

# UC Santa Barbara

## UC Santa Barbara Previously Published Works

### Title

Estimate of Rayleigh-to-Love wave ratio in the secondary microseism by a small array at Piñon Flat observatory, California

### Permalink

<https://escholarship.org/uc/item/9vp7k1j5>

### Journal

Geophysical Research Letters, 43(21)

### ISSN

0094-8276

### Authors

Tanimoto, Toshiro  
Lin, Chin-Jen  
Hadziioannou, Céline  
[et al.](#)

### Publication Date

2016-11-16

### DOI

10.1002/2016gl071133

Peer reviewed

1 **Estimate of Rayleigh-to-Love wave ratio in the secondary microseism**  
2 **by a small array at Piñon Flat Observatory, California**

3

4 Toshiro Tanimoto<sup>1\*</sup>, Chin-Jen Lin<sup>2,3</sup>, Céline Hadziioannou<sup>3</sup>, Heiner Igel<sup>3</sup>, and Frank  
5 Vernon<sup>4</sup>

6 1. Department of Earth Science and Earth Research Institute, University of  
7 California, Santa Barbara, California 93106, USA.

8 2. Institute of Earth Sciences, Academia Sinica, Taiwan

9 3. Department of Earth and Environmental Sciences, Ludwig-Maximilians-  
10 University, Theresienstr. 41 80333 Munich, Germany

11 4. Institute of Geophysics and Planetary Physics, Scripps Institution of  
12 Oceanography, La Jolla, California, USA.

13 \*Corresponding author: Email [toshiro@geol.ucsb.edu](mailto:toshiro@geol.ucsb.edu)

14

15 **Abstract**

16 Using closely located seismographs at Piñon Flat (PFO), California, for one-year long  
17 record (2015), we estimated the Rayleigh-to-Love wave energy ratio in the secondary  
18 microseism (0.1-0.35 Hz) in four seasons. Rayleigh-wave energy was estimated from a  
19 vertical component seismograph. Love-wave energy was estimated from rotation  
20 seismograms that were derived from a small array at PFO. Derived ratios are 2-2.5,  
21 meaning that there is 2-2.5 times more Rayleigh-wave energy than Love-wave energy at  
22 PFO. In our previous study at Wettzell, Germany, this ratio was 0.9-1.0, indicating  
23 comparable energy between Rayleigh waves and Love waves. This difference suggests  
24 that the Rayleigh-to-Love wave ratios in the secondary microseism may differ greatly  
25 from region to region. It also implies that an assumption of the diffuse wavefield is not  
26 likely to be valid for this low frequency range as the equipartition of energy should make  
27 this ratio much closer.

28

## 29 **1. Introduction**

30           The cross-correlation Green's function approach was introduced to seismology by  
31 Campillo and Paul [2003] and since then, seismic noise has become an indispensable data  
32 set for earth structure study. But why this approach works is not necessarily clear. In  
33 Campillo and Paul [2003], a diffusive wavefield was assumed for the coda of earthquakes  
34 signals in which the equipartition of energy occurred. The equipartition of energy was  
35 shown to hold for high-frequency waves (at least higher than 1 Hz), in the coda of  
36 seismic phases [Hennino et al., 2001; Margerin et al., 2009] but the main frequency range  
37 that we have benefitted by the cross-correlation approach has been the microseism  
38 frequency band (0.05-0.4 Hz). For such a low frequency range, Snieder [2004] argued  
39 that the equipartition of energy is not likely to occur and presented a ballistic wave  
40 concept. We tend to agree with his view for the microseism frequency range but our  
41 fundamental problem is the lack of understanding on the nature of seismic noise.

42           In this paper, we attempt to find out the relative amount of Love waves with  
43 respect to Rayleigh waves in seismic noise in the microseism frequency band. In our  
44 previous papers [Tanimoto et al., 2015, 2016], we took advantage of a unique set of  
45 instruments at Wettzell (WET), Germany, where an STS-2 seismograph and a ring laser  
46 [Schreiber et al., 2009; Schreiber and Wells, 2013] are co-located. Since the ring laser at  
47 WET records the vertical component of rotation in contrast to strain or translational  
48 components at Earth's surface, they are only sensitive to Love waves (for a plane-layered  
49 structure). Combined with a vertical-component seismometer, which mainly records  
50 Rayleigh waves, we made estimates for the energy ratio between Rayleigh waves and  
51 Love waves.

52 In this paper, instead of using the ring laser data, we retrieve the rotation from  
53 closely located broadband instruments at Piñon Flat [Lin et al., 2016], California, by  
54 following an approach by Spudich et al. [1995] and Spudich and Fletcher [2008, 2009].  
55 This dense array has been in operation since 2014. We use this data set for the entire  
56 2015 to estimate the Rayleigh-to-Love wave energy ratios at PFO. We find that the  
57 Rayleigh-to-Love wave energy ratio is about 2-2.5, which is quite different from our  
58 results at Wettzell (0.9-1.0). Rayleigh waves seem dominant in the secondary microseism  
59 at PFO. We also point out that this large difference between WET and PFO is  
60 inconsistent with the assumption of diffuse wavefield for the microseism frequency band.

61 We describe our data in section 2, surface accelerations between Rayleigh and  
62 Love waves in section 3 and their energy ratios in section 4. We briefly discuss the  
63 implications of our results in section 5.

## 64 **2. Data**

65 Since late in 2014, there have been thirteen broadband seismographs installed at  
66 PFO as a small array. Fig. 1a shows two maps to indicate the location of PFO and  
67 detailed locations of broadband seismic stations at PFO in addition to the ring laser  
68 (yellow) and three strain meters (pink lines). Broadband stations are indicated by green,  
69 blue, and red circles. Lin et al. [2016] has done a comparison study between the ring laser  
70 rotation data (yellow) and the rotation that can be derived by differencing various pairs of  
71 seismograms [Spudich and Fletcher, 2008, 2009]. A general conclusion by Lin et al.  
72 [2016] is that the rotation is best derived by using the large array, indicated by green  
73 circles in Fig. 1a. Even so, there are slight differences in Love-wave amplitudes between  
74 the array-derived amplitudes and the ring-laser rotation amplitudes. But as long as

75 waveform cross-correlation is larger than 0.94, amplitude differences are less than 4.5  
76 percent. This level of difference does not affect our conclusion in this paper.

77 Out of thirteen stations, BPH03 is explicitly marked in this figure because we  
78 analyzed the rotation for this location for the estimate of Love-wave energy. We used  
79 vertical component seismograms at this location to estimate Rayleigh-wave energy. The  
80 ring laser data (at the yellow square) were not used because the instrument was not  
81 sensitive enough to record microseisms. We present our analysis for one-year long data in  
82 2015, separately analyzed for four seasons.

