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The Three-Dipole Kicker Injection Scheme for the ALS-U Accumulator Ring

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The ALS-U light source will implement on-axis single-train swap-out injection employing an accumulator between the booster and storage rings. The accumulator ring design is a twelve period triple-bend achromat that will be installed along the inner circumference of the storage-ring tunnel. A non-conventional injection scheme will be utilized for top-off off-axis injection from the booster into the accumulator ring meant to accommodate a large ~ 300 nm emittance beam into a vacuumchamber with a limiting horizontal aperture radius as small as 8 mm. The scheme incorporates three dipole kickers distributed over three sectors, with two kickers perturbing the stored beam and the third affecting both the stored and the injected beam trajectories. This paper describes this "3DK" injection scheme and how it fits the accumulator ring's particular requirements. We describe the design and optimization process, and how we evaluated its fitness as a solution for booster-to-accumulator ring injection.

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I. INTRODUCTION

The ALS-U is the upgrade of the Advanced Light 17 Source to a 4th generation diffraction-limited soft x-18 ray light source [1]. Achieving ALS-U's high bright-19 ness goal requires strong focusing-magnet gradients; the 20 strong gradients necessitate strong chromatic sextupoles 21 and these will shrink the dynamic aperture of the storage 22 ring (SR) to about 0.5 mm radius once lattice imperfec-23 tions are taken into account. 24

To inject into such a small dynamic aperture, ALS-25 U will implement on-axis single-train swap-out injection 26 utilizing an accumulator ring (AR) housed along the in-27 ner wall of the SR tunnel. See Fig. 1 for an overview of 28 the ALS-U accelerator complex. A small 2 nm-rad natu-29 ral emittance, much smaller than the approximately 300 30 nm-rad emittance of the beam delivered by the existing 31 booster, is required to inject into the storage ring with 32 near-100% efficiency and sufficient margin. In addition 33 to its function as a damping ring, the AR is intended to 34 act as a beam-charge recycler in between swap-outs. The 35 SR average current is 500 mA, distributed evenly over a 36 284-bunch beam consisting of eleven trains of 26 (or 25) 57 37 bunches each. The AR is designed to carry a single train 58 38 at a time; this is swapped with one of the SR trains once ⁵⁹ 39 every about half-minute and replenished with top-off in-40 jection from the booster before the next swap-out. 62 42

The AR design has to fulfill two competing demands on 63 43 the vacuum-chamber aperture: it should be wide enough 64 44 to accept the large emittance beam from the booster, 65 45 with a goal of $\gtrsim 95\%$ injection efficiency, but as narrow 66 46 as possible to minimize the magnets' aperture and thus 67 47 their weight and volume so that the AR can fit in the 68 48 same tunnel as the SR. Consideration of these demands 69 49 has guided the choice of injection scheme that recognizes 70 50 that the AR can tolerate a significant injection transient. 71 51 Thus, an injection cycle leaves both the stored and in-72 52 jected beams with significant transients, both contained 73 53 in the dynamic aperture of the machine. Such a tech-74 54 nique is also referred to as aperture sharing. Fully ex-75 55 ploiting the latitude offered by the latter observation, we 76

TABLE I. Parameter list of the ALS-U Accumulator Ring and existing ALS.

	AR	ALS ^a		
Beam energy	$2.0{ m GeV}$	$1.9{ m GeV}$		
Circumference	$182.122\mathrm{m}$	$196.8\mathrm{m}$		
Tune x/y	16.221/8.328	16.165/9.25		
Natural chrom. x/y	-43/-36	-46.8/-39.6		
Mom. compaction	1.04×10^{-3}	0.9×10^{-3}		
Emittance	$1.8\mathrm{nm}$	$1.8\mathrm{nm}$		
Dispersion in straight	$11.6\mathrm{cm}$	$15.0\mathrm{cm}$		
Charge per bunch	$1.15\mathrm{nC}$	$1.1\mathrm{nC}$		
Energy spread	8.5×10^{-4}	9.6×10^{-4}		
Energy loss per turn	$269\mathrm{keV}$	$228\mathrm{keV}$		
Damping time $x/y/z$	6.2/8.5/5.2 ms	7.7/8.9/5.0 ms		
Harmonic number	304	328		
Main RF frequency	$500.417\mathrm{MHz}$	$499.654\mathrm{MHz}$		
Main RF voltage	$1.0\mathrm{MV}$	$1.2\mathrm{MV}$		
Synchrotron tune	4.9×10^{-3}	5.4×10^{-3}		

^a Emittance and energy loss per turn reported for the ALS are for the lattice without superbends and without insertion devices.

have developed a simple and nearly 100% efficient injection scheme, coined "3DK", that utilizes three dipole kickers distributed over three sectors in combination with a pair of thick and thin pulsed septa.

In short, the first two dipole kickers ("prekickers") kick only the stored beam and place it on a trajectory that partly compensates the main injection kick placed further downstream, which kicks both the stored and injected particles onto stable (but not closed) trajectories. The features of this scheme include 1) the reduced straight length of the AR is accommodated by distributing the kickers among 3 straights, 2) near-100% injection efficiency, 3) a reduced septum aperture that eases vacuum and magnet engineering in the injection straight, 4) flexibility to trade between residual oscillations of the stored and injected beams, and 5) reliance on only conventional power supply and kicker technology.

An important aspect of our study is the demonstration that potential drawbacks resulting from the combination



FIG. 1. The Advanced Light Source Upgrade complex. The 3 dipole kickers and injection septum of the 3DK booster-toaccumulator injection scheme are highlighted. Every 1.4s up to four bunches are generated and accelerated to 2 GeV through the existing linac and booster and then injected through the BTA into the new AR to fill or top-off bunches in a single 26- (or 25-) bunch train. Every \sim 30s this train is swapped with one of the eleven trains circulating in the Storage Ring (SR).

