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Title

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Permalink

<https://escholarship.org/uc/item/9z7644p6>

Journal

Renewable Energy, 130(C)

ISSN

0960-1481

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Publication Date

2019

DOI

10.1016/j.renene.2018.08.056

Peer reviewed

Corrective Receding Horizon EV Charge Scheduling Using Short-Term Solar Forecasting

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1 *Abstract*— Forecast errors can cause sub-optimal solutions in resource planning optimization, yet they are usually modeled
2 simplistically by statistical models, causing unrealistic impacts on the optimal solutions. In this paper, realistic forecast errors
3 are prescribed, and a corrective approach is proposed to mitigate the negative effects of day-ahead persistence forecast error by
4 short-term forecasts from a state-of-the-art sky imager system. These forecasts preserve the spatiotemporal dependence structure
5 of forecast errors avoiding statistical approximations. The performance of the proposed algorithm is tested on a receding horizon
6 quadratic program developed for valley filling the midday net load depression through electric vehicle charging. Throughout one
7 month of simulations the ability to flatten net load is assessed under practical forecast accuracy levels achievable from
8 persistence, sky imager and perfect forecasts. Compared to using day-ahead persistence solar forecasts, the proposed corrective
9 approach using sky imager forecasts delivers a 25% reduction in the standard deviation of the daily net load. It is demonstrated
10 that correcting day-ahead forecasts in real time with more accurate short-term forecasts benefits the valley filling solution.

11 *Keywords: Electric vehicle charging; Optimal scheduling; Solar forecast errors*

12

13 1. Introduction

14 1.1 Problem Statement and Literature Review

15

16 The variable nature of solar power is of concern to electric grid operators, where there is substantial growth in photovoltaic (PV)
17 installations. Variable power flow occurs primarily due to passing clouds. As a result, PV generation exhibits high variability,
18 leading to power quality issues such as flicker, power imbalance, reverse power flow, and increased wear on conventional voltage
19 regulator equipment at the distribution level [1, 2]. With high PV penetration, these effects aggravate and can cause challenges
20 to grid operations.

21

22 Accurate solar forecasts help grid operators integrate increased levels of solar generation while maintaining power quality.
23 However, forecast errors are inherent to any forecasting technique, and non-linear atmospheric dynamics make it challenging to
24 reduce or correct solar forecast errors. Forecast errors can be detrimental to reduce peak loads using energy storage [3-5], or
25 maximizing PV self-consumption [6]. While the characteristics of forecast errors vary with time scale and location [7, 8], grid
26 integration studies typically model forecast errors by two main approaches:

27

- 28 i. Generate an imperfect forecast by adding a synthetic error to the actual solar generation. The synthetic error is often
29 sampled from univariate distributions such as Gaussian, uniform, and Weibull [9-14]. Such error timeseries have zero
30 autocorrelation, failing to capture the autocorrelation properties of real forecast errors. Days with large forecast error
31 autocorrelation, especially persistent over-forecasts for several hours, usually present the most challenging conditions
32 for energy storage to reduce peak load [15]. On such days the energy storage system needs to discharge continuously
33 to make up for the shortfall in PV generation which may cause premature discharge, demand peaks, and associated
34 demand charges.

35

36 ii. Probabilistic modeling of errors: sophisticated statistical methods such as copula functions [16], Markov model [17],
37 enhanced Markov chain model [18] and kernel density estimation [19] are utilized to model the time series forecast.
38 However, these models do not fully capture the autocorrelation of forecast errors due to nonlinear and higher order
39 dependencies. For example, the transformation-based heuristic methodology in [20] captures the spatio-temporal
40 correlation properties of forecast errors on the day-ahead time scale, but not intra-day. Other forecast error modeling
41 considering autocorrelation include [15] where a parametric first-order autoregressive process is developed to generate
42 autocorrelated time series forecasts and [21] where a simulated autocorrelated PV forecast error through a transformed
43 multivariate ARMA model is presented.

44 1.2 Objectives and Contribution

45

46 While modeling forecast errors to support grid planning and operation studies has received much attention, corrections of the
47 impact of forecast errors in real time are typically not applied. Motivated by this, we propose a corrective approach with the
48 main contributions listed as follows:

49

50 i. We avoid statistical models of forecast errors by using a day-ahead persistence and 15 min-ahead sky imager forecast
51 to produce real forecast data which inherently preserves the temporal dependence structure of forecast errors.

52

53 ii. We apply a corrective optimization framework. The baseline day-ahead persistence forecast is corrected by three short-
54 term forecasts showcasing different levels of realistic forecast errors: day-ahead perfect forecasts, day-ahead persistence
55 forecasts corrected by imperfect short-term sky imagery forecasts, and day-ahead persistence forecasts corrected by
56 perfect short-term forecasts. This approach captures the real forecast property of improved accuracy with shorter
57 forecast horizon.

58

59 The proposed case study to implement and validate the above framework uses EVs as mobile energy storage systems (ESS).
60 Adopting ESS to compensate the mismatch between variable PV output and grid load [22, 23] has been extensively studied in
61 the past decade. For example, Nottrott et al. [24] modeled ESS dispatch schedules for peak net load minimization by linear
62 programming. Mixed-integer linear programming and quadratic programming are also commonly utilized to solve the ESS
63 scheduling problem at the distribution level [25-28]. The adoption of EV as an alternative to ESS has received significant
64 attention [29] because of low acquisition cost. The interaction between EVs and the power grid is comprehensively discussed in
65 [30]. High EV penetration can provide grid services [31] such as valley filling defined as increasing load demand during the load
66 depression [32] using unidirectional EV charging management (V1G) [33] or vehicle-to-grid (V2G) [34] schemes. We formulate
67 a typical valley filling problem through centralized [35] EV charge scheduling in a realistic, quasi-operational case study. Since
68 V2G still faces challenges such as market barriers and limited commercial availability we focus on V1G here. The impact of
69 realistic forecast errors is quantified as the deviation of the resulting valley filling solution from the ideal solution. Last, we
70 illustrate how correcting day-ahead forecasts in real time with more accurate short-term forecasts benefits the valley filling
71 solution.

72

73 1.3 Paper Organization

74

75 The remainder of this paper is organized as follows. In Section 2 we introduce the methodology for determining load demand,
76 solar forecasts, and EV charge events. Section 3.1 defines the problem statement, and sections 3.2 and 3.3 introduce a quadratic
77 programming (QP) optimization algorithm based on [28]. We extend the work by supplementing constraints for start and end
78 time of EV charging and energy demand satisfaction, and integrating a receding horizon framework. Section 3.4 introduces error
79 metrics. Section 4.1-4.2 provide a validation on a sample day, and statistical results from one month of valley filling results, and
80 the discussion of the results and limitations of the proposed methodology are given in Section 4.3-4.4. Lastly, Section 5 provides
81 conclusions and future work.

82

83 2. Problem setup and System Data

84 2.1 Geographic Setup

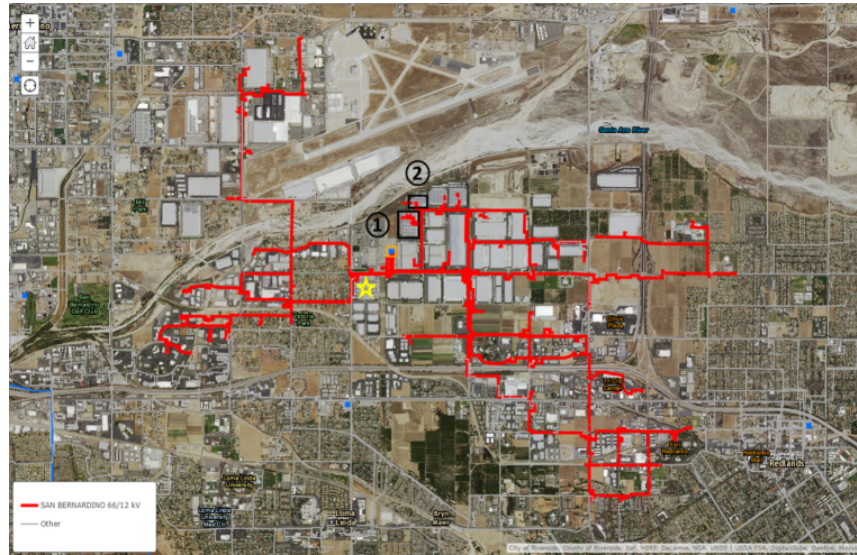
85

86 We select the region of San Bernardino located in Southern California, where Southern California Edison (SCE) installed 125
87 MW of multiple rooftop photovoltaic (PV) systems under the Solar Photovoltaic Program (SPVP) [36]. This region is home to
88 many commercial buildings, large warehouses, and abundant solar resources, which makes large PV rooftop arrays common.
89 Local distribution feeders are therefore prone to solar variability issues, making this region an ideal location for solar power

90 integration studies.

