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NUCLEON-NUCLEON POLARIZATION BETWEEN 300 AND TOO MeV

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NUCLEON-NUCLEON POLARIZATION RETWEEN 300 AND 700 MeV David Cheng, Burns Macdonald, Jerome A. Helland, and Philip M. Ogden

NUCLEON-NUCLEON POLARIZATION BETWEEN 300 AND 700 MEV<br>David Cheng, Burns Macdonald $\dagger$<br>Lawrence Radiation Laboratory University of California, Berkeley, California<br>Jerome A. Helland<br>University of California, Los Angeles, California<br>Philip M: Ogden<br>Seatcle Pacific College, Seattle, Washington

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ABSTRACT
The polarization parameter, $P\left(\theta^{*}\right)$, for pn and pp scattering has been measured at the Berkeley 184 -in. cyclotron at beam energies of $310,400,500,600$, and 700 MeV . This parameter was measured with a polarized proton beam, which was polarized by scattering at $\pm 6$ deg on carbon, then rescattered on an unpolarized nucleon target-a liquid-deuterium target for the pn system; both a liquid hydrogen and a liquid deuterium target for the pp system. Both of the outgoing nucleons from the elastic scatter were detected by an array of 27 scintillation counters in multi-channel coincidences.

In the pp system, $P\left(\theta^{*}\right)$ can be approximated by $A \sin \theta^{*} \cos \theta^{*}$, where A varies from 0.85 at 310 MeV to 1.1 at 700 MeV . In the pn system, $P_{\text {max }}$ in the forward direction varies from 0.42 at 310 MeV to 0.34 at 700 MeV , and $\mathrm{P}_{\mathrm{min}}$ in the backward direction varies from -0.25 at 310 MeV to -0.4 at 700 MeV . The shape of the NN polarization curves is nearly independent of energy in this range.

## I. INTRODUCTION

Nucleon-nucleon (NN) scattering amplitudes are determined experimentally by scattering experiments in the NN system involving polarizations. In the pp system, there are five (Wolfenstein ${ }^{1}$ ) amplitudes which are complex functions of energies and c.m. angles $\left(0 \leqslant \theta^{*} \leqslant \pi / 2\right)$. (See Appendix.) In order that the se five complex amplitudes be determined experimentally at a given energy and angle, in principle, at least nine linearly independent observables \{such as differential cross section; polarization, and rotation parameters) must be measured to solve for nine of the ten real quantities in the five complex amplitudes. (One phase is arbitrary. ${ }^{2}$ ) Since the experimental error for each measurement is not infinitesimal, and the equations for the observables and amplitudes are bilinear, in practice more than nine experiments must be performed in order to determine the pp scattering. amplitudes uniquely.

On the other hand, when one simultaneously analyzes both the pp and pn (collectively NN ) amplitudes, there are 10 complex amplitudes to be determined ( 5 for each isospin state), or 19 independent real numbers. (Again, one phase is arbitrary. ${ }^{2}$ ) On the basis of interference terms in the pp and pn amplitudes, one can obtain three equations by equating observables to amplitudes for each "set" of measurements. ${ }^{3}$ (A set contains a measurement of a pp observable at an angle $\theta^{*}$, $0 \leqslant \theta^{*} \leqslant \pi / 2$, and pn measurements of the same observables at angles $\theta^{*}$ and $\pi-\theta^{*}$.)

Thus, one can obtain 21 equations with seven sets of measurements, which, in principle, are more than sufficient to determine the NN amplitudes uniquely.

The advantages are realized experimentally also, since pn and pp measurements can usually be performed on the same experimental: setup with a change in either target nucleon or beam nucleon (or both) from proton to neutron or vice versa. One can switch between pp and pn measurements in a short time. With a counter hodoscope or spark chamber setup, one essentially measures the entire angular spectrum simultaneously. Therefore, it is possible to determine the NN scattering amplitudes with little more effort than the individual pp or pn scattering amplitudes alone.

In this experiment the pn and pp polarization parameters were measured at energies from 310 to 700 MeV , and c.m. angles from 30 to 150 deg with the same experimental setup.

## II. EXPERIMENTAL METHOD AND APPARATUS

In this experiment the nucleon-nucleon polarization was studied by double scattering. A polarized proton beam was produced by scattering an unpolarized external proton beam from the cyclotron on a carbon target at $\pm 6$ deg. The polarization of this beam was determined by means of a second scatter on an identical carbon target and measuring the asymmetry with a pair of counter telescopes at $\pm 6$ deg from the second target. By reversal of the first scattering angle, the beam polarization is caused to reverse sign (i.e., partial spin alignment changed from up to down or vice versa). By scattering the polarized beam on a nucleon target, we obtained the NN polarization by measuring, at a given angle, the asymmetry in the NN scattering due to beam polarized up and down, and then dividing this by the absolute value of the beam polarization.

The experimental setup is shown in Fig. 1. The external proton beam from the cyclotron, degraded to the desired energy with copper absorbers, entered the experimental area as shown at the top of the figure. The two bending magnets, $B_{2}$ and $B_{3}$, bent the beam away from and back toward the beam line, respectively. The beam intersected the original beam line at a carbon target with an angle $\theta_{1}$. (Due to geometry and the limitations of the maximum field available to those magnets, $\theta_{1} \leqslant 12$ deg at 700 MeV , and $\theta_{1} \leqslant 14 \mathrm{deg}$ at energies $\leqslant 600 \mathrm{MeV}$.) The scattered (hence polarized) protons passing through the lead defining slit were momentum analyzed (momentum spread $\Delta \mathrm{p} / \mathrm{p}=6 \% \mathrm{FWHM}$ ) and finally focused (achromatically) on the second target. Upon reversal of the fields in $B_{2}$ and $B_{3}$, the angle $\theta_{1}$ was reversed, and hence the sign of the beam polarization was also reversed. The angle $\theta_{1}$ was monitored by a pair of split ion chambers; one before and one after the polarizing target ensured that the angle $\theta_{1}$ was accurate and consistent to $\pm 0.2$ deg.