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of relatively large stored-beam oscillations and collective 97
effects are manageable. 98

79 Other schemes that were considered and ultimately 99 80 discarded included a non-linear kicker (NLK), a con-100 81 ventional 4-kicker single-straight closed-bump injection101 82 scheme, as well as a two-dipole kicker variant of the 3DK102 83 scheme. These will be briefly discussed in this paper as103 84 well. 104

Section II is a brief introduction to the ALS-U AR.¹⁰⁵ 85 The layout and design of the 3DK injection scheme is106 86 described in Sec. III. For completeness Sec. IV briefly¹⁰⁷ 87 describes the design of the booster-to-AR transfer line.108 88 The robustness of the injection scheme against lattice109 89 imperfections is discussed in Sec. V. Impedance and col-110 90 lective effects, as well as multi-bunch feedback issues are¹¹¹ 91 addressed in Sec. VII. Alternatives to the 3DK injection¹¹² 92 scheme are discussed in the appendix. 93 113

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II. ALS-U ACCUMULATOR RING

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The accumulator ring is an intermediary that needs to¹¹⁸ have a large enough acceptance to capture near-100% of¹¹⁹

the relatively large booster beam, and small enough emittance to inject with near-100% efficiency into the storage ring. To that end, the existing ALS twelve-sector triplebend acromat layout meets these needs. Such a layout is well-understood, allowing R&D efforts to be focused on the storage ring and transfer lines. With that, the ALS-U AR is essentially a slightly smaller version of the existing ALS twelve period triple-bend acromat. The AR's basic parameters are compared with those of the existing ALS in Table I. The optics and layout through one arc are shown in Fig. 2. To adapt the ALS layout to the AR layout, the length of the straight sections was shrunk from 9.386 m to 8.762 m and the arcs were shrunk from 7.014m to 6.415 m by reducing the magnet spacing. Nominal bend, quadrupole, and sextupole magnet lengths are the same between the ALS and AR. These adjustments bring the total circumference down from 196.805 m to 182.122 m which makes the AR fit neatly along the inner tunnel wall. The AR utilizes a non-swept gradient dipole design (picture a geometry similar to a partially opened book), as does the ALS. The beam energy is increased from 1.9 GeV to 2.0 GeV to match that of the ALS-U storage ring. The AR emittance of 1.8 nm is comparable to that of the

ALS. 120

To preserve egress, the AR will be mounted close to162 121 the tunnel ceiling, about 2 m above the floor and about₁₆₃ 122 0.6 m above the plane of the storage ring. The AR mag-165 123 net stands are a combination of floor and wall attach-166 124 ments. The elevated installation and limited space in-167 125 side the tunnel places a premium on reducing the size₁₆₈ 126 and weight of the magnets, and so the vacuum chamber₁₆₉ 127 dimensions were shrunk, bringing the pole tips closer to₁₇₀ 128 beam, achieving the same gradients with less bulky mag-171 129 nets. The arc and straight chambers are round and 14.2_{172} 130 mm in radius. The dipole chambers are elliptical with₁₇₃ 131 a 20 mm axis in the horizontal and 7.28 mm axis in the₁₇₄ 132 vertical. The limiting aperture is set by the injection₁₇₅ 133 septum, which has an 8 mm outward aperture. 134 176



FIG. 2. Lattice and magnet distribution of an arc in the ALS-188 U AR. The ring is composed of 12 such arcs. Shown are the189 beta and the dispersion functions (top), the aperture model¹⁹⁰ and the distribution of magnets (bottom). 191

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The AR-to-SR injection swap is expected to occur ap-193 proximately every 30 seconds. A long beam lifetime in¹⁹⁴ the AR is not necessary and so dynamic aperture and in-195 139 jection efficiency are prioritized when optimizing the AR.¹⁹⁶ 140 The AR dynamic aperture thus extends to the physical¹⁹⁷ 141 apertures. Simulations taking imperfections and correc-198 142 tion algorithms into account bring the expected usable 143 dynamic aperture close to linear acceptance. 144

Transfer lines intersect the AR along 3 consecutive 145 straights. Sector 12 is the take-off of the accumulator-146 to-storage ring (ATS) transfer line; the straight section 147 has to accommodate the dipole kicker and pulsed thin 148 septum required for extraction from the AR into the 149 ATS in addition to the first pre-kicker for AR injection 150 from the booster. Sector 1 houses the pair of booster-to-151 accumulator (BTA) injection septa, which are depicted in 152 Fig. 3; immediately upstream in the same straight sec-153 tion is the second pre-kicker for AR injection from the 154 booster. The sector 2 straight contains the landing point 155 of the storage ring-to-accumulator (STA) transfer line. 156 It has to accommodate the STA pulsed thin septum, as 157 well as both the dipole kicker for injection from the SR 158 and the main kicker for AR injection from the booster. 159 The close proximity of the three transfer lines and in-160

jection/extraction components posed a design challenge, requiring careful consideration of the layout and close interaction between the beam physics and engineering groups.

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The arrival of the injected bunches from the booster is timed to replenish the bunches of the depleted train in a top-off manner. In normal ALS-U operations we expect that a train circulating in the SR will lose about 10% of its charge before being swapped out. The beam coming out of the booster is 4 pulses long, with a separation of 3 empty buckets between each pulse. The total charge in the 4 pulses is approximately 0.5 nC, or about 10%of the charge that needs to be replenished, implying that about 10 injection shots will be needed to replenish the circulating train before swapping it back to the SR.

On-axis injection from the SR into the AR is more straightforward than injection from the booster; this and extraction from the AR into the SR are not in the scope of this paper.

3DK INJECTION SCHEME III.

The AR layout along with injection elements and beam trajectories during an injection cycle are depicted in Fig. 4. At the start of a BTA injection cycle, the stored bunch train is given an outward "pre-kick" at the upstream end of the sector 12 straight. A second outward pre-kick is applied at the upstream end of the next straight, which is sector 1. The injection septum is at the downstream end of sector 1. Injected particles make a large excursion through the sector 1 arc. The main injection kicker, located at the downstream end of sector 2, applies an outward kick to both the stored and injected particles, leaving both on trajectories that damp with very little particle loss. The strengths of the 3 kickers and injection septum are adjusted to control the injection transients and are shown in Table II. The kickers' bumps are confined to one turn and their flat top spans the entire bunch train and are timed to the train head,



FIG. 3. The layout diagram of the BTA thick and thin septa in sector 1. The separation between the injected beam and unkicked stored beam is 14 mm and the thickness of the thin septum blade is 1 mm.





