

Lawrence Berkeley National Laboratory

LBL Publications

Title

Ordering and Decomposition in the High-Temperature Superconducting Compound
YBa₂Cu₃O_{7-x}

Permalink

<https://escholarship.org/uc/item/9rq2f3z7>

Authors

Khachatryan, A G
Morris, J W, Jr

Publication Date

1987-07-01

Copyright Information

This work is made available under the terms of a Creative Commons Attribution License,
available at <https://creativecommons.org/licenses/by/4.0/>

Center for Advanced Materials

CAM

Submitted to Physical Review Letters

Ordering and Decomposition in the High-Temperature Superconducting Compound $\text{YBa}_2\text{Cu}_3\text{O}_x$

A.G. Khachaturyan and J.W. Morris, Jr.

July 1987

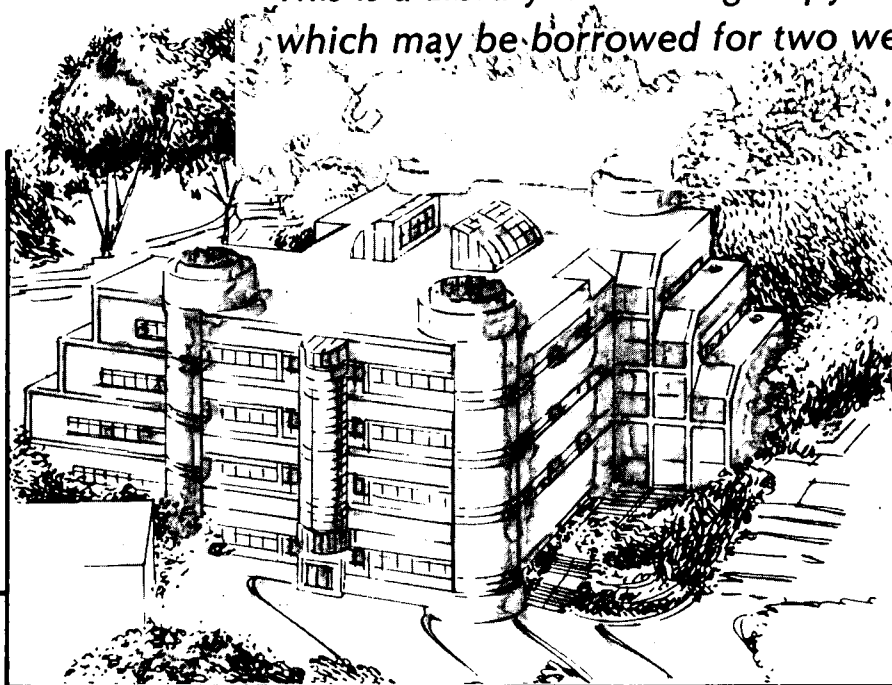
RECEIVED
LAWRENCE
BERKELEY LABORATORY

FEB 1 1988

LIBRARY AND
DOCUMENTS SECTION

TWO-WEEK LOAN COPY

*This is a Library Circulating Copy
which may be borrowed for two weeks.*



Materials and Chemical Sciences Division

Lawrence Berkeley Laboratory • University of California

ONE CYCLOTRON ROAD, BERKELEY, CA 94720 • (415) 486-4755

LBL-23791 Rev. c.2

DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.

**Ordering and Decomposition in the High-Temperature
Superconducting Compound $\text{YBa}_2\text{Cu}_3\text{O}_x$**

A. G. Khachaturyan and J. W. Morris, Jr.

Center for Advanced Materials
Materials and Chemical Sciences Division
Lawrence Berkeley Laboratory
University of California

and

Department of Materials Science and Mineral Engineering
University of California, Berkeley
Berkeley, California 97420

July 1987

This work is supported by the Director, Office of Energy Research, Office of Basic Energy
Science, Material Sciences Division of the U. S. Department of Energy under Control
No. DE-AC03-76SF00098

Ordering and Decomposition in the High-Temperature Superconducting Compound $\text{YBa}_2\text{Cu}_3\text{O}_x$

A. G. Khachaturyan and J. W. Morris, Jr.

Center for Advanced Materials, Lawrence Berkeley Laboratory
and
Department of Materials Science and Mineral Engineering
University of California, Berkeley

Abstract

The method of concentration waves is applied to structural transformations in superconducting Y-Ba-Cu oxide. The method predicts an ordering reaction that results in a tetragonal-to-orthorhombic phase transformation, and also yields the correct structure of the $\text{YBa}_2\text{Cu}_3\text{O}_7$ orthorhombic ordered phase. The results suggest that at low temperature the off-stoichiometric orthorhombic phase is thermodynamically unstable with respect to secondary decomposition into a mixture of ordered orthorhombic and disordered tetragonal phases, whose microstructure can be anticipated.