The polarized beam was monitored by three counters ( $M_{1}, M_{2}$, and $M_{3}$ ) in coincidence. Counter $M_{1}$ was at the intermediate focus of the beam where the momentum dispersion was maximum; the spatial extent of $M_{1}$ limited the momentum dispersion of the beam. Counter $M_{3}$, a thin counter close to the second target, selected beam particles going through only the central portion of the target.

The polarized proton beam was kept centered on the beam line by means of split counters $S_{1}$ to $S_{4}$, located near $M_{2}$. They counted the fraction of beam to the left and right of the beam line, and above and below the beam height, in coincidence with the monitor signals.

Counters $S_{5}$ and $S_{6}$ were located downstream to count the left and right portion of the beam. By slight trimming of the currents in magnets $B_{4}$ and $B_{5}$, it was possible to keep the left-right counters balanced to within $1 \%$ in both sets of split counters, thus ensuring that the beam was on the beam line.

To the left of the target (looking downstream) were 19 scintillation counters, $P_{1}$ to $P_{19}$. They detected charged particles (mainly scattered protons). To the right were counter $A_{9}, 1 / 2$-in. of lead, counters $A_{1}$ to $A_{8}$, and eight $6-i n$. thick scintillation counters, $N_{1}$ to $\mathrm{N}_{8}$. These thick counters detected high-energy neutrons ( $>5 \mathrm{MeV}$ ), that deflected protons in the scintillator. The efficiency of these counters ${ }^{4}$ was about $15 \%$. They were also used to detect charged particles directly with unit efficiency. During pn runs, $A_{1}$ to $A_{9}$ were in anticoincidence to veto events in which a proton or a $\gamma$ ray headed toward the $N$ counters. During pp runs, $A_{1}$ to $A_{8}$ and the $1 / 2-\mathrm{in}$. of lead were removed, and $A_{9}$ was put in coincidence to ensure that th'e N counters would detect only charged particles.

The N counters were shielded on all sides except the front by layers of paraffin, boric acid, lead, and steel totaling 18 to 24 in. thick for minimizing the neutron background.

This second target was a liquid hydrogen or liquid deuterium target of standard LRL design with a 7.5-mil Mylar target flask, 3-3/4 in. diam by 5 in. long. Surrounding the target was a vacuum jacket with a 310-deg window of $25-\mathrm{mil}$ Mylar.

The beam energy was measured by means of a telescope counter with variable thickness of copper absorbers in the beam. The energies,
normalized for the center of the second target, and widths (energy spreads) are tabulated in Table I. The approximate beam-intensity ratios at the second target due to beam loss through degrading are also listed.

An event was defined by a coincidence of the monitor counters $M_{1} M_{2} M_{3}=M$, at least one $P$ counter, at least one $N$ counter, and no anticounter. This system either detected two charged particles (predominantly pp), or one charged and one neutral particle (predominantly pn ) in the final state. The count from the particular $P$ and $N$ counters that fired for each event were recorded on a magnetic tape through an on-line PDP-5 computer. Six types of runs were made at each energy for both pp and pn systems: with deuterium (D), hydrogen (H), and empty flask (MT) targets, each with both signs of beam polarization. Thus there was a total of 12 different types of runs at each energy.

The three different target conditions in the pn runs were used for background elimination. The three in the pp runs were for comparison of pp runs in a free and quasi-free proton target.

## III. ANALYSIS AND RESULTS

The events of a specific type with only one $P$ and one $N$ counter counting were combined to form a $19 \times 8$ array, $M(P, N)$, where $M$ is the number of counts per monitor count in the channel $(P, N), P=1, \cdots, 19$, and $\mathrm{N}=1, \cdots, 8$. Typical distributions for pn and pp runs at 700 MeV are plotted in Figs. 2 and 3, respectively, for counter $\mathrm{N}_{3}$. The main peak on the left represents elastic (or quasi-elastic) pn or pp events. The rest is background.

For the pp runs in hydrogen, the "pure" pp events were obtained by making the subtraction $H$ - MT-E, where MT represents the background due to the empty.target, and E(extrapolation) is the additional background from inelastic events (see Fig. 3). The background E was determined by starting with the curve from $\mathrm{H}-\mathrm{MT}$ and subtracting a sufficient number of events from each of the three channels forming the main peak so as to be left with a smooth curve across those three channels and the three channels on each side.

For the pn and pp runs in deuterium, the quasi-elastic peaks have long tails in which backgrounds (mainly pion production) and NN events overlap. We have used the hydrogen target runs to determine the background contribution from the proton, and to estimate the additional contribution to background from the neutron in the deuterium target. In Table ti. we have summarized the particular $N N \rightarrow N N \pi$ processes (in which only two particles are detected by the counters) that can be confused with one $P$ or one $N$ events. Weighting the contribution of each interaction by its total cross section, ${ }^{5}$ one finds that for pn runs, elimination of the background requires the combination of D $-3 / 2 H+1 / 2 M T$. For pp runs with a deuterium target, $D-M T-E$ is required, where $E$ is the same $E$ as was determined for hycrogen. runs. Figure 4 shows three different combinations for pn runs in deuterium at 700 MeV . The chosen combination ( $\mathrm{D}-3 / 2 \mathrm{H}+1 / 2 \mathrm{MT}$ ) is clearly favored. Since the background is very small, the maximum differences of various combinations is only a $2 \%$ effect on the asymmetry calculation.

