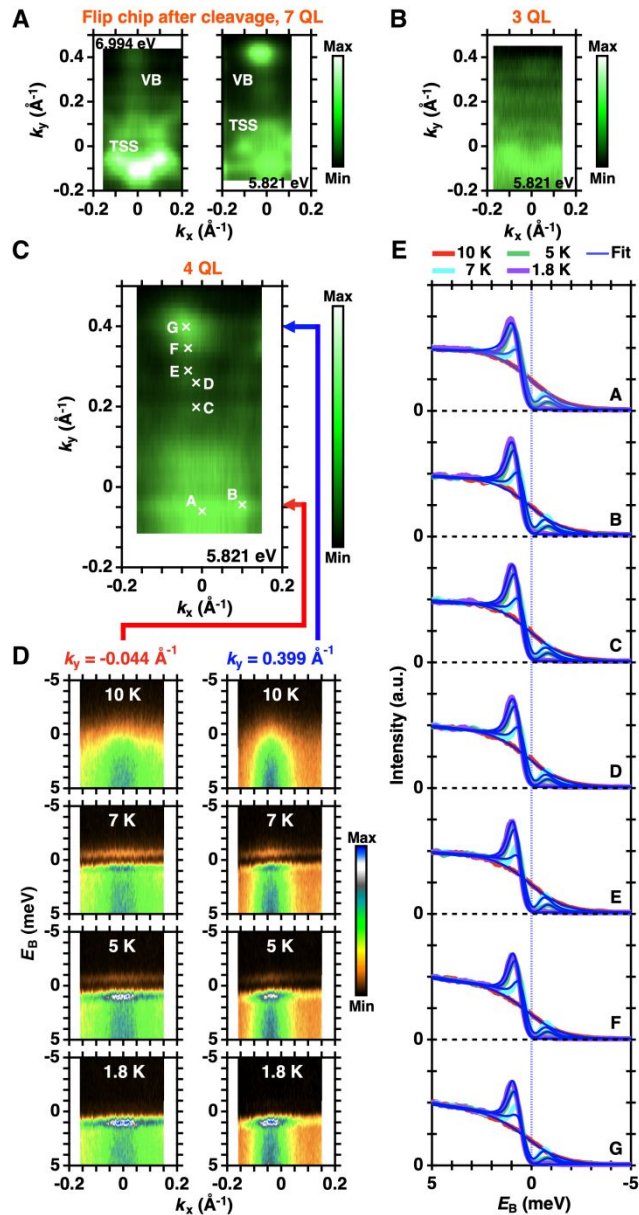


Figure 2. Constant energy contours and pairing in topological $\text{Sb}_2\text{Te}_3/\text{Nb}$. (A) Constant energy contours near the Fermi level of flip-chip 7 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ after cleavage obtained with 6.994-eV (left) and 5.821-eV (right) photons at 1.8 K; contours due to VB and TSS are indicated in both maps, and to generate each map, the ARPES intensity was integrated from $E_B = 0$ to 5 meV. (B) Similar to (A) but for 3 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ at 1.5 K. (C) Same as (B) but for 4 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ at 1.8 K. (D) Select band maps at momentum cuts k_y along $\overline{\Gamma\text{M}}$ through the TSS (left)

