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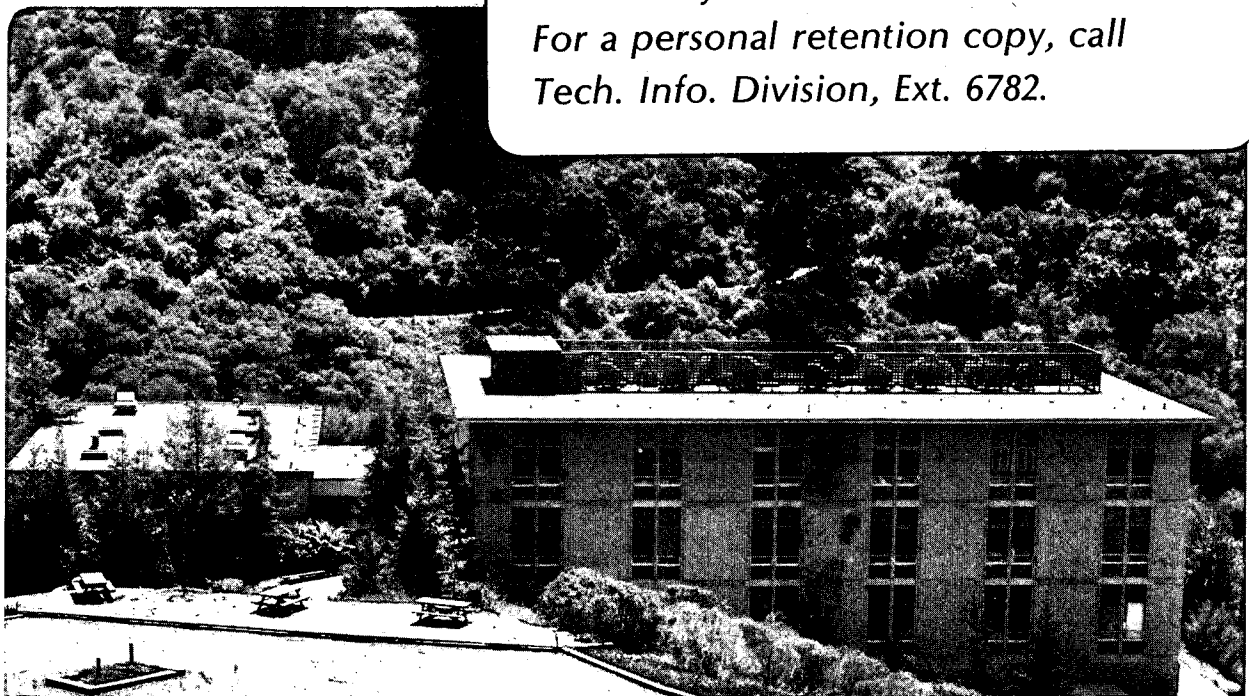
SIMULATION OF THE NOISE RISE IN THREE-PHOTON
JOSEPHSON PARAMETRIC AMPLIFIERS

J.F. Miracky and J. Clarke

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SIMULATION OF THE NOISE RISE IN THREE-PHOTON
JOSEPHSON PARAMETRIC AMPLIFIERS

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ABSTRACT

Analog simulations of the three-photon Josephson parametric amplifier indicate that the noise rise observed in experimental devices arises from occasional hopping between a mode at the pump frequency, ω_p , and a mode at the half-harmonic, $\omega_p/2$. The hopping is induced by thermal noise associated with the shunt resistance.

The three-¹⁻⁴ and four-⁵-photon Josephson parametric amplifiers have been plagued by the problem of "noise rise", a noise temperature that increases roughly as the power gain.⁶⁻⁹ Huberman et al.¹⁰ first suggested that chaos might be the explanation of this phenomenon in the four-photon case, and there has subsequently been a considerable literature on the subject.^{7-9,11} Pedersen and Davidson⁸ concluded that chaos could indeed explain the noise rise in the four-photon amplifier, while Levinsen⁹ concluded that chaos could not be the explanation in either the three- or four-photon case. Levinsen⁹ emphasizes that an important aspect of the real amplifiers has usually been neglected in the other studies of chaotic behavior, namely the circuit that couples the signal to and from the junction. Since the gain of the amplifier is intimately related to the impedance presented by the coupling circuit, any model that attempts to explain the noise rise must include this element.

