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Cathodic Arcs: Fractal Voltage and Cohesive Energy Rule

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The noise of the burning voltage of cathodic arcs in vacuum was analyzed for a range of cathode materials (C, Mg, Ti, V, Ni, Cu, Zr, Nb, Ag, Hf, Ta, W, Pt, Bi, and Si). Cathodic arcs were generated in a coaxial plasma source, and the voltage noise was measured with a broadband (250 MHz) measuring system. Each measurement of 50,000 points was analyzed by Fast Fourier Transform, revealing a power spectrum $\sim 1/f^2$ for all metals over several orders of magnitude of frequency f (brown noise). The absence of any characteristic time down to possible cutoffs at high frequencies supports a fractal model of cathode spots. Our preliminary research indicate that materials of high cohesive energy have a cutoff of self-similarity at 50 MHz while no cutoff could be found up to 100 MHz for non-refractory metals. The amplitude of colored noise scaled approximately linearly with the cathode's cohesive energy, which is another manifestation of the Cohesive Energy Rule.

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The plasma of cathodic vacuum arcs is produced at non-stationary cathode spots¹. Much research, both theoretically²⁻⁷ and experimentally⁸⁻¹⁴, has been done for decades to understand the spot phenomena that produce non-equilibrium plasmas containing multiply ion charge states. The plasma is mesosonic¹⁵, i.e., subsonic for electrons and supersonic for ions, with respect to the local ion sound velocity. Difficulties in experimentation and modeling are associated with the spots' fast changes, small sizes, and extreme gradients of power density and particle densities. The formation of spot plasma is often described as a sequence of microexplosions, where cathode material transitions through various phases, from solid to liquid, non-ideal plasma and/or gas phases, finally turning into in a non-equilibrium, expanding, fully ion ionized plasma^{6,16}.

With improvement of experimental techniques, faster and smaller phenomena have been discovered. This becomes especially striking when the issue of current density is considered. As the apparent area of electron emission was found to be smaller than previously thought, the corresponding current density increased accordingly^{17,18}. There were arguments what constitutes an electron-emitting site. In one extreme, electron emission should occur from areas much larger than the molten crater due to intense ion bombardment of the crater vicinity. On the other hand, the most relevant electron emission area might be smaller than the later visible crater because crater formation could be the result of the action of several spot fragments or cells.

In order to make any useful statements on cathode processes and parameters of cathodic arc plasma, many researches decided to repeat measurements and average the measured data. For example, one can find data on average ion charge states^{10,19}, average burning voltages^{20,21}, average ion velocities¹⁵, or average ion velocity distribution functions²².

All parameters fluctuate with large amplitude; in some cases up to 100% of the average value, which can be associated with the explosive nature of cathode spot ignition and plasma production. While research focused on finding trends and models for *averaged* distributions and other data, only limited attention was paid to fluctuations or "noise," although the fluctuating signals can be expected to contain information on plasma formation processes. Fluctuations have been described in some publications^{1,12,23-26} but only few quantitative statements were made. Smeets and Schulpen¹², looked at the noise of emitted light and ion fluxes. They noted a $1/f$ decay of the ion flux noise up to a frequency $f \approx 15$ MHz, followed

by white noise at higher frequencies. Schülke and Siemroth²⁷ observed that patterns of emitted light have self-similar properties, evident by using different optical magnification.

Among all physical quantities of cathodic arcs, the cathode fall voltage is special because it is intimately related to cathode processes, with very little distortion or superposition by secondary parameters of the system, such as the lifetime of excited levels in emission spectroscopy²⁸. From experiments with variable electrode distance and movable probes it is known that most of the total arc voltage drops in the cathode fall; the remaining small drop depends on many conditions, such as anode size and geometry, presence of magnetic fields, etc. The arc voltage determines the energy input invested: while the arc current is determined by the impedance of the electric circuit, the arc voltage is self-adjusting to satisfy the energy need of the discharge, and in particular the cathode region where plasma is produced. This is the underlying idea of the empirically found Cohesive Energy Rule²⁹, which states that the vacuum arc burning voltage depends approximately linearly on the cohesive energy of the material, E_{CE} . It was quantified as²⁹

$$V = V_0 + a E_{CE}, \quad (1)$$

with $V_0 \approx 14.3 \text{ V}$ and $a = 1.69 \text{ V}/(\text{eV/atom})$. Two arguments were brought forward to justify this empirical rule. First, the self-adjusting burning voltage connects properties of the plasma feedstock material with the energy conservation law. Second, many physical parameters show periodicity as expressed in the Periodic Table of the Elements, and therefore periodicity of the cohesive energy acts as a proxy for periodicity exhibited by other quantities such as melting and boiling temperatures or ionization energies.