91
92 Figure 1 shows an overview of the area served by the 66/12 kV substation in San Bernardino, CA. The substation load demand
93 was simulated by EnergyPlus, a building energy simulation tool developed by the U.S. Department of Energy. Power output
94 from two SPVP systems were provided by SCE. To produce short-term solar forecasts, we use a UC San Diego Sky Imager
95 system (USI). The USI is rooftop-mounted and its field-of-view covers all buildings within the substation service territory.
96 It can be used to geolocate clouds, measure cloud velocity, and track cloud motion [37, 38]. These measurements are then used to
97 predict future cloud shadow locations and solar irradiance up to 15 min ahead. For more detailed information of solar resource
98 assessment and forecasting using the USI, refer to [39, 40].
99

100



101
102 Figure 1: Southern California Edison’s (SCE) Distributed Energy Resource Interconnection Map (DERiM) showing the San Bernardino substation service
103 territory. The substation is marked by a blue box with orange border and feeder lines emanating from that substation are in red. Rooftop PV systems (black
104 boxes) and sky imager (yellow star) are located up to 1,100 m apart. The map spans 12 x 6.5 km.

105 2.2 Solar Forecasts

106 To demonstrate the net load flattening improvement through correcting day-ahead persistence forecast by short-term forecast
107 updates, we construct four different solar generation forecasts G in 24-hour time windows representing different forecast
108 accuracy through a combination of persistence G_p , USI G_{USI} , and perfect forecast $G_{perfect}$.

- 109 1. Base Forecast (G_p): As conventionally adopted [3, 41] as a baseline for load forecasting, a 24-hour persistence forecast is
110 defined as solar power at the same time of the previous day. Persistence forecasts are expected to have the largest forecast
111 error and largest autocorrelation of forecast errors.
112
- 113 2. Operational forecasts (G_{p+USI}): The base forecast is continually updated with the most recent USI forecast. Since USI
114 forecast horizons are limited to 15 min, only the G_p in the first 15 min of the 24-hour time horizon is replaced with G_{USI}
115 while the G_p in the remaining time horizons are left unchanged. As G_{USI} is more accurate than G_p (refer to Table A-2 in
116 the Appendix), G_{p+USI} is expected to exhibit smaller forecast errors than G_p .
117
- 118 3. Benchmark forecast ($G_{p+perfect}$): Similar to the operational forecast, but the first 15 min of G_p is replaced with $G_{perfect}$.
119 $G_{p+perfect}$ is expected to exhibit even smaller forecast errors than the operational forecast. Thus it elucidates whether
120 further improvements in the accuracy of short-term forecast would result in better mitigating the impact of forecast errors
121 on the net load.
- 122 4. Perfect Forecast ($G_{perfect}$): The entire 24-hour time horizon of G_p is replaced with $G_{perfect}$, yielding zero forecast error.
123 The perfect forecast brackets the net load flattening that is achievable. If EV availability was unconstrained, $G_{perfect}$
124 would yield a flat net load curve.

2.3 EV Fleet

We focus on workplace charging of EVs during regular business hours coinciding with times of peak PV production. A fleet of EVs connected to workplace charging stations is simulated. The EV make and models and their battery capacity and charge rates are selected based on the EV market share in the US as of 2015 (Table A-1).

Arrival time, layover duration, and the initial state of charge were sampled from the following distributions: 1) EV arrival time varies between 06:00 PST and 10:00 PST centered on a mean arrival time of 07:30 PST with a standard deviation of 1 h. 2) layover duration spans from 6 to 11 hours centered on 8 hours with a standard deviation of 1 h. 3) initial state of charge (χ_0 , in %) ranges from 0-100% centered on 60% with a standard deviation of 10%. The energy demand is derived assuming a full charge by the departure time. The resulting EV charging events are replicated for all 30 days of analysis. Since most employee day-to-day schedules are repetitive, the persistence of daily charging events is a reasonable assumption.

2.4 Summary of Data Sources and Availability

Table 1 provides an overview of the load, PV generation, and EV energy demand datasets. Because PV generation data is complete only for April 2013, the full month is selected for our analysis. During this month, there were 2 overcast days, 13 clear days, and the remaining 15 days were partly cloudy. The simulated substation loads were scaled down by a factor of 150x from 5.4 MW to 36 kW and PV data were also scaled down by 75x from 7.5MW to 100 kW so that the 31 EVs in Table A-1 are able to fill the entire energy valley on a clear day.

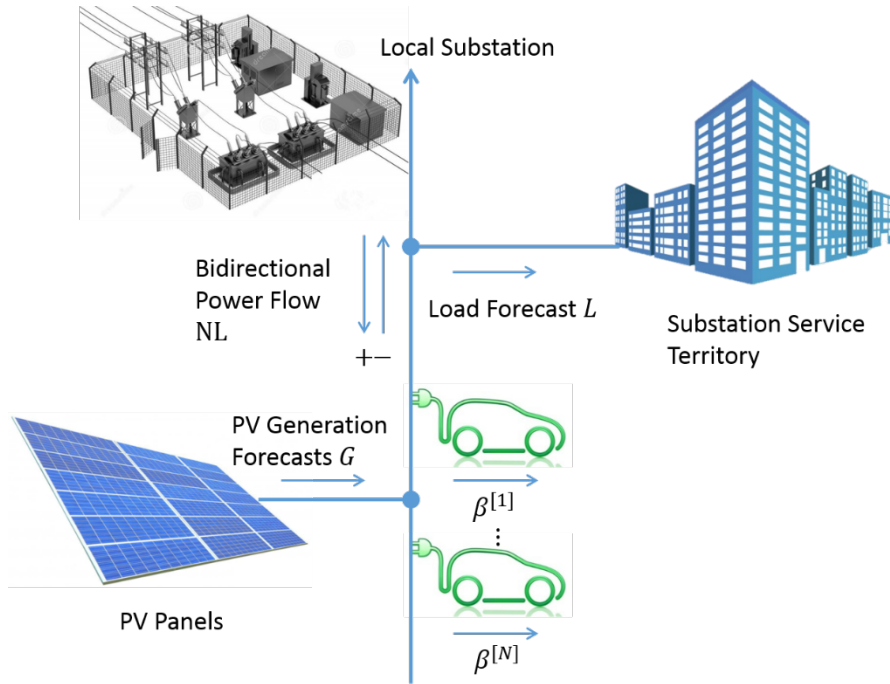
Table 1: Catalog of the datasets and their native temporal resolution. All data are interpolated to 15 min temporal resolution. The rated EV charge capacity is determined by the sum of the charge rates in Table A-1.

