
NUMERICAL SIMULATION--SITE SIMULATION

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NUMERICAL SIMULATION--SITE SIMULATION

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ABSTRACT

The Seasonal Thermal Energy Storage (STES) program at Lawrence Berkeley Laboratory during 1981 consists of four lines of work: (1) to solicit, review, organize, and edit appropriate articles for a quarterly international STES Newsletter; (2) to perform Aquifer Thermal Energy Storage (ATES) generic studies; (3) to carry out site-specific planning and simulation studies; and (4) to improve modeling techniques. These four tasks form a well-balanced program of work to stimulate interest and information exchange in this field, to provide technical support to field projects, and to develop techniques that may be useful for industrial applications of this concept. The present paper reviews our site-specific studies during 1981.

INTRODUCTION

Lawrence Berkeley Laboratory (LBL) began working on seasonal thermal energy storage in aquifers in 1976. Initial studies included comprehensive generic calculations based on a numerical model to calculate the coupled heat and fluid flow in a three-dimensional, complex geometry aquifer system. Proof-of-concept calculations were made for a number of hypothetical situations, the results of which have been published in a series of papers [for example, 1-3].
In 1978 LBL organized and hosted the First International Workshop on Aquifer Thermal Energy Storage (ATES). Active workers from nine countries participated in this workshop and their contributions were published in the workshop proceedings [4]. Since the workshop, a periodic newsletter [5] has kept researchers abreast of the current status of various projects worldwide. Many of these projects are reviewed in two survey papers published in 1979 [6,7] and an update survey to be published in 1981 [8].

The LBL 1981 ATES project includes four main tasks: (a) To solicit, review, organize, and edit appropriate articles for a quarterly international STES Newsletter; (b) to perform ATES generic studies; (c) to carry out site-specific planning and simulation studies; and (d) to improve modeling techniques. Of particular note among these is the STES Newsletter which is published quarterly with distribution to over 350 researchers, developers, and program managers in 23 countries.

This paper concentrates on our site-related studies during 1981: Site characterization for optimal storage conditions, and prediction and simulation of the Mobile field experiments.

SITE CHARACTERIZATION

The purpose of our ATES site-characterization studies is to develop some general parameters or procedures whereby, for a given site, the energy recovery factor may be predicted readily for a wide range of operating conditions. This provides the basic results needed for technical or economic optimization of the ATES system. Here, the energy recovery factor is defined as the energy
recovered divided by energy stored for the same amount of water injected into and produced from the aquifer. Energy is measured with reference to ambient aquifer temperature energy.

Two ATES site characterization schemes have been developed at LBL during the past year, the first neglecting buoyancy flow, the second including it.

The first study [9] considers the thermal behavior of an ATES system with steady radial fluid flow around a single injection/production well. Buoyancy flow is neglected and the aquifer is confined above and below by impermeable layers. Neglecting buoyancy flow may be a reasonable assumption for cases with low aquifer permeability, short storage cycle length, or small temperature difference between injected and ambient water. A criterion [10] exists which may be used to determine if buoyancy flow is negligible for a given case. However, conclusions from this study may still be applicable in a relative sense for cases in which buoyancy flow is significant.

With the above assumptions, the thermal behavior of the system can be described in terms of the following four dimensionless parameter groups:

\[ Pe = \frac{Q c_w}{2 \pi \lambda_a H} ; \quad Q = \frac{C_a H^2}{C \lambda_c t_i} ; \quad Bi = \frac{\lambda_a C_a}{\lambda_c C_c} ; \quad \frac{C_a}{C_c} \]

where \( Q \) is the flowrate; \( H \) is the aquifer thickness; \( \lambda_a \) and \( \lambda_c \) are the aquifer and aquitard thermal conductivities; \( C_w, C_a, \) and \( C_c \) are the water, aquifer, and aquitard volumetric heat capacities, and \( t_i \) is the injection time period.
A simple steady flow model has been used to calculate recovery factors and temperatures as a function of these parameters. Some of the results are shown in Figures 1 and 2.

Figure 1 shows the calculated energy recovery factor as a function of $\text{Pe}$ and $\Lambda$ numbers for the first cycle. Results for subsequent cycles have also been calculated. Note that the large initial increase in recovery factor is followed by a more gradual increase as $\text{Pe}$ and $\Lambda$ are increased.

Figure 2 displays the temperature of water extracted during the production period of the first and fifth cycles for different values of $\text{Pe}$ and $\Lambda$. For values of $\text{Pe}$ larger than 200, production temperature shows little dependence on $\text{Pe}$.