The two-body background reactions in pp interactions, such as $\mathrm{pd} \rightarrow \mathrm{pd}$ or $\mathrm{pp} \rightarrow \mathrm{m}^{+} \mathrm{d}$; have very negligible cross sections and most'of them do not overlap with the elastic peak. There is no background contribution in p n interactions from two -body final states.

After the above-mentioned background corrections were applied, the three bins with the maximum number of events were summed, and the asymmetry was calculated. Histograms for $700-\mathrm{MeV}$ pn (deuterium) and pp (hydrogen) runs in counter $\mathrm{N}_{3}$ are shown in Figs. 5 and 6, respectively. In each figure the histogram on the right is the Monte-Carlo calculated distribution with the input of experimental condition of the beam, target; and counter information. With pn runs, the target neutron is approximated by a "free" neutron moving with a Hulthén distribution. 6 For pp runs (Fig. 6), the Monte-Carlo distribution agrees in shape with the measured distribution. The pn Monte-Carlo distribution (Fig. 5) is shifted slightly to the left of the experimental distribution; this may be due to the off-mass shell effect of the target nucleon, or the binding effect of the spectator proton.

Because of the finite angular acceptance of the first scattering angle by the slit, the beam spot at the final target was not symmetrical in either spatial or angular distribution. This lack of symmetry is caused by the sharp forward peaking of the angular distribution of the proton in pC scattering. For example, at 725 MeV the data of Mc Manigal et al. ${ }^{7}$ indicate that the differential cross section at 7 deg is twice that at 5 deg. The spatial and angular distribution of the beam at the final target were not measured in this experiment. By assuming the worst
possible conditions, and making Monte-Carlo calculations, one can place an upper limit on the false scattering asymmetries arising from beam asymmetries. The maximum error in the scattering asymmetry from these calculations is about $10 \%$ in $\mathrm{N}_{1}$ and $\mathrm{N}_{8}$ for pp , about $5 \%$ in $\mathrm{N}_{8}$ for pn , and negligible for all the other channels.

The beam polarization was determined to within $\pm 3 \%$. This uncertainty dictates the maximum uncertainty in overall normalization.

The asymmetry and polarization for each neutron counter were calculated in the usual manner. The asymmetry is given by the expression $\epsilon(N)=[L(N)-R(N)] /[L(N)+R(N)]$, where $N$ is a given neutron counter, and $L(N)[R(N)]$ is the number of background subtracted counts mentioned earlier in this section for the first scatter to the left:[right]. The polarization for neution counter $N$ is $P(N)=\epsilon(N) / P_{B}$ where $P_{B}$ equals the beam polarization measured in this experiment (described in Sec. II).

Since each neutron counter is located at a fixed laboratory angle, its corresponding $c . m$. angle and spread in FWHM is calculated by the Monte Carlo method mentioned previously. For pp calculations, since $P\left(\theta^{*}\right)$ is antisymmetrical about $\theta^{*}=\pi / 2$, the data for those neutron counters (i.e., $N \geqslant 5$ ) corresponding to $\theta^{*}>\pi / 2$ have been altered in the following way. The angle has been changed to its complementary angle (i.e., $\theta^{*} \rightarrow \pi-\theta^{*}$ ) and the sign of polarization reversed.

Polarization parameters for pn and pp runs are tahulated in Tables III and IV, and are plotted in Figs. 7 and 8.

## iV. DISCUSSION

It is interesting to observe that the energy dependence of the NN polarization parameter $\mathrm{P}^{\mathrm{NN}}\left(\theta^{*}\right)$ is small and linear for pn and nearly linear for pp scattering (Figs. O and 10). Thus it is possible to parameterize the NN polarization data in the following simple form:

$$
P^{N N}\left(\theta^{*}, E\right)=\sin \theta^{*} \sum_{n, \ell} a_{n \ell} E^{n} P_{\ell}\left(\cos \theta^{*}\right)
$$

where $E$ is the beam kinetic energy (in $B e V), G^{*}$ is the $c . m$. scattering angle, and $P_{\ell}$ is the Legendre polynomial. For our results the parameters $a_{n \ell}$ are as follows:
(1) pn results: number of degrees of freedom $(d)=32$ and $\sqrt{x^{2} / d}=1.19$

$$
\begin{array}{ll}
a_{00}=0.074 \pm 0.023 & \therefore a_{10}=-0.172 \pm 0.043 \\
a_{01}=0.437 \pm 0.062 & a_{11}=0.056 \pm 0.112 \\
a_{02}=0.356 \pm 0.066 & \therefore a_{12}=0.164 \pm 0.124 \\
a_{03}=0.114 \pm 0.092 & a_{13}=-0.256 \pm 0.175
\end{array}
$$

(2) pp results: data for both pp in $\left(\mathrm{H}_{2}\right)$ and pp in $\left(\mathrm{D}_{2}\right)$

$$
\begin{aligned}
& d=59, \sqrt{X^{2} / d}=1.28 \\
& \begin{array}{lll}
a_{01}=0.295 \pm 0.283 & a_{11}=1.971 \pm 1.104 & a_{21}=1.033 \pm 1.040 \\
a_{03}=-0.543 \pm 0.438 & a_{13}=3.283 \pm 1.733 & a_{23}=-3.347 \pm 1.649 \\
a_{05}=-0.002 \pm 0.328 & a_{15}=-0.196 \pm 1.359 & a_{25}=0.534 \pm 1.342
\end{array}
\end{aligned}
$$