Recent¹² experimental studies of chaos in a Josephson tunnel junction shunted by a resistor with significant self-inductance have brought to light an important effect due to the presence of thermal noise in a non-linear system exhibiting subharmonic modes and chaos. In this system, noise-induced "hopping" between nearby modes can occur, resulting in copious levels of noise at low frequencies. To test whether such hopping effects can occur in a Josephson parametric amplifier, we have simulated the three-photon mode with an analog simulator that includes both a calibrated thermal noise source and a model for the coupling circuit. We conclude, first, that chaos cannot explain the noise rise, and, second, that there is strong evidence that the hopping mechanism accounts for the observed noise.

The analog circuit, suggested by Levinsen,⁹ is illustrated in Fig.

1. We assume the resistively shunted junction model with $\beta_C \equiv 2\pi I_0 R_J^2 C / \Phi_0 = 26.3$ for all simulations discussed here; I_0 is the critical current, $1/R_J$ is the quasiparticle conductance, C is the self-capacitance, and $\Phi_0 \equiv h/2e$ is the flux quantum. The pump is represented by a current source, $I_p \cos(\omega_p t)$, and the details of its coupling circuit are assumed to be unimportant. We report simulations for $\omega_p/\omega_0 = 1.12$, where $\omega_0 \equiv (2\pi I_0 / \Phi_0 C)^{1/2}$ is the maximum plasma frequency. Although Kautz¹¹ states that chaotic solutions exist only for $1/R_J C \lesssim \omega \lesssim \omega_0$, we have discovered no significant difference between simulations for $\omega_p/\omega_0 = 1.12$, $\omega_p/\omega_0 = 0.93$, and $\omega_p/\omega_0 = 0.84$, except in the pump amplitude required for maximum gain. In real parametric amplifiers, one generally uses a circulator to couple the signal into and out of the junction. We represent this element in our model by a resonant circuit tuned to the signal frequency, $\omega_S = (L' C')^{-1/2}$. We chose values of L' , C' and of the series and load resistors, R' and R_L , to achieve a Q for the coupling circuit, $(L'/C')^{1/2} / (R' + R_L)$, of about 20. We also maintained the conditions $R' = R_L$ and $R' + R_L \approx R_J$ necessary to achieve near-optimum noise performance.⁴ Finally, a white noise current, $I_N(t)$, was included to represent Nyquist noise in the shunt conductance of the junction.¹³ The magnitude of this noise is characterized by $\Gamma \equiv 2\pi k_B T / I_0 \Phi_0$.

We followed the standard procedure in setting up the correct pump and dc-bias levels. With low pump power and a small signal at $\omega_S \approx \omega_p/2$, we adjusted the dc-bias current, I_{dc} , until signal gain and an idler at frequency $\omega_i = \omega_p - \omega_S \approx \omega_S$ were observed. We then increased the pump amplitude, I_p , adjusting I_{dc} to achieve maximum gain. Maximum gain oc-

curs when $\omega_S = \omega_0 [J_0(\eta)]^{1/2} [1 - (I_{dc}/I_0)^2]^{1/4}$, where $\eta \equiv 2eV_P/\hbar\omega_P$ and V_P is the voltage across the junction at the pump frequency.