The structure of the high- T_c Y-Ba-Cu-O superconducting oxide has recently been determined by neutron diffraction [1,2] and is shown in an idealized form in Figure 1. The results imply a stoichiometric composition: $\text{YBa}_2\text{Cu}_3\text{O}_7$. While the source of the high superconducting critical temperature is not fully understood, it is apparently associated with the ordering of the oxygen atoms in the basal plane of the unit cell into alternate rows of filled and empty oxygen sites. The asymmetric distribution of oxygen in the basal plane causes an orthorhombic distortion of the structure that is observed at low temperature. The structure transforms reversibly from tetragonal to orthorhombic symmetry at about 750°C [3,4,5].

Despite the significant research effort that has recently been devoted to the study of the superconducting oxide, important aspects of its structural and microstructural behavior remain unclear. This is due in part to the difficulty of determining the composition and distribution of the oxygen constituent, whose concentration varies from six to seven atoms per unit cell. It is the purpose of this note to identify some of the probable structural properties of the superconducting oxides from known theory that treats the behavior of similar systems. The results interpret the order and orthorhombic character of the oxide, suggest that off-stoichiometric oxides will likely decompose into similar, but distinct oxides of different oxygen stoichiometry at low temperature, and point out the probable microstructures of the low-temperature state, which may have important consequences for its superconducting properties.

Recently one of us has shown that the structures of most of the common oxide phases can be understood and predicted by applying the method of concentration waves [6,7]. In this approach the oxide is treated as an interstitial compound that forms through the ordering of atoms and vacancies on the lattice and interstitial sites of a host lattice of simple symmetry. As we shall describe in detail elsewhere, the same approach can be used to generate the observed structure of YBa₂Cu₃O₇. The perovskite structure on which it is based can be obtained from an fcc lattice by placing a mixture of Cu atoms and vacancies on the fcc lattice sites and a disordered mixture of Y, Ba and O in the octahedral interstices. As discussed in reference [7], the perovskite structure results when both lattices are ordered by the star of the vector $\mathbf{k}_1 = [2\pi/a](100)$, where a is the lattice parameter of the parent fcc cell. A structure like that of YBa₂Cu₃O _{x} is achieved by a layer secondary ordering governed by the wavevector $\mathbf{k}_2 = [2\pi/a](00\frac{1}{3})$, which is one of the preferred secondary ordering vectors identified in [7]. The stoichiometric formula of the resulting ordered phase is YBa₂Cu₃O₆ (Figure 1a). In this phase all basal plane oxygen sites are vacant; by symmetry, the unit cell should be tetragonal. It has been found experimentally [3,5], and is referred to as the T-phase in the following.

1. The Ordered Structure of $YBa_2Cu_3O_7$

The orthorhombic $YBa_2Cu_3O_7$ phase (the O-phase) is derived from the T-phase by placing oxygen atoms in vacant sites on the basal plane. These sites form a base-centered tetragonal Bravais lattice, which we shall call the "basal sublattice". Since the oxygen content is not sufficient to fill the sites of the basal sublattice, the Nernst principle requires that at sufficiently low temperature the oxide is at least metastable with respect to tertiary ordering or decomposition into stoichiometric structures. It has been shown [7] that, with a single known exception (the Magneli phases), the stable superstructures that arise from an ordering of this type are generated by concentration waves belonging to one star. This condition restricts the possible ordering vectors that can generate superstructures. The appropriate set for the base-centered tetragonal basal sublattice of the oxide can be shown to have the form $\mathbf{k}_3 = (2\pi/a)(HKL)$, where

$$(HKL) = \{10L\}, \left\{\frac{1}{2}\frac{1}{2}L\right\}, \left\{\frac{1}{2}0L\right\}, \left\{\frac{2}{3}0L\right\}, \left\{\frac{1}{3}\frac{1}{3}L\right\}, \left\{\frac{1}{4}\frac{1}{4}L\right\} \quad (1)$$