Data Source	Rated Capacity	Scale Factor	Average Daily Power	Type	Original Time Resolution
Loads	5.4 MW	150	23 kW	Simulated	60 min
PV Generation	7.5 MW	75	13 kW	Measured	30 s to 2 min, irregularly spaced
USI PV Forecast	7.5 MW	75	13 kW	Measured Sky Images	30 sec
EV Charge Capacity	0.23 MW	1	19 kW	Simulated	5 min

3. Methodology

3.1 Problem Setup

To test our proposed approach, we formulate a valley filling optimization problem to schedule EV charging. Figure 2 schematically illustrates the problem configuration. The load demand estimate L for all buildings connected to the distribution feeder is offset by PV systems injecting power G . The substation is assumed to allow bidirectional power flow (i.e. net load NL , positive if delivering power and negative for reverse power flow). $NEVs$ draw charge power $\beta^{[N]}$ from the distribution grid. The arrowheads indicate positive power flow. As V2G (i.e. Vehicle to Grid charging) still faces challenges such as market barriers and limited commercial availability, we focus on V1G (unidirectional EV charging) in this study. However, EV discharging functionality is supported in the optimization framework.



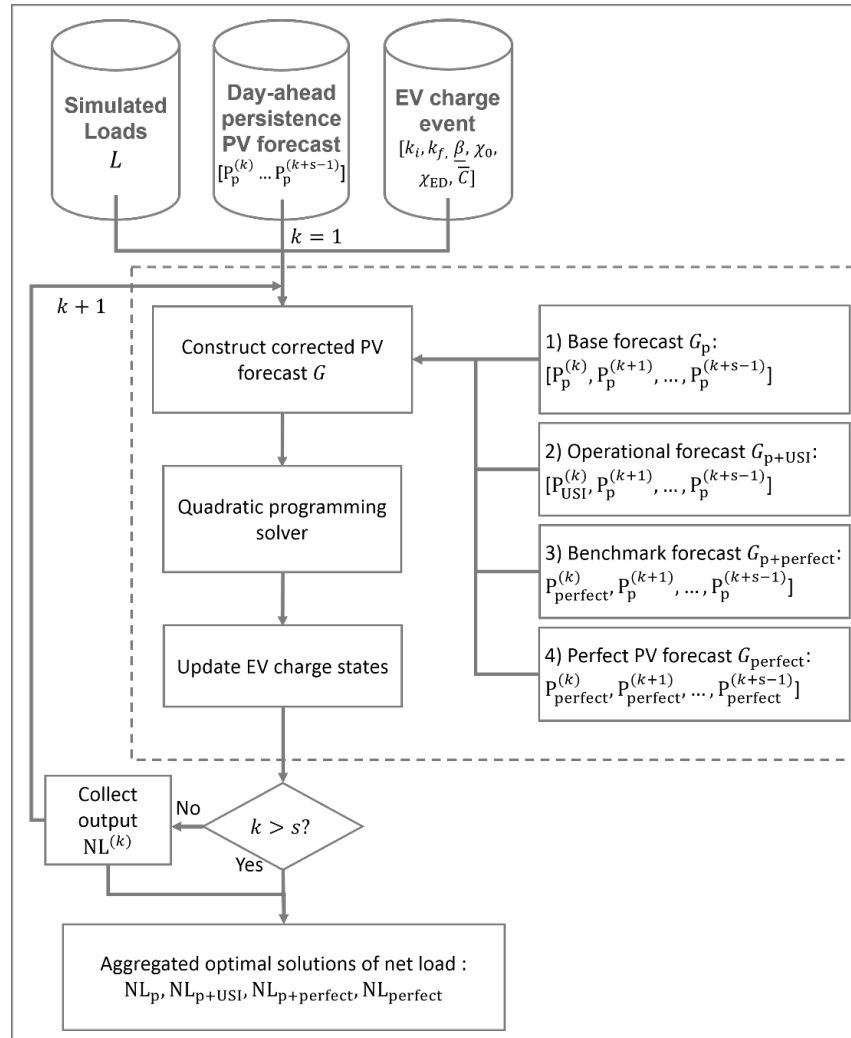
160
161 Figure 2: Notation and topology of the proposed optimization problem.

162
163 From Figure 2, the following power balance between the four power variables always holds true:

$$NL = L + \boldsymbol{\beta} - G, \quad 1$$

164 where EV charge power $\boldsymbol{\beta} = [\beta^{[1]} \dots \beta^{[N]}]$. As we are interested in a day-ahead optimal valley filling solution, the total length
165 of the planning horizon is 24 hours as in $s = 96$ steps at a temporal resolution Δ of 15 min (0.25 h), consistent with the USI
166 forecast horizon. The time index $T_k = k\Delta$. The power variables in Eqn. 1 at each time index represent the average power output
167 over the period from a time index ahead to present, expressed as $((k-1)\Delta, k\Delta)$, where $k \in [1 \dots s]$. For example, the power
168 balance at the first time index T_1 considers the average power output between midnight $0\Delta = 00:00$ h and $1\Delta = 00:15$ h. Refer to
169 Figure 4 for detailed illustration of planning horizon, temporal resolution and time step.

170
171 Figure 3 illustrates the schematic overview of the proposed study. The study solves the valley filling optimization problem with
172 individual input of four solar forecast scenarios (section 2.2) G_p , G_{p+USI} , $G_{p+perfect}$, and $G_{perfect}$, and compares the resulting
173 bidirectional net load NL_p , NL_{p+USI} , $NL_{p+perfect}$, and $NL_{perfect}$ respectively.
174



175
176 Figure 3: Flowchart of the proposed corrective approach. Refer to Table A-1 for the EV charge events.

177
178 **3.2 Mathematical Formulation of the Optimization Algorithm**

179 Battery scheduling to reduce peak load and minimize energy bills has been implemented through a variety of optimization
180 algorithms [42]. Considering potential future applications of implementing financial incentives and prioritizing EVs, we prefer
181 a framework which naturally supports weighting different objectives. Therefore, quadratic programming (QP) is selected owing
182 to its flexibility:

$$\min_x h(x - f)^2, \quad 2$$

183 where x is a vector of grid net load NL and EV charge power β of each EV (see Eqn. 6), and h is the corresponding matrix of
184 weighting factors. While the weighting factor is not activated in this paper, it enables future implementation of economic
185 objectives that allow trade-off between the decision variables (e.g., price, charge power). Thus, the weighting matrix h is set to
186 a $(1 + N)s \times (1 + N)s$ matrix with an $s \times s$ identity matrix I_s included in the top left corner for grid and zero elsewhere for
187 EV.

$$h = \begin{bmatrix} I_s & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & 0 \end{bmatrix} \in \mathbb{R}^{[(1+N)s \times (1+N)s]} \quad 3$$

188 In Eqn. 2, f is a vector composed of the preferred grid net load profile followed by preferred EV charge power. It defines the
189 power target for the objective function. Ideally, the optimized grid net load profile should be a flat line in case of perfect forecasts
190 (i.e. load forecast and solar forecast) and unrestricted EV availability. However, as discussed earlier, real solar forecasts have

191 errors, and also EV availability can be restricted depending on EV owner's work schedule. The resulting mismatch between the
 192 EV energy demand and the energy valley magnitude forces the optimized net load to deviate from a flat line (see Section 4). The
 193 preferred grid net load f should therefore be dynamically updated to align the future charge schedule with the remaining PV
 194 generation and EV charging needs, and is defined as

$$f_{(k)} = \begin{bmatrix} r \\ 0 \\ \vdots \\ 0 \end{bmatrix} \in \mathbb{R}^{(1+N)s}, \quad 4$$

195 where $r = [r, \dots, r]^T \in \mathbb{R}^s$ is the grid net load target with identical scalar element r , which is determined from the expected net
 196 load ($L - G$) and the cumulative EV energy demand (χ_{ED}) for the time period from the current time step (t_k) to when the last
 197 EV disconnects (t_{end}):

$$r = \frac{\sum_{t_k}^{t_{end}} L - G + \chi_{ED}}{t_{end} - t_k}. \quad 5$$

198 r is not computed before the first EV connects (t_{start}) and after the last EV disconnects (t_{end}), i.e. $t_{end} > t_k > t_{start}$, because
 199 we perform valley filling only during the EV layover time. As r assumes equal EV availability and charge rate capacity from
 200 present to the departure time of the last EV, the final optimized net load is expected to deviate slightly from the dynamic r even
 201 with a perfect solar forecast. The deviation is caused by EV departures that limit the available charging capacity. A detailed
 202 discussion is provided in Section 4. The remaining elements in Eqn. 4 are set to zero, indicating that individual EVs can draw
 203 power up to the maximum charge power capacity.