83 The approach in this paper is similar to the one in our previous studies [Tanimoto  
84 et al., 2015; 2016] except for minor details. In this study, we analyzed every 1-hour  
85 record in 2015, first computing the power spectral density (PSD) for all 1-hour records  
86 and eliminating time portions that were obviously influenced by large earthquakes and  
87 data gaps. Then we used two earthquake catalogues to reduce earthquake effects further;  
88 one was the Global Moment Tensor catalogue [Dziewonski et al., 1983; Ekström et al.,  
89 2012] that allowed us to remove global earthquake effects with magnitude 5.5 and larger.  
90 The other was the SCSN Moment tensor catalogue [SCEDC, 2013] that allowed us to  
91 remove regional (Southern California) earthquake effects with magnitude 3.0 and larger  
92 in 2015. For large earthquakes ( $M > 5.5$ ) we removed six hours after the origin time and  
93 for small earthquakes ( $M > 3.0$ ), we removed two hours from their origin times. This  
94 processing is important because large earthquakes generated large-amplitude body and  
95 surface waves near 0.1 Hz.

96 We then binned data into four seasons; Winter data are from January, February  
97 and December, Spring data from March, April and May, Summer data from July and

98 August and Fall data from September, October and November. Then for the identified  
99 “earthquake-free” 1-hour portions in 2015, we computed Fourier spectra and averaged  
100 Fourier amplitudes for each season. Fig. 1b shows the average vertical-component  
101 spectral amplitudes for each season as a function of frequency; blue is Winter, green is  
102 Spring, red is Summer and yellow is Fall. Fig. 1c shows the averaged spectral amplitudes  
103 for the rotation data. In both plots, instead of using the power spectral density, we show  
104 the averaged  $\sqrt{|F(\omega)|^2} / T$  where  $F(\omega)$  is the Fourier spectra and  $T$  is the length of  
105 time series (1 hour). We used Fourier amplitudes rather than PSD because we want to  
106 estimate surface amplitudes of Rayleigh and Love waves that are linearly proportional to  
107 spectral amplitudes.

108 For both vertical-component (Fig. 1b) and rotational spectra (Fig. 1c), amplitudes  
109 in winter (blue) are the largest and the peak frequency ( $\sim 0.15$  Hz) becomes the lowest  
110 frequency among the four seasons. Amplitudes in summer (red) are the smallest among  
111 the four seasons and their peak frequency becomes higher ( $\sim 0.2$  Hz). Amplitudes in  
112 spring and fall are between these two end-member seasons. These features are typical  
113 seasonal characteristics found for stations in the northern hemisphere. The main point  
114 here is that the effects from earthquakes seem to be removed successfully from these  
115 spectra as earthquakes could disturb the clean background seasonal variations in seismic  
116 noise.

117 For frequencies below 0.1 Hz, amplitudes show large differences between  
118 vertical-component spectra (Fig. 1b) and the rotational spectra (Fig. 1c). In Fig. 1b, we  
119 can see a small peak at about 0.05-0.07 Hz, which is the well-known primary microseism  
120 peak (the same frequency with ocean waves). However, we cannot see this peak in the

121 rotation spectra (Fig. 1c). Instead, we see a large peak at about 0.01-0.02 Hz. In fact,  
122 rotational spectral amplitudes seem to increase toward lower frequencies even further.  
123 We suppose that large tilt-related noise in horizontal component seismograms, which  
124 increases toward lower frequencies, might be the reason for this trend but the exact cause  
125 is not known for the moment. Fig. 1c shows a trend that goes to zero because we detrend  
126 data in the analyses and kept the zero-frequency data in this plot. For positive-frequency  
127 data the spectral amplitudes keep increasing toward lower frequencies. It seems clear that  
128 this large low-frequency noise is masking the primary microseism peak near 0.05-0.07  
129 Hz. Based on this observation, we report only on the results of secondary microseism in  
130 this paper.

### 131 **3. Acceleration spectra**

132 The rotational spectral amplitudes in Fig. 1c can be converted to surface  
133 transverse acceleration if twice the Love-wave phase velocity ( $2C$ ) is multiplied to the  
134 spectra [Pancha et al., 2000]. In this study, we examined three seismic velocity models  
135 for PFO and used their Love-wave phase velocities to obtain transverse spectral  
136 amplitudes. The three models are (i) SCEC CVM (Southern California Earthquake Center  
137 Community Velocity Model, Shaw et al., 2015), (ii) 1-D model based on tomographic  
138 results derived from the ANZA network data [Scott et al., 1994] where PFO is included,  
139 and (iii) a local structure at PFO based on the receiver function analysis [Baker et al.,  
140 1996]. P-wave and S-wave velocity in the upper 30 km are shown in the top panel of Fig.  
141 2 and their Love-wave dispersion curves are shown in the bottom panel. In these figures,  
142 SCEC CVM is the SCEC model, Anza refers to the structure by Scott et al. [1994] and  
143 RF refers to the receiver function results by Baker et al. [1996]. The first two models



144 (SCEC and Anza) have similar Love-wave phase velocity but the third one (RF) has  
145 Love-wave phase velocity that is about 10 percent slower. Since we multiply 2C (twice  
146 the Love-wave phase velocity) to the rotational spectra in Fig. 1(c) to obtain the  
147 transverse spectra [Pancha et al., 2000; Igel et al., 2005, 2007; Ferreira and Igel, 2009;  
148 Hadziioannou et al., 2012], these differences in phase velocity lead to about 10 percent  
149 differences in the transverse acceleration.

150 Fig. 3 shows four acceleration spectra, the transverse acceleration spectra (red)  
151 from the rotation time series and the vertical (Z, blue), the north-south (NS, green) and  
152 the east-west (EW, black) acceleration spectra obtained from seismograms at BPH03.  
153 Since three models give similar results, only the results for the SCEC model are shown in  
154 Fig. 3. Four panels correspond to the results in Winter (a), Spring (b), Summer (c) and  
155 Fall (d).

156 In all seasons, two horizontal accelerations (NS and EW) are slightly higher than  
157 transverse acceleration but they all have similar frequency dependence. Differences in  
158 amplitudes about 0.15 Hz among NS, EW and transverse spectra may be explained by the  
159 effects of Rayleigh waves. The maximum peak frequencies change according to season  
160 but all four acceleration spectra basically have the same peak frequencies in each season.

161 Love-wave phase velocity for the third seismic model (RF) is about 10 percent  
162 slower than two other models and it causes 10 percent reduction of transverse  
163 accelerations. But spectral shape of transverse acceleration remains quite similar. This  
164 amplitude difference leads to smaller estimates of transverse acceleration and Love-wave  
165 energy by 10 percent.