and $L=0, \frac{1}{6}$ or $\frac{1}{12}$ and the indices relate to the parent cubic lattice. Assuming a two-body effective interaction between the oxygen atoms, the preferred ordering wave from the list (1) is determined by the minimum of the k-space interaction potential

$$V(\mathbf{k}) = \sum_{\mathbf{r}} W(\mathbf{r})\exp(i\mathbf{k}\mathbf{r}) \quad (2)$$

where $W(\mathbf{r})$ is the effective interaction between oxygen atoms separated by the vector \mathbf{r} , that is, the potential for rearrangement of the oxygen atoms in the presence of the three-dimensional background structure.

We cannot use this equation (2) directly since we do not know the effective 0-0 interaction in Y-Ba-Cu-O. However, the preferred ordering wave can be inferred from the nature of primary ordering in the system; the concentration wave that accomplishes the greatest reduction in the energy is, by definition, the concentration wave that generates the primary structure. Since the primary perovskite cell of Y-Ba-Cu-O is generated by the star of the wavevector $\mathbf{k}_1=(2\pi/a)(100)$, the vector $\mathbf{k}_1=(2\pi/a)(100)$ (or the degenerate vector $(2\pi/a)(010)$) should be the member of the set (1) that governs tertiary ordering. There is

only one ordered distribution that is based on this vector and satisfies the condition [8] that it has only two values on the available sites of the basal sublattice of YBa₂Cu₃O₆ (the lattice of vacant sites designated in Figure 1). The distribution function is

$$n(\mathbf{r}) = c + \eta \cos(\mathbf{k}_1 \mathbf{r}) = c + \eta \cos(2\pi x) \quad (3)$$

where $n(\mathbf{r})$ is the probability that an oxygen atom is located at the site, \mathbf{r} , of the basal sublattice, c is the fraction of basal-plane vacancies that is filled by oxygen atoms and η is the long-range order parameter. The coordinate x in the second form is either an integer or half-integer. When $c = \eta = 1/2$ equation (3) generates the YBa₂Cu₃O₇ structure shown in Figure 1b. The structure is orthorhombic and is characterized by rows of O-atoms along with [010]-directions that alternate with rows of vacant sites. (De Fontaine and Moss [9] provided an independent treatment of this ordering reaction on the basis of a two-dimensional model with second-neighbor interactions.)

An examination of the structure shown in Figure 1 shows that the ordering described by equation (3) is already present on all other planes that are perpendicular to the c -axis of the unit cell. The ordering (3) hence obeys the rule [8] that the same order wave appear on every sublattice.

The concentration wave that induces tertiary order involves the single wavevector \mathbf{k}_1 . Since $3\mathbf{k}_1$ is not a reciprocal lattice vector of the basal sublattice, the ordering reaction may be second order, as recent experimental observations seem to show [10]. The order parameter is a function of concentration and temperature, whose specific form is known for various approximate treatments of the free-energy function [7,11,12].

The orthorhombicity (Δ) of the structure is the difference in length between the lattice parameters a and b in the basal plane, and should also be a function of the long range order parameter. It can be approximated by the linear relation

$$\Delta(\eta) = a-b = \gamma\eta \quad (4)$$

where γ is an expansion coefficient, which follows via a Taylor expansion about the point $\eta=0$. The linear term in (4) does not vanish as usual since the transformation $\eta \rightarrow -\eta$

reverses the a and b axes and, hence, the sign of Δ . The coefficient, γ , can be found experimentally from the maximum value of Δ , the value in the stoichiometric O-phase. Since $\Delta_{\max} = \gamma c$, $\Delta(\eta)/\Delta_{\max} = \eta/c$.

The orthorhombic distortion that occurs on ordering strains the parent lattice unless it occurs homogeneously in a single crystal. The microstructure that minimizes the internal strain is known from the established theory of similar systems [11]. The elastic strain is accommodated by dividing the crystal into parallel plates that are (110) twin-related 90° domains. The microstructure is shown schematically in Figure 2, and should be observed in congruently ordered YBa₂Cu₃O_x at temperatures below the ordering temperature. (Evidence for this microstructure seems to be present in the atomic resolution micrographs of Van Tendeloo, et al. [5].)

