Lawrence Berkeley National Laboratory

Recent Work

Title

THE CAPTURE OF PI-MESONS IN DEUTERIUM

Permalink

https://escholarship.org/uc/item/9zn7z3js

Authors

Brueckner, K. Serber, R. Watson, K.

Publication Date

1950-09-18

UNIVERSITY OF CALIFORNIA

UCRL ---- 913

cy 2

Radiation Laboratory

TWO-WEEK LOAN COPY

This is a Library Circulating Copy which may be borrowed for two weeks. For a personal retention copy, call Tech. Info. Division, Ext. 5545

BERKELEY, CALIFORNIA

DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.

UNCLASSIFIED

ÚCRL-913

UNIVERSITY OF CALIFORNIA

Radiation Laboratory

Contract No. W-7405-eng-48

THE CAPTURE OF $\pi\text{-}\text{MESONS}$ in deuterium

K. Brueckner, R. Serber and K. Watson

September 18, 1950

Berkeley, California

Unclassified Distribution

INSTALLATION

Number of Copies

8

1

2 1

1

4

1 1

4

4

1

ŀ

1 1

1

3 1

1

2

1

24

3

1

1

13

1

3 1

2

1

3

1

8

1

1.

2

2

1

15

1

1

11

Argonne National Laboratory Armed Forces Special Weapons Froject Atomic Energy Commission - Washington Battelle memorial Institute Brush Beryllium Company Brookhaven National Laboratory Bureau of Medicine and Surgery Bureau of Ships Carbide and Carbon Chemicals Division (K-25 Plant) Carbide and Carbon Chemicals Division (Y-12 Plant) Chicago Operations Office Columbia University (J. R. Dunning) Columbia University (G. Failla) Dow Chemical Company H. K. Ferguson Company General Electric Company, hichland Harshaw Chemical Corporation Idaho Operations Office Iowa State College Kansas City Operations Branch Kellex Corporation Knolls Atomic Power Laboratory Los Alamos Scientific Laboratory Mallinckrodt Chemical Works Massachusetts Institute of Technology (A. Gaudin) Massachusetts Institute of Technology (A. R. Kaufmann) Mound Laboratory National Advisory Committee for Aeronautics National Eureau of Standards Naval Medical Research Institute Naval Radiological Defense Laboratory New Brunswick Laboratory New York Operations Office North American Aviation, Inc. Oak Ridge National Laboratory Patent Branch - Washington Rand Corporation Sandia Corporation Santa Fe Operations Office Sylvania Electric Froducts, Inc. Technical Information Division (Oak Ridge) Armament Division, Deputy for Research and Development (Capt. Glenn Davis) Assistant for Atomic Energy, Deputy Chief of Staff (Col. Robert E. Greer) Chief of Documents and Disseminations Branch (Col. J. E. Mallory) USAF Assistant for Research Director of Lesearch and Development, Deputy Chief of Staff (Col. B. G. Holzman)

-2'-

Unclassified Distribution

Total

140

-28-

INSTALLATION

Number of Copies

Electronic Systems Division (Mr. E. C. Trafton) 1 Chief of Scientific Advisors (Dr. Theodore von Karman) 1 USAF, Eglin Air Force Base (Major A. C. Field) 1 USAF, Kirtland Air Force Base (Col. Marcus F. Cooper) 1 1 USAF. Maxwell Air Force Base (Col. F. N. Moyers) USAF, NEPA Office 2 USAF, Offutt Air Force Base (Col. H. R. Sullivan, Jr.) 1 USAF Surgeon General, Medical Research Division (Col. A. P. Gagge) 1 USAF, Wright-Patterson Air Force Base (Rodney Nudenberg) 1 U. S. Army, Atomic Energy Branch (Lt. Col. A. W. Betts) . . **1** U. S. Army, Army Field Forces (Captain James Kerr) 1 1 U. S. Army, Commanding General, Chemical Corps Technical Command (Col. John A. MacLaughlin thru Mrs. Georgia S. Benjamin) U. S. Army, Chief of Ordnance (Lt. Col. A. R. Del Campo) 1 1 U. S. Army, Commanding Officer, Watertown Arsenal (Col. Carroll H. Deitrick) U. S. Army, Director of Operations Research (Dr. Ellis Johnson) 1 U. S. Army, Office of Engineers (Allen O'Leary) 1 1 U. S. Army, Office of the Chief Signal Officer (Curtis T. Clayton thru Maj. George C. Hunt) U. S. Army, Office of the Surgeon General (Col. W. S. Stone) 1 U. S. Geological Survey (T. B. Nolan) 2 U. S. Public Health Service 1 1 University of Celifornia at Los Angeles 5 University of California Radiation Laboratory 2 University of Rochester ĩ University of Washington 2 Western Reserve University Westinghouse Electric Company 4 R. F. Bacher, California Institute of Technology) 1 Cornell University 1