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3 and VB (right) identified by the connecting red and blue arrows to (C), respectively.
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5 (E) Temperature-dependent EDCs overlaid with BCS fits (blue curves) at momenta A–G
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7 labelled in (C).
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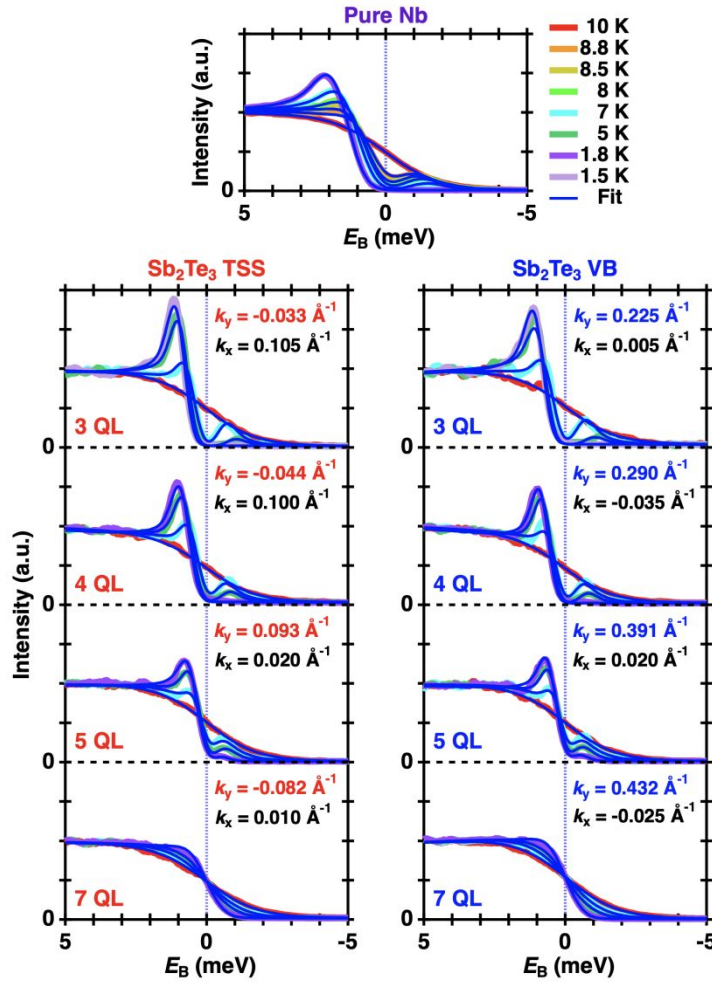


Figure 3. Bulk versus topological EDCs as a function of Sb_2Te_3 thickness. Results are reported for a pure Nb reference (top, 6.994-eV photons) and 3–7 QL $\text{Sb}_2\text{Te}_3/\text{Nb}$ (bottom, 5.821-eV photons), and the blue curves in each panel are BCS fits. For every $\text{Sb}_2\text{Te}_3/\text{Nb}$ EDC, the momentum components parallel to $\overline{\Gamma\text{K}}$ (k_x -direction) and $\overline{\Gamma\text{M}}$ (k_y -direction) are indicated.