Various other factors have also been considered such as thermal dispersion effects, dependence on cycle periods, the influence of a finite-thickness caprock, and long-term behavior. Table 1 displays the application to the Mobile [11] and Bonnaud [12] experiments. In this table, $E$ is the calculated energy recovery factor and $E_{\text{exp}}$ is the experimentally observed value. For the Auburn case, two calculations were made: (a) assuming that the well penetrates the full thickness of the aquifer, and (b) correcting for the fact that experimentally the well was open to only 9 m out of the 21 m thickness of the aquifer. The comparisons are very encouraging.

To investigate the effect of thermal front tilting caused by buoyancy flow, a second study [13] has been carried out. Calculations have been
Figure 1. Recovery factor as a function of $\sqrt{Pe}$ and $\sqrt{\Lambda}$ for the first cycle, when $\lambda_a/\lambda_c = 1$. [XBL 8012-6516]
Figure 2. First and fifth cycle production temperatures versus time for a range of Pe and Λ when λ_α/λ_c = 1. [XBL 8012-6582C]
Table 1.

<table>
<thead>
<tr>
<th></th>
<th>√Pe</th>
<th>√λ</th>
<th>ε</th>
<th>ε_{exp}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mobile (first cycle)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(a)</td>
<td>8.8</td>
<td>9.0</td>
<td>0.71</td>
<td>0.66</td>
</tr>
<tr>
<td>(b)</td>
<td>10.1</td>
<td>6.8</td>
<td>0.68</td>
<td></td>
</tr>
<tr>
<td>Bonnaud (fourth cycle)</td>
<td>3.9</td>
<td>5.0</td>
<td>0.63</td>
<td>0.677</td>
</tr>
</tbody>
</table>

conducted over a wide range of aquifer permeabilities and injection temperatures using the numerical model CCC, which takes into account the temperature-dependent parameters and the buoyancy flow process. In each case, an energy balance was kept for various times, separating radial diffusive losses in the aquifer and the vertical losses to the confining layers. A study of these results shows that over a wide range of conditions, the radial and vertical heat losses can be decoupled. Thus the energy recovery factor epsilon may be expressed as the product of two factors, \( \varepsilon = \varepsilon_a \cdot \varepsilon_c \), where \( \varepsilon_a \) is the energy recovery factor when the aquifer is insulated from the confining layers above and below, and \( \varepsilon_c \) is the energy recovery factor when the only heat loss is that due to vertical conduction diffused into the upper and lower confining layers.

The decoupling of radial and vertical heat losses reduces the number of parameter groups required to describe the system to three: \( Pe, A, \) and \( Bi. \) However, the thermal front tilting influences both the radial and vertical losses, since the tilting modifies the area over which heat conduction occurs. An empirical shape factor based on the thermal front angle of tilt is
introduced to modify the parameter groups. Thus $E_a$ depends on the modified
Pe number, $P_e^*$, while $E_c$ depends on $A^*$ and $B_i^*$.

$E_c$ as a function of $A^*$ and $B_i^*$ is calculated from a one-dimensional heat
conduction problem in which heat diffuses from aquifer to aquitard. $E_a$ as a
function of $P_e^*$ is calculated from vertically insulated cases of ATES cycles.
Hence, using values of $P_e^*$, $A^*$ and $B_i^*$ obtained from field input data, $E_c$ and
$E_a$ may be determined and combined to form epsilon. Although not mathemati-
cally rigorous, the method has been shown to yield accurate predictions for a
wide range of conditions when compared with CCC-simulated results.

**SIMULATION OF THE MOBILE EXPERIMENTS**

While the first cycle of the 1981 series of experiments was being carried
out by Auburn University at Mobile, Alabama, LBL performed a numerical simula-
tion based on the field operating conditions to predict the outcome of the
experiment before its conclusion. The goal was to test our understanding of
the aquifer storage problem and to verify our numerical model CCC.

Details of the Mobile experiment are described elsewhere in this volume.
The basic idea is that water at approximately 55 to 60°C is injected over a
period of one month into an aquifer approximately 21 m thick and with a perme-
ability of about 63 darcys. It is then stored for one month and subsequently
produced. The injected water is obtained from a supply well perforated in the
same aquifer 240 m away from the injection/production well. LBL was provided
with the basic geological, well test, injection flowrate, and injection temper-
ature data.
The simulation method was similar to that used by LBL to model the 1979-1980 Auburn experiment [14]. The well test data and geological information were studied and analyzed to obtain reservoir parameters and their range of uncertainty. Our results generally confirmed the analyzes done by Auburn University. The parameters used in our numerical simulation are listed in Table 2. Since the supply well is 240 m from the injection/storage well and radial calculation mesh would be adequate. Based on the injection flowrates and temperatures provided, we employed the numerical model CCC to calculate production temperature and energy recovery factor for a given production flow rate schedule. The result is presented as curve A in Figure 3, where the experimental result is also plotted. The experimental results were made known to us after we completed and presented our results. The predicted energy recovery factor is 0.62 compared to the experimental value of 0.56. This agreement is satisfactory.