Information Division Radiation Laboratory Univ. of California Berkeley, California

-3-

THE CAPTURE OF π -MESONS IN DEUTERIUM

K. Brueckner, R. Serber and K. Watson

Radiation Laboratory, Department of Physics University of California, Berkeley, California

September 18, 1950

Abstract

Panofsky, Aamodt and Hadley find that the capture of n-mesons in deuterium leads to two neutron emission in 70 percent of the cases, and to two neutrons and a Y-ray in the other 30 percent. The former process is forbidden for capture of scalar mesons from the K shell. A detailed balancing argument, based on the observed cross section for $2p \longrightarrow D + \pi^+$, permits calculation of the nonradiative capture rate from orbits of higher angular momentum. It is shown that this is too small to account for the observation, and the possibility that the meson is a scalar is thus ruled out. This conclusion could only be avoided by postulating the existence of an interaction between meson and nucleons sufficiently large to radically alter the magnitude of the p wave functions near the nucleons. For pseudoscalar mesons, non-radiative capture from the K shell is permitted, and the ratio of radiative to non-radiative transitions can be related to the ratio of meson photoproduction cross section to the cross section for $2p \longrightarrow D + \pi^{+}$. The result is compatible with the type of meson-nucleon coupling which might be expected for pseudoscalar mesons, but uncertainties in the measured quantities are too large to permit a sharper conclusion.

UCRL-913

-4-

THE CAPTURE OF π-MESONS IN DEUTERIUM K. Brueckner, R. Serber and K. Watson Radiation Laboratory, Department of Physics University of California, Berkeley, California

September 18, 1950

In UCRL-814 (Revised) Panofsky, Aamodt and Hadley report the finding, that the capture of negative mesons by deuterons occurs in either of two ways, leading to the emission of two neutrons in 70 percent of the cases, and to two neutrons and a Y-ray in the other 30 percent. The first point of interest is that the two neutron process occurs at all. For if the π^- -meson satisfied a scalar wave equation, and if the capture of the π^- -took place from the K shell of the $\pi^- + D$ system, this process would be forbidden, as Ferretti¹ has pointed out. The reason is that an s state of the $\pi^- + D$ system would have a total angular momentum J = 1, and be an even state, whereas the only state of the two neutron system with J = 1 is a ³P state, which is odd. Thus, the emission of two neutrons in about 70 percent of the captures proves either that the meson is not a scalar, or that the capture takes place from a higher Bohr orbit than the K shell, an orbit with $\ell \neq 0$.

To decide between these two possibilities we must estimate the rate, from the higher meson states, of capture with two neutron emission. We shall attempt to do this without recourse to an explicit meson theory, since we have learned by experience that meson theory cannot always be relied on even for orders of magnitude. In fact, we know of no meson theory which is not in gross disagreement with at least one of the presently believed experimental facts. The possibility of estimating the capture rate depends on the principle of detailed balancing. Although the cross section for the inverse of $w^- + D \longrightarrow 2n$ has not been

UCRL-913

measured, it may reasonably be supposed that the reactions $2n \longrightarrow D + \pi^{-}$ and $2p \longrightarrow D + \pi^{+}$ have the same cross section. The latter reaction has been studied by Cartwright, Richman, Wilcox and Whitehead,² who obtained a cross section $\sigma(2p \longrightarrow D + \pi^{+}) = 2 \times 10^{-28} \text{ cm}^{2}$ for 340 MeV protons bombarding hydrogen. The most direct experimental support for the supposition of charge symmetry comes from work of Bradner, Bowker and Rankin,³ who found a ratio of negative to positive mesons of 15 from carbon bombarded by 260 MeV neutrons, and the reciprocal ratio from carbon bombarded by protons of the same energy.