The plots for the fitted results are shown in Figs. 9 and 10.
Although the pn differential cross section $\mathrm{I}_{0}^{\mathrm{pn}}$ is known at only a few energies in this region, it is possible to get some $I=0, I_{0}$, and $P$ results from the pp and pn data in existence, by means of the following formulae:

$$
\begin{aligned}
& \mathrm{I}_{0}^{\mathrm{I}=0}\left(\theta^{*}\right)=2\left[\mathrm{I}_{0}^{\mathrm{pn}}\left(\theta^{*}\right)+\mathrm{I}_{0}^{\mathrm{pn}}\left(\pi-\theta^{*}\right)\right]-\mathrm{I}_{0}^{\mathrm{Pp}}\left(\theta^{*}\right) \\
& \mathrm{I}_{0} \mathrm{P}^{\mathrm{I}=0}\left(\theta^{*}\right)=2\left[\mathrm{I}_{0} \mathrm{P}^{\mathrm{pn}}\left(\theta^{*}\right)-\mathrm{I}_{0} \mathrm{P}^{\mathrm{pn}}\left(\pi-\theta^{*}\right)\right]-\mathrm{I}_{0} \dot{F}^{\mathrm{Pp}}\left(\theta^{*}\right) \\
& \mathrm{P}^{\mathrm{I}=0}\left(\theta^{*}\right)=\mathrm{I}_{0} \mathrm{P}^{\mathrm{I}=0}\left(\theta^{*}\right) / \mathrm{I}_{0}^{\mathrm{I}=0}\left(\theta^{*}\right),
\end{aligned}
$$

where $0 \leqslant \theta^{*} \leqslant \pi / 2$.
The angular distributions of $I_{0}^{I=0}$ and $P^{I=0}$ vs $\cos \theta^{*}$ for 350 , 500 , and 630 MeV at which the pn differential cross sections have been measured ${ }^{8}$ are shown in Fig. 11.

Because seven "sets" (see Sec. I) of pp and pn parameters are required to determine the nucleon-nucleon scattering amplitudes, these data represent only a partial contribution toward the determination of these amplitudes. However, the results of this experiment show that the deuteron can be used as a good neutron target at high energies, provided some precautions are taken. Furthermore, since this experiment shows that the pn polarization is quite large at these energies, it should be possible to perform the more difficult triple-scattering experiments in the pn system, and the measurement of the $D, R$, and $R$ ' parameters for both pp and pn systems have been scheduled for the 184-inch cyclotron in the near future.
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## APPENDIX

The scattering matrix for the two-nucleon system, when spatial rotational invariance, parity conservation, time reversal invariance and charge independence are assumed, can be written as ${ }^{1}$

$$
\mathrm{M}=\mathrm{a}+\mathrm{ic}\left(\sigma_{1 \mathrm{n}}+\sigma_{2 \mathrm{n}}\right)+\mathrm{m} \sigma_{1 \mathrm{n}} \sigma_{2 \mathrm{n}}+(\mathrm{g}+\mathrm{h}) \sigma_{1 \ell} \sigma_{2 \ell}+(\mathrm{g}-\mathrm{h}) \sigma_{1 \mathrm{~m}} \sigma_{2 \mathrm{~m}}
$$

where

$$
\sigma_{i \mathrm{ik}}=\sigma_{\mathrm{i}} \cdot \underset{\sim}{\mathrm{k}},
$$

$\sigma_{\dot{i}}$ is the Pauli spinor for particle $\left.i(i)=1,2\right)$ in either the initial or the final system, and $\hat{k}$ is a unit vector which takes the following three orthogonal directions $\hat{n}, \hat{l}$, or $\hat{m}$.

$$
\hat{n}=\left(k_{i} \times \ddot{k}_{n}\right) /\left|k_{i} \times x_{f}\right| \text { is the normal of the scattering plane, } k_{i}
$$ and $k_{f}$ are the initial and final momenta for either particle 1 or particle 2, respectively, in the c.m. system.

$$
\hat{\ell}=\left(k_{i}+k_{f}\right) /\left|k_{i}+k_{f}\right| . \quad \text { In the non-relativistic case for scattering }
$$ two particles of identical mass, $\hat{l}$ is in the direction of final momentum in the laboratory system.

$$
\hat{m}=\left(k_{f}-k_{i}\right) /\left|k_{m}-k_{i}\right| \text { is a unit vector perpendicular to both } \hat{n}
$$ and $\hat{l}$, and the three directions are mutually perpendicular and form a right-handed coordinate system.

For a given interaction(i.e., pp, pn, or nn), the coefficients a, $c, m, g$, and $h$ are the five complex (Wolfenstein) amplitudes (functions of $E$ and $\theta^{*}$ ) with names such as non-spin flip, one-spin flip, and doublespin flip associated with them.

## FOOTNOTES AND REFERENCES

*Work supported by the U.. S. Atomic Energy Commission.
${ }^{\dagger}$ Present address: Virginia Polytechnic Institute, Blacksburg, Virginia.

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Table I. Beam energies and intensities at the center of the second target.

| Beam <br> $(\mathrm{MeV})$ | Measured energy <br> $(\mathrm{MeV})$ | Cu degrader <br> thickness <br> (inches) | Approximate intensity <br> ratio |
| :---: | :---: | :---: | :---: |
| 310 | $307 \pm 11$ | $813 / 16$ | 0.0022 |
| 400 | $394 \pm 12$ | $71 / 4$ | 0.0035 |
| 500 | $498 \pm 11$ | $51 / 16$ | 0.0046 |
| 600 | $601 \pm 9$ | $27 / 16$ | 0.0071 |
| 700 | $702 \pm 5$ | 0 | 1.0000 |

a. For explanation, see text.