Table 2. Parameters used in numerical simulation.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Aquifer</th>
<th>Aquitard</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thermal conductivity:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aquifer</td>
<td>2.29 J/m.s.°C</td>
<td></td>
</tr>
<tr>
<td>Aquitard</td>
<td>2.56 J/m.s.°C</td>
<td></td>
</tr>
<tr>
<td>Heat capacity of rock</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aquifer</td>
<td>1.81 x 10^6 J/m^3.°C</td>
<td></td>
</tr>
<tr>
<td>Aquitard</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aquifer horizontal permeability</td>
<td>63 darcys</td>
<td></td>
</tr>
<tr>
<td>Aquifer vertical to horizontal permeability ratio</td>
<td>1:7</td>
<td></td>
</tr>
<tr>
<td>Aquitard to aquifer permeability ratio</td>
<td>10^-5</td>
<td></td>
</tr>
<tr>
<td>Porosity:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aquifer</td>
<td>0.25</td>
<td></td>
</tr>
<tr>
<td>Aquitard</td>
<td>0.35</td>
<td></td>
</tr>
<tr>
<td>Storativity:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aquifer</td>
<td>6 x 10^-4</td>
<td></td>
</tr>
<tr>
<td>Aquitard</td>
<td>9 x 10^-2</td>
<td></td>
</tr>
</tbody>
</table>
PARAMETER STUDY
PRODUCTION TEMPERATURE vs TIME

Figure 3. 1981 Mobile Experiment first cycle production temperature as a function of time. Curve A shows the basic numerical simulation result, while curves B, C, and D show parameter study results described in the text. [XBL 817-3266]
Subsequent to comparing our predictions with the experimental results, we made a series of parameter sensitivity studies. Several sets of calculations were made, including:

(1) **Mesh variation.** Results are found to be nearly mesh-independent.

(2) **An arbitrary increase of aquifer permeability from 63 darcys to 94 darcys.** The calculated recovery factor is reduced from 0.62 to 0.55. The production temperature is shown as curve B in Figure 3.

(3) **Two-layered-permeability aquifer system,** in which the upper layer is 1.5 times as permeable as the lower but with an average of 63 darcys corresponding to the field value. The recovery factor is calculated to be 0.60.

(4) **Three-layered-permeability aquifer system,** in which the middle layer is 1.5 times as permeable as the upper and lower layers while keeping the average at the field value of 63 darcys. The recovery factor is calculated to be 0.62; production temperature is displayed as curve C in Figure 3.

(5) **Simulation of a large thermal dispersion effect.** We followed Sauty [15] who approximated this effect by using an effective thermal conductivity value. A value ten times the normal value was used. Based on an approximate relationship developed by Doughty et al. [9], this corresponds to a dispersion length of 3 m. The energy recovery factor is calculated to be 0.57; production temperature is shown as curve D in Figure 3.
Several additional parameter-sensitivity calculations were made. It was found that although the recovery factor can be made to reproduce the experimental data, the time rate of decrease of calculated production temperature for many alternative cases is always faster than the experimental value. After these studies, we came to the preliminary conclusion that this production-temperature discrepancy may be due to either thermal dispersion or nonisothermal, transient wellbore effects. Efforts have been initiated to study both processes. Understanding the cause of this discrepancy is important for further prediction calculations. Although the comparison of experiment and calculation may be considered satisfactory, we want to be sure that the discrepancy will not increase with changes in storage temperature or other conditions.

SUMMARY AND CONCLUSIONS

In this paper we have concentrated on reporting the results of only one of our four tasks under the STES program, the site-related studies. Considerable progress has been made in site characterization for optimization. In sites where buoyancy flow may be neglected, dimensionless parameter groups have been derived and type curves have been plotted to quickly obtain energy recovery factors and production temperatures for different conditions. In sites where buoyancy flow cannot be neglected, a semi-empirical method has been developed which reproduces the results of a realistic numerical model (CCC) over a wide range of parameters.

Much progress has also been made in predicting the results of field experiments by Auburn University at Mobile, Alabama. Calculations were able to predict, to within about 5%, the experimental value of the energy recovery
factor and the production temperature (see Fig. 3). Studies of these results disclosed a discrepancy between calculated and observed rate of decrease of production temperatures which may be due to thermal dispersion and nonisothermal transient wellbore effects. Work has been initiated to study these, since an understanding of the discrepancy is important in ensuring a satisfactory prediction for further field cases.

ACKNOWLEDGEMENTS

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REFERENCES


5. STES Newsletter, a quarterly review of seasonal thermal energy storage, Chin Fu Tsang, editor, published by Lawrence Berkeley Laboratory, Berkeley, California 94720.


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