FIG. 4. Trajectories of the stored (green) and injected (red) beams during an injection cycle for the "balanced" Mode A kicker strength settings. Solid black profile indicates horizontal physical aperture. Dashed lines delineate 3σ of the beam size. Kickers are labeled and represented by orange bow-ties. The first pre-kicker is located at the start of sector 12. The second pre-kicker and injection septum are located in sector 1. The main injection kicker in sector 2 kicks both the stored and injected particles.

irrespective of which buckets are being injected into. 199

One Turn

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The vacuum chamber between the injection point and²²⁹ 200 the second downstream dipole is horizontally widened to²³⁰ 201 accommodate the large excursion of the injected-beam²³¹ 202 trajectory but no special-aperture magnets are required.²³² 203

The injected bunches arriving from the pulsed thin $\operatorname{sep-}^{^{233}}$ 204 tum are offset 14 mm outward from the nominal chamber $^{\rm 234}$ 205 center, as depicted in Fig. 3. The transverse position of $^{\scriptscriptstyle 235}$ 206 the septum was arrived at by considering both the $\lim^{_{236}}$ 207 itation the septum places on dynamic aperture and the $^{\scriptscriptstyle 237}$ 208 constraint it imposes on the beam-trajectory oscillation $^{^{\rm 238}}$ 209 amplitude during the post-injection transient. The dis-²³⁹ 210 tance of the injected beam centroid to the septum sheet $^{\rm 240}$ 211 was arrived at by considering particle loss on the $\operatorname{septum}^{^{241}}$ 212 242 sheet and the amplitude of the injected particles. 213

243 The starting point for determining the optimal sep-214 tum angle is found by manually adjusting the angle of $_{245}^{244}$ 215 the injected particles to create a zero-crossing at the 246 216 main injection kicker. The septum angle is then $refined_{247}$ 217 along with the strengths of the 3 kickers by $applying_{248}^{248}$ 218 a Levenburg-Marquardt minimizer to the amplitudes of 249 219 the stored and injected transients in action/angle coordi- $_{\scriptscriptstyle 250}$ 220 nates. The optimum is that which minimizes the $action_{251}$ 221 of the centroids while preserving minimum distances from₂₅₂ 222 the limiting physical apertures and tolerating no ${\rm losses}_{2^{53}}$ 223 out to 3σ of stored beam. Design and optimization of $^{254}_{254}$ 224 the injection scheme was done using Tao, which is based²¹⁵₂₅₅ 225 of the Bmad accelerator code[2]. 226

The parameter space is explored in Table II, which₂₅₆ 227

presents the thin septum and kicker strengths for different injection modes, as well as the maximum amplitude and rms of the horizontal injection transient for the stored and injected beams. The injection losses and stored beam survival percentages were calculated using a 9000 particle Gaussian-weighted distribution extending to 4- σ in all three planes, tracked for 300 turns. The "on-axis injection mode," as was done at MAX IV [3], is expected to be useful during early commissioning. It will place the injected beam on-axis, but the stored beam, if present, will be left with a large oscillation amplitude that limits imperfection tolerance and generates large short-range wake fields. The "closed stored-beam orbit bump mode" eliminates the stored beam injection transient, but achieves only 22.3% injection efficiency. It is included here to bound the parameter space. The remaining three modes indicate different strategies to optimize performance for small but non-zero residual amplitudes of the stored and injected beams. Mode A, or "balanced mode," represents a compromise solution between the two previous modes and maintains near-100% injection efficiency while reducing the amplitude of the stored beam oscillations with an injected beam that is matched to the storage ring. For this mode, the transient of the stored beam is allowed to be larger than that of the injected beam as it has a much smaller beam size than the injected particles. The trajectories in Fig. 4 are based on Mode A.

The parameters of the injection elements are further re-

TABLE II. Injection modes achieved by adjusting kickers and septum strength. Mode A achieves a high injection efficiency with a small stored beam transient. Mode B reduces the stored beam transient to mitigate short range wake fields, at the expense of greater losses on the BTA-side septum sheet and due to injected particles exceeding the acceptance. Mode C recovers high injection efficiency by shrinking (mismatching) the horizontal β of the injected beam. Short-range wake fields were not studied for the on-axis injection and closed stored-beam bump modes.

		On-axis injection	Closed stored-beam bump	Mode A	Mode B	Mode C
Injection element strengths	Thin septum (mrad)	35.82	35.85	35.85	35.72	35.67
	Pre-kicker 1 (mrad)	0.365	0.489	0.383	0.417	0.417
	Pre-kicker 2 (mrad)	1.09	0.759	1.04	0.933	0.933
	Inj. kicker (mrad)	1.21	0.613	1.11	0.987	0.987
Post-injection cycle residuals	Stored beam rms (mm)	3.54	0.0	3.00	2.27	2.31
	Stored beam max (mm)	6.32	0.0	5.39	4.18	4.18
	Injected beam rms (mm)	0.0	4.58	0.898	1.24	1.22
	Injected beam max (mm)	0.0	8.16	1.59	2.21	2.17
Optics at septum exit	β_x (m)	14.82	14.82	14.82	14.82	11.33
	α_x	-0.139	-0.139	-0.139	-0.139	-0.275
	BTA-side septum losses (%)	0.76	0.76	0.80	1.05	0.13
	Capture losses (%)					
	no wakes	0.21	77.7	0.30	1.77	1.30
	with wakes	_	_	16.4	6.8	6.9
	with wake mitigations	_	_	0.7	1.1	1.0
	Stored Beam Survival (%)	99.9	99.9	99.9	99.9	99.9

fined after considering short-range transverse wake fields.290 257 Because of the non-zero injection transient, the stored₂₉₁ 258 beam generates wakes strong enough to sweep some of₂₉₂ 259 the injected particles into the vacuum chamber. This is₂₉₃ 260 described in more detail in Sec. VI. When taking short₂₉₄ 261 range wakes into account, it is found that a smaller per-295 262 turbation to the stored beam improves the overall in-296 263 jection efficiency, even though the injected bunch has a₂₉₇ 264 larger initial offset and suffers slightly larger losses ini-298 265 tially. 299 266