#### 166 **4. Energy ratios between Rayleigh waves and Love waves**

167 Results in Fig. 3 give us information on surface amplitudes of Rayleigh waves  
 168 and Love waves. Essentially we get the surface values of Rayleigh-wave eigenfunctions  
 169 (U and V) and Love-wave eigenfunction (W) from them [Tanimoto et al., 2016]. Since  
 170 the energy of surface waves are given by the depth integrals as  
 171  $E_R = \omega^2 \int \rho \{U(z)^2 + V(z)^2\} dz$  and  $E_L = \omega^2 \int \rho W(z)^2 dz$ , where  $E_R$  and  $E_L$  are Rayleigh-  
 172 and Love-wave energy, we can evaluate them without any difficulty for three seismic  
 173 models.

174 Figures 4b, 4c and 4d show the Rayleigh-to-Love wave energy ratios (R/L) for  
 175 frequencies between 0.10 and 0.35 Hz. Each season is denoted by a different color. The  
 176 maximum ratios are found at about 0.20 Hz in summer and the ratios are about 4. In other  
 177 seasons, the ratios are about 2.0-3.0. The energy ratios become lower for frequencies  
 178 close to 0.1 Hz.

179 The average ratios between 0.10 and 0.35 Hz in each season are shown in Fig. 4a.  
 180 In this panel, three colors indicate three seismic models. All ratios fall within the range  
 181 2.0-2.5, meaning that the Rayleigh wave energy is about 2-2.5 times larger than the Love-  
 182 wave energy. But this is the overall average. It should be kept in mind that this ratio can  
 183 be as high as 4.0 in summer near its peak frequency (0.20 Hz) and about 3.0 in other  
 184 seasons near their peak frequencies (0.15 Hz).

185 There is a hint for higher R/L ratios in spring and summer in Fig. 4a, but it does  
 186 not stand the statistical test as error bars indicate. But we note this tendency of higher  
 187 summer R/L ratio is consistent with what Tanimoto et al. [2016] reported for the Wettzell  
 188 study.

## 189 **5. Discussion**

190           The main result in this paper is the average R/L energy ratio of 2.0-2.5 at PFO.  
191   Depending on the seismic velocity models, there are some variations but the estimated  
192   ratios fall in this relatively small range. This relative dominance of Rayleigh waves may  
193   have been the reason that Schulte-Pelkum et al. [2004] observed clean and azimuthally  
194   stable Rayleigh-wave arrivals from the ANZA array analysis.

195           In our analysis for Wettzell (Germany) data, we obtained the R/L ratio of about  
196   0.9-1.0. This value means that the Love-wave energy and the Rayleigh-wave energy are  
197   comparable. There are some uncertainties in those energy estimates that can arise from a  
198   choice of seismic velocity structure, but this difference in the R/L ratio by a factor of two  
199   is significant. It seems safe to state that the R/L energy ratios are substantially different  
200   between Wettzell and Piñon Flat.

201           This large difference in R/L ratio suggests that the assumption of diffuse  
202   wavefield fails for the microseism frequency range. The equipartition of energy should  
203   occur in a diffuse wavefield [e.g., Weaver, 2010] and if so, R/L ratios should not vary  
204   very much from region to region. It is not easy to test the validity of this assumption,  
205   however, because mode shapes are different depending on earth structure but one would  
206   not expect a large difference in the R/L ratios. Many seismic noise analyses for earth  
207   structure were conducted by assuming the diffuse wavefield, including the noise cross-  
208   correlation Green's function analysis [Campillo and Paul, 2003] and H/V analysis [e.g.  
209   Sanchez-Sesma et al., 2011]. We should stress, however, that the latter H/V analysis was  
210   done in higher frequency ranges than the microseism frequency range. The assumption of  
211   the diffuse wavefield was shown to work for higher frequencies, for example between 5

212 and 7 Hz [Margerin et al., 2009], in the coda of large-amplitude seismic phases. The  
213 result of this study only indicates that it does not hold in the microseism frequency range.

214         If a propagation path is long, the wavefield could become closer to a diffusive  
215 field even for the microseism frequency range, because for a long propagation path, there  
216 will be more chances of scattering and wave conversion. Comparable energy between  
217 Rayleigh waves and Love waves at WET may be related to this case as Wettzell is quite  
218 far from the coasts in all azimuths. On the other hand, since PFO is relatively close to the  
219 California coast, the propagation distance may be too short to create a diffusive wavefield  
220 for the microseism frequency range.

221         There are a few other recent studies that have estimated the energy ratios between  
222 Rayleigh and Love waves. Nishida et al. [2008] reported results in Japan and their ratio  
223 estimate for the secondary microseism of about 2 is close to our estimate for PFO.  
224 Juretzek and Hadziioannou [2016] obtained ratios from multiple array analyses in Europe  
225 and their results range between 0.8 and 2.5, depending on location and season. Our result  
226 for PFO is similar to Japanese results and is near the upper end of Juretzek and  
227 Hadziioannou [2016], although the latter study reported a somewhat large range of ratios.  
228 The lowest end of their estimate is consistent with our result for Wettzell. But we should  
229 be careful in those comparisons because even in our current results, the ratio can reach 4  
230 in summer for the peak frequency range (0.19-0.20 Hz) and 3 in other seasons for their  
231 peak frequency ranges of about 0.15 Hz. The total average for the range 0.10-0.35 Hz  
232 may be 2.0-2.5, there are quite large variations with respect to frequencies and seasons.

233         Our results also indicate a need for better understanding of the Love-wave  
234 excitation sources, especially their power and the mechanisms of their excitation.

235 Compared with our understanding of Rayleigh-wave excitation in the secondary  
236 microseism [Longuet-Higgins, 1950], our understanding of Love-wave excitation in the  
237 secondary microseism is still quite vague. It appears that we can form two hypotheses;  
238 one is a conversion hypothesis. Ocean wave collisions (the Longuet-Higgins mechanism)  
239 can create double-frequency Rayleigh waves in deep oceans. As these Rayleigh waves  
240 propagate toward seismic stations on land, a fraction of them may convert to Love waves  
241 at a sharp ocean-continent boundary. Numerical simulations (e.g., Ying et al, 2014;  
242 Gualtieri et al., 2013, 2015) are clearly needed to understand the importance of this  
243 propagation effect. The other hypothesis is that the double-frequency ocean waves that  
244 are generated by collision of ocean waves, reach shallow oceans near the coast and  
245 interact with the solid earth directly [e.g., Saito, 2010]. Both mechanisms may contribute  
246 to Love-wave excitation and regional variations in the R/L ratios may be explained by a  
247 combination of these effects. But we need more careful analysis in the future.