204 To proceed, x in Eqn. 2 is the decision variable consisting of temporal aggregated grid power load and all EV charge power.

$$x = \begin{bmatrix} NL \\ \beta^{[1]} \\ \vdots \\ \beta^{[N]} \end{bmatrix} \in \mathbb{R}^{(1+N)s} \quad 6$$

205 $NL = [NL_{(1)}, \dots, NL_{(k)}]^T$ and EV charge power follows $\beta^{[N]} = [\beta_{(1)}^{[N]}, \dots, \beta_{(k)}^{[N]}]^T$ where $k \in [1, \dots, s]$, N is the number of EVs,
 206 and parenthesis () indicate the time index.

207 The charge power β of each EV in Eqn. 6 is subject to the following five constraints (i.e. Eqns. 7-11). First, the EV charge power
 208 is limited to its maximum charge capacity. Because discharging is not considered, the EV charge rate constraint for all time steps
 209 k is:

$$0 \leq \beta_{(k)} \leq \bar{\beta}, \quad k \in [1, \dots, s] \quad 7$$

210 where $\bar{\beta}$ is the maximum of the rated charge capacity of the battery or charging station.

211 Second, the state of charge (SOC) of the battery is constrained by:

$$\underline{C} \leq \chi_0 \cdot \bar{C} + \sum_{k=1}^s \beta_{(k)} \cdot \Delta \leq \bar{C}, \quad k \in [1, \dots, s] \quad 8$$

212 where χ_0 is the initial SOC in %, \bar{C} is maximum SOC conventionally defined as the EV battery capacity and the minimum SOC
 213 \underline{C} is assumed to be 0. The EV battery capacity is assumed to equal the amount specified by the vehicle manufacturer. Battery
 214 degradation is assumed to be negligible.

215 Third, the charging has to occur within the constraints of the EV layover time. If the EV connects at time index k_i , no charging
 216 can occur during the period $[T_1, T_{k_i}]$. In other words, EV charge power equals to 0 prior to connecting at $k = k_i$:

$$\sum_{k=1}^{k_i} \beta_{(k)} \cdot \Delta = 0. \quad 9$$

217 Fourth, similarly given EV departure time index k_f , the EV battery charge is constrained to 0 after disconnecting at $k = k_f$:

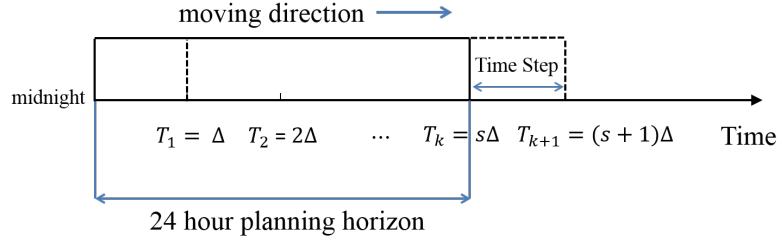
$$\sum_{k=k_f}^s \beta_{(k)} \cdot \Delta = 0. \quad 10$$

218 Last, the power supplied to the EV during the layover period equals the energy requested by the EV owner. We assume that all
219 EV owners request a fully charged battery.

$$\sum_{k=1}^s \beta_{(k)} \cdot \Delta = \chi_{ED} \quad 11$$

220 3.3 Receding Horizon Optimization Algorithm

221
222 To support the proposed corrective approach, a RHC algorithm is required [43-45]. The RHC algorithm modifies the control
223 action with respect to predicted solar energy generation while satisfying constraints over a time window of fixed length 24 h.
224 We use a moving time window resembling the receding horizon mechanism of RHC. The simulations are initialized at midnight
225 and the time window moves forward one step at a time, as presented in Figure 4.



226
227 Figure 4: Illustration of receding horizon time window. Refer to Section 3.1 for definitions of the notations.

228 The iterations in RHC demand a fast optimization solver and real time application can be limited by the number of constraints
229 and EVs. With 31 EVs, each iteration takes 1.5 s on an Intel I5 workstation, and a full day completes in 2.5 min. The computation
230 cost scales with the number of variables (i.e., the number of EVs).

231 3.4 Forecast and Valley Filling Benchmark

232
233 The valley filling performance is evaluated as follows. The accuracy of the solar forecasts is characterized by nRMSD e^G , which
234 is the root mean square difference normalized by the average solar power measurements:

$$e^G(\text{day}) = \frac{\sqrt{\frac{1}{s} \sum_{k=1}^s [G_{\text{forecast}}(k) - G_{\text{perfect}}(k)]^2}}{\frac{1}{s} \sum_{k=1}^s [G_{\text{perfect}}(k)]} \times 100\%. \quad 12$$

235 Similarly, the nRMSD for optimized net load e^{NL} is defined as:

$$e^{\text{NL}}(\text{day}) = \frac{\sqrt{\frac{1}{t_{\text{end}} - t_{\text{start}}} \sum_{k=t_{\text{start}}}^{t_{\text{end}}} [\text{NL}_{\text{imperfect}}(k) - \text{NL}_{\text{perfect}}(k)]^2}}{|\max(\text{NL}_{\text{perfect}}(k))|} \times 100\%. \quad 13$$

236 Thus, the nRMSD of valley filling using imperfect solar forecasts NL_p , $\text{NL}_{p+\text{USI}}$, and $\text{NL}_{p+\text{perfect}}$ can be evaluated by e_p^{NL} ,
237 $e_{p+\text{USI}}^{\text{NL}}$, and $e_{p+\text{perfect}}^{\text{NL}}$ respectively. Note that only the net load at the first time step (15 min) of all time windows is evaluated in
238 Eqn. 13 which means that at each index k , the solar forecasts for 15+ min horizon do not influence e^{NL} .
239

240 We also evaluate the net load variability as the average square of the deviation between the optimized net load and the idealized
241 valley filling result. The resulting metric σ^{NL} is the standard deviation of the optimized net load:

$$\sigma^{\text{NL}}(\text{day}) = \sqrt{\frac{1}{N} \sum_{k=t_{\text{end}}}^{t_{\text{start}}} [\text{NL}(k) - \overline{\text{NL}}]^2}, \quad 14$$

242 where $\overline{\text{NL}}$ is the average net load from t_{start} to t_{end} , and N is the number of time indices in between. Small σ indicates smoother
 243 net load profiles, and $\sigma = 0$ indicates a completely flat net load profile. The net load standard deviations after valley filling using
 244 solar forecasts NL_p , $\text{NL}_{p+\text{USI}}$, $\text{NL}_{p+\text{perfect}}$, and $\text{NL}_{\text{perfect}}$ are evaluated by σ_p^{NL} , $\sigma_{p+\text{USI}}^{\text{NL}}$, $\sigma_{p+\text{perfect}}^{\text{NL}}$, and $\sigma_{\text{perfect}}^{\text{NL}}$, respectively.
 245 Eqns. 13 and 14 are evaluated only during the maximum layover period (i.e. from t_{start} to t_{end}) when the energy valley can be
 246 filled.
 247