2. Low-Temperature Decomposition

The tertiary ordering reaction discussed above rearranges the oxygen atoms on the basal sublattice without changing their total concentration. It follows that an off-stoichiometric oxide remains off-stoichiometric after cooling to below T_c . By the Nernst principle such an alloy cannot be stable at low temperature. If $V(0) + V(\mathbf{k}_3) < 0$, it decomposes into a mixture of T-phase of composition close to YBa₂Cu₃O₆ and O-phase of composition near YBa₂Cu₃O₇. Otherwise it undergoes one or more additional ordering reactions before decomposing. Since there is no evidence for additional ordering reactions we consider the decomposition of the O-phase. The phase diagram that governs its decomposition is drawn schematically in Figure 3. Landau [13] and Krivoglaz [12] have suggested ways of calculating the critical point (T_K , c_K) at which instability with respect to congruent ordering is changed into instability with respect to decomposition.

The microstructure induced by a decomposition reaction of this sort is well known from the behavior of similar systems [11]. After ordering, the system consists of twin-related (110) lamellae of the O-phase. Each lamella undergoes secondary decomposition. To minimize the elastic energy the precipitates of O-phase maintain the a-axis orientation of the parent lamella and are hence aligned along $\langle 110 \rangle$ directions. The result is a microstructure of the "tweed" type, drawn schematically in Figure 2. If the microstructure is permitted to coarsen then strain-induced coarsening leads to a martensite-like structure in

which colonies of (110) twin-related platelets form plates that are embedded in a matrix of T-phase. The habit of the plate is determined by the condition that the macroscopic shape change of the plate is an invariant plane strain, to eliminate the volume-dependent part of the elastic energy. The decomposition of the off-stoichiometric oxide and the characteristic microstructures that result may be observable through high resolution electron microscopy.

The decomposition reaction should have an important effect on the superconducting properties of the off-stoichiometric oxide. The decomposition has the consequence that near-stoichiometric O-phase is present in off-stoichiometric oxides, so the critical temperature and critical field should not depend strongly on the overall stoichiometry. However, the decomposition also has the consequence that the O-phase in an off-stoichiometric oxide may be intimately embedded in a matrix of T-phase, which is believed to be semiconducting. The two phase microstructure should have a profoundly deleterious effect on the critical current of off-stoichiometric material. The microstructure that results from a decomposition of this sort also interacts strongly with grain boundaries in polygranular structures, and may share responsibility for the low superconducting critical current observed in bulk polygranular material.

ACKNOWLEDGMENT

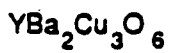
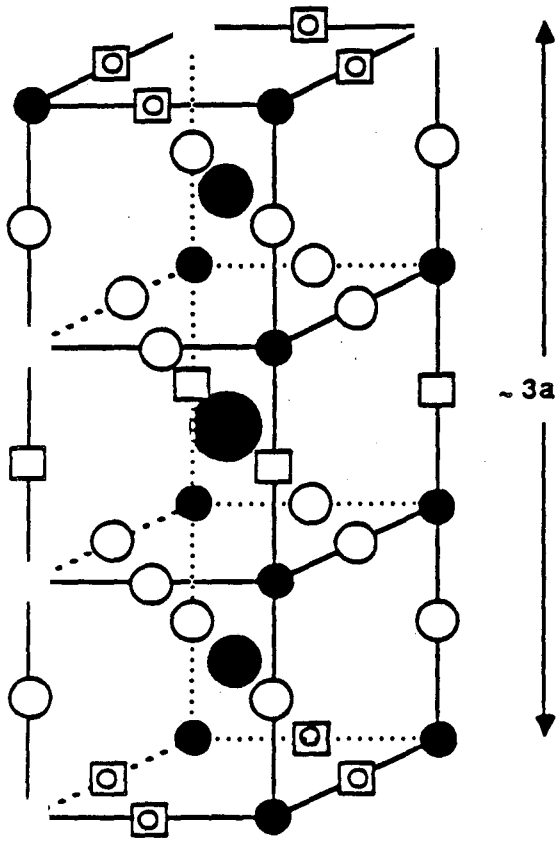
The authors are grateful to a number of researchers who have provided preprints of relevant work, including Professors S. Moss, University of Houston, D. de Fontaine, University of California, G. Van Tendeloo, University of Antwerp, and Dr. I. K. Schuller and his associates, Argonne National Laboratory. This work was supported by the Director, Office of Energy Research, Office of Basic Energy Sciences, U. S. Department of Energy, under Contract No. DE-AC03-76SF00098.