Figure 2 illustrates representative examples of our results. In Fig. 2(a), we plot the spectral density of the voltage across R_L for $I_P/I_0 = 0$ and $I_P/I_0 = 0.682$ (the point of maximum gain) in the absence of added thermal noise (the residual noise level corresponds to $\Gamma = 6.1 \times 10^{-7}$). The idler is approximately equal to the signal in amplitude. The smaller peaks at frequencies below ω_i and above ω_S represent resonances associated with the coupling circuit.¹⁴ The signal gain, G_S , is 19.9 dB, while the noise gain, G_N , at frequency ω_S increases by 31 dB as I_P/I_0 is increased from 0 to its value for maximum gain. (The signal gain, G_S , is the ratio of the power at $\omega = \omega_S$ for $I_P/I_0 = 0.682$ to that at $I_P/I_0 = 0$; the noise gain, G_N , is the ratio of the noise powers at $\omega \approx \omega_S$ for the same two pump levels.) For larger values of I_P or I_{dc} , a bifurcation occurs to an oscillation at $\omega_P/2$. This behavior is well-documented experimentally,¹⁵ and is a useful means of showing that the maximum gain condition has just been passed. At the bifurcation point, signal amplification drops sharply. Furthermore, there is no evidence for chaotic solutions at nearby bias points.

Figure 2(b) shows the results for the same range of pump amplitudes with $\Gamma = 1.8 \times 10^{-4}$, or $T = 4.2K$ for $I_0 = 1$ mA. The maximum signal gain decreases to 14.0 dB from its noise-free value of 19.9 dB. More importantly, the noise level near ω_S has increased far more sharply than the signal, by 32 dB as the gain is increased from unity to its maximum value.

An important issue in the history of both the three- and four-photon amplifiers has been the exact dependence of the noise temperature, T_N , on

the signal gain, G_S . To address this question, in Fig. 3 we plot G_N/G_S (a quantity proportional to T_N) versus G_S , where we varied G_S by varying I_P with I_{dc} kept fixed at its value for maximum gain. For $\Gamma = 6.1 \times 10^{-7}$ (upper curve) T_N rises somewhat as G_S rises to about 7 dB, and is constant for higher values of G_S . Thus, for $G_S > 7$ dB, T_N is independent of G_S , as one would expect for a useful amplifier. On the other hand, for $\Gamma = 1.8 \times 10^{-4}$ (lower curve), the noise temperature rises steadily as G_S is increased, by 18 dB as the gain increases from 0 to 14 dB. We note that T_N rises more rapidly than G_S for values of G_S below about 10 dB, and more slowly than G_S for higher values of G_S . This deviation from a linear relationship between T_N and G_S is very compatible with the experimental results of Mygind *et al.*² for values of G_S up to about 8 dB. However, it is difficult to make meaningful comparisons of the magnitudes of T_N obtained from our simulations with those obtained from real devices without more accurate information on the parameters of the real junction and, in particular, of the coupling circuit.^{3,4}

To explore whether there is a well-defined threshold for the onset of the noise rise, we measured G_S and G_N for several values of Γ ; the results are summarized in Table I. Even for values of Γ as low as 0.42×10^{-5} (corresponding to a temperature of 0.1K for $I_0 = 1$ mA), the noise rise is clearly present. The ratio G_N/G_S is almost independent of temperature over the range $0.1K \leq T \leq 0.42$ (for $I_0 = 1$ mA). Thus, only a low level of thermal noise is necessary to trigger the noise rise.

From these results, we can draw three conclusions about the noise rise in three-photon parametric amplifiers. First, chaos is excluded as a possible explanation. It is an inescapable fact that to achieve signif-

icant levels of gain the amplifier must be operated at values of bias current and pump power below the threshold for bifurcation to period two, and well-removed from possible chaotic modes that might exist at higher bias levels. Second, the noise rise occurs only when a non-zero level of thermal noise is present. Third, the noise rise is most likely the result of occasional hopping, induced by thermal noise, between a bias point in the unbifurcated region to an unstable one in the bifurcated region. Qualitatively, one would expect this picture to give rise to a noise temperature that increases with gain: One increases the gain by biasing the amplifier nearer to the threshold for a period-doubling bifurcation, so that the likelihood of noise-induced hopping is inevitably increased.