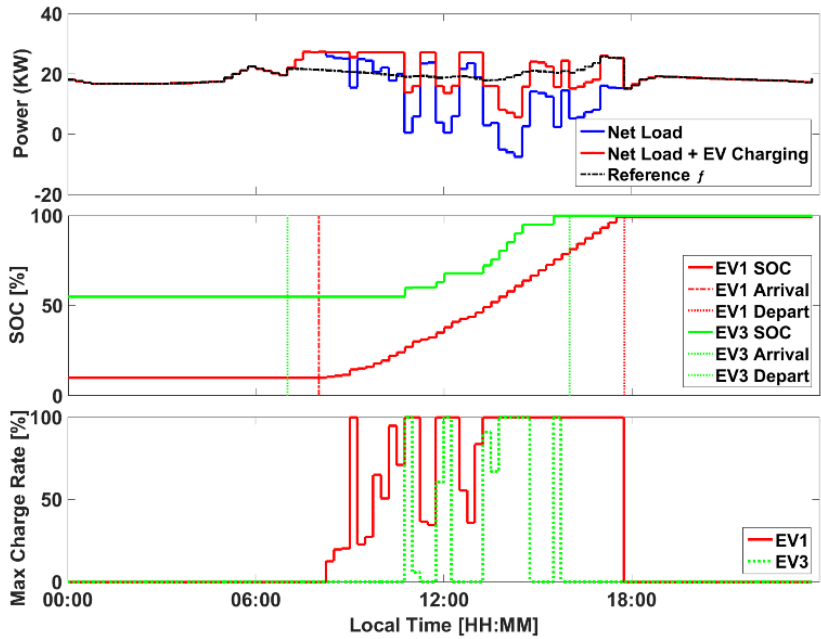
248 4. Results and Discussion

249 4.1 Case Study

250 The methodology discussed in Section 3.3 is first applied to a single day with the perfect forecast scenario G_{perfect} . Apr 1, 2013
 251 was a day with broken cumulus clouds, producing high PV output variability. Figure 5 shows the valley filling results by smart
 252 charging EV 1 and EV 3 defined in Table A-1. The algorithm dynamically schedules charging during energy valleys while
 253 obeying all constraints. Specifically, the grid net load profile on the top (subtracting actual PV power G_{perfect} from the feeder
 254 load profile L) shows an energy valley during midday interrupted by episodes of cloud cover. The area between blue and red
 255 indicates the share of the energy valley that is absorbed by coordinating charging of 2 EVs.
 256

257 EV 3 has a small energy demand of 7.7 kWh, but the layover period of 9 hours is comparably long since EV 3 only requires 2 h
 258 20 min of charging at the highest charging rate to reach full charge. Thus, the algorithm can schedule charging to occur only
 259 during the four major energy valleys (clear periods during midday) while reducing charging power to zero in cloudy conditions
 260 and at the beginning and end of the day. EV 3 is fully charged 2 h prior to its planned departure.
 261

262 On the contrary, EV 1 has much less charging flexibility with a larger energy demand (76.5 kWh or 7 h 39 min of charging at
 263 maximum capacity), which is spread over a similar layover period of 9 hours 40 min. Thus, the algorithm has limited flexibility
 264 (2 hours) to shift the battery charge schedule and/or reduce the charge rate. EV 1 connects to charge at 08:00 PST, and charging
 265 occurs from 08:15 PST when PV generation starts to depress the net load profile. The 2 h flexibility is used to charge at a rate
 266 below the maximum capacity from 08:15 to 13:30 PST. By lowering the charge rate, the algorithm shifts EV charging from
 267 times of relatively large net load to times with a larger energy valley later in the day. The algorithm boosts charge power of EV
 268 1 to maximum capacity after 13:30 PST so that EV 1 can reach full charge right at its planned departure. Note that limited EV
 269 flexibility prevents the algorithm from completely shifting the EV charging to periods with larger energy valleys and it schedules
 270 charging also during off-peak solar generation (08:00 – 10:45 PST).
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Figure 5: Sample optimized EV charge schedule for valley filling with 2 EVs. Top: Original grid net load profile showing an energy valley (blue), filling the valley towards a reference power (f , black) yields optimized net load (red). The PV output profiles are scaled down by a factor of 260x to create a reasonable energy valley for just two EVs. Middle: EV state of charge in %. Colors distinguish EV with their arrival time (dashed) and departure time (dotted). Bottom: EV charge power normalized by its maximum charge capacity.

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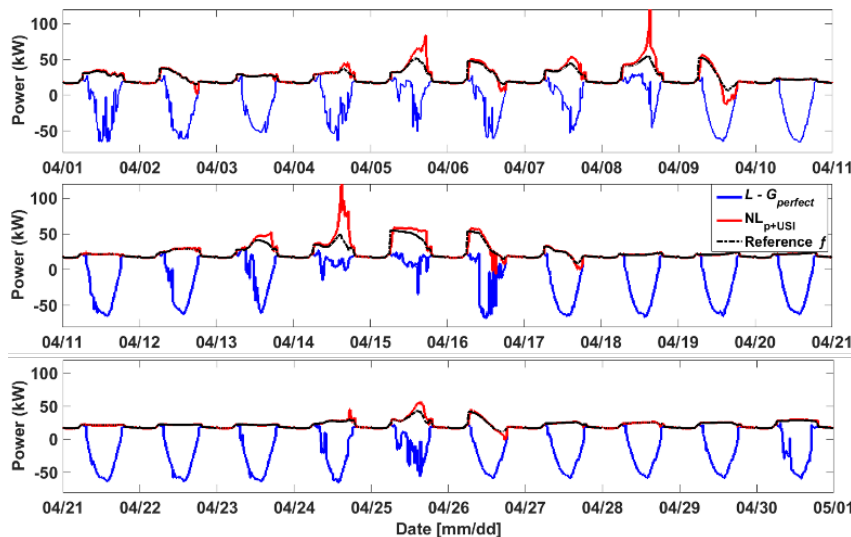
For this case, the power reference is unachievable due to the small number of EVs and restricted charge schedule for EV 1. But the algorithm's functionality and ability to reduce net load variability by shifting the charge schedule with respect to the energy valley availability is confirmed.

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4.2 Monthly Results and Statistics of Forecast Error Correction

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Now we consider a full month, 31 EVs (Table A-1 in the Appendix), and four solar forecast scenarios. For readability, only scenario NL_{p+USI} is presented in Figure 6. On most days, valleys are completely filled, and optimized net load is closely aligned with the reference f indicating that the method works as designed. On clear days (e.g., Apr 21 – Apr 23), the energy valley is sufficiently large to charge all EVs, yielding a flat net load. On partly cloudy days (e.g., Apr 1 and Apr 4), solar variability is large, and less energy is available in the valley, resulting in increased and fluctuating optimized net load.



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Figure 6: Results for one month of valley filling with forecast errors corrected by USI (using G_{p+USI}). The original grid net load without EV (blue) is flattened by scheduling EV charging to achieve a preferred net load profile (black), resulting in reduced net load variability (red).

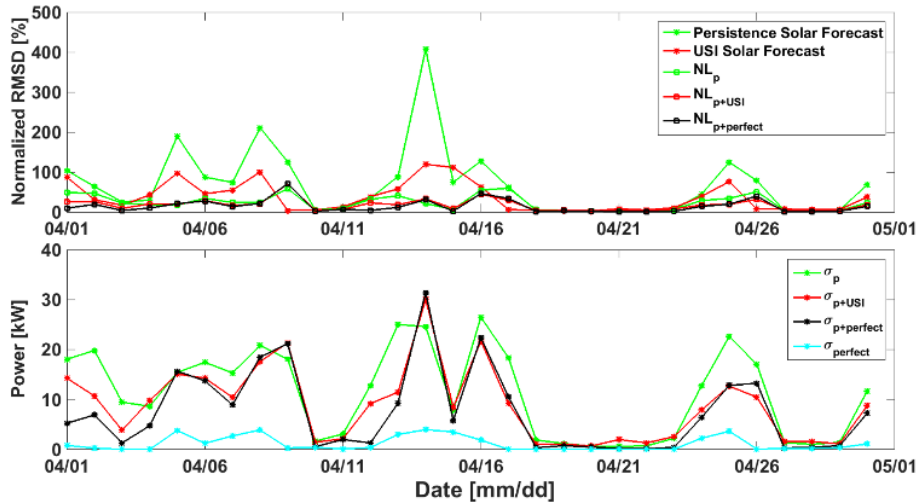
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Table 2 summarizes the monthly performance and a detailed day-by-day performance comparison is presented in Figure 7. The statistics of PV forecast errors and resulting valley filling performance are further investigated in the following sub-sections.

Table 2: Monthly summary of solar forecasts accuracy and optimized net load variability under different forecast error scenarios.