REFERENCES

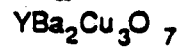
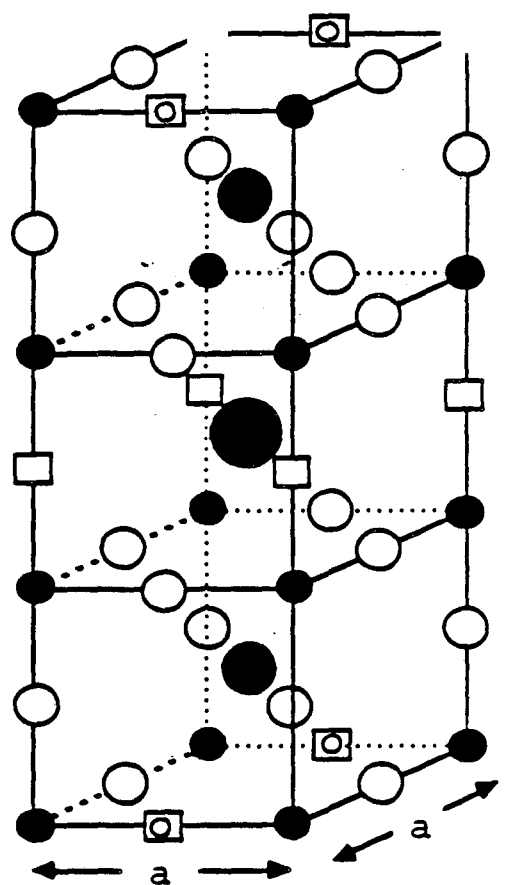
1. M. A. Beno, L. Soderholm, D. W. Capone, D. G. Hinks, J. D. Jorgenson, Y. K. Shuller, C. K. Segre, K. Zhang and J. D. Grace: *Applied Phys. Letters* (in press)
2. J. J. Capponi, C. Chaillout, A. W. Hewatt, P. Lejay, M. Marezio, N. Nguen, B. Raveau, C. L. Soubeyroux, J. L. Tholoned and R. Tourner: *Europhysics Letters* (in press).
3. I. K. Schuller, D. G. Hinks, M. A. Beno, K. W. Capone II, L. Soderholm, J. P. Locquet, Y. Bruynsenaede, C. K. Segre and K. Zhang: *Solid State Communications* (submitted)
4. A. H. Hewatt, J. J. Capponi, C. Chaillout, M. Marezio and E. A. Hewatt: *Nature* (submitted)
5. G. Van Tandeloo, H. W. Zanderbergen and S. Amelinckx: *Solid State Comm.* (in press)
6. B. I. Pokrovskii and A. G. Khachaturyan: *J. Solid State Chemistry* **61**, 137, 154 (1986)
7. A. G. Khachaturyan and B. I. Pokrovskii: in *Progress in Material Science*, J. W. Christian, P. Haasen and T. Massalski, eds., Pergamon Press, Oxford, vol. 29, pp. 1-138 (1985)
8. A. G. Khachaturyan: *Phys. Metall. and Metallography* **13**, 493 (1962), *Sov. Phys-Solid State* **5**, 16, 548 (1963), *Physics Status Solidi* **60(b)**, 9 (1973)
9. D. deFontaine and S. C. Moss (to be published)
10. J. D. Jorgensen, M. A. Beno, D. G. Hinks, L. Soderholm, K. Volin, R. L. Hitterman, J. D. Grace, I. K. Schuller, C. V. Segre, K. Zhang and M. S. Kleefisch (submitted to *Phys. Rev. Letters*)
11. A. G. Khachaturyan: *Theory of Structural Transformations in Solids*, J. Wiley and Sons, New York (1983)
12. M. A. Krivoglaz and A. A. Smirnov: *Theory of Order-Disorder in Alloys*, MacDonald, London (1969)
13. L. D. Landau: *Phys Zs. Sowjetunion*; **11**, 26 (1937)