-5-

In the 340 Mev $2p \longrightarrow D * \pi^+$ experiments the kinetic energy available in the center of mass system is 22 Mev. The principle of detailed balancing will give us the rate of D * $\pi^- \longrightarrow 2n$ for 22 Mev relative energy of meson and deuteron, and we must extrapolate to lower energy to make the desired connection. The question is thus the dependence of the transition matrix element on meson momentum. Since the wave function, $\phi(\vec{r})$, of a meson in a p state vanishes at the origin, we can write, for small \vec{r} ,

Here \vec{r} is the coordinate of the meson relative to the center of mass of the deuteron. Thus $\phi(\vec{r})$, and the matrix element, will be proportional to the momentum of the meson near the deuteron, as long as (1) is adequate, which will be true as long as the wave-length of the meson is large compared to the distances, r, which contribute to the process. The values of r in question are certainly not larger than the radius of the deuteron (which is about the same as the wave-length of a 20 Mev meson), but in fact will be considerably smaller because of the high relative energy (μc^2) which must be transferred to the nucleons. Such high energy transfers will occur only in intimate collisions of the nucleons; if the transfer takes place in a single collision of the nucleons the distance

-6-

would be about the wave-length of the neutrons, $r \sim \hbar/(M\mu)^{1/2} c = 4 \times 10^{-14}$ cm. Since the wave-length of a 20 Mev meson is about five times larger, the proportionality of the matrix element to meson momentum would be expected to hold over the energy range in question.⁴

In addition to its dependence on the relative momentum of meson and deuteron, the matrix element will also depend on the neutron momenta. However, as the meson energy changes from 20 Mev to zero, the neutron momenta change by only 7 percent. We shall therefore neglect this dependence. In fact, quite aside from questions of the trustworthiness of meson theory, one of the advantages of using the detailed balancing argument is that in calculating the capture rate one avoids the question of the magnitude of high frequency Fourier components of the deuteron wave function, since nearly the same Fourier components are involved in the production process.

Finally, it should be pointed out that the foregoing argument assumes that there does not exist an interaction between meson and nucleons sufficiently strong to radically change the form of the p wave function near the nucleons. Were such an interaction present, the argument would, of course, be invalidated.

Let us denote by $R(\pi^- + D \rightarrow 2n)$ the rate of capture from a bound p state, and by $\sigma(\pi^- + D \rightarrow 2n)$ the cross section of this process for an unbound meson. In the latter case let v_{π} and p_{π} be the relative velocity and momentum of meson and deuteron, v_n and p_n those of the two neutrons. According to the argument following (1), the ratio of the capture rate, $R(\pi^- + D \rightarrow 2n)$, from the bound state to the capture rate, $v_{\pi}\sigma(\pi^- + D \rightarrow 2n)$, from the amplitude should be the ratio of the square of the gradient of the bound state function, $|\nabla \phi(0)|^2$, to the square of the same quantity for the plane wave, p^2/h^2 . Thus

$$R(\pi^{-} * D \longrightarrow 2n) = \hbar^{2} \nabla_{\pi} \sigma(\pi^{-} * D \longrightarrow 2n) | \nabla \phi(0) |^{2} / p_{\pi}^{2}.$$
(2)

-7-

The principle of detailed balancing gives

$$\sigma(\pi^{-} + D \longrightarrow 2n) = \frac{2}{3} p_n^2 \sigma(2n \longrightarrow D + \pi^{-}) / p_n^2 \qquad (3)$$

The factor $\frac{2}{3}$ is the product of $\frac{4}{3}$, for the statistical weight of the spin states, and $\frac{1}{2}$, to allow for the indistinguishability of the two neutrons. Combining (2) and (3) we find

$$R(\pi^{-} + D \longrightarrow 2n) = \frac{2}{3} \hbar^2 p_n^2 \sigma(2n \longrightarrow D + \pi^{-}) |\nabla \phi(0)|^2 / \mu p_{\pi}^3$$

where μ is the reduced meson mass, or using the approximate energy relation, $p_n^2/M = \mu c^2$, with M the neutron mass, and the assumption of charge symmetry,

$$R(\pi^{-} + D \longrightarrow 2n) = \frac{2}{3} \hbar^{2} Mc^{2} \sigma(2p \longrightarrow D + \pi^{+}) \left| \nabla \phi(0) \right|^{2} / p_{\pi}^{3} .$$
 (4)