Looking at the *noise* of arcs, a straightforward approach is to measure the noise of the total arc voltage, thereby characterizing the noise of the cathode fall, and ultimately the cathode processes causing it.

The noise of arcs was experimentally investigated by recording the burning voltage of a coaxial cathodic arc plasma source, and analyzing the data by Fast Fourier Transform (FFT). In order to preserve the frequency characteristics of the voltage noise, the arc source must be designed like a broad-band line. The easiest was to opt for a coaxial design of about 50 Ohm impedance (Fig. 1). The center cathode was a rod of 6.25 mm diameter (1/4 inch), surrounded by a coaxial anode cylinder. On one end, the plasma source was essentially comprised of a high-current vacuum feedthrough. On the other end, a metal-coated

alumina ceramic piece served as a holder to accommodate different cathode materials and as a means to initiate pulsed arcs via the self-triggering or “triggerless” method³⁰.

The arc was fed by a large, 0.33 F capacitor bank and switched with a high-voltage, high-current transistor. The large capacity ensured that the arc current did not droop too much during the arc pulse. For most experiments, the arc had a current of 100 A for a duration of 2.5 ms. When desired, the arc duration could be adjusted by the transistor switch. The current amplitude could be changed by the capacitor’s charging voltage while keeping constant the current-limiting 2.0 Ω resistor. The maximum voltage of the capacitor bank was 350 V, which was supplemented a 600 V “kicker capacitor” for reliable arc initiation³⁰. The arc repetition rate was 1 p.p.s. All arc experiments were done in oil-free vacuum at a base pressure of about 10^{-4} Pa; no process gas was added.

The arc burning voltage was monitored directly at the vacuum feedthrough using a broadband 100:1 divider (Tektronix P5100, max. 250 MHz analog). The divider was connected to a digital storage scope (Tektronix TDS744, max. 500 MHz analog, 2 Gs/s). Voltage data were captured in sample mode (50,000 data points per arc) with various time resolutions and their associated sample rates. The data were then exported from the scope’s memory to a computer for further analysis.

FFT analysis results curves as shown in Fig. 2 for titanium. The most striking feature is the constant slope over several orders of magnitude, which is about $1/f$ in amplitude spectrum and $1/f^2$ in power spectrum. Occasionally, there are other features visible, like a little hump at the high-frequency end of some curves, but those features appear to be specific to a particular measurement or material. Another feature of FFT curves is the broad band of data, especially noticeable at the high-frequency end. To better evaluate FFT data from here on, 16 curves obtained for constant measuring conditions were averaged. It should be emphasized that this averaging is done *after* FFT, thus information on noise is not lost.

There are a number of interesting questions that need to be addressed to further learn about cathode processes. Among them are: What is the influence of arc current and cathode material on the noise of arcs? How does the noise relate the elementary cathode processes?

In a first step, the influence of the arc current was measured. In the current range from 50 A to 240 A it was found that the FFT curves did not change their character but shifted slightly: the higher the current the lower the noise amplitudes. The shifts are barely visible in log-log presentation.

The next step was to measure whether arcs on cathode materials other than titanium give the same of similar FFT curves. The arc plasma source was designed for exchangeable cathode materials. To limit the parameter space, the following experiments were done with a constant arc duration of 2.5 ms, constant arc current of 100 A, and constant time resolution of 100 ns/div (2 ns per data point, or 500 kS/s), with a total acquisition time of 100 μ s per measurement. A wide range of different cathode materials was selected, including C, Mg, Ti, V, Ni, Cu, Zr, Nb, Ag, Hf, Ta, W, Pt, Bi, and Si. Each of these elements gave FFT curves with approximately the same slope of $1/f$ (spectral amplitude vs. frequency) and $1/f^2$ (spectral power vs. frequency) in log-log presentation. However, each material has its own characteristic level of noise amplitude, resulting in a different position of the curve. Figure 3 shows curves of two extreme materials, Bi and W. For comparison, the FFT procedure was also applied to the voltage zero line (i.e., no arc burning). Interestingly, the zero-line gives about the same slope at relatively low frequency and white noise at higher frequencies, which will be further discussed below.

To quantify the material-dependent noise amplitude, a frequency of 40 MHz was arbitrarily picked and the amplitude difference between FFTs of zero line and arc noise was determined. The selection of this frequency is not critical as long as it is in the physically meaningful range. At too low frequencies, data are scarce, and at too high frequencies, the FFT curves approach the FFT of the zero line, i.e. there is no arc-caused noise signal anymore. The differences at 40 MHz were normalized with the respect to the largest difference observed, which was for tungsten. The result is plotted against the cohesive energy of the cathode material, as shown in Fig. 4.