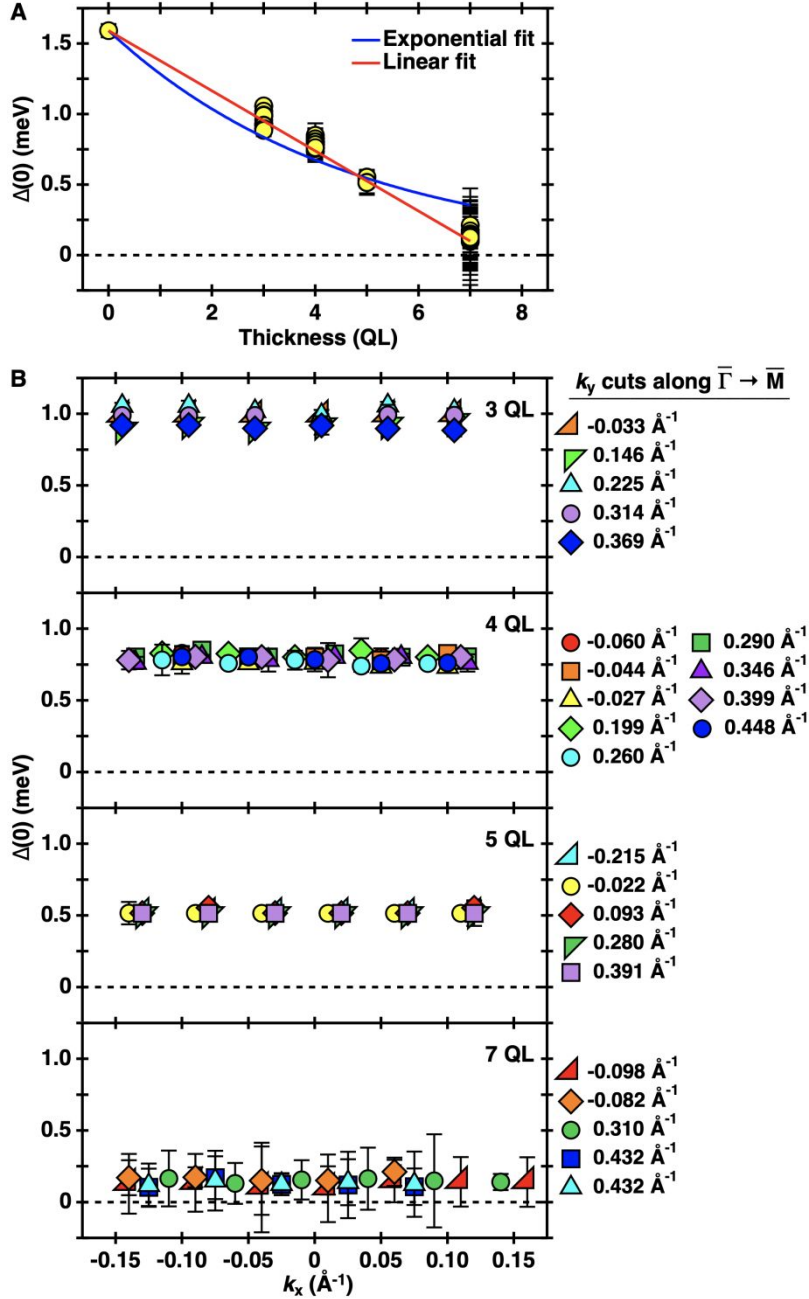


Figure 4. Momentum-resolved zero-temperature superconducting gaps versus thickness.

(A) Zero-temperature gap $\Delta(0)$ versus Sb_2Te_3 film thickness overlaid with exponential (blue) and linear (red) fits. (B) $\Delta(0)$ as a function of Sb_2Te_3 film thickness and in-plane momenta along $\bar{\Gamma}\bar{K}$ (k_x -direction) and $\bar{\Gamma}\bar{M}$ (k_y -direction). The error bar for each gap is the standard deviation estimated by each simultaneous fit.

AUTHOR INFORMATION

Author Contributions. J.A.H. and T.-C.C. conceived the project. J.A.H., Y.L., M.-K.L., and T.-C.C., with the aid of S.S.B. and J.N.E., conducted the MBE growths and with S.N., K.O., J.H., J.-E.L., and S.-K.M. designed and/or prepared flip-chip samples. S.N. and K.O., with the assistance of T.N., A.M., Y.Z., T.S., A.F., and S.S., performed the laser-ARPES measurements. Y.L. conducted the first-principles calculations. S.S.B. with J.N.E. performed the transport measurements. J.A.H., Y.L., M.-K.L., and T.-C.C., with feedback from J.H., J.-E.L., and S.-K.M., conducted ARPES characterizations at the University of Illinois. J.A.H., S.N., Y.L., T.N., A.M., M.-K.L., K.O., and T.-C.C. analyzed the data. T.-C.C., K.O., J.A.H., and S.N. interpreted the data. T.-C.C. led the group at the University of Illinois; K.O. led the group at the Institute for Solid State Physics. T.-C.C. organized the project.

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45 **ABBREVIATIONS**

46 CB, conduction band(s); TSS, topological surface state(s); VB, valence band(s); QL, quintuple
47 layer(s); MBE, molecular beam epitaxy; ARPES, angle-resolved photoemission spectroscopy;
48 EDC, energy distribution curve; DOS, density of states; RHEED, reflection high-energy electron
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ASSOCIATED CONTENT

Supporting Information. Photoemission VB Mappings of As-Grown Films and Sb₂Te₃/Nb; Transport Measurements of Bulk Nb Resistance; First-Principles Computations for Freestanding Sb₂Te₃; Methods for Determining the Fermi Level and BCS Gap; Supporting References.

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