If we put in the value of $|\nabla \phi(0)|^2$ for a p state of principal quantum number n, we find

$$R(\pi^{-} + D \longrightarrow 2n) = (2/9\pi) \hbar^{2} Mc^{2} (n^{2} - 1)\sigma(2p \longrightarrow D + \pi^{+})/n^{5} a^{5} P_{\pi}^{3}, \quad (5)$$

where a is the mesonic Bohr radius, $a = \hbar^2/\mu e^2$. With the measured value of $\sigma(2p \longrightarrow D + \pi^+)$, (5) gives

$$R(\pi^- + D \longrightarrow 2n) = 1.0 \times 10^{11} (n^2 - 1)/n^5 \text{ sec}^{-1}$$

In Table I this transition rate is compared with that for the radiative transition of the meson from the np state to the ls state. For n > 3 it is estimated that the transition rate by molecular collisions should predominate over that for radiation. The table shows that the rate of the two neutron

2.2

Table I

4p

- ----8----

A comparison is given of the transition rates for meson absorption and radiation to the ground state from the lower p state Bohr orbits.

| Transition from the | | Transition Rates in Units of 10 ¹⁰ sec-1 | |
|---------------------|-------|---|---------------------------|
| | State | Decay by fast neutrons emission | Radiation to ground state |
| | 2p | . 94 | 17.2 |
| | 3p | •33 | 5,1 |

.15

-9-

process is at least thirty times too small to account for the observed ratio of $\pi^- + D \longrightarrow 2n$ to $\pi^- + D \longrightarrow 2n + \gamma$.

The supposition that the meson is a scalar can thus be excluded, unless, indeed, the alternative of a large meson-nucleon interaction is the true one. If we imagine such an interaction to be representable by a short range potential well, it is evident that, in order to greatly change the p wave function near the . nucleon, the strength of the interaction must be nearly great enough to contain a bound p state in the well; that is, nearly great enough to produce an isobaric state of the nucleon.

If the π -meson is a pseudoscalar particle, the angular momentum and parity selection rules allow non-radiative capture from the K shell of the $\pi^- + D$ system. The question them is whether the observed ratio of the radiative and non-radiative processes can be easily understood.

If we suppose that s states alone, rather than p states, are involved in the reactions $\pi^- + D \longrightarrow 2n$ and $2p \longrightarrow D + \pi^+$, the relation (4) would have the factor $\hbar^2 \left| \nabla \phi(0) \right|^2 / p_{\pi}^2$ replaced by $\left| \phi(0) \right|^2$. There is, however, no reason to exclude p states from the production process, and we shall write

$$R(\pi^{-} + D \longrightarrow 2n) = \frac{2}{3} \frac{Mc^2 \sigma(2p \longrightarrow D + \pi^{+}) | p(0) |^2}{p_{\pi} (1 + bp_{\pi}^2 / \mu^2 c^2)}, \qquad (6)$$

where the term in the denominator proportional to p_{π}^2 represents the p state contribution (relative to that of the's state) to $\sigma(2p \longrightarrow D + \pi^+)$. Indeed, it is characteristic of pseudoscalar meson theory that it describes the mesonnucleon interaction as primarily taking place in the p state, the s state coupling arising only from "small" relativistic correction terms. The smallness of these terms is characterized by the mass ratio μ/M , which is not, in truth, a very small parameter. According to the theory, the constant b would be of order M/μ .

To obtain the rate of the $\pi^- + D \rightarrow 2n + \gamma$ reaction, we shall again appeal to the principle of detailed balancing, making use of the information available on the photoproduction process, $\gamma + n \rightarrow p + \pi^-$. This can be regarded as the inverse of the radiative capture in deuterium to the extent that the presence of the additional neutron does not affect the capture rate. We have calculated the effect to be expected because of the exclusion principle and the existence of n-n forces in the final state, and conclude that the capture rate in deuterium will be reduced by a factor, f, of approximately two-thirds.⁵ In analogy with (2), we now have

$$R(\pi^{-} + D \longrightarrow 2n + \Upsilon) = f \nabla_{\Pi}^{*} \sigma(\pi^{-} + p \longrightarrow n + \Upsilon) | \phi(0) |^{2}$$

where $\sigma(\pi^- + p \longrightarrow n + \gamma)$ is the cross section for this reaction for very slow mesons, of velocity $v_{\pi^\circ}^{\epsilon}$ From detailed balancing,

$$\sigma(\pi^{-} + p \longrightarrow n + \Upsilon) = 2\mu c^{2} \sigma(n + \Upsilon \longrightarrow p + \pi^{-}) / p_{\pi}^{\prime 2},$$