248

## 249 **Acknowledgments**

250 All data used in this study, the thirteen broadband seismic data at PFO, can be obtained  
251 from the IRIS data center in Seattle, Washington, USA. TT acknowledges support from  
252 NSF-EAR 1547523, HI from the ERC Advanced Grant "ROMY", CH from grant  
253 HA7019/1-1 by the Emmy-Noether Programme of the German Research Foundation  
254 (DFG).

255 **References**

256 Baker, G. Eli, J. B. Minster, G. Zandt, and H. Gurrola (1996), Constraints on crustal  
257 structure and complex Moho topography beneath Pinon Flat, California, from teleseismic  
258 receiver functions, *Bull. Seism. Soc. Am.*, 86, 1830-1844.

259

260 Campillo, M. and A. Paul, (2003). Long range correlations in the diffuse seismic coda,  
261 *Science*, 299, 547-549.

262

263 Dziewonski, A. M., T.-A. Chou and J. H. Woodhouse (1981), Determination of  
264 earthquake source parameters from waveform data for studies of global and regional  
265 seismicity, *J. Geophys. Res.*, 86, 2825-2852. doi:10.1029/JB086iB04p02825

266

267 Ekström, G., M. Nettles, and A. M. Dziewonski (2012), The global CMT project 2004-  
268 2010: Centroid-moment tensors for 13,017 earthquakes, *Phys. Earth Planet. Inter.*, 200-  
269 201, 1-9. doi:10.1016/j.pepi.2012.04.002

270

271 Ferreira, A. and I. Igel (2009), Rotational motions of seismic surface waves in a laterally  
272 heterogeneous Earth, *Bull. Seism. Soc. Am.*, 99(2B), 1429-1436.

273

274 Gualtieri, L., E. Stutzmann, Y. Capdeville, F. Ardhuin, M. Schimmel, A. Mangeney and  
275 A. Morelli (2013). Modelling secondary microseismic noise by normal mode summation,  
276 *Geophys. J. Int.*, 193, 1732-1745, doi:10.1093/gji/ggt090.

277

278 Gualtieri, L., E. Stutzmann, Y. Capdeville, V. Farra, A. Mangeney, and A. Morell(2015),  
279 On the shaping factors of the secondary microseismic wavefield, *J. Geophys. Res. Solid*  
280 *Earth*, *120*, 6241–6262, doi:10.1002/2015JB012157.

281

282 Hadziioannou, C., P. Gaebler, U. Schreiber, J. Wassermann, and H. Igel (2012),  
283 Examining ambient noise using co-located measurements of rotational and translational  
284 motion, *J. Seismol.*, **16**, 787, doi:10.1007/s10950-012-9288-5.

285

286 Hennino, R., Tregoures, N., Shapiro, N.M., Margerin, L., Campillo, M., van Tiggelen,  
287 B.A. & Weaver, R.L., 2001. Observation of equipartition of seismic waves, *Phys. Rev.*  
288 *Lett.*, *86*, 3447–3450, DOI: 10.1103/PhysRevLett.86.3447

289

290 Igel, H., U. Schreiber, A. Flaws, B. Schuberth, A. Velikoseltsev, and A. Cochard (2005),  
291 Rotational motions induced by the M8.1 Tokachioki earthquake, September 25, 2003,  
292 *Geophys. Res. Lett.*, *32*, L08309, doi:10.1029/2004GL022336.

293

294 Igel H, Cochard A, Wassermann J, Flaws A, Schreiber U, Velikoseltsev A, Pham Dinh N  
295 (2007) Broad-band observations of earthquake-induced rotational ground motions,  
296 *Geophys. J Int.*, *168*(1):182–196

297

298 Juretzek, C. and C. Hadziioannou (2016), Where do ocean microseisms come from? A  
299 study of Love-to-Rayleigh wave ratios, *J. Geophys. Res.*, *Solid Earth*, *121*,  
300 doi:10.1002/2016JB013017.

301

302 Lin, Chin-Jen, F. Vernon, J. Wassermann, A. Gebauer, U. Schreiber, S. Donner, C. Hadziioannou,  
303 D. Agnew, and Heiner Igel (2016), Comparison of Direct and Array-derived strain and rotation at  
304 the Piñon Flat Observatory, California, EGU General Assembly, 18, 7753.

305

306 Longuet-Higgins, M. (1950), A theory of the origin of microseisms. *Phil. Trans. R. Soc.*  
307 *Lond., Ser A, Math. Phys. Sci.*, 243(857), 1–35.

308

309 Margerin, L., M. Campillo, B. A. Van Tiggelen, and R. Hennino (2009). Energy partition  
310 of seismic coda waves in layered media: theory and application to Pinyon Flats  
311 Observatory, *Geophys. J. Int.*, 177, 571-585, doi: 10.1111/j.1365-246X.2008.04068.x

312

313 Nishida K, Kawakatsu H, Fukao Y, Obara K (2008) Background Love and Rayleigh  
314 waves simultaneously generated at the Pacific Ocean floors, *Geophys. Res. Lett.*,  
315 35(16):1–5

316

317 Pancha A., T.H. Webb, G. E. Stedman, D. P. McLeod, and K. U. Schreiber (2000), Ring  
318 laser detection of rotations from teleseismic waves, *Geophys Res Lett* 27(21):3553

319

320 Saito, T., (2010), Love-wave excitation due to the interaction between a propagating  
321 ocean wave and the sea-bottom topography, *Geophys. J. Int.*, 182, 1515-1523,  
322 doi:10.1111/j.1365-246X.2010.04695.x

323



- 324 SCEDC (2013): Southern California Earthquake Center. Caltech.Dataset.  
325 doi:10.7909/C3WD3xH1  
326
- 327 Schreiber, U., and J.-P. Wells (2013), Invited Review Article: Large ring laser for  
328 rotation sensing, *Rev. Sci. Instrum.*, 84, 041101, doi:10.1063/1.4798216.  
329
- 330 Schreiber, U., J. N. Hautmann, A. Velikoseltsev, J. Wassermann, H. Igel, J. Otero, F.  
331 Vernon, and J. -P. R. Wells (2009b), Ring laser measurements of ground rotations for  
332 seismology, *Bull. Seism. Soc. Am.*, 99(2B), 1190–1198, doi:10.1785/0120080171  
333
- 334 Schulte-Pelkum, V., P. S. Earle, and F. Vernon (2004). Strong directivity of ocean-  
335 generated seismic noise, *G-cubed*, 5, Q03004, doi:10.1029/2003GC000520  
336
- 337 Scott, J., T. G. Masters, and F. L. Vernon (1994). 3-D velocity structure of the San  
338 Jacinto Fault zone near Anza, California, *Geophys. J. Int.*, 119, 611-626.  
339
- 340 Shaw, J., A. Plesch, C. Tape, M.P. Suess, T. H.Jordan, G. Ely, E. Hauksson, J. Tromp, T.  
341 Tanimoto, R. Graves, K. Olsen, C. Nicholson, P. J.Maechling, C. Rivero, P. Lovely, C.  
342 M. Brankman, J. Munster (2015). Unified Structural Representation of the southern  
343 California crust and upper mantle, *Earth Planet. Sci. Lett.*, 415, 1-15. doi:  
344 10.1016/j.epsl.2015.01.016  
345
- 346 Snieder, R. (2004). Extracting the Green's function from the correlation of coda waves:

347 A derivation based on stationary phase, *Phys. Rev. E*, 69, 046610,

348 DOI:10.1103/PhysRevE.69.046610

349

350 Spudich, P. and J. B. Fletcher (2008). Observation and prediction of dynamic ground  
351 strains, tilts, and torsions caused by the M 6.0 2004 Parkfield, California, earthquake and  
352 aftershocks derived from UPSAR array observations, *Bull. Seism. Soc. Am.*, 98, 1898-  
353 1914, doi:10.1785/0120070157.

354

355 Spudich, P. and J. B. Fletcher (2009). Software for inference of dynamic ground strains  
356 and rotations and their errors from short baseline array observations of ground motions,  
357 *Bull. Seism. Soc. Am.*, 99, 1480-1482, doi:10.1785/0120080230

358

359 Spudich, P., L. K. Steck, M. Hellweg, J. Fletcher, and L. M. Baker (1995). Transient  
360 stresses at Parkfield, California, produced by the M 7.4 Landers earthquake of June 28,  
361 1992: observations from the UPSAR dense seismograph array, *J. Geophys. Res.*, 100,  
362 675-690.

363

364 Tanimoto, T., C. Hadziioannou, H. Igel, J. Wasserman, U. Schreiber, and A. Gebauer  
365 (2015), Estimate of Rayleigh-to-Love wave ratio in the secondary microseism by  
366 colocated ring laser and seismograph, *Geophys. Res. Lett.*, 42,  
367 doi:10.1002/2015GL063637.

368

369 Tanimoto, T., C. Hadziioannou, H. Igel, J. Wassermann, U. Schreiber, A. Gebauer, and

370 B. Chow (2016), Seasonal variations in the Rayleigh-to-Love wave ratio in the secondary  
371 microseism from colocated ring laser and seismograph, *J. Geophys. Res. Solid Earth*,  
372 121, 2447–2459, doi:10.1002/2016JB012885.

373

374 Weaver, R.L., 2010. Equipartition and retrieval of Green's function. *Earthquake Science*,  
375 23(5), pp.397-402.

376

377 Ying, Y., C. J. Bean, and P. D. Bromirski (2014), Propagation of microseisms from the  
378 deep ocean to land, *Geophys. Res. Lett.*, 41, 6374–6379, doi:10.1002/2014GL060979.

379

380 **Figure Captions**

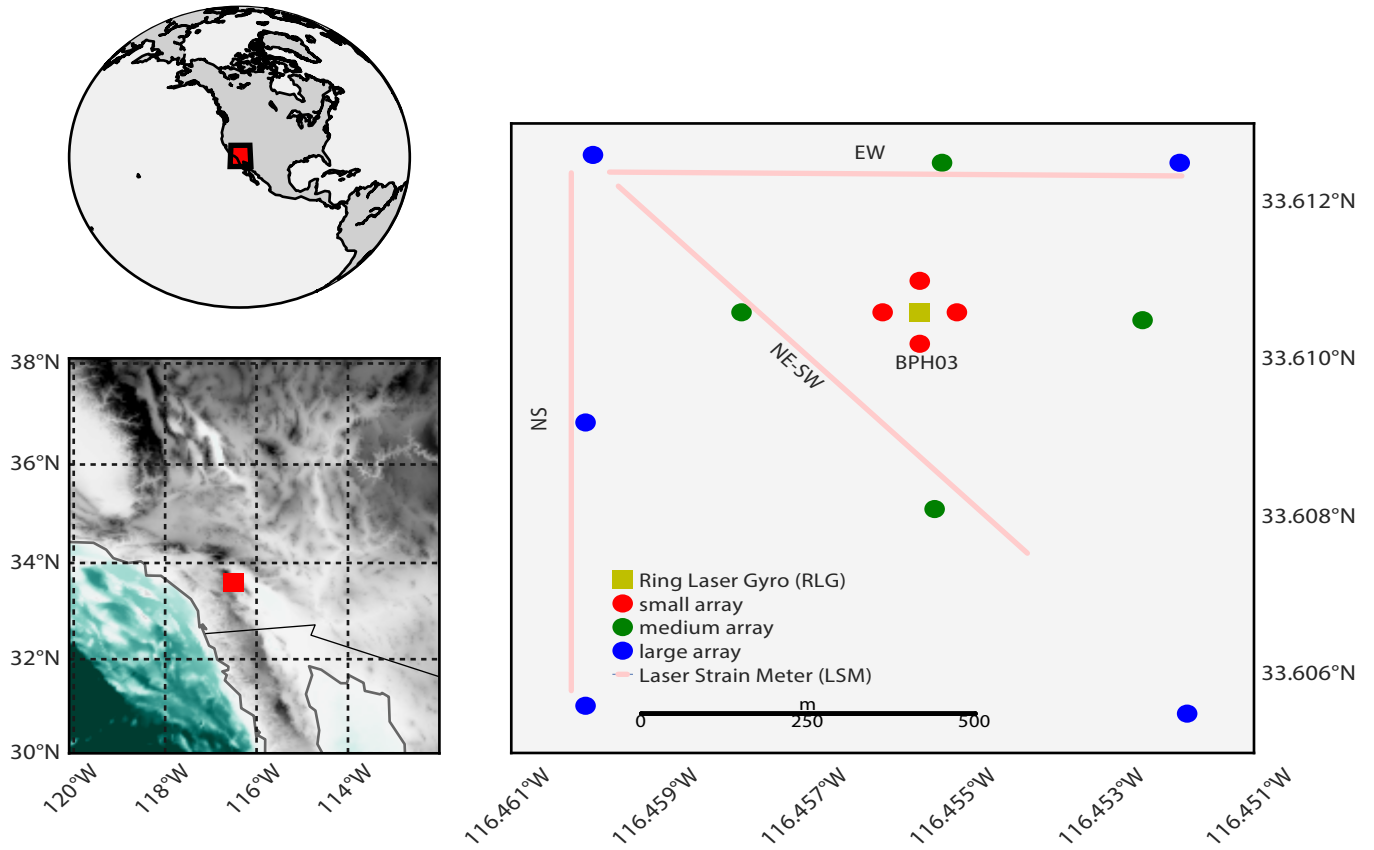
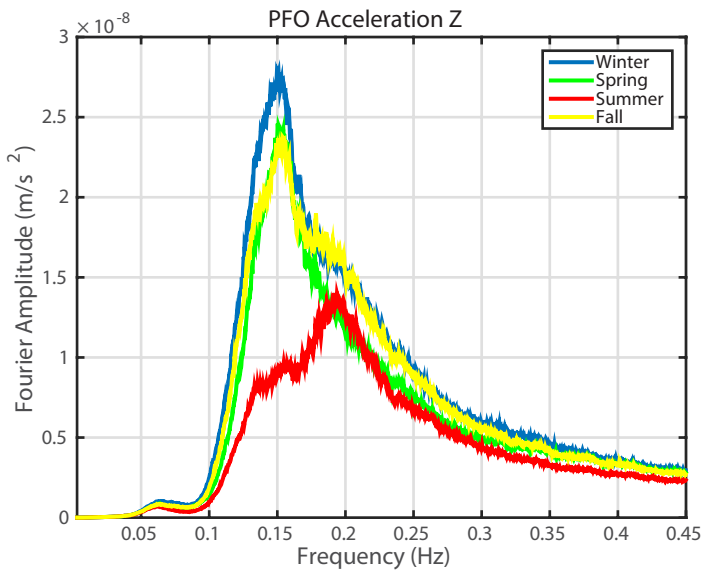
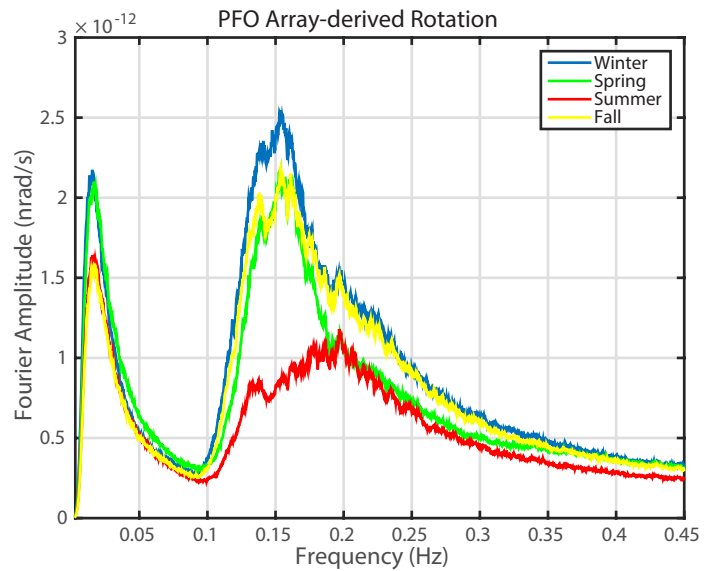
381 **Fig. 1. (a)** Two maps on the left indicate the location of PFO. Locations of thirteen  
 382 broadband seismographs at PFO are shown on the right (red, blue and green circles). We  
 383 analyzed rotation, derived from the green stations. BPH03 is the location around which  
 384 rotation was derived from this array. RLG is the ring laser gyroscope and three lines  
 385 indicate the locations of strain meters. **(b)** Fourier amplitudes of vertical acceleration at  
 386 BPH03 in four seasons. **(c)** Fourier amplitudes of rotation rate in four seasons.  
 387 Earthquake effects were removed from (b) and (c) by using two catalogues.