Mode B brings the injected beam closer to the septum³⁰⁰ as it enters from the BTA thus requiring a weaker main injection kick and allowing for a smaller stored beam transient at the expense of slightly reduced injection ef-³⁰¹ ficiency. The injected beam losses to the machine accep-³⁰²

tance increase from 0.30% to 1.77%, while the losses due

to wake fields decrease from 16.4% to 6.8%. BTA-side₃₀₃ septum sheet losses also increase slightly from 0.80% to₃₀₄ 1.05%.

Mode C has the same kicker settings as Mode B but₃₀₆ 276 decreases β_x to better fit the injected beam into the AR₃₀₇ 277 acceptance available after taking the septum sheet into₃₀₈ 278 account, similar to the technique applied in [4]. This dif-309 279 fers from Modes A and B where the beam distributions₃₁₀ 280 are matched to the ring. Reducing β_x shrinks the in-311 281 jected beam horizontally, reducing losses along the sep-312 282 tum sheet. After adjusting the septum strength to re-313 283 center the injected beam within the available machine $_{314}$ 284 acceptance, the centroid is brought closer to the septum,³¹⁵ 285 thereby reducing the injection transient. BTA-side sep-316 286 tum sheet losses are reduced to 0.13%, and losses to the₃₁₇ 287 acceptance are reduced to 1.30%. 318 288

 $_{289}$ Fig. 5 shows the DA of the latter three modes viewed₃₁₉

from the septum exit during an injection cycle, along with the injected and stored particle distributions, and also the thin septum. Both the inward and outward profiles of the thin septum in this figure were determined by particle tracking. Comparing Mode B to Mode A, the acceptance appears to move since the acceptance itself relative to the septum is affected by the choice of main injection kick.

In producing the nominal operational mode and its two variants, we conclude that the 3DK scheme has the flexibility to accommodate perturbations and offers various optimization opportunities.

IV. BTA LAYOUT DESIGN AND OPTICS MATCHING

Transport from the booster to the AR is through the Booster-to-Accumulator (BTA) transfer line. The BTA utilizes about 2/3 of the existing booster-to-ALS storage ring (BTS) transfer line. For early commissioning a slow bending switch will be installed for on-demand steering of the beam into the new BTA branch while ALS can continue normal operation.

To accommodate the different elevation between booster and AR (see Fig. 1), the BTA includes a vertical two-bend achromatic dogleg [5], where the achromatic condition is met with two quadrupoles between the two dogleg bends to generate the required vertical π phase advance. The BTA terminates into a pair of pulsed thin and thick septa providing a combined 12 deg (horizontal) bending. Since the space is limited, thick and thin septa are located at the far end of the injection straight (straight 1) as shown in Fig. 3 to increase the distance from the last bend of the BTA to the septa and lower
the incoming angle into the septa, therefore reducing the
required kick angles from septa.

The main design difficulty posed by the BTA is the 323 avoidance of interference between the BTA and other sys-324 tems' components in the tight and congested injection 325 region while meeting the layout and lattice functions' 326 matching boundary conditions. Linear-optics matching 327 was performed with constraints on beam sizes along the 328 transfer line to minimize vacuum chamber and mag-329 nets' aperture. The decoupling of horizontal and ver-330



FIG. 5. Injected and stored beam profiles out to 3σ at septum³⁵⁰ exit during an injection cycle for the three injection modes.³⁵¹ The white region is the acceptance in x-x' space at the sep-³⁵² tum exit. The septum is drawn in black and is 1 mm thick³⁵³ with its inward edge 8 mm from the stored beam reference³⁵⁴ trajectory. The septum drawing was obtained by tracking.³⁵⁵ The parameters of the three modes are detailed in Table II. ³⁵⁶



FIG. 6. Twiss functions (a) and layout (b) of the BTA transfer line.

tical planes provided by the dogleg simplifies the match-331 ing problem but we found it useful to deploy a Multi-332 Objective Genetic Algorithm (MOGA) [6] to optimize 333 the design. The optics functions and beam-size envelopes 334 of the baseline lattice are shown in Fig. 6. The desired 335 Twiss functions at the end of the transfer line are ob-336 337 tained and the beam sizes are below 4 mm throughout, which satisfies the design requirements. 338

V. INJECTION EFFICIENCY ANALYSIS AND ROBUSTNESS AGAINST LATTICE ERRORS

The injection efficiency is evaluated using AR and BTA lattices obtained after undergoing a process of simulated commissioning [7].

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Optimizing the injection efficiency in the presence of errors requires small adjustments to the nominal kick angles, with the exact value depending on the error realization. In simulations and eventually in operation, the optimization can be accomplished by running parameter scans in a neighborhood of the kick-angle nominal settings.

While one would have the freedom to adjust all three DKs independently, in the simulations we used a simplified setup in which both pre-DKs are varied by the same amount, thus resulting in a 2D optimization problem. We found that this setup gave satisfying results while significantly reducing the computation time compared to a full

TABLE III. Imperfections assigned to injection elements in the commissioning simulations. The error distributions are Gaussian and truncated at 2σ . The stability errors are relative to the set point, while the roll error is absolute.

Error Type	Distribution Width
Septum stability	$2.5 \cdot 10^{-4}$
Dipole kicker stability	$1 \cdot 10^{-3}$
Dipole kicker roll	$4\mathrm{mrad}$

³⁵⁷ 3-parameter scan.