These measurements deserve critical interpretation. First, it is remarkable that for all materials investigated, FFT curves have a constant slope (in log-log presentation) over several orders of magnitude. The well-known theory of colored noise^{31,32} is based on power laws

$$P(f) \sim 1/f^\alpha, \quad (2)$$

where P is the spectral power and α an exponent determining the “color” of the noise. The noise is *white* for $\alpha = 0$, i.e. independent of frequency; *pink* for $\alpha = 1$, typical for systems of self-organized criticality³³; *brown* for $\alpha = 2$, for systems exhibiting large-scale fractal stochastic (Brownian) motion³¹; and *black* for $\alpha > 2$, occurring in self-similar systems with positive feedback, like the stock market³².

In a recent work³⁴ it was proposed that arc cathode spots are stochastic fractal objects that lack scaling over a wide range of values in space *and* time. It is clear that physical cutoffs exist but the (rather elusive) characteristic *elementary* size and times have not been confirmed despite numerous sophisticated investigations^{13,35,36}. Since the early work by Kesaev⁹, the existence of spot cells or fragments was confirmed by high-resolution diagnostics^{13,37}, though the lower scaling cutoff would only be confirmed if higher resolution techniques did *not* find smaller structures and faster changes.

Our measurements (Fig. 3) indicate that there is no cutoff of self-similarity in the fractal voltage until one approaches the region of 50 MHz and faster (or inverse, 20 ns and shorter). There are deviations from the power law, Eq. (2), for materials of high cohesive energy (e.g. Ta, W). At this time it is not clear whether these deviations are true features of cathode processes, or, for example, plasma instabilities unrelated to cathode processes. Further research is needed to address this issue.

The slight reduction of noise with increasing current can readily be explained by the superposition of short-lived elementary processes: fragments, cells, or ectons in Mesyats' terminology¹⁶. Superposition would reduce the expected standard deviation of a measured stochastic signal as $\sigma \sim 1/\sqrt{n}$, where n is the number of active emission sites. The same argument was brought forward to explain a reduction in noise of collected ion current when the arc current was enhanced³⁸.

Interestingly, even the zero-line itself showed power-law (fractal) behavior, at least at low frequencies. This is not unexpected because the superposition of small elementary events causes larger fluctuations at lower frequency³⁹. At high frequencies, white noise is observed, which is associated with the small-amplitude cutoff given by the digitizing depth of the digital oscilloscope.

With these considerations one may return to the physical picture of arc cathode processes and conclude that they are comprised of fast, small-scale events of electron emission and plasma production, which are sufficiently fast that all observation at longer times lack characteristic scale, indicating self-similar, fractal behavior. The observed spectral power is proportional to $1/f^2$, which is *brown* noise. It is interesting to contemplate that the brown noise found by *time* series analysis is associated with two-dimensional *spatial* Brownian motion on the cathode surface. Brownian motion is known to be the scaling limit of Random Walk for vanishing step length, and therefore Brownian motion is often approximated by random walk models to make computation more efficient. Random walk of cathode spots was extensively

investigated^{40,41} and a fractal dimension of 2 (characteristic for Brownian motion) was experimentally found by analyzing arc traces⁴².

Thus, the present arc voltage noise measurements support a fractal model of cathode spots for all materials, with possible scaling cutoffs at 50 MHz or higher frequency. The preliminary data show that cathode materials of higher cohesive energy have a lower cutoff frequency than material with small cohesive energy, indicating that the emission current per fragment or emission site is higher for materials of high cohesive energy. Peaks observed for $f > 50$ MHz, could be a signature of fast elementary emission processes (ectons⁵), though that conclusion remains to be confirmed. Materials of low cohesive energy have shorter elementary times, hence self-similar scaling cutoff are not easily observed. The amplitude frequency spectrum of arc voltage was found to be an approximate linear function of the cathode's cohesive energy, which is a manifestation of the Cohesive Energy Rule.

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Figure Captions

Fig. 1 Schematic of the coaxial plasma source used for the voltage noise experiments.

Fig. 2 Example of FFT of voltage data for a 50 A titanium arc, captured with different time resolution at the oscilloscope (5 ns/div, 1 μ s/div, 100 μ s/div), where each division has 50 data points.

Fig. 3 FFT curves (average of 16 amplitude vs. frequency measurements) for two extreme materials, Bi and W. For comparison, the same FFT procedure was also applied to the voltage zero line (i.e., no arc burning). All arc and analysis conditions were identical, except the cathode material: 100 A, 500 kS/s, for 100 μ s per measurement.