Table II. Background contribution from $\mathrm{NN} \rightarrow \mathrm{NN} \pi$ in $\mathrm{LH}_{2}$ and $\mathrm{LD}_{2}$ targets.


Table III. Polarization parameters in the pn system. (Overall normalization uncertainty is $<3 \%$.
Errors shown are due to statistics only.)

| Beam energy and polarization | $\theta^{*}$ (deg) | $\epsilon(\%)$ | P |
| :---: | :---: | :---: | :---: |
| 700 MeV | $29.5 \pm 6.7$. | $9.15 \pm 0.75$ | $0.334 \pm 0.027$ |
| $\mathrm{P}_{\mathrm{B}}=0.274$ | $44.3 \pm 6.7$ | $8.36 \pm 0.46$ | $0.305 \pm 0.017$ |
|  | $60.4 \pm 6.5$ | $4.29 \pm 0.91$ | $0.157 \pm 0.033$ |
|  | $77.1 \pm 6.0$ | $-1.86 \pm 0.81$ | $-0.068 \pm 0.030$ |
|  | $93.8 \pm 5.7$ | $-9.65 \pm 0.72$ | $-0.352 \pm 0.026$ |
|  | $110.9 \pm 5.4$ | $-11.27 \pm 0.87$ | $-0.411 \pm 0.032$ |
|  | $127.1 \pm 5.3$ | $-6.78 \pm 0.53$ | $-0.247 \pm 0.019$ |
|  | $143.2 \pm 4.9$ | $-3.99 \pm 0.52$ | $-0.146 \pm 0.019$ |
| 600 MeV | $33.0 \pm 6.0$ | $11.49 \pm 1.26$ | $0.364 \pm 0.040$ |
| $P_{B}=0.316$ | $48.5 \pm 5.8$ | $7.92 \pm 1.30$ | $0.251 \pm 0.041$ |
|  | $64.8 \pm 5.6$ | $2.67 \pm 0.96$ | $0.084 \pm 0.030$ |
|  | $81.3 \pm 5.7$ | $-4.90 \pm 0.88$ | $-0.155 \pm 0.028$ |
|  | $97.8 \pm 5.6 \ldots$ | $-9.95 \pm 0.99$ | $-0.315 \pm 0.031$ |
|  | $114.7 \pm 5.6$ | $-10.89 \pm 0.96$ | $-0.345 \pm 0.030$ |
|  | $130.5 \pm 5.6$ | $-7.61 \pm 0.74$ | $-0.241 \pm 0.023$ |
|  | $145.6 \pm 5.1$ | $-2.85 \pm 0.73$ | $-0.090 \pm 0.023$ |
| 500 MeV | $33.4 \pm 5.8$ | $10.23 \pm 0.82$ | $0.297 \pm 0.024$ |
| $\mathrm{P}_{\mathrm{B}}=0.345$ | $48.5 \pm 6.1$ | $8.79 \pm 0.54$ | $0.255 \pm 0.016$ |
|  | $64.7 \pm 5.9$ | $3.11 \pm 0.57$ | $0.090 \pm 0.017$ |
|  | $81.2 \pm 5.9$ | $-5.35 \pm 0.60$ | $-0.155 \pm 0.017$ |
|  | $97.9 \pm 5.9$ | $-9.11 \pm 0.62$ | $-0.264 \pm 0.018$ |
|  | $115.0 \pm 5.9$ | $-9.08 \pm 0.60$ | $-0.263 \pm 0.017$ |
|  | $130.9 \pm 5.7$ | $-5.06 \pm 0.59$ | $-0.147 \pm 0.017$ |
|  | $145.2 \pm 4.9$ | $-3.82 \pm 0.60$ | $-0.111 \pm 0.017$ |

Table III. (cont.)

| Beam energy and polarization | $\theta^{*}(\mathrm{deg})$ | $\epsilon(\%)$ | P |
| :---: | :---: | :---: | :---: |
| 400 MeV | $33.1 \pm 6.9$ | $15.70 \pm 3.31$ | $0.4 \hat{1} 1 \pm 0.087$ |
| $\mathrm{P}_{\mathrm{B}}=0.382$ | $48.3 \pm 6.9$ | $10.10 \pm 0.86$ | $0.264 \pm 0.023$ |
|  | $66.6 \pm 7.2$ | $3.18 \pm 1.24$ | $0.083 \pm 0.032$ |
|  | $83.1 \pm 7.0$ | $-5.80 \pm 0.98$ | $-0.152 \pm 0.026$ |
|  | $99.7 \pm 6.8$ | $-11.82 \pm 0.94$ | $-0.309 \pm 0.025$ |
|  | $116.5 \pm 6.6$ | $-10.40 \pm 0.83$ | $-0.272 \pm 0.022$ |
|  | $131.1 \pm 5.9$ | $-6.02 \pm 0.69$ | $-0.158 \pm 0.018$ |
|  | $144.3 \pm 5.1$ | $-3.97 \pm 2.14$ | $-0.104 \pm 0.056$ |
| 310 MeV | $33.1 \pm 6.7$ | $18.00 \pm 1.61$ | $0.421 \pm 0.038$ |
| $P_{B}=0.428$ | $47.8 \pm 7.2$ | $12.27 \pm 1.11$ | $0.287 \pm 0.026$ |
|  | $66.7 \pm 8.1$ | $3.96 \pm 0.85$ | $0.093 \pm 0.020$ |
|  | $83.2 \pm 8.0$ | $-4.87 \pm 1.02$ | $-0.114 \pm 0.024$ |
|  | $99.8 \pm 7.8$ | $-10.22 \pm 0.80$ | $-0.239 \pm 0.019$ |
|  | $116.5 \pm 7.6$ | $-9.31 \pm 0.69$ | $-0.218 \pm 0.016$ |
|  | $130.7 \pm 6.8$ | $-7.45 \pm 0.75$ | $-0.174 \pm 0.018$ |
|  | $141.5 \pm 7.2$ | $-5.68 \pm 1.32$ | $-0.133 \pm 0.031$ |
| $\theta^{*}=$ proton scattering angle in c.m. $\quad \epsilon=$ asymmetry |  |  |  |