50

$$R(\pi^{-} + D \longrightarrow 2n + \gamma) = 2f\mu c^{2} \sigma(n + \gamma \longrightarrow p + \pi^{-}) \left| \phi(0) \right|^{2} / p_{\pi}^{\dagger} .$$
(7)

In this equation, $\sigma(n + \Upsilon \longrightarrow p + \pi^{\infty}) / p_{\Pi}^{*}$ is to be evaluated just above threshold.

The experiments of Steinberger and Bishop⁶ on photoproduction in hydrogen give an approximate value of the cross section $\sigma(\gamma + p \longrightarrow n + \pi^+) = 7 \times 10^{-29} \text{ cm}^2$ for a γ -ray of 180 Mev, corresponding to 23 Mev relative energy of meson and neutron in the center of mass system. According to an argument of Brueckner and Goldberger,⁷ the cross section for $\gamma + n \longrightarrow p + \pi^-$ would be expected to be -Ìl-

larger, for non-relativistic meson energies, in the ratio $1/(1 - \mu/M)^2 = 1.3$. The existence of a negative excess in the photoproduction from carbon has been demonstrated experimentally by McMillan, Peterson and White⁸ and Peterson.⁹ While there is some doubt as to how well the observations agree in detail with the predictions of Brueckner and Goldberger, there is no doubt that the negative to positive ratio is at least as large as indicated above. We shall accordingly take $\sigma(\Upsilon + n \rightarrow p + \pi^{-}) = 10^{-28} \text{ cm}^{2}$. Since the lowest energy for which experimental data is available is that just quoted for production of 23 Mev mesons, while (7) requires the cross section just above threshold, an assumption about the energy dependence of the photoproduction cross section is necessary. If the matrix element for the process is a constant (i.e., if the variation of the cross section is determined solely by the available phase space) over this energy range, $\sigma(n + \gamma \longrightarrow p + \pi^{-})$, p_{π}^{i} will be independent of energy, and the 23 Mev value may be used in (7). While this assumed energy dependence is the one to be expected on the basis of pseudoscalar meson theory, it should be emphasized that it is not based on any direct experimental information: our present knowledge of the excitation function for photoproduction of mesons is not sufficiently accurate to permit an unambiguous extrapolation to zero energy.

The ratio of (7) to (6) gives

$$\frac{R(\pi^{-} + D \rightarrow 2n + \Upsilon)}{R(\pi^{+} + D \rightarrow 2n)} = 3f \frac{\mu}{M} \frac{p_{\pi}!}{p_{\pi}} \frac{\sigma(n + \Upsilon \rightarrow p + \pi^{-})}{\sigma(2p \rightarrow D + \pi^{+})} \left(1 + b \frac{p_{\pi}^{2}}{\mu^{2}c^{2}}\right) \quad (8)$$

Inserting 3/7 for the ratio of the R's, f = 2/3, $\mu/M = 1/7$, $p_{\pi}'/p_{\pi} = 1$, 1/2 for the ratio of the σ 's, we find $(1 + bp_{\pi}^2/\mu^2c^2) = 3$. This evaluation, in view of the uncertainties in the measurements of the various quantities appearing in (8), can hardly be trusted to better than a factor two. However the result is quite compatible with the notions one has to the proper behavior of a pseudoscalar -12-

field; since $p_{\mu}/\mu c = 1/2$, a value of b of the order M/μ is indeed permissable. Quite aside from the uncertainties in the measured quantities, it should also be pointed out that the value here found is in the nature of an upper limit for the s state contribution, since if the photoproduction cross section decreases more rapidly with decreasing meson momentum than we have assumed, the s wave coupling will be correspondingly reduced. Cartwright, Richman, Whitehead and Wilcox² and Peterson¹⁰ have found that mesons from the $2p \rightarrow D + \pi^+$ reaction have a markedly non-uniform angular distribution in the center of mass system, which shows quite definitely the existence of coupling to other than s states.