FIG. 7. Top: particle losses in the injected (left) and stored³⁸⁸ (center and right) beam vs. kickers' angles for the ideal lat-³⁸⁹ tice. The pre-kickers' kick (vertical axis) is reported relative₃₉₀ to Mode A settings (red lines). Bottom: for each one of 100₃₉₁ lattice-error realizations, a DK scan is carried out on a grid₃₉₂ to identify the setting yielding the highest injection efficiency.³⁹³ The ensemble of the best DK settings is reported in the right figure. The left figure is the injection efficiency cumulative density function (CDF).³⁹⁶

In a preliminary study we took a first cut at the pa $^{397}_{398}$ rameter space by delimiting the region that exhibits no $^{399}_{390}$ or minimal losses in both injected and stored beam in $^{400}_{401}$ the absence of errors: see the top images in Fig. 7. In $^{401}_{401}$ the simulations the injected and stored bunches are represented with 1000 particles and tracked for 1000 turns.

When errors are added to the lattice, the best combi-364 nation of kicker settings may vary slightly depending on⁴⁰² 365 the specific random error realization and correction. For⁴⁰³ 366 each of 100 random lattice-error realizations, the kicker 367 settings are scanned in the vicinity of their nominal, ideal⁴⁰⁴ 368 values. For each error realization, the kickers' settings⁴⁰⁵ 369 that induce no stored-beam particle losses were selected⁴⁰⁶ 370 and among these the one kickers' setting that gives the407 371 highest injection efficiency was identified. The set of⁴⁰⁸ 372 those best 100 settings (one per lattice) is shown in the409 373 bottom-right image of Fig. 7 (only 15 distinct data points⁴¹⁰ 374 appear, as a single kickers' setting will in general repre-411 375 sent the optimum for several lattice-error realizations.)₄₁₂ 376



FIG. 8. Temporal and spatial profiles of the thin-septum leakage field as included in the injection efficiency studies. The left plot shows the integrated kick at various horizontal coordinates as a function of turns. Conversely, the right plot shows the integrated kick at various times as a function of a particle horizontal coordinate.

The bottom-left picture in Fig. 7 is the cumulative density function (CDF) of this set, showing that about half of the lattices have injection efficiency larger than 98.5%.

We then proceeded by refining the simulations to include a more complete set of errors and perturbations. Specifically, to the AR lattice errors we added: septa and kickers shot-to-shot variations (Table III), nonuniformity of the kicker-pulse temporal profile, and septum leakage fields.

The non-uniformity of the kicker pulse is simulated by assigning a linear slope to the pulse profile. The slope is defined as the difference between the kicks on the first and last bunch of the bunch train relative to the nominal kick. The simulation of the leakage fields is done by calculating the kick map associated with the field accounting for both the temporal and spatial field extension, to be applied at every turn before the field has died off, Fig. 8. A result from these more complete simulations is shown in Fig. 9 demonstrating the sensitivity of injection efficiency to the sloping of the kickers' pulse. As before, for each lattice-error realization, the injection efficiency was determined after performing a 2D scan of the kicker's amplitude to identify the optimum. Among other things, from these results we concluded that a 4% slope would be acceptable.

VI. SINGLE BUNCH (SHORT-RANGE WAKE FIELDS)

During injection both the electrons from the booster and the stored bunch onto which they are added undergo several millimeter transverse oscillations and this has the potential to induce potentially harmful transverse collective effects. The investigation of these effects is the topic of this section. These investigations were conducted using the **Elegant** accelerator code[8].

The short-range transverse wake fields have been calculated for each vacuum chamber element using a de-



FIG. 9. Sensitivity of the injection efficiency to the nonuniformity of the injection kickers' pulse profile. The three data sets correspond to a 0%, 4%, and 10% sloping of the pulse profile. The simulation is conducted with a complete set of errors including shot-to-shot variation of the kick and septa strengths, as well as septum leakage fields.

tailed model of its geometry. Longitudinal wakes are not 413 included in these results, however only the horizontal 414 wakes have been observed to have a significant impact 415 on the injection process. The wakes are applied close 416 to the location of the impedance, although simulations 417 are in good agreement with simpler calculations that use 418 beta-function weighting to group together the impact of 419 wake fields in every sector or even at a single location 420 in the ring. The threshold for the Transverse Mode-421 Coupling Instability (TMCI) is 5.8 nC, about 8 times 422 the nominal charge for a single bunch. Fig. 10 shows the 423 beta-weighted wakefields from different components in 424 both horizontal and vertical planes, along with their to-425 tal. Wake fields are calculated for a Gaussian beam with 426 rms bunch length of 1 mm, and serve as pseudo-Green 427 functions in the following beam dynamics simulations. 428

The resulting transverse oscillations, especially of the 429 stored bunch (because it contains about 90% of the 430 charge), induce short-range wake fields. Despite the fact 431 that the total bunch charge is expected to be far from the 432 threshold for instabilities driven by short-range wakes,451 433 the wake fields do build up in intensity over a time $\operatorname{scale}_{_{452}}$ 434 of order 1 ms (roughly 1600 passes around the ring). $\operatorname{Sim}_{_{453}}$ 435 ulations show that the wake fields are strong enough $\mathrm{to}_{_{454}}$ 436 confine the stored bunch and delay phase decoherence, $_{\scriptscriptstyle 455}$ 437 as shown in Fig. 11. At the same time, the more $\operatorname{diffuse}_{_{456}}$ 438 injected electrons increase in both oscillation $\operatorname{amplitude}_{_{457}}$ 439 and transverse width. 440 458

The 3DK 'balanced' configuration (Mode A) was cho-459 441 sen by optimizing for injection efficiency, but without $_{460}$ 442 considering the impact of wakes. Less than 1% beam₄₅₁ 443 losses are predicted in this case. However, when the ex_{-462} 444 pected wake fields are included, the injection $\operatorname{efficiency}_{\scriptscriptstyle 463}$ 445 drops to 83.6%. As shown in Fig. 12, most of the losses₄₆₄ 446 occur between 0.5 ms and 1 ms after injection, roughly₄₆₅ 447 between 1000 and 2000 passes around the ring. 448 466

An important aspect of the 3DK scheme is that it is₄₆₇ flexible enough to allow for additional adjustments to₄₆₈



FIG. 10. Transverse short-range wakefields in the AR from individual components and their combined total. The wake potentials are calculated for a Gaussian beam with rms bunch length of 1 mm and serve as pseudo-Green functions in beam dynamics simulations. Left: horizontal plane, right: vertical plane

accommodate the impact of wake fields. An alternate set of all three kicker magnet amplitudes, referred to as 'Mode B', was found that reduced the displacement of the trajectory of the stored beam by 20%, while increasing losses by a modest amount when wake fields are neglected. These additional losses occur in the first 50 passes around the ring. The capture efficiency remains above 99%. For the nominal wake fields the capture efficiency is 93.2%, a significant improvement compared to 83.6% for Mode A. In none of these cases are there losses in the stored bunch.