Table IV(a). pp polarization in $\mathrm{LH}_{2}$ target. (Overall normalization uncertainty is less than $3 \%$. Errors shown are due to statistics only.

| Beam energy and polarization | $\theta^{*}(\operatorname{deg})$ | $\epsilon(\%)$ | P | $\mathrm{P} / \sin ^{*}{ }^{*}$ |
| :---: | :---: | :---: | :---: | :---: |
| 700 MeV | $30.8 \pm 1.7$ | $15.2 \pm 0.52$ | $0.555 \pm 0.019$ | $1.083 \pm 0.037$ |
| $\mathrm{P}_{\mathrm{B}}=0.274$ | $35.7 \pm 1.7$ | $14.3 \pm 0.33$ | $0.522 \pm 0.012$ | $0.894 \pm 0.021$ |
|  | $43.2 \pm 3.5$ | $15.3 \pm 0.44$ | $0.558 \pm 0.016$ | $0.816 \pm 0.023$ |
|  | $52.4 \pm 3.1$ | $14.5 \pm 0.61$ | $0.529 \pm 0.022$ | $0.668 \pm 0.028$ |
|  | $60.1 \pm 3.6$ | $13.0 \pm 0.30$ | $0.474 \pm 0.011$ | $0.547 \pm 0.013$ |
|  | $68.7 \pm 3.3$ | $9.7 \pm 1.08$ | $0.354 \pm 0.039$ | $0.380 \pm 0.042$ |
|  | $77.0 \pm 3.6$ | $7.0 \pm 0.42$ | $0.255 \pm 0.015$ | $0.262 \pm 0.016$ |
|  | $86.1 \pm 3.5$ | $3.0 \pm 1.04$ | $0.109 \pm 0.038$ | $0.110 \pm 0.038$ |
| 600 MeV | $33.6 \pm 2.5$ | $16.2 \pm 0.31$ | $0.513 \pm 0.010$ | $0.926 \pm 0.018$ |
| $\mathrm{P}_{\mathrm{B}}=0.316$ | $34.5 \pm 1.5$ | $18.8 \pm 1.10$ | $0.595 \pm 0.035$ | $1.059 \pm 0.061$ |
|  | $46: 1 \pm 3.6$ | $16.3 \pm 0.32$ | $0.516 \pm 0.010$ | $0.716 \pm 0.014$ |
|  | $49.5 \pm 3.2$ | $15.3 \pm 0.32$ | $0.484 \pm 0.010$ | $0.637 \pm 0.013$ |
|  | $63.1 \pm 3.6$ | $12.6 \pm 0.61$ | $0.399 \pm 0.019$ | $0.446 \pm 0.022$ |
|  | $65.6 \pm 3.4$ | $11.4 \pm 1.20$ | $0.361 \pm 0.038$ | $0.396 \pm 0.042$ |
|  | $80.2 \pm 3.6$ | $5.3 \pm 0.32$ | $0.168 \pm 0.010$ | $0.170 \pm 0.010$ |
|  | $82.9 \pm 3.5$ | $3.6 \pm 0.79$ | $0.114 \pm 0.025$ | $0.115 \pm 0.025$ |
| 500 MeV | $3.3 .7 \pm 2.3$ | $16.9 \pm 0.38$ | $0.490 \pm 0.011$ | $0.883 \pm 0.020$ |
| $\mathrm{P}_{\mathrm{B}}=0.345$ | $36.8 \pm 1.0$ | $17.6 \pm 2.03$ | $0.510 \pm 0.059$ | $0.852 \pm 0.098$ |
| Norm. error | $46.9 \pm 3.6$ | $15.9 \pm 0.61$ | $0.461 \pm 0.018$ | $0.631 \pm 0.024$ |
| 1.4\% | $48.7 \pm 3.1$ | $15.6 \pm 0.49$ | $0.452 \pm 0.014$ | $0.602 \pm 0.019$ |
|  | $64.1 \pm 3.6$ | $9.3 \pm 0.35$ | $0.270 \pm 0.010$ | $0.300 \pm 0.011$ |
|  | $64.6 \pm 3.3$ | $10.8 \pm 0.87$ | $0.313 \pm 0.025$ | $0.347 \pm 0.028$ |
|  | $81.3 \pm 3.6$ | $3.7 \pm 0.52$ | $0.107 \pm 0.015$ | $0.108 \pm 0.015$ |
|  | $81.8 \pm 3.5$ | $3.9 \pm 0.55$ | $0.113 \pm 0.016$ | $0.114 \pm 0.016$ |

Table IV(a). (cont.)