388 **Fig. 2: (a)** P-wave and S-wave velocity structure for three seismic models. Models are  
 389 SCEC CVM, 1-D structure from a tomographic study [Scott et al., 1994] and structure  
 390 from a receiver function study at PFO [Baker et al., 1996]. **(b)** Love-wave fundamental-  
 391 mode phase velocity for the three models. They were used to transform rotation rate to  
 392 transverse acceleration.

393 **Fig. 3:** Acceleration spectra at BPH03. Z (blue), N (green) and E (black) are vertical, NS  
 394 and EW acceleration spectra from seismometer at BPH03. Transverse acceleration (red)  
 395 was obtained from the rotation spectra by multiplying  $2C$  where  $C$  is Love-wave phase  
 396 velocity (Fig. 2b). Results for (a) winter, (b) spring, (c) summer and (d) fall.

397 **Fig. 4: (a)** Rayleigh-to-Love wave energy (R/L) ratios in four seasons. The results for  
 398 three seismic velocity models are shown in different colors. They are averaged ratios for  
 399 frequencies between 0.1 and 0.35 Hz. (b) R/L ratios when the SCEC CVM model was  
 400 used. Different colors are for different seasons. (c) Same with (b) except that the Anza  
 401 model was used. (d) Same with (b) except that the RF model was used.