FIGURE CAPTIONS

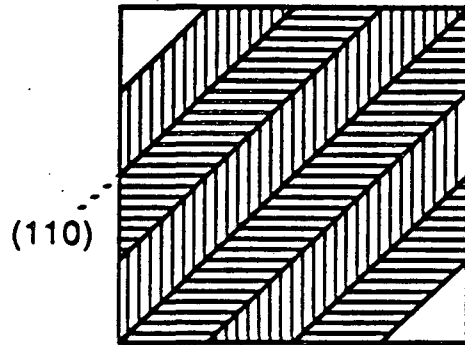
- Figure 1: a. The structure of the tetragonal parent phase. b. The structure of the orthorhombic ordered phase: ● = Cu, ● = Ba, ● = Y, ○ = O atom, □ = O atom vacancies in basal planes, □ = O-atom vacancies.
- Figure 2: Schematic picture of the expected microstructure of the two-phase state of YBa₂Cu₃O_x: (a) the (110) twin structure of the off-stoichiometric O-phase formed due to congruent ordering at the first stage of decomposition; (b) the "tweed-like" <110> aligned structure; and (c) the morphology of colonies of twin-related (110) lamella.
- Figure 3: Schematic drawing of the equilibrium diagram: O = ordered orthorhombic phase field; T = disordered tetragonal phase field. The dotted line designates the secondary spinodal curve for decomposition of the off-stoichiometric O-phase. K = critical point.



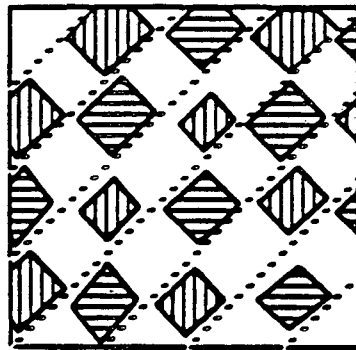
(a)



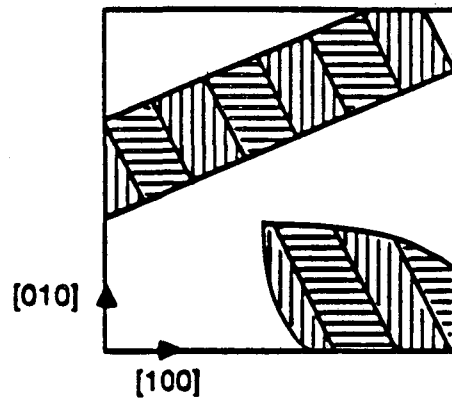
(b)



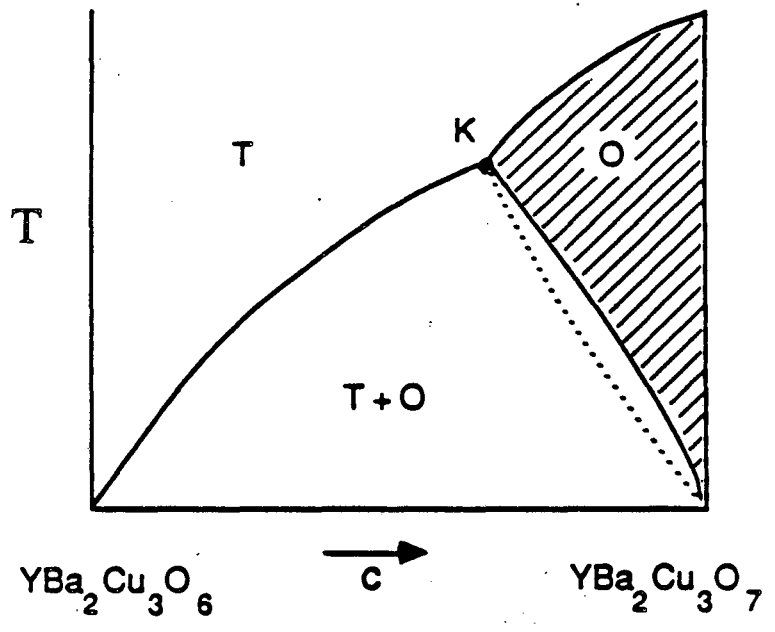
a



b



c



*LAWRENCE BERKELEY LABORATORY
TECHNICAL INFORMATION DEPARTMENT
UNIVERSITY OF CALIFORNIA
BERKELEY, CALIFORNIA 94720*