| Beam energy and polarization | $\theta^{*}(\mathrm{deg})$ | $\epsilon(\mathrm{deg})$ | P | $\mathrm{P} / \sin \theta^{*}$ |
| :---: | :---: | :---: | :---: | :---: |
| 400 MeV | $33.8 \pm 2.3$ | $16.9 \pm 0.52$ | $0.442 \pm 0.014$ | $0.795 \pm 0.024$ |
| $\mathrm{P}_{\mathrm{B}}=0.382$ | $47.8 \pm 3.1$ | $16.0 \pm 0.29$ | $0.419 \pm 0.008$ | $0.565 \pm 0.010$ |
|  | $48.0 \pm 3.6$ | $16.0 \pm 0.41$ | $0.419 \pm 0.011$ | $0.564 \pm 0.014$ |
|  | $63.5 \pm 3.3$ | $10.5 \pm 0.30$ | $0.275 \pm 0.008$ | $0.307 \pm 0.009$ |
|  | $65.2 \pm 3.7$ | $10.4 \pm 0.37$ | $0.272 \pm 0.010$ | $0.300 \pm 0.011$ |
|  | $80.6 \pm 3.5$ | $4.0 \pm 0.32$ | $0.105 \pm 0.008$ | $0.106 \pm 0.008$ |
|  | $82.5 \pm 3.7$ | $3.2 \pm 0.33$ | $0.084 \pm 0.009$ | $0.084 \pm 0.009$ |
| 310 MeV | $33.6 \pm 2.4$ | $17.2 \pm 1.05$ | $0.402 \pm 0.025$ | $0.726 \pm 0.044$ |
| $\mathrm{P}_{\mathrm{B}}=0.428$ | $47.3 \pm 2.8$ | $16.0 \pm 0.31$ | $0.374 \pm 0.007$ | $0.509 \pm 0.010$ |
|  | $50.1 \pm 2.7$ | $15.5 \pm 0.49$ | $0.362 \pm 0.011$ | $0.472 \pm 0.015$ |
|  | $62.4 \pm 3.2$ | $11.8 \pm 0.30$ | $0.276 \pm 0.007$ | $0.311 \pm 0.008$ |
|  | $66.3 \pm 3.7$ | $9.3 \pm 0.35$ | $0.217 \pm 0.008$ | $0.237 \pm 0.009$ |
|  | $79.4 \pm 3.5$ | $5.0 \pm 0.30$ | $0.117 \pm 0.007$ | $0.119 \pm 0.007$ |
|  | $83.7 \pm 3.6$ | $1.5 \pm 0.35$ | $0.035 \pm 0.008$ | $0.035 \pm 0.008$ |

Table IV(b). pp polarization in $L D_{2}$ target. (Overall normalization uncertainty is less than $3 \%$. Errors shown are due to statistics only.')

| Beam energy and polarization | $\theta^{*}(\mathrm{deg})$ | $\epsilon(\%)$ | P | $P / \sin \theta^{*}$ |
| :---: | :---: | :---: | :---: | :---: |
| 700 MeV | - $29.5 \pm 6.7$ | $11.6 \pm 1.41$ | $0.423 \pm 0.051$ | $0.860 \pm 0.105$ |
| $\mathrm{P}_{\mathrm{B}}=0.274$ | $36.8 \pm 4.9$ | $13.4 \pm 0.88$ | $0.489 \pm 0.032$ | $0.816 \pm 0.054$ |
|  | $44.3 \pm 6.7$ | $14.7 \pm 0.67$ | $0.536 \pm 0.024$ | $0.768 \pm 0.035$ |
|  | $52.9 \pm 5.2$ | $13.7 \pm 0.05$ | $0.500 \pm 0.018$ | $0.627 \pm 0.023$ |
|  | $60.4 \pm 6.5$ | $11.7 \pm 0.76$ | $0.427 \pm 0.028$ | $0.491 \pm 0.032$ |
|  | $69.1 \pm 5.4$ | $11.5 \pm 0.73$ | $0.420 \pm 0.027$ | $0.449 \pm 0.029$ |
|  | $77.1 \pm 6.0$ | $6.2 \pm 0.76$ | $0.266 \pm 0.028$ | $-0.232 \pm 0.028$ |
|  | $86.2 \pm 5.7$ | $3.5 \pm 0.99$ | $0.128 \pm 0.036$ | $0.128 \pm 0.036$ |
| 600 MeV | $33.0 \pm 6.0$ | $16.9 \pm 2.45$ | $0.535 \pm 0.078$ | $0.982 \pm 0.142$ |
| $P_{B}=0.316$ | $34.4 \pm 5.1$ | $15.0 \pm 1.29$ | $0.475 \pm 0.041$ | $0.840 \pm 0.072$ |
|  | $48.5 \pm 5.8$ | $17.6 \pm 1.26$ | $0.557 \pm 0.040$ | $0.744 \pm 0.053$ |
|  | $49.5 \pm 5.6$ | $14.2 \pm 0.67$ | $0.449 \pm 0.021$ | $0.591 \pm 0.028$ |
|  | $64.8 \pm 5.6$ | $11.8 \pm 0.91$ | $0.373 \pm 0.029$ | $0.413 \pm 0.032$ |
|  | $65.3 \pm 5.6$ | $10.6 \pm 0.32$ | $0.335 \pm 0.010$ | $0.369 \pm 0.011$ |
|  | $81.3 \pm 5.7$ | $3.9 \pm 0.85$ | $0.123 \pm 0.027$ | $0.125 \pm 0.027$ |
|  | $82.2 \pm 5.6$ | $4.5 \pm 0.82$ | $0.142 \pm 0.026$ | $0.144 \pm 0.026$ |
| 500 MeV | $33.4 \pm 5.8$ | $17.5 \pm 2.31$ | $0.507 \pm 0.067$ | $0.921 \pm 0.122$ |
| $\mathrm{P}_{\mathrm{B}}=0.345$ | $48.5 \pm 6.1$ | $14.7 \pm 1.16$ | $0.426 \pm 0.034$ | $0.569 \pm 0.045$ |
|  | $49.1 \pm 5.7$ | $14.2 \pm 0.73$ | $0.412 \pm 0.021$ | $0.545 \pm 0.028$ |
|  | $64.7 \pm 5.9$ | $9.1 \pm 0.78$ | $0.264 \pm 0.023$ | $0.292 \pm 0.025$ |
|  | $65.0 \pm 5.9$ | $9.5 \pm 0.68$ | $0.275 \pm 0.020$ | $0.304 \pm 0.022$ |
|  | $81.2 \pm 5.9$ | $4.0 \pm 0.74$ | $0.116 \pm 0.021$ | $0.117 \pm 0.022$ |
|  | $82.1 \pm 5.1$ | $3.8 \pm 0.71$ | $0.110 \pm 0.021$ | $0.111 \pm 0.021$ |