Mode C is similar to Mode B except that the septum field is weaker and the horizontal beta function at the end of the septum is lower than the matched value so as to reduce transfer-line losses on the injection septum. These adjustments also reduce the injected beam transient slightly, though when wake fields are taken into account the capture efficiency is comparable to that of





FIG. 11. Horizontal phase space of the stored (orange) and injected (blue) bunches after 2000 turns, without wakes (above) and with nominal wakes (below). The left figures show the results for Mode A, the right for Mode C.

⁴⁶⁹ Mode B. The performance of Modes B and C are much
⁴⁷⁰ more similar to each other than they are to Mode A, and
⁴⁷¹ comparisons will focus on the differences between Mode
⁴⁷² A and Mode C.

Figure 12 shows the evolution of the size and horizontal 473 offset of the injected bunch when short-range wake fields 474 are either included or ignored. Results for Mode A are 475 shown on the left-side plots, and for Mode C on the right- $^{\rm 504}$ 476 side plots. In Mode A, the width of the injected bunch⁵⁰⁵ 477 steadily decays without wake fields, while with the nom-506 478 inal wakes the width of the bunch grows until it peaks⁵⁰⁷ 479 after 1800 turns around the ring with an rms of 3.5 mm,⁵⁰⁸ 480 up from 2.2 mm. The centroid motion rapidly damps⁵⁰⁹ 481 from 1.5 mm without wakes, but with the nominal wakes⁵¹⁰ 482 it increases to 3.5 mm amplitude, followed by envelope 483 oscillations which slowly decay over thousands of passes⁵¹¹ 484 around the ring. For Mode C, there is similar behavior in₅₁₂ 485 the width of the injected bunch but the amplitude of thesis 486 centroid motion starts out at 2 mm and only grows to₅₁₄ 487 3.0 mm. The centroid motion again has continued enve-515 488 lope oscillations in the presence of wakes, but at a lower⁵¹⁶ 489 amplitude than for Mode A. 490 517

For the nominal wake fields, the goal of at least 95%⁵¹⁸ 491 injrection efficiency is not met even for Mode C. Thus, 519 492 other strategies to mitigate the impact of short-range₅₂₀ 493 wake fields have been examined. The nominal chromatic-521 494 ity of 1 in both planes can easily be increased and will₅₂₂ 495 drive more rapid phase decoherence of the bunches. Both₅₂₃ 496 horizontal and vertical chromaticities contribute to this524 497 effect at high amplitudes. A small temporal offset of the525 498 injected bunch relative to the stored bunch directly re-526 499 duces the wake field forces experienced by the injected₅₂₇ 500 electrons, as the injected particles experience the peak₅₂₈ 501 of the wake field for only brief periods during their syn-529 502



FIG. 12. Comparison of the evolution of the size (top) and centroid motion (bottom) of the injection bunch for the cases without wake fields (red) and with nominal wake fields (green). The left figures show results for the 3DK settings referred to as Mode A ('balanced'), and right figures show Mode C, which is tuned for better performance in the presence of wake fields. The corresponding injection efficiencies for the two cases are 83.6% and 93.1%.

chrotron oscillations.

Increasing the chromaticity from 1 to 1.2 increases the capture efficiency to 93.5% for Mode A and 97.7% for Mode C. Similarly, keeping the chromaticity at unity and delaying the injected bunch by 100 ps relative to the stored bunch leads to an capture efficiency of 98.5% for Mode A nd 98.9% for Mode C. Applying both changes brings the capture efficiency above 99% in both modes.

To exercise a measure of caution, we considered the possibility that wake fields would be twice as high as expected ("enhanced wakes") In this case, the capture efficiency drops to 64.8% for Mode A and 78.3% for Mode C without additional mitigations. The evolution of the capture efficiency as a function of number of passes after injection is shown in Fig. 13 for both Mode A and Mode C. The wake field levels are varied among no wakes, nominal wakes and enhanced wakes. In addition, some examples include using a combined mitigation of setting both chromaticities to 1.2 and shifting the injected bunch by 100 ps. For the enhanced wakes, this brings the capture efficiency to 97.8% for Mode A and 98.3% for Mode C. Creating a temporal offset between the stored and injected bunches is particularly effective at reducing the impact of wake fields. For Mode C with the above mitigations, the capture efficiency is 97.2% when the strength of the wake fields is multiplied by a factor of three. The corresponding efficiency for Mode A is 95.9%.



FIG. 13. Capture efficiency as a function of number of passes⁷⁴ around the ring after injection, comparing Mode A, where⁵⁷⁵ the kicker settings are optimized without including wake field effects, to Mode C, which uses an alternative set of kicker strengths which is more tolerant to wake fields and also changes the injection beta function. Results are shown with and without wake fields, for enhanced wake fields, and for⁵⁷⁶ additional mitigations.