Fig. 4. Amplitude difference between FFT curves of arc voltage and FFT of the voltage zero line, measured at 40 MHz and under conditions like in Figure 3, normalized with respect to the difference for tungsten and plotted versus the cohesive energy of the cathode material.

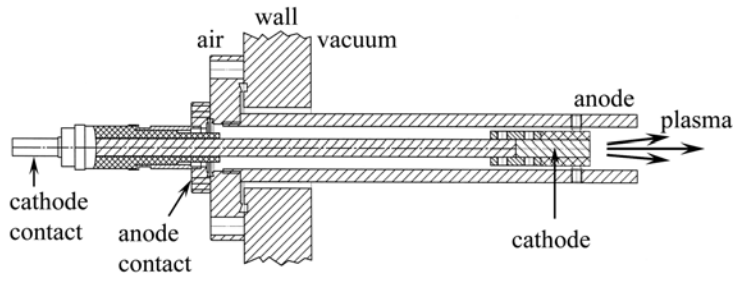


Fig. 1

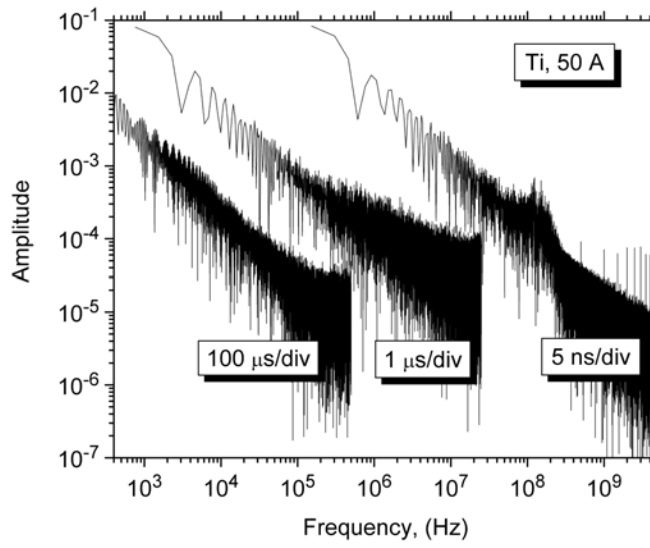


Fig. 2

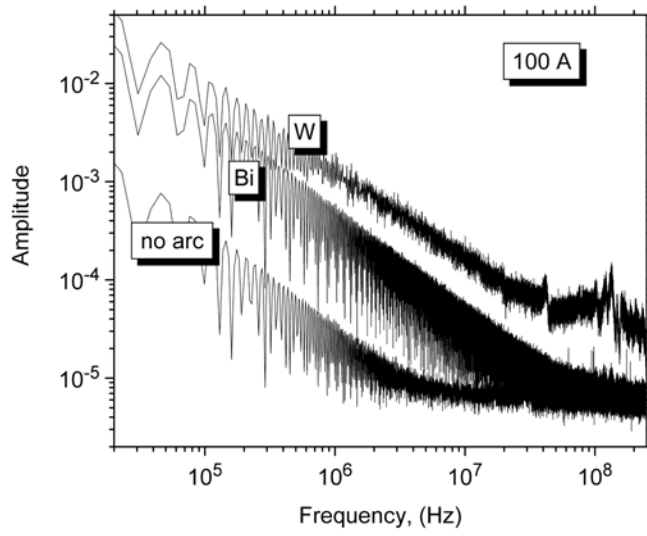


Fig.3

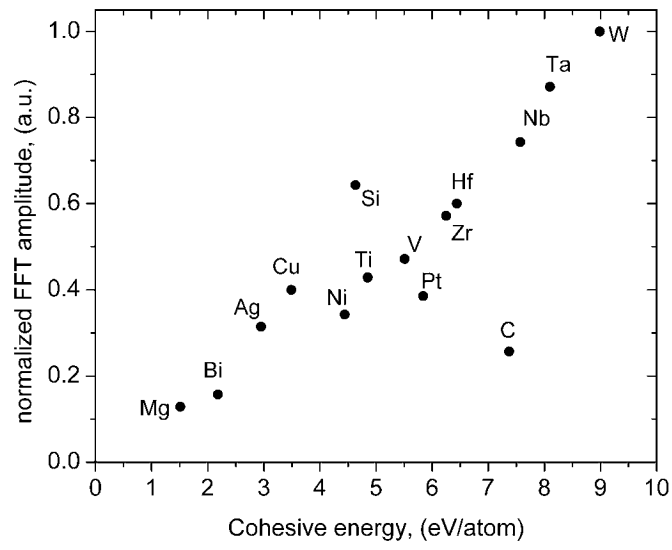


Fig. 4