Finally, we emphasize that it is most unlikely that the mechanism we have presented here for the noise-rise in the three-photon amplifier accounts for the noise-rise in the four-photon amplifier, for which the amplification process involves significantly different dynamics.

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13. Strictly speaking, one should use an expression for the quasiparticle current noise. Given the uncertainties in the parameters of real amplifiers, however, the use of the Nyquist formula is an adequate

approximation.

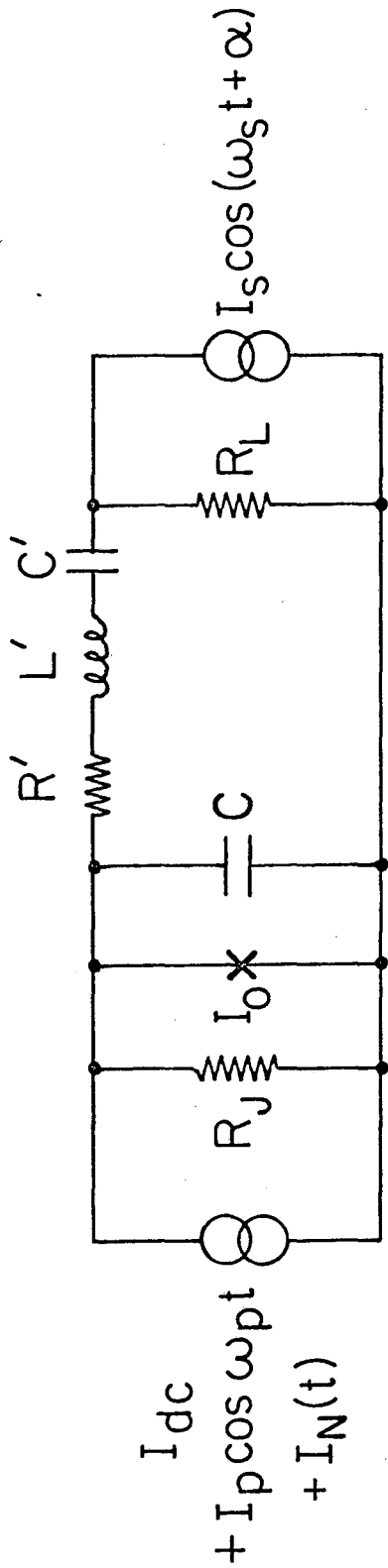
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TABLE I. Dependence of G_S , G_N and G_N/G_S on level of thermal noise.