Table IV(b). (cont.)

| Beam energy and polarization | $\theta^{*}(\mathrm{deg})$ | $\epsilon(\%)$ | P | $\mathrm{P} / \sin \theta^{*}$ |
| :---: | :---: | :---: | :---: | :---: |
| 400 MeV | $33.1 \pm 6.9$ | $16.9 \pm 2.96$ | $0.442 \pm 0.007$ | $0.810 \pm 0.142$ |
| $\mathrm{P}_{\mathrm{B}}=0.382$ | $48.3 \pm 6.9$ | $14.8 \pm 1.00$ | $0.387 \pm 0.026$ | $0.519 \pm 0.035$ |
|  | $48.9 \pm 6.9$ | $16.0 \pm 0.61$ | $0.419 \pm 0.016$ | $0.556 \pm 0.021$ |
|  | $63.5 \pm 6.6$ | $9.4 \pm 0.58$ | $0.246 \pm 0.015$ | $0.275 \pm 0.017$ |
|  | $66.6 \pm 7.2$ | $10.3 \pm 0.74$ | $0.270 \pm 0.019$ | $0.294 \pm 0.021$ |
|  | $80.3 \pm 6.8$ | $2.9 \pm 0.59$ | $0.076 \pm 0.015$ | $0.077 \pm 0.016$ |
|  | $83.1 \pm 7.0$ | $2.4 \pm 0.62$ | $0.063 \pm 0.016$ | $0.063 \pm 0.016$ |

## FIGURE CAPTIONS

Fig. 1. Layout of the experimental 'setup.
Fig. 2. Comparison of pnevents in all proton counters for neutron counter $\mathrm{N}_{3}$ at $700-\mathrm{MeV}$ incident proton energy for three different target conditions: target filled with liquid deuterium, target filled with liquid hydrogen, and target empty. Horizontal lines indicate position of zero counts.

Fig. 3. Comparison of ppents in all proton counters for neutron counter $\mathrm{N}_{3}$ at $700-\mathrm{MeV}$ incident proton energy for two different target conditions: target filled with liquid hydrogen, target empty, and background extrapolation from off-center peak events under target filled.minus target empty.

Fig. 4. Comparison of pn events in all proton counters for $\mathrm{N}_{3}$ at $700-\mathrm{MeV}$ incident proton energy for different methods of background subtraction (see text). Horizontal lines indicate position of zero counts.

Fig. 5. Comparison of prents in proton counters for neutron counter $\mathrm{N}_{3}$ at $700-\mathrm{MeV}$ incident proton energy for beam polarization up and down, and Monte-Carlo calculation simulation of this experiment, assuming the target neutron is moving with just the Hulthén momentum distribution (see text). Horizontal lines indicate position of zero counts.

Fig. 6. Same as Fig. 5 for pp events.
 comparison with other experimental results. Errors are only statistical. Overall normalization uncertainty is less than $3 \%$.

See text for upper limits of systematic errors．（a） $700-\mathrm{MeV}$ incident proton energy；（b） 600 MeV ；$\{635 \mathrm{MeV}$ ，from Golovin et al。（Ref．3）； （c） 500 MeV ；（d） 400 MeV ；（e） 310 MeV ；$\{350 \mathrm{MeV}$ ，Siegel et al． （Ref．9）；〈 310 MeV ，Chamberlain et al．（Ref．10）．
Fig．8．pp polarizations from results of this experiment plus（ Then $^{\boldsymbol{T}}$ data taken with hydrogen target， $\mid$ I data taken with deuterium target） plus comparisons with other experimental results that do not agree with this experiment．Errors are statistical．Overall normalization uncertainty is less than $3 \%$ ．See text for upper limits of systematic errors．（a） $700-\mathrm{MeV}$ incident proton energy；（b） 600 MeV ； 635 MeV ，Meshcheryakov et al．（Ref．11）；（c） 500 MeV ；（d） 400 MeV ； （e） 310 MeV ．

Fig．9．Fitted curves of pn polarizations from results of this experi－ ment．Note that only small and linear energy dependence is present．

Fig．10．Same as Fig． 9 for pp results．
Fig．11．Differential cross sections and polarization results for isospin $=0$ NN states at 350,500 ，and 630 MeV ．


Fig. 1


Fig. 2


XBL671-57
Fig. 3


XBL 671-61
Fig. 4


Fig. 5


$$
X B L 671-60
$$

Fig. 6


Fig. 7(a)
MU-3625.


Fig. 7(b)
MU-36248


Fig. $7(c)$


Fig. 7(d)
MU. 36243


MU. 36246
Fig. 7(e)


MUB-9503
Fig. 8(a)


MU. 36247
Fig. 8(b)


MUB:9502
Fig. 8(c)


MU-36258
Fig. $8(\mathrm{~d})$

$M U-36242$
Fig. 8(e)



Fig. 11

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