	Persistence Forecast	USI Forecast	NL _p	NL _{p+USI}	NL _{p+perfect}	NL _{perfect}
nRMSD e [%]	68.2	37.2	23.1	17.5	14.1	N/A
Std. σ [kW]	N/A	N/A	11.7	8.8	7.3	1.1

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Figure 7: Monthly comparison of nRMSD (top, Eqn. 13) and net load variability (bottom, Eqn. 14). Line colors distinguish solar forecasts scenarios (Section 2.1). See Table A-2 for the same information in tabular form.

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4.2.1 Persistence and USI PV Forecast Accuracy

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Overall, the USI solar forecast outperforms 24-hour persistence on 17 out of 30 days. While the persistence forecast outperforms USI by an average nRMSD of 6.2 percentage points (30.8%) on the remaining 13 days, the USI solar forecast lowers monthly average nRMSD by 31.0 percentage points (45.4%) placing it about halfway between persistence and perfect forecast. In general, the solar forecast results confirm our expectation that correcting persistence forecast by USI forecast reduces forecast error.

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4.2.2 Valley Filling with USI Forecast Correction

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Overall, NL_{p+USI} delivers monthly nRMSD and σ averages of 17.5% and 8.8 kW, which are 24.2% and 24.8% below NL_p, respectively. The optimization for NL_p and NL_{p+USI} forecasts performs similarly for mostly clear days and errors are small; specifically, both NL_p and NL_{p+USI} yield low error and variability averages less than 5.0 percentage point and 2.0 kW, respectively. On the 15 partly cloudy days NL_{p+USI} outperforms NL_p by 33.0% and 32.7%. While NL_{p+USI} performs worse than NL_p on some of the days when sky conditions in present day significantly differ from a day earlier (Apr 5, 8, 9, 14, 16, 25 and 26, see Section 4.3), the average error reductions of NL_{p+USI} over NL_p on these days are still 7.9% and 11.2% for nRMSD and σ , respectively. Note that the large improvement in solar forecast accuracy by the USI over persistence forecast (45.4%) does not translate to an equal improvement in optimized net load variability, which will be discussed in Section 4.4.

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4.2.3 Valley Filling with Perfect Forecast Correction

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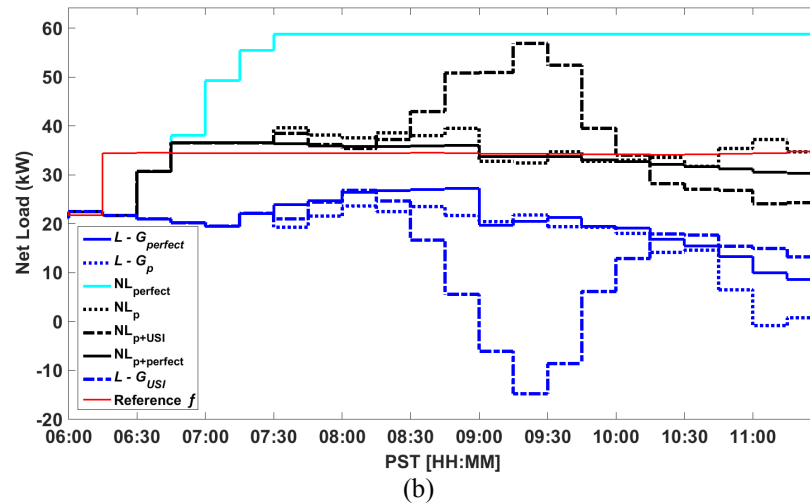
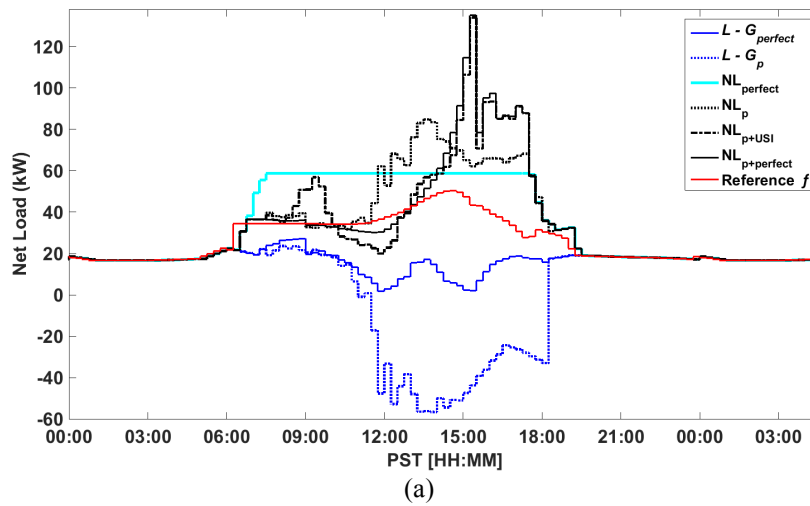
The error reductions by NL_{p+perfect} over NL_{p+USI} are relatively smaller (19.4% and 17.0% less with respect to nRMSD and σ). The fact that NL_{p+USI} is closer to NL_{perfect} than NL_p demonstrates the feasibility of operational forecast deployment of USI forecasts.

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327 Valley filling with perfect 24-hour forecasts performs the best as expected with monthly average σ_{perfect} of 1.1 kW. Although
 328 NL_{perfect} may be expected to be perfectly flat with zero variance, the optimized net load in the morning and evening usually
 329 ramps up and down over a finite time period (e.g. cyan in Figure 8a), causing non-zero variance. This ramp is a result of limited
 330 EV availability just after the first EV connects and before the last EV disconnects. For example, just the first EV by itself is not
 331 capable of dispatching sufficient charging power to follow a desired power r that is determined by spreading the energy of all
 332 EVs over the entire charging interval.

333 4.3 Characterization of Solar Forecast Error Impacts

334
 335 The proposed receding horizon optimization with forecast error corrected by more accurate short-term forecasts (G_{p+USI}) is
 336 generally effective in filling the energy valley. Exceptions are observed on Apr 5, 8, 9, 14, 16, 25, and 26 with a large peak in
 337 the optimized net load (Figure 6). To understand the challenges of the optimization on those days and further investigate the
 338 negative impact of solar forecast errors, we showcase a detailed example for Apr 14 in Figure 8.



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Figure 8: Comparison of valley filling performance using different solar forecasts (i.e. G_p , G_{p+USI} , $G_{p+perfect}$, $G_{perfect}$) on Apr 14 (a) and zooming in to the period from 06:00 to 11:00 PST (b). Line styles distinguish solar forecast scenarios, and blue and black colors differentiate net load with and without EV charging, respectively. The perfect net load forecast (load minus perfect PV forecast, solid blue) yields the ideal optimized net load (cyan).

346 On Apr 14, the baseline forecast G_p predicts large PV generation and net load valley (dotted blue) while this day is actually
 347 overcast with limited excess energy (solid blue). Between 06:30 PST and 12:00 PST, operating under the assumption of
 348 persistence forecast for >15 minute horizons, the algorithm expects a large energy valley later in the day. Therefore, it delays
 349 most of the non-critical EV charging while maintaining a flat net load profile. Because G_p is close to G_{perfect} (i.e. dotted blue
 350 follows solid blue) until 12:00 PST, the EV charging is on an ideal trajectory; if the excellent accuracy of G_p had continued, the
 351 valley filling would have flattened the net load across the day. However, after 12:00 PST, G_p deviates from G_{perfect} . Even though
 352 the energy valley is in fact not available, the forecasts still predicts an abundant energy valley from 12:00 until 18:00 PST, thus

353 EV charging is postponed to that time. The charge rate for each interval roughly equals the difference between f and G_p .
354 Therefore, the variations in the resulting valley filling scenario NL_p , mirror the difference between perfect net load forecast
355 ($L - G_{\text{perfect}}$) and persistence net load forecast ($L - G_p$). The peak error in G_p corresponds to the largest net load peak in NL_p at
356 about 13:30 PST.
357