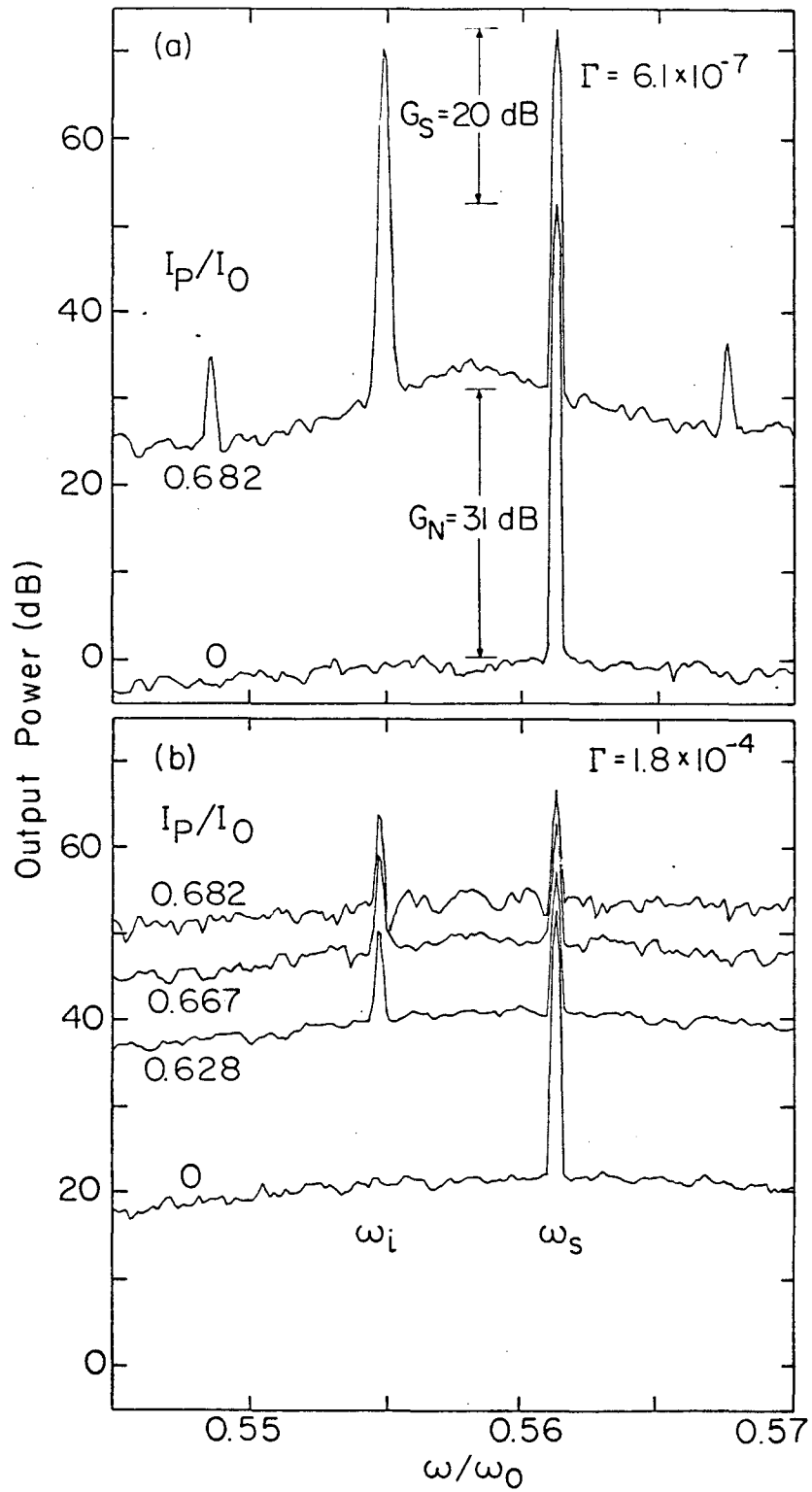
$\Gamma (\times 10^{-5})$	G_S (dB)	G_N (dB)	G_N/G_S (dB)
0.061	19.9 ± 0.1	31.1 ± 1.1	11.2 ± 1.1
0.42	18.8 ± 0.1	36.6 ± 0.7	17.8 ± 0.7
4.2	16.7 ± 0.1	36.3 ± 0.7	19.6 ± 0.7
8.4	15.6 ± 0.1	34.7 ± 0.5	19.1 ± 0.5
18.0	14.0 ± 0.1	32.0 ± 0.7	18.0 ± 0.7