The absolute value of the capture rate given by (7), found by inserting $| \phi(0) |^2 = 1/\pi a^3$ and the previously quoted value of the cross section, is $R(\pi^- + D \longrightarrow 2n + \gamma) = 2.7 \times 10^{14} \text{ sec}^{-1}$.

The capture of π^{-} mesons in elements heavier than deuterium leads characteristically to stars, rather than high energy γ -emission. Panofsky, Asmodt and Hadley¹¹ give as upper limits for the fraction of high energy γ -emissions 10 percent in helium and 0.5 percent in carbon. As we have previously remarked, the non-radiative capture in deuterium depends on the probability of finding a high relative momentum of the nucleons in the deuteron. In more tightly bound systems this probability will be considerably larger. Crude estimates, based on a semi-empirical momentum distribution for the nucleons in carbon given by Chew and Goldberger,¹² indicate that an increase in the non-radiative capture rate by a factor as large as 30 may be expected. On the other hand, the rate of emission of high energy γ -rays will be reduced in the more tightly bound systems relative to deuterium, because of the greater inhibiting effect of the exclusion principle in the final state. The experiments of Peterson and White¹³ -]3- (

and Mozley,¹⁴ on the photoproduction of mesons show that a proton bound in carbon has only one-third as large a photoproduction cross section, at 260 Mev photon energy, as a free proton. Calculations by Bruno¹⁵ indicate that a similar reduction by a factor three is to be expected in the radiative capture rate in carbon. The Y-ray emission rate may thus be expected to be reduced. relative to deuterium, by a factor two, The combination of these two effects leads to the expectation that the 30 percent of Y-emission found in deuterium will be reduced to something of the order of 0.5 percent in heavier elements. Finally, it may be mentioned that if it be supposed that the π^- -meson has spin one (despite the fact that the π^{o} certainly has not, since it decays to two Y-rays), an explanation of the observed ratio of the $\pi^- + D \longrightarrow 2n$ and π^{-} + D \rightarrow 2n + γ processes can be based solely on selection rules. A vector meson in the K shell would have odd parity, and J = 0, 1 or 2. It could thus decay to the ${}^{3}P$ states of the two neutron system. However, a pseudovector meson would give states of even parity; those with J = 0 and 2 could decay to the ${}^{1}S_{0}$ and ${}^{1}D_{2}$ two neutron states, but decay from the J = 1 state would be forbidden. If we suppose the states are occupied in proportion to their statistical weights, a ratio of radiative to non-radiative transitions of 1/2 is thus to be expected.

Information Division scb/10-25-50 -14-

References

1. B. Ferretti, Report on the International Conference on Low Temperatures and Fundamental Particles, Cambridge (1946) p. 75. Also S. Tamor, Phys. Rev. <u>78</u>, 221 (A) (1950).

2. Cartwright, Richman, Wilcox and Whitehead, private communication. Although the experimental energy resolution is not good enough to conclusively establish the high energy meson peak as due to $2p \rightarrow D + \pi^+$ rather than $2p \rightarrow p + n + \pi^+$, we shall clearly overestimate the rate of capture in deuterium if we ascribe the observed cross section to the former process.

- 3. H. Bradner, private communication.
- 4. For states with $\mathcal{L} > 1$, the matrix element will fall off even more rapidly as the momentum is reduced. Use of a linear momentum dependence, which is tantamount to assuming the entire production process takes place from p states, can therefore only overestimate the rate of meson capture.
- 5. The exact value of f depends upon the detailed structue of the transition matrix element for this process. The value of approximately two-thirds is obtained from pseudoscalar meson theory. In any case it is not expected to differ much from this value.
- 6. J. Steinberger and A. S. Bishop, Phys. Rev. 78, 494 (1950)
- 7. K. Brueckner and M. Goldberger, Phys. Rev. 76, 1725 (1949)
- 8. E. McMillan, J. Peterson, and R. S. White, Science 110, 579 (1949)
- 9. J. Peterson, Dissertation, University of California (1950)
- 10. V. Z. Peterson, private communication.
- 11. Panofsky, Aamodt and Hadley, private communication.
- 12. G. F. Chew and M. L. Goldberger, Phys. Rev. 77, 470 (1950)
- 13. J. M. Peterson and R. S. White, Phys. Rev. 78, 84 (A) (1950)
- 14. R. Mozley, Phys. Rev. (in press)
- 15. B. Bruno, private communication