358 On this day, the day-ahead forecast error correction actually worsens the net load variability. Starting from 12:00 PST, when G_p
359 is replaced with the USI forecast G_{USI} or the perfect forecast G_{perfect} for the next 15 min, the energy valley forecasted by G_p for
360 the next 15 min is no longer available. Therefore, the optimization delays scheduling EV charging at the present time step,
361 because it still expects an energy valley 15+ minutes from now (where G_p has not been updated yet). At the next time step, the
362 situation is similar and EV charging is again rescheduled for later. Thus, non-critical EV charging is delayed until 13:30 PST
363 when a number of early-departure EVs start to approach their charge time limit. Since those EVs must start to charge at their
364 maximum charge capacity immediately to be fully charged (refer to Eqn. 11 for the constraint) by their planned departure time,
365 the algorithm has to schedule those EVs immediately, independent of load flattening objectives, causing a steep net load rise.
366 After 16:00 PST, another set of EVs approach their charge time limit, resulting in a second peak. Overall the resulting net load
367 profiles $NL_{p+\text{USI}}$ and $NL_{p+\text{perfect}}$ resemble that of a maximum delay strategy, causing most EVs to concurrently charge at their
368 full charge rate. On the contrary, operating under G_p only causes the algorithm to allocate the charge power more equally across
369 the afternoon, reducing the peak in the corresponding optimized net load profile NL_p (dotted black). Consequently NL_p shows
370 lower σ (24.6 kW) than $NL_{p+\text{USI}}$ and $NL_{p+\text{perfect}}$ (30.0 kW, 30.4 kW, Table A-2). Lastly, the perfect forecast G_{perfect} (solid blue)
371 yields a perfect valley filling NL_{perfect} (cyan) during the EV layover time ($\sigma \cong 0$).
372

373 The subtle difference between the impacts of the three imperfect solar forecast inputs G_p , $G_{p+\text{USI}}$ and $G_{p+\text{perfect}}$ on the resulting
374 net load profiles is further analyzed in Figure 8b by zooming into the period from 06:00 to 11:00 PST. Before 07:30 PST, the
375 lack of PV power output makes all optimized net load profiles identical. However, the algorithm still schedules to charge early-
376 arrival EVs because of overall insufficient energy valley across the day, pushing the grid net load upward. Later on at 07:30 PST,
377 PV starts generating power and because G_p and G_{USI} forecast errors differ, G_p , $G_{p+\text{USI}}$ and $G_{p+\text{perfect}}$ exhibit small optimized net
378 load valleys. The original net load differences (all in blue) carry through to the resulting optimized net load profiles NL_p , $NL_{p+\text{USI}}$
379 and $NL_{p+\text{perfect}}$ (all in black). From 08:30 to 10:30 PST, erroneous G_{USI} causes a predicted net load valley (dashed blue), so the
380 algorithm schedules EVs to charge, producing a net load peak (dashed black) at 09:00 PST. After 10:30 PST, the net load peak
381 starts to diminish as G_{USI} starts to mostly follow G_{perfect} again. During the entire morning the valley filling resulting from the
382 three imperfect solar forecasts deviates significantly from the idealized result (cyan). If the algorithm understood the true solar
383 generation from the beginning of planning horizon, it would schedule the charging much earlier in the day and flatten the entire
384 net load profile. This comparison further demonstrates the negative impact of forecast errors on flattening grid net load.
385

386 Furthermore, the day discussed in Figure 8 illustrates the relationship between day-to-day change in sky conditions (larger and
387 more auto-correlated error in base forecast) and net load peaks (refer to Figure 6 and Appendix Table A-2). On Apr 14 (the first
388 of two consecutive overcast days of Apr 14 and Apr 15), the persistence solar forecast error, e_p^G is large (241% greater than
389 $e_{p+\text{USI}}^G$) because cloud conditions change from a clear day with few thin cirrus (Apr 13) to an overcast day with thick clouds.
390 The high persistence error results in a large evening peak in optimized net load with σ_p^{NL} of 24.6 kW. On Apr 14, correcting base
391 forecast by better sky imagery forecasts actually worsens the net load variability ($\sigma_{p+\text{USI}}^{\text{NL}} = 30.0$ kW). However, on the second
392 overcast day (Apr 15), the persistence forecast performs better (74 percentage points), consequently both NL_p and $NL_{p+\text{USI}}$
393 performs better with σ_p^{NL} and $\sigma_{p+\text{USI}}^{\text{NL}}$ reduced to 7.8 kW and 8.4 kW, and large net load peaks are eliminated. Similar load peaks
394 occur on other days with changes in day-to-day sky conditions. If the present day is cloudier than the previous day, the day-
395 ahead persistence forecast will cause the algorithm to push the EV charging peak forward (Apr 5, Apr 8, Apr 14, Apr 25).
396 Conversely, if the present day has less clouds than the previous day, the persistence forecast will push the peak backward (Apr
397 9, Apr 16, Apr 26).

398 4.4 Discussion and Potential Limitations 399

400 The autocorrelation of the forecast error, i.e. persistent over- or underforecasts over a few hours, causes the largest deviations in
401 optimized net load with erroneous forecasts from the optimized net load with perfect forecasts. Section 4.2 verifies that the
402 forecast error structure is an important determinant of optimized net load variability. For example, as observed in Figure 8, if
403 clear sky is predicted on a cloudy day, then the midday net load depression is over-forecast and EV charge schedule in the
404 morning would be unnecessarily delayed. In the valley filling literature, forecast errors have mostly been modeled through
405 statistical approaches. When forecast errors are sampled from a distribution such as in [11], then the forecast error autocorrelation

406 is around zero making it more likely to happen that an overforecast during one interval is balanced by an underforecast in the
407 following intervals. While forecast errors with zero autocorrelation will result in temporary small deviations in optimized net
408 load, these idealistic forecast errors are unlikely to produce the cumulative effects that results in dramatic optimized net load
409 deviations. This means that simple statistical models in the valley filling literature degrade the autocorrelation of forecast data,
410 resulting in optimistic solutions.

411
412 The proposed corrective approach and the use of the realistic forecast data reveal that the deviation of practical valley filling
413 performance from the ideal valley filling is tied to three conditions: 1) EV charging flexibility. Because of the constraint to
414 satisfy EV energy needs, EVs with short layover periods and large energy needs limit scheduling flexibility. EV charging
415 inflexibility prevents the load flattening objectives from being fully met even with perfect forecasts. 2) Accuracy of day-ahead
416 forecasts. Large changes in cloud conditions on two consecutive days worsen day-ahead persistence forecasts, leading to large
417 peaks in optimized net load. 3) Accuracy of the short-term forecast. Reducing forecast error by short-term forecast generally
418 yields better valley filling performance (Figure 7).

419
420 For a more accurate valley filling problem, the following improvements should be considered. 1) Accelerated adoption of EVs
421 is needed to provide adequate amounts of controllable loads. In this work, the load and PV generation data had to be scaled down
422 significantly for 31 EVs to just fully balance the energy valley. More financial incentives are necessary to encourage adoption
423 of the smart charging standards. 2) The load demand timeseries was simulated through an energy simulation tool because feeder
424 load data are typically not published by distribution system operators. As the simulated data may lack real power variability, the
425 value of smart charging may be higher than shown in this paper. 3) Last, integrating economic incentive and EV battery aging
426 models in the framework can make the study more comprehensive.

427 428 **5. Conclusions**

429
430 Electric utilities are experiencing unprecedented growth in the adoption of grid-connected solar PV. Solar forecasts are essential
431 to the integration of PV and balancing supply and demand. This paper successfully demonstrates a corrective approach to
432 mitigate negative impacts of day-ahead forecast errors using a sky imager based forecasting technique. The proposed
433 methodology was tested against 24-hour persistence solar forecasts with one month of PV generation and substation load data.
434 We showcase smart EV scheduling as a promising mechanism for absorbing the net load depression created by high PV
435 penetration. This study differs from the literature regarding the forecast error modeling as we use real data to preserve
436 autocorrelation characteristics of forecast errors and avoid statistical approximations. Our primary findings are:

- 437
438 i. Realistic forecast errors prevent the optimal charge strategy from flattening the net load.
439
440 ii. More accurate short-term forecasts input to the corrective receding horizon optimization reduce net load variability.