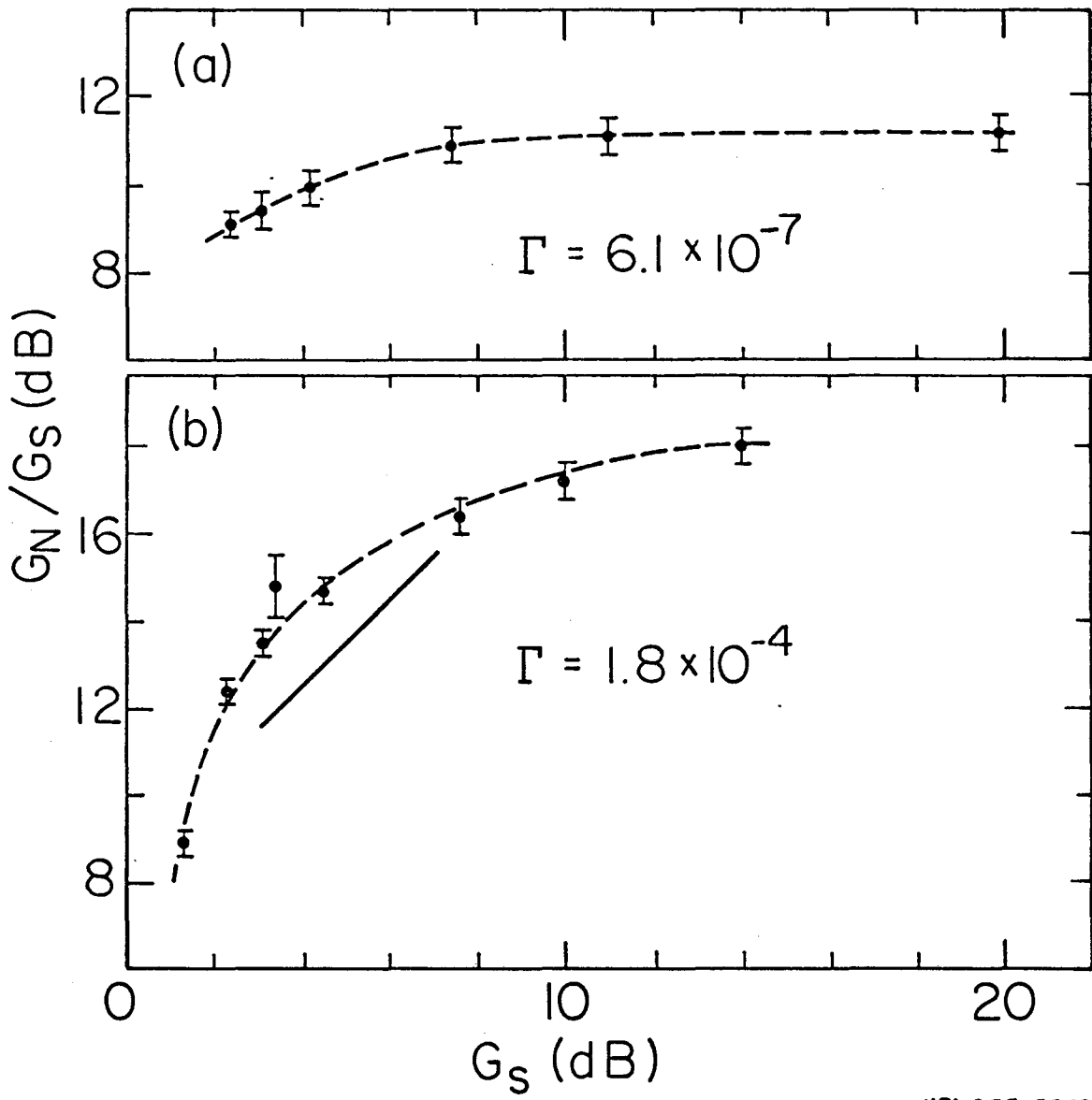
Figure Captions

- Fig. 1 Circuit for analog simulation of three-photon Josephson parametric amplifier.
- Fig. 2 Spectral density of voltage across R_L for analog parametric amplifier with $\beta_C = 26.3$ and $\omega_P/\omega_O = 1.12$ for various pump powers. In (a) $\Gamma = 6.1 \times 10^{-7}$ while in (b) $\Gamma = 1.8 \times 10^{-4}$. In both cases, the 0dB reference level is the noise level at ω_S in (a).
- Fig. 3 G_N/G_S (proportional to T_N) vs. G_S for (a) $\Gamma = 6.1 \times 10^{-7}$ and (b) $\Gamma = 1.8 \times 10^{-4}$. Solid line represent $T_N \propto G_S$.



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