VII. MULTI-BUNCH STABILITY AND INTERFERENCE WITH TFB SYSTEM

The transverse bunch-by-bunch feedback system₅₈₃ 532 (TFB) will detect the transient of the stored beam and₅₈₄ 533 apply kicks to damp it. Unfortunately, those kicks will₅₈₅ 534 anti-damp the injected particles since the stored beam₅₈₆ 535 and injected particles are out of phase. The injected₅₈₇ 536 particles carry relatively little charge and will offset only 537 slightly the center-of-charge that the feedback system de-538 tects. To prevent the loss of injected particles as the TFB 539 damps the injection transient, the TFB will be masked 540 for those buckets into which charge is injected. A sin-541 gle injection shot delivers charge into 4 buckets, spaced 542 4 buckets apart, for example, buckets 10, 14, 18, and 22. 543 Masking the buckets significantly diminishes the ability 544 of the TFB to damp multibunch instabilities and so we 545 investigate here the injection transient and TFB interac-546 tion using a tracking simulation. 547

Under nominal conditions, the growth rates of multi-588 548 bunch impedance instabilities in the AR are less than₅₈₉ 549 that of the radiation damping and multibunch feedback₅₉₀ 550 system. The accumulator ring HOM wakes have been₅₉₁ 551 evaluated with theory and tracking simulations. The₅₉₂ 552 strongest cavity HOM growth rate is 0.03 ms^{-1} , and the₅₉₃ 553 radiation damping rate is 0.16 ms^{-1} . The growth rates₅₉₄ 554 of the resistive wall modes are shown in Fig. 14. Except₅₉₅ 555 for the two highest order modes, all are below the ra-596 556 diation damping time, and the highest order modes are₅₉₇ 557 well-within the capabilities of the TFB. 558

Following an injection cycle the stored beam is left with a large transverse offset and the 4 buckets into which charge is injected are masked from the multi-bunch feed-602

back. Since the resistive wall modes are near or exceed the radiation damping rate, a tracking simulation is used to evaluate their stability during the injection transient when the effectiveness of the TFB is diminished.

The simulation models the long-range resistive wall wakes at any position in the ring using a fit of 15 pseudomodes to the $1/\sqrt{t}$ dependence of the long-range wake fields and follows closely the technique described in [9]. The long-range resistive wall wake is,

$$W(t) = \frac{\sqrt{c}}{\pi b^3} \sqrt{\frac{Z_0}{\pi \sigma}} \frac{L}{\sqrt{t}},\tag{1}$$

where b is the chamber dimension and σ its conductivity; c and Z_0 are the speed of light and impedance of free space; L is the length of the chamber and t is time since the passage of the source particle[10]. The basis of pseudo-modes is

$$W_i(t) = \frac{A_i^2}{S_i^2} \exp\left(-\frac{d_i^2}{S_i^2}t\right),\tag{2}$$

where A_i , S_i , and d_i are fit parameters. Here, S_i is redundant but including it as a fit parameter has been found to help the fitter converge consistently and quickly with simply default parameters. The fitter is Mathematica's NonlinearModelFit [11]. The log of the basis is fit to $\log(1/\sqrt{t})$ sampled with a logarithmic distribution of t. The residuals of the fit are less than 0.1% from 1 ns to 44,000 turns, and reliably decay to zero beyond the ends of the fit. The same basis is used for all chambers, but is scaled according to the local chamber material and dimension shown in Eq. (1). Resistive wall wakes are represented at 216 locations in the ring.

For each horizontal mode n, each bunch i in the train is seeded with an appropriate offset,

$$x_i = \sqrt{J\beta_x} \cos\left(\frac{\pi}{2} + \frac{2\pi ni}{N_{bunches}}\right) \tag{3}$$

$$x'_{i} = \sqrt{\frac{J}{\beta_{x}}} \left(\alpha_{x} \cos\left(\frac{\pi}{2} + \frac{2\pi ni}{N_{bunches}}\right) + \sin\left(\frac{\pi}{2} + \frac{2\pi ni}{N_{bunches}}\right) \right). \tag{4}$$

and tracked for 5000 turns.

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The multi-bunch tracking simulation is developed using Bmad [2], which keeps track of the pseudo-modes as they build up and influence the beam turn-by-turn. Radiation damping is implemented by a per-turn decrement to the action of each macro-particle. The multibunch feedback is simulated using a pickup, FIR filter, and kicker.

Each turn the normal mode coordinates of each bunch are recorded and a Fourier transform is taken along the bunch train. For the seeded mode, the growth rate is obtained from the fit of an exponential to the the height of the spectral peak versus turn number. This is done similarly for the vertical modes. The growth rates of each of the 25 modes are shown in Fig. 14. From Fig. 14 we



FIG. 14. Per-mode growth rates of a 25 bunch train in the⁶⁴⁴ accumulator ring determined by multi-bunch macro-particle⁶⁴⁵ tracking with resistive wall wake fields. During steady-state,⁶⁴⁶ all RW modes are safely damped with a total growth rate of⁶⁴⁷ about -2.5 ms^{-1} . During the injection transient the effective-⁶⁴⁸ ness of the TFB is significantly diminished by the necessity of⁶⁴⁹ masking the 4 buckets into which charge is injected, thougheso all modes remain damped.

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conclude that while masking will significantly reduce the
 damping obtained from the multibunch feedback system,
 all resistive wall modes will remain stable by comfortable
 margin during the transient.

Following an injection cycle, the bunch train is offset₆₅₉ 607 with a large uniform transient. However, the study just₆₆₀ 608 described used small amplitudes and particular offsets661 609 given by Eqs. (3) and (4). To simulate absolute stability₆₆₂ 610 following an injection cycle, the beam is given a uniform663 611 5 mm horizontal offset and tracked for 5000 turns. With-664 612 out masking, after 1702 turns the bunch oscillating with665 613 the largest amplitude has an action that is 50% of the ini-666 614 tial condition. With 4 bunches masked, 50% is achieved₆₆₇ 615 after 3266 turns. All 15 RW pseudo-modes are reliably⁶⁶⁸ 616 decaying in strength throughout the simulation. 669 617

VIII. CONCLUSION

The three-dipole kicker injection scheme is well-fit to the particular constraints and allowances of the ALS-U accumulator ring. It reliably injects the relatively large beam coming out of the booster with nearly 100% efficiency using conventional technology. It meets the accumulator ring's tight space constraints by distributing the injection kickers across multiple straights. It fits the large beam coming in from the booster into the relatively small vacuum chamber by allowing a transient on the stored beam so as to shrink the transient of the injected beam.