**Figure 1.**

**a****b****c**

**Figure 2.**

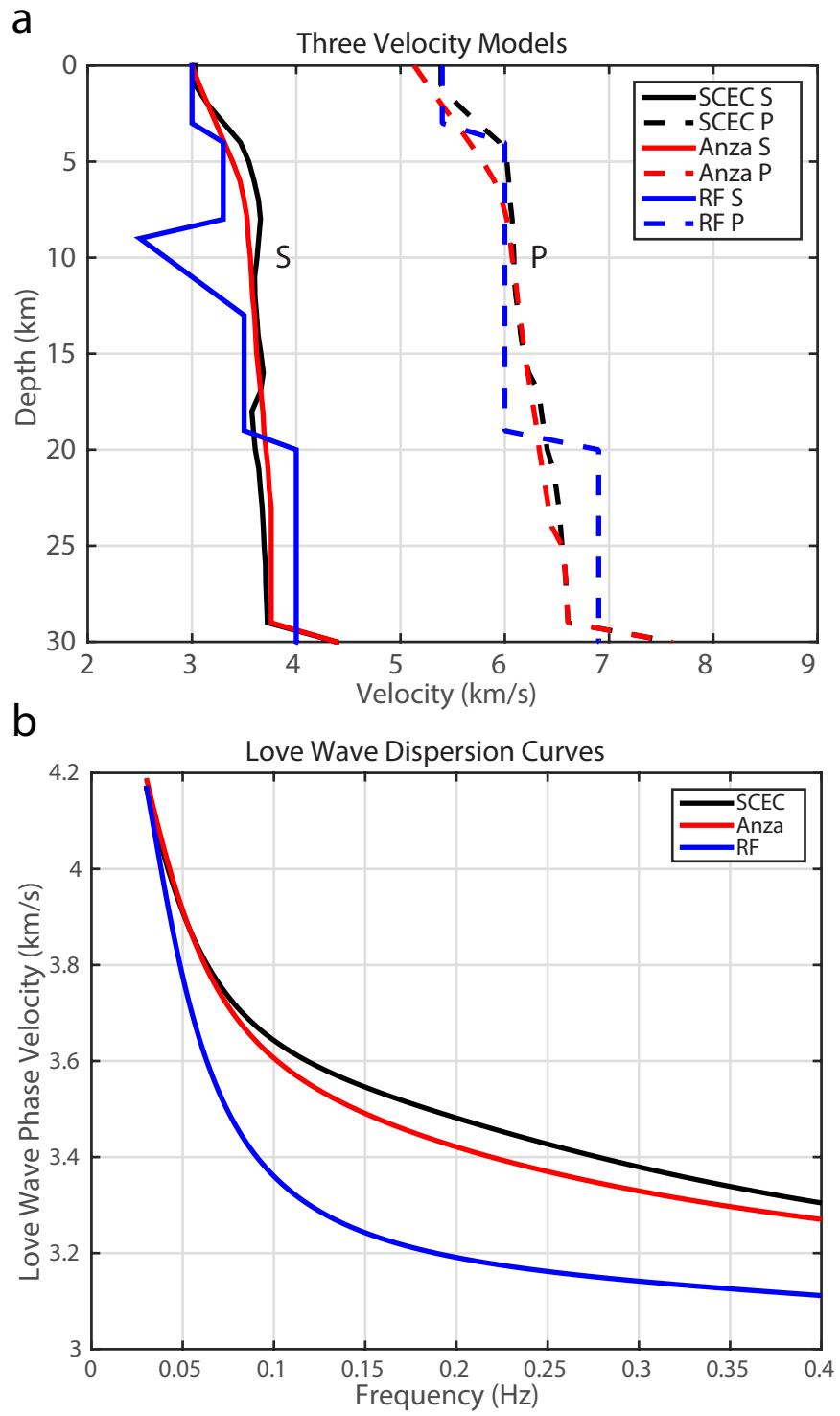


Figure 2



**Figure 3.**

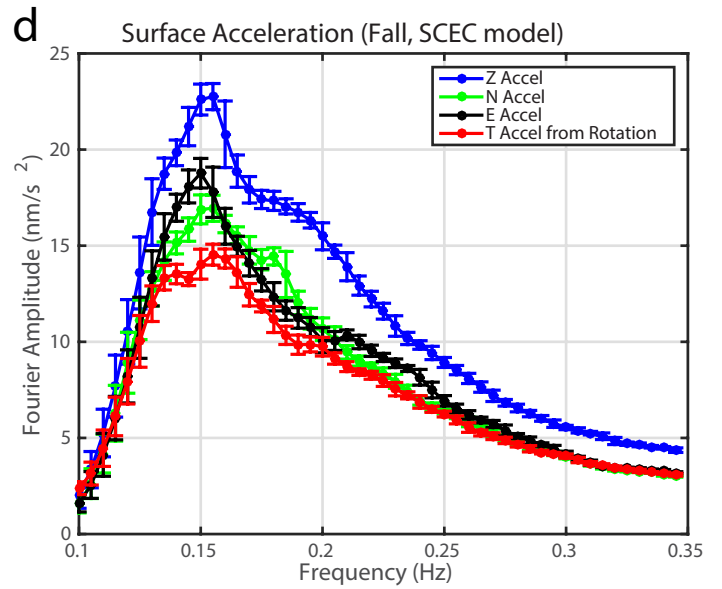
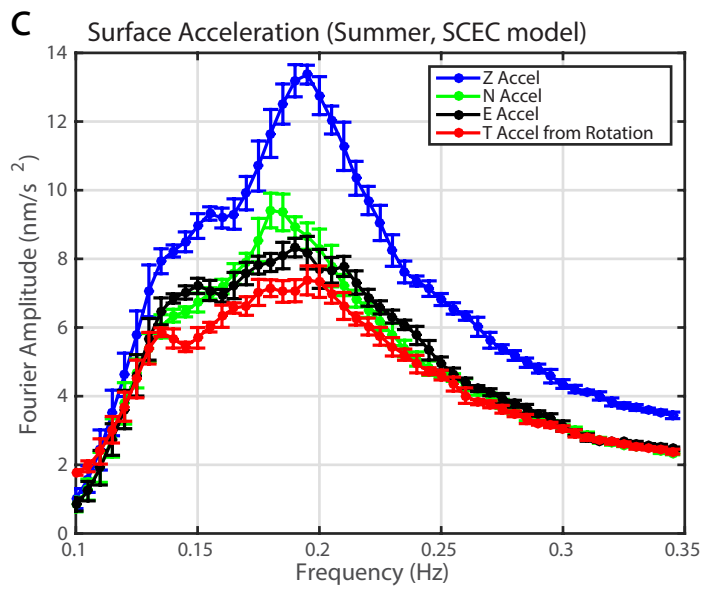
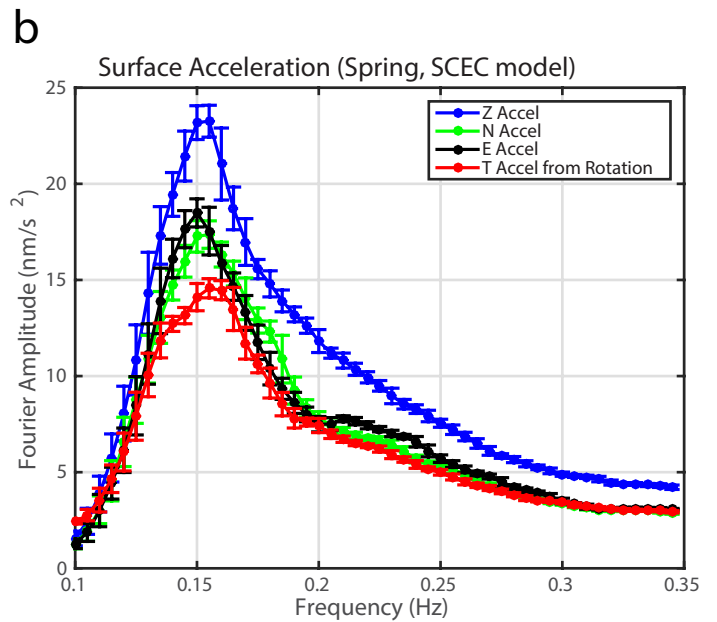
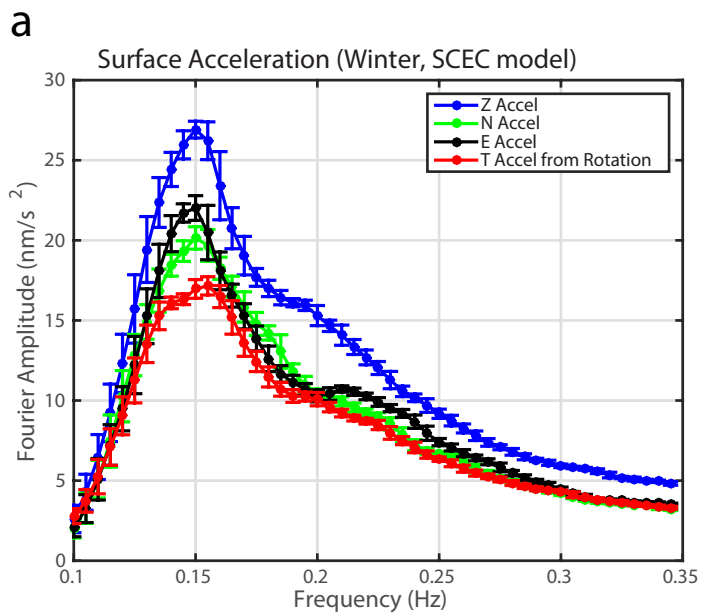