441
442 Correcting the day-ahead persistence forecasts by sky imager forecasts for 15 min horizons reduces net load variability on 20
443 out of 30 days, and presents comparable results on the remaining days which are mostly clear. On average over the month, the
444 standard deviation of the net load profile is reduced by 24.7%. On the 15 partly cloudy days, the short-term forecast correction
445 reduces net load variability by 32.7%. On clear days, the proposed correction scenario optimizes net load variability to be below
446 3.0 kW given a scaled energy valley of 50 kW, which is only 1.5 kW worse than for a perfect forecast correction.

447
448 For future work, we will use real EV charge events and EV charging forecasts. More accurate day-ahead solar forecasts generated
449 by numerical weather prediction and machine learning techniques will also be pursued. Because sub-optimal charging strategies
450 worsen the net load variability, understanding possible variations associated with forecast errors around a single deterministic
451 strategy will be of great benefit to grid operators. Finally, a stochastic optimization framework that integrates probabilistic PV
452 forecast and EV availability and demand forecasts allows a more robust valley filling.

453

Appendix:

Table A-1: Daily EV charging events database. Refer to Section 3 for a detailed definition of the variable names.

ID and EV Model	Arrival Time k_i [PST]	Departure Time k_f [PST]	Charge capacity β [kW]	Rate of Charge χ_0 [%]	Initial State of Charge χ_0 [%]	Energy Demand χ_{ED} [kWh]	Battery Capacity \bar{C} [kWh]
1: Tesla Model S	08:00	17:40	10	10	10	76.5	85
2: Toyota Prius	06:10	14:35	3.3	5	5	3.8	4
3: Chevy Volt	07:00	16:00	3.3	55	55	7.7	17
4: Toyota Prius	06:10	15:40	3.3	80	80	0.8	4
5: Nissan Leaf	06:30	16:45	6.6	95	95	1.2	24
6: Chevy Volt	08:30	19:15	3.3	15	15	14.5	17
7: Chevy Volt	08:00	17:10	3.3	60	60	6.8	17
8: Nissan Leaf	07:10	15:10	6.6	50	50	12	24
9: Toyota Prius	09:10	17:10	3.3	40	40	2.4	4
10: Toyota Prius	06:10	14:35	3.3	20	20	3.2	4
11: Chevy Volt	07:30	17:30	3.3	80	80	3.4	17
12: Toyota Prius	07:20	15:45	3.3	35	35	2.6	4
13: Toyota Prius	08:20	18:15	3.3	55	55	1.8	4
14: Nissan Leaf	08:20	16:40	6.6	20	20	19.2	24
15: Tesla Model S	06:50	17:20	10.0	65	65	29.8	85
16: Chevy Volt	07:30	16:10	3.3	30	30	11.9	17
17: Ford Fusion Energi	07:30	15:40	3.3	70	70	2.1	7
18: Toyota Prius	08:00	16:25	3.3	70	70	1.2	4
19: Tesla Model S	08:10	17:30	10	75	75	21.3	85
20: Toyota Prius	08:10	17:10	3.3	50	50	2	4
21: Nissan Leaf	07:00	15:40	6.6	10	10	21.6	24
22: Chevy Volt	08:00	18:00	3.3	30	30	11.9	17
23: Tesla Model S	08:00	17:15	10.0	90	90	8.5	85
24: Toyota Prius	06:40	15:50	3.3	20	20	3.2	4
25: Nissan Leaf	06:30	16:55	6.6	85	85	3.6	24
26: Tesla Model S	07:30	16:00	10.0	60	60	34	85
27: Tesla Model S	09:10	18:55	10.0	10	10	76.5	85
28: Ford Fusion Energi	07:10	16:50	3.3	50	50	3.5	7
29: Nissan Leaf	07:50	16:35	6.6	15	15	20.4	24
30: Chevy Volt	06:50	16:00	3.3	80	80	3.4	17
31: School Bus	11:00	16:15	70.0	50	50	57.5	115

Table A-2: Normalized RMSD for solar forecast (e^G) and optimized net load (e^{NL}), and standard deviation of the optimized net load σ^{NL} under scenarios of base forecast, operational forecast, benchmark forecast, and perfect forecast. Superscripts indicate the type of validations and subscripts indicate the solar forecasts scenarios used in the valley filling problem.

Date	e_p^G [%]	e_{US1}^G [%]	e_p^{NL} [%]	e_{p+US1}^{NL} [%]	$e_{p+perfect}^{NL}$ [%]	σ_p^{NL} [kW]	σ_{p+US1}^{NL} [kW]	$\sigma_{p+perfect}^{NL}$ [kW]	$\sigma_{perfect}^{NL}$ [kW]
04/01/13	103.8	86.8	49.0	25.0	9.6	18.1	14.3	5.2	0.8
04/02/13	63.6	30.6	46.4	25.9	18.8	19.8	10.7	6.9	0.3
04/03/13	24.6	16.8	22.1	9.0	3.5	9.5	3.8	1.3	0.0
04/04/13	29.9	42.6	17.9	20.0	9.9	8.6	9.8	4.7	0.0
04/05/13	189.1	96.9	16.9	20.0	20.7	15.4	15.1	15.7	3.8
04/06/13	87.1	45.5	34.0	27.9	27.3	17.4	14.3	13.7	1.2
04/07/13	73.9	54.5	23.4	16.0	13.5	15.3	10.4	8.9	2.7
04/08/13	210.9	99.9	23.6	20.4	21.3	20.9	17.6	18.5	3.9
04/09/13	125.5	4.0	58.2	70.0	70.9	18.1	21.3	21.2	0.3
04/10/13	4.4	4.9	4.4	3.9	1.4	1.7	1.5	0.5	0.4
04/11/13	10.9	12.6	9.2	6.5	6.7	3.1	2.1	2.0	0.1
04/12/13	34.2	38.1	31.6	22.6	4.0	12.8	9.2	1.3	0.4

04/13/13	89.0	58.1	40.8	17.9	11.3	25.0	11.5	9.3	3.0
04/14/13	407.4	119.5	20.9	33.0	31.1	24.6	30.0	30.4	4.0
04/15/13	74.1	111.1	6.5	8.2	1.8	7.8	8.4	5.8	3.5
04/16/13	127.4	62.8	54.8	44.4	45.9	26.5	21.7	22.4	1.9
04/17/13	62.7	6.0	59.6	29.3	33.7	18.4	9.2	10.5	0.0
04/18/13	4.0	4.4	5.6	3.9	1.2	1.9	1.1	0.3	0.0
04/19/13	3.4	3.8	3.7	4.1	2.9	1.2	1.1	0.7	0.0
04/20/13	2.9	2.5	2.3	2.6	1.9	0.6	0.7	0.5	0.0
04/21/13	1.8	7.8	1.9	5.9	0.6	0.6	2.0	0.2	0.0
04/22/13	1.6	5.0	2.1	3.9	0.5	0.7	1.3	0.1	0.0
04/23/13	5.6	10.6	6.5	7.4	1.5	2.2	2.6	0.4	0.0
04/24/13	44.8	39.2	28.5	17.3	14.1	12.8	7.9	6.4	2.3
04/25/13	124.4	75.8	33.9	19.0	19.2	22.6	12.7	12.8	3.6
04/26/13	78.3	7.6	50.6	31.7	39.7	17.0	10.5	13.3	0.1
04/27/13	3.1	7.0	3.7	4.6	0.9	1.3	1.6	0.3	0.1
04/28/13	2.7	6.5	2.7	4.3	1.3	1.0	1.6	0.4	0.2
04/29/13	4.7	6.5	3.7	3.5	2.0	1.4	1.1	0.8	0.4
04/30/13	48.7	47.7	29.4	17.5	5.4	14.2	8.5	2.2	0.0
All Days	68.2	37.2	23.1	17.5	14.1	11.7	8.8	7.3	1.1

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