The injection transient has consequences for long- and short-range wake fields, but several techniques have been prepared to effectively mitigate these consequences. The scheme is robust in the presence of lattice and pulsed element imperfections. Both the wake field issues and imperfection tolerances benefit from the ability of the scheme to tune the amplitudes of the stored and injected transients.

In the appendix, the merits of three alternative injection schemes are compared to those of the 3DK scheme.

Appendix A: Alternate Injection Options

1. Nonlinear Kicker

Unlike conventional dipole-kicker magnets, a nonlinear kicker (NLK) generates a transverse nonlinear magnetic-field profile with a maximum located off-axis at the injected-beam arrival point and zero in the center. The injected beam is kicked while the stored beam at the center is minimally perturbed. In addition, a single NLK device is sufficient for injection, thus easing issues of space and synchronization. Because of these reasons, several light source facilities have adopted NLK in alternative to more conventional closed-orbit bump schemes [12–15].

Although injection perturbations to the stored beam are not a major concern in the AR (the stored beam does not serve user experiments), NLK injection represents an attractive option because of its compactness and simplicity, while a relaxed tolerance to stored-beam perturbation can be exploited to optimize the design in ways that are not suitable for light-source applications.

The NLK design configuration we considered consisted of 8 main conductors symmetrically positioned around the vacuum chamber in the direction of the beam as shown in Fig. 15. The NLK was located in the same lattice position as the main kicker in the 3DK scheme. The conductor placement was optimized using MOGA methods [6] in start-to-end macroparticle injection simulations; for a detailed description of the optimization setup and results see Ref. [16]. With an optimized NLK design, injection tracking studies in the presence of lattice errors and including orbit/optics correction showed injection efficiency above 95% (not including transverse⁶⁹⁴
 wakefield effects).

While these simulations were encouraging, an NLK-696 solution for the AR injection was eventually abandoned after the R&D effort initiated at ALS [16] encountered technical difficulty with the prototyping of the ceramic vacuum-chamber.

Conventional closed orbit bump 4DK injection 703 in one sector 704

The existing ALS utilizes a conventional 4-kicker orbit-706 679 bump injection scheme with all four kickers in the same⁷⁰⁷ 680 straight section. A similar scheme was explored for the⁷⁰⁸ 681 AR with all 4 injection kickers placed in Sector 2. Poten-⁷⁰⁹ 682 tial advantages of this scheme are: 1) it is conventional,⁷¹⁰ 683 2) residual oscillations of the stored beam following the⁷¹¹ 684 injection cycle are eliminated, 3) it eliminates the need⁷¹² 685 to carefully control the phase advance between the pre-713 686 kicker and main injection kicker. 714 687

The straights in the AR are 0.624 m shorter than those⁷¹⁵ in the ALS. This shorter space drives up the strength re-⁷¹⁶ quired from the dipole kickers. Additionally, because the⁷¹⁷ orbit bump is closed for the stored beam, the injected particles oscillate with larger amplitude. To avoid loss of

⁶⁹³ injected particles, the injection septum aperture would⁷¹⁸



FIG. 15. NLK-design concept. Top: main conductors' transverse positions (the return conductors are not shown). Bot-tom: magnetic-field profile in the mid plane.

need to be increased to the nominal vacuum chamber aperture of about 14 mm. This complicates engineering in the injection straight and further increases the necessary dipole kick to about 10 mrad. Such a large dipole kick requires some combination of kicker R&D, a multi-turn ramp, or placing the 4 kickers on a single power supply string. A multi-turn ramp would constrain the machine tune, thus negating one potential advantage of this scheme. Placing the 4 kickers on a single string would make it difficult to trade off between stored beam and injected beam oscillation amplitudes, which is a disadvantage compared to the 3DK scheme. An additional drawback is that the septa would need to be moved upstream (toward the center of the straight) to make room for the 4 kickers. This has the consequence of forcing a stronger bending requirement in the thick septum.

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Even with a 14 mm septum aperture, a conventional 4-kicker design delivers less than 90% injection efficiency, as shown in Fig. 16. In contrast, the 3DK scheme approaches 100% injection efficiency. The 3DK scheme also compares well in requiring only an 8 mm septum aperture, and its kicker technology requirements are modest: three 0.6 m long ferrite-loaded dipole kickers delivering ~ 1 mrad kick.

3. Two dipole kicker (2DK)

It is possible to implement an injection scheme simi-719 lar to 3DK while using only two dipole kickers. Coined 720 "2DK" this scheme saves costs by requiring one less 721 kicker. With 3DK, the two pre-kickers allow adjustment 722 of the position and angle of the stored beam at the main 723 injection kicker. With 2DK, only one pre-kicker is em-724 ployed and its location in the storage ring is chosen to 725 726 have a horizontal phase advance from the pre-kicker to 727 the main injection kicker such that the stored beam has a near-zero crossing at the main injection kicker. The pre-728 kicker is placed in sector 7, which is six sectors upstream 729 of the main injection kicker. 730

⁷³¹ 2DK is competitive as far as injection efficiency goes,
⁷³² but the lack of flexibility limits the ability to accommodate difficult-to-predict consequences of imperfections
⁷³⁴ and wake fields. It also constrains the ring tune, as the



FIG. 16. Injection efficiency for the conventional 4DK scheme evaluated over a population of 100 lattice-error realizations including orbit and optics corrections. Results are for the septum positioned at 8 mm (left) and 13 mm (right) from the vacuum chamber center. Tracking simulations were done with 10k particles over 10k machine turns.

 $_{735}$ pre-kicker to main injection kicker phase advance must $_{737}$ $_{736}$ be precisely set. Generally, the phase advance along a_{738}

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single straight is too little to allow for significant adjustment. It was judged that the versatility of the 3DK scheme justified the cost.

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