Figure 3

**Figure 4.**

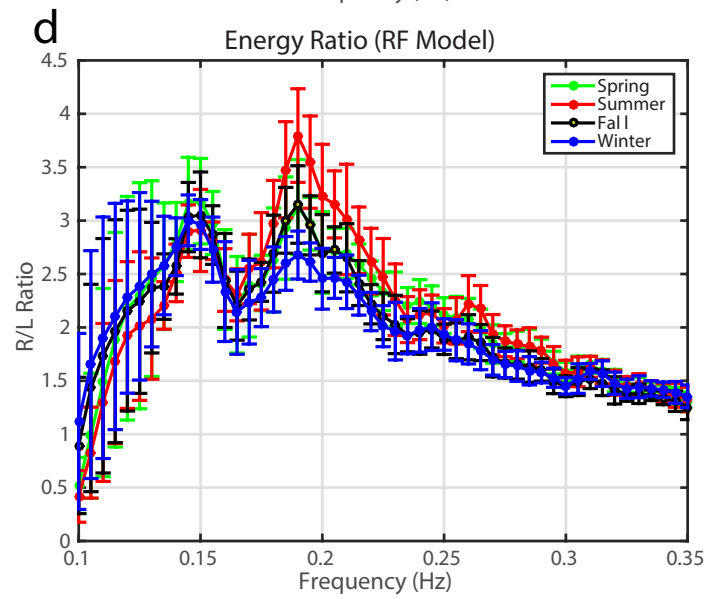
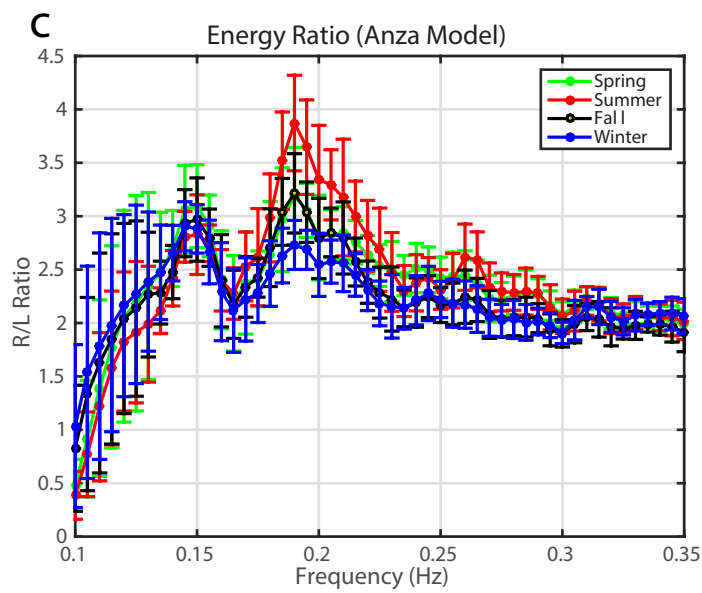
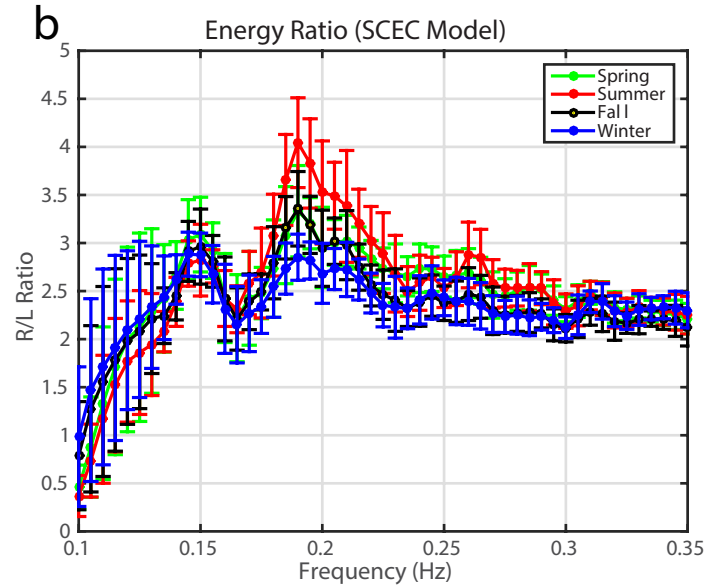
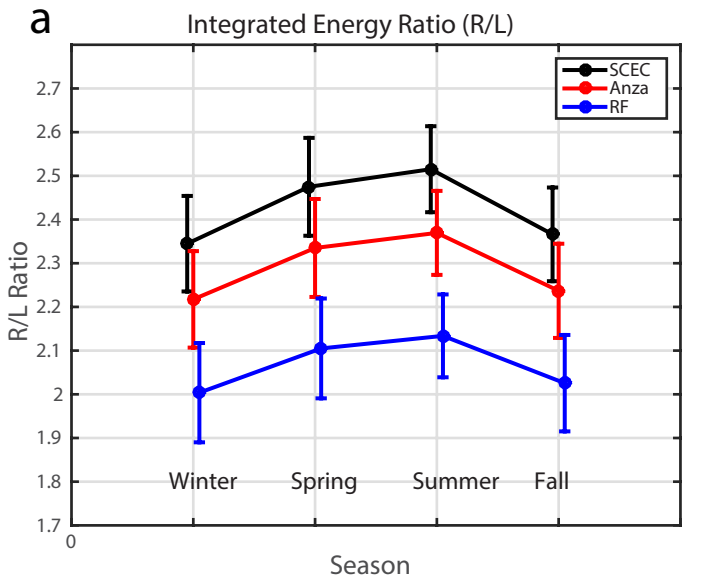


Figure 4